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“TNOs are Cool”: A survey of the trans-Neptunian region

X. Analysis of classical Kuiper belt objects from *Herschel*^{*} and *Spitzer* observations

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ABSTRACT

Context. The Kuiper belt is formed of planetesimals which failed to grow to planets and its dynamical structure has been affected by Neptune. The classical Kuiper belt contains objects both from a low-inclination, presumably primordial, distribution and from a high-inclination dynamically excited population.

Aims. Based on a sample of classical trans-Neptunian objects (TNOs) with observations at thermal wavelengths we determine radiometric sizes, geometric albedos and thermal beaming factors for each object as well as study sample properties of dynamically hot and cold classicals.

Methods. Observations near the thermal peak of TNOs using infrared space telescopes are combined with optical magnitudes using the radiometric technique with near-Earth asteroid thermal model (NEATM). We have determined three-band flux densities from *Herschel*/PACS observations at 70.0, 100.0 and 160.0 μm and *Spitzer*/MIPS at 23.68 and 71.42 μm when available. We use reexamined absolute visual magnitudes from the literature and ground based programs in support of *Herschel* observations.

Results. We have analysed 18 classical TNOs with previously unpublished data and re-analysed previously published targets with updated data reduction to determine their sizes and geometric albedos as well as beaming factors when data quality allows. We have combined these samples with classical TNOs with radiometric results in the literature for the analysis of sample properties of a total of 44 objects. We find a median geometric albedo for cold classical TNOs of $0.14^{+0.09}_{-0.07}$ and for dynamically hot classical TNOs, excluding the Haumea family and dwarf planets, $0.085^{+0.084}_{-0.045}$. We have determined the bulk densities of Borasisi-Pabu ($2.1^{+2.6}_{-1.2} \text{ g cm}^{-3}$), Varda-Ilmarë ($1.25^{+0.40}_{-0.43} \text{ g cm}^{-3}$) and 2001 QC₂₉₈ ($1.14^{+0.34}_{-0.30} \text{ g cm}^{-3}$) as well as updated previous density estimates of four targets. We have determined the slope parameter of the debiased cumulative size distribution of dynamically hot classical TNOs as $q = 2.3 \pm 0.1$ in the diameter range $100 < D < 500 \text{ km}$. For dynamically cold classical TNOs we determine $q = 5.1 \pm 1.1$ in the diameter range $160 < D < 280 \text{ km}$ as the cold classical TNOs have a smaller maximum size.

Key words. Kuiper belt: general – methods: observational – techniques: photometric – infrared: planetary systems

1. Introduction

Trans-Neptunian objects (TNOs) are believed, based on theoretical modeling, to represent the leftovers from the formation process of the solar system. Different classes of objects may

* *Herschel* is an ESA space observatory with science instruments provided by European-led Principal Investigator consortia and with important participation from NASA.

probe different regions of the protoplanetary disk and provide clues of different ways of accretion in those regions (Morbidelli et al. 2008). Basic physical properties of TNOs, such as size and albedo, have been challenging to measure. Only a few brightest TNOs have size estimates using direct optical imaging (e.g. Quaoar with *Hubble*; Brown & Trujillo 2004). Stellar occultations by TNOs provide a possibility to obtain an accurate size estimate, but these events are rare and require a global network of

observers (e.g. Pluto’s moon Charon by [Sicardy et al. 2006](#); and a member of the dynamical class of classical TNOs, 2002 TX₃₀₀, by [Elliot et al. 2010](#)). Predictions of occultations are limited by astrometric uncertainties of both TNOs and stars. Combining observations of reflected light at optical wavelengths with thermal emission data, which for TNOs peaks in the far-infrared wavelengths, allows us to determine both size and geometric albedo for large samples of targets. This radiometric method using space-based ISO (e.g. [Thomas et al. 2000](#)), *Spitzer* (e.g. [Stansberry et al. 2008](#); [Brucker et al. 2009](#)) and *Herschel* data ([Müller et al. 2010](#); [Lellouch et al. 2010](#); [Lim et al. 2010](#); [Santos-Sanz et al. 2012](#); [Mommert et al. 2012](#); [Vilenius et al. 2012](#); [Pál et al. 2012](#); [Fornasier et al. 2013](#)) has already changed the size estimates of several TNOs compared to those obtained by using an assumed albedo and has revealed a large scatter in albedos and differences between dynamical classes of TNOs.

Observations at thermal wavelengths also provide information about thermal properties ([Lellouch et al. 2013](#)). Depending on the thermal or thermophysical model selected it is possible to derive the thermal beaming factor or the thermal inertia, and constrain other surface properties. Ground-based submillimeter observations can also be used to determine TNO sizes using the radiometric method (e.g. [Jewitt et al. 2001](#)), but this technique has been limited to very few targets so far.

TNOs, also known as Kuiper belt objects (KBO), have diverse dynamical properties and they are divided into classes. Slightly different definitions and names for these classes are available in the literature. Classical TNOs (hereafter CKBOs) reside mostly beyond Neptune on orbits which are not very eccentric and not in mean motion resonance with Neptune. We use the [Gladman et al. \(2008\)](#) classification: CKBOs are non-resonant TNOs which do not belong to any other TNO class. The eccentricity limit is $e \lesssim 0.24$, beyond which objects belong to detached objects or scattering/scattered objects. Classical TNOs with semimajor axis $39.4 < a < 48.4$ AU occupy the main classical belt, whereas inner and outer classicals exist at smaller and larger semi-major axis, respectively. Apart from the Gladman system, another common classification is defined by the Deep Ecliptic Survey Team (DES, [Elliot et al. 2005](#)). For the work presented here, the most notable difference between the two systems is noticed with high-inclination objects. Many of them are not CKBOs in the DES system.

In the inclination/eccentricity space CKBOs show two different populations, which have different frequency of binary systems ([Noll et al. 2008](#)), different luminosity functions (LF; [Fraser et al. 2010](#)), different average geometric albedos ([Grundy et al. 2005](#); [Brucker et al. 2009](#)) and different color distributions ([Peixinho et al. 2008](#)). The low-inclination “cold” classicals are limited to the main classical belt and have a higher average albedo, more binaries and a steeper LF-derived size distribution than high-inclination “hot” classicals. Some amount of transfer between the hot and cold CKBOs is possible with an estimated maximum of 5% of targets in either population originating from the other than its current location ([Volk & Malhotra 2011](#)).

The “*TNOs are Cool*”: A survey of the trans-Neptunian region open time key program ([Müller et al. 2009](#)) of *Herschel* Space Observatory has observed 12 cold CKBOs, 29 hot CKBOs, and five CKBOs in the inner classical belt, which are considered to be dynamically hot. In addition, eight CKBOs have been observed only by *Spitzer* Space Telescope, whose TNO sample was mostly overlapping with the *Herschel* one.

This paper is organized in the following way. We begin by describing our target sample in Sect. 2.1, followed by *Herschel* observations and their planning in Sect. 2.2 and *Herschel* data

reduction in Sect. 2.3. More far-infrared data by *Spitzer* are presented in Sect. 2.4 and absolute visual magnitudes in Sect. 2.5. Thermal modeling combining the above mentioned data is described in Sect. 3.1 and the results for targets in our sample in Sect. 3.2, comparing them with earlier results when available (Sect. 3.3). In Sect. 4 we discuss sample properties, cumulative size distributions, correlations and binaries as well as debiasing of the measured size distributions. Conclusions of the sample analysis are given in Sect. 5.

2. Target sample and observations

2.1. Target sample

The classification of targets in the “TNOs are Cool” program within the [Gladman et al. \(2008\)](#) framework is based on the list used by Minor Bodies in the Outer Solar System 2 data base (MBOSS-2, [Hainaut et al. 2012](#); and Ejeta, priv. comm.). The inclination distributions of the dynamically cold and hot components of CKBOs are partly overlapping. A cut-off limit of $i = 4.5^\circ$ is used in this work, and the inclinations we use from the Minor Planet Center are measured with respect to the ecliptic plane, which deviates slightly from the invariable plane of the Solar System, or the average Kuiper belt plane. All the cold CKBOs with measured sizes available have inclinations $i < 4.0^\circ$ (see Table 6 in Sect. 4). Three CKBOs listed as dynamically hot in Table 7 (2000 OK₆₇, 2001 QD₂₉₈ and Altjira) have $4.5 < i < 5.5^\circ$. Since the two populations overlap in the inclination space some targets close to the cut-off limit could belong to the other population. In the DES classification system all targets in Table 1 with $i > 15^\circ$ would belong to the scattered-extended class of TNOs. DES uses the Tisserand parameter and orbital elements in the CKBO/scattered objects distinction, whereas the Gladman system requires an object to be heavily interacting with Neptune in order to be classified as a scattered object.

In this work we have reduced the flux densities of 16 CKBOs observed with *Herschel*. Together with [Vilenius et al. \(2012\)](#), [Fornasier et al. \(2013\)](#), and [Lellouch et al. \(2013\)](#) this work completes the set of CKBOs observed by *Herschel*, except for the classical Haumea family members with water signatures in their spectra, whose properties differ from the “bulk” of CKBOs ([Stansberry et al.](#), in prep.). Photometric 3-band observations were done in 2010–2011 with *Herschel*/PACS in the wavelength range 60–210 μm . Seven of the 16 targets have been observed also with two bands of *Spitzer*/MIPS imaging photometer at 22–80 μm in 2004–2008. In addition, our target sample (Table 1) includes two previously unpublished targets 2003 QR₉₁ and 2001 QC₂₉₈ observed only with MIPS and are included in the radiometric analysis of this work.

The relative amount of binaries among the cold CKBOs with radiometric measurements is high (Table 6) with only very few non-binaries. While the binary fraction among cold CKBOs has been estimated to be 29% ([Noll et al. 2008](#)) the actual frequency may be higher because there probably are binaries which have not been resolved with current observing capabilities. Furthermore, in the target selection process of “TNOs are Cool” we aimed to have a significant sample of binary TNOs observed, and the highest binary fraction of all dynamical classes is in the cold sub-population of CKBOs.

For sample analysis we have included all CKBOs with radiometric results from this work and literature, some of which have been reanalysed in this work. We achieve a total sample size of 44 targets detected with either *Herschel* or *Spitzer*

Table 1. Orbital and color properties of the sample of 18 classical TNOs with new flux densities presented in this work.

Target		q (AU)	Q (AU)	i ($^\circ$)	e	a	Color taxa ^a	Spectral slope ^d (%/100 nm)	$V - R$
(2001 QS ₃₂₂)		42.3	46.1	0.2	0.043	44.2
66652 Borasisi (1999 RZ ₂₅₃)	B	40.0	47.8	0.6	0.088	43.9	RR	$33.8 \pm 2.7^{e,f}$	$0.646 \pm 0.058^{f,l}$
(2003 GH ₅₅)		40.6	47.3	1.1	0.076	44.0	...	26.0 ± 5.6^g	0.63 ± 0.06^g
135182 (2001 QT ₃₂₂) in inner belt		36.6	37.9	1.8	0.018	37.2	...	15.6 ± 11.1^h	0.53 ± 0.12^h
(2003 QA ₉₁)	B	41.4	47.7	2.4	0.071	44.5
(2003 QR ₉₁)	B	38.1	55.0	3.5	0.182	46.6
(2003 WU ₁₈₈)	B	42.4	46.3	3.8	0.043	44.3
35671 (1998 SN ₁₆₅) in inner belt		36.4	39.8	4.6	0.045	38.1	BB	$6.9 \pm 3.1^{f,i,j,k,l}$	$0.444 \pm 0.078^{f,i,j,k,l}$
(2001 QD ₂₉₈)		40.3	45.1	5.0	0.056	42.7	...	30.4 ± 8.3^m	0.67 ± 0.09^m
174567 Varda (2003 MW ₁₂)	B	39.0	52.2	21.5	0.144	45.6	IR ^{b,c}	19.2 ± 0.6^n	...
86177 (1999 RY ₂₁₅)		34.5	56.5	22.2	0.241	45.5	BR	$3.8 \pm 3.5^{l,o,p}$	$0.358 \pm 0.090^{l,o}$
55565 (2002 AW ₁₉₇)		41.2	53.2	24.4	0.127	47.2	IR	$22.1 \pm 1.4^{g,k,q,r,s}$	$0.602 \pm 0.031^{g,k,q,r,v}$
202421 (2005 UQ ₅₁₃)		37.3	49.8	25.7	0.143	43.5	...	18.1 ± 2.0^f	...
(2004 PT ₁₀₇)		38.2	43.1	26.1	0.060	40.6	0.65 ± 0.10^v
(2002 GH ₃₂)		38.1	45.7	26.7	0.091	41.9	...	24.8 ± 4.7^u	$0.425 \pm 0.228^{m,u,w}$
(2001 QC ₂₉₈)	B	40.6	52.1	30.6	0.124	46.3	...	$10.3 \pm 2.4^{e,g,p}$	0.490 ± 0.030^g
(2004 NT ₃₃)		37.0	50.1	31.2	0.150	43.5	BB-BR ^c
230965 (2004 XA ₁₉₂)		35.5	59.4	38.1	0.252	47.4

Notes. Perihelion distance q , aphelion distance Q , inclination i , eccentricity e , semi-major axis a (orbital elements from IAU Minor Planet Center, URL: <<http://www.minorplanetcenter.net/iau/lists/TNOs.html>>, accessed June 2012), color taxonomy, spectral slope, and $(V - R)$ color index ordered according to increasing inclination. The horizontal line marks the limit of dynamically cold and hot classicals at $i = 4.5^\circ$ (targets in the inner belt are dynamically hot regardless of their inclination). B denotes a known binary system (Noll et al. 2008; except Varda (2003 MW₁₂) from Noll et al. 2009; and Benecchi & Sheppard 2013). Targets are located in the main classical belt unless otherwise indicated.

