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Phenotypic plasticity, the Baldwin effect, and the speeding up of evolution: The computational roots of an illusion

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HIGHLIGHTS

- Some current debates revolve around the role of genes as leaders or followers in the evolutionary process.
- The tenet that phenotypes are leaders and genes are followers is an old one and relates to the Baldwin effect.
- This effect was not part of evolutionary thinking during the Modern Synthesis in the 1930s and 1940s.
- People working in evolutionary computation revitalized the Baldwin effect by showing how and why it could work.
- A standard population genetics treatment can achieve what many people thought was unsolvable without the Baldwin effect.

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ABSTRACT

An increasing number of dissident voices claim that the standard neo-Darwinian view of genes as 'leaders' and phenotypes as 'followers' during the process of adaptive evolution should be turned on its head. This idea is older than the rediscovery of Mendel's laws of inheritance, with the turn-of-thetwentieth-century notion eventually labeled as the 'Baldwin effect' as one of the many ways in which the standard neo-Darwinian view can be turned around. A condition for this effect is that environmentally induced variation such as phenotypic plasticity or learning is crucial for the initial establishment of a trait. This gives the additional time for natural selection to act on genetic variation and the adaptive trait can be eventually encoded in the genotype. An influential paper published in the late 1980s claimed the Baldwin effect to happen in computer simulations, and avowed that it was crucial to solve a difficult adaptive task. This generated much excitement among scholars in various disciplines that regard neo-Darwinian accounts to explain the evolutionary emergence of high-order phenotypic traits such as consciousness or language almost hopeless. Here, we use analytical and computational approaches to show that a standard population genetics treatment can easily crack what the scientific community has granted as an unsolvable adaptive problem without learning. Evolutionary psychologists and linguists have invoked the (claimed) Baldwin effect to make wild assertions that should not be taken seriously. What the Baldwin effect needs are plausible case-histories.

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What role does the Baldwin effect play in evolution? By Baldwin effect -a term coined by Simpson (1953) – we refer to

a turn-of-the-twentieth-century idea (Baldwin, 1896; Morgan, 1896; Osborn, 1896) cogently described by Maynard Smith (1987, p. 761) as follows: "If individuals vary genetically in their capacity to learn, or to adapt developmentally, then those most able to adapt will leave most descendants, and the genes responsible will increase in frequency. In a fixed environment, when the best thing to learn remains constant, this can lead to the genetic determination of a character that, in earlier generations, had to be acquired afresh in each generation". The Baldwin effect

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involves two transitions (Turney et al., 1997; Godfrey-Smith, 2003): the first has to do with the evolutionary value of phenotypic plasticity, or some particular form of plasticity such as learning; the second with the 'genetic accommodation' [i.e., evolution in response to both genetically based and environmentally induced novel traits (Griffiths, 2003; West-Eberhard, 2003; Crispo, 2007)] of the learned trait. We use genetic accommodation instead of the more familiar term 'genetic assimilation' coined by Waddington (1953) because this last term should not be equated to the Baldwin effect (Crispo, 2007; see also West-Eberhard, 2003, pp. 153–154). Genetic assimilation can work with pre-existing genetic variation: the Baldwin effect (as originally posited) requires a new gene or genes.

14 Some towering figures in the Modern Synthesis – an expression 15 borrowed from the title of Julian Huxley's (1942) book - were either 16 indulgent with the theoretical plausibility of the Baldwin effect (Simpson, 1953) or utterly hostile towards it, recommending to discard 18 this concept altogether (Mayr, 1963; Dobzhansky, 1970). This advice is 19 followed by several influential textbooks in evolutionary biology 20 (Ridley, 2004; Futuyma, 2005; Barton et al., 2007) that do not even mention Baldwin at all. However, although at present there appears 22 to be no clear empirical evidence for the Baldwin effect, several 23 authors have called for a radical revision of the consensus view and 24 argued that much evolution involves genetic accommodation 25 (Schlichting and Pigliucci, 1998; Avital and Jablonka, 2001; West-26 Eberhard, 2003; Schlichting and Wund, 2014; but see Braendle and Flatt, 2006). The current tension among evolutionary biologists (Laland et al., 2014) is unmatched by scholars working in evolutionary 29<mark>0</mark> computation (Mitchell, 1996; Back et al., 1997; Turney, 1997) and in 30 others disciplines (typically evolutionary psychologists and cognitive 31 scientists; Weber and Depew, 2003), who invoke the Baldwin effect 32 as a major evolutionary force that could have led to the emergence of 33 mind (Dennett, 1995; Deacon, 1997; Pinker, 1997) and to modern 34 language (Pinker and Bloom, 1990; Briscoe, 1997; Calvin and Bickerton, 2000; Dor and Jablonka, 2001). As Yamauchi (2004, p. 3) 36 put it, "the Baldwin effect is particularly appealing because ... It may provide a natural Darwinian account for language evolution: It is an 38 especially popular idea among linguists that language evolution is 39 somehow saltational. This leads them to conclude that neo-Darwinian 40 theories are 'incompetent' for accounting for language evolution" (our addition in italics). (Neo-Darwinism is used here to describe the 42 Modern Synthesis version of Darwinism.)

43 Much of the recent 'excitement' about the Baldwin effect stems 44 from a seminal paper published by computer scientists Geoffrey Hinton and Steven Nowlan in the late 1980s (Hinton and Nowlan, 45 46 1987), which has been cited 1,101 times (Google Scholar) to date. They 47 developed a computational model combining a genetic algorithm 48 with learning by trial and error in a sexual population of chromo-49 somes (the 'organisms') that were initially segregating at L=20 loci 50 with three alleles each: 1,0, and ? This chromosome determines the 51 connectivity of a neural network: allele 1 at a given locus indicates 52 that a particular connection exists whereas allele 0 at that locus 53 indicates that it does not. The question marks are plastic alleles that 54 allow the organism to set (or not) the connection at the end of a 55 learning period. The neural network has only one correct configura-56 tion of connections and the task the organisms had to solve was to 57 find this configuration out of the $2^L \approx 10^6$ possible configurations. We 58 can assume without loss of generality that the right answer is the 59 chromosome with all alleles1; i.e., a fully connected neural network. 60 The catch is that any other configuration provides no information 61 whatsoever about where the correct answer might be. In such 62 problems, there is no better way to search than by exhaustively 63 sampling the entire combinatorial space; a situation termed a 64 'needle-in-the-haystack' problem. In other words, there is no efficient algorithm that can find the fitness maximum unless we introduce 65 some 'trick'; namely, to somehow smooth the spiked fitness 66

