

**TURBULENT HEAT TRANSFER IN A TRAPEZOIDAL CHANNEL  
WITH TRANSVERSE AND V-SHAPED RIBS ON TWO OPPOSITE  
WALLS**

A Thesis

by

KARTHIK SUBRAMANIAN

Submitted to the Office of Graduate Studies of  
Texas A&M University  
in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

December 2005

Major Subject: Mechanical Engineering

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## ABSTRACT

Turbulent Heat Transfer in a Trapezoidal Channel with Transverse and V-shaped Ribs  
on Two Opposite Walls. (December 2005)

Karthik Subramanian, B.E., University of Madras

Chair of Advisory Committee: Dr. Sai Lau

This study investigates the turbulent heat transfer and friction in a trapezoidal channel with opposite walls roughened with transverse and v-shaped ribs. The roughened channel depicts the internal cooling passage of an aerofoil near the trailing edge. The various configurations investigated for this study are smooth channel, channel with 90° transverse ribs and channel with v-shaped ribs angled at 45°. The pitch-to-height ratio ( $P/e$ ), rib height-to-hydraulic diameter ratio ( $e/D_h$ ) and the aspect ratio ( $W/e$ ) were maintained at 12, 0.1906 and 1, respectively. The configuration was tested for Reynolds number ranging from 7,000 to 40,000. The 45° rib was found to produce the maximum heat transfer and minimum pressure loss.

TO  
MY GRANDPARENTS & PARENTS

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Last, but not least, I would like to thank my lab mates and my friends whose support has been instrumental in the successful completion of my project.

## NOMENCLATURE

A	heat transfer surface area
B	bias limit
$C_p$	specific heat at constant pressure
$D_h$	hydraulic diameter
$d_o$	diameter of orifice
e	rib height
f	friction factor
$f_o$	friction factor in fully developed tube flow
H	Heat transfer coefficient
I	current input
K	thermal conductivity of air
l	plenum length
L	length of slab
$\dot{m}$	mass flow rate
Nu	Nusselt number
$\overline{Nu}$	Average Nusselt number
$Nu_o$	Nusselt Number in fully developed tube flow
$\Delta p$	pressure drop across test section
P	rib pitch
$p_o$	pressure upstream of orifice

$P_w$	wetted perimeter
$P_x$	random error
$Pr$	prandtl number
$\dot{q}$	heat flux
$Re$	Reynolds number
$S_x$	precision index
$t(N,C)$	confidence level
$T_i$	temperature of slab
$T_b$	bulk mean temperature
$T_w$	local wall temperature
$U_x$	relative uncertainty of x
$V$	voltage input
$W$	flow channel width
$W/H$	channel aspect ratio

#### Constants (calculated)

$C$	discharge coefficient
$Y$	expansion coefficient

#### Greek symbols

$\alpha$	rib angle-of-attack
$\sigma$	standard deviation

$\mu$	average dynamic viscosity of air
$\rho$	average density of air



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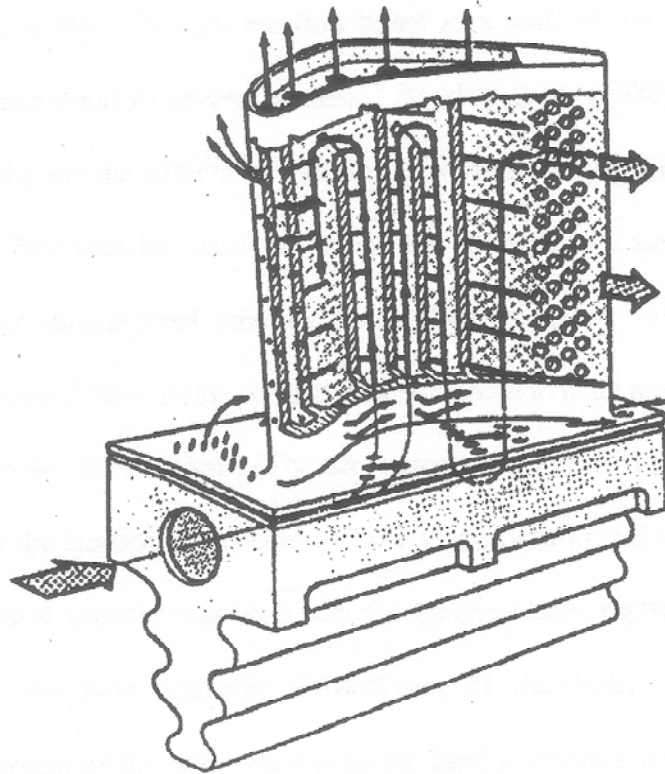
## INTRODUCTION

Gas turbines, as a prime mover, find a wide range of applications in the industrial world today. Therefore, it is important to develop highly efficient gas turbines using the latest state-of-the-art technologies. One of the traditional methods used to improve the efficiency of a gas turbine is to increase the inlet temperature; thereby increasing the power output and, in turn, the efficiency.

The problem associated with increasing the inlet temperature of a gas turbine is the failure of material due to excessive thermal stresses. This brings in the concept of cooling of turbine blades to incorporate the increase in the inlet temperature. The cooling should be optimized, as lack of cooling will cause failure of material and excess cooling will cause a decrease in efficiency of the turbine.

The two main methods of cooling are internal and external cooling. The three main internal cooling methods are namely jet impingement cooling, rib-turbulated cooling and end cooling. The main focus of this research is rib-turbulated cooling.

Fig. 1 shows the cooling methodology in a typical blade of a gas turbine, which is cooled mainly by convection. The turbine consists of internal passages, which are serpentine. The passage near the trailing edge of the blade consists of pin fins so as to enhance the heat transfer rate. Part of air is ejected out through small holes near the leading edge, which is used for film cooling on the outer blade surface. This ejected cool air forms a thin film over the surface, thereby insulating it from the hot gases.



**Fig. 1 Gas Turbine Cooling Methodology**

Jet impingement cooling is one of the most effective ways of internal cooling as high heat transfer coefficients can be achieved. Therefore the jet impingement cooling is mostly used near the leading edge of the airfoil where the thermal loads are high. Also the thicker cross section near the leading edge makes the housing of nozzle easier. Jet impingement cooling is not preferred at the mid-chord section of the rotor blade as the arrangement reduces the structural strength of the blade; however it is used in the mid-chord section of the stator blade.

The trailing edge of the blade is usually cooled using pin fins. The fins are arranged in such a manner that they block the flow, which results in forced convected fin cooling. These fins help in two different ways to enhance the heat transfer. Firstly, they introduce wakes into the stream thereby creating free stream turbulence. These wakes not only disturb the flow but also enhance the heat transfer from the fins down-stream. Secondly, the pin fins help in increasing the effective heat transfer area there by helping in effective removal from the surface.

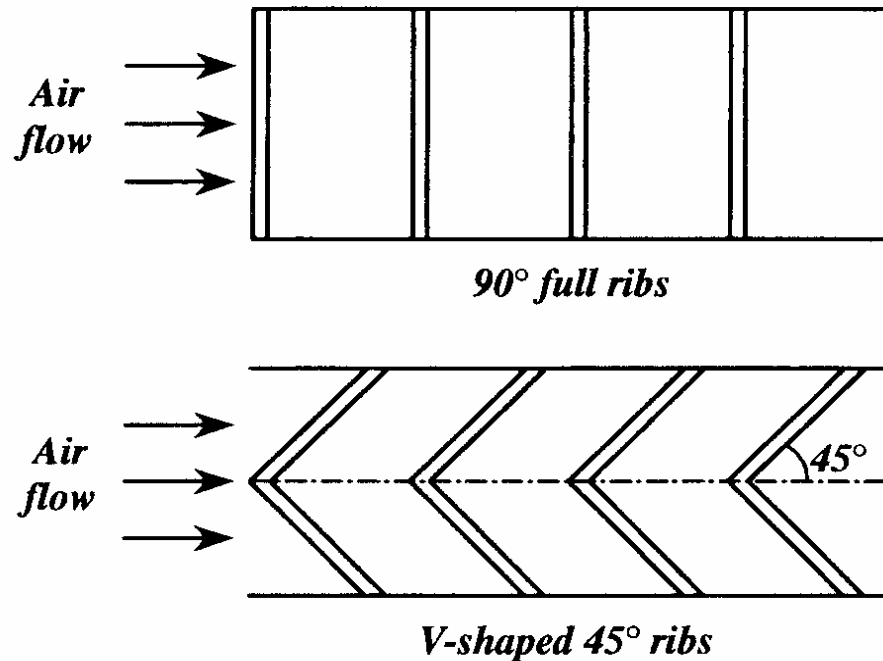
The internal passages in the mid-rib section of the airfoil usually have either a rectangular cross section or a trapezoidal cross section. These passages are usually roughened with ribs on two opposite walls that are exposed to hot combustion gases on the outside, so as to augment the heat transfer from the blade to the cooling air. These ribs causes flow separation. In some cases secondary flows cause turbulent mixing near the wall where these flow separations reattach the boundary layer to the wall.

The current research is aimed at studying the streamwise variation of the regional average heat transfer coefficient, along a duct, trapezoidal in cross-section, which



models the internal cooling passage of an airfoil. The study will be conducted with three channels: one with smooth walls, one with  $90^\circ$  transverse ribs on two opposite walls and one with  $45^\circ$  V-shaped ribs on two opposite walls, for Reynolds number varying between 8,000 and 40,000 as shown in Fig. 2. The pitch-to-height ( $P/e$ ) ratio will be maintained at 12 and the rib height at about 10% of the hydraulic diameter.

The Nusselt number, which is a dimensionless heat transfer coefficient, will be normalized with the Nusselt number for the fully developed turbulent flow in a smooth channel, calculated with a correlation by McAdama/Dittus-Boelter to study the heat transfer augmentation.



**Fig. 2 Rib Configuration Examined**

## LITERATURE REVIEW

### Review of Previous Work

Extensive research has been conducted in the field of turbulated cooling both experimentally and numerically. The research focuses have been on channels with square, rectangular, and triangular cross sections, and with either single pass or multiple passes. The heat transfer coefficients have been studied for various rib configurations, Reynolds numbers, aspect ratios ( $W/H$ ), and pitch-to-height ( $P/e$ ) ratios. Procedures adopted for studying heat transfer coefficient have included both steady state heat transfer experiments and mass transfer experiments using mass-heat transfer analogy.

The effect of Prandtl number on heat transfer and friction in smooth and rough tubes was studied by Dippery et al. [1]. The results showed that the heat transfer increased by a factor to 2-3 when rough tubes replaced smooth tubes at the expense of increase in friction. However at high Prandtl number the improvement in heat transfer was achieved without any losses by roughening.

Han et al. [2] investigated the heat transfer and friction characteristics of rib roughened surfaces for various angle of attacks, rib profiles and  $P/e$  ratios. It was found that ribs placed at an angle of attack of  $45^\circ$  had superior heat transfer performance for a given friction power when compared to that of ribs at an angle of attack of  $90^\circ$ . Also it was once again concluded that the heat transfer and friction was maximum for a  $P/e$  ratio of 10.

Han [3] studied the heat transfer and friction in square channel with opposite rib-roughened wall for Reynolds number ranging from 7,000 to 90,000. The Stanton number at the ribbed wall was found to be 1.5 to 2.2 times than that of the four-sided smooth duct. The average friction factor also was found to increase by a factor of 2.1 to 6.

The variation of pressure drop and average heat transfer along a square duct for Reynolds number ranging from 7,000 to 90,000,  $P/e$  ratio varying from 10 to 20 and for various rib configuration was studied by Han et al. [4]. The results showed that for ( $\alpha = 90^\circ$ ) the average Nusselt number was twice the average Nusselt number for a smooth channel and the friction factor increase about four to six times. The heat transfer enhancement was found to be better for ( $\alpha = 45^\circ$  and  $30^\circ$ ) in comparison to other configuration. The heat transfer for ( $\alpha = 45^\circ$ ) was found to be twenty five times greater than that for ( $\alpha = 90^\circ$ ) but the friction factors remained the same. The  $45^\circ$  angled ribs were found to consume 20-50% less pump power when compared to  $90^\circ$  straight ribs. Also the pump power required for  $P/e = 10$  was found to be less than for  $P/e = 20$ . In general the angled ribs were found to provide better cooling effect than the  $90^\circ$  straight ribs and  $P/e$  ratio of 10 was found to be advantageous than  $P/e$  ratio of 20.

The internal cooling passage near the leading edge of the airfoil is usually triangular in cross section. Therefore Metzger et al. [5] and Luo [6] investigated the heat transfer in triangular channels with angled roughness ribs on two walls. It was once more proven that the V-shaped ribs produced higher heat transfer augmentation than the  $90^\circ$  transverse rib due to the stream-wise growing cross-channel secondary flow induced by the angled ribs. The  $60^\circ$  V-shaped ribs resulted in higher heat transfer than the  $30^\circ$  ribs

and the optimum  $P/e$  ratio was found to be around 7.5. The study revealed that the heat transfer coefficient reached a maximum along the test channel and finally decreased towards the end of the channel due to the reflection of the secondary flow thus affecting the flow pattern. It was concluded that the heat transfer augmentation in triangular channel with ribs, was higher than that in square channel with ribs.

Han et al. [7] investigated the developing heat transfer in rectangular channels with rib turbulators for rib angle varying from  $90^\circ$  to  $30^\circ$ . The combined effects of rib angle and channel aspect ratio on local heat transfer coefficient were studied. The results indicate that the best heat transfer in square channel was obtained with angled ribs at  $30^\circ$ - $45^\circ$  and was about 30% higher than the  $90^\circ$  transverse ribs for constant pumping power. However, for rectangular channel with aspect ratio of 2 and 4, the heat transfer enhancement using  $30^\circ$ - $45^\circ$  ribs was only 5% more than the  $90^\circ$  transverse rib. In general, it was noted that in square channel the heat transfer increased with decrease in rib angle whereas in rectangular channel the dependence of heat transfer on rib angle was negligible.

Han [8] investigated the heat transfer and friction characteristics in rectangular channel with rib turbulator. The distribution of local heat transfer coefficient was studied for varying channel aspect ratio at various Reynolds numbers ranging from 10,000-60,000. The rib angle of attack was maintained at  $90^\circ$  and the experiment was conducted for two  $P/e$  ratios of 10 and 20. The result suggests that the local Nusselt number becomes uniformly periodic between the ribs. The local Nusselt number was found to increase by a factor of 2-3 for various ribbed configuration in comparison to the smooth

channel. The local Nusselt number was found to decrease with increase in spacing and Reynolds number and found to increase with increase in rib height and aspect ratio for a given Reynolds number. The heat transfer augmentation was found to be higher for smaller aspect ratio for a given pumping power.

Lau et al. [9] studied the turbulent heat transfer and friction in square channel with discrete rib turbulators for Reynolds number ranging from 10,000 to 80,000. The studies revealed that the heat transfer in 90° discrete ribs were 10-15% higher than that of the 90° transverse ribs. The overall thermal performance of oblique ribs at ( $\alpha = 60^\circ$ , 45° and 30°) was found to be 20% more than that of 90° discrete ribs. Also the crossed oblique ribs were found to have poor thermal performance and so are not recommended for internal cooling of gas turbines.

The effect of rib configuration and Reynolds number on the local heat transfer distribution and pressure drop in a square channel with two opposite in-lined ribbed walls was studied by Han et al. [10]. The results show that for the various rib configurations the Nusselt number ratio decreases with increase in axial distance and attains a constant value downstream. The studies also indicate that for V-shaped ribs the heat transfer augmentation was higher in comparison with other configurations and the reversed V-shaped ribs produced the maximum pressure drop. The heat transfer performance was found to decrease with increase in Reynolds number.

The effect of V-shaped rib arrays on turbulent heat transfer and friction of fully developed flow in a square channel was studied by Lau et al. [11]. The configuration investigated included V-shaped ribs angled at 45°, 60°, 90°, 120° and 135° for a  $P/e$

ratio of 10. The results indicated that the V-shaped ribs at ( $\alpha = 46^\circ$  and  $60^\circ$ ) produced a 38%-46% and 47%-66% increase in thermal performance when compared to the  $90^\circ$  full rib. Similarly, when the following ribs were reversed, the heat transfer performance was enhanced by 26%-32% and 39%-48% respectively. This enhancement in thermal performance was accompanied by a 55%-79% increase in the pressure drop for various V-shaped configurations in comparison to the  $90^\circ$  rib. The reversed V-shaped ribs was found to result in poor heat transfer performance. The crossed ribs whose performance was also investigated resulted in poor heat removal. It was also found that doubling the  $P/e$  ratio lowers the heat transfer augmentation and friction.

Liou [12] investigated the turbulent heat transfer augmentation and friction in periodic fully developed channel flow using laser holographic interferometer and thermocouples. The distribution of average friction factor as well as the average and local Nusselt was studied for Reynolds number varying from 5,000 to 54,000, the  $P/e$  ratio of 10, 15 and 20 and  $e/D_h$  ratios of 0.063, 0.081 and 0.106. The results showed that there was 2.2 to 17 fold increase in the average Nusselt number for various  $e/D_h$  ratios and Reynolds number. The heat transfer augmentation was found to increase with increase in  $e/D_h$  ratios. The ribs were found to transfer more heat than the duct wall does on a unit area basis. The results proved that the heat transfer decreases with the increase spacing between the ribs. The rate of increase in Nusselt number with Reynolds number is less for the ribbed duct in comparison to the smooth duct, which results in the decrease in the Nusselt number ratio with increase in Reynolds number. The reason attributed to this behavior is that a fraction of the mean flow energy is converted into turbulent kinetic

energy in the ribbed duct, which subsequently results in enhancement of heat transfer through turbulent transport.

The influence of surface heat flux on heat transfers augmentation in square channels with parallel, crossed and V-shaped angles ribs were studied by Han et al. [13]. The test was conducted on square channel with  $L/D$  ratio of 20,  $e/D$  ratio of 0.0625,  $P/e$  ratio of 10 and Reynolds number ranging from 15,000 to 80,000. It was found that the ribbed wall heat transfer coefficient increased with increase in the ratio of ribbed side to smooth side wall flux. It also showed that two ribbed side wall heating provided a higher ribbed side wall heat transfer augmentation than the four wall uniform heating. The effect of wall flux ratio was found to reduce with increasing Reynolds number. The results indicate that the  $60^\circ$  v-shaped and parallel ribs performed better than  $60^\circ$  crossed rib and  $90^\circ$  rib irrespective of the wall heat flux ratio and Reynolds number.