References. ^(a) Taxonomic class from Fulchignoni et al. (2008) unless otherwise indicated. ^(b) Perna et al. (2010). ^(c) Perna et al. (2013). ^(d) Spectral slopes from MBOSS-2 online database (except 2005 UQ₅₁₃ and 2002 GH₃₂) of Hainaut et al. (2012) at <http://www.eso.org/~ohainaut/MBOSS>, accessed October 2012. References of original data indicated for each target. ^(e) Benecchi et al. (2009). ^(f) Delsanti et al. (2001). ^(g) Jewitt et al. (2007). ^(h) Romanishin et al. (2010). ⁽ⁱ⁾ Jewitt & Luu (2001). ^(j) Gil-Hutton & Licandro (2001). ^(k) Fornasier et al. (2004). ^(l) Doressoundiram et al. (2001). ^(m) Doressoundiram et al. (2005a). ⁽ⁿ⁾ Fornasier et al. (2009). ^(o) Boehnhardt et al. (2002). ^(p) Benecchi et al. (2011). ^(q) Doressoundiram et al. (2005b). ^(r) DeMeo et al. (2009). ^(s) Rabinowitz et al. (2007). ^(t) Pinilla-Alonso et al. (2008). ^(u) Carry et al. (2012). ^(v) Snodgrass et al. (2010). ^(w) Santos-Sanz et al. (2009).

(Tables 6 and 7). The absolute V -magnitudes (H_V , see Sect. 2.5) of the combined sample range from about 3.5 to 8.0 mag (0.1–8.0 mag if dwarf planets are included). A typical characteristic of CKBOs is that bright classicals have systematically higher inclinations than fainter ones (Levison & Stern 2001). Our combined sample shows a moderate correlation (see Sect. 4.5.2) between absolute magnitude and inclination at 4σ level of significance. For about half of the targets a color taxonomy is available. Almost all very red targets (RR) in the combined sample are at inclinations $i < 12^\circ$. This is consistent with Peixinho et al. (2008) who report a color break at $i = 12^\circ$ instead of at the cold/hot boundary inclination near 5° .

2.2. Herschel observations

Herschel Space Observatory (Pilbratt et al. 2010) was orbiting the Lagrange 2 point of the Earth-Sun system in 2009–2013. It has a 3.5 m radiatively cooled telescope and three science instruments inside a superfluid helium cryostat. The photometer part of the PACS instrument (Poglitsch et al. 2010) has a rectangular field of view of $1.75' \times 3.5'$. It has two bolometer arrays, the short-wavelength one is for wavelengths 60–85 μm or 85–125 μm , selectable by a filter wheel, and the long-wavelength array for 125–210 μm . The absolute calibration 1σ uncertainty is 5% in all bands (Balog et al. 2013). The detector pixel sizes are $3.2'' \times 3.2''$ in the short-wavelength array, whereas the long-wavelength array has larger pixels of $6.4'' \times 6.4''$. The instrument is continuously sampling the detectors and produces 40 frames/s, which are averaged on-board

by a factor of four. *Herschel* recommended to use the scanning technique for point sources instead of chopping and nodding, to achieve better sensitivity (PACS AOT release note 2010). Pixels in the image frames, sampled continuously while the telescope was scanning, were mapped in the data reduction pipeline (see Sect. 2.3) into pixels of a sub-sampled output image.

Our observations (Table 2) with PACS followed the same strategy as in Vilenius et al. (2012). We made three-band observations of all targets in two scan directions of the rectangular array, and repeated the same observing sequence on a second visit. We used mini-scan maps with 2–6 repetitions per observation. The final maps are combinations of four observations/target, except at the 160 μm band where all eight observations/target were available independent of the filter wheel selection. To choose the number of repetitions, i.e. the duration of observations, we used a thermal model (see Sect. 3.1) to predict flux densities. We adopted a default geometric albedo of 0.08 and a beaming factor of 1.25 for observation planning purposes. For two bright targets we used other values based on earlier *Spitzer* results (Stansberry et al. 2008): for 1998 SN₁₆₅ a lower geometric albedo of 0.04 and for 2002 AW₁₉₇ a higher geometric albedo of 0.12. In the combined maps the predicted instrumental signal-to-noise ratios (S/N) for the 16 targets with the above assumptions were $S/N \sim 13$ (faintest target $S/N \sim 4$) at the 70 and 100 μm channels and $S/N \sim 7$ (faintest target $S/N \sim 2$) at the 160 μm channel. The sensitivity of the 70 μm channel is usually limited by instrumental noise, while the aim of our combination of observations is to remove the background confusion noise affecting the other two channels, most notably the 160 μm band.

Table 2. *Herschel* observations and monochromatic flux densities at all three PACS bands.

Target	1st OBSIDs of visit 1/2	Dur. (min)	Mid-time	r (AU)	Δ (AU)	α ($^\circ$)	Flux densities (mJy)		
							$70\ \mu\text{m}$	$100\ \mu\text{m}$	$160\ \mu\text{m}$
2001 QS ₃₂₂	1342212692/...2726	188.5	15-Jan.-2011 22:54	42.36	42.78	1.22	1.8 ± 1.1	4.0 ± 1.6	4.3 ± 2.0
Borasisi	1342221733/...1806	226.1	27-May-2011 23:21	41.62	41.74	1.40	<1.0	<1.4	<1.4
2003 GH ₅₅	1342212652/...2714	188.5	15-Jan.-2011 13:14	40.84	41.16	1.31	2.0 ± 1.0	<1.3	<1.4
2001 QY ₂₉₇	1342209492/...9650	194.8	19-Nov.-2010 03:28	43.25	43.25	1.31	<1.3	<2.1	<2.1
2001 QT ₃₂₂	1342222436/...2485	226.1	10-Jun.-2011 15:15	37.06	37.38	1.50	2.6 ± 1.1	<6.7	<1.5
2003 QA ₉₁	1342233581/...4252	226.1	05-Dec.-2011 06:06	44.72	44.85	1.26	1.8 ± 1.1	2.3 ± 1.3	<1.6
2003 WU ₁₈₈	1342228922/...9040	226.1	20-Sep.-2011 04:57	43.31	43.58	1.29	<1.0	<1.0	<1.1
1998 SN ₁₆₅	1342212615/...2688	113.3	15-Jan.-2011 00:39	37.71	37.95	1.46	9.5 ± 1.2	14.2 ± 1.9	5.7 ± 1.8
2001 QD ₂₉₈	1342211949/...2033	188.5	16-Dec.-2010 01:37	41.49	41.85	1.27	2.7 ± 1.1	4.1 ± 1.3	<1.3
Altjira	1342190917/...1120	152.0	23 Feb.-2010 00:32	45.54	45.58	1.25	4.5 ± 1.4	<4.2	<2.3
Varda	1342213822/...3932	113.3	08-Feb.-2011 06:52	47.62	47.99	1.11	23.1 ± 1.7	26.2 ± 2.0	19.0 ± 2.1
1999 RY ₂₁₅	1342221751/...1778	188.5	28-May-2011 01:04	35.50	35.67	1.63	6.6 ± 1.1	5.7 ± 1.6	<2.4
2002 AW ₁₉₇	1342209471/...9654	113.3	19-Nov.-2010 01:59	46.34	46.27	1.24	17.0 ± 1.3	20.2 ± 1.7	15.3 ± 1.5
2005 UQ ₅₁₃	1342212680/...2722	113.3	15-Jan.-2011 20:26	48.65	48.80	1.16	5.3 ± 1.5	6.7 ± 2.0	5.6 ± 2.2
2004 PT ₁₀₇	1342195396/...5462	113.3	23-Apr.-2010 12:01	38.30	38.66	1.41	8.3 ± 1.6	8.6 ± 2.2	7.9 ± 2.8
2002 GH ₃₂	1342212648/...2710	188.5	15-Jan.-2011 11:35	43.29	43.64	1.22	<1.1	<1.5	<1.6
2004 NT ₃₃	1342219015/...9044	113.3	19-Apr.-2011 07:34	38.33	38.69	1.42	17.3 ± 1.7	18.3 ± 2.0	9.7 ± 2.7
2004 XA ₁₉₂	1342217343/...7399	75.7	29-Mar.-2011 10:36	35.71	35.82	1.60	15.0 ± 1.7	14.2 ± 2.2	8.2 ± 5.9

Notes. 2001 QY₂₉₇ and Altjira from [Vilenius et al. \(2012\)](#) have been reanalysed in this work with changes in flux densities and radiometric results. OBSIDs are the observation identifiers in the *Herschel* Science Archive. Each target was observed four times in visit 1 and four times in visit 2. The first OBSID of the consecutive four OBSIDs/visit are given. Duration is the total duration of the two visits, mid-time is the mean UT time, r is the mean heliocentric distance, Δ is the mean *Herschel*-target distance, and α is the mean Sun-target-*Herschel* phase angle (JPL Horizons Ephemeris System, [Giorgini et al. 1996](#)). Flux densities are color-corrected and the 1σ uncertainties include the absolute calibration uncertainty. Upper limits are 1σ noise levels of the final maps. Targets below the horizontal line have $i > 4.5^\circ$.

The selection of the observing window was optimized to utilize the lowest far-infrared confusion noise circumstances ([Kiss et al. 2005](#)) of each target during the *Herschel* mission. Targets were visited twice within the same observing window with a similar set of 2×2 observations on each of the two visits for the purpose of background subtraction ([Kiss et al. 2013](#)). The time gap between the visits was 11–42 h depending on the proper motion of the target.

2.3. PACS data reduction

We used data reduction and image combination techniques developed within the “TNOs are Cool” key program ([Kiss et al. 2013](#), and references cited therein). *Herschel* Interactive Processing Environment (HIPE¹, version 9.0/CIB 2974) was used to produce Level 2 maps with modified scan map pipeline scripts. The pipeline script provided a two-stage high-pass filtering procedure to handle the $1/f$ noise, which is dominating the timelines of individual detectors in the PACS photometer arrays. The script removes from each timeline, excluding the masked parts of timelines where we expect the source to be present, a value obtained by a running median filter. The filter width parameters we used were typically 8/9/16 readouts, and for some targets 10/15/25 readouts at the $70/100/160\ \mu\text{m}$ channels, respectively. We set the map-pixel sizes to $1.1''/\text{pixel}$, $1.4''/\text{pixel}$ and $2.1''/\text{pixel}$ for the three channels, respectively, to properly sample the point spread functions.

For combining the projected output images and reducing the background we use two methods: “super-sky-subtracted” images ([Brucker et al. 2009](#); [Santos-Sanz et al. 2012](#)) and

“double-differential” images ([Mommert et al. 2012](#); [Kiss et al. 2013](#)). The “super-sky” is constructed by masking the source (or an area surrounding the image center when the target is too faint to be recognized in individual images) in each individual image, combining these sky images and subtracting this combined background from each individual image. Then, all background-subtracted images are co-added in the co-moving frame of the target. The “double-differential” images are produced in a different way. Since the observing strategy has been to make two sets of observations with similar settings, we subtract the combined images of the two visits. This yields a positive and a negative beam of the moving source with background structures eliminated. A duplicate of this image is shifted to match the positive beam of the original image with the negative one of the duplicate. After subtracting these from each other we have a double-differential image with one positive and two negative beams, where photometry is done on the central, positive beam. It can be noted that this method works well even if there is a systematic offset in target coordinates due to uncertain astrometry. A further advantage is in the detection of faint sources: they should have one positive and two negative beams in the final image (with negative beams having half the flux density of the positive one). In both methods of combining individual observations of a target we take into account the offsets and uncertainties in pointing and assigned image coordinates ([Pál et al. 2012](#); [Kiss et al. 2013](#)).

Photometry is performed with DAOPHOT routines ([Stetson 1987](#)), which are available via commonly used astronomy software tools such as HIPE, IDL and IRAF (for details how photometry is done in the “TNOs are Cool” program see [Santos-Sanz et al. 2012](#)). A color correction to flux densities is needed because TNOs have a spectral energy distribution (SED) resembling a black body whereas the PACS photometric system assumes a flat SED. The correction, based on instrumental transmission and response curves available from HIPE, is typically at the level of 2% or less depending on the temperature of the TNO.

¹ Data presented in this paper were analysed using “HIPE”, a joint development by the *Herschel* Science Ground Segment Consortium, consisting of ESA, the NASA *Herschel* Science Center, and the HIFI, PACS and SPIRE consortia members, see <http://herschel.esac.esa.int/DpHiPeContributors.shtml>

Table 3. *Spitzer*/MIPS observations.

Target	PID	Mid-time of observation(s)	r (AU)	Δ (AU)	α ($^\circ$)	MIPS 24 μm band		MIPS 70 μm band	
						Dur. (min)	F_{24} (mJy)	Dur. (min)	F_{70} (mJy)
2001 QS ₃₂₂	3542	03-Dec.-2005 13:12	42.32	41.87	1.23	467.2	<0.015	308.5	<1.1
Borasisi	3229	02-Dec.-2004 00:29	41.16	41.16	1.41	99.1	<0.030	218.2	3.6 \pm 0.9
	50024	29-Jul.-2008 16:48	41.41	40.97	1.29	170.45	0.057 \pm 0.007	369.3	1.3 \pm 0.7
2001 QY ₂₉₇	50024	25-Nov.-2008 02:40	43.09	42.73	1.28	170.45	0.016 \pm 0.006	239.17	2.0 \pm 0.9
2001 QT ₃₂₂	3542	26-Dec.-2004 23:46	36.92	36.95	1.56	406.6	<0.037	406.6	<1.5
2003 QA ₉₁	50024	28-Dec.-2008 16:34	44.91	44.87	1.29	431.8	0.079 \pm 0.006	639.2	3.8 \pm 0.4
Teharonhiawako	3229	09-Nov.-2004 20:15	45.00	44.72	1.25	153.27	0.027 \pm 0.010	179.03	1.6 \pm 0.6
2003 QR ₉₁	50024	24-Nov.-2008 13:26	39.12	38.70	1.37	340.9	0.107 \pm 0.007	1074.2	4.8 \pm 0.6
1998 SN ₁₆₅	55	05-Dec.-2004 08:10	37.97	37.54	1.39	no observations		37.3	<13.9
2001 QD ₂₉₈	3542	05-Nov.-2004 13:41	41.19	40.91	1.36	283.3	<0.059	283.3	<1.5
1996 TS ₆₆	3542	29-Jan.-2005 06:34	38.53	38.21	1.42	114.96	0.104 \pm 0.009	268.54	2.3 \pm 0.8
2002 GJ ₃₂	3542	19-Feb.-2006 07:31	43.16	43.16	1.33	214.06	0.024 \pm 0.006	132.87	4.2 \pm 0.9
2002 AW ₁₉₇	55	12-Apr.-2004 16:34	47.13	46.70	1.10	56.7	0.143 \pm 0.027	56.7	13.7 \pm 1.9
2001 QC ₂₉₈	50024	29-Jul.-2008 20:53	40.62	40.31	1.38	170.45	0.158 \pm 0.010	369.25	5.8 \pm 0.7

Notes. Targets 2003 QR₉₁, 2001 QC₂₉₈, 1996 TS₆₆ and 2002 GJ₃₂ were not observed by *Herschel*. The latter two targets are from Brucker et al. (2009) and have been remodeled based on updated flux densities with significant changes in radiometric results. Flux densities of Teharonhiawako and 2001 QY₂₉₇ have been updated from those in Vilenius et al. (2012), and they have been reanalysed in this work. PID is the *Spitzer* program identifier. Observing geometry (heliocentric distance r , *Spitzer*-target distance Δ and Sun-target-*Spitzer* phase angle α) is averaged over the individual observations. The “Dur.” column gives the total observing time of several visits. The durations of observing epochs were 4–8 days, except for 1998 SN₁₆₅ and 2002 AW₁₉₇, which had only one observation. The effective monochromatic wavelengths of the two MIPS bands we use are 23.68 μm and 71.42 μm . Targets below the horizontal line have $i > 4.5^\circ$. In-band fluxes from Mueller et al. (in prep.). Flux densities presented in this table have been color-corrected.