landscape through phenotypic plasticity (Frank, 2011). Hinton and 67 Nowlan (1987) assumed that each organism could try up to a 68 maximum of G=1000 random guesses for the settings of the ? 69 70 states; these alleles define the 'plastic genome'. The organisms were also given the ability to recognize whether they have found the 71 72 correct settings after g < G learning trials and, in such a case, stop 73 guessing (see below for details). Therefore, those organisms that were relatively fast at learning the correct configuration of alleles enjoyed a 74 fitness advantage and produced more offspring. In the long run 75 - well before 50 generations in the simulation performed by Hinton 76 and Nowlan (1987) – , natural selection redesigned the genotypes in 77 the population and the correct alleles 1 increased in frequency. 78 79 Nonetheless, they did not take over and undecided alleles ? remained segregating at relatively high frequency because in the end organisms 80 were able to learn quickly and, therefore, there was not much 81 selective pressure to fix the 'innately correct' fitter alleles. (Note, 82 therefore, that the model that worked was the one in which what 83 really mattered was how close an organism got to the correct 84 configuration). 85

The scenario in Hinton and Nowlan (1987) showed (i) that the 86 Baldwin effect can be observed in silico, and (ii) that once the wrong 87 88 0 alleles are being eliminated by selection learning can dramatically accelerate adaptive evolution in a flat fitness landscape with a single 89 isolated peak; what Ancel (2000) characterized as the 'Baldwin 90 expediting effect'. Maynard Smith (1987, p. 762) explained this effect 91 by making a simple contrast with a population where organisms do 92 not learn: "In a sexual population of 1000 with initial allele frequen-93 cies of 0.5, a fit individual would arise about once in 1000 generations 94 ... Mating would disrupt the optimum genotype, however, and its 95 offspring would have lost the adaptation. In effect, a sexual population 96 would never evolve the correct settings... (or does so excessively 97 slowly)". Actually, "the problem was never solved by an evolutionary 98 99 search without learning" (Hinton and Nowlan, 1987, p. 497). Conversely, Maynard Smith (1987) claimed that in the absence of learning 100 a large asexual population would include optimal individuals and the 101 correct settings would soon be established by selection. 102

The first claim about non-learning sexual organisms has been 103 taken for granted, whereas the second claim concerning asexual 104 organisms was analytically investigated by Fontanari and Meir (1990) 105 to answer the question: how soon is 'soon'? Using their recursion 106 equation (3.1) to analyze the evolution of correct alleles, the answer is 107 that it would take more than 3000 generations for the population to 108 evolve the correct settings with initial allele frequencies 0.5 and no 109 mutation. Therefore, the conclusion seems to be fairly clear: in the 110 single-peaked fitness landscape assumed by Hinton and Nowlan 111 (1987) learning has a drastic effect on evolution. 112

Here, we show that this conclusion is generally incorrect and 113 requires careful considerations. The heart of the problem was also 114 pointed out by Maynard Smith (1987) and relates to the strong 115 positive epistasis in Hinton and Nowlan's (1987) scenario. This 116 epistasis generates, in turn, strong positive associations between 117 the correct alleles in the non-learning organisms that can greatly 118 accelerate evolution (Appendix A). The former solution of more than 119 3000 generations for the asexual population to evolve the correct 120 121 settings is likely to be a gross overestimate as Fontanari and Meir 122 (1990) ignored the generation of linkage disequilibrium due to 123 directional selection. The remainder of the paper is organized as follows. First, we discuss Hinton and Nowlan (1987) model in more 124 detail as it will make the reason for our skepticism about what they 125 have really demonstrated very clear. Second, we derive the exact 126 recursion equations for the asexual case and show that evolution is 127 indeed quite fast in this case. Third, challenging the conventional 128 wisdom we show that a finite population of sexual organisms that 129 130 do not learn does evolve the correct settings, and estimate the 131 probability of fixation and mean time to fixation of the correct 132 genotype as a function of population size *N* and chromosome length

L. Finally, we summarize our results and point out the misconceptions generated by the computer simulations in Hinton and Nowlan (1987). The main conclusion is that their claim is untenable.

2. The simulation by Hinton and Nowlan

Hinton and Nowlan's (1987) basic idea was to show that a haploid sexual population of organisms with plasticity (learning ability) will evolve towards an optimal phenotype in fewer generations than a population of organisms that do not learn. They assumed that the L=20 loci code for neural connections and alleles 1 specify innately correct connections, alleles 0 innately incorrect connections, and alleles ? guessable (plastic) connections containing a switch that can be on (right) or off (wrong). Learning consists of giving each individual up to a maximum of G=1000 random combinations of switch settings (with equal probability for on and off) on every trial. Those individuals that have a 0 allele at any locus will never produce the right connectivity of the neural network. On the other hand, if the combination of switch settings and the genetically specified connections produce the good net (i.e., a fully connected neural network) after g < G trials the individual stops guessing.

Hinton and Nowlan's (1987) evolutionary algorithm performs two operations. First, each organism (i = 1, 2, ..., N) is evaluated according to fitness, which determines the mating probability and offspring production according to the following fitness function

$$w_i = 1 + \frac{(L-1)\eta_g}{G},\tag{1}$$

where $\eta_g = (G-g)$ is the number of trials remaining after the correct configuration of connections has been found. This fitness function is central to Hinton and Nowlan (1987) argument. It indirectly smoothes out the landscape and the organisms nearby the attraction zone of the peak (i.e., those chromosomes with ones and question marks that can be correctly set after g < G trials) enjoy increased fitness. The basal fitness is $w_i = 1$ if the organism never gets the right answer after G trials, and has a maximum value of $w_i = L$ for an organism that already has all its connections innately specified.

Second, the crossover operation picks one point $(1 \le m \le L-1)$ at random from each of parents' chromosomes to form one offspring chromosome by taking all alleles from the first parent up to the crossover point, and all alleles from the second parent beyond the crossover point. Although not explicitly stated in Hinton and Nowlan (1987), taking $m \le L-1$ as the upper bound guarantees that the offspring will always be a recombinant string. None of the learning is passed on to children, which inherit the same allelic configuration their parents had at the different loci. Hinton and Nowlan (1987) simulation is replicated in Fig. 1.

