Modeling the virtual machine allocation problem*

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Abstract

Finding the right allocation of virtual machines (VM) in cloud data centers is one of the key optimization problems in cloud computing. Accordingly, many algorithms have been proposed for the problem. However, lacking a single, generally accepted formulation of the VM allocation problem, there are many subtle differences in the problem formulations that these algorithms address; moreover, in several cases, the exact problem formulation is not even defined explicitly. Hence in this paper, we present a comprehensive generic model of the VM allocation problem. We also show how the often-investigated problem variants fit into this general model.

Keywords: Virtual machines, VM placement, VM consolidation, Cloud computing, Data centers

1 Introduction

Workload allocation in data centers (DCs) has been an important optimization problem for decades [7]. More recently, the wide spread of virtualization technologies and the cloud computing paradigm have established several new possibilities for resource provisioning and workload allocation [4], opening up new optimization opportunities.

Virtualization makes it possible to co-locate multiple applications on the same physical machine (PM) in logically isolated virtual machines (VMs). This way, a high utilization of the available physical resources can be achieved, thus amortizing the capital and operational expenditures associated with the purchase, operation, and maintenance of the DC resources. What is more, *live migration* of VMs makes it possible to move a VM from one PM to another one without noticeable service interruption [2]. This enables the dynamic re-optimization of the allocation of VMs to PMs, reacting to changes in the VMs' workload and the PMs' availability.

Consolidating multiple VMs on relatively few PMs helps not only to achieve good utilization of hardware resources, but also to save energy because unused PMs can be switched off or at least to a low-energy state such as sleep mode. However, too aggressive consolidation may lead to performance degradation. In particular, if the load of some VMs starts to grow, this may result in an overload of the accommodating PM's resources. In many cases, the expected performance levels are laid down in a service level agreement (SLA), defining also penalties if the provider fails to comply. Thus, the provider must find the right balance between the conflicting goals of utilization, energy efficiency, and performance [11].

Beside virtualization and live migration, the most important characteristic of the cloud computing paradigm is the availability of online services with practically unbounded capacity that can be provisioned elastically as needed. This includes Software-as-a-Service, Platform-as-a-Service, and Infrastructure-as-a-Service [21]. In the latter case, VMs are directly offered to customers; in the first two cases, VMs can be used to provision virtualized resources for the services in a flexible manner. Given the multitude of available public cloud offerings with different capabilities and pricing schemes, it is increasingly difficult for customers to make the best selection for their needs. The problem is further complicated by *hybrid cloud* setups that are increasingly popular in enterprises [5]. In this case, VMs can be either placed on PMs in the own DC(s) or using offerings from external providers, thus further enlarging the search space.

Since the allocation of VMs is an important and challenging optimization problem, several algorithms have been proposed for it. However, as shown in a recent survey, the existing literature includes a multitude of different problem formulations, making the existing approaches hardly comparable [13]. Even worse, some existing works failed to explicitly and precisely define the version of the problem that they are addressing, so that this must be figured out from the algorithm that they proposed or from the way the algorithm was evaluated.

We believe that addressing an algorithmic problem should start with *problem modeling*: a thorough consideration of the problem's characteristics and their importance or non-importance, leading to one or more precisely defined – preferably formalized – problem formulation(s) that capture the important characteristics of the problem. Then and only then should algorithms be proposed if the problem is already well-understood and well-defined.

*This paper was published in the *Proceedings of the International Conference on Mathematical Methods, Mathematical Models and Simulation in Science and Engineering (MMSSE 2015)*, pp. 102-106, 2015.

It seems that in the case of the VM allocation problem, this critically important phase was skipped, resulting in a rather chaotic situation where algorithms for "the VM allocation problem" actually address many different problems with sometimes subtle, sometimes serious differences.

The aim of this paper is to remedy this deficiency. Specifically, we devise a rather general formulation of the VM allocation problem that includes most of the problem formulations studied so far in the literature as special cases. We provide a taxonomy of important special cases and analyze their complexity. Section 2 contains the general problem model and Section 3 discusses special cases, followed by our conclusions in Section 4.

2 General problem model

We consider a *Cloud Provider (CP)* that provides VMs for its customers. For provisioning, the CP can use either its own PMs or external cloud providers (eCPs). The CP attempts to find the right balance between the conflicting goals of cost-efficiency, energy-efficiency, and performance. In the following, we describe the details of the problem.

