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1

## 2 **Supplementary Information for**

### 3 **Scale-free movement patterns in termites emerge from social interactions and preferential** 4 **attachments**

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#### 9 **This PDF file includes:**

- 10     Supplementary text
- 11     Figs. S1 to S14
- 12     Legends for Movies S1 to S2

#### 13 **Other supplementary materials for this manuscript include the following:**

- 14     Movies S1 to S2

15 **Supporting Information Text**

16 Raw data will be made available at Harvard Dataverse (<https://dataverse.harvard.edu/>).

17 **Social interactions and collective behaviours**

18 As the density of the arena is increased, termite workers tend to cluster tightly. Under these conditions individuals effectively  
19 decrease their moving speed in order to engage in social interactions so that the probability of truncating their otherwise free  
20 trajectories is increased as well. This situation is, however, highly dynamic as cluster of different sizes persistently form and  
21 disintegrate afterwards. Individuals in the border of a cluster may detach from it but individuals in the center, albeit not  
22 often, would also spontaneously walk slowly and find their way out from the cluster to explore the arena. Individuals freely  
23 walking far from the cluster may come across the cluster in its way and may attach to it or not, preferentially (see the following  
24 [VIDEO](#) | 5:03 min, as an example).

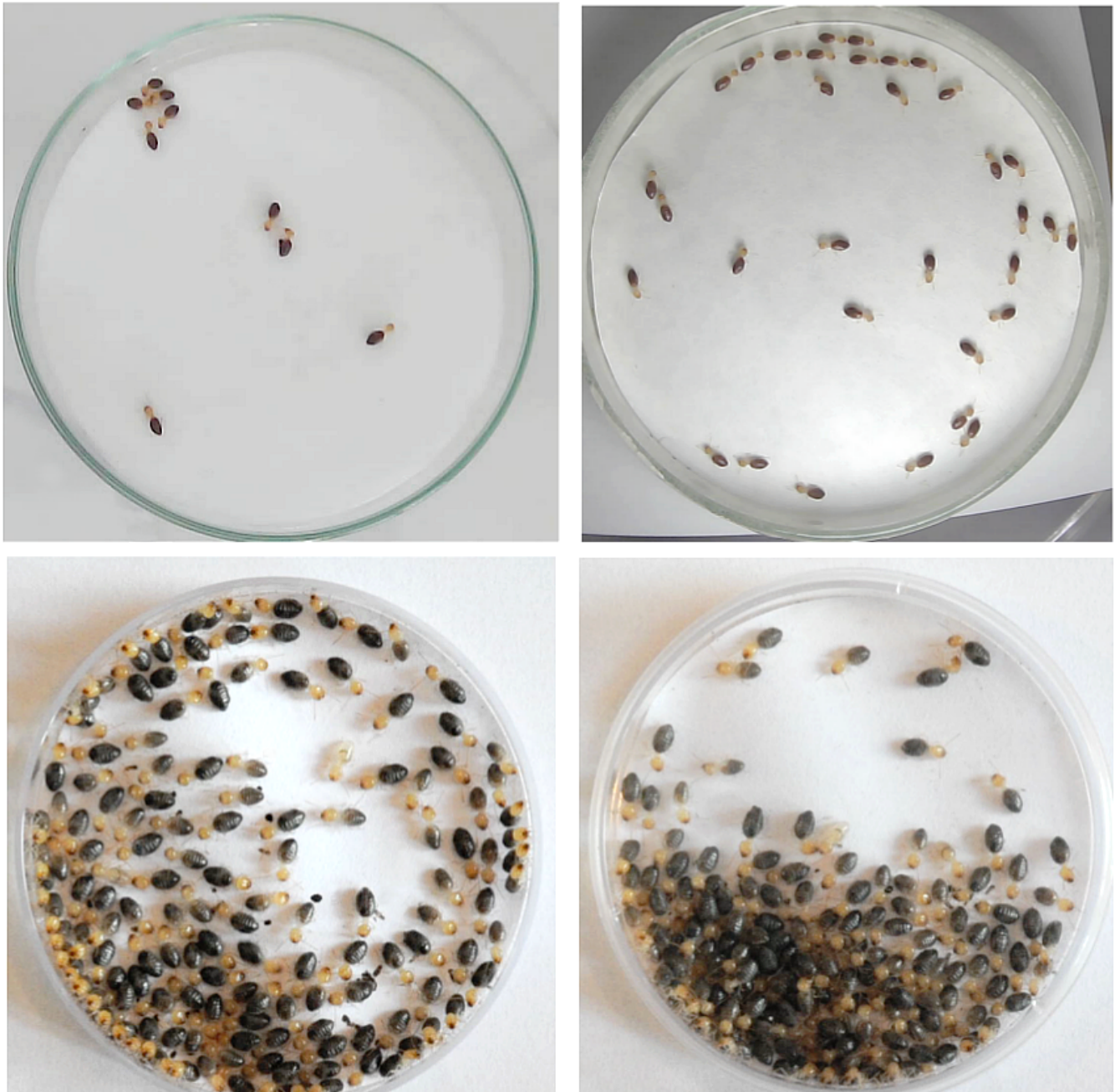


Fig. S1. Examples of termite groups of different sizes forming as the density is increased. Notice also separate individuals wandering around while exploring a Petri dish of diameter 53 mm.

25 Social trapping –or social jamming– may well be a term to describe this process of attaching and detaching from a cluster,  
26 since it is modulated by social interactions. Social trapping induces waiting times while the individuals stands still (these  
27 waiting times are known to be power law distributed [1]). It is also a factor to induce the shortening of the exploration steps  
28 and so it is the collective mechanism that induce a statistical distribution of steps lengths described by power laws, as described  
29 in the text. A graphical evidence of the emergence of Lévy trajectories patterns can be seen in the examples depicted in  
30 Figure S2. An extra observational experiment was performed where around 400 workers were located on a large rectangular  
31 arena (60x40cm). In this experiment, all individuals were initially located at the center of the container and were allowed  
32 to move from there. Initially they tend to move away until reaching the edges, after an initial transient time, the arena was  
33 characterized by a heterogeneity in the density and size of social clusters and a number of moving individuals hopping among  
34 them when detaching and re-attaching. No large clusters were observed but multiple small clusters, this suggests strongly that  
35 individuals attach preferentially and do not interact all-against-all, simultaneously (see the following [VIDEO](#) 20:00 min, as an  
36 example)