3. Evolution without learning in an asexual population: equations for the deterministic limit

We will consider the case where learning is absent in order to show that the neglect of linkage disequilibrium (Fontanari and Meir, 1990) greatly overestimates the number of generations required for the correct genotype to become preponderant in the population. In fact, in an infinite asexual population the prevalence of the correct genotype takes place so rapidly that the effect of learning (if any) is not significant.

61 In this case the genotypes are binary strings of size *L* because 62 without learning there is no difference between alleles 0 and ? 63 There are 2^{L} different such strings and we denote their frequencies 64 in the infinite population at generation *t* by $Y_{\alpha}(t)$, with $\alpha = 1$, 65 ..., 2^{L} . Without loss of generality, we will assume that the correct 66 genotype, i.e. the string (1, 1, ..., 1), corresponds to $\alpha = 1$. Recalling



Fig. 1. Replication of Hinton and Nowlan's original simulation. The population is able to quickly learn the solution as innately incorrect alleles 0 are eliminated from the population, although the frequency of plastic alleles ? remains relatively high.

that the fitness w_{α} of all genotypes but the correct one is set to the baseline value $w_{\alpha \neq 1} = 1$, and that the fitness of the correct genotype is set to $w_1 = L$, we obtain

$$Y_1(t) \approx 1 - \frac{1 - Y_1(0)}{[Y_1(0)]^{1/L}} \exp\left[-(L-1)t/L\right],$$
(2)

in the regime $t \gg 1$ for which $Y_1(t) \approx 1$ (see Appendix B). This expression allows us to estimate the number of generations needed for $Y_1(t)$ to attain some arbitrary value close to one in the modified Hinton and Nowlan (1987) scheme. Solving Eq. (2) for t yields

$$t \approx -\frac{1}{L-1} \ln \left\{ Y_1(0) \left[\frac{1 - Y_1(t)}{1 - Y_1(0)} \right]^L \right\},\tag{3}$$

from which we see that *t* increases with the logarithm of $Y_1(0)$ rather than with a negative power of $Y_1(0)$ as in the case where linkage disequilibrium is neglected (Fontanari and Meir, 1990).

At this stage, it is instructive for comparative purposes with previous work (Fontanari and Meir, 1990) to derive the corresponding equations for the evolution of an infinite asexual population ignoring the generation of linkage disequilibrium. This is important because the paper by Fontanari and Meir (1990) has routinely been cited as giving additional support for the benefits of learning, without realizing that their analytical treatment was inappropriate for an asexual population. Their derivation begins with the expression for the frequency of alleles 1 at generation t+1, which we denote by p(t+1), given that one knows the genotype frequencies at generation t; i.e.,

$$p(t+1) = \frac{1}{L} \frac{\sum_{\alpha} P_{\alpha} w_{\alpha} Y_{\alpha}(t)}{\sum_{\alpha} w_{\alpha} Y_{\alpha}(t)},$$
(4)

were P_{α} stands for the number of alleles 1 in string α . Ignoring linkage disequilibrium transforms this equation into an autonomous recursion equation for p(t) by assuming that $Y_{\alpha}(t) = [p(t)]^{P_{\alpha}}[1-p(t)]^{L-P_{\alpha}}$ for all α and t. This means that the abundance of a genotype depends only on the number of alleles 1 and not on the specific location of those alleles in the string. In addition, those abundances are completely determined by the global frequency of alleles 1 in the population according to the previous expression. It is as if all genotypes were disassembled and then reassembled again at random following a procedure akin to Wilson's (1980); that is, Fontanari and Meir (1990) wrongly assumed L-1 recombination points. In fact, the reason why ignoring linkage disequilibrium is an inappropriate and uncontrolled approximation in this context, as well as its connection to group selection, was already pointed out in Alves et al. (2000, section V). This neglect gives the following incorrect recursion equation (Eq. 3.1 ignoring mutation in Fontanari and Meir, 1990)

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$$p(t+1) = \frac{p(t) + (L-1)[p(t)]^{L}}{1 + (L-1)[p(t)]^{L}}.$$
(5)

For L = 20 and p(0) = 0.25 (i.e., $Y_1(0) = 1/2^{40}$), the numerical solution of Eq. (5) shows that it takes about $t = 5.2 \times 10^8$ generations to reach the regime where $1 - p(t) = 10^{-6}$. This was the reason why Fontanari and Meir (1990) concluded that learning has a drastic effect on evolution in Hinton and Nowlan's (1987) scenario. However, using the correct Eq. (3) we find that only t = 15 generations are sufficient to reach that regime.

In the same vein than Hinton and Nowlan (1987) we did not include mutation in the foregoing treatment, but it is easy to derive exact recursion equations for the non-learning asexual case assuming mutation (Appendix C). In summary, the preponderance of the correct genotype in an infinite asexual population without learning takes place extremely fast so the effect of learning, if any, is not significant in this case.

4. Evolution without learning in a sexual population

Having shown that Maynard Smith's (1987, p.762) remark that a non-learning asexual population of "many millions would breed true, and the correct settings would soon be established by selection" ('soon' is indeed very soon) is essentially correct, what of a sexual population? In this context, it is interesting to recall what Hinton and Nowlan (1987, p. 497) wrote (our emphasis in italics): "The same problem was never solved by an evolutionary search without learning. This was not a surprising result; the problem was selected to be extremely difficult for an evolutionary search, which relies on the exploitation of small co-adapted sets of alleles to provide a better than random search of the space... To preserve the co-adaptation from generation to generation it is necessary for each good genotype, on average, to give rise to at least one good descendant in the next generation. If the dispersal of complex co-adaptations due to mating causes each good genotype to have less than one expected good descendant in the next generation, the co-adaptation will not spread, even if it is discovered many times. In our example, the expected number of good immediate descendants of a good genotype is below 1 without learning and above 1 with learning." This conclusion was echoed by Maynard Smith (1987, p. 762): "In a sexual population of 1000 with initial allele frequencies of 0.5, a fit individual would arise about once in 1000 generations ... Mating would disrupt the optimum genotype, however, and its offspring would have lost the adaptation. In effect, a sexual population would never evolve the correct settings".

Here, we show that this conclusion is incorrect. Some hints why this is mistaken can be gained from Eq. (5), which basically assumes that all genotypes are disassembled and then reassembled again at random following a procedure akin to Wilson's (1980) trait group selection framework; namely, Eq. (5) assumes L-1 recombination points as already stated above. This wrong assumption notwithstanding, an eventual fixation of the correct string is attained (Fontanari and Meir, 1990).

