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Multi-channel sub-Nyquist cross-Spectral Estimation for Modal Analysis of Vibrating Structures

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Abstract - Operational modal analysis (OMA) is a widely used construction verification and structural health monitoring technique aiming to obtain the modal properties of vibrating civil engineering structures subject to ambient dynamic loads by collecting and processing structural response acceleration signals. Motivated by the need for cost-efficient OMA using wireless sensor networks which acquire and transmit measurements at a lower than the Nyquist rate, a novel OMA approach is put forth to derive modal properties directly from sub-Nyquist sampled (compressed) acceleration measurements from arrays of sensors. This is achieved by adopting sub-Nyquist deterministic nonuniform multi-coset sampling devices and by extending a previously proposed in the literature power spectrum blind sampling (PSBS) method for single-channel spectral estimation of stochastic processes to treat the case of multiple channel crossspectral estimation. The standard frequency domain decomposition is used to obtain the modal properties from the cross-spectral matrix derived directly from the sub-Nyquist measurements. The applicability and efficiency of the proposed approach is exemplified by retrieving mode shapes of a whitenoise excited simply supported steel beam with good accuracy according to the widely used modal assurance criterion (MAC) using 70% less than the Nyquist rate measurements.

Keywords - Power spectrum blind sampling; multi-channel crossspectral estimation; compressive sub-Nyquist sampling; structural health monitoring

I. INTRODUCTION AND MOTIVATION

Operational modal analysis (OMA) relies on linear system identification techniques to derive the dynamic (modal) properties of vibrating civil engineering structures (i.e., natural frequencies, damping ratios, and mode shapes) subject to lowamplitude ambient dynamic excitations (e.g., due to wind or traffic induced loads) [1][2]. This is achieved by processing only acceleration structural response signals recorded by relatively dense arrays of sensors, while the input excitation loads are not measured but are assumed to have a flat spectrum over a wide range of frequencies (i.e., white noise excitation assumption). OMA is a widely used structural health monitoring technique since it obtains modal properties efficiently, under operational conditions, which are then used for condition assessment, design verification, and damage detection of civil engineering structures. From a practical viewpoint, the use of wireless sensor networks (WSNs) offers low-cost and rapid OMA implementations compared to tethered sensors, especially in large scale and geometrically complex structures [3],[4]. On the antipode, the consideration of WSNs for OMA increases maintenance costs as wireless

sensors require frequent battery replacement (or expensive local energy harvesting), while they pose limitations to the amount of data that can be transmitted.

To address the above issues, fairly recently, various researchers considered compressive sensing (CS) based techniques for OMA aiming to reduce the energy consumption at the sensors by considering slower sampling rates at the analog-to-digital converter (ADC) units and, at the same time, to reduce the data transmitted within WSNs [5][7]. The latter is achieved without local on-board offline data storage and compression-before-transmission, which is the current norm for wireless sensors [3]. Therefore, CS techniques may also lead to simpler and cheaper sensors. However, in all CS approaches reported in the literature, the response acceleration signals are treated as deterministic, which is not in alignment with the assumption of white-noise excited structural systems, while a certain level of sparsity is assumed for measured signals which may not hold true for noisy environments encountered in practice. Further, with the exception of [5], computational expensive signal reconstruction from the compressed measurements is required after transmission [8].

To circumvent the above limitations, this paper proposes a novel sub-Nyquist approach for OMA which treats response acceleration signals as stochastic processes (i.e., white noise filtered through linear structural systems), does not theoretically require signal sparsity, and provides estimates of modal properties directly from the compressed (sub-Nyquist sampled) measurements without signal reconstruction. The proposed approach builds on recent work by the authors on power spectrum blind sampling (PSBS) for system identification of white-noise excited structural systems [9],[10], and extends the works in [11],[12], to achieve cross-spectral estimation from simultaneous multiple sensing channels. Specifically, the multi-coset sampling device in [11] is adopted yielding deterministic, non-uniform, periodic samples taken at a sub-Nyquist rate [13]. The PSBS technique in [12] is extended to estimate the cross-spectral matrix from sub-Nyquist measurements from an array of such devices. The standard frequency domain decomposition algorithm [14] is finally employed to retrieve structural modal properties.