Taslim et al. [14] studied the effects of turbulator profile and spacing on heat transfer and friction in a channel with traverse ribs. It was concluded that the heat transfer coefficient was higher for aspect ratios greater than unity but resulted in higher pressure loss. The trapezoidal shaped ribs spaced properly were found to be effective in heat removal. The optimum pitch to height ratio for the  $90^\circ$  square turbulator was found to be around 8. The sensitivity of Nusselt number was found to decrease with decrease in the blockage ratio ( $e/D_h$ ).

Taslim et al. [15] experimentally investigated the heat transfer and friction in channel roughened with angled V-shaped and discrete ribs on two opposite walls for Reynolds number ranging from 5,000 to 30,000. The results showed that the  $90^\circ$

transverse ribs produced the lowest heat transfer performance. The 45° angled V-shaped ribs produced the highest heat transfer performance in comparison to other rib configurations. For V-shaped ribs facing downstream of flow, the one with lowest blockage ratio had better heat removal rate. The discrete ribs also produced better performance in comparison to the transverse ribs.

Kato et al. [16] investigated the heat transfer enhancement and pressure loss by surface roughness in turbulent channel flows. The objective of the study was to investigate the relationship between the heat transfer enhancement and the increase in drag by the rough surface using time-space averaged momentum and energy equation. It was concluded that the efficiency of the heat transfer surface in general was less than unity when the molecular Prandtl number of the working fluid is less than the turbulent Prandtl number and vice versa. For fluids with low Prandtl number the drag increase is usually greater than the heat transfer augmentation; however for liquids with higher Prandtl number the eddy viscosity over the rough surfaces has a significant effect on the heat transfer enhancement. This increase in efficiency of the heat transfer surface is true only for smaller roughness elements and for higher roughness elements the efficiency does not normally exceed unity.

Ekkad et al. [17] and Murata et al. [18] studied the heat transfer measurements inside straight and tapered two-pass channel with turbulator ribs as in reality the internal cooling passage has a decreasing cross sectional area from the hub to the tip. The study was conducted for various Reynolds numbers with and without ribs for both straight and tapered channel. The results indicate that at low Reynolds number the heat transfer



augmentation in the first pass in the straight channel is comparable to that of the tapered channel. However, at higher Reynolds numbers, the acceleration effect in the tapered channel results in higher Nusselt number ratios when compared to the straight channel. The tapered channel with ribs, enhanced the heat transfer by a factor of 1.5-2.0 when compared to the tapered smooth channel but in the after-turn region the Nusselt number ratios were found to be comparable. The tapered ribbed channel and straight ribbed channel was found to provide similar augmentation level in most of the channel.

Heat transfer and friction behaviors in rectangular channel with varying number of ribbed walls were investigated by Chandra et al. [19]. The test was performed with ribs on one, two, three and four walls for Reynolds number ranging from 10,000 to 80,000. The  $P/e$  and  $e/D_h$  ratios were maintained at 8 and 0.0625, respectively. It was clear, by the results, that the heat transfer enhancement increased with increase in the number of ribbed walls due to increase in turbulence. The Nusselt number ratio was found to decrease along the streamwise direction and remains a constant once the flow becomes fully developed. The Nusselt number ratio also decreased with increase in Reynolds number. The heat transfer enhancement for the two-sided ribbed wall was found to be in the range of 2.64 to 1.92. It was also noted that the friction factor ratio increased with increase Reynolds number. The heat transfer performance was studied and the results indicate a significant decrease in the performance with increase in the number of ribbed walls and Reynolds number.

## **Objective**

As stated earlier, with the invention of high efficiency gas turbine engines, there is a need to effectively cool the turbine blades to prevent the failure of material due to excess heating by the high-temperature combustion gases flowing over the exterior surfaces of the blades. Most of the studies carried out thus far by researchers have been conducted on channels that had square, rectangular, or triangular cross sections. The actual passages in the airfoil are all not exactly rectangular in cross section. In fact, most of these passages are trapezoidal in cross section as shown in Fig. 3. So, the need arises to study the heat transfer coefficient distribution along a trapezoidal channel for various rib configurations and flow rates.

The objective of this research is to determine the streamwise variation of the regional average heat transfer coefficient along a smooth trapezoidal channel and two channel of the same trapezoidal cross section with  $90^\circ$  transverse ribs and  $45^\circ$  V-shaped ribs on two opposite walls. The Nusslet number, which is a dimensionless heat transfer coefficient, will be normalized with the Nusselt number for the fully developed turbulent flow in a smooth channel, calculated with a correlation by McAdama/Dittus-Boelter to study the heat transfer augmentation.

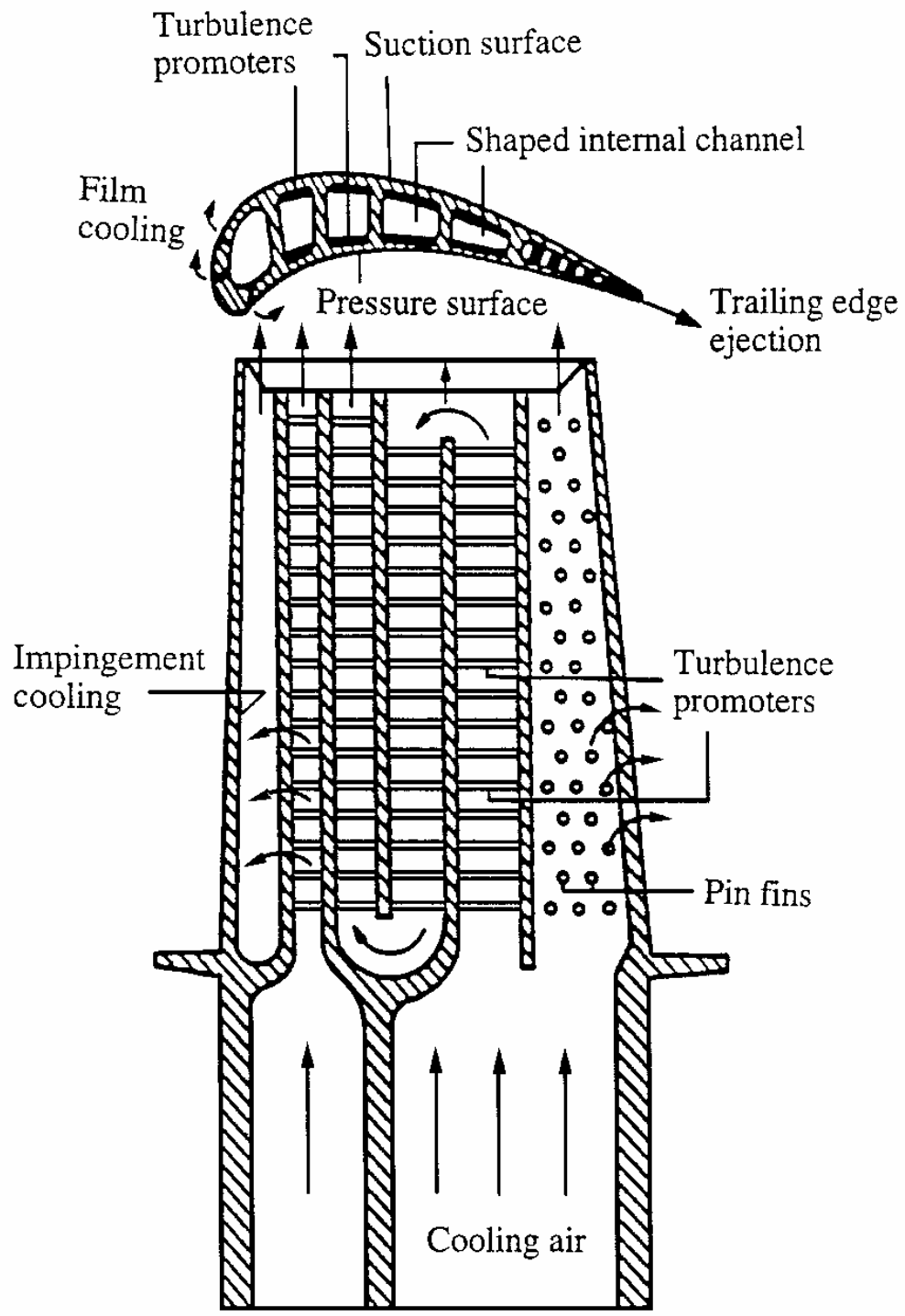


Fig. 3 Cooling Concept in Modern Turbine Blade

## EXPERIMENTAL ANALYSIS

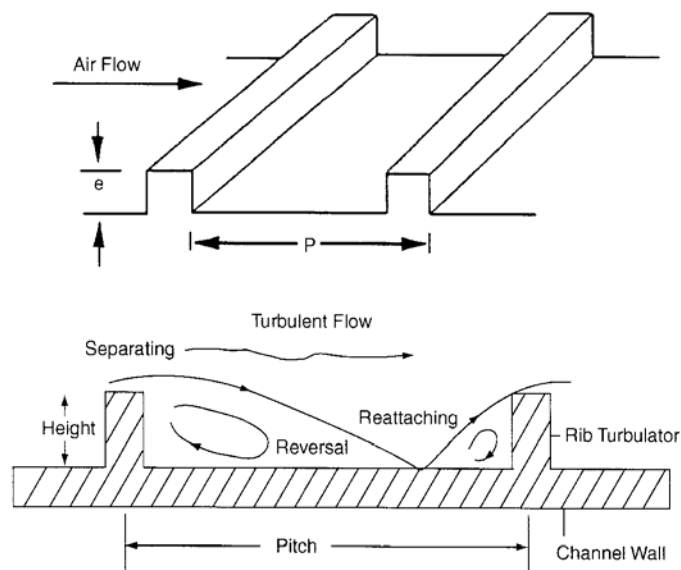
### Rib Turbulated Cooling Theory

The rib turbulated cooling is one of the most common methods used in the mid rib section of a blade. In rib turbulated cooling, ribs are cast on two opposite walls usually on the walls of the suction and pressure sides of the aerofoil. These turbulent promoters help in transferring the heat effectively from the blade to the flowing air, thereby enhancing the cooling process. Researchers have found that parameters that mainly influence the heat transfer are the Reynolds number, the channel aspect ratio ( $W/H$ ), blockage ratio ( $e/D_h$ ) and the rib configurations. In general, the pitch to rib height ratio ( $P/e$ ) and blockage ratio  $e/D_h$  are selected in the ranges of 7 to 15 and 5% to 10% respectively, so as to optimize the heat transfer augmentation and pressure drop losses.

The flow, past the turbulent promoters cast on the walls of the passages are characterized by boundary layer separations and are followed by reattachment of the boundary layer to the heat transfer surface, which results in the enhancement of the heat transfer coefficient. The schematic representation of the rib on the wall and the flow separation near the rib are shown in Fig. 4.

The separation occurs at the ribs, which lead to the formation of a shear layer and finally reattaches at about 6-8 times the rib height, downstream of the rib. The reverse flow boundary was found to originate from the reattachment point and had grown in thickness. The wall shear stress is zero at the reattachment point and was found to

increase in the reverse flow region. Research by Webb [20] has shown that reattachment does not take place below a particular  $P/e$  ratio.



**Fig. 4 Flow Separation on the Ribs**

Various researchers have studied the effects of ribs and the results have been discussed previously. The secondary flow produced by V-shaped ribs is shown in Fig. 5.



**Fig. 5 Cross Stream Secondary Flows Induced by V-shaped Ribs**

These flows induce turbulent mixing which result in effective transfer of heat from the walls to the flowing fluid because of the increase in heat transfer coefficient. However, increase in the heat transfer augmentation is accompanied by pressure drop penalty.

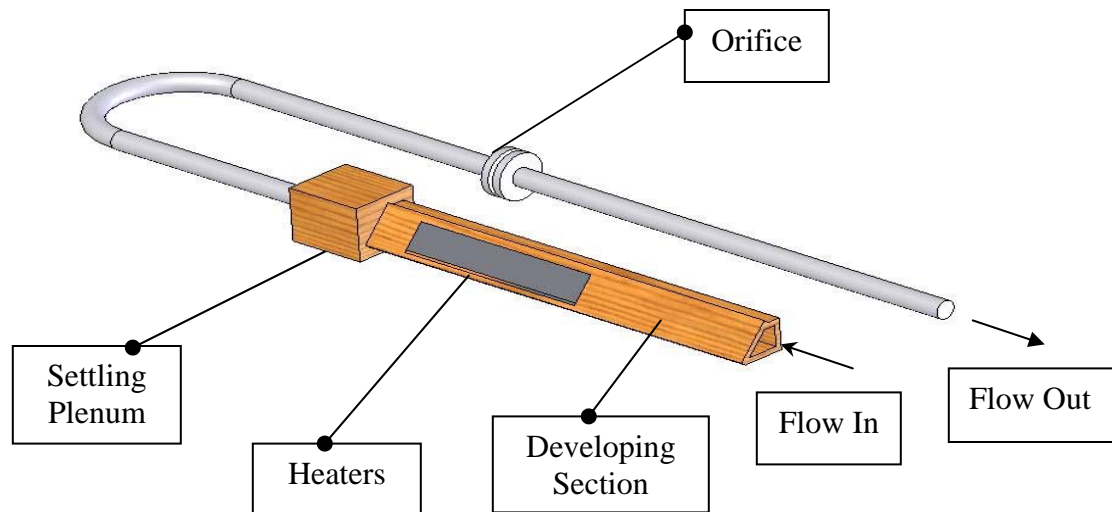
### **Methodology**

To study the heat transfer coefficient distribution along the internal passage of an aerofoil, a test section was constructed. The test section is 137.16 cm (54 in.) in length with a trapezoidal cross section whose parallel walls are 3.81 cm (1.5 in.) and 11.43 (4.5 in.) wide, and the other walls are 7.62 cm (3 in.) and 10.78 cm (4.2426 in.) wide, respectively as shown in Fig. 6. The first 60.96 cm (24 in.) of the test channel is used for developing a flow and the last 15.24 cm (6 in.) connects to the settling plenum. The remaining 60.96 cm (24 in.) in the middle is the actual test section with the parallel walls made of wood and the other walls made of aluminum wall segments.

One of the two aluminum wall is oriented at an angle of  $45^\circ$  with respect to the other. One of these walls is made of 16 identical aluminum wall segments of dimension 7.46 cm x 3.73 cm x 1.27 cm (2.938 in. x 1.469 in. x 0.5 in.). These wall segments are separated by balsa wood strips of thickness 0.159 cm (0.0625 in.) arranged in an array of 2 by 8. The opposite wall is again made of 16 identical aluminum wall segments but, of dimension 7.46 cm x 5.31 cm x 1.27 cm (2.938 in. x 2.09 in. x 0.5 in.) separated by balsa wood and arranged in a similar fashion. The balsa strips are glued to the wall segments

using silicon gel II to prevent conduction of heat from one wall segment to the other as shown in Fig. 7.

Two heaters are glued to the backside of the aluminum arrays to provide a uniform heat flux, which is used as heat input to the test section. The heat input to the two heaters was controlled independently by two variable transformers. Two thermocouples were installed in each wall segment to measure the average temperature of the wall segment. Holes of appropriate diameters were drilled at various locations and the thermocouples were inserted into the holes and glued using 5 min epoxy.



**Fig. 6 Schematic of Teat Apparatus for Average Heat Transfer Measurement**

The exit of the channel is connected to a settling plenum. An orifice is attached to the pipe to measure the flow rate through the channel. Pressure taps were installed across the test section and across the orifice to measure the respective pressure drop.



**Fig. 7 Schematic of Test Section with V-shaped Ribs**

Three additional thermocouples were installed to measure the temperature of air entering the channel, the exit air temperature, and the air temperature, immediately downstream



of the orifice. The output of all the thermocouple was recorded with a computer-controlled data acquisition system that uses hardware and LabView software from National Instruments, Inc.

The pressure drop across the orifice was measured with an inclined manometer and the drop across the test section was measured with micromanometer. The voltage and current are measured with a multimeter and an ammeter, respectively, product of which gives the power supplied to the two heaters and, in turn, the heat flux supplied to the test section.

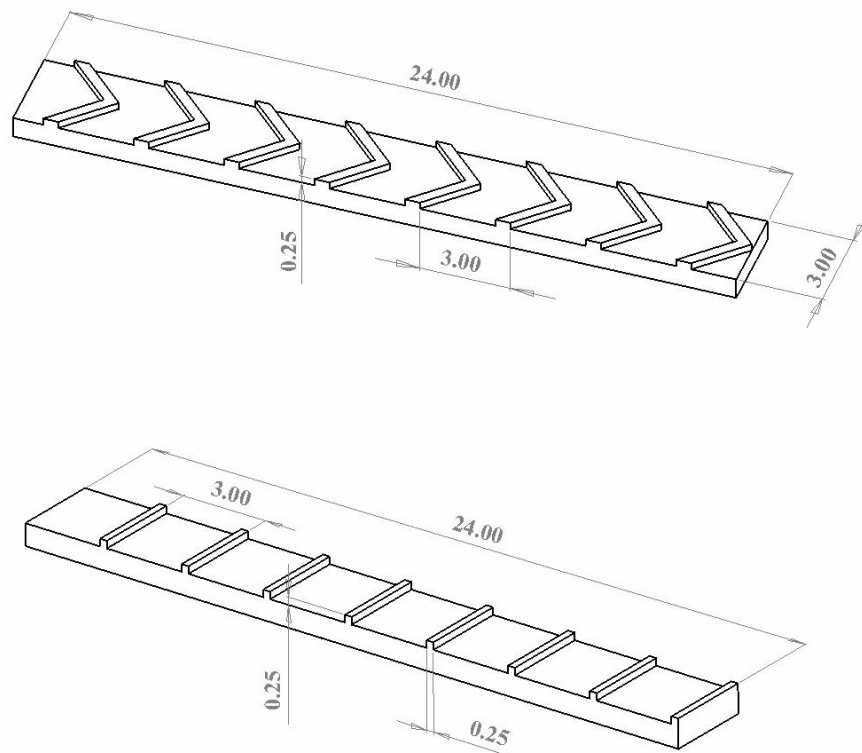
The ribs used for various cases are made of aluminum with dimensions 6.35 mm x 6.35 mm (0.25 in. x 0.25 in.). The pitch-to-height ratio was maintained at 12 and the height of the rib was approximately 9.25% of the channel hydraulic diameter. The ribs were machined to the required dimensions and angles and were glued to the slab at the required locations as shown in Fig. 8. The thickness of the glue was kept to a minimum so as to reduce the thermal resistance offered to the flow of heat.