A more straightforward demonstration that a non-learning sexual population can find the solution to the 'needle-in-the-haystack' problem is obtained by showing that the expected number of good immediate descendants of a good genotype is actually above 1, in stark contrast to Hinton and Nowlan's claim quoted before. In fact, assuming that the correct all 1 s string is present in the population at some generation we can easily calculate the distribution of the number of good offspring it generates by mating with a random string following the crossover operation in Hinton and Nowlan (1987). As indicated above, the

single offspring of each mating is generated by randomly choosing a crossover point and taking all alleles from the first parent up to the crossover point, and from the second parent beyond the crossover point. Let us take the all 1 s string as the first parent and pick another string at random from the 2^L possible strings as the second parent. The probability that the resulting offspring is an all 1 s string is simply

$$\rho = \frac{1}{L-1} \sum_{i=1}^{L-1} \frac{1}{2^i} = \frac{1}{L-1} \left(1 - \frac{1}{2^{L-1}} \right) \approx \frac{1}{L-1},\tag{6}$$

since all crossover points are equiprobable and the second parent must be all 1 s after the crossover point. Therefore, the mean number of good offspring produced in *L* matings (the fitness of the correct genotype is $w_1 = L$) is $L\rho = L/(L-1) > 1$ and so the "expected number of good immediate descendants of a good genotype" is not below one as claimed (Hinton and Nowlan, 1987; see also Maynard Smith, 1987) but, quite the opposite, the good genotype is expected to increase exponentially once it has appeared in the population. This is shown in Fig. 2 using the same parameter values (population size N=1000, chromosome length L=20) than Hinton and Nowlan (1987) with allele frequencies 0.5, where the correct genotype went to fixation in 14 out of 100 independent runs (14%) in less than 150 generations. Obviously, the former conclusion that a non-learning sexual population would never evolve the correct settings is just plain wrong.

As an application of Eq. (6), we can derive the mean number of good offspring in a two-generation dynamics of a population of size *N*. Assume the population at the first generation is composed of a single correct genotype (fitness *L*) plus N-1 random genotypes (fitness 1). Since two distinct parents are chosen in each mating, the probability that the good genotype is chosen is

$$\frac{L}{L+N-1} + \frac{N-1}{L+N-1} \times \frac{L}{L+N-2},$$
(7)

where the first term is the probability that the good genotype is the first chosen mate and the second term is the probability that it is the second mate. As a generation comprises N such mates and the probability of resulting a good offspring is ρ , we obtain that the



Fig. 2. Evolutionary search without learning in a sexual population. The simula-tions follow Hinton and Nowlan (1987) scheme with the exception that each organism is a binary string. Initial frequencies were 0.5, population size N = 1000and chromosome length L = 20. A total of 100 independent runs were followed for 150 generations, and fixation of the correct genotype was observed in 14 runs (14%). This fixation is conditional on the first appearance of the correct genotype in the population; once it appears, its frequency increases exponentially. With the parameters values used, the probability of occurrence of the correct genotype at the initial generation is equal to $1/2^{20} \times 1000 = 9.5367 \times 10^{-4}$. Therefore, when $N/2^L \ll 1$ the probability of fixation of the correct genotype is mostly dependent on the balance between the mean time to its first appearance by recombination and the mean time to fixation by genetic drift of the incorrect allele 0 at any single locus; an event that prevents the fixation of the correct genotype (mutation was ignored in these simulations).

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mean number of good offspring in the second generation is

$$\mu = \frac{NL}{(L+N-1)(L-1)} \left[1 + \frac{N-1}{L+N-2} \right].$$
(8)

Since we have assumed that good offspring are produced only by mates involving the good genotypes and not by the recombination of random strings, Eq. (8) yields a lower bound for μ but it fits the simulation data very well in the regime $N < < 2^{L}$ (data not shown). Most interestingly, for large populations N > > L we find that μ tends to 2 regardless the value of *L*, which explains the very fast growth of the good genotype once it appears in the population (Fig. 2).

Our findings open a number of questions. What is the prob-ability of fixation of the correct string as a function of N and the search space 2^{L} ? What is the expected number of generations for the correct genotype to reach fixation? What is the scaling factor between N and L for successful fixation? The reason why these questions are important is the following. As discussed by Belew (1990), Hinton and Nowlan (1987) picked the parameters in their simulations very carefully as they assumed a population size of N = 1000 organisms, and allele frequencies of 0.25 for zeros, 0.25 for ones, and 0.50 for question marks. With L=20, on average half of the alleles will be ? and there are $2^{10} = 1024$ combinations to try. Therefore, it is no surprise that given 1000 organisms and up to G = 1000 learning trials per organism the correct settings for the ? connections were easily found. If, for instance, we keep G constant and let the chromosome length L to increase from 20 to 30, the time taken for the population to solve the task in Hinton and Nowlan (1987) scenario increases exponentially (Fontanari and Meir, 1990): with G = 1000 and L = 30 it would take more than 10³ generations before an arbitrary large population of learning organisms can find the solution (results not shown). Therefore, both G and L need to be cautiously chosen (i.e., $G/2^{L/2} \approx 1$) to sustain the claim that learning speeds up evolution in a single-peaked fitness landscape. Nonetheless, to the extent that the scientific community accepted that the problem was unsolvable in any reasonable fashion without learning (e.g., Maynard Smith, 1987; Dennett, 1995, pp. 77-80; Pinker, 1997, p. 178; Puentedura, 2003; Sznajder et al., 2012), this could be considered as a relatively 'minor' detail in Hinton and Nowlan (1987) simulations. After all, they provided a proof of concept and the Baldwin effect seemed to be essential to solve their difficult adaptive task, which has generated a growing scientific literature ever since. However, the demonstration that a population of non-learning sexual organisms can also find the needle in the haystack converts what appeared to be a qualitative issue into a quantitative problem in its own right (Fig. 3). To put it bluntly, Hinton and Nowlan's (1987) original claim is untenable but is anyhow interesting to explore the regime under which learning will be of little help in their model.

