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Evolution of magnetic field induced ordering in the layered quantum Heisenberg triangular-lattice antiferromagnet Ba₃CoSb₂O₉

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Quantum fluctuations in the effective spin- $\frac{1}{2}$ layered triangular-lattice quantum Heisenberg antiferromagnet $Ba_3CoSb_2O_9$ lift the classical degeneracy of the antiferromagnetic ground state in magnetic field, producing a series of novel spin structures for magnetic fields applied within the crystallographic *ab* plane, including a celebrated collinear "up-up-down" spin ordering with magnetization equal to 1/3 of the saturation magnetization over an extended field range. Theoretically unresolved, however, are the effects of interlayer antiferromagnetic coupling and transverse magnetic fields on the ground states of this system. Additional magnetic field induced phase transitions are theoretically expected and in some cases have been experimentally observed, but details regarding their number, location, and physical character appear inconsistent with the predictions of existing models. Conversely, an absence of experimental measurements as a function of magnetic-field orientation has left other key predictions of these models untested. To address these issues, we have used specific heat, neutron diffraction, thermal conductivity, and magnetic torque measurements to map out the phase diagram as a function of magnetic field intensity and orientation relative to the crystallographic ab plane. For H||ab, we have discovered an additional magnetic field induced phase transition at low temperature and an unexpected tetracritical point in the high-field phase diagram, which coupled with the apparent second-order nature of the phase transitions eliminates several theoretically proposed spin structures for the high-field phases. Our calorimetric measurements as a function of magnetic field orientation are in general agreement with theory for field-orientation angles close to plane parallel (H||a) but diverge at angles near plane perpendicular; a predicted convergence of two phase boundaries at finite angle and a corresponding change in the order of the field induced phase transition are not observed experimentally. Our results emphasize the role of interlayer coupling in selecting and stabilizing field induced phases, provide guidance on the nature of the magnetic order in each phase, and reveal the need for new physics to account for the nature of magnetic ordering in this archetypal two-dimensional spin- $\frac{1}{2}$ triangular-lattice quantum Heisenberg antiferromagnet.

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I. INTRODUCTION

The layered transition-metal oxide $Ba_3CoSb_2O_9$ is a nearly ideal realization of an isotropic two-dimensional (2D) spin- $\frac{1}{2}$

triangular-lattice quantum Heisenberg antiferromagnet. The 2D triangular arrangement of nearest-neighbor Co^{2+} ions with effective spin $\frac{1}{2}$ frustrates the otherwise expected classical magnetic ordering of the spins in an applied magnetic field, and its inversion symmetry means that there is no competing Dzyaloshinskii-Moriya interaction between nearest-neighbor Co^{2+} ions. As a result, the magnetic ordering in Ba₃CoSb₂O₉ arises from zero-point motion that lifts the degeneracy of the classical ground state [1]. Interlayer coupling leads to long-range order at a finite temperature at zero field [2] but also

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FIG. 1. Theoretically proposed spin orderings for the quantum S = 1/2 Heisenberg triangular antiferromagnet in the isotropic 2D limit. Structures in (a)–(d) are the coplanar Y, UUD, and V colinear spin orderings favored by quantum fluctuations, while (e) represents the competing classically favored noncoplanar 3D cone (umbrella) spin arrangement. The structure in (f) represents the alternative high-field coplanar spin ordering Ψ (also referred to as a fan structure). In zero field, theory predicts that the spins order in a 120° arrangement within the easy plane; phase transitions from the Y in (b) to the UUD in (c) to the V spin structure in (d) occur as the magnetic field is increased [1].

alters the nature of magnetic ordering in an applied field. For this reason, $Ba_3CoSb_2O_9$ serves as an experimental touchstone for quantum mechanical models of antiferromagnetic ordering in 2D materials with weak interlayer exchange [3,4].