A centrifugal pump of power 1.5 Hp was used to force the required amount of air through the duct and the exhaust from the pump was forced out through the hood. The pump was operated at two different speeds depending on the mass flow rate required. For safe operation of the pump at low Reynolds number a bypass valve is used to feed in air.

The experiment was run for 5 different Reynolds numbers ranging from 8,000 to 40,000. The variable transformers were adjusted in such a way that equal flux was

supplied through the aluminum wall segments and the average steady state temperature was maintained at around  $30^\circ$  over the ambient temperature so as to minimize the error.

The test section of model was insulated with fiberglass and other insulating material in order to minimize heat loss to the surrounding. Heat loss experiments were carried out in plugged flow condition, in order to evaluate the percentage heat loss to the ambience.



**Fig. 8 Rib Orientation**

The values of the average heat transfer coefficient and Nusselt numbers were calculated by reducing the data obtained and the results presented graphically and in tables are analyzed.

### Data Reduction

The heat transfer coefficient for the “i” wall segment was calculated using the net heat input to the wall; the wall temperature and the bulk mean temperature as

$$h_i = \frac{q_i}{A_{s,i}(\overline{T}_{w,i} - \overline{T}_{b,i})} \quad (3.1)$$

The actual heat going into the duct is given by the amount of power supplied which is the product of voltage applied and the current flowing in the circuit minus the amount of heat loss from each plate. The flexible heaters were assumed to supply uniform heat to all the slabs. The heat loss from the test section to the surrounding was calculated experimentally by conducting a no-flow condition. The heat loss to the surrounding was found to vary between 5-15% for various Reynolds number. The major heat loss was found to occur through the thick wired copper thermocouples installed in each wall segment.

The Nusselt number was normalized using the Nusselt number correlation for a fully developed flow in a smooth circular channel. The relative uncertainty on Nusselt number was found to be 5%.

$$\frac{Nu}{Nu_o} = (hD_h/k) / [0.023Re^{0.8}Pr^{0.4}] \quad (3.2)$$

All the temperatures were measured using the thermocouples. The bulk mean air temperature at the inlet and the exit was measured using the thermocouples and the bulk mean temperature at the end of each plate was calculated using the formula given by

$$T_{b,out} = T_{b,in} + \frac{q}{\dot{m}c_p} \quad (3.3)$$

The pressure drop measured with a micromanometer across the test section, was used to calculate the friction factor. The relation between pressure drop and friction factor is given by

$$f = \frac{\left(\frac{\Delta p}{\Delta x}\right) D_h}{\frac{\rho \bar{u}^2}{2}} = 2\rho \left(\frac{\Delta p}{\Delta x}\right) D_h \left(\frac{A_c}{\dot{m}}\right)^2 \quad (3.4)$$

The friction factor is normalized by Gnielinski equation

$$f_o = [0.79 \ln(Re_{D_h}) - 1.64]^{-2} \quad (3.5)$$

The correlation for thermal performance is given by

$$TP = (\overline{Nu}/Nu_o) / (\bar{f}/f_o)^{1/3} \quad (3.6)$$

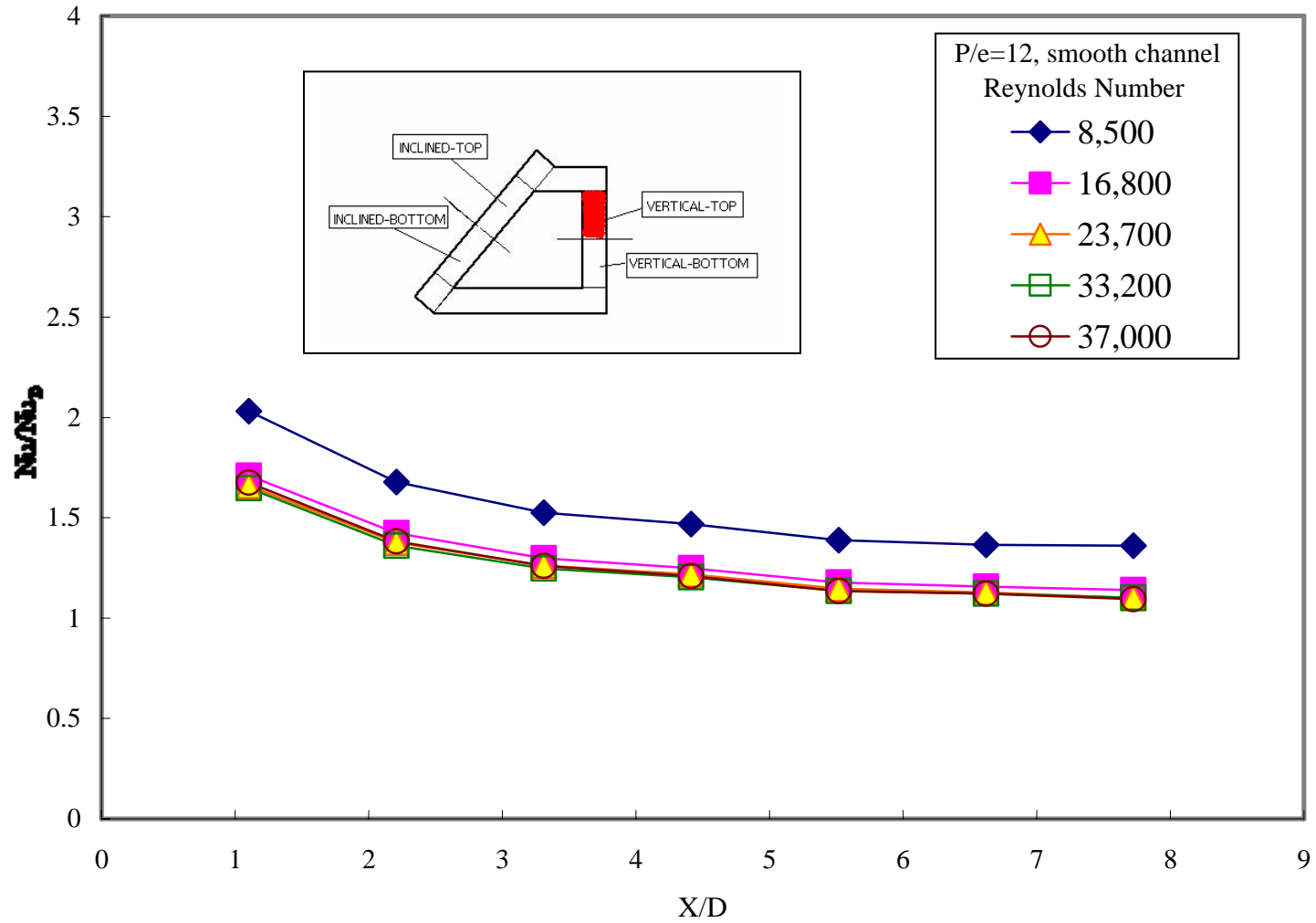
## RESULT AND DISCUSSION

### Heat Transfer Distribution in Smooth Channel

The average heat transfer results for a smooth channel at four different walls are represented as the streamwise distribution of a normalized Nusselt number in Figs. 10-13. The Nusselt number was normalized with the Nusselt number for fully developed turbulent flow in smooth circular tube correlated by McAdams/Dittus-boelter. The Nusselt number ratios at all four cases was found to decrease with increasing axial distance and finally reaches a constant value where, normalized axial distance  $X/D_h$  is greater than four and the flow becomes fully developed for a given Reynolds number.

The maximum uncertainty in the Nusselt number ratios was found to be 5% and the deviation of the Nusselt Number from the McAdams/Dittus Boelter correlation was found to be 15%-20% for the smooth channel. The average Nusselt number was calculated as a mean of Nusselt numbers corresponding to values of  $X/D_h$  between 2.2 and 7.7, corresponding to the developed region.

The Nusselt number was found to increase on all the four walls with increasing Reynolds number. The reason attributed to this behavior is as Reynolds number increases the turbulent mixing is enhanced in the channel which leads to effective removal of heat. However, the Nusselt number ratio which is obtained by normalizing the average Nusselt number with the fully developed turbulent flow in smooth circular tubes correlated by McAdams/Dittus Boelter was found to decrease as shown in Fig. 14.



**Fig. 10 Effect of Reynolds Number on Heat Transfer Distribution on Vert-Top Wall in Smooth Channel**

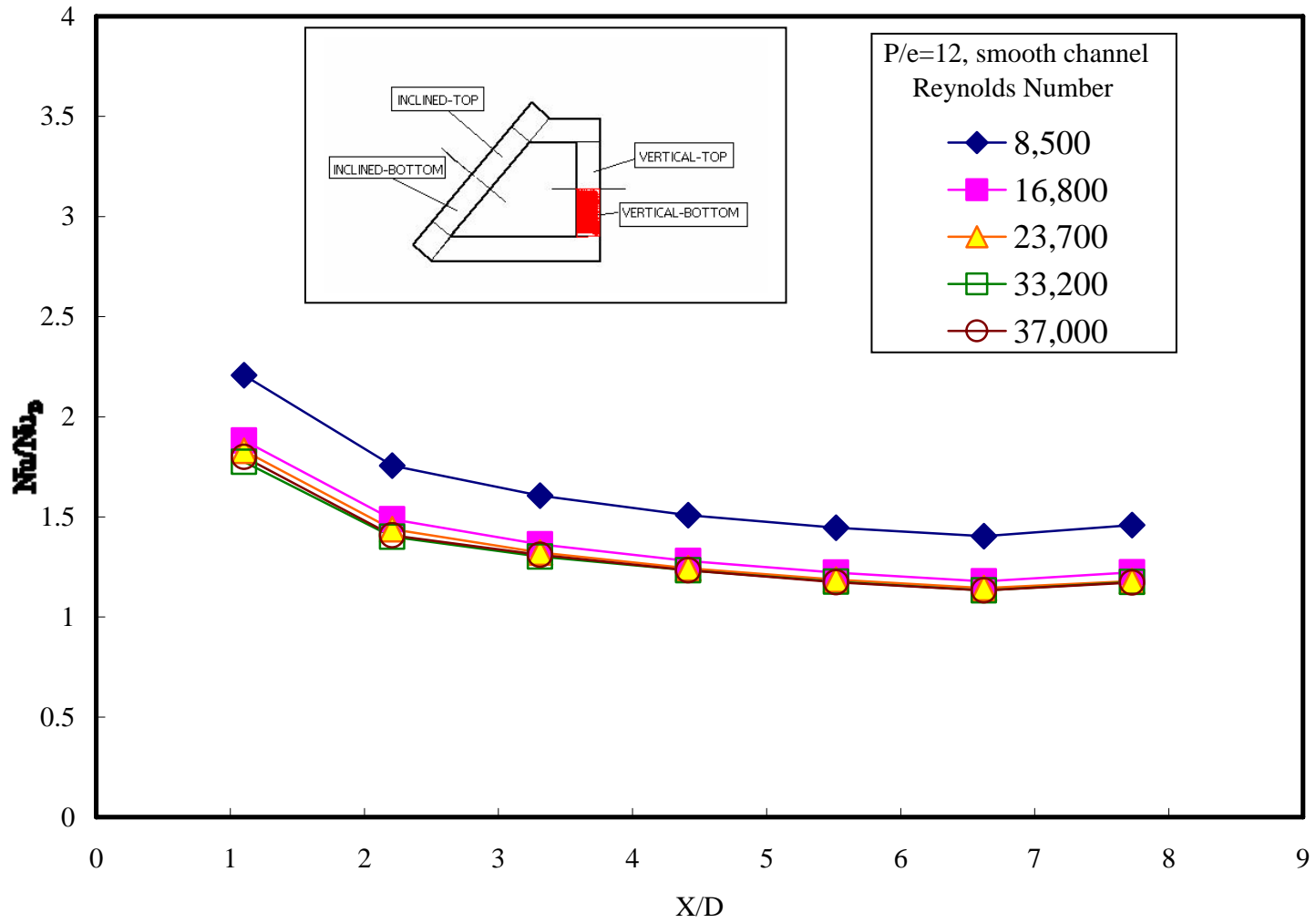


Fig. 11 Effect of Reynolds Number on Heat Transfer Distribution on Vert-Bot Wall in Smooth Channel

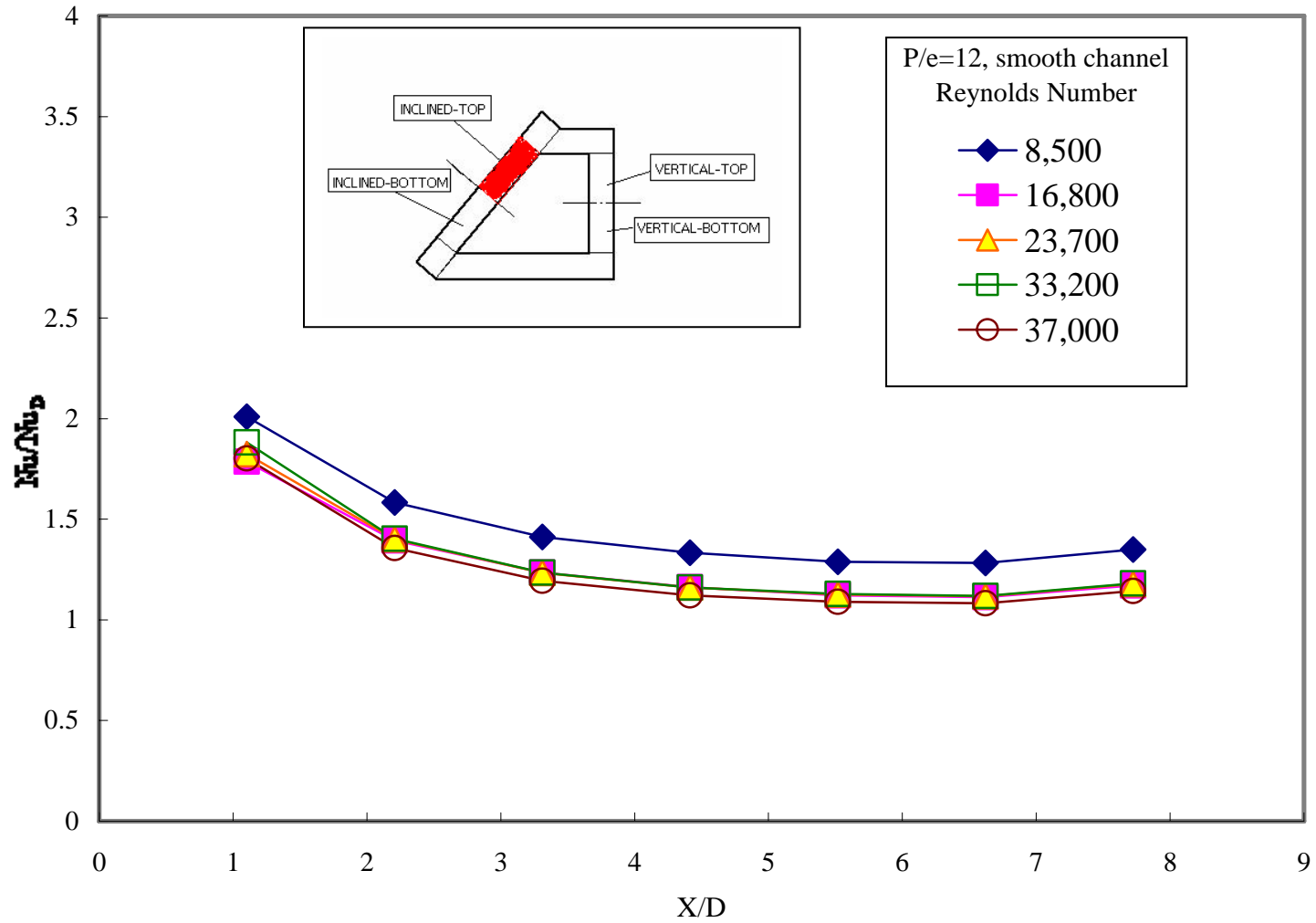
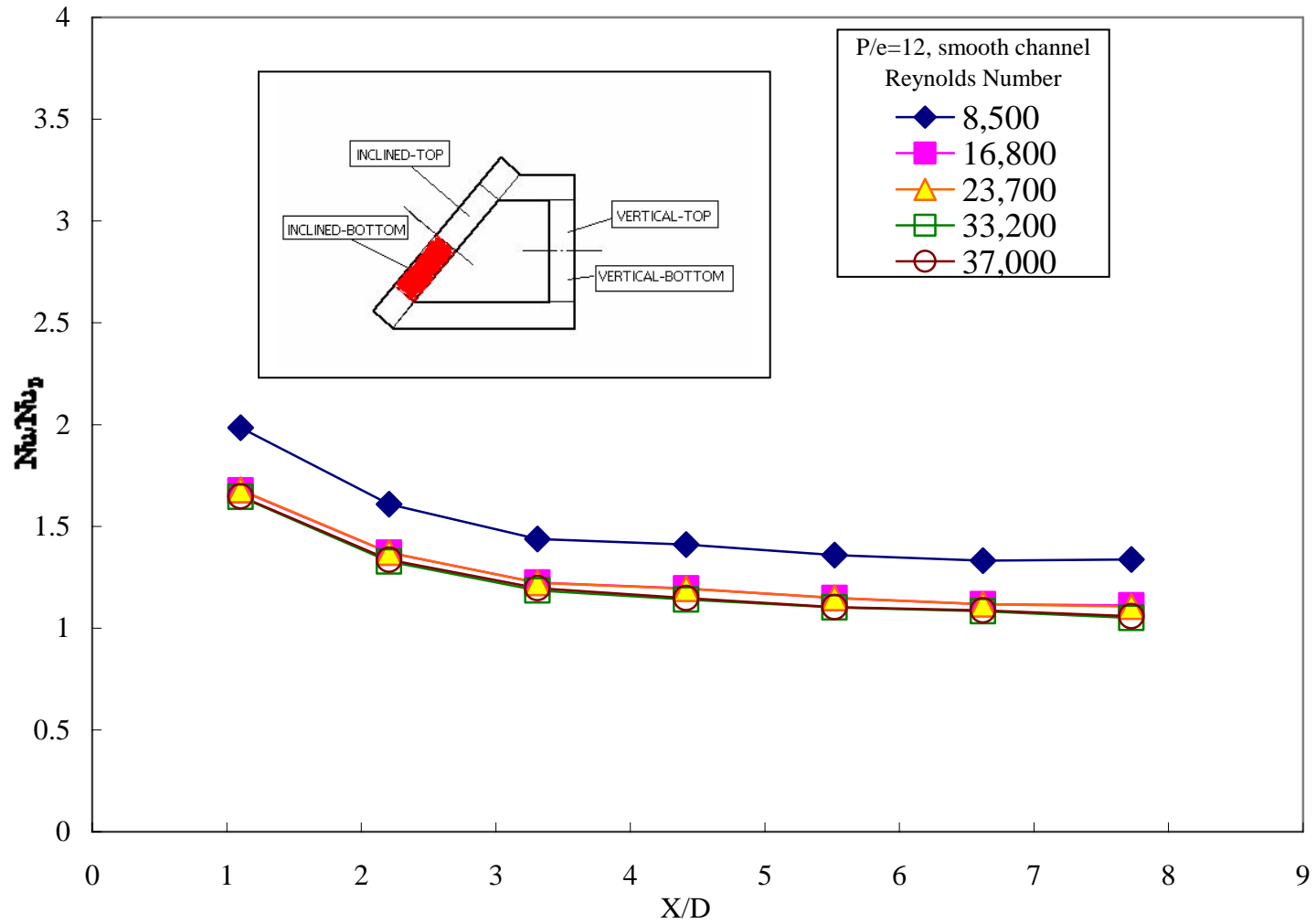