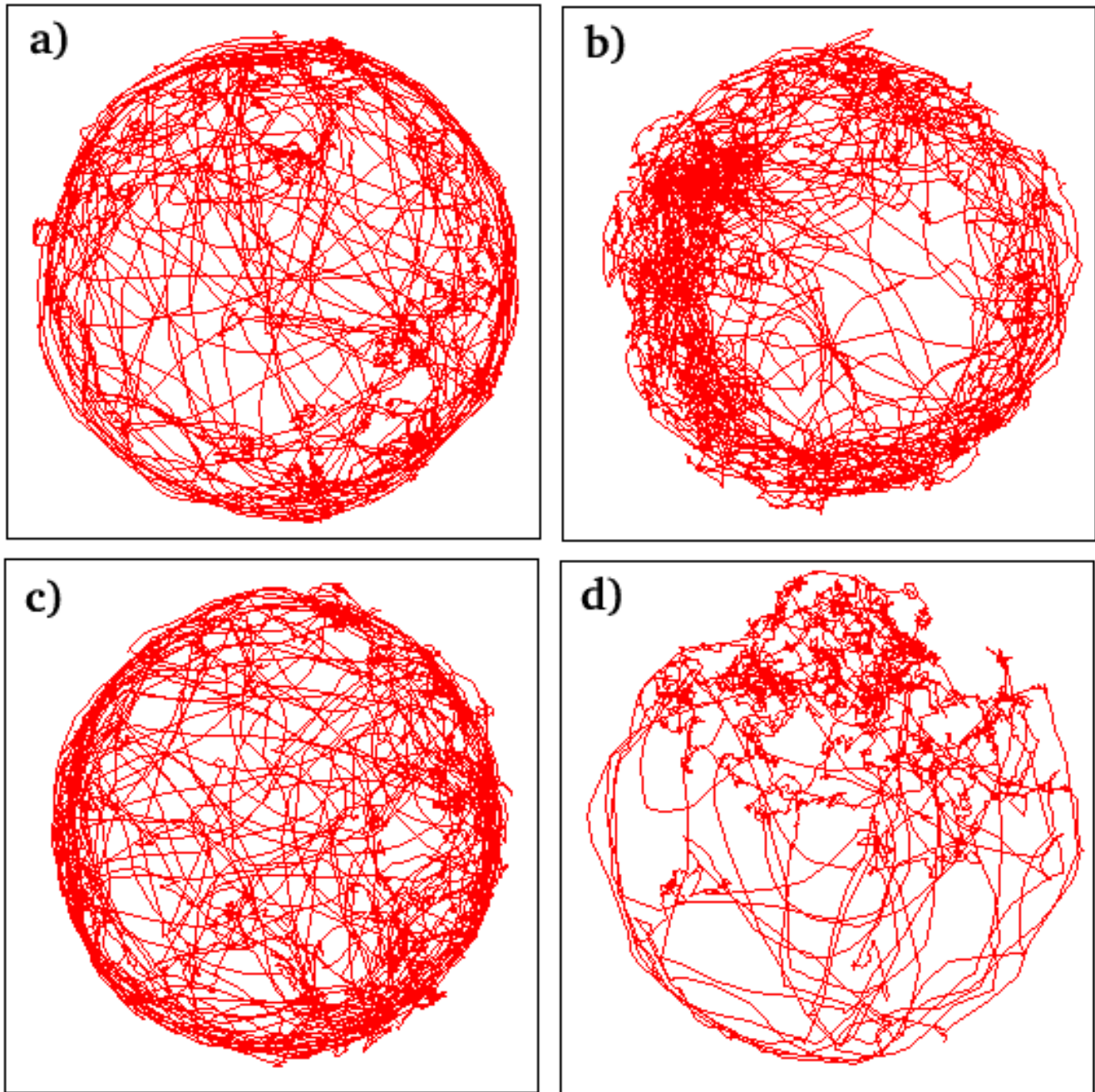
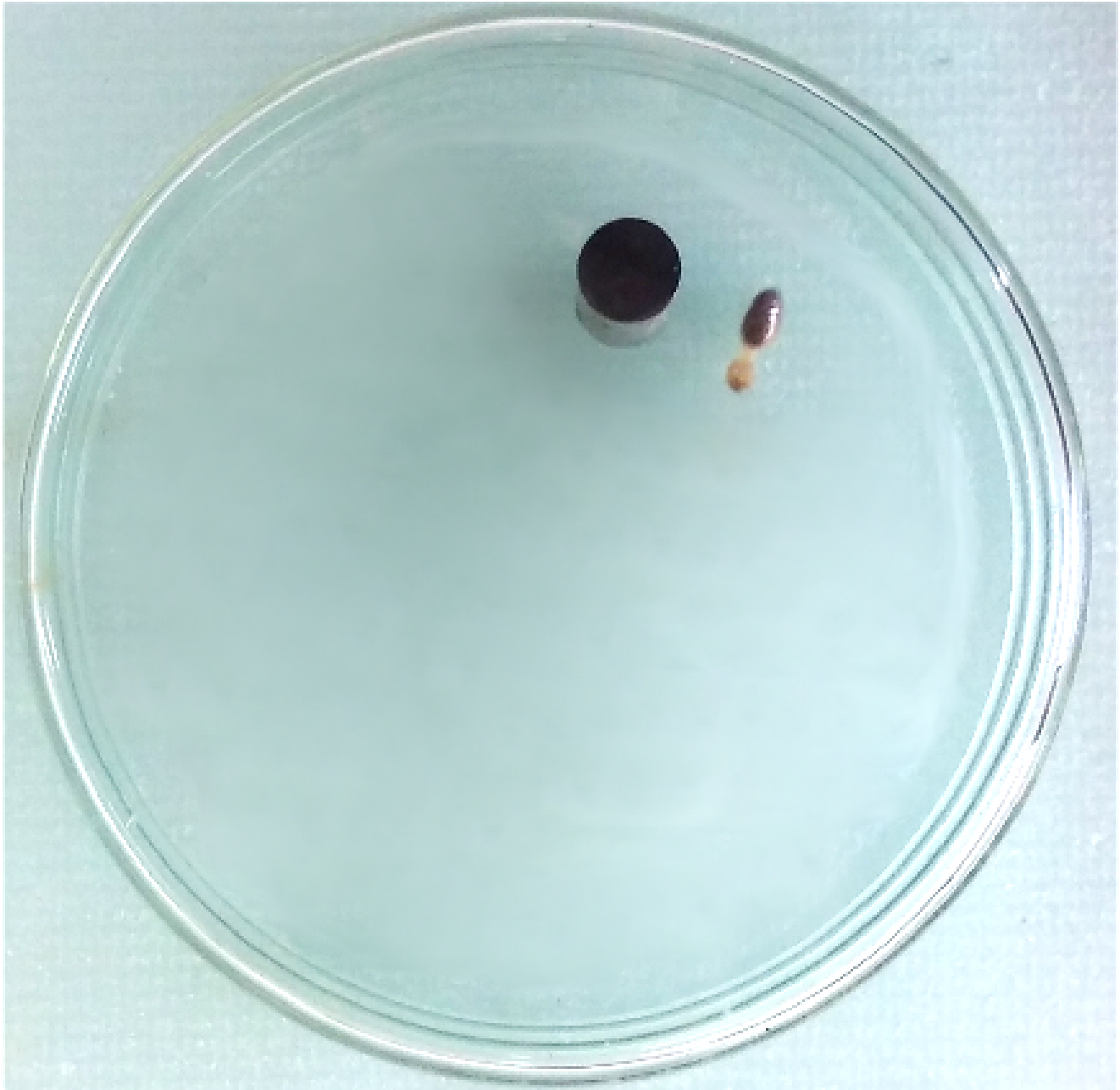


Fig. S2. Visual emergence of Lévy trajectories as the density of workers in the container arena is increased. Individuals wander around while exploring the Petri dish of diameter 53 mm. Notice that in the low density situation (a), the worker trajectory is mostly ballistic where large steps dominate. In (d) the focal individual have its trajectories truncated when engaging in social interactions with another individuals. Group sizes are (a) 12, (b) 15, (c) 18 and (d) 29 individuals in a 53 mm Petri dish.

### 37 Motion with inert passive obstacles

38 In order to test if the emergence of Levy walks could be due to non social mechanical stimulation rather than social interactions,  
 39 a null experiment was designed where inert obstacles were introduced in the arena, as shown in Fig S3, in a range of densities  
 40 and different spatial configurations. Only one termite was introduced and tracked, no social interactions are present but only  
 41 space restrictions due to the obstacles.

42 Sandblasted glass arenas with an upside down 53mm diameter Petri dish as cover were used and 1, 10, 13, 16 and 29  
 43 obstacles were introduced glued into the arenas. Each of these obstacles is a cylinder made of steel with 9.3 mm height and  
 44 cross-section area equals to  $19.59\text{mm}^2$ , close to the mean area occupied by a termite, estimated as  $18.53\text{mm}^2$  (antennae and  
 45 “legs” considered). The steel was chosen as it has a smooth surface, so the termite was not able to climb it, and it is chemically

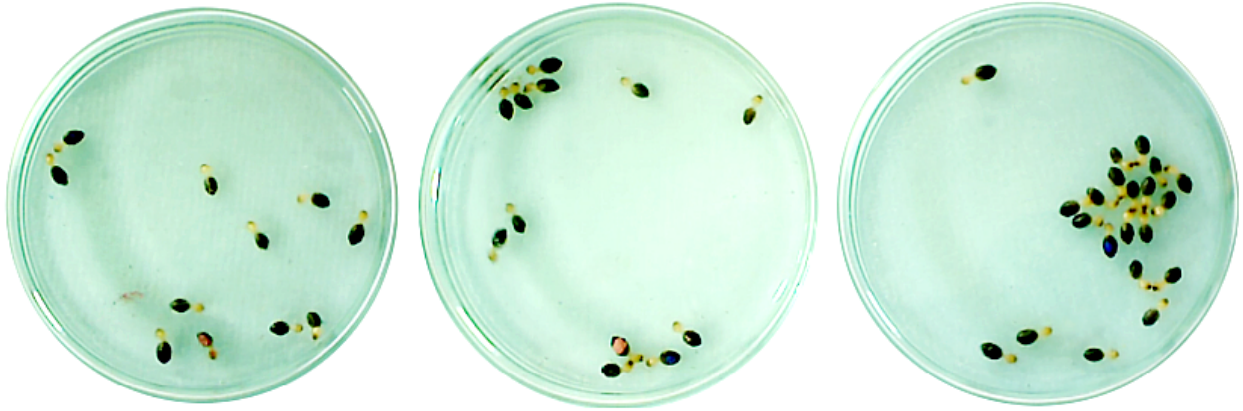


**Fig. S3.** One individual can be seen while exploring an arena with metal poles on it as obstacles in order to simulate the mechanical presence of other individuals. Arena diameter is 53 mm and the pole diameter is the same average length of an adult termite.