2.1 Hosts

Let D denote the set of data centers available to the CP. For data center $d \in D$, let P_d denote the set of PMs available in d, also including any switched-off PMs. Furthermore, $P = \bigcup\{P_d : d \in D\}$ is the set of all PMs.

Each PM $p \in P$ is characterized by the following numbers:

- $cores(p) \in \mathbb{N}$: number of processor cores
- $cpu\_capacity(p) \in \mathbb{R}_+$: processing power per CPU core, e.g., in MIPS (million instructions per second)
- $capacity(p, r) \in \mathbb{R}_+$: capacity of resource type $r \in R$. For example, R can contain the resource types RAM and HDD, so that the capacity of these resources are given for each PM (e.g., in GB). This should be the net capacity available for VMs, not including the capacity reserved for the OS, the virtualization platform, and other system services

Our approach to model the CPU explicitly and all other resources of a PM through the generic $capacity$ function has several advantages. First, this gives maximum flexibility regarding the number of resource types that are taken into account. For instance, also caches, SSD drives, network interfaces, or GPUs can be considered, if relevant. On the other hand, the CPU is quite special, particularly because of multi-core technology. A multi-core processor is not equivalent to a single-core processor of capacity $cores(p) \cdot cpu\_capacity(p)$. It is also not appropriate to model each core as a separate resource, because VMs' processing power demand is not specific to each core of the PM, but rather to the set of its cores as a whole. The other reason why it makes sense to model the CPU separately is the impact that the CPU load has on energy consumption.

Each PM $p \in P$ has a set of possible states, denoted by $States(p)$. $States(p)$ always contains the state On, in which the PM is capable of running VMs. In addition, $States(p)$ may contain a finite number of low-power states (e.g., Off and $Sleep$). Each PM $p \in P$ and $state \in States(p)$ is associated with a static power consumption of $static\_power(p, state)$ per time unit. In addition, the On state also incurs a dynamic power consumption depending on the PM's load, as defined later. The possible state transitions are given in the form a directed graph $(States(p), Transitions(p))$, where a $transition \in Transitions(p)$ is an arc from one state to another. For each $transition \in Transitions(p)$, $delay(transition)$ and $energy(transition)$ denote the time it takes to move from the source to the target state and the energy consumption associated with the transition, respectively. (It should be noted that most existing works do not model PM states and transitions in such detail; an exception is the work of Guenter et al. [10].)

Let E denote the set of eCPs from which the CP can lease VMs. For each eCP $e \in E$, $Types(e)$ denotes the set of VM types that can be leased from e, and $Types = \bigcup\{Types(e) : e \in E\}$ is the set of VM types available from at least one eCP. Each VM type $type \in Types$ is characterized by the same set of parameters as PMs: $cores(type)$, $cpu\_capacity(type)$, and $capacity(type, r)$ for all $r \in R$. In addition, for an eCP $e \in E$ and a VM type $type \in Types(e)$, $fee(type, e)$ specifies the fee per time unit for leasing one instance of the given VM type from this eCP. It should be noted that the same VM type may be available from multiple eCPs, potentially for different fees.

Since VMs can be either hosted by a PM or mapped to a VM type of an eCP, let

$$Hosts = P \cup \{(e, type) : e \in E, type \in Types(e)\}$$

denote the set of all possible hosts.

2.2 VMs

What we defined so far is mostly constant: although sometimes new PMs are installed or existing PMs are taken out of service, eCPs sometimes introduce new VM types or change rental fees, such changes are rare, and can be seen as special events. On the other hand, the load of VMs changes incessantly, sometimes quite quickly. For the purpose of modeling such time-variant aspects, let $Time \subseteq \mathbb{R}$ denote the set of investigated time instances. We make no restriction on $Time$: it can be discrete or continuous, finite or infinite etc.

The set of VMs in time instance $t \in Time$ is denoted by $V(t)$. For each VM $v \in V(t)$, $cores(v)$ is the number of processor cores of v. The CPU load of v in time instance t is a $cores(v)$-dimensional vector: $vcpu\_load(v,t) \in \mathbb{R}_+^{cores(v)}$, specifying the computational load per core, e.g., in MIPS. The load of the other resources is given by $vload(v,r,t) \in \mathbb{R}_+$ for a VM $v \in V(t)$, resource type $r \in R$, and time instance $t \in Time$.