Fig. 12 Effect of Reynolds Number on Heat Transfer Distribution on Inc-Top Wall in Smooth Channel





**Fig. 13 Effect of Reynolds Number on Heat Transfer Distribution on Inc-Bot Wall in Smooth Channel**

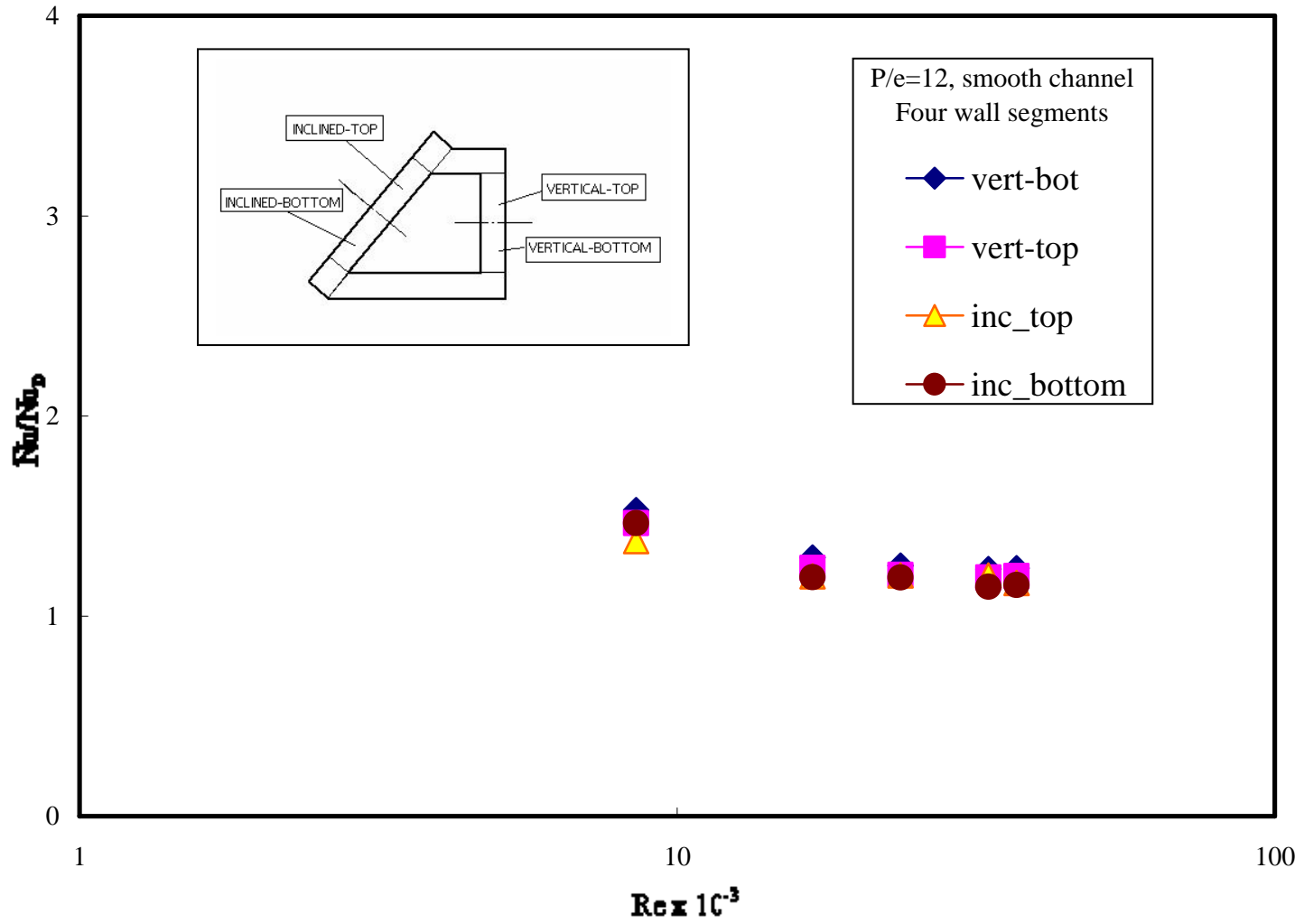


Fig. 14 Average Nusselt Number Ratio versus Reynolds Number on the Two Walls in Smooth Channel

The Nusselt number was found to vary from 38 to 100 and the Nusselt number ratio was found to vary from 1.1 to 2.25. The results were found to match with results obtained by Han [10] for the square channel.

In the case of smooth channel the variation of Nusselt number ratio with increasing Reynolds number is very small as there is no flow separation and reattachments in this case and so Reynolds number does not have any effect on the heat transfer augmentation. Therefore, the Nusselt number ratio for all five Reynolds number follow a similar trend on all the four walls. The Nusselt number ratio was found to approach unity along the streamwise direction in the fully developed region. The Nusselt number ratio was found to be highest for the lowest Reynolds number and lowest for the highest Reynolds number. It was found to vary between 2.25 and 1.1 along the axial direction. A variation of 5% in average Nusselt number was observed in the transverse direction on both the walls and the variation in average Nusselt number on all the four walls was found to be less than 10%.

Fig. 9 shows the graphical notation used to describe the walls in the test section. Each of the two aluminum walls consists of two rows of wall segments one at the top and the other at the bottom represented as VERT-TOP and VERT-BOT for one of the walls and INC-TOP and INC-BOT for the other wall inclined at  $45^\circ$ .

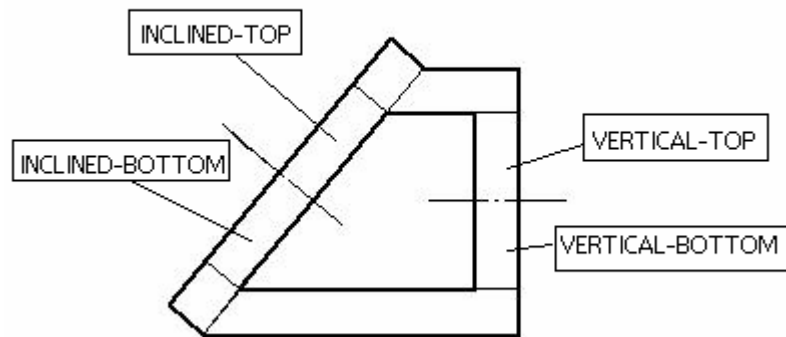


Fig. 9 Graphical Notation Used

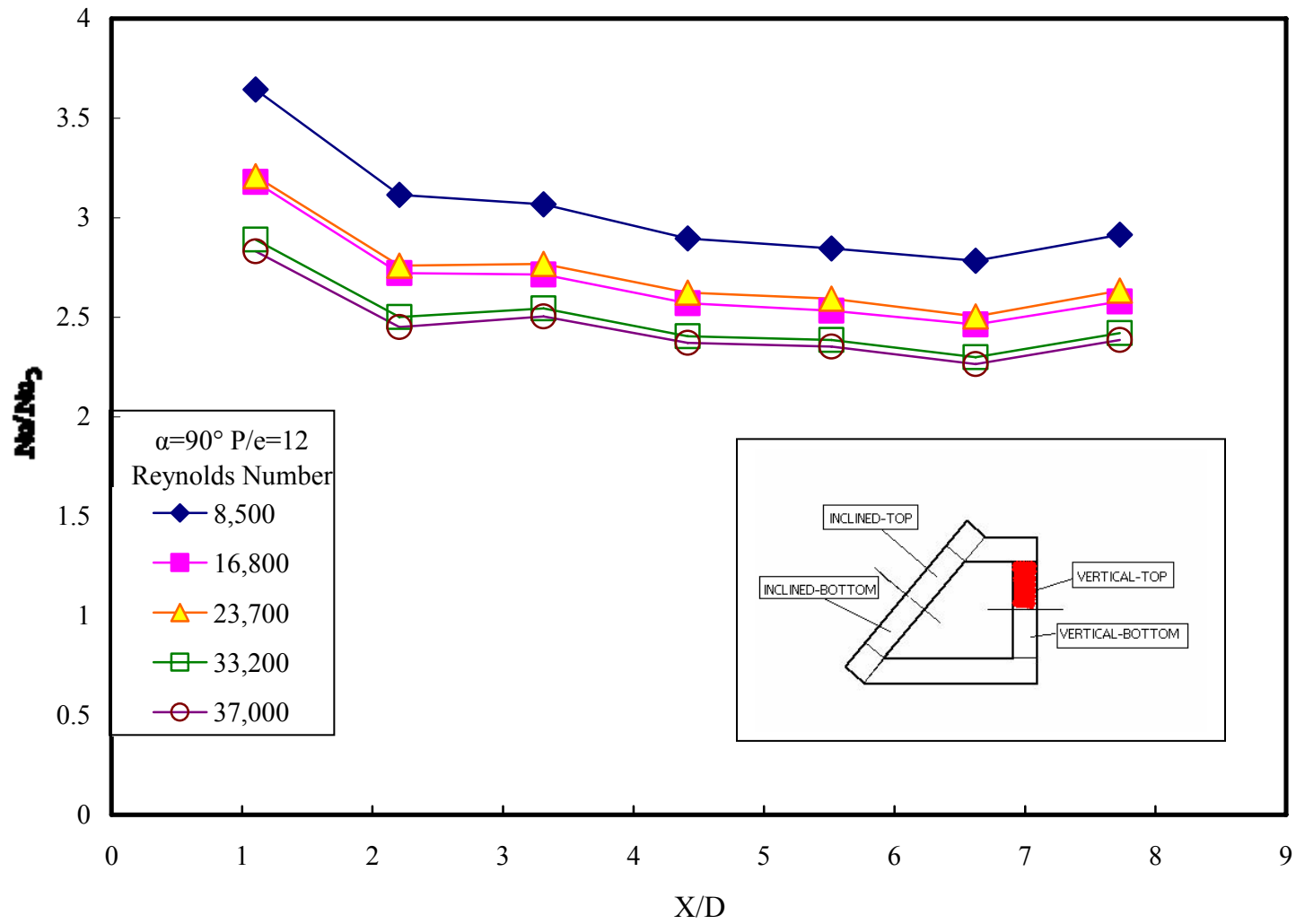
### **Heat Transfer Distribution in Channel with 90° Transverse Ribs**

The heat transfer and friction characteristic was studied for the same channel ribbed with 90° transverse ribs. The  $P/e$  ratio was maintained at 12 and was tested for five different Reynolds numbers. It was once again seen that Nusselt number ratio decreases with increase in axial distance and attains a constant value in the fully developed region as shown in Figs. 15-18.

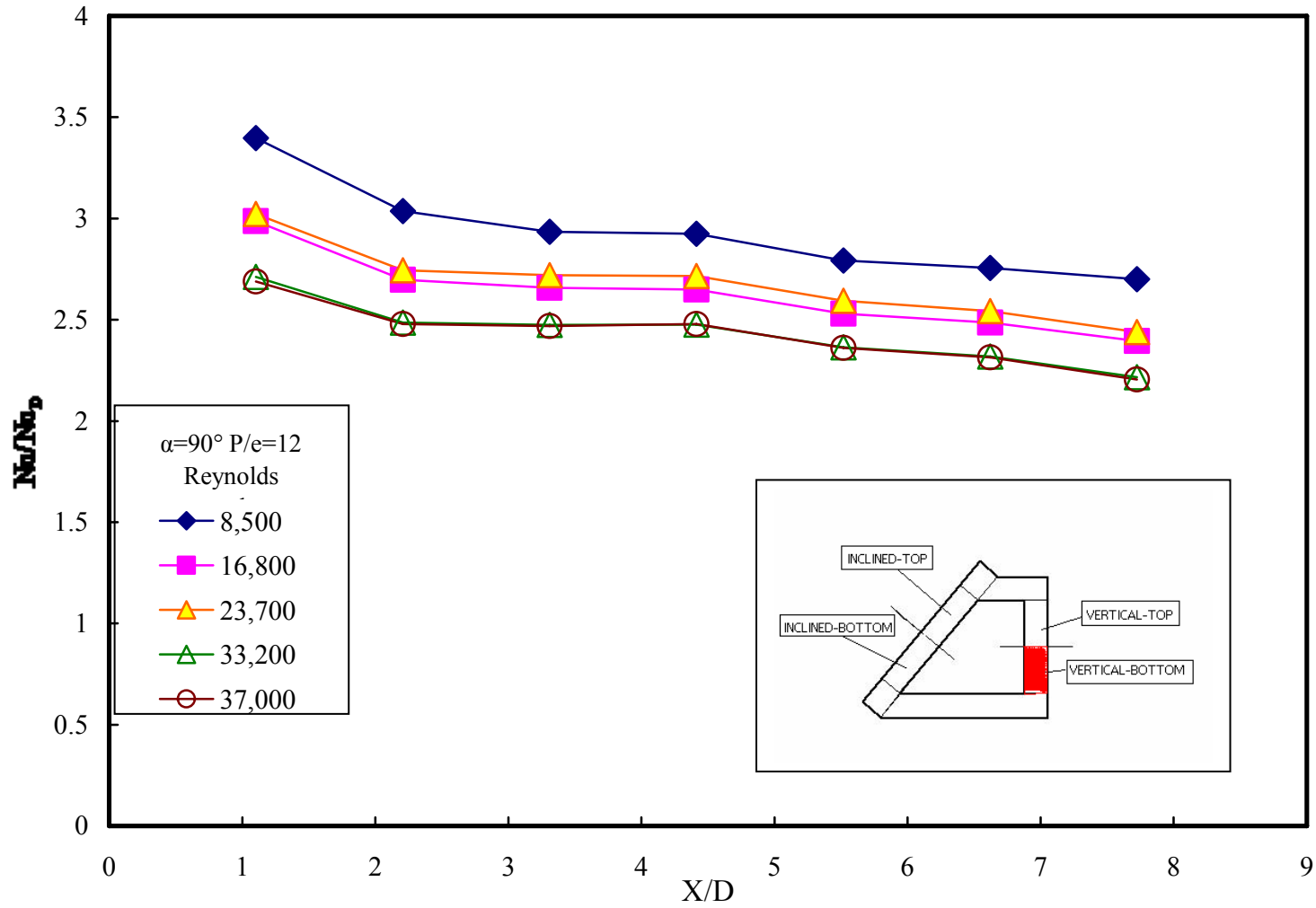
The trend in Nusselt number ratio obtained was found to be similar to that of a smooth channel, except that there was 5%-15% fluctuation in the data obtained. The heat transfer augmentation at all Reynolds resulted in a 1.85-2.20 fold increase in comparison to the smooth channel.

The increase in heat transfer augmentation is due to the induced flow separation followed by reattachment by the ribs. The flow separation was thought to occur at the ribs and reattach downstream at about 6-8 times the rib height from the rib. It is also thought that a reverse flow boundary originates at the reattachment point and grows in thickness till the next flow separation occurred.