46 inert as not having smell that could attract (or repel) the termites. The height of the obstacles was chosen so they have about  
47 the same height as the Petri dish. If they were smaller, the termite could be able to climb it. The identical obstacles were  
48 glued following three different spatial configurations and a range of densities, as explained below.  
49

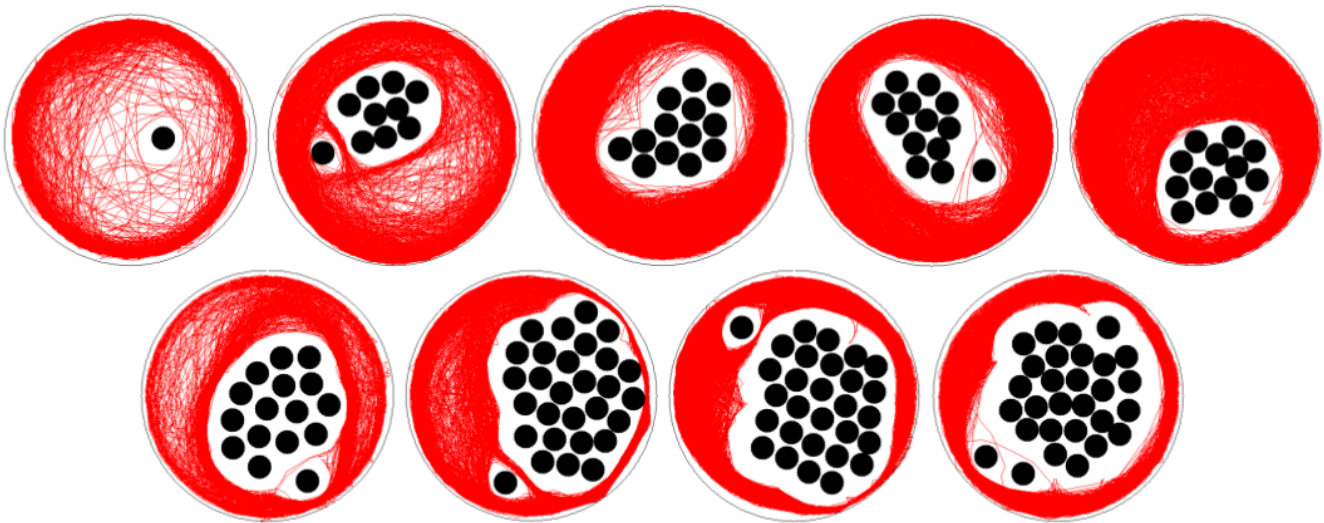
50 **Clustering configuration experiment.** As a way to represent the space that would be occupied by the inert obstacles, a few  
51 experiments were performed with confined termites. In these experiments, termites were free to walk in the arenas and pictures  
52 of the typical pattern of the configuration of them were taken (Fig. S4). Inspired by these pictures, the obstacles were glued in  
53 the positions indicated by the black dots in Fig. S5. This configuration is referred to as a “clustering pattern”.

54 The arenas were prepared with the obstacles forming asymmetrical aggregates with different sizes, and small space between  
55 each obstacle. In some arenas, one or two obstacles were put apart from the cluster, again to make the configuration of the  
56 obstacles as similar as possible to real termite clustering configurations. In all cases of this configuration, the clusters did not



**Fig. S4.** Pictures of typical spatial distribution of confined termites forming groups, which motivated the clustering configuration of the obstacles experiment. At the left, there were no evident clusters and social interactions occurred in pairs mostly (11 individuals). At the center, 12 individuals formed small clusters, for example four individuals clustered at the top of the arena. At the right, 21 individuals in the container, exhibited few free walking individuals but also a large size social cluster.

57 touch the arena's walls, so the termite could also follow a large unobstructed path close to the arena border.



**Fig. S5.** Termite trajectories (red) for 1, 10, 13, 16 and 29 obstacles, placed following the clustering configuration. The black circles represent the real position and size of the obstacles. Notice that even that there was a fair amount of space between the obstacles, the individuals mostly avoided entering the clusters.

58 Examples of the arenas used in this clustering configuration experiment are depicted In Fig. S5, together with the trajectories  
 59 of the termite (red) in each one of them. Black circles represent the real position (and size) of the obstacles. As the borders of  
 60 the arena were unobstructed, individual workers walked close to the borders of the arena, apparently following this pattern  
 61 most of the time. The free paths between the obstacles were rarely explored and, as expected, the termite largely ignored the  
 62 obstacles spending little or no time trying to interact with them.

63  
 64 **Obstacles distributed homogeneously.** Obstacles placed homogeneously were explored as an alternative spatial configuration.  
 65 As before, the borders of the arena were kept free of obstacles. However, in this configuration there are some wide paths  
 66 between the obstacles, so it is expected that this can influence the walking patterns of the termite. Examples of termite  
 67 trajectories are depicted in Figure S6 where termite trajectories in each arena, with 1, 10, 13, 16 and 29 obstacles, are depicted.  
 68 As before, termite walked most of the time close to the arena border. It was observed that, until 16 obstacles, termites walk  
 69 often between the obstacles, but beyond this number and particularly with 29 obstacles, inner incursions are scarce and termites  
 70 walked almost entirely at the border of the arena.

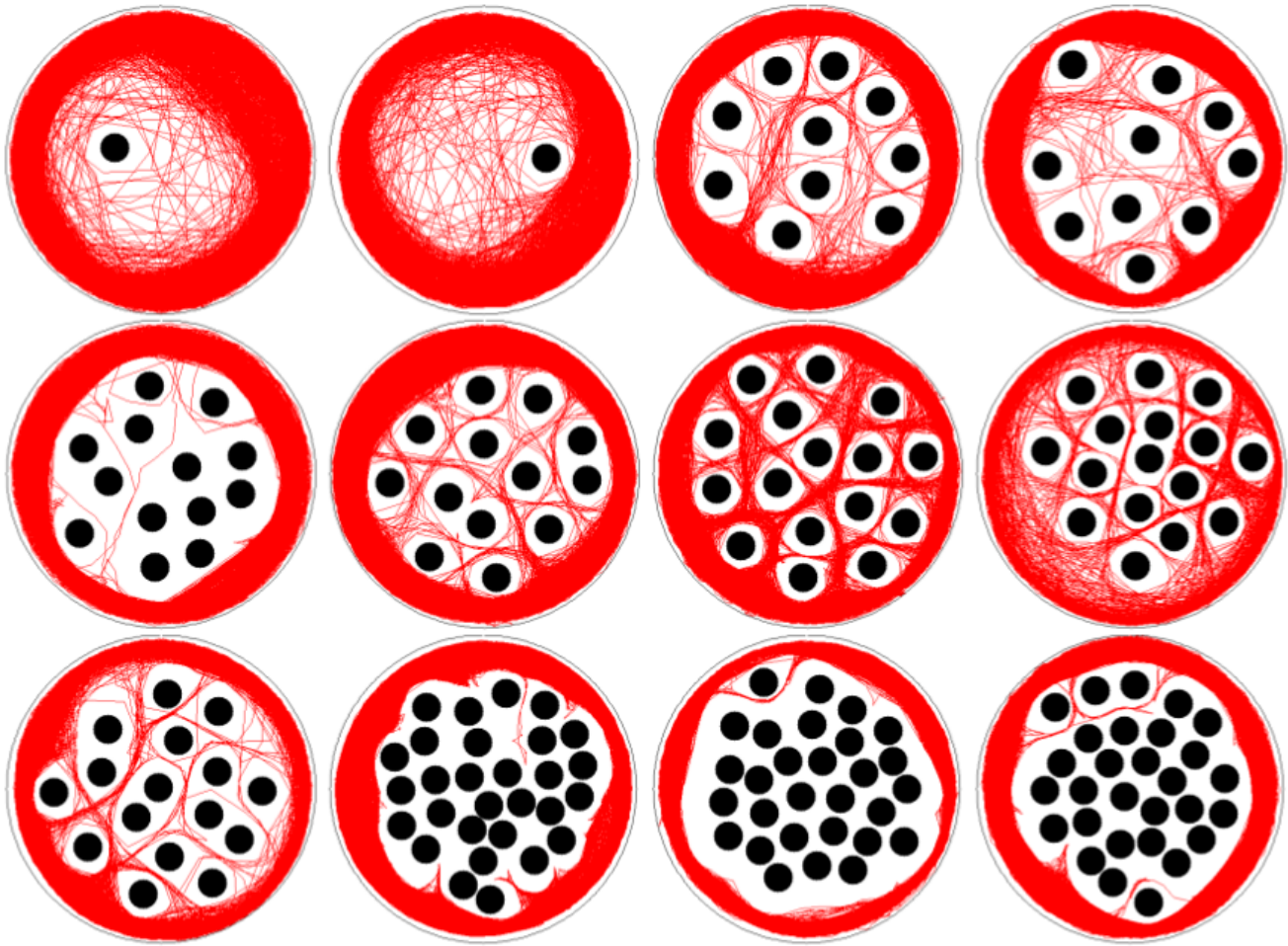


Fig. S6. Termite trajectories (red) are depicted for 1, 10, 13, 16 and 29 obstacles, placed in a random configuration. The black circles represent the real position and size of the obstacles.