Of particular interest in $Ba_3CoSb_2O_9$ are three questions: (1) how phase transitions between different magnetic spin structures are induced by an applied magnetic field, (2) what type of spin structure exists in each magnetic field induced phase, and (3) how the phases and spin structures vary with magnetic field orientation.

In the zero-temperature, isotropic 2D limit, S = 1/2 spins in a frustrated triangular lattice arrange at zero field in the threefold-degenerate 120° coplanar spin configuration shown in Fig. 1(a); in the case of the easy-plane antiferromagnet Ba₃CoSb₂O₉ studied here, the spins lie in the easy (*ab*) plane, normal to the *c* axis.

In an externally applied magnetic field, theory predicts this state will continuously evolve into the first of three quantum fluctuation stabilized phases: A coplanar phase in which the spins order in the shape of a Y, as shown in Fig. 1(b). The angle between the two spins forming the top branches of the Y depends on the strength of the applied magnetic field [1].

At an applied field equal to approximately 3/10 of the saturation magnetic field H_s , a phase transition to the collinear up-up-down (UUD) spin structure shown in Fig. 1(c) occurs, one signature of the UUD phase being a plateau in the magnetization at 1/3 of the saturation magnetization. In Ba₃CoSb₂O₉, this plateau is experimentally observed between 10 and 15 T for fields directed within the easy plane [5–7].

The third predicted phase is a different coplanar spin ordering denoted V: Two of the three spins share a common orientation, thereby forming a rotated V shape, as shown in Fig. 1(d). These three phases are followed by a final field induced transition at H_s to the fully polarized state.

Incorporating interlayer exchange and weak in-plane anisotropy is expected to result in additional ordered phases



FIG. 2. Theoretically proposed spin orderings for a quantum S = 1/2 Heisenberg triangular antiferromagnet with interlayer coupling in a two-layer model. Spins 1–3 correspond to layer 1; spins 4–6 correspond to layer 2. The orderings are named as follows: (a) the zero-field 120° structure, (b) distorted combined Y, (c) alternating ordered Y, (d) parallel ordered Y, (e) UUD, (f) V, (g) distorted V, (h) V', (i) staggered V', and (j) the ψ (fan) spin structure. The ordering in (k) corresponds to the classically expected cone (umbrella) phase.

at high field, as the spins can now alternate directions on adjacent layers, and the phase diagram becomes magnetic field orientation dependent [8–14]. A representative collection of the various spin orderings that have been proposed to occur when interlayer coupling is taken into account for magnetic fields aligned with the easy plane is shown in Fig. 2.

In this paper, we report results of specific heat, magnetic torque, thermal conductivity, and neutron scattering measurements on Ba₃CoSb₂O₉ as a function of magnetic field intensity and field orientation within the 2D plane (H||a), normal to the 2D plane (H||c), and as a function of angle ϕ for rotations from c ($\phi = 0^{\circ}$) to a ($\phi = 90^{\circ}$). We present evidence for additional phase transitions in both the lowand high-field limits below the saturation field H_s . We use thermodynamic and symmetry-based arguments to constrain the range of possible spin structures for the high-field phase, in some cases ruling out previously assumed configurations, and suggest physics beyond the standard J- J_z -J' weakly in-layer anisotropic coupled layer model that might account for our results.

II. EXPERIMENT

Single crystals of Ba₃CoSb₂O₉ were grown by using the optical floating-zone technique. Specific heat measurements $C_p(H, T, \phi)$ were carried out on 1.0- and 2.5-mg crystals as a function of temperature, magnetic field, and field orientation between 0.3 and 6 K in fields between 0 and 35 T using custom-built single-axis rotation microcalorimeters [15,16] cross calibrated in magnetic field to correct for magnetoresistance of the thermometers [17]. The thermal conductivity κ was measured by using a "one-heater, two-thermometer" technique [18,19]. The magnetic torque τ was measured by using a 13- μ m-thick CuBe cantilever. The single-crystal



FIG. 3. Magnetic field dependence of the specific heat as a function of temperature for H||a. Features corresponding to magnetic field induced phase transitions are observed at 6, 10, 15, 24, and 33 T in the low-temperature limit.

neutron diffraction measurements were made using a ³He insert at the Cold Neutron Triple-Axis Spectrometer CG4C at the High Flux Isotope Reactor, with the crystal aligned on the [HHL] scattering plane and in a vertically directed magnetic field.