The color correction is fine-tuned in an iterative way (for details see Vilenius et al. 2012). For uncertainty estimation of the derived flux density we use 200 artificial implanted sources within a region close to the source, excluding the target itself.

The color corrected flux densities from PACS are given in Table 2, where also the absolute calibration uncertainty has been included in the 1σ error bars. The flux densities are preferably averaged from the photometry results using the two techniques discussed above: the “super-sky-subtracted” and the “double-differential”. Since the super-sky-subtracted way gives more non-detected bands than the double-differential way we take the average only when the super-sky-subtracted method produces a 3-band detection, otherwise only flux densities based on the double-differential images are used for a given target. In Table 2 the seven targets whose flux densities at 160 μm are >5 mJy have flux densities averaged from the double-differential and super-sky-subtracted methods.

The flux density predictions used in the planning (Sect. 2.2) of these observations differ by factors of ± 2 or more compared to the measured flux densities. On the average, the measured values are lower ($\sim 50\%$) than the predicted ones. Only three targets are brighter than estimated in the PACS bands and there are four targets not detected in the PACS observations. The average S/Ns of detected targets are half of the average S/Ns of the predictions used in observation planning.

2.4. *Spitzer* observations

The Earth-trailing *Spitzer* Space Telescope has a 0.85 m diameter helium-cooled telescope. The cryogenic phase of the mission ended in 2009. During that phase, one of four science instruments onboard, the Multiband Imaging Photometer for *Spitzer* (MIPS; Rieke et al. 2004), provided useful photometry of TNOs at two bands: 24 and 70 μm . The latter is spectrally overlapping with the PACS 70 μm band whereas the former can provide strong constraints on the temperature of the warmest regions of TNOs. The telescope-limited spatial resolution is $6''$ and $18''$

in the two bands, respectively. The nominal absolute calibration, photometric methods, and color corrections are described in Gordon et al. (2007), Engelbracht et al. (2007) and Stansberry et al. (2007). For TNOs we use larger calibration uncertainties of 3% and 6% at the 24 and 70 μm bands, respectively (Stansberry et al. 2008).

Spitzer observed about 100 TNOs and Centaurs and three-quarters of them are also included in the “TNOs are Cool” *Herschel* program. Many of the *Spitzer* targets were observed multiple times within several days, with the visits timed to allow subtraction of the background. A similar technique has been applied also to the *Herschel* observations (Sect. 2.3/“super-sky-subtraction” method). In this work and Vilenius et al. (2012) there are 20 targets (out of 35 *Herschel* targets analysed in these two works) which have reanalysed *Spitzer*/MIPS data available (Mueller et al., in prep.). In addition, we have searched for all classical TNOs observed with *Spitzer* but not with *Herschel*: 1996 TS₆₆, 2001 CZ₃₁, 2001 QB₂₉₈, 2001 QC₂₉₈, 2002 GJ₃₂, 2002 VT₁₃₀, 2003 QR₉₁, and 2003 QY₉₀. The dynamically hot CKBOs 1996 TS₆₆ and 2002 GJ₃₂ have been published in Brucker et al. (2009), but their flux densities have been updated and reanalysed results of this work have changed their size and albedo estimates (Table 7). An updated data reduction was recently done for 2001 QB₂₉₈ and 2002 VT₁₃₀ and we use the results from Mommert (2013) for these two targets. Of the other targets only 2001 QC₂₉₈ and 2003 QR₉₁ are finally used because all the other cases do not have enough observations for a background removal or there was a problem with the observation. *Spitzer* flux densities used in the current work are given in Table 3. For most of these targets flux densities have been derived using multiple observations during an epoch lasting one to eight days. Borasisi was observed in two epochs in 2004 and 2008. The color corrections of CKBOs in our sample are larger than in the case of the PACS instrument. For MIPS the color corrections are 1–10% of the flux density at 24 μm and about 10% at 70 μm obtained by a method which uses the black body temperature which fits the 24:70 flux ratio the best (Stansberry et al. 2007).

Table 4. Optical auxiliary data based on a linear phase curve fit using V -band data points from the literature or databases.

Target	H_V ref.	N	Phase coefficient (mag/°)	L.c. Δm_R (mag)	L.c. period (h)	H_V (mag)	Comment
(2001 QS ₃₂₂)	(x)	4	(default)	6.91 ± 0.68	Default $V - R$
66652 Borasisi (1999 RZ ₂₅₃)	B (e, l, f, y)	7	0.176 ± 0.073	0.08 ± 0.02^z	6.4 ± 1.0^z	6.121 ± 0.070	New β fit
(2003 GH ₅₅)	(c)	3	(default)	6.43 ± 0.12	
135182 (2001 QT ₃₂₂)	(h, x)	5	(default)	7.29 ± 0.67	$V - R$ from (h)
(2003 QA ₉₁)	B (x)	13	(default)	5.76 ± 0.63	Default $V - R$
(2003 QR ₉₁)	B (x)	8	(default)	6.55 ± 0.56	Default $V - R$
(2003 WU ₁₈₈)	B (x)	8	(default)	5.96 ± 0.64	Default $V - R$
35671 (1998 SN ₁₆₅)	(j, k, l, y, b2)	20	0.146 ± 0.063	0.16 ± 0.01^{a2}	8.84^{a2}	5.707 ± 0.085	New β fit
(2001 QD ₂₉₈)	(m)	1	(default)	6.71 ± 0.17	
174567 Varda (2003 MW ₁₂)	B (c)	6	(default)	0.06 ± 0.01^{e2}	5.9^{e2}	3.61 ± 0.05	
86177 (1999 RY ₂₁₅)	(c)	1	(default)	$<0.1^v$...	7.235 ± 0.093	
55565 (2002 AW ₁₉₇)	(s)	(phase curve study)		0.08 ± 0.07^{d2}	8.86 ± 0.01^{d2}	3.568 ± 0.046	
202421 (2005 UQ ₅₁₃)	(v)	10	(default)	0.06 ± 0.02^{e2}	7.03^{e2}	3.87 ± 0.14	Default $V - R$
(2004 PT ₁₀₇)	(v)	24	(default)	0.05 ± 0.1^v	$\sim 20^v$	6.33 ± 0.11	Default $V - R$
(2002 GH ₃₂)	(m, w)	2	(default)	6.58 ± 0.28	$V - R$ from (w)
2001 QC ₂₉₈	B (e, g, v)	3	1.01 ± 0.29	0.4 ± 0.1^v	$\sim 12^v$	6.26 ± 0.32	Default $V - R$
(2004 NT ₃₃)	(c)	6	(default)	0.04 ± 0.01^{e2}	7.87^{e2}	4.74 ± 0.11	
230965 (2004 XA ₁₉₂)	(x)	17	(default)	0.07 ± 0.02^{e2}	7.88^{e2}	4.42 ± 0.63	Default $V - R$

Notes. B denotes a known binary system (Noll et al. 2008, 2009; Benecchi & Sheppard 2013), N is the total number of individual V or R -band data points used, the phase coefficient is explained in the text and Eq. (2), H_V are the absolute V -band magnitudes with uncertainties taking into account light curve (L.c.) amplitude Δm_R . Targets below the horizontal line have inclinations $>4.5^\circ$.

References. (c)–(w) given below Table 1. ^(x) R -band data from IAU Minor Planet Center http://www.minorplanetcenter.net/db_search/, accessed July 2012. ^(y) McBride et al. (2003). ^(z) Kern (2006). ^(a2) Lacerda & Luu (2006). ^(b2) From Ofek (2012) using Eq. (1). ^(c2) Thirouin et al. (2010). ^(d2) Ortiz et al. (2006). ^(e2) Thirouin et al. (2012).

2.5. Optical data

We use the V -band absolute magnitudes (H_V as given in Table 4) as input in the modeling (Sect. 3.1). The quantity and quality of published H_V s or individual V -band or R -band observations vary significantly for our sample. Some of our targets have been observed in the Sloan Digital Sky Survey and to convert from their r and g bands to V -band we use the transformation²

$$V = g - 0.5784(g - r) - 0.0038. \quad (1)$$

The estimated uncertainty of this transformation is 0.02 mag.

To take into account brightening at small phase angles we use the linear method commonly used for distant Solar System objects:

$$H_V = V - 5 \log(r\Delta) - \beta_V \alpha, \quad (2)$$

where r is the heliocentric distance, Δ the observer-target distance, β_V the linear phase coefficient in V -band, and α the Sun-target-observer phase angle. Often the linear phase coefficient cannot be deduced in a reliable way from the few data points available and in those cases we use as default the average values $\beta_V = 0.112 \pm 0.022$ or $\beta_R = 0.119 \pm 0.029$ (Belskaya et al. 2008). Many published H_V values are also based on an assumed phase coefficient. We prefer to use mainly published photometric quality observations due to their careful calibration and good repeatability. For each target we try to determine H_V and β by making a fit to the combined V -data collected from literature. We have determined new linear phase coefficients of Borasisi: $\beta_V = 0.176 \pm 0.073$, 1998 SN₁₆₅: $\beta_V = 0.132 \pm 0.063$ and 2001 QC₂₉₈: $\beta_V = 1.01 \pm 0.29$.

When no other sources are available, or the high-quality data is based on one or two data points, we also take into account data

from the Minor Planet Center (MPC). These observations are often more numerous, or only available at, the R -band. We check if consistency and phase angle coverage of MPC data allow to fit the slope (i.e. β) in a reliable way, otherwise the fit is done using the default phase coefficient. Unless available for a specific target (Table 1), we use the average ($V - R$) color index for CKBOs, which has been determined separately for cold and hot classical³. The average of 49 cold CKBOs is $V - R = 0.63 \pm 0.09$ and of 43 hot CKBOs $V - R = 0.51 \pm 0.14$ (Hainaut et al. 2012). The MPC is mainly used for astrometry and can differ significantly from well-calibrated photometry. Comparisons by Romanishin & Tegler (2005) and Benecchi et al. (2011) indicate an offset of ~ 0.3 mag (MPC having brighter magnitudes) with a scatter of ~ 0.3 mag. We have assigned an uncertainty of 0.6 mag to MPC data points. The absolute magnitudes and their error bars used as input in our analysis (Table 4) take into account additional uncertainties from known or assumed light curve variability in H_V as explained in Vilenius et al. (2012).

3. Analysis

3.1. Thermal modeling

We aim to solve for size (effective diameter D assuming spherical shapes), geometric albedo p_V and beaming factor η by fitting the two or more thermal infrared data points as well as the optical H_V data in the pair of equations

$$F(\lambda) = \frac{\epsilon(\lambda)}{\Delta^2} \int_S B(\lambda, T(S, \eta)) dS \cdot \mathbf{u} \quad (3)$$

$$H_V = m_\odot + 5 \log(\sqrt{\pi}a) - \frac{5}{2} \log(p_V S_{\text{proj}}), \quad (4)$$

³ Note that Vilenius et al. (2012) used one average in their analysis of *Herschel* data on classical TNOs: $V - R = 0.59 \pm 0.15$ based on an earlier version of the MBOSS data base.

² <http://www.sdss.org/dr5/algorithms/sdssUBVRITransform.html>, accessed February 2013.

where F is the flux density, λ the wavelength, ϵ the emissivity, Δ the observer-target distance, $B(\lambda, T)$ Planck’s radiation law for black bodies, $T(S, \eta)$ the temperature distribution on the surface S adjusted by the beaming factor η , \mathbf{u} the unit directional vector towards the observer from the surface element dS , m_\odot the apparent magnitude of the Sun, a the distance of one astronomical unit and S_{proj} the area of the target projected towards the observer. To model the temperature distribution on the surface of an airless, spherical TNO we use the Near-Earth Asteroid Thermal Model NEATM (Harris 1998). For a description of our NEATM implementation for TNOs we refer to Mommert et al. (2012). The temperature distribution across an object differs from the temperature distribution which a smooth object in instantaneous equilibrium with insolation would have. This adjustment is done by the beaming factor η which scales the temperature as $T \propto \eta^{-0.25}$. In addition to the quantities explicitly used in NEATM (solar flux, albedo, heliocentric distance, emissivity) the temperature distribution is affected by other effects combined in η : thermal inertia, surface roughness and the rotation state of the object. Statistically, without detailed information about the spin-axis orientation and period, large η indicates high thermal inertia, and $\eta < 1$ indicates a rough surface. Thermal properties of TNOs have been analysed in detail by Lellouch et al. (2013).

Emissivity is assumed to be constant $\epsilon(\lambda) = 0.9$ as discussed in Vilenius et al. (2012). This assumption is often used for small Solar System bodies. A recent *Herschel* study using both PACS and SPIRE instruments (70, 100, 160, 250, 350 and 500 μm photometric bands) shows that in a sample of nine TNOs/Centaurs most targets show significant indications of an emissivity decrease, but only at wavelengths above 250 μm , except for one active Centaur (Fornasier et al. 2013). Thus, we assume that emissivity of CKBOs is constant at MIPS and PACS wavelengths.