It should be noted that all the cores of a PM's CPU are expected to have the same capacity. In contrast, the cores of the CPU of a VM do not have to have the same load.

2.3 Mapping VMs to hosts

The CP's task is to maintain a mapping of the VMs to the available hosts. Formally, this is a function

$$Map : \{(v,t) : t \in Time, v \in V(t)\} \to Hosts.$$

$Map(v,t)$ defines the mapping of VM v in time instance t to either a PM or a VM type of an eCP. Furthermore, if $Map(v,t) = p \in P$, that is, the VM v is mapped to a PM p, then also the mapping of processor cores must be defined, since p may have more cores than v and each core of p may be shared by multiple VM cores, possibly belonging to multiple VMs. Hence in such a case, the function

$$Map\_core_v : \{1,\dots,cores(v)\} \times Time \to \{1,\dots,cores(p)\}$$

defines for each core of v the accommodating core of p, in a given time instance.

Given the mapping of VMs, the load of a PM can be calculated. For a PM $p \in P$ and time instance $t \in Time$, let

$$V(p,t) = \{v \in V(t) : Map(v,t) = p\}$$

be the set of VMs mapped to p in t. The CPU load of p in time instance t is a $cores(p)$-dimensional vector: $pcpu\_load(p,t) \in \mathbb{R}_+^{cores(p)}$, the ith coordinate of which is the sum of the load of the VM cores mapped to the ith core of p, that is:

$$pcpu\_load(p,t)_i = \sum_{\substack{v \in V(p,t),\\ Map\_core_v(j,t)=i}} vcpu\_load(v,t)_j.$$

Similarly, for a resource type $r \in R$, the load of PM p with respect to r in time t is

$$pload(p,r,t) = \sum_{v \in V(p,t)} vload(v,r,t).$$

The dynamic power consumption of a PM p is a monotonously increasing function of its CPU load. This function can be different for each PM. Hence, for a PM $p \in P$, let $dynamic\_power_p : \mathbb{R}_+^{cores(p)} \to \mathbb{R}_+$ define the dynamic power consumption of p per time unit as a function of the load of its cores. This function is monotonously increasing in all of its coordinates. If PM p is in the On state between time instances t_1 and t_2, then its dynamic energy consumption in this time interval is given by

$$\int_{t=t_1}^{t_2} dynamic\_power_p(pcpu\_load(p,t))dt. \tag{1}$$

2.4 Data transfer

For each pair of VMs, there may be communication between them. The intensity of the communication between VMs $v_1, v_2 \in V$ in time instance $t \in Time$ is denoted by $vcomm(v_1,v_2,t)$, given for example in MB/s. If there is no communication between the two VMs in t, then $vcomm(v_1,v_2,t) = 0$. The communication between a pair of hosts $h_1, h_2 \in H$ is the sum of the communication between the VMs that they accommodate, i.e.,

$$pcomm(h_1,h_2,t) = \sum_{\substack{v_1,v_2 \in V(t),\\ Map(v_1,t)=h_1,\\ Map(v_2,t)=h_2}} vcomm(v_1,v_2,t).$$

For each pair of hosts $h_1, h_2 \in Hosts$, the bandwidth available for the communication between them is $bandwidth(h_1, h_2)$, given for example in MB/s.

2.5 Live migration

The migration of a VM v from a host h_1 to another host h_2 takes time $mig\_time(v, h_1, h_2)$. During this period of time, both h_1 and h_2 are occupied by v. This phenomenon can be modeled by the introduction of an extra VM v'. Let t_{start} and t_{end} denote the time instances in which the migration starts and ends, respectively. Before t_{start}, only v exists, and is mapped to h_1. Between t_{start} and t_{end}, v continues to occupy h_1, but starting with t_{start}, also v' appears, mapped to h_2. In t_{end}, v is removed from h_1, and only v' remains. Furthermore, data transfer of intensity $mig\_comm(v)$ takes place between v and v' during the migration period, which is added to $pcomm(h_1, h_2, t)$.