4.1. Probability of fixation

We used computer simulations to estimate the probability of fixation of the correct genotype (denoted as P_1). The simulations followed Hinton and Nowlan (1987) scheme. In particular, the population consists of N binary strings of length L and update is parallel; i.e., generations do not overlap. To create the next generation from the current one, we perform N matings. The two parents of a mating are different individuals that are chosen at random from the current generation with probability proportional to fitness ($w_1 = L$ is the fitness of the correct genotype and $w_{\alpha \neq 1} = 1$ is the fitness of all genotypes but the correct one). The single offspring of each mating is generated after applying the one point crossover operation (see above). The initial population is generated randomly by choosing the *L* digits of each string as 0 or 1 with equal probability.

For different string lengths, the probability of fixation P_1 as a function of *N* is plotted in Fig. 4A, and as a function of the rescaled



Fig. 3. Evolutionary search with (A) and without (B) learning in a sexual population. (A) The simulation uses Hinton and Nowlan (1987) algorithm with allele frequencies of 0.25 for zeros, 0.25 for ones, and 0.50 for question marks; but different parameter values for population size (N = 2500), chromosome length (L = 16), and maximum number of learning trials per organism (G = 250). With L = 16 there are $2^8 = 256$ combinations to try as an average for the settings of ? alleles; that is, we kept the same relationship $G/2^{L/2} = 0.977$ than Hinton and Nowlan's original simulation. (B) The simulation follows Hinton and Nowlan (1987) scheme with the exception that each organism is a binary string. Initial frequencies were 0.5, population size N = 2500 and chromosome length L = 16. The point here is that in this scenario the claim that learning allows organisms to evolve much faster than their non-learning counterparts does not seem to be fully justified.

variable $\xi = N^{1.9}/2^L$ in Fig. 4B. The probability P₁ is estimated as the fraction of simulations in which we observed the fixation of the correct genotype. The number of simulations varied from 10^7 to 10⁴ so as to guarantee that a statistically significant number of correct fixations have occurred. The variable ξ reveals the way N must scale with L in order to maintain P_1 invariant, resulting thus in the collapse of the data of Fig. 4A into a single universal scaling function, which seems to be well approximated by the fitting function $f(\xi) = 1 - \exp(-0.353 \times \xi^{0.7})$ as shown in Fig. 4B. We note that for a *finite asexual* population the corresponding scaling is given by $\xi = N/2^L$ (data not shown). Thus, with L = 20 fixation $(P_1 \ge 0.99)$ of the correct genotype in the sexual case is almost guaranteed when $N \ge 10, 170$; that is, with a population size well below the size of the solution space $(N/2^L = 0.0097)$. The reason for this can be understood from the following heuristic argument. Assume for simplicity that once the all 1 s string appears in the population its eventual fixation will occur because its frequency will increase exponentially (see above). With $N < 2^{L}$, the correct genotype will be present at the initial population with probability $N/2^{L}$, which is quite low for N = 10, 170 and L = 20. It will likely arise through recombination with the same probability $N/2^{L}$ at each generation (we ignore the fact that allele frequencies will drift apart from their initial frequency of 0.5), which means that the probability of no occurrence of the correct genotype decreases with the number of generations as $(1-N/2^L)^{L}$. With a large enough population size genetic drift will not be very important and the correct genotype will eventually appear and spread to

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Fig. 4. Probability of fixation (*P*₁) of the correct genotype in a non-learning sexual population as a function of population size *N*. (A) plots from left to right chromosome lengths *L*=8 (red, times signs), 10 (green, squares), 12 (blue, diamonds), 15 (magenta, inverted triangles), 18 (cyan, triangles) and 20 (black, circles). Each symbol represents the fraction of the simulations in which we observed the fixation of the correct genotype and the lines are guides to the eyes. For *N* = 1000 and *L* = 20 we find *P*₁ = 0.172. (B) is the same but the probability of fixation is plotted against the rescaled variable $\xi = N^{1.9}/2^L$. The solid grey line is the fitting function $f(\xi) = 1 - \exp(-0.353 \times \xi^{0.7})$. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

fixation. Maynard Smith (1987) previous argument needs to be rewritten as follows: In a sexual population of 1,000 with initial allele frequencies of 0.5, a fit individual would arise about once in 1,000 generations. Once it appears, it will reach fixation in few generations (actually, the probability of fixation in this case is $P_1 = 0.172$; Fig. 4A). In a sense, low-fitness strings that exhibit concatenated sequences of the correct allele 1 can be thought of as cryptic sequences (Rajon and Masel, 2011, 2013) since it is the recombination process between them that produces the highfitness string.

4.2. Mean time to fixation

The previous computer simulations also allowed estimating the (conditional) mean time to fixation of the correct genotype (denoted as T_1). For different string lengths, T_1 is plotted as a function of the number of strings N in Fig. 5A, and as a function of the ratio between N and the size of the solution space $N/2^{L}$ in Fig. 5B. For L > 20 we find that the height of the T_1 peak increases as $2^{L/2}$ which, most interestingly, coincides with the form the number of learning trials G scales with the string length *L*. In particular, for L = 20 we find (mean \pm SD) $T_1 = 174 \pm 142$ generations with $N = 10^3$, and $T_1 = 28 \pm 14$ generations with $N = 10^5$. In other words, when $N/2^L \approx 0.1$ the mean time to fixation of the correct genotype is similar to Hinton and Nowlan (1987) situation with learning (Fig. 1). In general, for fixed L and very large N we have that T_1 grows with log N and is practically insensitive to L. This is in sharp contrast with what happens with learning because both *L* and *G* have to increase simultaneously $(G/2^{L/2} \approx 1)$, otherwise the time taken for the population to solve the task in Hinton and



Fig. 5. Conditional mean time to fixation (T_1) of the correct genotype in a nonlearning sexual population as a function of population size *N*. (A) plots from bottom to top chromosome lengths L = 8 (red, times signs), 10 (green, squares), 12 (blue, diamonds), 15 (magenta, inverted triangles), 18 (cyan, triangles) and 20 (black, circles). For L = 20 we find (mean \pm SD) $T_1 = 174 \pm 142$ generations with $N = 10^3$, and $T_1 = 28 \pm 14$ generations with $N = 10^5$. (B) is the same but the mean time to fixation is plotted against the ratio between the population size and the size of the solution space $(N/2^L)$. The lines are guides to the eyes. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Nowlan (1987) scenario increases exponentially (Fontanari and Meir, 1990) as pointed out above.