The free parameters p_V , $D = \sqrt{\frac{4S_{\text{proj}}}{\pi}}$ and η are fitted in a weighted least-squares sense by minimizing

$$\chi_\nu^2 = \frac{1}{\nu} \sum_{i=1}^N \frac{[F(\lambda_i) - F_{\text{model}}(\lambda_i)]^2}{\sigma_i^2}, \quad (5)$$

where χ_ν^2 is called the “reduced χ^2 ”, ν is the number of degrees of freedom, N the number of data points, $F(\lambda_i)$ the observed flux density at wavelength λ_i , or H_V transformed to flux density scale, with uncertainty σ_i , and F_{model} is the calculated thermal emission or optical brightness from Eqs. (3) and (4). The number of degrees of freedom is $N - 3$ when H_V is counted as one data point. If the fit fails or gives an unphysical η then a fixed- η fit is made instead (see Sect. 3.2) and the number of degrees of freedom is $N - 2$.

The error estimates of the fitted parameters are determined by a Monte Carlo method (Mueller et al. 2011) using a set of 1000 randomized input flux densities and absolute visual magnitudes for each target, as well as beaming factor for fixed- η cases. Our implementation of the technique is shown in Mommert et al. (2012). In cases of poor fit, i.e. reduced- χ^2 significantly greater than one, the error bars are first rescaled so that the Monte Carlo method would not underestimate the uncertainties of the fitted parameters. This is discussed in (Santos-Sanz et al. 2012, Appendix B.1). The assumption that the targets are spherical may slightly overestimate diameters, since most TNOs are known to be MacLaurin spheroids (Duffard et al. 2009; Thirouin et al. 2010). NEATM model accuracy at small phase angles is about 5% in the diameter estimates and 10% in the geometric albedo (e.g. Harris 2006).

3.1.1. Treatment of upper limits

Tables 2 and 3 list several data points where only an upper limit for flux density is given. As mentioned in Sect. 2.3 the observed flux densities of our sample were often lower than predictions by a factor of two or more. In the planning we aimed at $S/N = 2-4$ for the faintest targets (Sect. 2.2). If a target has at least one $S/N > 1$ data point we can assume that the flux densities are not far below the $S/N = 1$ detection limit in the other, non-detected, bands. Such upper limits we replace by a distribution of possible flux densities. We assign them values, using a Monte Carlo technique, from a one-sided Gaussian distribution with the map noise (upper limits in Tables 2 and 3) as the standard deviation. We calculate the optimum solution in the sense of Eq. (5) and repeat this 500 times. The adopted D , p_V and η are the medians of all the obtained values of the fitted parameters, respectively.

It should be noted that both the treatment of upper limit bands as well as non-detected targets (discussed below) is done in a different way in this work than in previous works who treated upper limits as data points with zero flux density: $0 \pm 1\sigma$. We have remodeled the CKBO sample of Vilenius et al. (2012) using our new convention and find changes in size larger than $\sim 10\%$ for a few targets (see Sect. 3.3).

For targets which are non-detections in all bands we give upper limits for diameters and lower limits for geometric albedos. We calculate them by making a fixed- η fit to the most constraining upper limit and assign a zero flux density in that band, which is the 70 μm band in all the three cases (2002 GV₃₁, 2003 WU₁₈₈, 2002 GH₃₂), using a 2σ uncertainty. The reason to choose 2σ instead of 1σ for non-detections is explained in the following. At the limit of detection $S/N = 1$ and we have a flux density of $F = s \pm s$, where s is the 1σ Gaussian noise level of the map determined by doing photometry on 200 artificial sources randomly implanted near the target. Thus, the probability that the “true” flux density of the target is more than 1σ above the nominal value s (i.e. $F > 2s$) is 16%. On the other hand, if the $S/N = 1$ observation is interpreted as an upper limit a similar probability for the flux density to exceed $F > 2s$ should occur. This requires that upper limits, which have been assigned zero flux for non-detections, are treated as $0 \pm 2\sigma$ in order to avoid this discontinuity at $S/N = 1$.

3.2. Results of model fits

The results of model fits using the NEATM (see Sect. 3.1) are given in Table 5. For binary systems the diameters are to be interpreted as area-equivalent diameters because our observations did not spatially resolve separate components. The preferred solutions, based on the combination of *Herschel*/PACS and *Spitzer*/MIPS data when available, are shown in Fig. 1. Although size estimates can be done using one instrument alone, the combination of both instruments samples the thermal peak and the short-wavelength side of the SED by extending the wavelength coverage and number of data points. When possible, we solve for three parameters: radiometric (system) diameter, geometric albedo and beaming factor. If data consistency does not allow a three-parameter solution we fit for diameter and albedo. This type of “fixed- η ” solution is chosen if a floating- η solution (i.e. η as one of the parameters to be fitted) gives an “unphysical” beaming factor ($\eta \lesssim 0.6$ or $\eta > 2.6$). An often used value for the fixed- η is 1.20 ± 0.35 (Stansberry et al. 2008) and it was used also in previous works based on *Herschel* data (Santos-Sanz et al. 2012; Mommert et al. 2012; Vilenius et al. 2012). A three-parameter fit may give a solution which has very large error bars

Table 5. Solutions of radiometric modeling.

Target	Instruments	No. of bands	D (km)	p_V ^(a)	η	Solution type	Comment
(2001 QS ₃₂₂)	PACS	3	253 ⁺⁸⁷ ₋₂₉	0.048 ^{+0.587} _{-0.030}	1.20 ± 0.35	fixed η	default η
(2001 QS₃₂₂)	PACS, MIPS	5	186 ⁺⁹⁹ ₋₂₄	0.095 ^{+0.531} _{-0.060}	1.20 ± 0.35	fixed η	default η
66652 Borasisi (1999 RZ₂₅₃)	B PACS, MIPS	5	163 ⁺³² ₋₆₆	0.236 ^{+0.438} _{-0.077}	0.77 ^{+0.19} _{-0.47}	floating η	
(2003 GH₅₅)	PACS	3	178 ⁺²¹ ₋₅₆	0.150 ^{+0.182} _{-0.031}	1.20 ± 0.35	fixed η	default η
135182 (2001 QT ₃₂₂)	PACS	3	173 ⁺²⁵ ₋₅₅	0.071 ^{+0.091} _{-0.044}	1.20 ± 0.35	fixed η	default η
135182 (2001 QT₃₂₂)	PACS, MIPS	5	159 ⁺³⁰ ₋₄₇	0.085 ^{+0.424} _{-0.052}	1.20 ± 0.35	fixed η	default η
(2003 QA ₉₁)	B PACS	3	233 ⁺⁴⁰ ₋₅₆	0.162 ^{+0.162} _{-0.094}	1.20 ± 0.35	fixed η	default η
(2003 QA₉₁)	PACS, MIPS	5	260 ⁺³⁰ ₋₃₆	0.130 ^{+0.119} _{-0.075}	0.83 ^{+0.10} _{-0.15}	floating η	
(2003 QR₉₁)	B MIPS	2	280 ⁺²⁷ ₋₃₀	0.054 ^{+0.035} _{-0.028}	1.20 ^{+0.10} _{-0.12}	floating η	
(2003 WU₁₈₈)	B PACS	3	<220	>0.15	1.20 ± 0.35	fixed η	default η
35671 (1998 SN ₁₆₅)	PACS	3	392 ⁺⁴³ ₋₅₂	0.060 ^{+0.020} _{-0.012}	1.22 ± 0.35	fixed η	adjusted η
35671 (1998 SN₁₆₅)	PACS, MIPS	4	393 ⁺⁴⁹ ₋₄₈	0.060 ^{+0.019} _{-0.013}	1.23 ± 0.35	fixed η	adjusted η
(2001 QD ₂₉₈)	PACS	3	237 ⁺²⁵ ₋₅₃	0.065 ^{+0.039} _{-0.013}	1.20 ± 0.35	fixed η	default η
(2001 QD₂₉₈)	PACS, MIPS	5	233 ⁺²⁷ ₋₆₃	0.067 ^{+0.062} _{-0.014}	1.26 ± 0.35	fixed η	adjusted η
174567 Varda (2003 MW₁₂)	B PACS	3	792 ⁺⁹¹ ₋₈₄	0.102 ^{+0.024} _{-0.020}	0.84 ^{+0.28} _{-0.22}	floating η	
86177 (1999 RY₂₁₅)	PACS	3	263 ⁺²⁹ ₋₃₇	0.0325 ^{+0.0122} _{-0.0065}	1.20 ± 0.35	fixed η	default η
55565 (2002 AW ₁₉₇)	PACS	3	714 ⁺⁷⁶ ₋₇₄	0.130 ^{+0.031} _{-0.023}	1.04 ^{+0.31} _{-0.27}	floating η	
55565 (2002 AW₁₉₇)	PACS, MIPS	5	768 ⁺³⁹ ₋₃₈ ^(b)	0.112 ^{+0.012} _{-0.011}	1.29 ^{+0.13} _{-0.10}	floating η	
202421 (2005 UQ₅₁₃)	PACS	3	498 ⁺⁶³ ₋₇₅	0.202 ^{+0.084} _{-0.049}	1.27 ± 0.35	fixed η	adjusted η
(2004 PT₁₀₇)	PACS	3	400 ⁺⁴⁵ ₋₅₁	0.0325 ^{+0.0111} _{-0.0066}	1.53 ± 0.35	fixed η	adjusted η
(2002 GH₃₂)	PACS	3	< 230	> 0.075	1.20 ± 0.35	fixed η	default η
2001 QC₂₉₈	B MIPS	2	303 ⁺²⁹ ₋₃₂	0.063 ^{+0.029} _{-0.018}	0.983 ^{+0.085} _{-0.097}	floating η	
(2004 NT₃₃)	PACS	3	423 ⁺⁸⁷ ₋₈₀	0.125 ^{+0.069} _{-0.039}	0.69 ^{+0.46} _{-0.32}	floating η	
230965 (2004 XA₁₉₂)	PACS	3	339 ⁺¹²⁰ ₋₉₅	0.26 ^{+0.34} _{-0.15}	0.62 ^{+0.79} _{-0.49}	floating η	

Notes. The preferred solution (target name and instruments in boldface) is the one with data from two instruments, when available (see also Sect. 3.2). “B” indicates a known binary system and the diameter given is the area-equivalent system diameter. ^(a) Lower uncertainty limited by the uncertainty of H_V for 2001 QS₃₂₂ (both solutions), 2003 QA₉₁ (both solutions), 2003 QR₉₁, 2001 QT₃₂₂ (both solutions), 2001 QC₂₉₈, and 2004 XA₁₉₂. ^(b) Error estimate limited by the diameter uncertainty of 5% of the NEATM model.

such that the uncertainty in η would cover its whole physical range. In such cases we have adopted the fitted value of η as an “adjusted fixed- η ” value and run the fit again keeping η constant. In these cases we assign an error bar of ± 0.35 to the “adjusted fixed- η ” value to be consistent with estimates produced with the default fixed eta of 1.20 ± 0.35 . The type of solution is indicated in Table 5.

Since many of our targets have data only from PACS we show also the PACS-only solutions in Table 5 for all targets which have been detected in at least one PACS band. In many cases the data from PACS and the combined data set are consistent with each other and the difference is small. An exception is 2001 QS₃₂₂. For this target the different solutions are due to the effect of the 24 μ m MIPS upper limit.

3.3. Comparison with earlier results

Of the 18 targets in our sample only 2001 QD₂₉₈ and 2002 AW₁₉₇ have earlier published diameter/albedo solutions and additionally 2001 QS₃₂₂ and 2001 QT₃₂₂ have upper size limits in the literature. For 2001 QD₂₉₈ the *Spitzer*/MIPS based result, with different MIPS flux densities and H_V than used in this work (Table 3), was $D = 150^{+50}_{-40}$, $p_V = 0.18^{+0.17}_{-0.08}$, $\eta = 0.79^{+0.28}_{-0.26}$ (Brucker et al. 2009). Our new diameter (233⁺²⁷₋₆₃ km) is larger and geometric albedo (0.067^{+0.062}_{-0.014}) is lower than the previous estimate.

The first size measurement of 2002 AW₁₉₇ was done with the Max Planck Millimeter Bolometer at the IRAM 30 m telescope. The result of Margot et al. (2002) was $D = 886^{+115}_{-131}$