II. SUB-NYQUIST OPERATIONAL MODAL ANALYSIS

A. Multicoset Sampling Strategy and Device

Let x(t) be a continuous in time t real-valued wide-sensestationary stochastic process (or random signal) characterized in the frequency domain by the power spectrum $P_x(\omega)$ bandlimited by $2\pi/T$. It is desired to sample x(t) at a rate lower than the Nyquist sampling rate 1/T (in Hz), and still be able to obtain a useful estimate of the spectrum $P_x(\omega)$. To this aim, the multi-coset sampling strategy is herein adopted [13], which can be implemented by utilizing M interleaved ADC devices operating at a sampling rate 1/(NT). A discrete-time model of such a sampling device is shown in Figure 1 in which the discrete-time signal x[n]=x(n/T) enters M branches and at each m branch (m= 0, 1,..., M–1), the signal is convolved by an Nlength sequence $c_m[n]$ and down-sampled by N [11]. The selection of M samples (sampling pattern) within each block is governed by the coefficients $c_m[n]$ of the filter written as $c_m[n]$ = 1 for $n = -n_m$ and $c_m[n] = 0$ for $n \neq -n_m$ where there is no repetition in n_m , i.e., $n_m \neq n_m$ $\forall m_l \neq m_j$. The output of the

m-th branch is given as $y_m[k] = \sum_{p=1-N}^{0} c_m[p] x[kN-p]$. The

limiting case of M=N samples x[n] at the Nyquist rate, while the case of M/N<1 corresponds to sub-Nyquist sampling and the y_m sequences become "compressed measurements" of x[n].



Figure 1. Discrete-time model of the adopted AIC device in [11]

B. Input/Output Correlation Function Relationships

Consider an array of D identical multi-coset sampling devices measuring acceleration response signals at different locations of a white-noise excited structure. Each device has M branches with output sequences $y_m^d[1]$ where m= 0,1,..., M-1 and d=1, 2, ..., D. The cross-correlation function between two output sequences of the mi branch of the da device and of the mi branch of the db device is hereafter denoted by $\mathbf{r}_{\mathbf{y}_{a}^{a},\mathbf{y}_{i}^{b}}[\mathbf{k}] = \mathbf{E}_{y} \left\{ \mathbf{y}_{m}^{d_{a}}[1] \; \mathbf{y}_{m_{i}}^{d_{b}}[1-\mathbf{k}] \right\}, \text{ where } \mathbf{E}_{a}\{\cdot\}$ the is mathematical expectation operator with respect to a. Further, the cross-correlation function between the input signals x^{d} [m] to the devices d_{a} and d_{b} is denoted bv $\mathbf{r}_{\mathbf{x}^{a}\mathbf{x}^{b}}[\mathbf{n}] = \mathbf{E}_{\mathbf{x}} \left\{ \mathbf{x}^{d_{a}}[\mathbf{m}] \ \mathbf{x}^{d_{b}}[\mathbf{m} - \mathbf{n}] \right\}.$

Under the assumption that all considered devices have the same sampling pattern across their branches, the common pattern cross-correlation function is expressed as $r_{c_i,c_j}[n] = \sum_{k=l-N}^{0} c_{m_i}[k] c_{m_j}[k-n] = \delta[n - (n_{m_i} - n_{m_j})]$, where $\delta[n]$

= 1 for n = 0 and $\delta[n] = 0$ for $n \neq 0$. The above assumption allows to relate the cross-correlation functions of the output sequences in the array as

$$\mathbf{r}_{y^{a}y^{b}}[k] = \sum_{l=0}^{1} \mathbf{R}_{c}[l] \ \mathbf{r}_{x^{a}x^{b}}[k-1],$$
(1)

which is a generalization of the single device (channel) case considered in [9][12]. In the previous expression, $\mathbf{r}_{y^a y^b}[\mathbf{k}] = \left[\mathbf{r}_{y^a_0, y^b_0}[\mathbf{k}] \cdots \mathbf{r}_{y^a_0, y^b_{(M-1)}}[\mathbf{k}] \mathbf{r}_{y^a_1, y^b_0}[\mathbf{k}] \cdots \mathbf{r}_{y^a_{(M-1)}, y^b_{(M-1)}}[\mathbf{k}]\right]^{\mathrm{T}}$, is the M²-by-D matrix collecting the output cross-correlation sequences $\mathbf{r}_{y^a_1, y^b_1}[\mathbf{k}]$ among the M branches of the array of devices, where a "T" superscript denotes matrix transposition; $\mathbf{r}_{x^a x^b}[\mathbf{n}] = \left[\mathbf{r}_{x^a x^b}[\mathbf{n}N] \mathbf{r}_{x^a x^b}[\mathbf{n}N+1] \cdots \mathbf{r}_{x^a x^b}[(\mathbf{n}+1)N-1]\right]^{\mathrm{T}}$ is the N-by-D matrix collecting the input cross-correlation sequences; and $\mathbf{R}_c[1]$ is the M²-by-N matrix defined as $\mathbf{R}_c[1] = \left[\mathbf{r}_{c_0, c_0}[1] \cdots \mathbf{r}_{c_0, c_{M-1}}[1] \mathbf{r}_{c_1, c_0}[1] \cdots \mathbf{r}_{c_{M-1}, c_{M-1}}[1]\right]^{\mathrm{T}}$.