The Nusselt number variation in the transverse direction on the straight wall was less than 2% for the complete range of Reynolds number. In the case of inclined wall the variation in the Reynolds number was in the range of 7.5%-10%. On inclined wall the bottom wall had a lower heat transfer coefficient. This is probably due to the accumulation of hot fluid at the sharp corner of the trapezoid which prevents entry of cool fluid. This suppresses the effect created by flow separation at the ribs. Thus, giving rise to a larger variation in the Reynolds number on the inclined wall. This behavior was



**Fig. 15 Effect of Reynolds Number on Heat Transfer Distribution on Vert-Top Wall in Transverse Ribbed Channel**



**Fig. 16 Effect of Reynolds Number on Heat Transfer Distribution on Vert-Bot Wall in Transverse Ribbed Channel**

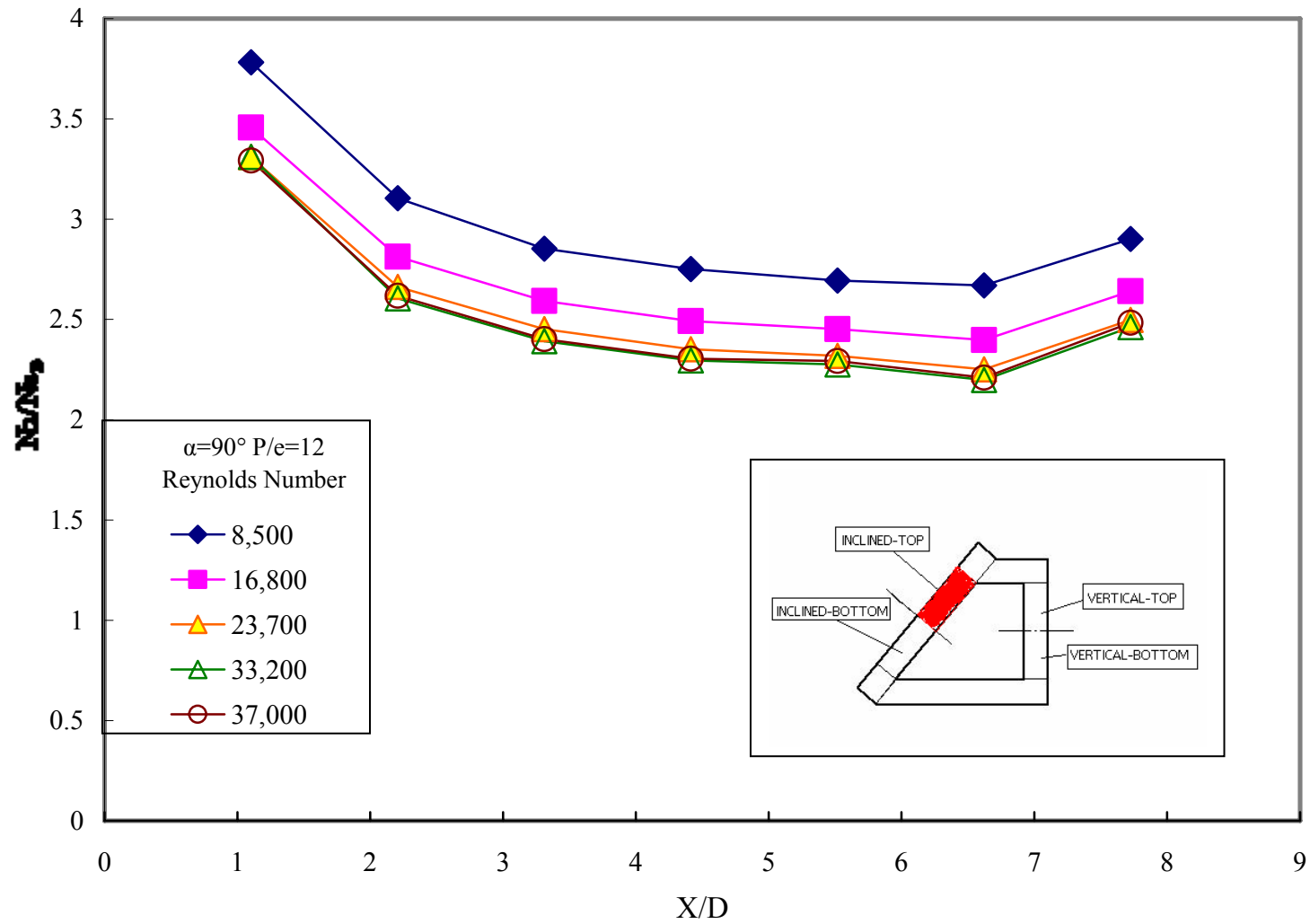
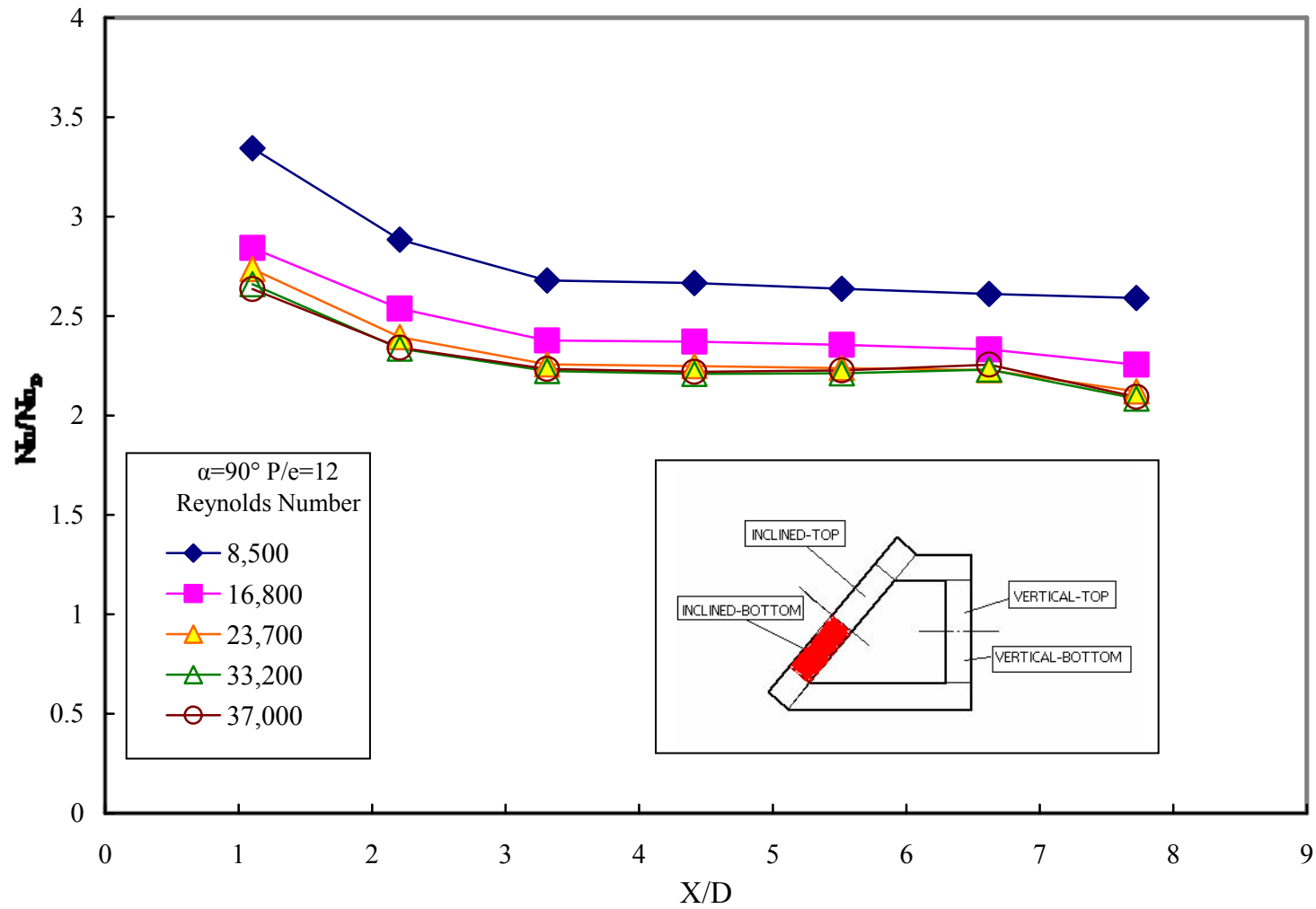
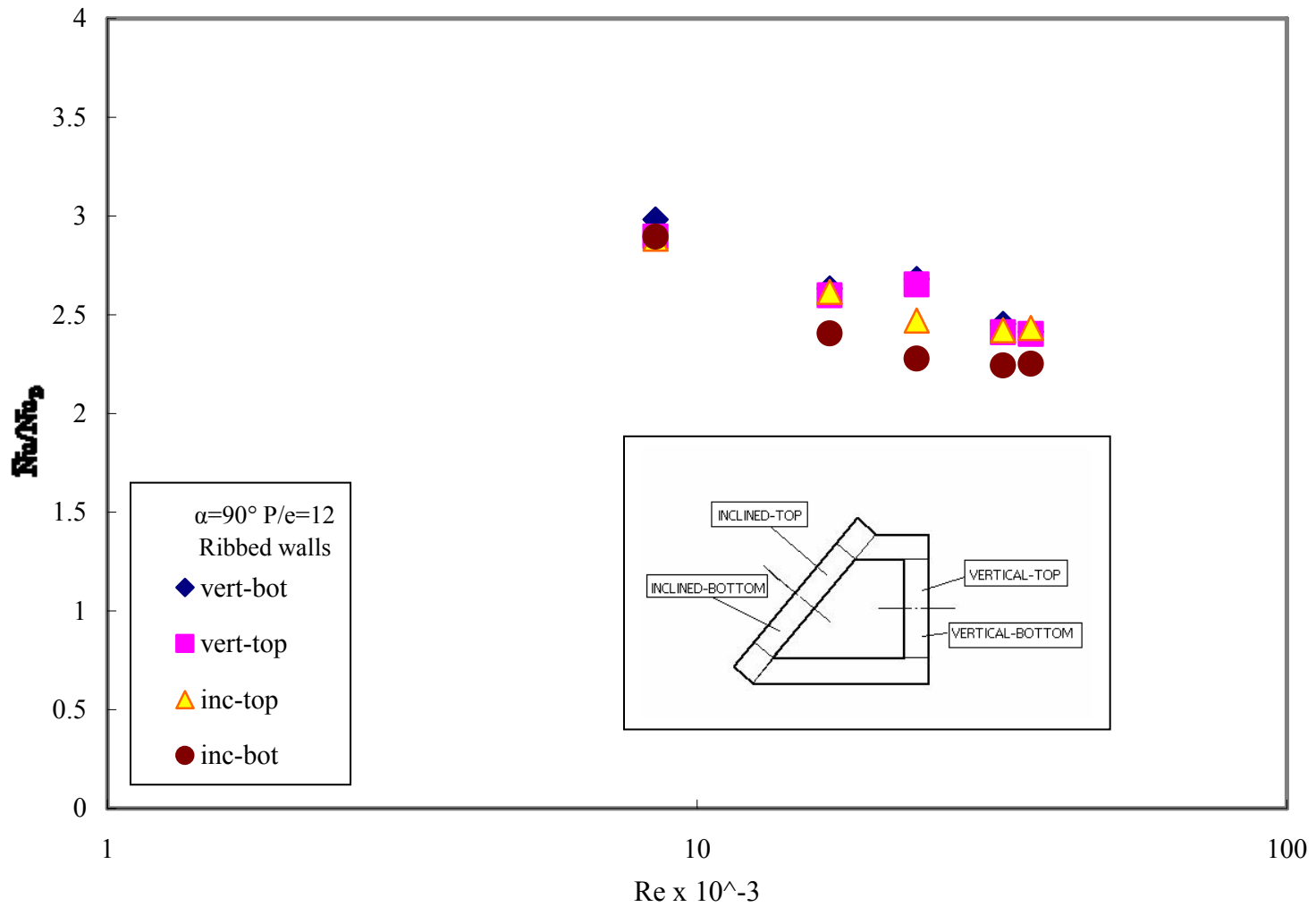


Fig. 17 Effect of Reynolds Number on Heat Transfer Distribution on Inc-Top Wall in Transverse Ribbed Channel





**Fig. 18 Effect of Reynolds Number on Heat Transfer Distribution on Inc-Bot Wall in Transverse Ribbed Channel**



**Fig. 19 Average Nusselt Number Ratio versus Reynolds Number on Two Walls in Transverse Ribbed Channel**

also found in triangular channel by Metzger et al. [5]. It was also found that the geometry had a significant effect on the heat transfer coefficients on the four walls which resulted in 10-15 variation in the heat transfer among them because the bulk flow seemed to prefer the wider section as studied by Taslim [21].

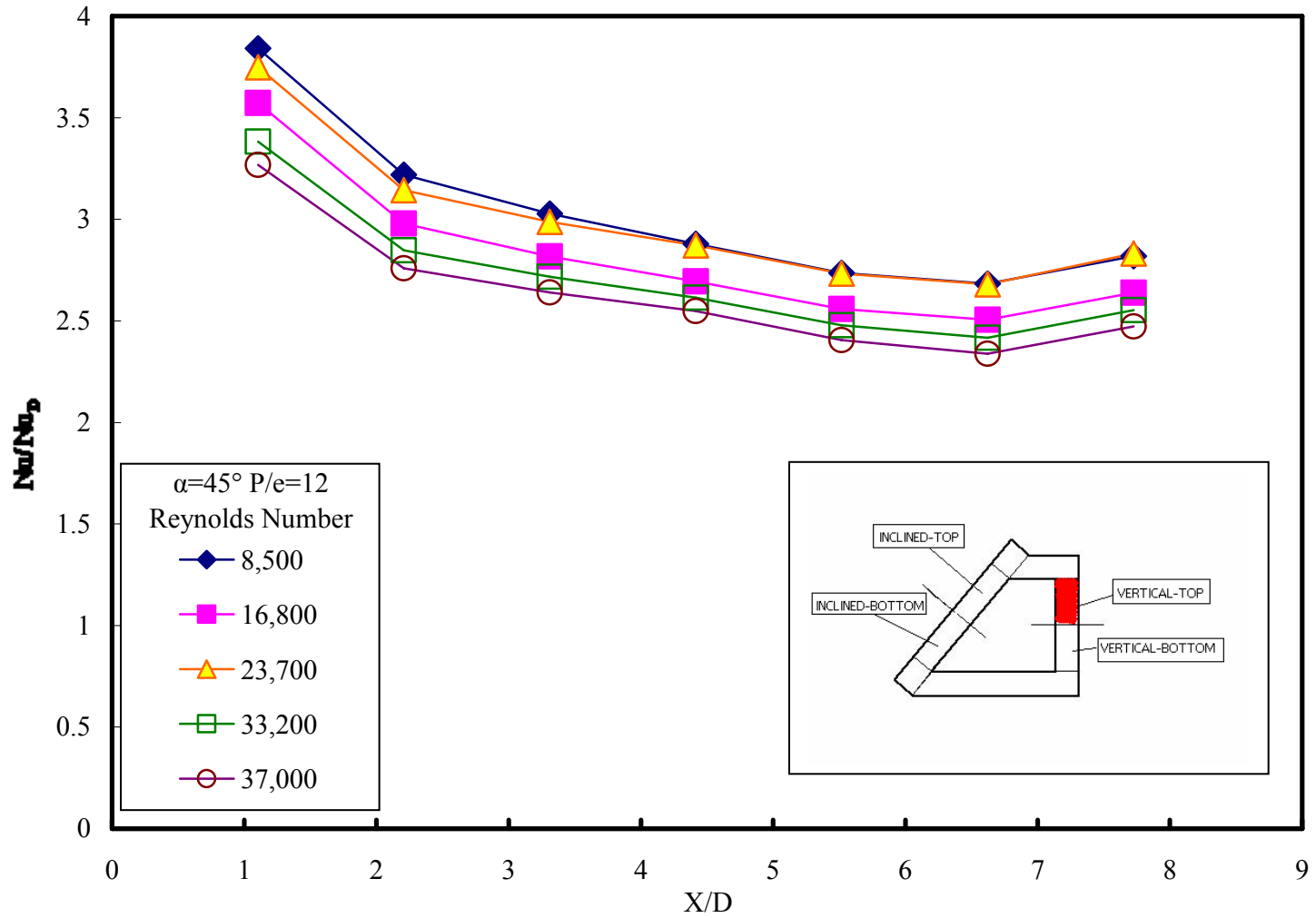
The average Nusselt number on all four wall was wound to increase with increase in Reynolds number which is caused from better turbulence mixing. The increase in Reynolds number also causes an increase in the unsteady reverse flow just behind the rib which helps in better mixing. However, the Nusselt number ratio decreased appreciably with increase in Reynolds number as shown in Fig. 19. This is due to the fact that as Reynolds number increases the flow tends reattach quickly and so the effect on the heat transfer coefficient is considerably reduced. The study conducted by Liou et al. [12] showed that the increase in Nusselt number in a ribbed channel is proportional  $Re^{0.6}$ , whereas, in the case of fully developed turbulent flow in smooth circular tube correlated by McAdams/Dittus Boelter, the Nusselt number is proportional to  $Re^{0.8}$ . Therefore the rate of increase in Nusselt number in ribbed channel is less than that in smooth channel which results in the decrease of Nusselt number ratio with increase in Reynolds number.

The heat transfer augmentation in case of  $90^\circ$  transverse ribs was found to be 100% more than that in a smooth channel for the complete range of Reynolds number. The uncertainty of Reynolds number was found to be close to 2% and that of the Nusselt number was found to be around 5%. The values were found to be within the uncertainty limit.