As expected, for any population size such that $N < < 2^{L}$ the evolutionary search takes exponentially long in the sequence length L to hit the high fitness peak. Chatterjee et al. (2014) have recently offered a mathematical proof for this result by considering a class of fitness landscapes in which peaks are surrounded by extended, flat valleys. Interestingly and perhaps not so differently from Hinton and Nowlan (1987) rationale, to solve the 'puzzle' of exponentially long evolutionary times, Chatterjee et al. (2014) proposed a new evolutionary mechanism – the regeneration process – which would allow evolution to work on polynomial time scales.

To sum up, in the single-peaked fitness landscape learning speeds up evolution whenever the ratio between the maximum number of allowed guesses per organism *G* and the size of the 'guessing space' $2^{L/2}$ is on the same order, i.e. $G/2^{L/2} \approx 1$, and the ratio between population size N and the size of the solution space 2^{L} in non-learning organisms is $N/2^L < 0.1$. That is, with G = 1000, L = 20 and 1000 organisms as in Hinton and Nowlan (1987) the $10^6 \approx 2^L$ queries to the fitness function per generation accomplish the same result than sampling $10^5 \approx 2^L/10$ genotypes per generation in the non-learning situation (one extra genotype is worth 10 queries). Decrease the ratio $G/2^{L/2}$ below 1 and keep the ratio $N/2^{L}$ around 0.1 and the result is that non-learning sexual organisms will start doing better than their learning equivalents.

4.3. Exploring other models of recombination

The successful fixation of the good genotype once it appears in the population is critically dependent on the expected number L_{ρ} 130 of good offspring after recombination, where ρ is the probability 131 that any single offspring is an all 1 s string. As we have previously 132

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shown, $L\rho > 1$ in the one point recombination scenario assumed by Hinton and Nowlan (1987). Our question now is to what extent this result is robust to a more general recombination model.

Here we follow the stochastic multilocus method of Fraser and Burnell (1970) and model recombination as a random walk along the length of the two parental chromosomes, changing from one to the other within the constraint of the probability of such a change; namely, the recombination rate among two adjacent loci. Under the assumption that the probability of recombination between any two loci is constant and equal to r, the probability that a mate between a L loci good genotype and a random genotype produces a good offspring is

$$\rho = (1 - r)\rho_1 + r\rho_2, \tag{9}$$

where ρ_1 is the probability that the offspring is the good genotype when the random walk starts from the all 1 s parent, and ρ_2 is the same probability when the random walk starts from the other random parent. Here

$$\rho_1 = (1-r)^{L-1} + \sum_{k=1}^{L-1} r^k (1-r)^{L-1-k} \sum_{i=0}^{L-M} \binom{O-1+i}{i} \binom{L-i-O-1}{L-M-i} 2^{i+O-L},$$
(10)

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$$\rho_2 = (1-r)^{L-1} 2^{-L} + \sum_{k=1}^{L-1} r^k (1-r)^{L-1-k} \sum_{i=0}^{L-M} {\binom{E-1+i}{i} \binom{L-i-E-1}{L-M-i}} 2^{i+E-L},$$
(11)

where M = k+1, *O* is the number of odd numbers in the sequence 1, 2, 3, ..., *M*, i.e., O = M/2 if *M* is even and O = (M+1)/2 if *M* is odd; and *E* is the number of even numbers in the same sequence, i.e., E = M/2 if *M* is even and E = (M-1)/2 if *M* is odd. As before, the mean number of good offspring genotypes is $L\rho$; the product between the fitness of the good parental genotype and ρ .

Eqs. (10) and (11) allow us to set an upper bound for *r* such that $L\rho > 1$ (Fig. 6). These results agree perfectly with simulation results (not shown). Thus, with L = 20 the upper bound is around r = 0.156, which is a large recombination rate between adjacent loci. For instance, a recombination frequency of only $r = 10^{-3}$ in our analysis would correspond to a chromosome with 1,000 loci and a map length of approximately 100 centimorgans; about the map length of each of the two major chromosomes of Drosophila melanogaster (Comeron et al., 2012), which together contain about 80% of the species' genome. Therefore, the conclusion that once the good string appears recombination would do little harm to its spread by selection seems to be robust. This conclusion was checked by performing 100 independent simulation runs as in Fig. 2 but now using the stochastic multilocus recombination method of Fraser and Burnell (1970) with r = 0.15. The correct genotype went to fixation in 12 runs (12%) in less than 150 generations (results not shown).



Fig. 6. Expected number of good offspring when an all 1 s parental chromosome mates with *L* random chromosomes. The curves plot L_{ρ} , where ρ is the probability that any single offspring is an all 1 s string given by Eq. (9) following the stochastic multilocus recombination method of Fraser and Burnell (1970).

5. Conclusions

As pointed out by Dennett (2003), many scholars including himself thought that Hinton and Nowlan (1987) and Maynard Smith (1987) had shown clearly and succinctly how and why the Baldwin effect worked, to the extent that in his bestseller book "Consciousness Explained" he (Dennett, 1991, p. 186) wrote that "thanks to the Baldwin effect, species can be said to pretest the efficacy of particular different designs by phenotypic (individual) exploration of the space of nearby possibilities". We grant this sort of claims as misleading for two reasons. First, it takes for granted the happening of an effect that still waits for convincing empirical support after more than 100 years since its original inception. Second, it disregards the countless times proved effectiveness of standard neo-Darwinian selection to evolve complex biological traits (Futuyma, 2005; Orr, 1999) and contribute to some of the major evolutionary transitions (Maynard Smith and Szathmáry, 1995; Michod, 1999).

Yeh and Price (2004) speculated that colonization and establishment of a new population of dark-eyed juncos in coastal California was facilitated by a plastic response in breeding season, and claimed that their results provide the first quantitative evidence of Baldwin's proposition that plasticity aids individuals to deal with novel situations. Baldwin (1896) certainly deserves the merit of "setting out a nascent theory of the evolution of phenotypic plasticity" (Scheiner, 2014, p. iii); however, it should be remembered that the Baldwin effect involves two transitions: the evolutionary value of phenotypic plasticity and the genetic accommodation of the induced trait. Because Yeh and Price (2004) did not prove that breeding season - a highly plastic trait (Dawson, 2008) – was genetically accommodated, we do not think their paper can be cited as a clear example of Baldwin effects (Crispo, 2007). Simpson's (1953) careful scrutiny made on the plausibility of Baldwin effects also applies here.