2.6 SLA violations

Normally, the load of each resource must be within its capacity. A resource overload, on the other hand, may lead to an SLA violation. Specifically:

- If, for a PM $p \in P$ and one of its processor cores $1 \leq i \leq cores(p)$, $pcpu\_load(p,t)_i \geq cpu\_capacity(p)$, then this processor core is overloaded, resulting in SLA violation for all VMs using this core, i.e., for each VM $v \in V(p,t)$, for which there is a core of v, $1 \leq j \leq cores(v)$, such that $Map\_core_v(j,t) = i$.
- Similarly, if, for a PM $p \in P$ and resource type $r \in R$, $pload(p,r,t) \geq capacity(p,r)$, then this resource is overloaded, resulting in SLA violation for all VMs using this resource, i.e., for each VM $v \in V(p,t)$, for which $vload(v,r,t) > 0$.
- Assume that $Map(v,t) = (e, type)$, where $e \in E$. An SLA violation occurs relating to v, if either $vcpu\_load(v,t)_i \geq cpu\_capacity(type)$ for some $1 \leq i \leq cores(v)$ or if $vload(v,r,t) \geq capacity(type, r)$ for some $r \in R$.
- If, for a pair of hosts $h_1, h_2 \in Hosts$, $pcomm(h_1, h_2, t) \geq bandwidth(h_1, h_2)$, then the communication channel between the two hosts is overloaded, resulting in SLA violation for all VMs contributing to the communication between these hosts. That is, the set of affected VMs is $\bigcup\{\{v_1, v_2\} : Map(v_1,t) = h_1, Map(v_2,t) = h_2, vcomm(v_1, v_2, t) > 0\}$.

It should be noted that, in practice, loads will never exceed capacities. However, the loads in the above definitions are calculated as the sum of the loads of the relevant VMs; such a sum can exceed the capacity, and this indeed is a sign of an overload.

In any case, if there is an SLA violation relating to VM v, this leads to a penalty of

$$SLA\_fee(v, \Delta t), \tag{2}$$

where Δt is the duration of the SLA violation. The SLA violation fee may be linear in Δt, but it is also possible that longer persisting SLA violations are progressively penalized [9].

In principle, there can be two kinds of SLAs: hard SLAs must be fulfilled in any case, whereas soft SLAs can be violated, but this incurs a penalty. Our above definition allows both: hard SLAs can be modeled with an infinite SLA_fee, whereas soft SLAs are modeled with finite SLA_fee.

2.7 Optimization objectives

Based on the above definitions, the total power consumption of the CP for a time interval $[t_1, t_2]$ can be calculated as the sum of the following components:

- For each PM p, the interval $[t_1, t_2]$ can be divided into subintervals, in which p remained in the same state. For such a subinterval of length Δt, the static power consumption of p is $static\_power(p, state) \cdot \Delta t$. The sum of these values is the total static power consumption of p.
- For each PM p and each state transition of p, $energy(transition)$ is consumed.
- For each PM p and each subinterval of $[t_1, t_2]$ in which p is in state On, the dynamic power consumption is calculated as in Equation (1).

The total monetary cost can be calculated as the sum of the following components:

- The fees to be paid to eCPs. Assume that for $t \in [t_1, t_2]$, $Map(v, t) = (e, type)$, where $e \in E$. This incurs a cost of $(t_2 - t_1) \cdot fee(type, e)$. This must be summed for all VMs mapped to an eCP.
- SLA violation fees, calculated according to Equation 2, for all SLA violations.
- The cost of the consumed power, which is the total power consumption, as calculated above, times the unit power cost.

The objective is to minimize the total monetary costs, by means of optimal arrangement of the Map and Map_core functions and the PMs' states. As a special case, if the other costs are assumed to be 0, the objective is to minimize the overall power consumption of the CP.

It should be noted that there is no need to explicitly constrain or minimize the number of migrations. Rather, the impact of migrations is already contained in the objective function in the form of increased power consumption and potentially SLA violations because of increased system load. (With appropriate costs of migrations and SLA fees, it is possible to also model constraints on migrations, if necessary.)

3 Important special cases and subproblems

The above problem formulation is very general. Most authors investigated simpler problem formulations. We introduced some important special cases and subproblems in [13] and categorized the existing literature on the basis of these problem variants. In the following, we show how these problem variants can be obtained as special cases of our general model. It should be noted that the addressed problem variants are not necessarily mutually exclusive, so that combinations of them are also possible.