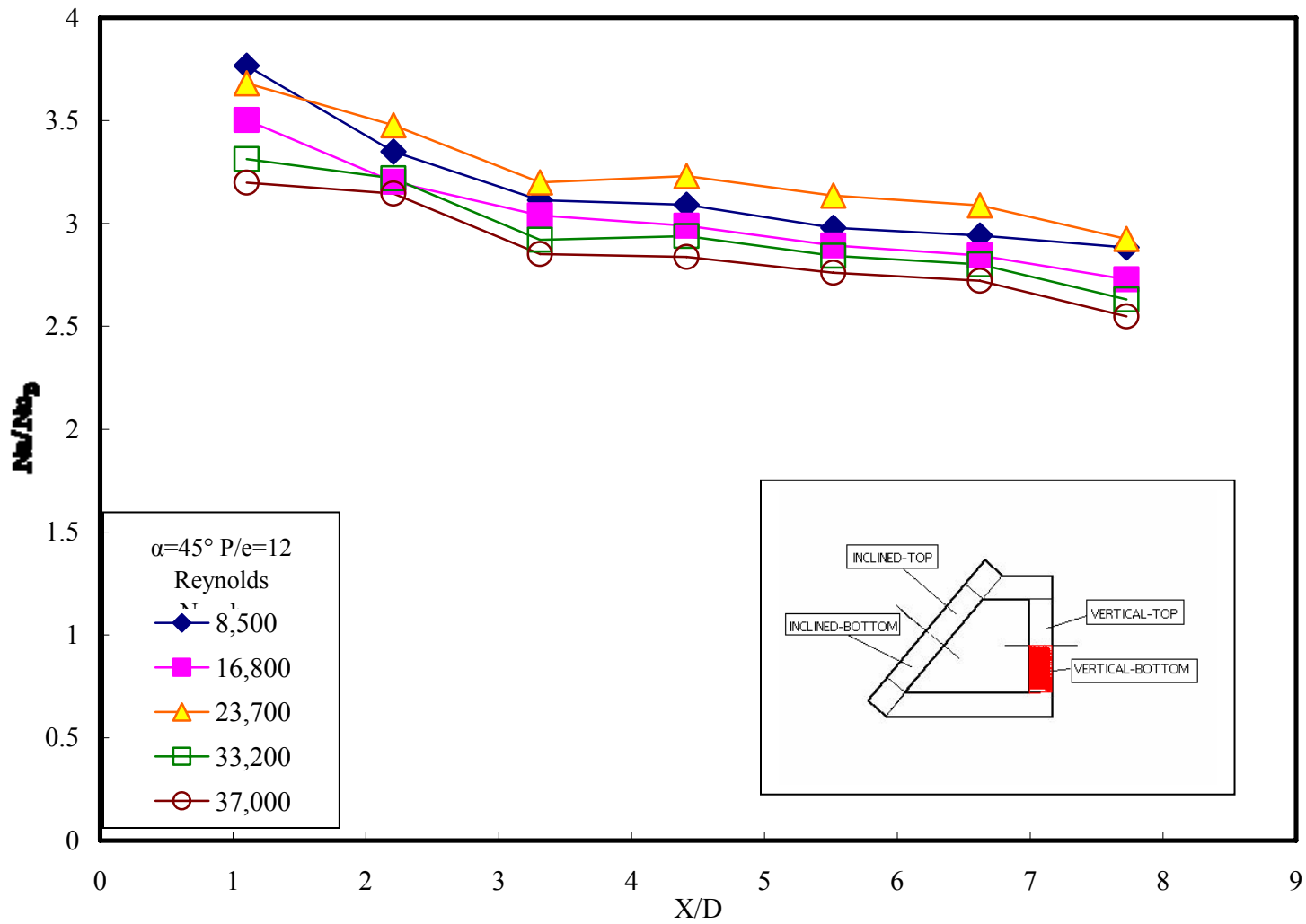
### **Heat Transfer Distribution in V-shaped Ribbed Channel**

The heat transfer distribution on the trapezoidal channel with V-shaped ribs at  $45^\circ$  was studied and the characteristic curves were plotted as shown in Figs. 20-23. It was seen that the Nusselt number ratio along the stream wise direction behaved very similar to that in a square channel and channel ribbed with transverse ribs. The fluctuation in Nusselt number ratio was found to vary between 5%-20%. The heat transfer augmentation was found to increase by factor of 1.9 to 2.3 in comparison to the smooth channel and by a factor of 1.09 to 1.23 in comparison to the transverse ribbed channel. The increase in heat transfer coefficient is attributed to the induction of cross stream secondary flow which results in better turbulent mixing. The V-shaped ribs were also found to produce lesser pressure drop than the transverse ribs.

The Nusselt number ratio variation in the transverse direction on the straight walls was found to increase for 5% to 11% with increase in Reynolds number. However, the variation in the inclined wall was found to be less than 6%. In both cases the heat transfer from the top wall was more than the bottom wall. The reason for this trend could be attributed to higher density of secondary flow near the top walls in comparison to that of the bottom wall which are separated by a greater distance than the top walls.



**Fig. 20 Effect of Reynolds Number on Heat Transfer Distribution on Vert-Top Wall in V-shaped Ribbed Channel**



**Fig. 21 Effect of Reynolds Number on Heat Transfer Distribution on Vert-Bot Wall in V-shaped Ribbed Channel**

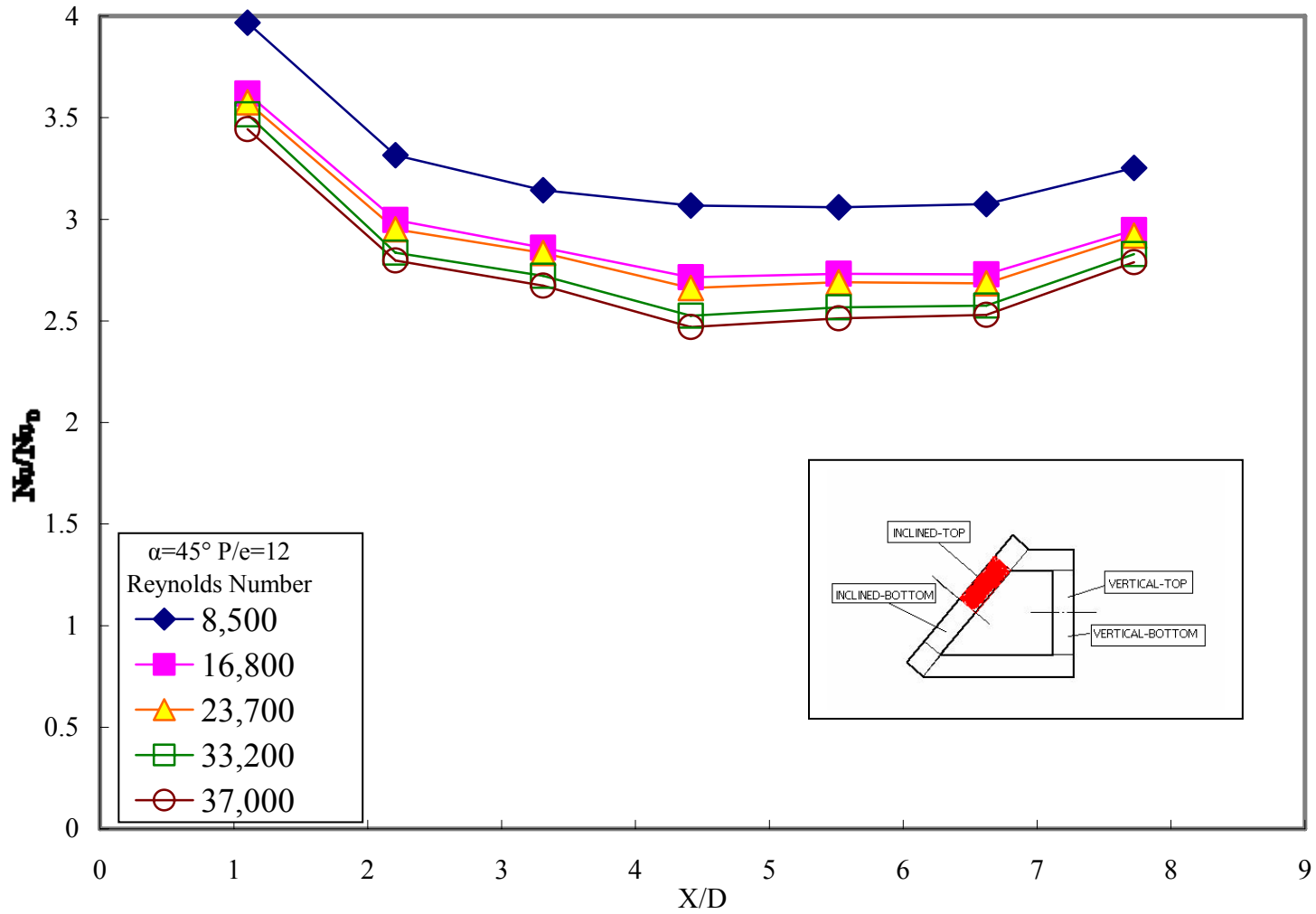


Fig. 22 Effect of Reynolds Number on Heat Transfer Distribution on Inc-Top Wall in V-shaped Ribbed Channel

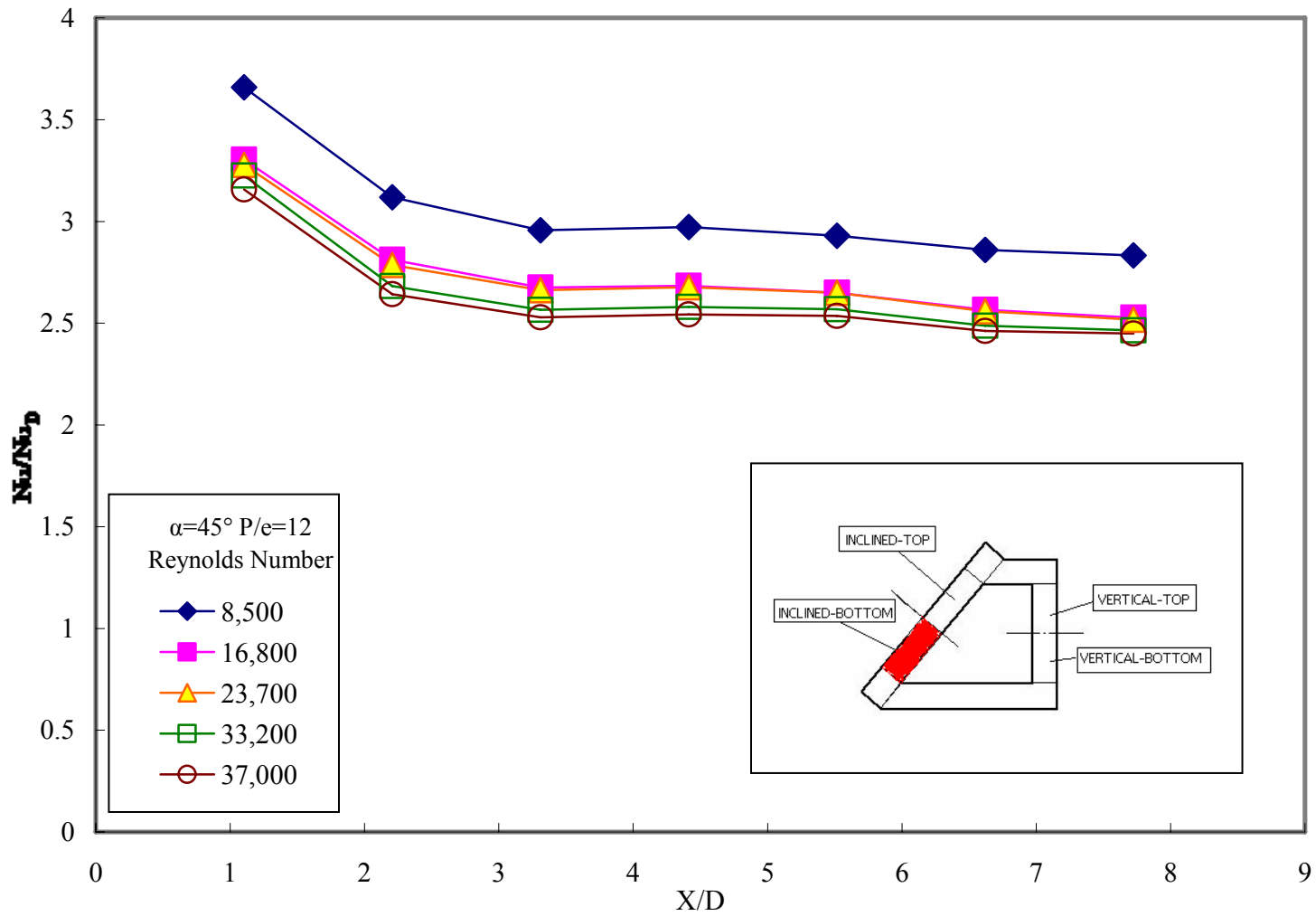


Fig. 23 Effect of Reynolds Number on Heat Transfer Distribution on Inc-Bot Wall in V-shaped Ribbed Channel



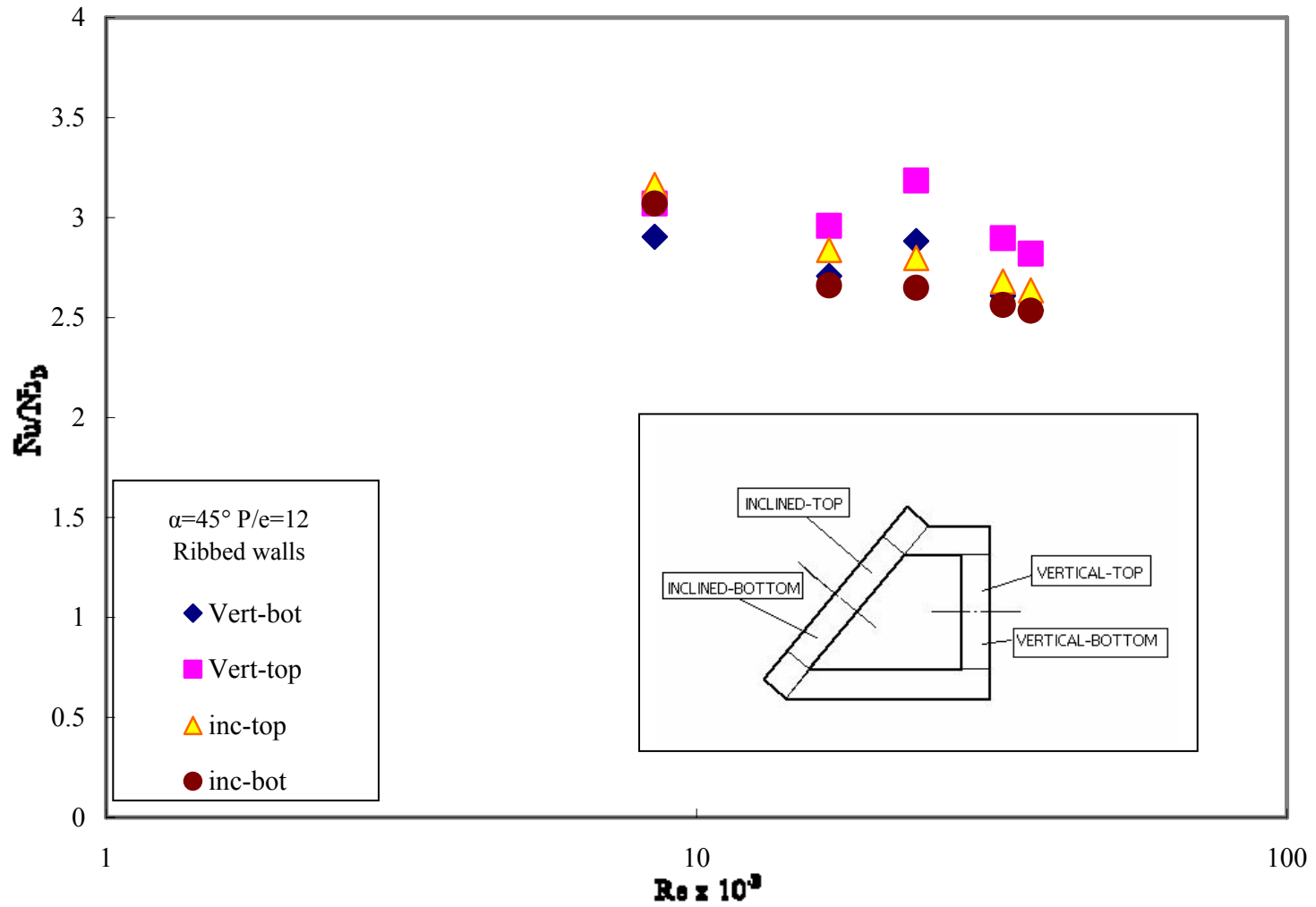


Fig. 24 Average Nusselt Number Ratio versus Reynolds Number on the Two Walls in V-shaped Ribbed Channel

The variation in Nusselt number in transverse direction in the inclined wall was found to be less than that in the straight wall is due to better turbulent mixing near the bottom wall on the inclined wall caused from the combination of cross stream secondary flow created by the V-shaped ribs and the flow separation at the ribs in comparison to the 90° transverse ribbed channel. However, the low Nusselt number on the bottom wall on the inclined side could be due to the reflection of secondary flows from the adjacent wall and accumulation of hot fluid in the sharp corner of the trapezoid which suppresses the effect of secondary flow caused from the ribs.

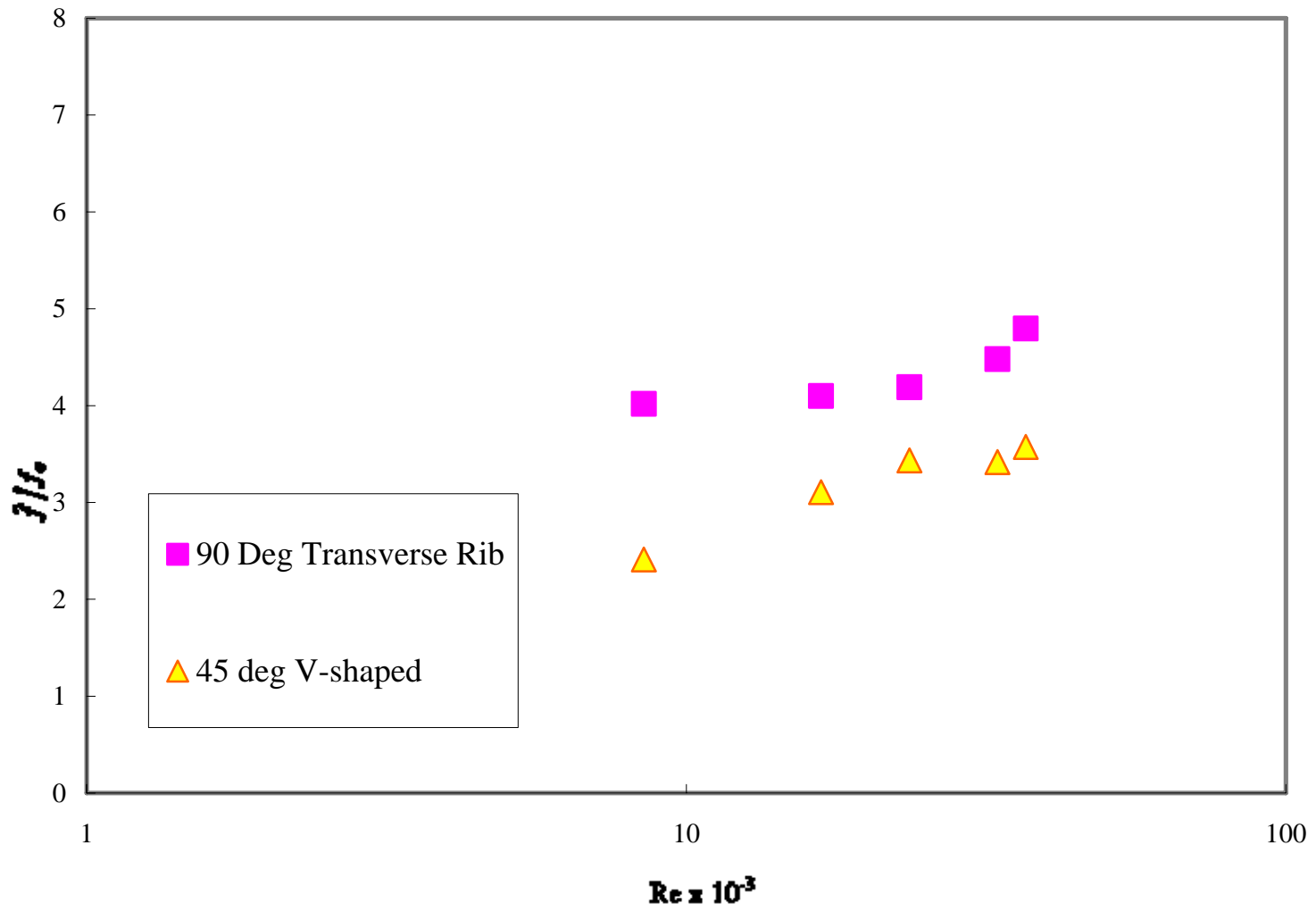
The average Nusselt number was once again found to decrease with increase in Reynolds number as shown in Fig. 24. As discussed in the earlier case, the rate of increase in Nusselt number with Reynolds number in ribbed channel is less than that in smooth channel because the mean flow energy is converted to turbulent kinetic energy which induces better mixing and in turn effective heat transfer. However, at low Reynolds number where the flow rate is low, there is no appreciable difference in the heat transfer augmentation in the four plates for both the ribbed configurations.