71 **Obstacles forming barriers at the border.** Observations indicate that single termites walk mostly following the borders of the  
 72 arena. As a way to modify this persistent behaviour, in our third spatial configuration experiment, the obstacles were placed  
 73 forming barriers in radial directions. Here, the obstacles were glued close to the borders of the arena, as can be see in Figure  
 74 S7 where the termite trajectory is represented in red and the black dots are the obstacles, as before. For this configuration, an  
 75 atypical behaviour was observed. Most of the experiments failed, since the termite was very persistent trying to push or climb  
 76 the obstacles. Eventually, the termites fell upside down and were unable to walk anymore. We succeed in registering only  
 77 three cases where the termite actually walked along the container. The two first cases, where just one obstacle was put in the  
 78 arena, had distinct outcomes. In the first case, the termite follows his trial most of the time, and it explored only a fraction of  
 79 the available space. In the second case, almost all the arena was explored. One should mention that there was no significant  
 80 difference between both experimental conditions (room temperature, luminosity, etc). In the last case, the termite did not  
 81 engaged in trying to push away the obstacles and an intricate pattern resulted.

82 As a conclusion, if space restriction were to induce Lévy-like movements due to trajectory truncation one should identify  
 83 Lévy walks as the density of obstacles increased. However, Lévy walks were not evident in these experiments, independently of  
 84 the configuration of the obstacles, as explained in the main text.



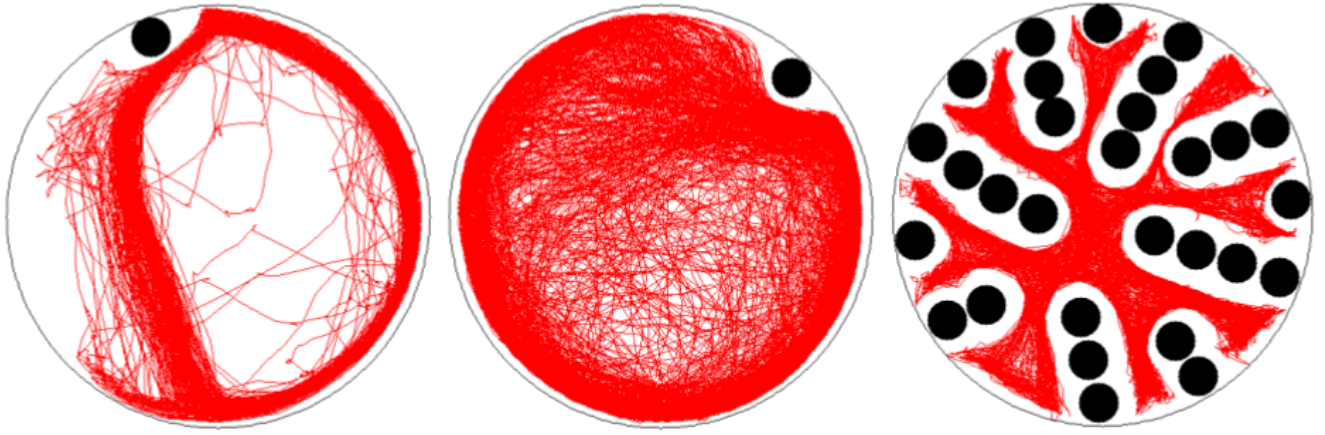


Fig. S7. Termite trajectories (red) for 1 and 29 obstacles, placed in the barrier configuration. The black circles represent the real position and size of the obstacles.

### 85 An agent based model for annular motion

86 Our agent-based model was inspired in the walking patterns of termite workers while freely exploring arenas formed by a bond  
 87 paper of size A0. Figure S8 shows a typical trajectory registered with four thousand steps obtained from a termite walk after  
 88 about 140 seconds of video recording. The arrow indicates the start point of the trajectory. It is easy to see that the termite  
 89 follows a trajectory resembling a correlated random walk where a new step is in a direction very close to that of the preceding  
 90 one and few cases with a large deviation (see three cases indicated by the red open circles in figure S8).

91 Figure S9 shows the typical distributions obtained for the step size and turn angles for a trajectory of a free termite walk.  
 92 Notice that, the step length distribution is well fitted by a normal function. The mean step value is  $\bar{\delta} = 1.1\text{mm}$  and the  
 93 standard deviation  $\sigma = 0.4\text{mm}$ . Notice as well, that for angles around zero we observed a good exponential fit although, for  
 94 values of the turning angle above a value close to  $\pi/2$  a deviation is observed. Above this value, an uniform value to the  
 95 distribution is observed. In fact, the solid line in the figure S9 is a fit to the termite data using

$$96 \quad F(\theta) = p_{\theta} + \frac{1}{\sigma_{\theta}\sqrt{2\pi}} \exp\left(-\frac{\theta^2}{2\sigma_{\theta}^2}\right) \quad [1]$$

97 with  $p_{\theta} = 0.01$  and  $\sigma_{\theta} = 0.4$ .

98 For simplicity, modeled termites are represented by circles of radius  $a$ . Termite can stay in two states: active or inactive.  
 99 An active termite becomes inactive with a probability  $p_w$  and stays inactive by a time interval  $\tau$  (waiting time) or with  
 100 complementary probability  $(1 - p_w)$  it tries to move. The waiting time is a random variable with a distribution that decays as  
 101 a power-law with slope  $\gamma$  [1].

102 The walk of an active termite is described by a persistent random walk, in which the position of the  $i$ th termite at  $(n + 1)$ th  
 103 step is given by

$$104 \quad \vec{r}_i^{n+1} = \vec{r}_i^n + \vec{d}r_i^{n+1}, \quad [2]$$

105 where  $\vec{d}r_i^{n+1}$ , the  $(n + 1)$ th step, is given by

$$106 \quad \vec{d}r_i^{n+1} = \delta \cos(\theta_i^n + \eta_i^{n+1})\hat{i} + \delta \sin(\theta_i^n + \eta_i^{n+1})\hat{j} \quad [3]$$

107 here  $\delta$  is a random step size chosen from a Gaussian distribution,  $\theta_i^n$  is the direction of the  $(n)$ th step and  $\eta_i^{n+1}$  is a random  
 108 perturbation on the direction of the preceding step chosen  $\in (-\pi, \pi)$  with probability  $p_{\theta}$  according to a uniform distribution  
 109 and with a complementary probability according to a Gaussian distribution. The figure S10 shows schematically a few steps of  
 110 a walk. Notice that the trajectory becomes ballistic if the variance and  $p_{\theta} \rightarrow 0$  or random if it  $\rightarrow \infty$  and  $p_{\theta} \rightarrow 1$ .

111 The model evolution rules are as follows.

112 *i)* The waiting time of all inactive termite is updated (subtracted by  $dt = 1/N$ ) and if it becomes less than zero the  
 113 termite is activated.

114 *ii)* An active individual  $i$  is randomly selected. With probability  $p_w$  it becomes inactive and, with the complementary  
 115 probability, it tries to perform a step according to the equation (2).

116 – Once in the AB model overlaps are forbidden, when the individual  $i$  met another  $j$  the walk is interrupted.

117 – And with a probability  $p_{crowd}$  both individuals become inactive with their waiting times  $\tau_i$  and  $\tau_j$  randomly obtained.