By assuming that the input cross-correlation sequences $\mathbf{r}_{x_a x_b}[n]$ take on negligible values outside the range $-L \le k \le L$, the input/output relationship can be cast in matrix form

$$\mathbf{r}_{\mathbf{y}^{a}\mathbf{y}^{b}} = \mathbf{R}_{c}\mathbf{r}_{\mathbf{x}^{a}\mathbf{x}^{b}},\tag{2}$$

where $\mathbf{r}_{y^a y^b}$ is the M²(2L+1)-by-D matrix defined as $\mathbf{r}_{y^a y^b} = \left[\mathbf{r}_{y^a y^b}^{\mathrm{T}}[0] \cdots \mathbf{r}_{y^a y^b}^{\mathrm{T}}[L] \mathbf{r}_{y^a y^b}^{\mathrm{T}}[-L] \cdots \mathbf{r}_{y^a y^b}^{\mathrm{T}}[-1]\right]^{\mathrm{T}}$, $\mathbf{r}_{x^a x^b}$ is the N(2L+1)-by-D matrix defined in a similar manner, and \mathbf{R}_c is the M²(2L+1)-by-N(2L+1) matrix given by

$$\mathbf{R}_{c} = \begin{bmatrix} \mathbf{R}_{c}[0] & \mathbf{O} & \cdots & \mathbf{O} & \mathbf{R}_{c}[1] \\ \mathbf{R}_{c}[1] & \mathbf{R}_{c}[0] & \mathbf{O} & \ddots & \mathbf{O} \\ \mathbf{O} & \mathbf{R}_{c}[1] & \mathbf{R}_{c}[0] & \ddots & \vdots \\ \vdots & \ddots & \ddots & \ddots & \mathbf{O} \\ \mathbf{O} & \cdots & \mathbf{O} & \mathbf{R}_{c}[1] & \mathbf{R}_{c}[0] \end{bmatrix}, \quad (3)$$

Equation (2) defines an overdetermined system of linear equations which can be solved for $\mathbf{r}_{x_a x_b}$ without any sparsity constraints provided that \mathbf{R}_c is full column rank. The latter condition is satisfied for $M^2 \ge N$ [11].

C. Power Spectrum Blind Sampling from compressed sub-Nyquist measurements

Suppose that $x^a[n]$ and $x^b[n]$ are sampled at the Nyquist rate from the band-limited continuous-time processes $x^a(t)$ and $x^b(t)$ respectively. Then, the cross power spectrum of $x^a(t)$ and $x^b(t)$ can be expressed within the $0 \le \omega \le 2\pi$ range as

 $P_{x^{a}x^{b}}(\omega) = \sum_{n=-\infty}^{\infty} r_{x^{a}x^{b}}[n] e^{-in\omega}$, where $i = \sqrt{-1}$. The latter expression is further discretized in the frequency domain and cast in matrix form as

$$\mathbf{s}_{\mathbf{x}^{a}\mathbf{x}^{b}} = \mathbf{F}_{(2L+1)N}\mathbf{r}_{\mathbf{x}^{a}\mathbf{x}^{b}},\tag{4}$$

where $\mathbf{F}_{(2L+1)N}$ is the N(2L+1)-by-N(2L+1) standard discrete Fourier transform matrix and $\mathbf{s}_{x^ax^b}$ is a N(2L+1)-by-D power spectrum matrix evaluated at discrete frequencies $\omega = [0, 2\pi/((2L+1)N), ..., 2\pi(2L+1)N-1/((2L+1)N)].$

Consider the unbiased estimator of the output crosscorrelation function $\hat{r}_{y_i^a, y_j^b}[k]$. The following weighted least squares criterion is adopted [12]

$$\hat{\mathbf{r}}_{\mathbf{x}^{a}\mathbf{x}^{b}} = \arg\min_{\mathbf{r}_{\mathbf{x}_{a}\mathbf{x}^{b}}} \left\| \hat{\mathbf{r}}_{\mathbf{y}^{a}\mathbf{y}^{b}} - \mathbf{R}_{c} \mathbf{r}_{\mathbf{x}^{a}\mathbf{x}^{b}} \right\|_{\mathbf{W}}^{2}, \tag{5}$$