Our aim here was not to dismiss Hinton and Nowlan's (1987) seminal contribution persuasively demonstrating the feasibility of the Baldwin effect. Their short paper offers *pima facie* evidence of Haldane's conviction that "if you are faced by a difficulty or a controversy in science, an ounce of algebra is worth a ton of verbal argument" (Maynard Smith, 1965, p. 239), which is undoubtedly the reason behind the huge positive influence of their work. Hinton and Nowlan (1987) showed how the Baldwin effect could happen, but our present results show that there is no need for Baldwin effects to happen – at least in the proposed scenario.

Some previous criticisms and extensions of Hinton and Nowlan's 111 (1987) work focused on the problem of how plasticity and react-112 ion norms can smooth fitness landscapes, and have emphasized 113 that learning accelerates evolution only under certain conditions 114 (e.g., Ancel, 2000; Anderson, 1995; Behera and Nanjundiah, 1995). 115 Although the special assumptions in the Hinton and Nowlan (1987) 116 model are likely unrealistic and the needle-in-the-haystack problem 117 may hardly ever be relevant to evolution anyway, we do not think 118 this sort of criticisms are fatal to their conceptual work. It is again 119 120 interesting to recall what Hinton and Nowlan (1987, p. 501) wrote at the end of their paper: "We therefore conclude with a disjunction: 121 For biologists who believe that evolutionary search spaces contain 122 nice hills (even without the restructuring caused by adaptive 123 processes) the Baldwin effect is of little interest, but for biologists 124 who are suspicious of the assertion that the natural search spaces 125 are so nicely structured, the Baldwin effect is an important mechan-126 ism that allows adaptive processes within the organism to greatly 127 improve the space in which it evolves." This is a clever ending and 128 warns against attempts to disprove their model by simply assuming 129 different fitness landscapes. Granting that the fitness landscape is 130 flat with a single isolated peak as Hinton and Nowlan (1987) 131 132 assumed, the key question to answer is whether or not their basic

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claims are indeed correct. The answer is not, and this single fact invalidates their conclusion.

It is critical to clarify what we have and have not shown here. We have shown that finding a needle-in-the-haystack without learning is a trivial enterprise for a large population of asexual organisms, as well as for a sexual population depending on the scaling factor between population size and the search space. Therefore, Hinton and Nowlan's (1987) 'genes as followers' scenario (West-Eberhard, 2003) for the Baldwin effect could also be reframed into the traditional (Modern Synthesis) perspective that genes are 'leaders' and phenotypes are 'followers' during the process of adaptive evolution.

We have not shown that Baldwin effects are unlikely to happen in nature. Although we are not completely hostile but share Simpson's (1953) skepticism about the concept, to prove or disprove Baldwin effects is ultimately an empirical question. It should also be clarified that our doubts on the actual relevance of Baldwin effects should not be taken as a criticism to the role of behavior in evolution (Duckworth, 2009; Corning, 2014), as it is already obvious by contrasting Mayr's (1963) hostility towards Baldwin effects and his vindication of behavior as an important pacemaker or driver of evolutionary change (Mayr, 1960). Actually, one of us has conjectured that behavioral thermoregulation has been responsible for the fading of adaptive latitudinal clines (Castañeda et al., 2013); the so-called 'Bogert effect' (Huey et al., 2003). One thing is to assume that by choosing a specific temperature the organisms mitigate fluctuations in their thermal environment and little selection for temperature-related changes occur as we did, and quite another is to suppose that this behavior helps the survival of the organisms until hereditary variation favored by natural selection in the new environment can be accommodated (Baldwin effect).

To conclude, the demonstration that a standard neo-Darwinian account without learning can easily solve Hinton and Nowlan's (1987) harsh task should move "Baldwin boosters" (Weber and Depew, 2003) to their winter retreats. Interested colleagues, including ourselves, are invited to come up with a more convincing case for a fascinating and potentially important mechanism.

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Appendix A

Epistasis in a single-peaked fitness landscape

In the scenario without learning the neural connections are also specified by L loci but now with two alleles each, 1 and 0, because in this situation there is no difference between alleles 0 and ?. Since there is no smoothing out of the fitness landscape the fitness function is

$$w_i = \begin{cases} L & \text{if the organism has all correct alleles 1} \\ 1 & \text{otherwise} \end{cases}$$
(A.1)

With L = 2 the haplotype frequencies x_i and the corresponding fitness values are given by the following table

$$1 \quad x_1 = p_1 p_2 + D \quad x_3 = q_1 p_2 - D$$
Locus 2
$$w_1 = 2 \quad w_3 = 1 \quad p_2$$

$$0 \quad x_2 = p_1 q_2 - D \quad x_4 = q_1 q_2 + D$$

$$w_3 = 1 \quad w_4 = 1 \quad q_2$$
(A.2)

$$w_2 = 1$$
 $w_4 = 1$ q_2
 p_1 q_1 1

where $D(D = x_1 - p_1 p_2)$ is the linkage disequilibrium due to the non-random association of alleles within haplotypes. The multiplicative fitness epistasis is

$$E' = \ln\left(\frac{w_1 w_4}{w_2 w_3}\right) = 0.6931 \tag{A.3}$$

For the haploid case Felsenstein (1965) has shown that directional two-locus selection will tend to generate linkage disequilibrium of the same sign as the multiplicative epistatic parameter. This is illustrated here by iterating the standard recursion equations to calculate gametic frequencies after selection:

$$\begin{aligned} x_1' &= w_1(x_1 - rD)/\overline{w} \\ x_2' &= w_2(x_2 + rD)/\overline{w} \end{aligned} \tag{A.4}$$

$$x'_3 = w_3(x_3 + rD)/\overline{w} \tag{11.4}$$

 $x_4' = w_4(x_4 - rD)/\overline{w}$

where r is the amount of recombination between the two loci and

$$\overline{w} = \sum_{i=1}^{4} w_i x_i. \tag{A.5}$$

Assuming $D_0 = 0$ and $p_1 = p_2 = 0.1$, the linkage disequilibrium over time is plotted in Fig. A1 for two extreme recombination values (r = 0; r = 0.5). D can increase up to near its theoretical maximum 0.25.

Felsenstein (1965) also showed that if the linkage disequilibrium generated by epistatic selection is positive, tighter linkage accelerates the change in allelic frequencies. Therefore, the analytical recursion equations to analyze the evolution of allele frequencies in Hinton and Nowlan's (1987) model without learning (Fontanari and Meir, 1990) are expected to grossly overestimate the speed of evolution as they did not take into account the generation of linkage disequilibrium.