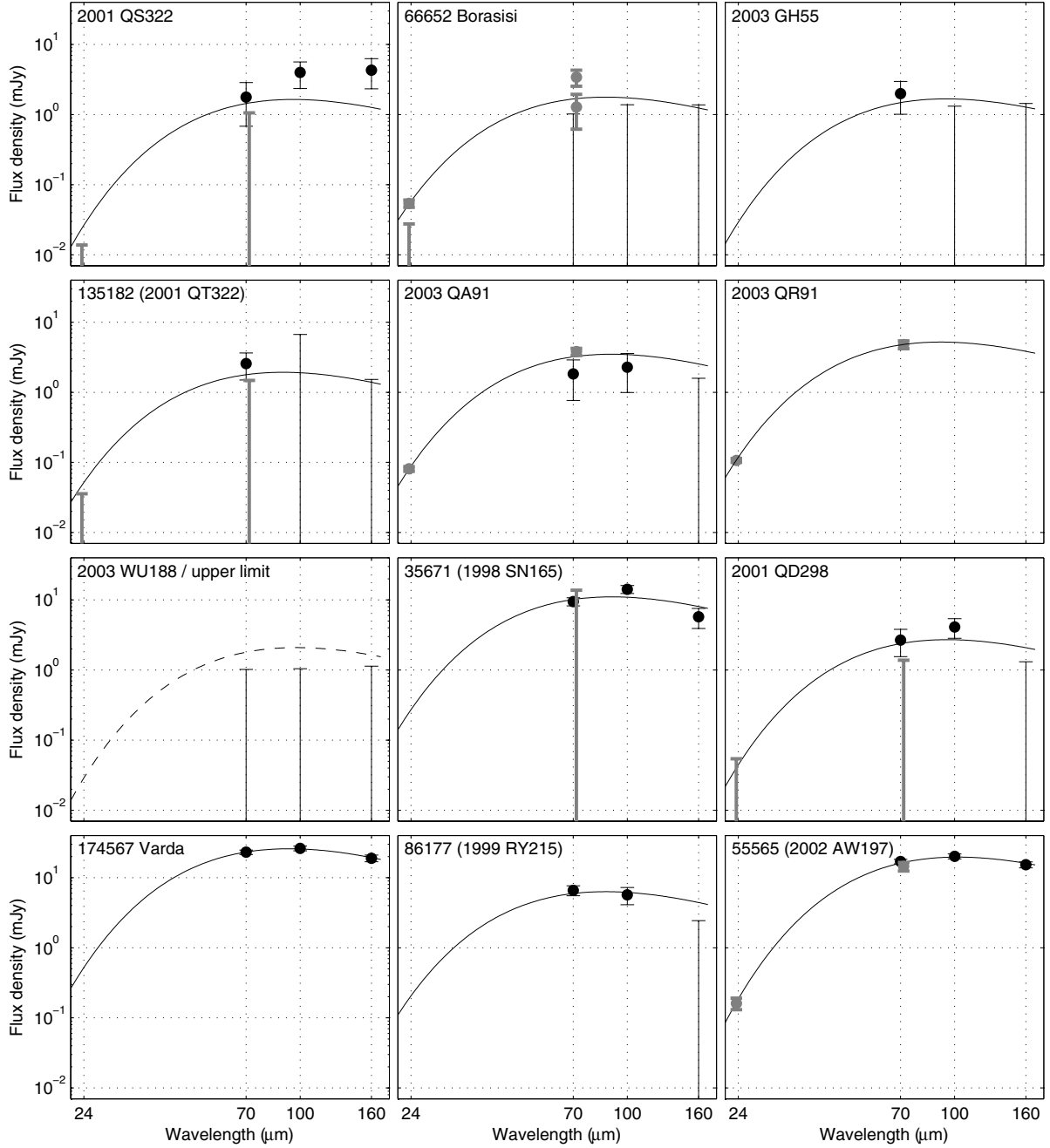


Fig. 1. SEDs calculated from the model solutions (Table 5). The black data points are from PACS (70, 100 and 160 μm) and the gray points are from MIPS (23.68 and 71.42 μm) normalized to the observing geometry of PACS. Error bars without a data point indicate 1σ upper limits. An upper-limit solution based on a non-detection is marked with a dashed line (see text). Target 2003 QR₉₁ was not observed by PACS.

and $p_R = 0.101^{+0.038}_{-0.022}$. *Spitzer* measurements gave a smaller size $D = 740 \pm 100$ km and $p_V = 0.12^{+0.04}_{-0.03}$ (Brucker et al. 2009). Our new result is close to this and has significantly smaller error bars ($D = 768^{+39}_{-38}$, $p_V = 0.112^{+0.012}_{-0.011}$).

The previous limits of 2001 QS₃₂₂ were $D < 200$ km and $p_V > 0.15$ (Brucker et al. 2009). While the diameter limit is compatible with the new size estimate (186⁺⁹⁹₋₂₄ km) the new geometric albedo is lower (0.095^{+0.531}_{-0.060}) due to PACS data points and updated H_V . Also the MIPS data has been reanalysed and has changed for this target. Similarly, the geometric albedo estimate of 2001 QT₃₂₂ is now 0.085^{+0.424}_{-0.052} which is lower than the previous lower limit of 0.21 (Brucker et al. 2009). We use a different absolute visual magnitude $H_V = 7.29 \pm 0.67$, whereas Brucker et al. (2009) used 6.4 ± 0.5 .

For binary targets it is possible to estimate a size range based on the assumptions of spherical shapes and equal albedos of the primary and secondary components. Assuming a bulk density range of 0.5–2.0 g cm⁻³ and using the system mass and brightness difference from Grundy et al. (2011) the diameter range for Borasisi (primary component) is 129–205 km. Our solution for the Borasisi-Pabu system is 163⁺³²₋₆₆ km and the derived density 2.1^{+2.6}_{-1.2} g cm⁻³ (see Sect. 4.6). Our new estimate for the primary component is 126⁺²⁵₋₅₁ km (Table 9).

We have remodeled Teharonhiawako (from Vilenius et al. 2012) with updated *Spitzer*/*MIPS* flux densities given in Table 3. The updated result gives a 24% larger size and 34% smaller albedo (See Fig. 2 and Tables 6–7 for all results.). Previously, MIPS data reduction gave upper limits only for 2001 QY₂₉₇.

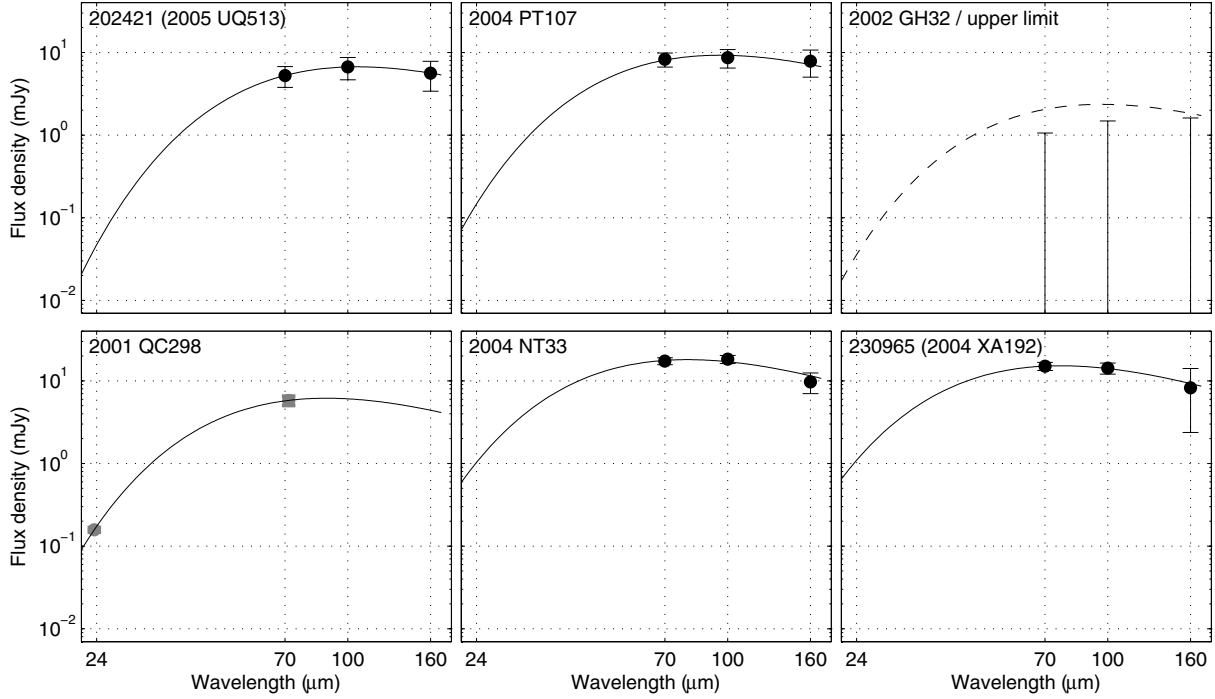


Fig. 1. continued. 2002 GH₃₂ has an upper limit solution (see text).

Table 6. Adopted physical properties of cold classical TNOs.

Target	i (°)	a (AU)	D (km)	p_V	η	No. of bands	Reference
(2001 QS ₃₂₂)		44.2	186^{+99}_{-24}	$0.095^{+0.531}_{-0.060}$	(fixed)	5	This work
66652 Borasisi (1999 RZ ₂₅₃)	B	0.6	163^{+32}_{-66}	$0.236^{+0.438}_{-0.077}$	$0.77^{+0.19}_{-0.47}$	5	This work
(2003 GH ₅₅)		44.0	178^{+21}_{-56}	$0.150^{+0.182}_{-0.031}$	(fixed)	3	This work
(2001 XR ₂₅₄)	B	1.2	221^{+41}_{-71}	$0.136^{+0.168}_{-0.044}$	(fixed)	3	(*) Vilenius et al. (2012)
275809 (2001 QY ₂₉₇)	B	1.5	229^{+22}_{-108}	$0.152^{+0.439}_{-0.035}$	$1.52^{+0.22}_{-0.92}$	5	(*) Vilenius et al. (2012)
(2002 VT ₁₃₀)	B	1.2	324^{+57}_{-68}	$0.097^{+0.098}_{-0.049}$	1.20 ± 0.35	2	Mommert (2013)
(2001 QB ₂₉₈)		42.6	196^{+71}_{-53}	$0.167^{+0.162}_{-0.082}$	1.20 ± 0.35	2	Mommert (2013)
(2001 RZ ₁₄₃)	B	2.1	140^{+39}_{-33}	$0.191^{+0.066}_{-0.045}$	$0.75^{+0.23}_{-0.19}$	5	Vilenius et al. (2012)
(2002 GV ₃₁)		43.9	<180	>0.19	(fixed)	3	(*) Vilenius et al. (2012)
79360 Sila	B	2.2	343 ± 42	$0.090^{+0.027}_{-0.017}$	$1.36^{+0.21}_{-0.19}$	5	Vilenius et al. (2012)
(2003 QA ₉₁)	B	2.4	260^{+30}_{-36}	$0.130^{+0.119}_{-0.075}$	$0.83^{+0.10}_{-0.15}$	5	This work
88611 Teharonhiawako	B	2.6	220^{+41}_{-44}	$0.145^{+0.086}_{-0.045}$	$1.08^{+0.30}_{-0.28}$	5	(*) Vilenius et al. (2012)
(2005 EF ₂₉₈)	B	2.9	174^{+27}_{-32}	$0.16^{+0.13}_{-0.07}$	(fixed)	3	Vilenius et al. (2012)
(2003 QR ₉₁)	B	3.5	280^{+27}_{-30}	$0.054^{+0.035}_{-0.028}$	$1.20^{+0.10}_{-0.12}$	2	This work
(2003 WU ₁₈₈)	B	3.8	<220	>0.15	(fixed)	3	This work

Notes. “B” indicates a known binary system (Noll et al. 2008, 2009; Benecchi & Sheppard 2013) and the diameter given is the area-equivalent system diameter. (*) Marks a target remodeled in this work using input data from the reference.

After updated data reduction from both instruments the solution of 2001 QY₂₉₇ is now based on a floating- η fit instead of a fixed- η as was the case previously in Vilenius et al. (2012). The new albedo estimate is lower, and the new size estimate is 15% larger. Altjira, which has updated PACS flux densities, is now estimated to be 29% larger than in Vilenius et al. (2012). The dynamically hot CKBOs 1996 TS₆₆ and 2002 GJ₃₂, which have only *Spitzer* observations (Brucker et al. 2009), have been remodeled (see Table 7) after significant changes in flux densities. In our new estimates target 2002 GJ₃₂ has low albedo and large size, whereas the result of Brucker et al. (2009) was a smaller target

with moderately high albedo. Contrary, 1996 TS₆₆’s new size estimate is smaller than the previous one, with higher albedo.

Due to the different treatment of upper limits (Sect. 3.1.1) the sizes of 2000 OK₆₇, 2001 XR₂₅₄, 2002 KW₁₄, and 2003 UR₂₉₂ have changed while input values in the modeling are the same as in Vilenius et al. (2012) (see Tables 6, 7 and Fig. 2). The authors of that work had ignored all three upper limits of 2002 KW₁₄ to obtain a floating- η fit for this target but with the new treatment of upper limits there is no need to ignore any data. Instead of a 319 km target with geometric albedo 0.08 the new solution gives a high geometric albedo of 0.31 and a diameter of 161 km. The

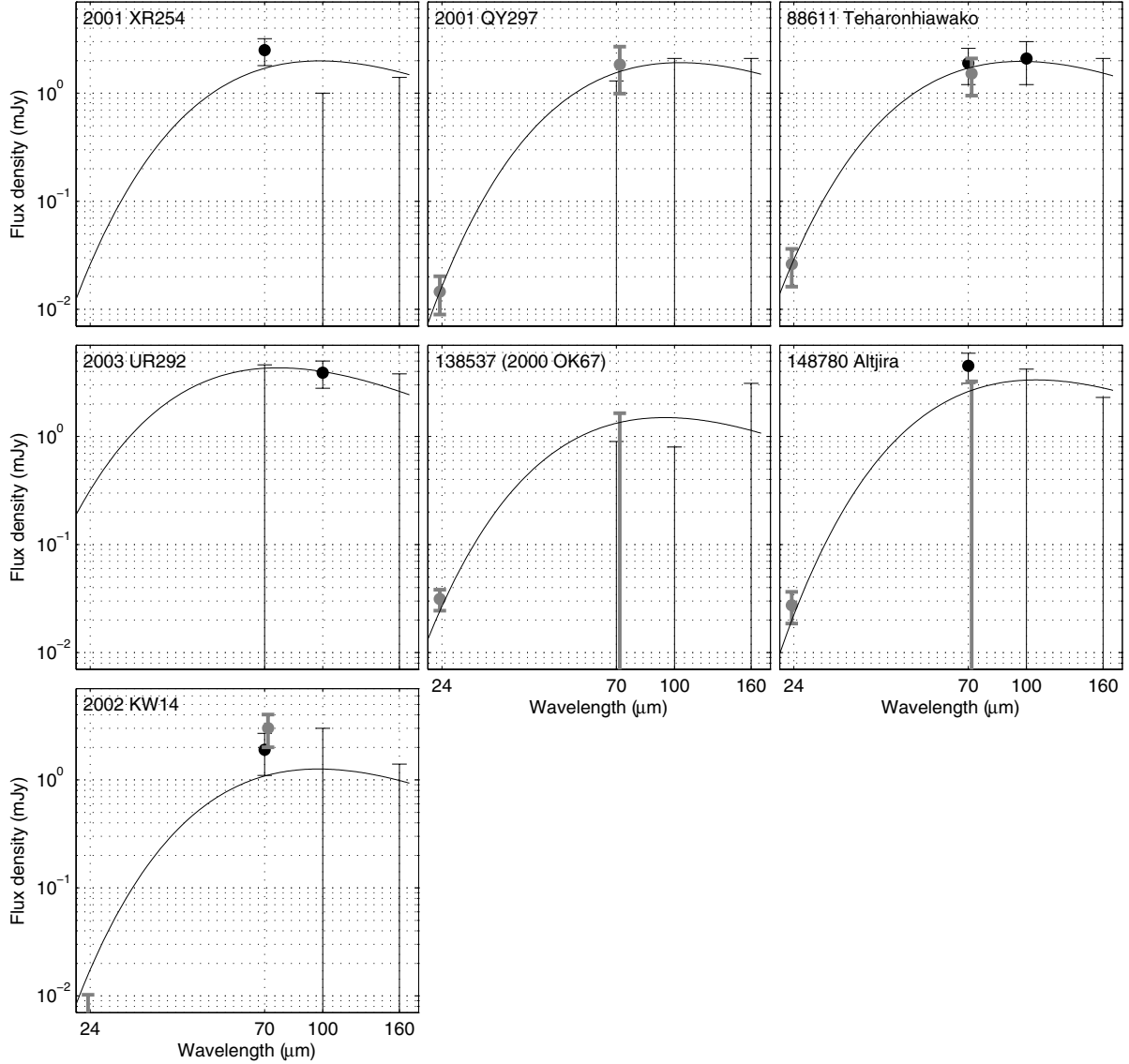


Fig. 2. SEDs calculated for remodeled targets from Vilenius et al. (2012). *Spitzer* data (gray points at 24 and 71 μm) have been reduced to *Herschel* observing geometry.

only case where we have ignored one upper limit is 2000 OK₆₇, which has four upper limits and was not detected by PACS. The upper limit at 160 μm is an outlier compared to the others at 70–100 μm and therefore we do not assume that band to be close to the detection limit (see the adopted solution in Fig. 2).