in which the weighted version of the Euclidean norm is given by $\|\mathbf{a}\|_{\mathbf{W}}^2 = \mathbf{a}^T \mathbf{W} \mathbf{a}$, and \mathbf{W} is a weighting matrix. An estimate of the cross-spectrum matrix $\mathbf{s}_{x^a x^b}$ is obtained by

$$\hat{\mathbf{s}}_{\mathbf{x}^{a}\mathbf{x}^{b}} = \mathbf{F}_{(2L+1)N} \left(\mathbf{R}_{c}^{T} \mathbf{W}^{-1} \mathbf{R}_{c} \right)^{-1} \mathbf{R}_{c}^{T} \mathbf{W}^{-1} \hat{\mathbf{r}}_{\mathbf{y}^{a}\mathbf{y}^{b}}, \qquad (6)$$

where the "-1" superscript denotes matrix inversion. In the last equation, the $(2L+1)M^2$ -by-D matrix $\hat{\mathbf{r}}_{y^a y^b}$ is an unbiased estimator of the matrix $\mathbf{r}_{y^a y^b}$. The cross-spectrum matrix in (6) is efficiently computed directly from the cross-correlation estimator of the compressed acceleration measurements from the array of D AIC devices. This is achieved by exploiting the sparse structure of the \mathbf{R}_c matrix as detailed in [12].

D. Frequency Domain Decomposition (FDD) algorithm

Any established frequency domain algorithm for OMA can be utilized to derive structural modal properties from the crossspectral matrix in (6) obtained directly from sub-Nyquist acceleration measurements of white-noise excited structures. In this study, the standard frequency domain decomposition (FDD) algorithm is used, which applies the singular value decomposition to the matrix in (6) , i.e. $\mathbf{s}_{\mathbf{x}^a \mathbf{x}^b} = \mathbf{U} \boldsymbol{\Sigma} \mathbf{V}^T$, where Σ is a diagonal positive semi-definite matrix comprised of the singular values, and U, V are the unitary singular matrices holding the left and right singular vectors respectively. The modal information is carried on the singular values and singular vectors of the first coordinate (principal component) which retains the highest variance [15]. In this respect, natural frequencies are located at the peaks of the principal singular values and the pertinent mode shapes are obtained from the left singular vector of the principal components.

III. NUMERICAL ASSESSMENT

For numerical validation, it is sought to verify the vertical in-plane mode shapes and corresponding natural frequencies of the simply supported IPE300 steel beam depicted in Figure 2 with length l=5m and elastic modulus E=210GPa using the proposed sub-Nyquist OMA approach. A critical damping ratio of 1% is assumed for all modes. The dynamic properties (natural frequencies and mode shapes) of this beam are found by application of standard continuous structural dynamics formulae (e.g. [2]). The first 4 natural frequencies are given in Table I. Further, the n-th mode shape of the beam is given as $\varphi_n(x) = \sin(n\pi x/l)$ along the x longitudinal ordinate ($0 \le x \le l$).



Figure 2. Simply supported steel beam instrumented with 15 sampling devices measuring vertical acceleration response signals.

It is assumed that the vertical response acceleration of the beam is measured at 15 equi-distant locations along its length, as indicated in Figure 2, using the multi-coset sampling device of Figure 1 for white noise excitation applied at location 1 along the gravitational direction. The discrete-time Nyquistsampled sequence that enters each sampling device is simulated by filtering band-limited zero-mean discrete-time white noise sequences through appropriately defined autoregressive-moving-average (ARMA) filters. Specifically, for each of the 15 measurement locations, a different ARMA filter is considered defined by "fitting" the magnitude of its transfer function to the following power spectral density function

$$\begin{split} \left|\mathbf{H}_{ij}(\boldsymbol{\omega})\right|^{2} &= \boldsymbol{\omega}^{4} \cdot \sum_{r,s=l}^{4} \left[\frac{2\phi_{ir}\phi_{jr}\phi_{is}\phi_{js}}{\delta_{rs}+1} \cdot \\ &\cdot \frac{(\boldsymbol{\omega}_{r}^{2}-\boldsymbol{\omega}^{2})(\boldsymbol{\omega}_{s}^{2}-\boldsymbol{\omega}^{2})+4\boldsymbol{\omega}^{2}\boldsymbol{\omega}_{r}\boldsymbol{\omega}_{s}\zeta_{r}\zeta_{s}}{[(\boldsymbol{\omega}_{r}^{2}-\boldsymbol{\omega}^{2})^{2}+(2\boldsymbol{\omega}\boldsymbol{\omega}_{r}\zeta_{r})^{2}]\cdot[(\boldsymbol{\omega}_{s}^{2}-\boldsymbol{\omega}^{2})^{2}+(2\boldsymbol{\omega}\boldsymbol{\omega}_{s}\zeta_{s})^{2}]} \right], \end{split}$$
(7)