A. Results and discussion for H||a|

We begin with a discussion of our results for the magnetic field applied within the easy (*ab*) plane, parallel to the *a* axis. For this orientation, we expect the spins to remain within the easy plane, starting from the 120° easy-plane spin configuration at zero field.

The magnetic field dependence of the specific heat at 0.3 K presented in Fig. 3 for H||a ($\phi = 90^{\circ}$ plane-parallel orientation) reveals a series of magnetic field induced phase transitions, starting with an unexpected additional transition at 6 T, transitions into and out of the UUD phase at 10 and 15 T, a sharp rise in the specific heat followed by a plateau corresponding to a transition around 24 T, and, finally, a sharp drop in the specific heat corresponding to a transition out of the antiferromagnetic state at a saturation field of 33 T. Additional features seen in the 0.3 K field sweep may correspond to emerging transitions but are not resolved at higher temperature.

The magnetic field induced phase transition from the lowfield orderings to the UUD spin ordering can also be seen in thermal conductivity measurements $\kappa(H)/\kappa(0)$ for H||a. Figure 4 shows the field dependence for temperatures above 1 K. At temperatures above $T_N(0) = 3.7$ K, an applied magnetic field induces a phase transition directly from the lower field paramagnetic state into the UUD spin state (at approximately 7 T for the 4.1 K trace); the initial field dependence



FIG. 4. Magnetic field dependence of the thermal conductivity for H||a at temperatures above and below the zero-field magnetic ordering temperature $T_N(0) = 3.7$ K, revealing field induced phase transitions from the zero-field paramagnetic $T > T_N(0)$ and antiferromagnetic $T < T_N(0)$ states to the UUD spin state.

below the zero-field ordering temperature $T_N(0)$ arises from change in spin orientation within the low-field antiferromagnetic state with applied field. The peak in the thermal conductivity at still higher magnetic field corresponds to the transition from this low-field state into the UUD spin state (at approximately 9 T for the 1.95 K trace), in good agreement with the specific heat results presented earlier.

Below 1 K, two peaks are seen as a function of magnetic field, as shown in Fig. 5. The first of these occurs between 6 and 10 T; the second of these begins at 10 T, the onset of the UUD phase, and continues up to the maximum measured field of 14 T. These results match what is seen in our specific



FIG. 5. Magnetic field dependence of the thermal conductivity for H||a| revealing the onset of a new magnetic phase between 6 and 10 T below 1 K.



FIG. 6. Intensities of magnetic Bragg scattering peaks (1/3, 1/3, 0), (1/3, 1/3, 1), and (1/3, 1/3, 2) at 8 T as a function of temperature for H||a.

heat measurements, further supporting our identification of a different low-field phase just below UUD at temperatures below 1 K.

Neutron scattering measurements provide additional information regarding the low-field spin orderings. Temperaturedependent measurements at 8 T shown in Fig. 6 reveal the onset of antiferromagnetic order in field at temperatures below 4.5 K followed by a pronounced decrease in interplanar scattering intensity at temperatures below 1 K. The L dependence of this decrease, much steeper for the (1/3, 1/3, 1) and (1/3, 1/3, 1)1/3, 2) magnetic Bragg scattering peaks than for the in-plane (1/3, 1/3, 0) scattering peak, suggests a change in the periodicity of the spin order along the c axis at 1 K.