### Friction Factor Characteristics for Various Rib Configurations

Figure 24 shows the variation of friction factor with Reynolds number for the smooth channel and the two ribbed channel investigated. The friction factor ratio was found to increase with increase in Reynolds number due to the resistance offered to the flow of fluid as given in Table 1. The heat transverse augmentation was found to vary between 2-2.5 for the transverse rib and 2.5-3 for the V-shaped rib. This enhancement in both the cases was accompanied by pressure drop penalty of 2.5 to 4 on the V-shaped ribbed channel and 4 to 5 on the 90° transverse ribbed channel. The 90° transverse ribs produced 25 % to 60% higher pressure drop when compared to the V-shaped ribs at 45° for the complete range of Reynolds number investigated. The results obtained were in accordance with previously obtained data by Chandra [19].

**Table 1 Friction Factor Ratio for Cases Investigated**

Reynolds Number	Transverse Ribs	V-shaped Ribs
8,500	4.018	2.410
16,800	4.100	3.106
23,700	4.189	3.434
33,200	4.479	3.416
37,000	4.796	3.573



**Fig. 25 Average Friction Factor Ratio versus Reynolds Number for Various Rib Configurations**

## Heat Transfer Performance

The thermal performance comparison for different rib configuration on the four walls was plotted as shown in Figs. 25-28. The Nusselt number ratio was plotted against the friction factor ratio for the entire range of Reynolds number. As discussed in the earlier section the Nusselt number ratio decreased with increase in Reynolds Number, whereas the friction factor ratio increased with increase in the Reynolds number. From this it is deduced that the performance decreases with increase in Reynolds number.

The thermal performance is also represented in Table 2-3 on different wall segments using thermal performance correlation for various Reynolds number. It was once again seen that the performance decreased with increase in Reynolds number. It was also noted that on all the four wall segments the thermal performance for the smooth channel was increasing with increasing Reynolds number in comparison to the ribbed channel. This is due to the higher rate of increase in friction penalty, in turn, the pump power with increase in the Reynolds number in comparison to the heat transfer augmentation.

The heat transfer enhancement for the 90° transverse ribs was found to be carrying at 2.25 to 2.75 on the four walls and the pressure drop penalty was found to vary between 4 and 5. In the case of the V-shaped ribs the heat transfer enhancement was found to be ranging from 3.25 to 25 and the friction factor ratio was between 2 and 4.

It is found that there is only small lateral variation in the heat transfer on the straight wall whereas the variation on the inclined wall was found to be around 15% in

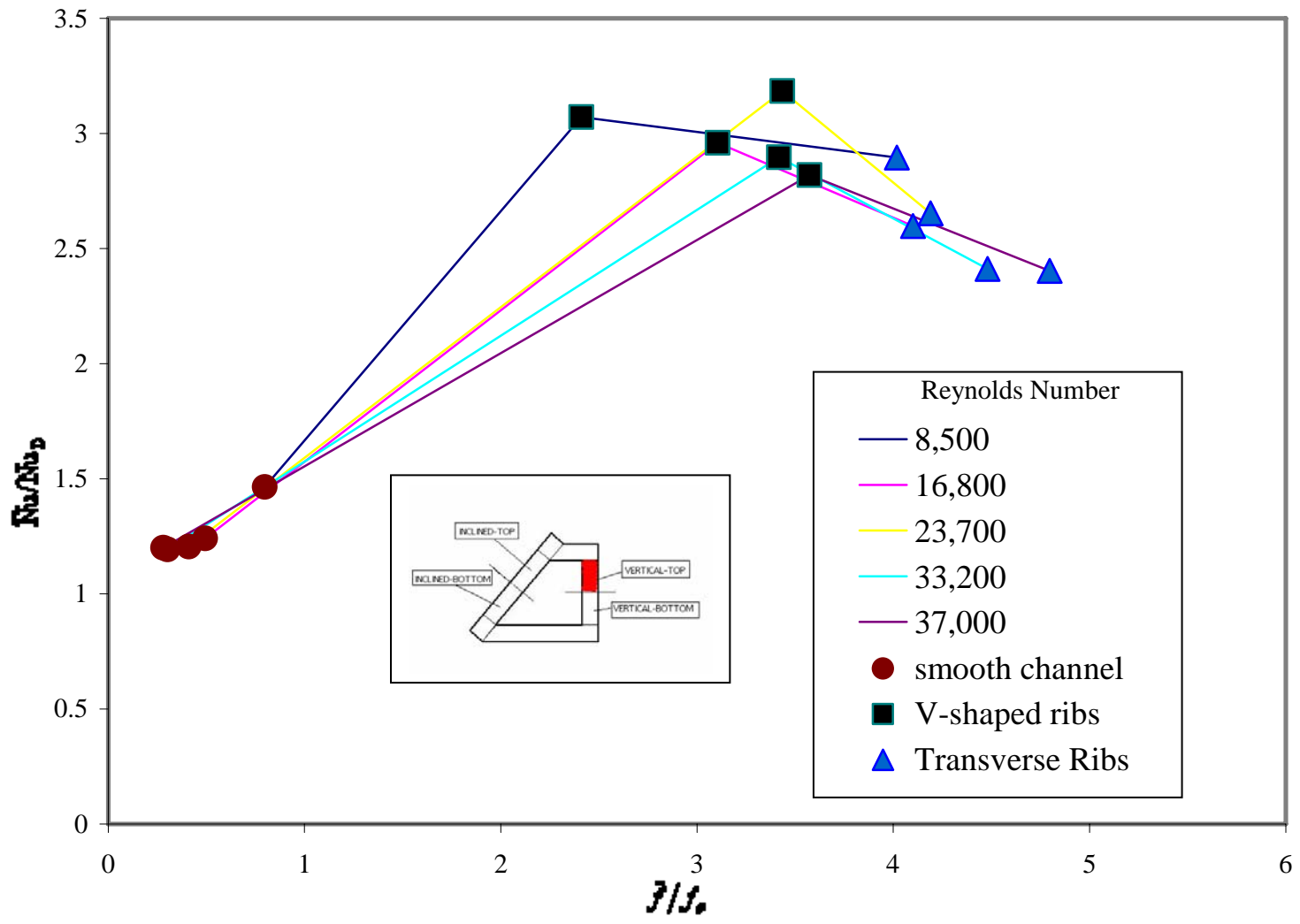


Fig. 26 Average Nusselt Number Ratio versus Friction Factor Ratio for Vert-Top Wall

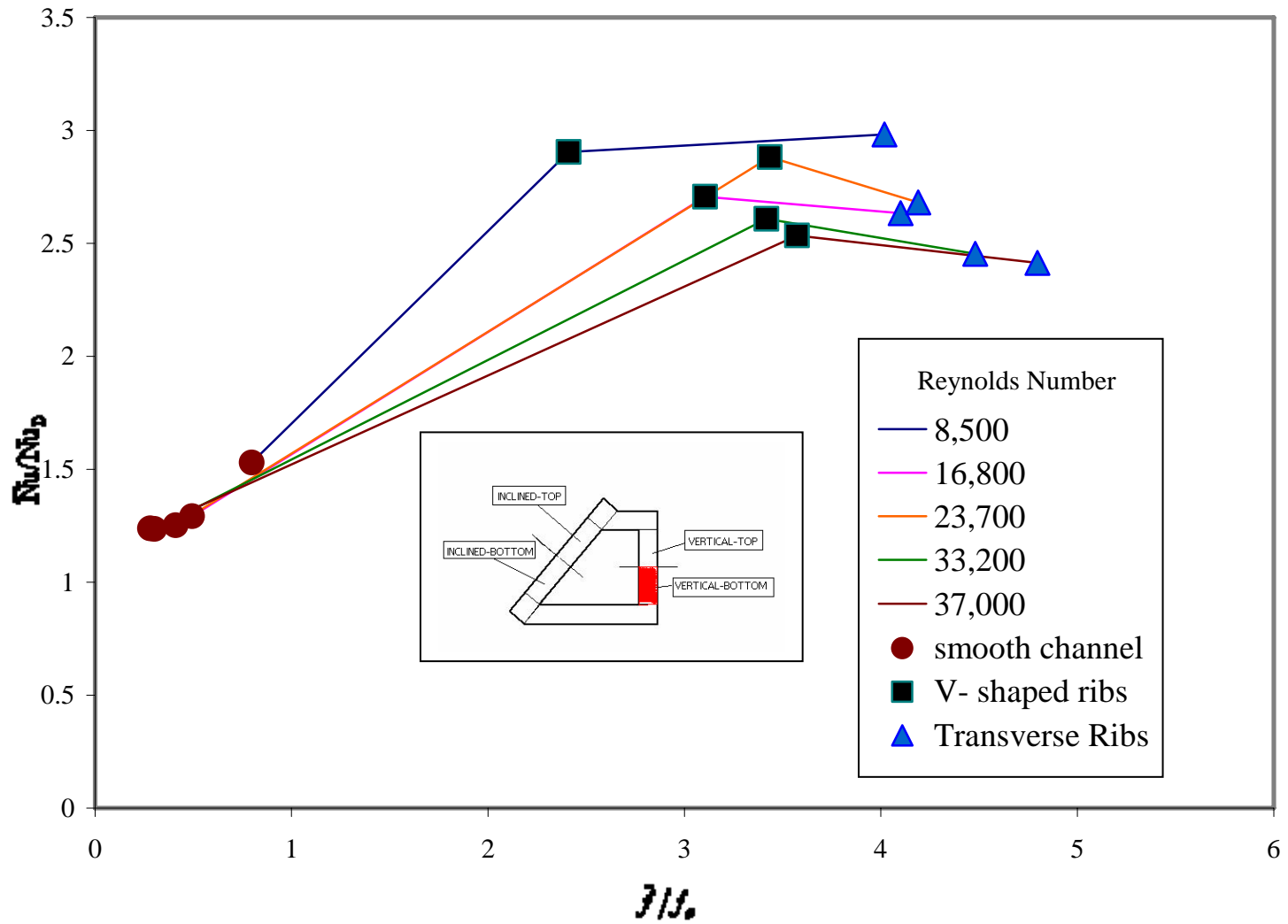


Fig. 27 Average Nusselt Number Ratio versus Friction Factor Ratio for Vert-Bot Wall

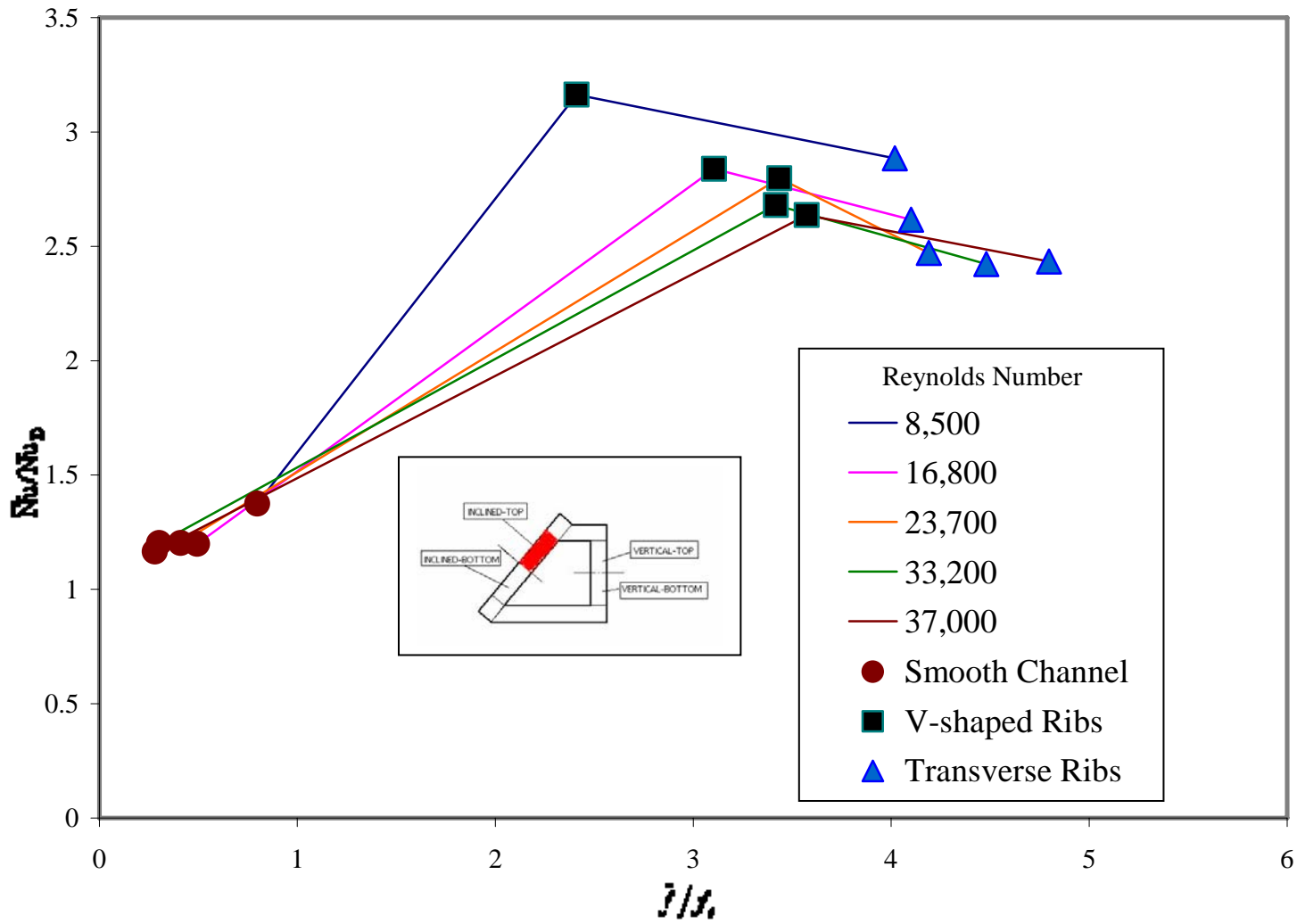


Fig. 28 Average Nusselt Number Ratio versus Friction Factor Ratio for Inc-Top Wall



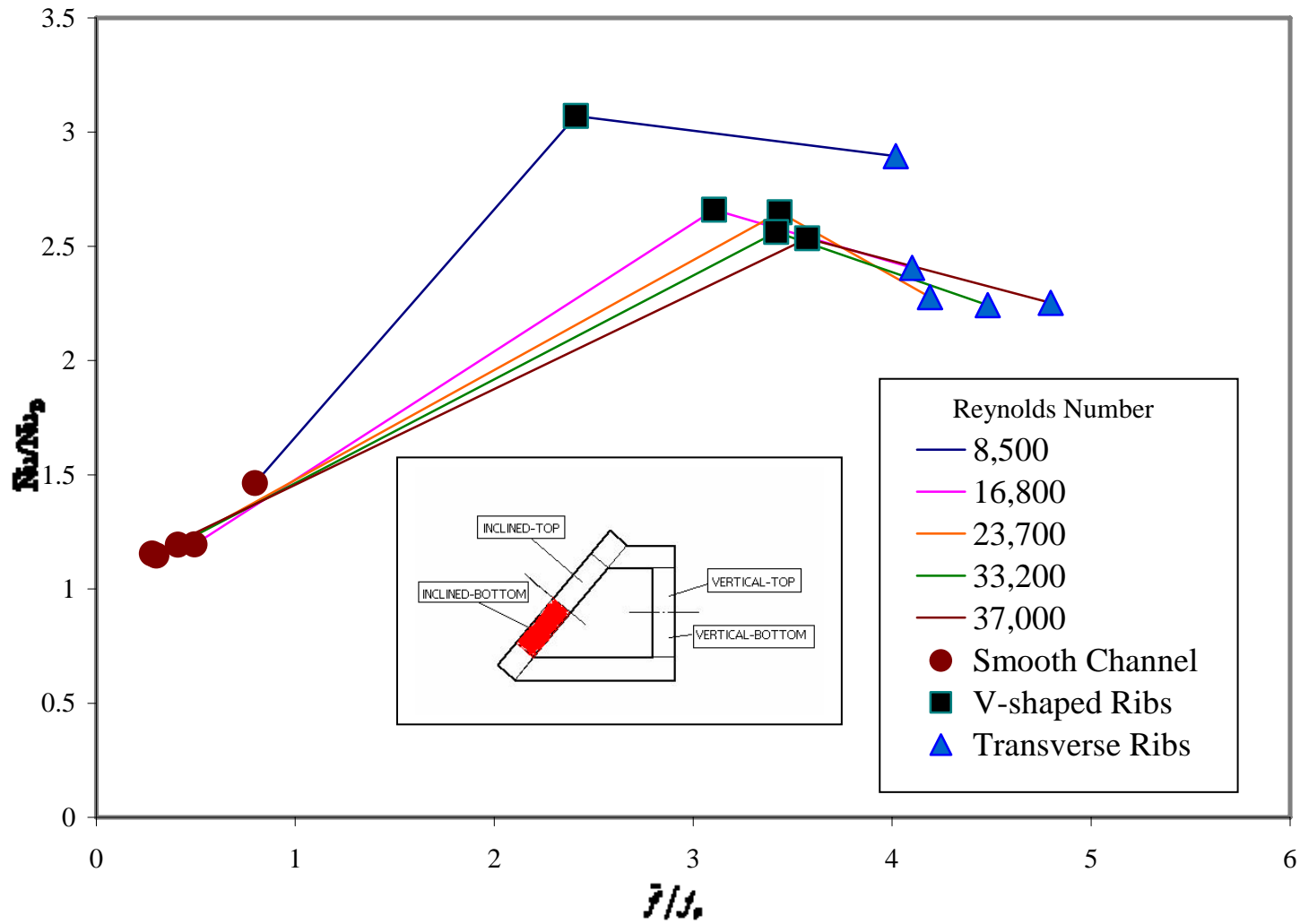


Fig. 29 Average Nusselt Number Ratio versus Friction Factor Ratio for Inc-Bot Wall