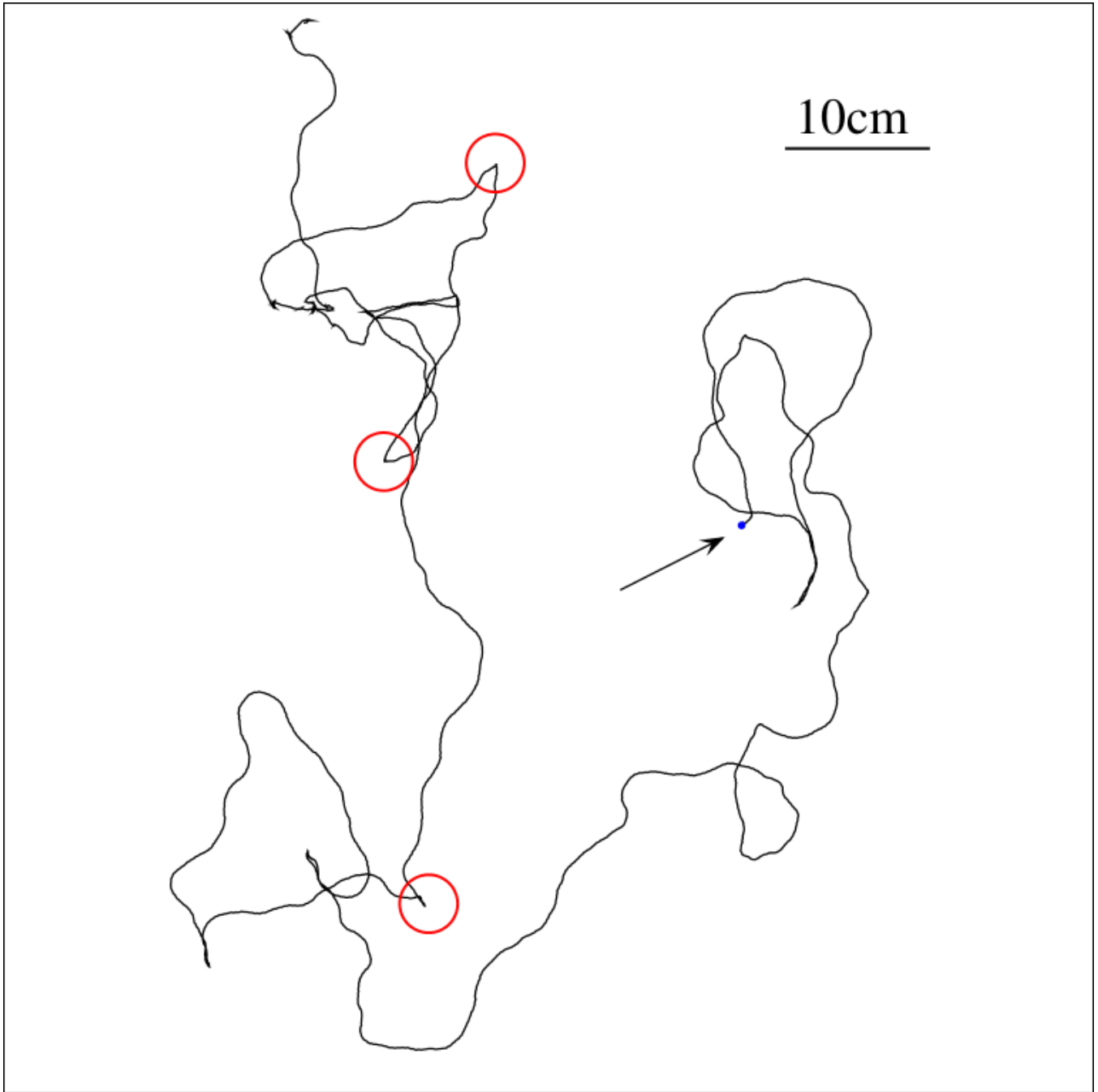


Fig. S8. A typical trajectory with four thousands frames on a free arena obtained after 140s. The arrow indicates the start point of the trajectory (blue circle). Three large deviations in the step direction are highlighted by open circles in red.

118 *iii)* The time is updated ( $t = t + dt$ ), we return to the rule  $i$  and implement it iteratively.

119 The figure S10 shows a trajectory of one individual obtained on a free arena after four thousand steps. The trajectory is very  
 120 similar to the termite in figure S8. The parameters used in the simulation were  $\bar{\delta} = 1$ ,  $\sigma = 0.4$ ,  $p_w = 0$ ,  $p_\theta = 10^{-2}$  and  $\sigma_\theta = 0.4$ .

121 **Confined termites in an annulus configuration.** The simulations are performed in a circular arena with diameter  $d$  and in an  
 122 annulus (formed by two concentric circles) where  $N$  termites move (see VIDEO| 15:00 min, as an example). Initial condition are  
 123 as follows.  $N$  termites are released at random positions on the arena (overlaps are forbidden) and its direction  $\theta^0$  is randomly  
 124 chosen  $\in [0, 2\pi)$ . The state of each termite is set as inactive with probability  $p_w$  and the waiting time is chosen from the  
 125 power-law distribution while another fraction is active. Trajectories obtained after  $10^4$  times step using 1, 2, 4 and 16 termites  
 126 for circular and anular arenas are show in Figure S11.

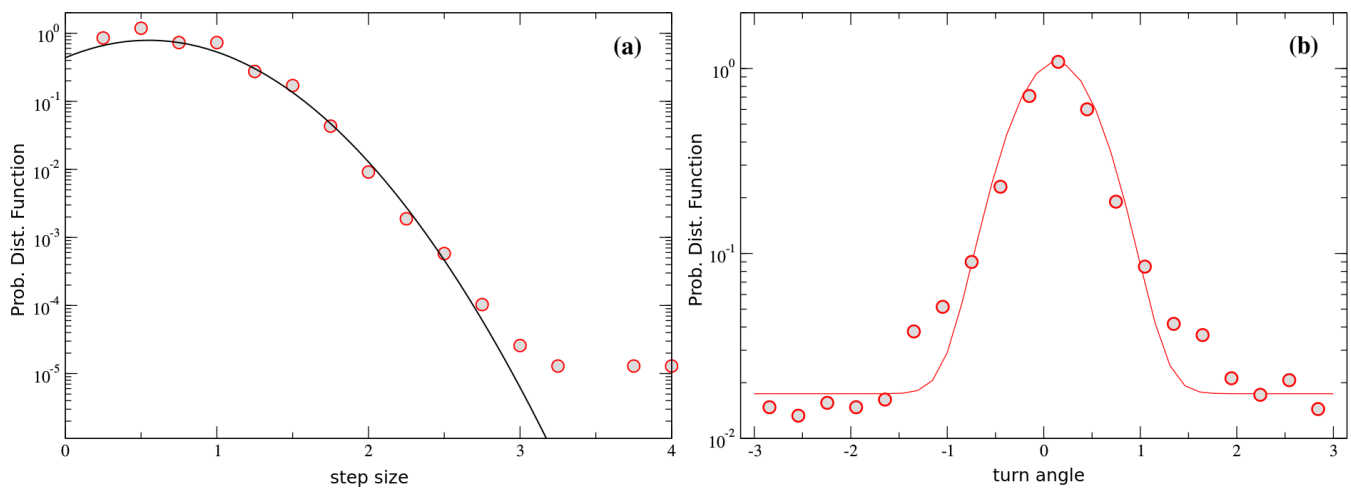


Fig. S9. Circles depict (a) the Probability distribution of step size and (b) the typical turning angle as measured from the trajectory of a termite worker moving freely in the arena. The fits are obtained using the equation 1 and the numerical data considering the proposed model for the termite walk.