In contrast, NMR measurements as a function of magnetic field see only a second-order transition from a low-field "distorted combined Y" phase [Fig. 2(b)] to the UUD phase [12] [Fig. 2(e)]. Those measurements, however, were done at 1.6 K, well above the 1 K transition temperature for this phase.

The possibility of a magnetic field induced phase transition between two Y phases with differing interplanar couplings below UUD was predicted in an early study [8], but the expected temperature dependence appears to be inconsistent with what is observed here experimentally. We leave the determination of the true microscopic spin ordering in this low-field phase to future experiments.

We now turn to the higher-field phase transitions and the construction of a phase diagram for H||a. Magnetic torque τ measurements between 0 and 35 T at 0.32 K for H oriented close to the *a* axis provide a complement to specific heat measurements over this same field range. As shown in Fig. 7, taking the first derivative of the magnetic torque to remove a background term in the measured response reveals features at fields corresponding to each of the phase transitions observed in the specific-heat measurement, including the transition observed at 6 T. We focus here, however, on the transition seen here at 24 T. Calculations assuming alternating-layer



FIG. 7. Magnetic field dependence of the magnetic torque τ at 0.32 K for a Ba₃CoSb₂O₉ sample for H||a| (after scaling for small changes in field orientation). A derivative of τ has been taken with respect to magnetic field to remove a background term in the magnetometer response. Phase transitions observed in the specific heat at 6, 10, 15, 24, and 32 T appear here as extrema and breaks in slope, confirming the magnetic nature of these transitions. The dashed line is a guide to the eye.

six-sublattice spin structures predict, and perhaps only allow, a first-order phase transition at this field [8,12,13]. The secondorder nature of the transition seen here in the specific heat and magnetic torque, while contrary to prediction, is nonetheless consistent with earlier evidence from magnetization [6]. NMR [12], and neutron diffraction measurements [14].

In particular, although sometimes taken in the literature to provide evidence of a first-order phase transition, magnetization measurements show a continuous M(H) curve with a peak at 24 T rather than a discontinuity in M(H) [6]. Further, changes in neutron scattering observed at this field [14] are consistent with either (1) a first-order transition from a distorted V spin structure [Fig. 2(g)] to a V' structure [13,14] [Fig. 2(h)] or staggered V [12] [Fig. 2(i)] or (2) a second-order transition to the Ψ (fan) spin structure [Fig. 2(j)]. Finally, NMR measurements reveal a change in spin ordering corresponding to a phase transition at this field but are unable to identify the order of the transition in this particular case [12]. The identification of the 24-T transition as a first-order phase transition has been on the basis of theory, not experiment.

A magnetic phase diagram for H||a constructed from the results presented above is shown in Fig. 8. In this diagram we also mark the location of a possible additional phase transition at 29 T but stress that this identification is tentative and at the limit of our resolution for H||a.

Several features emerge in this phase diagram, most notably the existence of a tetracritical point (at 17 T, 3.8 K) corresponding to the upper vertex of the phase directly above the UUD phase in field. In Landau mean-field theory [21-24], bicritical and tetracritical points can be found in a number of antiferromagnets in which the lattice anisotropy is not strong enough to produce complete spin alignment. Common examples include spin-flop transitions in which either (1)



FIG. 8. Phase diagram for H||a ($\phi = 90^{\circ}$). Solid black circles correspond to the locations of phase transitions observed in this work, blue diamonds refer to earlier, lower-field specific heat measurement by Zhou *et al.* [20], and red squares refer to NMR measurements by Koutroulakis *et al.* [12] Open black circles correspond to a possible additional high-field transition more clearly resolved for $\phi < 90^{\circ}$.

a single first-order transition line terminating in a bicritical point separates a lower-field antiferromagnetic phase and a spin-flop phase (as seen in MnF_2 [25]) or (2) a pair of second-order phase transitions terminating in a tetracritical point bounds an intermediate phase that separates a low-field antiferromagnetic phase and a high-field spin-flop phase (as seen in GdAlO₃ [26]).