Fig. A1. Generation of gametic linkage disequilibrium without learning.

Appendix B

Exact recursion equations for the non-learning asexual case

We will consider the case where learning is absent in order to show the effect of neglecting the generation of linkage disequilibrium due to selection. In this case the genotypes are binary strings of size *L* because without learning there is no difference between alleles 0 and ? There are 2^{L} different such strings and we denote their frequencies in the infinite population at generation *t* by $Y_{\alpha}(t)$, with $\alpha = 1, ..., 2^{L}$. Without loss of generality, we will assume that the correct genotype, i.e. the string (1, 1, ..., 1), corresponds to $\alpha = 1$. Recalling that the fitness w_{α} of all genotypes but the correct one is set to the baseline value $w_{\alpha \neq 1} = 1$, and that the fitness of the correct genotype is set to $w_1 = L$, we can immediately write the recursion equations

$$Y_1(t+1) = \frac{w_1 Y_1(t)}{\sum_a w_a Y_a(t)} = \frac{L Y_1(t)}{1 + (L-1)Y_1(t)},$$
(B.1)

$$Y_{a \neq 1}(t+1) = \frac{w_{a \neq 1}Y_{a \neq 1}(t)}{\sum_{a} w_{a}Y_{a}(t)} = \frac{Y_{a \neq 1}(t)}{1 + (L-1)Y_{1}(t)}.$$
(B.2)

The denominator of the fractions in the right-hand-side of these equations is the average fitness of the population. It is also of interest to calculate the frequency of alleles 1 at generation *t*, which we denote by p(t). To simplify this calculation, let us assume that at generation t = 0 the frequencies of all genotypes different from the correct one take on the same value, say $Y_{a \neq 1}(0) = Y_2(0)$. Hence, Eq. (B.2) guarantees that these frequencies will always remain identical, i.e., $Y_{a \neq 1}(t) = Y_2(t)$ for all *t*. With this assumption, it is straightforward to write an equation for p(t)

$$p(t) = \frac{1}{L} \sum_{\alpha} P_{\alpha} Y_{\alpha}(t) = Y_{1}(t) + \left(2^{L-1} - 1\right) Y_{2}(t) = \frac{2^{L-1} [1 + Y_{1}(t)] - 1}{2^{L} - 1},$$
(B.3)

were P_{α} stands for the number of alleles 1 in string α and we have used the normalization condition $Y_1(t) + (2^L - 1)Y_2(t) = 1$. For large *L*, Eq. (B.3) reduces to $p(t) = [1 + Y_1(t)]/2$.

Thus, the study of the case of evolution without learning reduces to finding the solution of Eq. (B.1) that yields the frequency of the correct genotype $Y_1(t)$ as a function of the generation number *t*. For $t \gg 1$ we can rewrite the recursion Eq. (B.1) as the ordinary differential equation

$$\frac{dY_1}{dt} = (L-1)\frac{Y_1(1-Y_1)}{1+(L-1)Y_1},$$
(B.4)

the solution of which is simply

$$\frac{Y_1(t)}{\left[1 - Y_1(t)\right]^L} = \frac{Y_1(0)}{\left[1 - Y_1(0)\right]^L} \exp[(L - 1)t].$$
(B.5)

Since we are interested in the regime $t \gg 1$ for which $Y_1(t) \approx 1$, this equation can be further rewritten as

$$Y_1(t) \approx 1 - \frac{1 - Y_1(0)}{\left[Y_1(0)\right]^{1/L}} \exp\left[-(L - 1)t/L\right],\tag{B.6}$$

This expression is useful because it allows us to estimate the number of generations needed for $Y_1(t)$ to attain some arbitrary value close to one. In fact, solving Eq. (B.6) for *t* yields

$$t \approx -\frac{1}{L-1} \ln \left\{ Y_1(0) \left[\frac{1-Y_1(t)}{1-Y_1(0)} \right]^L \right\},\tag{B.7}$$

from which we see that *t* increases with the logarithm of $Y_1(0)$ rather than with a negative power of $Y_1(0)$ as in the case where linkage disequilibrium is neglected [37].

Appendix C

Exact recursion equations for the non-learning asexual case assuming mutation

We sketch the derivation here solely to emphasize the equivalence between the asexual case and the well-known single-peak fitness landscape of the quasispecies model (Eigen, 1971). The analysis simplifies greatly if one assumes that the relevant feature to distinguish the strings is the number of correct alleles they have without regard to their specific positions in the string. Provided that the initial condition is consistent with this assumption (i.e., all strings with the same number of alleles 1 have the same initial frequencies) the derived recursion equations are exact for the single peak landscape.

We begin by grouping all strings into L+1 classes, i = 0, 1, ..., L, according to the number of alleles 1 they have. The frequencies of those classes are simply $\Pi_i = \sum_{\alpha} Y_{\alpha} \delta_{iP_{\alpha}}$, where δ_{ij} is the Kronecker delta. Hence $\Pi_L = Y_1$ since $P_1 = L$ and there is only one string with L alleles 1. The idea is to derive a recursion equation for the class frequencies rather for the string frequencies, which amounts to reducing the number of equations from 2^L to L+1. The probability that a string with j 1 s mutates to a string with i 1 s is given by

$$M_{ij} = \sum_{k=a}^{b} {j \choose k} {L-j \choose i-k} (1-u)^{L-i-j+2k} u^{i+j-2k},$$
(C.1)

where μ is the per site probability of mutation. Here, $a = \max(0, i+j-L)$ and $b = \min(i, j)$. In particular,

$$M_{iL} = {\binom{L}{i}} (1-u)^{i} u^{L-i}.$$
 (C.2)

With this in mind we can write the recursion equation for the frequency of strings with i 1 s as

$$\Pi_{i} = \frac{1}{\overline{w}} \left[L M_{iL} \Pi_{L} + \sum_{j=0}^{L-1} M_{ij} \Pi_{j} \right],$$
(C.3)

where $\overline{w} = 1 + (L-1)\Pi_L$. Note that this is the equation for Eigen's (1971) model in the single-peak fitness landscape. In particular, the reproduction rate of the 'master sequence' (i.e., the all 1 s string) is *L*, which is identical to the sequence length. Hence, we expect the error threshold transition to take place at $u_c \approx 1 - 1/L^{1/L} \approx 0.139$ for L = 20. Simulation results (not shown) indicate that this figure is a good approximation.

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