4. Sample results and discussion

In planning the *Herschel* observations we used a default assumption for geometric albedo of 0.08. As seen in Tables 6, 7, almost all dynamically cold CKBOs and more than half of hot CKBOs have higher albedos implying lower flux densities at far-infrared wavelengths. This has led to the moderate S/Ns and several upper limit flux densities in our sample. The frequency of binaries among the cold CKBOs is high due to the selection process of *Herschel* targets (see Sect. 2.1). We use this sample of cold CKBOs, affected by the binarity bias, in the debiasing procedure of their size distribution because of the very small number of non-binaries available. In the analysis of sample properties of CKBOs we sometimes use a restricted sample, which we call “regular” CKBOs, where dwarf planets (Quaoar,

Varuna, Makemake) and Haumea family members (Haumea and 2002 TX₃₀₀) have been excluded. All five targets mentioned are dynamically hot so that no cold CKBOs are excluded when analysing the “regular CKBOs” sample.

4.1. Measured sizes

The diameter estimates in the “regular CKBO” sample are ranging from 136 km of 2003 UR₂₉₂ up to 934 km of 2002 MS₄. The not detected targets (2002 GV₃₁, 2003 WU₁₈₈ and 2002 GH₃₂) may be smaller than 2003 UR₂₉₂. Dynamically cold targets in our measured sample are limited to diameters of 100–400 km whereas hot CKBOs have a much wider size distribution up to sizes of ~900 km in our measured “regular CKBO” sample and up to 1430 km when dwarf planets are included.

We show the cumulative size distribution $N(>D) \propto D^{1-q}$ of hot classicals (from Table 7) and cold classicals (from Table 6) in Fig. 3⁴. In the measured, biased, size distribution of hot CKBOs

⁴ Note that in Vilenius et al. (2012) the authors used a different definition: $N(>D) \propto D^{-q}$, but that notation differs from most of the literature.

Table 7. Adopted physical properties of hot classical TNOs.

Target	i (°)	a (AU)	D (km)	p_V	η	No. of bands	Reference
2002 KX ₁₄	0.4	38.9	455 ± 27	0.097 ^{+0.014} _{-0.013}	1.79 ^{+0.16} _{-0.15}	5	Vilenius et al. (2012)
2001 QT ₃₂₂	1.8	37.2	159 ⁺³⁰ ₋₄₇	0.085 ^{+0.424} _{-0.052}	(fixed)	5	This work
2003 UR ₂₉₂	2.7	32.6	136 ⁺¹⁶ ₋₂₆	0.105 ^{+0.081} _{-0.033}	(fixed)	3	(*) Vilenius et al. (2012)
1998 SN ₁₆₅	4.6	38.1	393 ⁺³⁹ ₋₃₈	0.060 ^{+0.019} _{-0.013}	(fixed)	4	This work
2000 OK ₆₇	4.9	46.8	164 ⁺³³ ₋₄₅	0.169 ^{+0.159} _{-0.052}	(fixed)	5	(*) Vilenius et al. (2012)
2001 QD ₂₉₈	5.0	42.7	233 ⁺²⁷ ₋₆₃	0.067 ^{+0.062} _{-0.014}	(fixed)	5	This work
148780 Altjira	B	5.2	331 ⁺⁵¹ ₋₁₈₇	0.0430 ^{+0.1825} _{-0.0095}	1.62 ^{+0.24} _{-0.83}	5	(*) Vilenius et al. (2012)
1996 TS ₆₆	7.3	44.2	159 ⁺⁴⁴ ₋₄₆	0.179 ^{+0.173} _{-0.070}	0.75 ^{+0.21} _{-0.27}	2	(*) Brucker et al. (2009)
50000 Quaoar	B	8.0	1074 ± 38	0.127 ^{+0.010} _{-0.009}	1.73 ± 0.08	8	Fornasier et al. (2013)
2002 KW ₁₄	9.8	46.5	161 ⁺³⁵ ₋₄₀	0.31 ^{+0.281} _{-0.094}	(fixed)	5	(*) Vilenius et al. (2012)
2002 GJ ₃₂	11.6	44.1	416 ⁺⁸¹ ₋₇₈	0.035 ^{+0.019} _{-0.011}	2.05 ^{+0.38} _{-0.36}	2	(*) Brucker et al. (2009)
2001 KA ₇₇	11.9	47.3	310 ⁺¹⁷⁰ ₋₆₀	0.099 ^{+0.052} _{-0.056}	2.52 ^{+0.18} _{-0.83}	5	Vilenius et al. (2012)
19521 Chaos	12.0	46.0	600 ⁺¹⁴⁰ ₋₁₃₀	0.050 ^{+0.030} _{-0.016}	2.2 ^{+1.2} _{-1.1}	4	Vilenius et al. (2012)
2002 XW ₉₃	14.3	37.6	565 ⁺⁷¹ ₋₇₃	0.038 ^{+0.043} _{-0.025}	0.79 ^{+0.27} _{-0.24}	3	Vilenius et al. (2012)
20000 Varuna	17.2	43.0	668 ⁺¹⁵⁴ ₋₈₆	0.127 ^{+0.040} _{-0.042}	2.18 ^{+1.04} _{-0.49}	3	Lellouch et al. (2013)
2002 MS ₄	17.7	41.7	934 ± 47	0.051 ^{+0.036} _{-0.022}	1.06 ± 0.06	5	Vilenius et al. (2012)
2005 RN ₄₃	19.2	41.8	679 ⁺⁵⁵ ₋₇₃	0.107 ^{+0.029} _{-0.018}	(fixed)	3	Vilenius et al. (2012)
2002 UX ₂₅	B	19.4	697 ± 35	0.107 ± 0.010	1.07 ^{+0.08} _{-0.05}	8	Fornasier et al. (2013)
174567 Varda	B	21.5	792 ⁺⁹¹ ₋₈₄	0.102 ^{+0.024} _{-0.020}	0.84 ^{+0.28} _{-0.22}	3	This work
2004 GV ₉	22.0	41.8	680 ± 34	0.0770 ^{+0.0084} _{-0.0077}	1.93 ^{+0.09} _{-0.07}	5	Vilenius et al. (2012)
1999 RY ₂₁₅	22.2	45.5	263 ⁺²⁹ ₋₃₇	0.0388 ^{+0.0122} _{-0.0065}	(fixed)	3	This work
120347 Salacia	B	23.9	901 ± 45	0.044 ^{+0.004} _{-0.004}	1.16 ± 0.03	8	Fornasier et al. (2013)
2002 AW ₁₉₇	24.4	47.2	768 ⁺³⁹ ₋₃₈	0.112 ^{+0.012} _{-0.011}	1.29 ^{+0.13} _{-0.10}	5	This work
2005 UQ ₅₁₃	25.7	43.5	498 ⁺⁶³ ₋₇₅	0.202 ^{+0.084} _{-0.049}	(fixed)	3	This work
2002 TX ₃₀₀	25.8	43.5	286 ± 10	0.88 ^{+0.15} _{-0.06}	1.15 ^{+0.55} _{-0.74}	occultation +3	Elliot et al. (2010), Lellouch et al. (2013)
2004 PT ₁₀₇	26.1	40.6	400 ⁺⁴⁵ ₋₅₁	0.0325 ^{+0.0111} _{-0.0066}	(fixed)	3	This work
2002 GH ₃₂	26.7	41.9	<180	>0.13	(fixed)	3	This work
136108 Haumea	B	28.2	1240 ⁺⁶⁹ ₋₅₉	0.804 ^{+0.062} _{-0.095}	0.95 ^{+0.33} _{-0.26}	3	(Fornasier et al. 2013, 2013)
136472 Makemake	29.0	45.5	1430 ± 9	0.77 ± 0.03	2.29 ^{+0.46} _{-0.40}	occultation +3	Ortiz et al. (2012), Lellouch et al. (2013)
2001 QC ₂₉₈	B	30.6	303 ⁺²⁷ ₋₃₀	0.061 ^{+0.027} _{-0.017}	0.985 ^{+0.084} _{-0.095}	2	This work
2004 NT ₃₃	31.2	43.5	423 ⁺⁸⁷ ₋₈₀	0.125 ^{+0.069} _{-0.039}	0.69 ^{+0.46} _{-0.32}	3	This work
2004 XA ₁₉₂	38.1	47.4	339 ⁺¹²⁰ ₋₉₅	0.20 ^{+0.34} _{-0.15}	0.62 ^{+0.79} _{-0.49}	3	This work

Notes. “B” indicates a known binary system and the diameter given is the area-equivalent system diameter. (*) marks a target remodeled in this work.

we can distinguish three regimes for the power law slope: $100 < D < 300$ km, $400 < D < 600$ km and $700 < D < 1300$ km. The slope parameters for the latter two regimes are $q \approx 2.0$ and $q \approx 4.0$. In the small-size regime there are not enough targets in different size bins to derive a reliable slope. The measured, biased, cold CKBO sample gives a slope of $q \approx 4.3$ in the size range $200 < D < 300$ km. The debiased size distribution slopes are given in Sect. 4.3.

4.2. Measured geometric albedos

Haumea family members and many dwarf planets have very high geometric albedos. The highest-albedo regular CKBO is 2002 KW₁₄ with $p_V = 0.31$ and the darkest object is 2004 PT₁₀₇ with $p_V = 0.0325$, both dynamically hot. Among dynamically

cold objects geometric albedo is between Sila’s $p_V = 0.090$ and Borasisi’s $p_V = 0.236$.

The sub-sample of cold CKBOs are lacking low-albedo objects compared to the hot sub-sample. Figure 4 shows probability density functions constructed from the measured geometric albedos and their asymmetric error bars using the technique described in detail in Mommert (2013). The probability density for each individual target is assumed to follow a lognormal distribution, whose scale parameter is calculated using the upper and lower uncertainties given for the measured geometric albedo. The median geometric albedo of the combined probability density (Fig. 4) of cold classicals is $0.14^{+0.09}_{-0.07}$, of regular hot CKBOs $p_V = 0.085^{+0.084}_{-0.045}$, and of all hot CKBOs including dwarf planets and Haumea family the median is $p_V = 0.10^{+0.16}_{-0.06}$. These medians are compatible with averages obtained from smaller sample

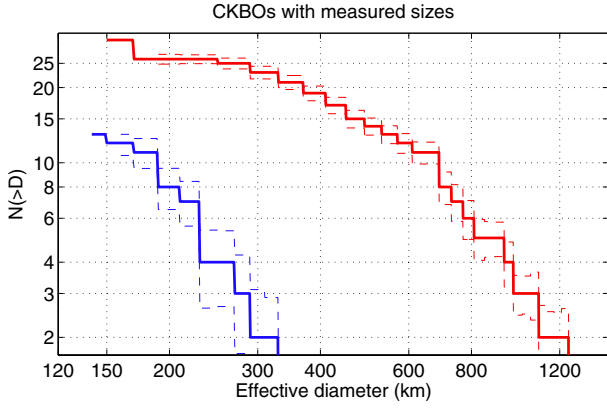


Fig. 3. Cumulative size distribution of all measured dynamically hot (red, upper) classicals from Table 7 and dynamically cold (blue, lower) classicals from Table 6. The dotted lines are uncertainties obtained by a Monte Carlo technique where the sizes of targets are varied using their measured error bars, and a set of size distributions is created. The standard deviation of these size distributions is calculated at each size bin.

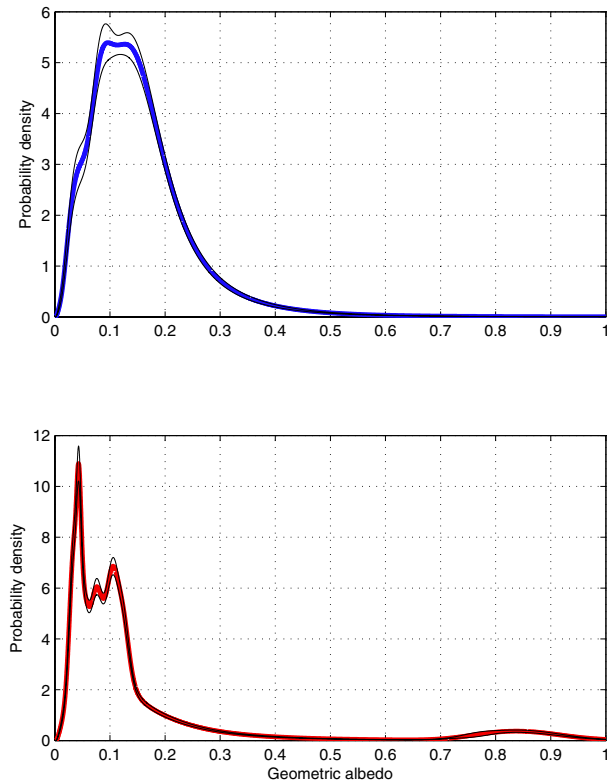


Fig. 4. Distribution of measured geometric albedos: *upper panel* for cold CKBOs and *lower panel* for hot CKBOs. The thin lines show the standard deviation of all probability density distributions, where each of the distributions has been determined with one target excluded, each target having been excluded once.

sizes: 0.17 ± 0.04 for cold CKBOs and 0.11 ± 0.04 for hot CKBOs in Vilenius et al. (2012) but the difference between the dynamically cold and hot sub-samples is smaller than previously reported.