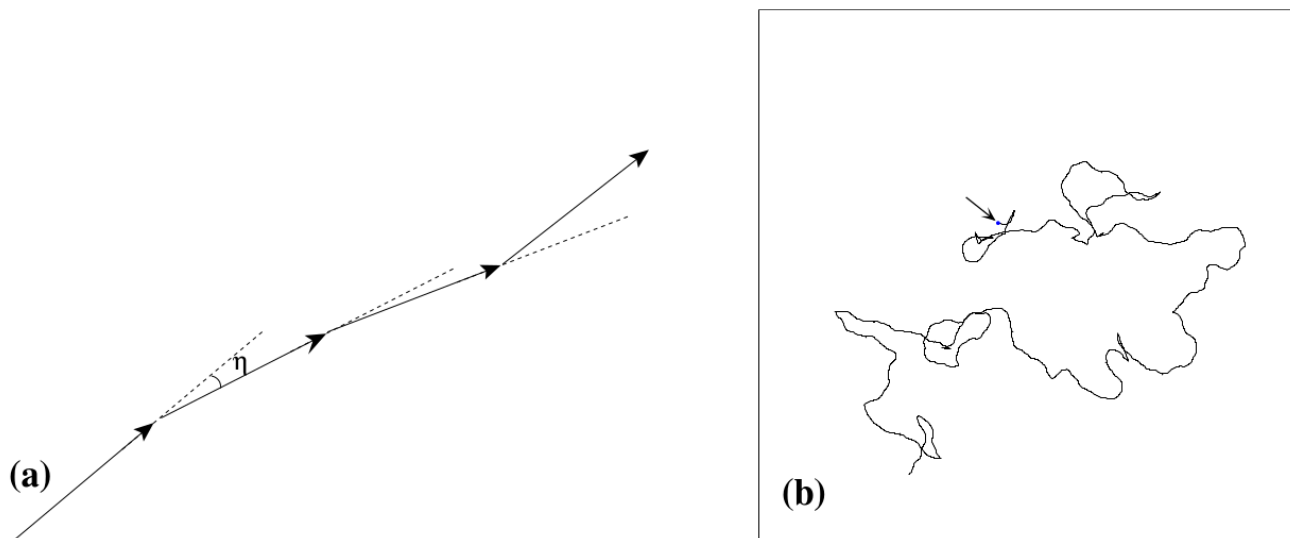


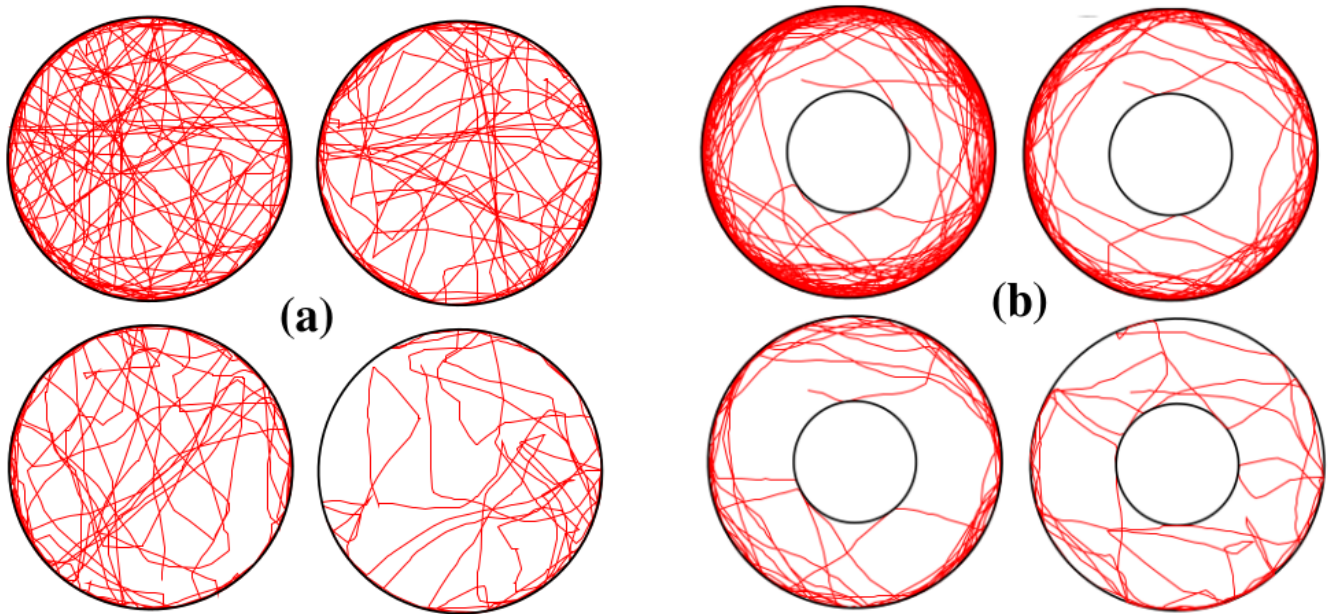
Fig. S10. (a) Schematic illustration of the trajectory rule. (b) A trajectory of a modeled termite on a free arena considering a walk with four thousand steps.

## 127 A solvable model for annular motion the emergence of Lévy walks in social groups with preferential attachments

128 Reynolds (2013)[2] showed how Lévy walks can emerge in social groups with preferential attachments. Here for completeness  
 129 we briefly describe this model, as predicted dependency of the Lévy exponent,  $\mu$ , on the number of preferential attachments  
 130 matches our observations of termites. Model groups consist of an ignorant but responsive “leader” and its “followers”. The  
 131 leader is responsive to a small number,  $N$ , of its followers. The leader moves with constant speed and randomly selects a  
 132 new direction of travel each time it encounters one of its followers –a collision avoidance response–; otherwise it continues to  
 133 move with constant speed along a straight line. Immediately after each such turn the followers regroup around the leader.  
 134 Follower movements comprise a superposition of a straight-line movement and a random walk which, unless stated otherwise,  
 135 is a Brownian walk. The straight-line movement runs parallel to the leaders’ movements and keeps pace with the leader.  
 136 The orthogonal random movements result in occasional encounters with the leader. Analysis reveals that the distribution of  
 137 distances travelled by the leaders (and so followers) between consecutive turns has a power tail with characteristic exponent  
 138  $\mu = 1 + N/2$ . These movement patterns correspond to a Lévy walk when  $N \leq 4$ , and are consistent with our observations of  
 139 confined termites.

### 140 Preferential interactions

141 **Preferential interactions and individual recognition.** As many other social insects, termites are able to recognize their nestmates  
 142 which is important to maintain colony integrity in front of intruders and parasites. How this is achieved at the individual level?



**Fig. S11.** (a) Trajectory of a termite after  $10^4$  times step on the circular (of diameter  $10a$ ) and annulus (of inner  $5a$  and outer  $12a$ ) arena (b). The parameter used were  $\sigma = 0.1$ ,  $p_w = 0$ ,  $p_{crowd} = 0$ ,  $p_w = 0.01$ ,  $p_\theta = 10^{-3}$ ,  $\sigma = 0.2$  and  $\bar{\ell} = 0.4$ .

143 It is not very well understood. However individuals can easily recognize other individuals even from the same species but from  
 144 different nests [4]. Another potentially interesting feature of insect social recognition would be ability to recognize specific  
 145 individuals or specific groups. There is only one example of this reported in the literature and that is the case of the paper  
 146 wasps [4] who apparently are able to identify facial features of specific individuals. This complex feature, it has been argued,  
 147 may be associated with an increase of size and sophistication of brain structures, in a conjecture that is known as the *Social*  
 148 *Brain Hypothesis* [5,6]. However there is limited evidence, at best, that termite brain has evolved large neuronal structures  
 149 associated to individual recognition [7,8]. Moreover, it has been speculated that the ability of individual recognition and the  
 150 memory involved in keeping a record of social acquaintances is also modulated by brain size in such a way that large brains  
 151 give the opportunity of keeping in memory a large social network.

152 The average number of social acquaintances for a given individual –the Dunbar number [9]– is of about 150 in humans  
 153 and would be less in species with less well endowed brains. With their tiny and barely unsophisticated brains, it would  
 154 be almost impossible to think on a Dunbar number for them. However, we are reporting that social interactions among *C.*  
 155 *cumulans* individuals seem to be selective and preferential, a feature not reported before with Dunbar-like numbers of less than  
 156 5 nestmates per individual as concluded from the above model and the experimental observations of preferential interactions  
 157 with the methodology described below.

158 **Experimental evidence of preferential interactions in termites.** To retrieve termite positions from the experimental arenas  
 159 we built a custom video tracking algorithm on top of open-sourced libraries of the Python scientific computing ecosystem.  
 160 The computer code is freely available at GitHub (<https://github.com/dmrib/trackingtermites>) with tracking examples as well. In  
 161 summary, it works as follows.

162 **Termite detection.** The first step consists in informing to the tracking algorithm the initial position of each termite individual.  
 163 This is accomplished with a manual selection screen where the first frame of the video under study is displayed to the user, who  
 164 employs the computer mouse to draw a box around every termite of interest. After the selection, each box is automatically  
 165 recorded under a unique identity that persists until the end of the algorithm’s execution.

166 Here, some implementation details are needed to ease understanding of the posterior data analysis stage:

- 167 1. when the users selects a termite area, the bounding box is constrained to  $16 \times 16$  pixels. This is done in order to have a  
 168 fixed distance parameter for reporting encounters between individuals (please refer to the explanation on how to detect  
 169 encounters for better detail).
- 170 2. we have empirically found that the tracking algorithm works very much better if we try to track the termite abdomen area  
 171 instead of its entire body. This seems to be due to the fact that the abdomen area is seen by the kernelized filter as a  
 172 more stable region leading to better prediction of its position

173 **Computing positions.** After the initial position of each termite is known, this information is fed into the KCF algorithm. It is  
 174 important to notice here that even though the tracking of all the individuals happens in parallel, each individual is evaluated

175 by a different instance of the algorithm. There is no sharing of data or parameters between each execution thread.