A third example—particularly relevant here—is when the weakness of the interlayer coupling in a layered quasi-2D antiferromagnet with in-plane isotropy leads to a high-field tetracritical point in the magnetic phase diagram (as previously seen in $K_2Mn_{0.978}Fe_{0.022}F_4$ [27]). In layered triangular-lattice quantum Heisenberg antiferromagnets such as Ba₃CoSb₂O₉, this weak interlayer coupling can lead to a field-induced phase transition that doubles the period of the magnetic structure along the direction normal to the layer. This happens, for example, when the spins alternate directions in alternating layers [4,8]. If second order, the boundary between the bounded intermediate phase and the high-field phase and the UUD phase can terminate in a tetracritical point.

Magnetic phases terminating in a tetracritical point indicate breaking of the rotational symmetry of the ideal Heisenberg model, and a symmetry-based argument dictates that the magnetic ordering in the bounded intermediate phase is related to the ordering in the two adjacent phases [4,21]. In determining the nature of the high-field spin states, it will therefore be convenient to describe each state in terms of an *order parameter manifold* [4] representing the symmetries broken by that spin arrangement.

The three broken symmetries relevant here are (1) the discrete Z_3 symmetry (corresponding, for example, to the choice

of sublattice for the down spin in the UUD state), (2) the discrete Z_2 chiral symmetry associated with clockwise or counterclockwise rotation, as in the classical cone state, and (3) the continuous spin-rotation symmetry U(1) about the axis parallel to the magnetic field. Since commensurate coplanar states break both U(1) symmetry and Z_3 symmetry, the order parameter manifold for both the Y and V spin structures is $U(1) \times Z_3$; the corresponding order parameter manifold for the classical cone (umbrella) state is $U(1) \times Z_2$. In contrast, the commensurate collinear spin structure in the UUD phase breaks Z_3 symmetry but not U(1) symmetry, so the order parameter manifold for the UUD phase is Z_3 .

We can assign an order parameter manifold for the phase directly above the UUD phase from NMR [12] and neutron diffraction [14]. These measurements indicate that the spin structure in this phase is coplanar and commensurate, with order parameter $U(1) \times Z_3$; in particular, NMR results are consistent with the distorted V [12] spin structure shown in Fig. 2(g). As a result, the still higher field phase above 24 T can be neither a collinear phase, which is ruled out in the first place by the absence of a magnetization plateau in this field region, nor an incommensurate noncoplanar phase but must instead be either a commensurate coplanar phase [with order parameter $U(1) \times Z_3$] or an incommensurate coplanar phase [with order parameter $U(1) \times U(1)$].

Models incorporating interplane exchange and intraplane exchange anisotropy on high-field magnetic ordering [12,13] have focused on the first of these options for the high-field phase: A commensurate coplanar ordering with order parameter $U(1) \times Z_3$. In particular, for H||a, most calculations predict this spin ordering [12,13] just below the saturation field H_s (see, however, Ref. [8]).

The specific type of spin ordering is dependent on the interplane coupling J' and easy-plane anisotropy $\Delta = 1 - J_z/J$, where $\Delta = 0$ for an isotropic Heisenberg antiferromagnet and $\Delta = 1$ in the XY limit. For easy-plane anisotropies below a critical threshold Δ_{c1} the previously proposed V' spin structure is expected, whereas for stronger anisotropies, the coplanar Ψ spin structure occurs. In the absence of interplane exchange J', analysis of a triangular-lattice antiferromagnet with exchange anisotropy near saturation [10] predicts that $\Delta_{c1} = 0.45/S$, corresponding to a transition from V' to Ψ at $J_z = 0.1J$ for S = 1/2, but including even a small nonzero interplane exchange term J' enables this transition to occur for a much smaller degree of in-plane anisotropy Δ (larger J_z), with the V' spin structure favored at lower values of J' and the Ψ spin structure favored at higher values [13].