Of the other dynamical classes, the Plutinos have an average albedo of 0.08 ± 0.03 (Mommert et al. 2012), scattered disk objects have 0.112 (Santos-Sanz et al. 2012), detached objects have 0.17 (Santos-Sanz et al. 2012), gray Centaurs have 0.056 (Duffard et al. 2013) and red Centaurs 0.085 (Duffard et al. 2013). Dynamically hot classicals have a similar average albedo

as Plutinos and red Centaurs whereas the average albedo of cold CKBOs is closer to the detached objects.

4.3. Debiased size distributions

The measured size distributions are affected by biases: the radiometric method has a detection limit, and the measured sample is not representative of all those targets which could have been detectable in principle. For the debiasing we use a synthetic model of outer Solar System objects by the Canada-French Ecliptic Plane Survey (CFEPS, Petit et al. 2011), which is based on well-calibrated optical surveys. CFEPS provides H_g magnitudes and orbital parameters of more than 15 000 cold CKBOs and 35 000 hot synthetic CKBOs. We perform a two-stage debiasing of the measured size distribution (see Appendix A for details) and derive slope parameters. We have constructed a model of the detection limit of *Herschel* observations, which depends on objects’ sizes, albedos and distances. This model is used in the first stage of debiasing. In the second stage we debias the size distribution in terms of how the distribution of H_g of the measured targets are related to the H_g distribution of the synthetic sample of those objects, which would have been detectable.

CFEPS has synthetic objects to the limit of $H_g = 8.5$. All cold CKBOs in our measured sample have $H_g < 7.5$ and all hot CKBOs have $H_g < 8.0$. Therefore, these limits are first applied to the CFEPS sample before debiasing the size distributions. Since all of the measured hot CKBOs are in the inner or main classical belts, we exclude the outer CKBOs of CFEPS in the debiasing. Furthermore, we have excluded a few measured targets which are outside the orbital elements space of CFEPS objects, or which are close to the limit of dynamically cold/hot CKBOs, to avoid contamination from one sub-population to the other.

In translating the optical absolute magnitude of simulated CFEPS objects into sizes, a step needed in the debiasing (Appendix A), we use the measured albedo probability densities (Fig. 4) in a statistical way. Our measured dynamically hot CKBOs cover the relevant heliocentric distance range of inner and main classical belt CFEPS objects. While our measured sample of cold CKBOs is limited to $38 < r < 45$ AU we assume that the shape of the albedo distribution applies also to more distant cold CKBOs. Although there is an optical discovery bias preferring high- p_V objects at large distances, the radiometric method has an opposite bias: low- p_V objects are easier to detect at thermal wavelengths than high- p_V objects. Among the radiometrically measured targets we do not find evidence of any significant correlations (see Sect. 4.5) between geometric albedo and orbital elements, heliocentric distance at discovery time nor ecliptic latitude at discovery time.

The debiased size distributions are shown in Fig. 5. Our analysis of cold CKBOs gives a debiased slope of $q = 5.1 \pm 1.1$ in the range of effective diameters of $160 < D < 280$ km. In the measured sample there are seven binaries and three non-binaries in this size range. For dynamically hot CKBOs the slope is $q = 2.3 \pm 0.1$ in the size range $100 < D < 500$ km. The slope is steepening towards the end tail of the size distribution and in the size range $500 < D < 800$ km we obtain a slope parameter of $q = 4.3 \pm 0.9$. When comparing the slopes of the cold and hot sub-populations it should be noted that for the cold subsample we are limited to the largest objects and the maximum size of cold CKBOs is smaller than that of hot CKBOs.

Size distribution is often derived from the LF using simplifying assumptions about common albedo and distance. Fraser et al. (2010) have derived a LF based slope for dynamically cold

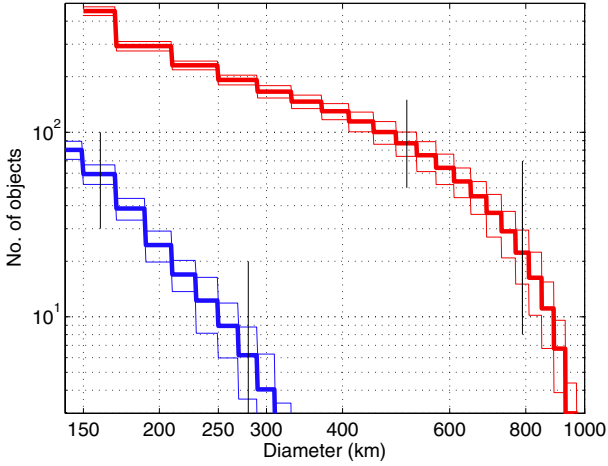


Fig. 5. Debiased size distributions (see text): hot CKBOs (red, upper) and cold CKBOs (blue, lower). The thin red and blue lines are the error bars of each size bin (bin size 20 km for dynamically cold and 40 km for dynamically hot CKBOs). The vertical lines mark the ranges for which slope parameters have been determined.

objects ($i < 5$ deg, $38 < r < 55$ AU): $q = 5.1 \pm 1.1$, which is well compatible with our value from a debiased measured size distribution. For dynamically hot CKBOs Fraser et al. (2010) derived two slopes depending on the distance of objects. For dynamically hot objects with $38 < r < 55$ AU and $i > 5$ deg: $q = 2.8 \pm 1.0$ and for a combined sample of these hot and “close” objects ($30 < r < 38$ AU): $q = 3.0 \pm 0.6$. Both of the LF based results are compatible within the given uncertainties with our estimate of $q = 2.3 \pm 0.1$.

4.4. Beaming factors

The temperature distribution over an airless object affects the observed SED shape. In the NEATM model temperature is adjusted by the beaming factor η as explained in Sect. 3.1. For CKBOs, the PACS bands are close to the thermal peak of the SED whereas MIPS provides also data from the short-wavelength part of the SED. Therefore, in order to determine a reliable estimate for the average beaming factor of classical TNOs we select those solutions which are based on detections with both PACS and MIPS and detected in at least three bands. Furthermore, we require that the MIPS 24 μ m band has been detected because it constrains the overall shape of the SED making inferences based on those results more reliable. There is a large scatter of beaming factors among CKBOs spanning the full range of $0.6 < \eta < 2.6$. There are five cold CKBOs and eight hot CKBOs with floating- η solutions fulfilling the above mentioned criteria. The averages of the two subpopulations do not differ much compared to the standard deviations. The average beaming factor of 13 cold and hot CKBOs is $\eta = 1.45 \pm 0.46$ and the median is 1.29. This average is very close to the previous average based on eight targets: $\eta = 1.47 \pm 0.43$ (Vilenius et al. 2012). The new average η is compatible with the default value of 1.20 ± 0.35 for fixed η fits as well as with averages of other dynamical classes: seven Plutinos have the average $\eta = 1.11^{+0.18}_{-0.19}$ (Mommert et al. 2012) and seven scattered and detached objects have $\eta = 1.14 \pm 0.15$ (Santos-Sanz et al. 2012). Statistically, beaming factors of a large sample of TNOs from all dynamical classes are dependent on heliocentric distance (Lellouch et al. 2013). Therefore, η values are likely to differ due to different distances of the populations in different dynamical classes.

4.5. Correlations

In the sample of measured objects we have checked possible correlations between geometric albedo p_V , diameter D , orbital elements (inclination i , eccentricity e , semimajor axis a , perihelion distance q), beaming factor η , heliocentric distance at discovery time, ecliptic latitude at discovery time, visible spectral slope, as well as $B - V$, $V - R$ and $V - I$ colors. We use a modified form of the Spearman correlation test (Spearman 1904) taking into account asymmetric error bars and small numbers statistics. The details of this method are described in Peixinho et al. (2004) and Santos-Sanz et al. (2012, Appendix B.2). We consider correlation coefficient ρ to show a “strong correlation” when $|\rho| \geq 0.6$ and “moderate correlation” when $0.3 \leq |\rho| < 0.6$. Our correlation method does not show any significant (confidence on the presence of a correlation $> 3\sigma$) correlations between any parameters within the dynamically cold subpopulation with $N = 13$ targets. Similarly, when making the correlation analysis on the CKBOs according to the DES classification ($N = 23$) we do not find any significant correlations.

4.5.1. Diameter and geometric albedo

There is a lack of large objects at small inclinations and of small objects at high inclinations in our measured sample. The latter are subject to discovery biases since many of the surveys have been limited close to the ecliptic plane (H_V and ecliptic latitude at discovery time show a moderate anti-correlation in the sample of all radiometrically measured targets). There is a strong size-inclination correlation when all targets are included (4.4σ), and a moderate correlation if dwarf planets and Haumea family are excluded (3.9σ). The strong correlation within the subsample of hot CKBOs reported by Vilenius et al. (2012) is only moderate with our larger number of targets, and it is no longer significant (2.3 – 2.5σ). Levison & Stern (2001) found the presumable size-inclination trend from the correlation between intrinsic brightness and inclination and showed that their result is unlikely to be caused by biases. When observing with the radiometric techniques, there is a selection bias of targets, which we estimate to have high enough flux density to be detectable. According to Eq. (3) the observed flux is approximately proportional to the projected area and inversely proportional to the square of distance. A statistical study of 85 TNOs and Centaurs, with partially overlapping samples with this work, showed a strong ($\rho = 0.78$, significance $> 8\sigma$) correlation between diameter and instantaneous heliocentric distance (Lellouch et al. 2013). Dynamically hot CKBOs show a moderate correlation between effective diameter and heliocentric distance at discovery time (3.2σ). However, it is not significant when analysed without dwarf planets and Haumea family (the “regular” subsample). A diameter/inclination correlation could appear if there is a correlation between diameter and distance as well as between distance and inclination. Our analysis finds no evidence of a correlation between inclination and heliocentric distance for the whole measured sample ($\rho = 0.20$, significance 1.2σ) or any of the sub-samples. Therefore, we consider the correlation between diameter and inclination reported here not to be caused by a selection bias.

There is a moderate ($\rho \approx -0.5$) anti-correlation between diameter and geometric albedo among the “regular” CKBOs (3.4σ). This correlation disappears when the dwarf planets and Haumea family members are added, or when the “regular” CKBOs is divided into its cold or hot components. Inclination may be a common variable, which correlates both with diameter

Table 8. Density estimates of classical TNO binaries with a known mass.

Target	Adopted ΔV^a (mag)	Mass ^a ($\times 10^{18}$ kg)	Bulk density/literature (g cm ⁻³)	Reference	Bulk density/this work (g cm ⁻³)
Borasisi	0.45	3.433 ± 0.027	$2.1^{+2.6}_{-1.2}$
2001 XR ₂₅₄	0.43	4.055 ± 0.065	$1.4^{+1.3}_{-1.0}$	Vilenius et al. (2012)	$1.00^{+0.96}_{-0.56}$
2001 QY ₂₉₇	0.20	4.105 ± 0.038	$1.4^{+1.2}_{-1.3}$	Vilenius et al. (2012)	$0.92^{+1.30}_{-0.27}$
Sila	0.12^b	10.84 ± 0.22^b	0.73 ± 0.28	Vilenius et al. (2012), (b)	...
Teharonhiawako	0.70	2.445 ± 0.032	$1.14^{+0.87}_{-0.91}$	Vilenius et al. (2012)	$0.60^{+0.36}_{-0.33}$
Altjira	0.23	3.986 ± 0.067	$0.63^{+0.68}_{-0.63}$	Vilenius et al. (2012)	$0.30^{+0.50}_{-0.14}$
2002 UX ₂₅	$\sim 2.7^g$	$\sim 125 \pm 3^g$	0.82 ± 0.11	Brown (2013)	...
Varda	1.45^f	265.1 ± 3.9^f	$1.27^{+0.41}_{-0.44}$
2001 QC ₂₉₈	0.44^f	11.88 ± 0.14^f	$1.14^{+0.34}_{-0.30}$
Quaoar	5.6 ± 0.2^e	$1300\text{--}1400^e$	$2.18^{+0.43}_{-0.36}$	Fornasier et al. (2013)	...
Salacia	2.372 ± 0.060^d	436 ± 11^d	$1.29^{+0.29}_{-0.23}$	Fornasier et al. (2013)	...

Notes. The primary and secondary are assumed to have equal albedos and equal densities.

References. ^(a) Grundy et al. (2011) unless otherwise indicated. ^(b) Grundy et al. (2012). ^(c) Fraser et al. (2012). ^(d) Stansberry et al. (2012). ^(e) Brown & Suer (2007). ^(f) Grundy et al. (in prep.) ^(g) Brown (2013).

and tentatively with albedo as explained in the following. There is a moderate anticorrelation between inclination and albedo among the “regular” CKBOs, although it is not considered significant (2.5σ). This is probably caused mainly by the cold CKBOs ($\rho = -0.51$, 1.8σ , $N = 13$) and less by the “regular” hot CKBOs ($\rho = -0.17$, 0.8σ , $N = 26$). When combining the significant diameter/inclination correlation (3.9σ) with a tentative albedo/inclination correlation this combination may explain the moderate diameter/albedo anti-correlation we observe in our “regular” CKBOs sample. Therefore, we do not confirm the finding of Vilenius et al. (2012) about an anti-correlation between size and albedo within the classical TNOs as it is probably due to a bias. The anti-correlation between size and albedo was not observed in Plutinos (Mommert et al. 2012), which do not show any correlation between size and albedo, nor with scattered/detached-disc objects which show a positive correlation instead (Santos-Sanz et al. 2012).

We find no evidence of other correlations with orbital elements or colors involving size or geometric albedo.

4.5.2. Other correlations

CKBOs are known to have an anti-correlation between surface color/spectral slope and orbital inclination (Trujillo & Brown 2002; Hainaut & Delsanti 2002). In our measured sample a moderate correlation exists for the whole sample (3.2σ) but is not significant for the “regular” CKBOs (2.0σ), which do not include dwarf planets and Haumea family members. We do not find any correlations of the $B - V$, $V - R$ and $V - I$ colors with parameters other than spectral slope.