176 In very broad terms, we can understand each instance as one task of learning a classifier capable of distinguishing the  
177 appearance of the object being followed from the background of each video frame. This classifier can be evaluated in the  
178 neighbouring areas of the subsequent frame so that to find the new region containing the object. Each detection provides a new  
179 image patch that can be used to update the model. Visually the process can be understood as in Figure S12.

180 Although effective in most of the duration of the footages, some errors can arise from the temporary occlusion of the object  
181 being tracked (*e.g.*, by other termites, shadows in the arena, etc). To treat these cases, we introduced tools to let the user to  
182 interfere directly, manually resolving conflicts and errors. These tools are:

183 **Frame rate control:** the user can manipulate the minimal time interval required to change the frames displayed to the user  
184 to it is easier to visually inspect the progress of the tracking process and detect errors.

185 **Restart tracking instance:** the user is able to restart the tracker instance, putting it back in a coherent state right before  
186 errors had arisen.

187 **Rewind to previous states:** the user is able to rewind the tracking algorithm to a previous state, stopping the process,  
188 making necessary corrections to the bounding box and resume tracking.

189 The combination of the above features made this algorithm robust enough to handle the tracking of up to 120 termites  
190 simultaneously.

191 **Detecting encounters.** Since the termites' bodies are represented by a bounding box, an encounter between them would cause  
192 an intersection between these boxes area. By examining a posteriori all positions of each bounding box and expanding boxes to  
193 include the termite head, we can identify intersections and report the respective termite identities (Figure S13).

194 **Statistical analysis of preferential attachments.** Here we inspected whether termites walking in annular arenas would preferen-  
195 tially contact some of their nestmates over others along a *ca.* 30 min period. The step-by-step analysis and the full dataset are  
196 available at Harvard Dataverse: <https://doi.org/10.7910/DVN/7USPOA>.

197 To do so, we filmed and tracked each individual termite in the confined group, tallying the number of time-steps this focal  
198 termite spent contacting a given target termite along the whole footage. This has produced a dataset such as:

199 Talled time-steps for a group of 3 individuals.  
200 -----

201	trajectory	focalTermite	targetTermite	steps
202	1 traj00006	termite01	termite02	640
203	2 traj00006	termite01	termite03	676
204	3 traj00006	termite02	termite01	635
205	4 traj00006	termite02	termite03	500
206	5 traj00006	termite03	termite01	702
207	6 traj00006	termite03	termite02	502

208 -----

209 Then, for each individual we averaged number of time-steps it acted as a target of an interaction along the whole footage,  
210 producing a result such as:

211 Averaged time-steps a termite spent as a target.  
212 -----

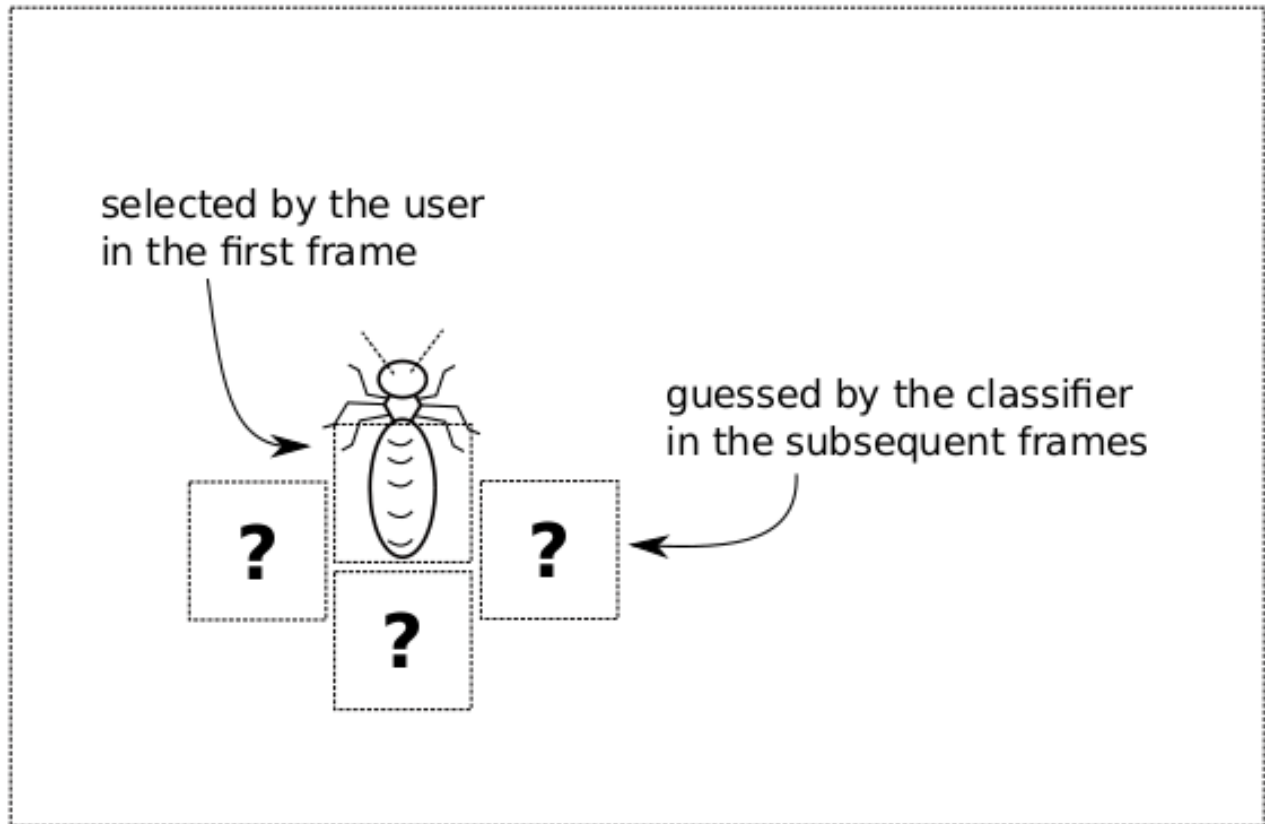
213	targetTermite	steps
214	1 termite01	668.5
215	2 termite02	571.0
216	3 termite03	588.0

217 -----

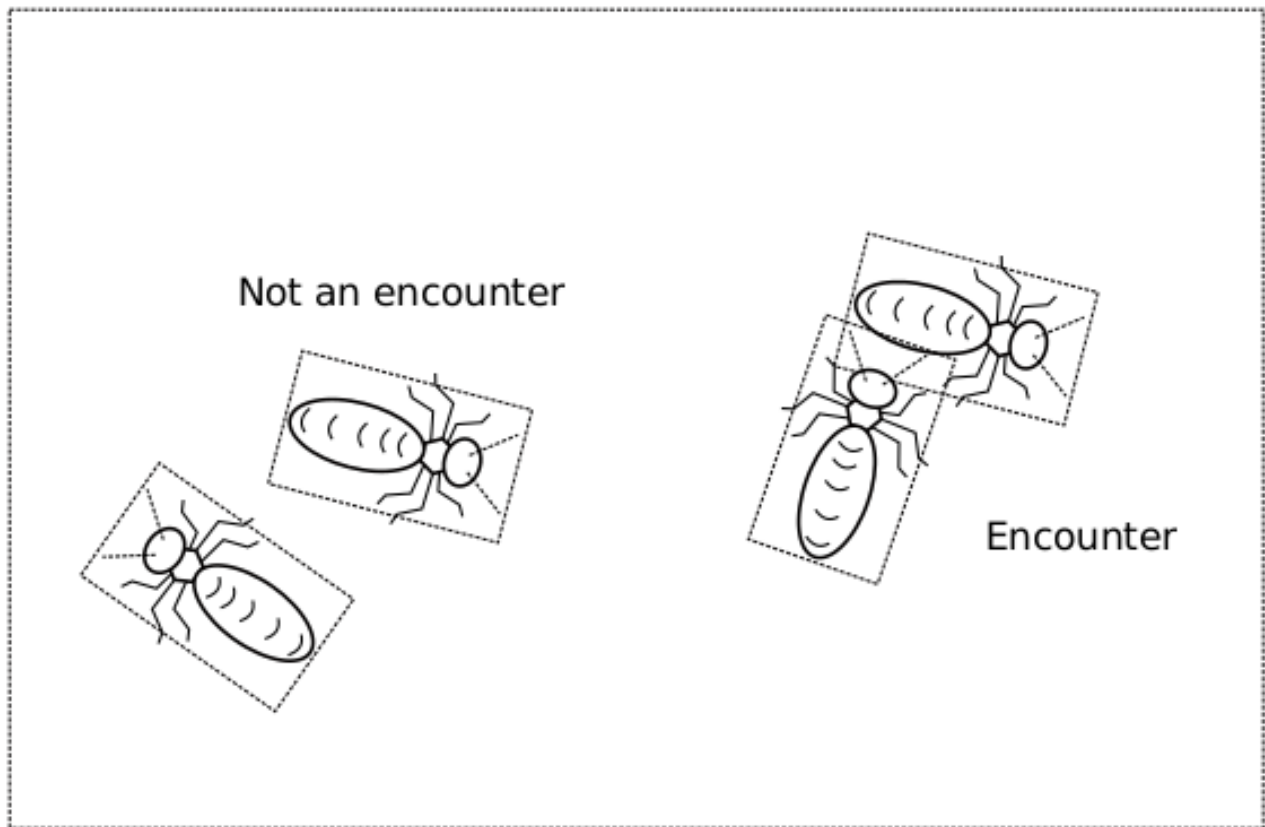
218 Then, we ran a Chi-square test to verify whether the proportion of time-steps spent as a target would vary among termite  
219 individuals. That is to say, we inspected whether these proportions would depart from an uniform distribution and, if so, to  
220 point to the existence of 'favourite targets'.