An early electron spin resonance (ESR)-based estimate of $J'/J \sim 0.03$ [6] has been a starting point for most theoretical calculations, but more recent neutron scattering experiments at zero field [28] and in the UUD state [29] consistently establish a higher value of J'/J = 0.052. Similarly, estimates of J_z/J also vary, ranging from 0.77 [11,13] to 0.93 [6]. Within existing theory, the numerical estimates used thus far for J' and J_z have led to the expectation that the high-field phase will correspond to the spin arrangement V' rather than Ψ [12,13]. There are, however, a number of unresolved discrepancies [12] between experiment and theory for this particular spin order, raising the question of whether this V' identification is accurate.

Following [14], we therefore now consider both the V' and Ψ arrangements to see if we can choose between the two thermodynamically. A key distinction between the V' and Ψ spin structures is as follows: In the V'-type spin arrangements, no spins align directly along the direction of the applied field, and the majority spins align at a different angle to the applied magnetic field than the minority spin, whereas in the symmetric Ψ arrangement, one spin aligns directly with the field, while the other two align at equal angles on either side of the first. The difference in symmetry between the distorted V, V', and Ψ structures means that the phase transition between the two adjacent phases should be first order when between distorted V and V' spin states but second order when between distorted V and Ψ [14]. On the basis of the evidence presented here, the spin structure for the phase above 24 T cannot be the previously theoretically proposed V' arrangement, but it could be of the Ψ type.

As an alternative to the Ψ structure, we must also consider an incommensurate planar phase with order parameter $U(1) \times U(1)$. This would not normally be expected in a crystal with sixfold symmetry, and the only prior experimental support for this possibility lies in the NMR data, which, although inconclusive, are said to bear some resemblance to what would result from incommensurate structures [12]. Theoretically, however, commensurate planar to incommensurate planar phase transitions satisfying $U(1) \times U(1)$ have been predicted only for intraplane spatial anisotropy [4,10], which is absent in Ba₃CoSb₂O₉. The experimentally more likely spin ordering for this high-field phase is therefore Ψ .

Distinguishing definitively between a highly symmetric, commensurate planar spin ordering like the Ψ structure, an incommensurate planar ordering based on one of the commensurate structures proposed for the *V* phase, and some third yet unconsidered spin structure likely requires new, even higher resolution NMR measurements than reported to date. The broadening of the ¹³⁵Ba and ¹³⁷Ba spectra with field makes such any measurements challenging, but recent advances in condensed-matter-NMR compatible high-homogeneity, high-field magnets may make this feasible [30].

B. Results and discussion for $H||a \rightarrow H||c$

We turn now to a discussion of the system's behavior as a function of magnetic field orientation for orientations from H||a to H||c ($\phi = 90^{\circ} \rightarrow \phi = 0^{\circ}$). Rotating the applied magnetic field out of the easy plane from H||a towards H||cintroduces a transverse field component that can be expected to distort the coplanar and collinear states that occur for H||aand alter the expected locations of the phase boundaries.

In the case of the distorted combined Y spin structure [Fig. 2(b)] experimentally confirmed by NMR for H||a ($\phi = 90^{\circ}$) below 10 T at 1.6 K [12], it is predicted that the spins will continuously deform with changing ϕ into the umbrella phase expected for H||c ($\phi = 0^{\circ}$). A similar deformation is expected for the UUD phase. At higher fields, however, the increasing distortion of the coplanar phases introduces the possibility of a magnetic field orientation induced phase transition instead of a continuous distortion of the H||a spin structure [12].