using the two-stage method detailed in [16]. The function in (7) is the square magnitude of the frequency response function for an input excitation force at location j and an output acceleration response at location i on the beam [2]. In particular, ω_n and ζ_n are the natural frequency and critical damping ratio of the n-th mode, respectively, ϕ_{ni} is equal to the $\phi_n(x_i)$ mode shape ordinate at a distance x_i of point i from the left end of the beam, and $\delta_{rs}=1$ for r=s, and $\delta_{rs}=0$ for r≠s. All 15 sampling devices considered are identical comprising M=5 branches with a down-sampling parameter N=16 and a common deterministic, non-uniform, and periodic sub-Nyquist multi-coset sampling pattern given by the sequence $\mathbf{n} = [0 \ 1 \ 2 \ 5 \ 8]^{T} \ [8], [10][12].$ They achieve a compression ratio of M/N≈30%. Following the PSBS approach in section II, the spectral matrix in (6) is approximated using the output cross-correlation estimates derived directly from the sub-Nyquist measurements of the 15 AIC devices. The thus obtained matrix is used together with the standard FDD algorithm to estimate the natural frequencies and mode shapes of the beam under study.

Table I reports the percentage error between the estimated and the exact natural frequencies for the first 4 mode shapes. The case of natural frequency estimation from measurements sampled at the Nyquist rate (i.e., for M/N=100%) is also reported. The differences found are small and well within the range of engineering accuracy. Further, Fig. 3 plots the first 4 mode shapes estimated from the left singular vector U of the decomposed spectral matrix (solid curves), together with the exact mode shapes of the beam (broken curves). Mode shapes estimated from Nyquist sampled measurements are also included in Fig. 3 for comparison. It is seen that the herein proposed OMA approach using sub-Nyquist samples yield reasonably accurate mode shapes. The level of accuracy for the estimated mode shapes is quantified using the modal assurance criterion (MAC) [2] which is widely used in OMA for the purpose. Note that MAC is a correlation measure between two eigenvectors (in this work between the exact and the estimated mode shapes) taking values between 0 and 1. It is common to assume that MAC values above 0.9 represent practically valid estimates of mode shapes [2]. Table I reports the obtained MAC values for the sub-Nyquist OMA approach which are well above 0.9 for all mode shapes considered.



Figure 3. Exact (dashed curves) and estimated (solid and dotted curves) mode shapes of the beam in Figure 2.

TABLE I. NATURAL FREQUENCIES AND MODE SHAPES VALIDATION

Natural Frequencies			Mode Shapes	
Theoretical	Difference [%]		MAC	
	Nyquist	Sub-Nyquist	Nyquist	Sub-Nyquist
54.9	0.3	0.3	0.955	0.955
153.1	0.89	-0.11	0.964	0.967
313.5	-0.01	-0.01	0.958	0.953
409.2	0.52	0.52	0.970	0.971
	Nat Theoretical values (Hz) 54.9 153.1 313.5 409.2	Natural Freque Differ Nyquist 54.9 0.3 153.1 0.89 313.5 -0.01 409.2 0.52	Natural Frequencies Differme [%] Nyquist Sub-Nyquist 54.9 0.3 0.3 153.1 0.89 -0.11 313.5 -0.01 -0.01 409.2 0.52 0.52	Mode Differec [%] Mode Differec [%] M Nyquist Sub-Nyquist Nyquist 54.9 0.3 0.955 153.1 0.89 -0.11 0.964 313.5 -0.01 -0.058 0.970 409.2 0.52 0.52 0.970

IV. CONCLUDING REMARKS

A novel OMA approach is put forth to derive modal properties directly from sub-Nyquist sampled (compressed) acceleration measurements from arrays of sensors. This is achieved by adopting sub-Nyquist deterministic non-uniform multi-coset sampling devices and by extending a previously proposed in the literature power spectrum blind sampling (PSBS) method for single-channel spectral estimation of stochastic processes to treat the case of multiple channel crossspectral estimation. The standard frequency domain decomposition is used to obtain the modal properties from the cross-spectral matrix derived directly from the sub-Nyquist measurements. The applicability and efficiency of the proposed approach is exemplified by retrieving mode shapes of a white-noise excited simply supported steel beam with good accuracy according to the widely used modal assurance criterion (MAC) using 70% less than the Nyquist rate measurements. These numerical results render the proposed approach a promising tool for cost-efficient and rapid implementation of OMA using WSNs, though further numerical work pertaining to more complex structures and to noisy measurements is warranted.

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