3.1 The Single-DC problem

The subproblem that has received the most attention is the Single-DC problem. In this case, $|D| = 1$ and $|E| = 0$, i.e., the CP has a single DC with a number of PMs, and its aim is to optimize the utilization of these PMs. $|P|$ is assumed to be high enough to serve all customer requests, so that no eCPs are needed. Since all PMs are co-located, $bandwidth$ is usually assumed to be uniform and sufficiently high so that the constraint that it represents can be ignored.

Some representative examples of papers dealing with this problem include [1, 2, 18, 20].

3.2 The Multi-DC problem

This can be seen as a generalization of the Single-DC problem, in which the CP possesses more than one DC. On the other hand, this is still a special case of our general problem formulation, in which $|D| > 1$ and $|E| = 0$. An important difference between the Single-DC and Multi-DC problems is that in the latter, communication between DCs is a non-negligible factor. Moreover, the DCs can have different characteristics regarding energy efficiency and carbon footprint. This problem variant, although important, has received relatively little attention [12, 15].

3.3 The Multi-IaaS problem

In this case, $P = \emptyset$, i.e., the CP does not own any PMs, it uses only leased VMs from multiple IaaS providers. Since there are no PMs, all concerns related to them – states and state transitions, sharing of resources among multiple VMs, load-dependent power consumption – are void. Power consumption plays no role, the only goal is to minimize the monetary costs. On the other hand, $|E| > 1$, so that the choice among the external cloud providers becomes a key question, based on offered VM characteristics and prices. In this case, it is common to also consider the data transfer among VMs.

The Multi-IaaS problem has quite rich literature. Especially popular is the case when communication among the VMs is given in form of a directed acyclic graph (DAG), the edges of which also represent dependencies. Representative examples include [8, 17, 19].

3.4 Hybrid cloud

This is actually the most general case, in which $|D| \geq 1$ and $|E| \geq 1$. Despite its importance, only few works address it [3, 6].

3.5 The One-dimensional consolidation problem

In this often-investigated special case, only the computational demands and computational capacities are considered, and no other resources. In our general model, this special case is obtained when the CPU is the only resource considered, and the CPU is taken to be single-core, making the problem truly one-dimensional. That is, $R = \emptyset$ and $cores \equiv 1$.

Whether a single dimension is investigated or also others (e.g., memory or disk), is independent from the number of DCs and eCPs. In other words, all of the above problem variants (Single-DC, Multi-DC, Multi-IaaS, Hybrid cloud) can have a special case of one-dimensional optimization.

3.6 The On/Off problem

In this case, each PM has only two states: $States(p) = \{On, Off\}$ for each $p \in P$. Furthermore, $static\_power(p, Off) = 0$, $static\_power(p, On)$ is the same positive constant for each $p \in P$, and $dynamic\_power_p \equiv 0$ for each $p \in P$. Between the states On and Off, the transition is possible in both directions, with $delay(transition)$ and $energy(transition)$ both assumed to be 0. As a consequence, the aim is simply to minimize the number PMs that are on. This is an often-investigated special case of the Single-DC problem.

3.7 Connections to bin-packing

The special case of the Single-DC problem, in which a single dimension is considered, power modeling is reduced to the On/Off problem, all PMs have the same capacity, there is no communication among VMs, migration costs are 0, and hard SLAs are used, is equivalent to the well-known bin-packing problem, since the only objective is to pack the VMs, as one-dimensional objects, into the minimal number of unit-capacity PMs. This has an important consequence: since bin-packing is known to be NP-hard in the strong sense [14], it follows that all variants of the VM allocation problem that contain this variant as special case are also NP-hard in the strong sense.

If multiple dimensions are taken into account, then we obtain a well-known multi-dimensional generalization of bin-packing, the vector packing problem [16].

4 Conclusions

In this paper, we attempted to lay a more solid foundation for research on the VM allocation problem. Specifically, we presented a detailed problem formalization that is general enough to capture all important aspects of the problem. We showed how some often-investigated problem variants can be obtained as special cases of our general model. Our work can also be seen as a taxonomy of problem variants, filling the problem modeling gap in the literature between the physical problem and the proposed algorithms. We hope that this will catalyze further high-quality research on VM allocation by showcasing the variety of problem aspects that need to be addressed as well as by defining a set of standardized models to build on. This will hopefully improve the comparability of the proposed algorithms, thus contributing to the maturation of the field.

Acknowledgments

This work was partially supported by the Hungarian Scientific Research Fund (Grant Nr. OTKA 108947).

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