Our results for the angle dependence of the specific heat are shown at 0.4 K in Fig. 9 and at 1.0 K in Fig. 10. For angles



FIG. 9. Variation of the specific heat of Ba₃CoSb₂O₉ at 0.4 K with magnetic field strength and orientation for magnetic field orientations near H||a. The horizontal axes represent magnetic field strength and magnetic field orientation ϕ with respect to the *c* axis (normal to the easy plane). The horizontal plane serves as an (H, ϕ) phase diagram; the dashed lines on the phase diagram represent the predictions of T = 0 semiclassical mean-field theory [12]. The solid dots on the phase diagram represent locations of experimentally observed magnetic field induced phase transitions; dashed vertical lines leading from the dots mark the corresponding features in the data.

near H||a, the predicted locations in field for the phase boundaries (at T = 0) are in good agreement with our calorimetric measurements shown here, except, of course, for the transition seen at 6 T and an additional unexpected transition at 29 T.

In contrast, we find a significant deviation between theory and experiment at lower angles: Two-layer model calculations of interlayer coupling predict an experimentally unobserved field rotation induced phase transition due to the convergence of the lower and upper phase boundaries of an "upperintermediate-field" (UIF) phase, the phase observed between 15 and 24 T for H||a with decreasing ϕ . The transition should occur at fields and angles corresponding to the termination of phase boundary shown as a dashed green line at a dashed blue line in Fig. 10. As a result, the UIF phase should not exist at all below $\phi_c = 18^\circ$. Experimentally, however, we find that the upper and lower boundaries of the UIF phase fail to converge as a function of ϕ before $\phi = 0$. It would be interesting to theoretically investigate how ϕ_c varies with a change in the interplane coupling parameter J' and/or inclusion of next-nearest-neighbor exchange terms.

C. Results and discussion for H||c|

Our measurements at H||c are more limited in scope but still provide some additional insights regarding these various phase boundaries. The magnetic field dependence of the



FIG. 10. Variation of the specific heat of Ba₃CoSb₂O₉ with magnetic field strength and orientation for magnetic field orientations near $H||c|(\phi = 0)$ at T = 1 K. The horizontal axes represent magnetic field intensity and magnetic field orientation ϕ with respect to the *c* axis. The horizontal plane serves as an (H, ϕ) phase diagram; the dashed lines on the phase diagram represent the predictions of T = 0 semiclassical mean-field theory [12]. The solid dots on the phase diagram represent locations of experimentally observed magnetic field induced phase transitions; dashed vertical lines leading from the dots mark corresponding features in the data.

specific heat between 9 and 35 T for temperatures ranging from 0.4 to 3.7 K (shown in Fig. 11) reveal magnetic field induced phase transitions at low temperature at 12, 21, 29, and 33 T, the last of these being the transition at the saturation field H_s . NMR measurements at 1.89 K were the first to reveal the existence of the 21-T transition predicted by theory; the same set of NMR measurements was also the first to raise the possibility of an additional transition somewhere between 27.5 and 29 T for this field orientation [12].

As before, the magnetic torque measurement for H||c at 0.32 K shown in Fig. 12 confirms the magnetic character of these transitions. Transitions are observed at 12, 21, and 33 T. The additional transition at 29 T seen in NMR [12] and also in the specific heat is too weak to resolve above the noise floor here in magnetization.

We present in Fig. 13 a phase diagram constructed from these measurements. Additional measurements of thermal conductivity up to 14 T (not shown here) are consistent with this phase diagram. We also include two previously reported features in NMR measurements at 1.89 K between 14.5 and 30 T [12]. The NMR measurements are in good agreement with the specific heat and magnetic torque results presented here, although the 29-T transition was identified as tentative [12]. For H||c, the lowest-field phase below 12 T was identified as the classically expected umbrella (or cone) spin structure; measurements at the same temperature in the intermediate-field phase between 12 and approximately 21 T



FIG. 11. Magnetic field dependence of C_p/T for H||c from 9 T, just below the UUD phase transition at 12 T, up to the saturation field $H_s = 33$ T. Features corresponding to magnetic field induced phase transitions are observed at 12, 20, 29, and 33 T at 0.41 K. Lower-field data were not collected for this field orientation.

are consistent with the coplanar distorted V state [12] shown in Fig. 2(g). Measurements in the high-field phase between 21 and approximately 29 T, however, are inconsistent with the theoretically predicted staggered V [Fig. 2(i)] spin structure [12]. The nature of the spin state above 29 T in this orientation has also not been established. A transition just below H_s to a high-field cone phase was predicted in an early work [8] but has not been reproduced in more recent theoretical calculations [10,12,13].