221 In case the Chi-square test did point to significant differences, we counted the number of 'favourites' within that given  
222 group. These 'favourites' were defined as being the termites whose average number of time-steps spent as a target was larger  
223 than the global average of targeting time-steps in the whole footage.

224 The number of preferred target-termites in each arena (y-var) was then regressed against the number of termites therein  
225 confined (x-var), in order to inspect how preferential attachments would correlate with group size. Analysis consisted in  
226 contrasting the model thereby obtained with a model with zero intercept and slope = 1, that is, a model in which favouritism  
227 was absent. Modelling was performed in R, under Generalised Linear Modelling and normal error distribution, followed by  
228 residual analysis. Contrasts were made using Akaike Information Criterion (AIC).



**Fig. S12.** The tracking process by means of bounding boxes: (i) the user manually draws a box encompassing the termite's abdomen; (ii) a classifier is trained to discriminate between areas containing the object and the background; (iii) the classifier evaluates the neighbourhood around the last known location of the object and the region with higher probability of containing the object is reported; (iv) a new classifier is trained with the new position; (v) the process is repeated until the end of the video. Termite drawing modified from DeSouza (2018)[10]. Arthropod drawings at Zenodo. <http://doi.org/10.5281/zenodo.1318188>



**Fig. S13.** Detecting encounters by recording bounding boxes intersections. Termite drawings modified from DeSouza (2018)[10]. Arthropod drawings at Zenodo. <http://doi.org/10.5281/zenodo.1318188>

229 **More on power-laws in models and real termite data**

230 Consider the fact that the turning points on a termite walk define a dimensionless time series,  $u(t) : u(t)=1$  if a turn occurred  
 231 at time  $t$  otherwise  $u(t)=0$ . The net displacement,  $n(t)$ , of the time series  $u(t)$  is given by the running sum  $n(t)=\sum_{t'=0}^t u(t')$ .  
 232 If the values of  $n(t)$  are completely uncorrelated and behave like “white noise”, then the root-mean-square value of the running  
 233 sum  $F = \sqrt{\langle(\Delta n(t) - \langle \Delta n(t) \rangle)^2\rangle} \propto t^\alpha$  where  $\alpha=1/2$  and where  $\Delta n(t) = n(t) - n(t + t_0)$ . The angular brackets denote an  
 234 average over all possible times  $t_0$  [11]. Short-term correlations in the data may cause the initial slope of a plot of  $\log(F)/\log(t)$   
 235 to differ from  $1/2$ , although it will still approach  $1/2$  at longer times. Consequently, Markov processes also give  $\alpha = 1/2$  for  
 236 sufficiently large  $t$ . Long-term power-law correlations [11] however, will generate  $\alpha$  values  $\neq 1/2$ . Most of our data shows that  
 237  $\alpha \approx 0.75$ , and this implies that long term power-law correlations exist in the data, or in other words, the termite walking  
 238 patterns were similar on all temporal scales.

239 On the other hand, mechanistic models that are essentially CCRW can converge on a Lévy motion distribution. Two  
 240 cases are well documented. When searching for patchily distributed resources some foragers switch between extensive and  
 241 intensive search patterns. This can result in bi-phasic walks with bi-exponential step-lengths that can resemble Lévy walks with  
 242 power-law step-lengths [12](Benhamou, 2007). But close resemblance to a Lévy walks requires fine-tuning of the bi-exponential  
 243 walk, i.e. fine-tuning of the distribution of search targets. The search targets in our study (conspecifics) are, however, uniformly  
 244 distributed. Intrinsic multiphasic walks, so-called Weierstrassian random walks, that resemble Lévy walks have been identified in  
 245 mud snails (*Hydrobia ulvae*) and in mussels (*Mytilus edulis*) [13-15]. These movement pattern appear to have their mechanistic  
 246 origins in the coupling between neurobiology and motor properties and may be specific to organisms with stick-slip locomotion  
 247 [15].

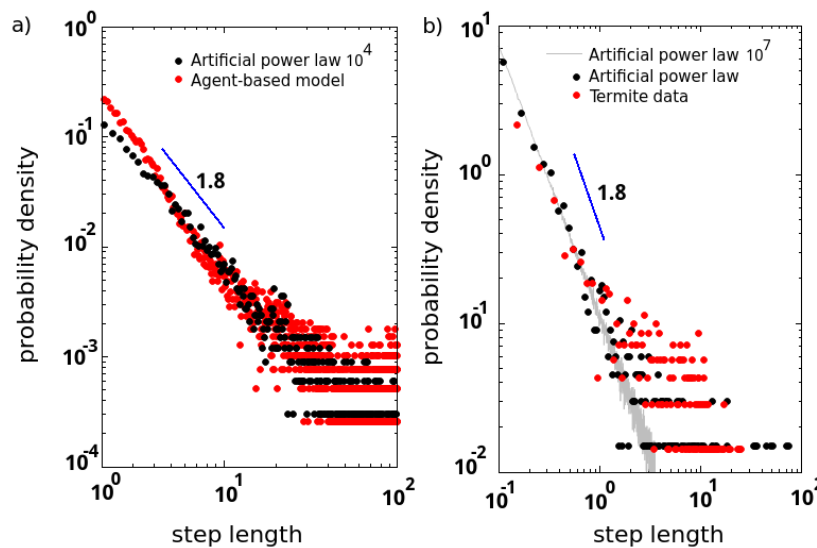


Fig. S14. artificial power law superimposed on (a) an agent-based and (b) on real termite data. See the text for more details.

248 We have plotted termite walking step distributions as accumulated plots because this is the preferred way of doing it in order  
 249 to avoid the binning issues of a frequency plot (Figures 1 and 5, in the main text). We advise against presenting frequency  
 250 plots when the time series are not long enough. We have presented frequency plots in Figure 3 of the main text since these are  
 251 model data and so can be of an arbitrary length (10<sup>7</sup> points), binning in this case is not a significant problem, especially if  
 252 they are presented more in a qualitative way. it may be interesting, nevertheless, to directly compare frequency plots for a  
 253 qualitative visual comparison. Consider Figure S14(a) where we have matched fairly precisely an example of a segment from a  
 254 step length distribution coming from the agent-based model (red, 10<sup>5</sup> points) and an artificially generated smooth power-law  
 255 with scaling exponent -1.8 (black, 10<sup>5</sup> points). In Figure S14(b) we show the same smooth artificial power law with scaling  
 256 exponent -1.8 of length 10<sup>7</sup> (grey) superimposed on the frequency distribution of the termite data (red, 1500 points) and a  
 257 short artificially generated power law (black, 1500 points) in order to show how well they match the fluctuations of a pure  
 258 power law behavior. As said before, the correct way of presenting step-length distributions is by means of the accumulated plot  
 259 when a careful measure of the scaling exponent is needed.

260 **Movies**

261 Movie S1. Termite social clustering, available at [https://lape.fisica.unam.mx:/termite/social\\_clustering.mp4](https://lape.fisica.unam.mx:/termite/social_clustering.mp4)

262 Movie S2. Termite social trapping in large container, available at [https://lape.fisica.unam.mx:/termite/large\\_](https://lape.fisica.unam.mx:/termite/large_container.mp4)  
 263 [container.mp4](https://lape.fisica.unam.mx:/termite/large_container.mp4)



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