The apparent H_V vs. i anti-correlation in our target sample mentioned in Sect. 2.1 is moderate and significant for the whole sample (3.9σ) as well as for the hot sub-population (3.1σ), but less significant on the “regular” hot CKBOs sub-sample (2.5σ).

4.6. Binaries

In deriving bulk densities of binary systems, whose effective diameter D has been determined by the radiometric method, we assume that the primary and secondary components i) are spherical, and ii) have equal albedos. A known brightness

difference between the two components ΔV can be written as $k = 10^{-0.2\Delta V} = \frac{D_2}{D_1} / l$, where D_1 and D_2 are the diameters of the primary and the secondary component and $l = \sqrt{p_{V1}/p_{V2}}$ (components’ geometric albedos p_{V1} and p_{V2}). The radiometric (area-equivalent) effective diameter of the system is $D^2 = D_1^2 + D_2^2$

and the “volumetric diameter” is $D_{Vol} = \frac{(1+(kl)^3)^{1/3}}{\sqrt{1+(kl)^2}} D$, which is

then used in calculating mass densities: $\frac{6m}{\pi D_{Vol}^3}$ with the usual assumption that l equals unity. The new radiometric mass density estimates of Borasisi, Varda and 2001 QC₂₉₈, and updated (see Sect. 3.3) densities of Teharonhiawako, Altjira, 2001 XR₂₅₄, and 2001 QY₂₉₇ are given in Table 8 and shown in Fig. 6. When ΔV is small, the density estimate does not change to significantly higher densities by changing the assumed ratio of geometric albedos unless the albedo contrast between the primary and the secondary was extreme. The sizes of the binary components (Table 9) for <400 km objects are not significantly different from each other. If we make the assumption that $D_1 = D_2$ and determine densities and relative albedos we get densities close to those in Table 8 for the <400 km objects and albedo ratios of 1.1–1.9.

The new density estimates of four targets are lower than those determined by Vilenius et al. (2012). The reason for the large change in density estimates is the *Spitzer* flux update of three of the targets and a different technique of treating upper limits in the cases of Teharonhiawako, Altjira and 2001 XR₂₅₄. Our assumption that the objects are spherical may give too low density estimates for elongated objects. The relatively large light curve variation of 2001 QY₂₉₇ of ~ 0.5 mag (Thirouin et al. 2012) suggests a shape effect whereas the light curve amplitude of Altjira is not well known and is probably < 0.3 mag (Sheppard 2007). Lower density limits can be derived based on rotational properties but the period is not known for these two targets. Densities lower than that of water ice have been reported for TNOs in the literature (e.g. Stansberry et al. 2006). The density of a sphere of pure water ice under self-compression is slightly less than 1 g cm⁻³ and porosity at micro and macro scales reduces the bulk density. Another common low-density ice is methane with a density of ~ 0.5 g cm⁻³. A statistical study of TNOs from all dynamical classes shows that their surfaces are

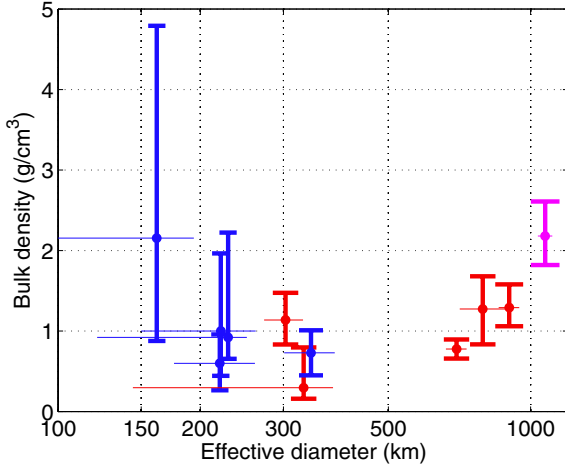


Fig. 6. Bulk densities of classical TNOs. Blue marks cold CKBOs, red hot CKBOs, and magenta dwarf planet Quaoar.

Table 9. Sizes of primary and secondary components assuming equal albedos and spherical shapes of both components.

Target	Primary's size D_1 (km)	Secondary's size D_2 (km)
Borasisi	126^{+25}_{-51}	103^{+20}_{-42}
2001 XR ₂₅₄	171^{+32}_{-55}	140^{+26}_{-45}
2001 QY ₂₉₇	169^{+16}_{-80}	154^{+15}_{-73}
Sila	249^{+30}_{-31}	236^{+28}_{-29}
Teharonhiawako	178^{+33}_{-36}	129^{+24}_{-26}
Altjira	246^{+38}_{-139}	221^{+34}_{-125}
2002 UX ₂₅	670 ± 34	193 ± 10
Varda	705^{+81}_{-75}	361^{+42}_{-38}
2001 QC ₂₉₈	235^{+21}_{-23}	192^{+17}_{-19}
Quaoar ^a	1070 ± 38	81 ± 11
Salacia	829 ± 30	278 ± 10

Notes. ^(a) Quaoar's D_1 and D_2 from Fornasier et al. (2013).

very porous (Lellouch et al. 2013) indicating that the material on the surface has a low density. However, the low bulk densities of Altjira and Teharonhiawako reported here require significant porosities of 40–70% for material densities of 0.5–1.0 g cm⁻³. This would indicate the presence of macroporosity, i.e. that the objects are rubble piles of icy pieces.

5. Conclusions

The *Herschel* mission and the cold phase of *Spitzer* have ended. The next space mission capable of far-infrared observations of CKBOs will be in the next decade. Occultations can provide very few new size estimates annually, and the capabilities of the *Atacama Large Millimeter Array* (ALMA) to significantly extend the sample of measured sizes of TNOs already presented may be limited by its sensitivity⁵.

In this work we have analysed 18 classical TNOs to determine their sizes and albedos using the radiometric technique and data from *Herschel* and/or *Spitzer*. We have also re-analysed previously published targets, part of them with updated flux

⁵ Moullet et al. (2011) estimated 500 TNOs to be detectable by ALMA, based on assumed albedos commonly used at that time.

densities. The number of CKBOs with size/albedo solutions in literature and this work is increased to 44 targets and additionally three targets have a diameter upper limit and albedo lower limit. We have determined the mass density of three CKBOs and updated four previous density estimates. Our main conclusions are:

1. The dynamically cold CKBOs have higher geometric albedo (0.14) than the dynamically hot CKBOs (0.085 without dwarf planets and Haumea family, 0.10 including them), although the difference is not as great as reported by Vilenius et al. (2012).
2. We do not confirm the general finding of Vilenius et al. (2012) that there is an anti-correlation between diameter and albedo among all measured CKBOs as that analysis was based on a smaller number of targets.
3. The cumulative size distributions of cold and hot CKBOs have been inferred using a two-stage debiasing procedure. The characteristic size of cold CKBOs is smaller, which is compatible with the hypothesis that the cold sub-population may have formed at a larger heliocentric distance than the hot sub-population. The cumulative size distribution's slope parameters of hot CKBOs in the diameter range $100 < D < 500$ km is $q = 2.3 \pm 0.1$. Dynamically cold CKBOs have an inferred slope of $q = 5.1 \pm 1.1$ in the range $160 < D < 280$.
4. The bulk density of Borasisi is $2.1^{+0.58}_{-0.59}$ g cm⁻³, which is higher (but within error bars) than other CKBOs of similar size. The bulk densities of Varda and 2001 QC₂₉₈ are $1.25^{+0.40}_{-0.43}$ g cm⁻³ and $1.14^{+0.34}_{-0.30}$ g cm⁻³, respectively. Our re-analysis of four targets ($D < 400$ km) has decreased their density estimates and they are mostly between 0.5 and 1 g cm⁻³ implying high macroporosity.

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Appendix A: Debiasing of size distributions

A.1. Targets

In the debiasing we use those measured targets which are compatible with the orbital element space of CFEPS synthetic objects. Due to different classification used in our observing program, one cold CKBO (2001 QB₂₉₈) and two hot CKBOs from the inner belt (2003 UR₂₉₂ and 2002 XW₉₃) have been excluded from the debiasing. To prevent possible contamination between cold/hot sub-populations we have also excluded four hot CKBOs, whose inclinations are not far above the $i = 4.5$ deg cut-off limit (Quaoar, Altjira, 2001 QD₂₉₈ and 2000 OK₆₇). Three measured targets have their semi-major axis within the gap in CFEPS objects reserved for the 2:1 mean motion resonance with Neptune. To our knowledge these three targets are not in resonance, therefore they are included. In total, 25 hot

CKBOs from the inner and main belts are included in the debiasing as well as 12 cold CKBOs.

A.2. Magnitude conversion

CFEPS uses H_g values for their synthetic objects. If $V - R$ color is known then H_g can be converted into H_V . We use the average color of cold classicals: $V - R = 0.63 \pm 0.09$ ($N = 49$) and hot classicals: $V - R = 0.51 \pm 0.14$ ($N = 43$) from the MBOSS-2 data base. Lupton (2005) conversion formulas and conversion uncertainties are (see Footnote 2 for reference):

$$V = g - 0.5784 * (g - r) - 0.0038, \quad \sigma = 0.0054 \quad (\text{A.1})$$

$$R = r - 0.1837 * (g - r) - 0.0971, \quad \sigma = 0.0106. \quad (\text{A.2})$$

Using the average $V - R$ color we get

$$\text{cold: } V = g - 0.52, \quad \sigma = 0.09 \quad (\text{A.3})$$

$$\text{hot: } V = g - 0.40, \quad \sigma = 0.14. \quad (\text{A.4})$$

A.3. PACS detection limit

Many of the measured cold CKBOs were very faint, the flux densities being <5.5 mJy. Contrary, the hot CKBOs were brighter and only one out of 29 observed by PACS was a non-detection. The PACS observations were executed in a standardized way using similar observation durations and parameters. While the repetition factor in “TNOs are Cool” was designed separately for each target, in the range $\text{REP} = 1, \dots, 6$, for the cold CKBOs the most common choice was $\text{REP} = 5$ (total 2-visit duration at $70 \mu\text{m}$ or $100 \mu\text{m}$ band 94 min). Of the cold CKBOs only Sila, Teharonhiawako, 2001 XR254 and 2002 GV31 had shorter durations with $\text{REP} = 3$ or $\text{REP} = 4$. 2002 GV31 was a non-detection, the other three are large ($D > 200$ km) and relatively bright ($H_V < 6.1$). The lowest flux densities with 2-band detections in our sample are at the level of 1.7 mJy at $100 \mu\text{m}$. According to NEATM (in the following we assume $\eta = 1.2$), the peak flux density of 1.7 mJy would be emitted by an object at $r_h = \Delta = 40$ AU if its diameter is $D_{\text{ref}} = 167.5$ km and geometric albedo $p_{V,\text{ref}} = 0.04$. In the following, we make the simplifying assumption that during our observations $r_h \approx \Delta$. The peak flux density remains constant (but with a small shift in wavelength position) if a target is at different distance and its size with respect to the reference size is scaled according to the distance change. If s is a scale factor in the distance then the diameter scales as $s^{1.75}$, i.e. at a distance of $40s$ AU the object’s size should be $s^{1.75}D_{\text{ref}}$ to maintain the same peak flux density. In the above, albedo was kept constant. The effect of albedo depends on the phase integral because we have for the Bond albedo $A: A = p_V q(p_V)$, where $q(p_V) = 0.336p_V + 0.479$ (Brucker et al. 2009). Other values being constant, if geometric albedo changes then the diameter has to be scaled in order to maintain the constant maximum flux density. If t is the scaling factor of geometric albedo, then diameter scales as

$$\left(\frac{1 - p_{V,\text{ref}} q(p_{V,\text{ref}})}{1 - t p_{V,\text{ref}} q(t p_{V,\text{ref}})} \right)^{\frac{1}{1.75}}. \quad (\text{A.5})$$

A.3.1. Debiasing stage 1

First we debias with respect to the radiometric detection limit (Sect. A.3). Diameters are assigned to each CFEPs CKBO in a random way using the geometric albedo probability densities

derived from measured targets (see Sect. 4.2). Then, size distributions of synthetic objects are calculated. The debiasing factors of stage (1) are obtained by dividing the numbers of CFEPs CKBOs in the cumulative size distribution bins by the numbers of potentially detectable CFEPs objects in the same size bins. For each synthetic object we have the distance, randomly selected albedo, and the diameter calculated using that albedo and H_g . Each object is checked against the detection limit derived in Sect. A.3. The uncertainties are calculated as the 1σ uncertainties of the calculated ratio, where the two distributions have been produced 500 times with randomly assigned albedos to the synthetic objects.

The debiasing factors are applied to the size distributions of measured targets. The numbers of targets in the measured size distribution bins are multiplied by the corresponding stage (1) debiasing factors.

A.3.2. Debiasing stage 2

In stage (2) we are debiasing the selection effects of our target sample compared to the sample which could have been detected with PACS. The selection effects of the measured target sample include the discovery bias of known TNOs. This debiasing is done using optical absolute magnitudes H_g of both the synthetic CFEPs objects and the measured targets (steps 1–3 below) and translated into debiasing factors for each bin in the size distribution (steps 4–6). The stage (2) debiasing factors are calculated in the following way:

1. Create cumulative H_g distribution of both the measured sample and the potentially detectable CFEPs synthetic objects. The latter is an average of a large number of sets of potentially detectable objects, where the detection limit calculation is using randomly assigned albedos (from the probability density distribution similar to those in Fig. 4) for each synthetic object.
2. Calculate the ratio of numbers of objects in each H_g bin of the potentially detectable distribution and the measured distribution. Normalize these factors so that the smallest factor is equal to one.
3. Multiply the measured H_g distribution by the factors from step 2.
4. Generate sizes for objects in each H_g bin after step 3 in a statistical way using the measured albedo probability density distribution. The relative differences in the numbers of objects in each H_g bin of this step is given by the relative differences of numbers of objects in the H_g distribution of step 3.
5. Calculate a size distribution using all the objects generated in step 4.
6. Calculate debiasing factors from step 5 and the measured size distribution. Normalize these factors so that the largest target has a factor equal to one. In the dynamically hot sub-population Haumea and Makemake, two targets outside the CFEPs H_g range, were not included in calculating debiasing factors.

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