FIG. 12. Magnetic field dependence of the torque τ at 0.32 K for H||c. Phase transitions observed in the specific heat for this field orientation at 12, 21, and 33 T manifest here as extrema and breaks in slope, confirming the magnetic nature of these transitions.



FIG. 13. Phase diagram for $H||c \ (\phi = 0^{\circ})$. Black circles correspond to the locations of phase transitions observed in this work, and the solid (open) red square represents transitions definitively (tentatively) identified by NMR measurements [12] at 1.89 K between 14.5 and 30 T.

III. GENERAL DISCUSSION

Our results indicate that the present S = 1/2, twolayer J- J_z -J' understanding of the triangular-lattice quantum Heisenberg antiferromagnetic model captures many aspects of the behavior of Ba₃CoSb₂O₉ but must now be modified or expanded in some way to account for the second-order nature of the phase transitions observed here, the unexpected emergence of additional phase transitions at low temperature, and the evolution of the phase diagram with field orientation. We suggest three possibilities: Relaxing the assumption of an effective S = 1/2 spin system for the Co²⁺ ions, incorporating next-nearest exchange terms, and other more general modifications of the alternating layer six-sublattice structure used in calculations so far.

First, the magnetic properties of the Co^{2+} ions in Ba₃CoSb₂O₉ are associated with a well-separated Kramers doublet ground state [5], leading to the approximation of Ba₃CoSb₂O₉ as an effective S = 1/2 spin system. Including higher-order spin-orbital exchanges, however, alters the expected magnetic ordering [31] in a related Co²⁺ easy-plane honeycomb quantum magnet with significant interplane coupling: CoTiO₃. Could including higher-order spin-orbital exchanges alter the expected magnetic ordering in Ba₃CoSb₂O₉ as well?

Second, including a next-nearest intraplane exchange term J_2 as small as $J_2/J \simeq 0.07$ is known to destroy the 120° zero-field magnetic ordering otherwise expected for the S = 1/2

triangular-lattice antiferromagnet [32]. It would be interesting to investigate what happens for a still smaller nonzero J_2 term which preserves the zero-field ordering [28] if a magnetic field is applied.

Third, present calculations assume an alternating layer, sixsublattice spin structure for the multilayer triangular-lattice quantum Heisenberg antiferromagnet model. Modifying this could allow periodicities in the spin structures other than simple aligned/antialigned order, including the possibility of incommensurate order [33]. Since multiple periodicities can have the same exchange energy [34], the periodicity could then be selected by some other interaction weaker than nearest-neighbor exchange coupling, such as next-nearest exchange or dipole-dipole interactions. These have been seen to lead to differences in the expected magnetic field induced phase transitions [34], an example being the S = 5/2triangular-lattice compound RbFe(MoO₄)₂. In this material, as with Ba₃CoSb₂O₉, two phases appear below the UUD phase for H||a, but only one—the umbrella phase—appears for H || c [34-36].

Further experimental work is also needed: The prepandemic experiments presented above necessarily focused on mapping out the angle dependence of the previously theoretically expected phase boundaries in the limited magnet time available, leading us to constrain the range of most field sweeps for $\phi \neq 0^{\circ}$ to fields above 9 T. Postpandemic, we hope to carry out systematic investigations of the 29-T feature seen near the saturation field for some field angles as well as the low-field umbrella phase that exists for H||c below 12 T [12], including the interesting question of whether the low-field 6-T transition seen for H||a persists as $H \rightarrow c$.

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