**Table 2 Thermal Performance on the Vertical Wall Segment**

Re	Vertical-Top Wall Segment		Vertical-Bottom Wall Segment	
	Transverse Ribs	V-shaped Ribs	Transverse Ribs	V-shaped Ribs
	90 Deg	45 Deg	90 Deg	45 Deg
8,500	1.82	2.29	1.88	2.17
16,800	1.62	2.03	1.65	1.86
23,700	1.65	2.11	1.66	1.91
33,200	1.46	1.92	1.49	1.73
37,000	1.43	1.84	1.43	1.66

**Table 3 Thermal Performance on the Inclined Wall Segment**

Re	Inclined-Top wall Segment		Inclined-Bottom wall segment	
	Transverse Ribs	V-shaped Ribs	Transverse Ribs	V-shaped Ribs
	90 Deg	45 Deg	90 Deg	45 Deg
8,500	1.81	2.36	1.82	2.29
16,800	1.63	1.95	1.5	1.82
23,700	1.53	1.85	1.41	1.76
33,200	1.47	1.78	1.36	1.7
37,000	1.44	1.72	1.34	1.66

case of transverse ribs. In case of the V-shaped ribs the variation is significant on both the straight and the inclined wall and was close to 10%. So, from the graph it is clear that the V-shaped ribs produced 20% higher heat transfer enhancement but also resulted in 25%-60% lesser pressure drop penalty.

It was observed that at high Reynolds number the bottom wall segments on the inclined wall always resulted in poor performance due to the accumulation of slowed-heated fluid also referred as vortices near the sharp corner of the trapezoid.

## SUMMARY AND CONCLUSIONS

The average heat transfer and friction characteristics measurement was performed in a trapezoidal channel; with 90° transverse ribs and V-shaped ribs angled at 45° for Reynolds number ranging from 7,000 to 40,000 with a  $P/e$  ratio of 12 and  $e/D_h$  ratio of 0.016. The main findings are as follows

- 1) For the smooth channel, channel ribbed with 90° transverse ribs and 45° V-shaped ribs, the Nusselt number ratio decreased with increase in axial distance and reached a constant value a few ribs downstream of the channel from the entrance.
- 2) The 45° V-shaped produced 20% better heat transfer augmentation than the 90° transverse ribs and 120% better heat transfer augmentation than the smooth channel for the complete range of Reynolds number due to the induction of the cross stream secondary flow which augments the heat removal.
- 3) The V-shaped ribs produced 25%-60% less pressure drop than the 90° transverse ribs for the complete range of Reynolds number.
- 4) The thermal performance on all the four wall segments was found to decrease with increase in Reynolds number due to higher friction losses.
- 5) The heat transfer on ribbed walls at sharp corners was found to be low due to the slowed and heated boundary layer formation at the corners which results in accumulation of hot fluid.

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## APPENDIX A

### Data Reduction

The mass flow rate of air through the test section is calculated as

$$\dot{m} = \frac{\pi}{4} d_o^2 C Y \left[ \frac{2 p_o \Delta p_o}{R T_o (1 - \eta^4)} \right]^2 \quad (\text{A})$$

Where  $d_o$  is the diameter of the orifice and is equal to 3.81 cm,  $Y$  is the expansion coefficient,  $C$  is the discharge coefficient,  $p_o$  is the pressure at the upstream of the orifice,  $\Delta p_o$  is the pressure drop across the orifice,  $R$  is the universal gas constant for air [287 J/Kg.K],  $T_o$  is the temperature at the orifice and  $\eta$  is the orifice-diameter-to-pipe-diameter ratio and is equal to 0.6.

The expansion and discharge coefficient is calculated as

$$Y = 1.0 - \frac{(0.41 + 0.35\eta^4)\Delta p_o}{1.4 p_o} \quad (\text{B})$$

$$c = 0.5959 + 0.0312\eta^{2.1} + \frac{91.71\eta^{2.5}}{Re_{dp}^{0.75}} - 0.01584 + \frac{0.0390\eta^4}{1 - \eta^4} - 0.184\eta^8 \quad (\text{C})$$

Where,  $Re_{dp}$  is given by

$$Re_{dp} = \frac{4\dot{m}}{\pi d_p \mu} \quad (\text{D})$$

The power input to the ith wall is given as



$$q_i = VI \left( \frac{L_i}{L_h} \right) \quad (\text{E})$$

where, I is the current, V is the voltage across the heater,  $L_i$  is the length wall segment and  $L_h$  is the total length of the heater.

The bulk air temperature is determined as

$$T_{b,out,i} = T_{b,in,i} + \frac{q_i}{\dot{m}c_p} \quad (\text{F})$$

Where,  $c_p$  is the specific heat of air.

The starting value is the measured inlet bulk temperature and the bulk temperature at the outlet of the wall segment is calculated using the above equation. This outlet bulk temperature is taken as the inlet bulk for the subsequent wall segment.

## APPENDIX B

### Uncertainty Analysis

The precision index is given by

$$S_x = \sqrt{\frac{1}{N-1} \sum_{i=1}^n (x_i - \bar{x})^2} \quad (\text{A})$$

Where

$$\bar{x} = \frac{1}{N} \sum_{i=1}^n x_i \quad (\text{B})$$

The Random error is given by

$$P_x = tS_x \quad (\text{C})$$

The overall all uncertainty is given by

$$U_x = \sqrt{(B^2 + P_x^2)} \quad (\text{D})$$

Mass flow rate:

$$\dot{m} = \frac{\pi}{4} d_o^2 CY \left[ \frac{2p_o \Delta p_o}{RT_o (1 - \eta^4)} \right]^2 \quad (\text{E})$$

$$\frac{U_{\dot{m}}}{\dot{m}} = \left[ \left( \frac{1}{2} \frac{U_{p_o}}{p_o} \right)^2 + \left( \frac{1}{2} \frac{U_{\Delta p_o}}{\Delta p_o} \right)^2 + \left( \frac{-1}{2} \frac{U_{T_o}}{T_o} \right)^2 \right]^{\frac{1}{2}} \quad (\text{F})$$

Reynolds Number:

$$Re_{Dh} = \frac{4\dot{m}}{\mu P_w} = \frac{\dot{m}}{\mu W} \quad (\text{G})$$

$$\frac{U_{Re_{D_h}}}{Re_{D_h}} = \left[ \left( \frac{1}{2} \frac{U_{p_o}}{p_o} \right)^2 + \left( \frac{1}{2} \frac{U_{\Delta p_o}}{\Delta p_o} \right)^2 + \left( \frac{-1}{2} \frac{U_{T_o}}{T_o} \right)^2 + \left( -\frac{U_{\mu_o}}{\mu} \right)^2 + \left( -\frac{U_W}{W} \right)^2 \right]^{\frac{1}{2}} \quad (\text{H})$$

Friction Factor:

$$f = \frac{\left( \frac{\Delta p}{\Delta x} \right) D_h}{\frac{\rho \bar{u}^2}{2}} = 2\rho \left( \frac{\Delta p}{\Delta x} \right) D_h \left( \frac{A_c}{\dot{m}} \right)^2 \quad (\text{I})$$

$$\frac{U_f}{f} = \left[ \left( \frac{U_\rho}{\rho_o} \right)^2 + \left( \frac{U_{\Delta p}}{\Delta p} \right)^2 + \left( -\frac{U_{\Delta x}}{\Delta x} \right)^2 + \left( \frac{4U_W}{W} \right)^2 + \left( \frac{U_W}{W} \right)^2 + \left( \frac{-2U_{\dot{m}}}{\dot{m}} \right)^2 \right]^{\frac{1}{2}} \quad (\text{J})$$

Bulk Mean Temperature:

$$T_{b,out} = T_{b,in} + \frac{q}{\dot{m}c_p} = T_{b,in} + \frac{VI(L/L_h)}{\dot{m}c_p} \quad (\text{K})$$

$$\frac{U_{T_{b,out}}}{T_{b,out}} = \left\{ \left[ \left( \frac{T_{b,in}}{T_{b,out}} \right) \left( \frac{U_{T_{b,in}}}{T_{b,in}} \right) \right]^2 + \left[ \left( \frac{\Delta T_b}{T_{b,out}} \right) \left( \frac{U_V}{V} \right) \right]^2 + \left[ \left( \frac{\Delta T_b}{T_{b,out}} \right) \left( \frac{U_I}{I} \right) \right]^2 + \left[ \left( \frac{\Delta T_b}{T_{b,out}} \right) \left( \frac{U_L}{L} \right) \right]^2 + \left[ \left( \frac{\Delta T_b}{T_{b,out}} \right) \left( \frac{-U_{L_h}}{L_h} \right) \right]^2 + \left[ \left( \frac{\Delta T_b}{T_{b,out}} \right) \left( \frac{-U_{\dot{m}}}{\dot{m}} \right) \right]^2 + \left[ \left( \frac{\Delta T_b}{T_{b,out}} \right) \left( \frac{-U_{C_p}}{C_p} \right) \right]^2 \right\} \quad (\text{L})$$

$$U_{\bar{T}_b} = U_{T_{b,in}}$$

Nusselt Number:

$$Nu_{D_h} = \frac{hD_h}{k} = \frac{q}{A_s(\bar{T}_w - \bar{T}_b)} \left( \frac{D_h}{k} \right) = \frac{VI(L/L_h)}{(LW)(\bar{T}_w - \bar{T}_b)} \left( \frac{W}{k} \right) \quad (\text{M})$$

$$\frac{U_{Nu_{D_h}}}{Nu_{D_h}} = \left[ \left( \frac{U_V}{V} \right)^2 + \left( \frac{U_I}{I} \right)^2 + \left( -\frac{U_{L_h}}{L_h} \right)^2 + \left( \frac{-U_{\bar{T}_w}}{\bar{T}_w - \bar{T}_b} \right)^2 + \left( \frac{U_{\bar{T}_b}}{\bar{T}_w - \bar{T}_b} \right)^2 - \left( \frac{-U_k}{k} \right)^2 \right]^{\frac{1}{2}} \quad (\text{N})$$

**APPENDIX C****Table 4 Properties of Air at Room Temperature**

Properties	Value
Thermal conductivity [W/m K]	$2.67 \times 10^{-2}$
Density [Kg/m <sup>3</sup> ]	1.181
Specific Heat at Constant Pressure [KJ/Kg]	1006
Prandtl Number	0.69
Dynamic Viscosity [Kg/ m s]	$1.87 \times 10^{-5}$

## APPENDIX D

**Table 5 Value of  $t(N,C)$  for a Confidence Level  $C$  and Number of Degrees of Freedom  $\nu=N-1$**

$\nu = N - 1$	$C$				
	0.900	0.950	0.990	0.995	0.999
1	6.314	12.70	63.65	127.3	636.6
2	2.920	4.303	9.925	14.09	31.60
3	2.353	3.182	5.841	7.453	12.92
4	2.132	2.776	4.604	5.598	8.610
5	2.015	2.571	4.032	4.773	6.869
6	1.943	2.447	3.707	4.317	5.959
7	1.895	2.365	3.499	4.029	5.408
8	1.860	2.306	3.355	3.833	5.041
9	1.833	2.262	3.250	3.690	4.781
10	1.812	2.228	3.169	3.581	4.587
11	1.796	2.201	3.106	3.497	4.437
12	1.782	2.179	3.055	3.428	4.318
13	1.771	2.160	3.012	3.372	4.221
14	1.761	2.145	2.977	3.326	4.140
15	1.753	2.131	2.947	3.286	4.073
16	1.746	2.120	2.921	3.252	4.015
17	1.740	2.110	2.898	3.223	3.965
18	1.734	2.101	2.878	3.197	3.922
19	1.729	2.093	2.861	3.174	3.883
20	1.725	2.086	2.845	3.153	3.850
25	1.708	2.060	2.787	3.078	3.725
30	1.697	2.042	2.750	3.030	3.646
40	1.684	2.021	2.704	2.971	3.551
60	1.671	2.000	2.660	2.915	3.460
120	1.658	1.980	2.617	2.860	3.373
$\infty$	1.645	1.960	2.576	2.807	3.291

## APPENDIX E

### Table 6 Tabulated Reading for Smooth Channel

	Re1=8,500	Re2=16,800	Re3=23,700	Re4=33,200	Re5=37,000
T1	324.3	320.8	321.1	322.2	322.2
T2	325.4	321.8	322.2	323.3	323.4
T3	332.7	328.4	328.9	329.6	330
T4	332.2	328	328.4	330	330.4
T5	336.2	331.4	331.7	332.6	332.8
T6	336.2	331.3	331.6	332.4	332.8
T7	339	333.9	334.1	334.7	335.3
T8	339	333.8	334	334.5	335.1
T9	341.4	336.1	336.2	336.9	337.6
T10	340.8	335.5	335.7	336.3	337
T11	0	0	0	0	0
T12	342.7	337.4	337.5	338.2	338.9
T13	341.6	336.4	336.8	337.2	338
T14	340.9	335.8	336.2	336.7	337.4
T15	336.3	332.1	333.3	332.7	333.6
T16	337.2	333.1	334.3	333.6	334.5
T17	327	323.5	323.9	324.3	324.2
T18	327.6	324.1	324.6	325.3	325.3
T19	334.3	329.8	330.2	331	331
T20	334	329.6	330	330.7	330.6
T21	338.3	333.2	333.4	334.1	334.3
T22	338.2	333.1	333.3	334	334.2
T23	0	0	0	0	0
T24	340.2	334.8	334.8	335.5	336
T25	343	337.3	337.3	338.1	338.8
T26	342.9	337.2	337.2	337.9	338.6
T27	344.2	338.3	338.3	338.9	339.6
T28	343.8	338	338	338.3	339
T29	344.4	338.9	339.3	339.4	340.4
T30	344.5	339	339.4	339.7	340.7
T31	337.6	332.9	333.5	333.4	334.5
T32	337.4	332.8	333.4	333.3	334.4
T33	327.6	324.8	325.9	325.8	325.3
T34	327.9	325	326.1	0	325.8
T35	335.5	331.7	332.8	333	332.5
T36	335.6	331.7	332.8	332.9	332.5
T37	0	0	0	0	0
T38	340.6	336.2	337.5	337.4	336.8
T39	341.8	337.3	338.6	339.1	338.7
T40	342	337.5	338.8	339.3	338.9
T41	344	339.5	340.7	341.1	340.8
T42	343.8	339.3	340.5	340.8	340.6
T43	345.2	340.7	342	341.8	341.4
T44	345.4	340.9	342.1	342	341.6
T45	345.7	341.6	343	343.9	343.2
T46	345.2	341.1	342.5	343.2	342.6
T47	340.3	336.8	338.2	339.4	338.2
T48	340	336.5	337.9	339	337.8
T49	327.2	322.9	323.4	322.1	322.8
T50	327.6	323.3	323.9	0	323.4
T51	336.1	331	332	330.9	331.9
T52	336.2	331.1	332.1	331.1	332
T53	341.4	335.8	337.1	335.8	336.9
T54	341.4	335.9	337.1	335.9	337
T55	344.4	338.6	339.9	338.5	339.7
T56	344.4	338.6	339.9	338.6	339.8
T57	346.6	340.5	341.6	340.1	341.3
T58	346.3	340.2	341.3	339.8	341
T59	347.1	341	342.1	340.5	341.7
T60	347	341	342	340.5	341.7
T61	344.9	339	339.9	338.3	339.4
T62	345.2	339.2	340.2	338.7	339.7
T63	341.9	336.8	338	336.7	337.4
T64	341.7	336.7	337.8	336.5	337.2
Power input to the straight wall					
Voltage(V)	26.171	29.153	32.19	36.44	38.166
Current(I)	1.409	1.577	1.74	1.96	2.062
Power input to the inclined wall					
Voltage(V)	30.778	34.806	39.41	43.9	45.71
Current(I)	1.655	1.876	2.129	2.36	2.452
Pressure upstream of the orifice(Pressure transducer)					
Vdc(V)	0.064	0.152	0.257	0.469	0.573
Pressure drop across the test section (in of H2O)					
Del p	0.002	0.003	0.006	0.007	0.009



Table 8 Tabulated Reading for Channel with 45° V-shaped Ribs

Table with 3 main columns: Trial 1, Trial 2, Trial 3. Each trial has sub-columns Re1 to Re5. The table lists velocity readings (V) in m/s and current readings (I) in A for various test sections (K). It includes summary rows for voltage, current, pressure upstream of the orifice, and pressure drop across the test section.



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