

**SOLVING TWO-DIMENSIONAL GROUNDWATER FLOW EQUATION USING  
ALTERNATING DIRECTION IMPLICIT METHOD**

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ALTERNATING DIRECTION IMPLICIT METHOD**

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requirements for the award of the degree of  
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*To my beloved mother, Suziana binti Sidek, my father, Ahmad Nordin bin Abdullah,  
My brothers Muhammad Muizzuddin and Muhammad Luqma'nul Hakim  
Thank you for all of your greatest support and everlasting love*

*Lastly, millions of thankful to my supervisor  
Tuan Haji Hamisan Bin Rahmat*

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## ABSTRACT

Groundwater model can be described as a mathematical model and the equation of groundwater is governed by partial differential equation. In order to solve the groundwater flow equation, numerical method such that Finite Difference Method (FDM) is used. In this research, a two-dimensional transient groundwater flow equation for a confined, nonleaky, and homogeneous with mixed boundary conditions is solved using Alternating Direction Implicit (ADI) method where ADI method is one of the FDM. The algorithm of ADI method has been developed for three different types of boundary conditions that is Dirichlet condition, Neuman condition and Mixed condition. The transient groundwater flow equation has been derived and was solved using ADI method by Matlab software. Then, the results obtained were compared to analytical solution. Since the solutions from numerical method provide the small error when compared to the analytical solutions, it therefore can be concluded that ADI method provides good approximations in solving two-dimensional groundwater transient flow problem.

## **ABSTRAK**

Model air bawah tanah boleh digambarkan sebagai model matematik dan persamaan air bawah tanah diwakilkan oleh persamaan pembezaan separa. Bagi menyelesaikan persamaan aliran air bawah tanah, kaedah berangka digunakan iaitu Kaedah Beza Terhingga. Dalam kajian ini, persamaan aliran air bawah tanah dua dimensi yang terbatas, tiada kebocoran, dan homogen dengan syarat bercampur diselesaikan menggunakan kaedah Lelaran Tersirat Berarah (LTB). Kaedah ini merupakan salah satu kaedah beza terhingga. Algoritma kaedah Lelaran Tersirat Berarah telah dibangunkan untuk tiga jenis syarat sempadan iaitu syarat Dirichlet, syarat Neumann dan syarat bercampur. Persamaan aliran air bawah tanah mantap telah diperolehi dan telah diselesaikan dengan kaedah LTB serta perisian Matlab. Kemudian, keputusan yang diperolehi dibandingkan dengan penyelesaian analisis. Oleh kerana penyelesaian berangka memberikan ralat yang kecil apabila dibandingkan dengan penyelesaian analitikal, kaedah Lelaran Tersirat Berarah dapat memberikan penyelesaian yang baik bagi menyelesaikan masalah aliran dua dimensi air bawah tanah.