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A fault diagnosis methodology for rolling element bearings based on advanced signal pretreatment and autoregressive modelling

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Abstract

This study proposes a methodology for rolling element bearings fault diagnosis which gives a complete and highly accurate identification of the faults present. It has two main stages: signals pretreatment, which is based on several signal analysis procedures, and diagnosis, which uses a pattern-recognition process. The first stage is principally based on linear time invariant autoregressive modelling. One of the main contributions of this investigation is the development of a pretreatment signal analysis procedure which subjects the signal to noise cleaning by singular spectrum analysis and then stationarisation by differencing. So the signal is transformed to bring it close to a stationary one, rather than complicating the model to bring it closer to the signal. This type of pretreatment allows the use of a linear time invariant autoregressive model and improves its performance when the original signals are non-stationary. This contribution is at the heart of the proposed method, and the high accuracy of the diagnosis is a result of this procedure. The methodology emphasises the importance of preliminary noise cleaning and stationarisation. And it demonstrates that the information needed for fault identification is contained in the stationary part of the measured signal.

The methodology is further validated using three different experimental setups, demonstrating very high accuracy for all of the applications. It is able to correctly classify nearly 100% of the faults with regard to their type and size. This high accuracy is the other important contribution of this methodology. Thus, this research suggests a highly accurate methodology for rolling element bearing fault diagnosis which is based on relatively simple procedures. This is also an advantage, as the simplicity of the individual processes ensures easy application and the possibility for automation of the entire process.

Keywords

Rolling element bearings, fault diagnosis, linear autoregressive modelling, stationarisation, singular spectrum analysis, pattern recognition

1. Introduction

Rolling element bearings are considered the most common reason for failures in rotating machinery. The literature shows that, for example, roller bearings are considered a major reason for over 40% of failures in induction machines [1]. When a fault occurs in a bearing, the overall vibration level is affected. If the fault is not detected and the

correct decision is not taken in time, the consequences of fault development can be catastrophic. Thus, the inspection and detection of faults at an early stage is crucial to prevent such consequences. However, detection of this change is sometimes difficult at an early stage. A number of strategies have been developed for the purpose of fault diagnosis in rolling element bearings, and it is a subject of continuing interest.

For rolling element bearings, vibration-based fault diagnosis is the most popular strategy. This strategy is based on the analysis of vibration signals acquired from bearing housings. Many techniques have been developed for analysing bearing vibration signals and for the purpose of fault diagnosis [2-4]. Some studies compare the performance of different techniques [5-9].

Generally, these techniques can be divided into non-parametric and parametric. When using a non-parametric technique, signals can be analysed in the time domain, using parameters such as kurtosis and crest factors [10-12], in the frequency domain, e.g. through application of the fast Fourier transform (FFT) [13], and/or in the time-frequency domain, using techniques such as the wavelet transform [14-20].

Bearing signals are almost always non stationary because bearings are inherently dynamic. The non-stationarities in the benign bearing are generally due to abrupt changes in the bearing signal that might come from a clearance between the bearing outer race and the housing, sliding of a rolling element [21]. The non-stationarities can also come from the impacts of the damaged and the non damaged part of a bearing, flaking of one of the bearing raceways [22]. For this reason, conventional non-parametric techniques have some limitations. For instance, the FFT is an efficient numerical algorithm that transforms signals from the time domain to a frequency spectrum; however, it is not appropriate for non-stationary signals [23], and it requires long time intervals to form a good resolution spectrum [24]. To overcome the

limitations of using FFT with non-stationary signals, a lot of studies for bearing fault detection are proposed. Some of these studies include analysing the signal instantaneously in its time and frequency domain such as using short term Fourier transform [25] and the wavelet transform [26-29] which are able to present the overall view of non-stationary signals in time-frequency domains. Nevertheless, on some occasions they are still unable to obtain a good frequency resolution [30]. Others do some transformations which are usually aimed at decomposing the signal into a number of simpler components such as the empirical mode decomposition [31-33]. But it should be noted that these transformations are much more complicated than the proposed differencing technique.

Parametric techniques can be introduced to overcome the problems of the frequency resolution limitation associated with non-parametric techniques. They are based on considering the bearing vibration signal as time series which can be predicted using a suitable model with few parameters [23].

The use of autoregressive modelling for the purpose of fault diagnosis in rolling element bearings has been the subject of several research papers. As bearing vibration signals are originally non-stationary, some researchers suggest the use of time-varying autoregressive (TVAR) models which take into account the presence of nonstationarities in the signal. In [30] a parametric time- frequency spectrum is made using a time varying autoregressive model. Then singular value decomposition (SVD) is used to form features which are used as input to a radial basis function (RBF) neural network. In [34, 35], three different algorithms, namely, Kalman, extended Kalman and modified extended Kalman filter, of model coefficients estimation are investigated. In these TVAR models, the model coefficients are assumed to evolve over time in order to facilitate the modelling of the non-stationary signals. Nevertheless, there are several obstacles implicit in such models. Since the coefficients of such models are evolving over time, it is necessary to adopt a coefficient set with proper evolution; a good initial set of coefficients is also required. Thus, the entire process may be jeopardised by an improper assumption for coefficient evolution or an inappropriate initial set of coefficients.

Other studies use nonlinear autoregressive models in which the data points of the signal are related in a nonlinear form [36, 37]. However, these models are complex in terms of selection of the nonlinear relationship form, and they require relatively long computational time.

There are other forms of AR models used in the fault diagnosis of rolling element bearings, such as periodic time –varying AR model [38]. Such a model assumes that bearing vibration signal has cyclostationary behaviour.

In terms of complexity, linear autoregressive models of time invariant coefficients are the simplest way of representing signals. However, these models are suitable for stationary signals, while bearing vibration signals are originally non-stationary [39]. To overcome this limitation, some pretreatment of signals has been proposed to enhance the modelling goodness of fit (i.e. the ability of the model to correctly predict a signal).

In this study, a new pretreatment is proposed, based on the combination of singular spectrum analysis (SSA) and a particular type of stationarisation, the differencing technique.

The pretreatment goals are:

 noise suppression using singular spectrum analysis (SSA), as the presence of noise deteriorates the quality of model prediction 2. Achievement of stationarity by subjecting the non-stationary sub-signals to differencing which is essentially a kind of high frequency filtering process.

Singular spectrum analysis is one of the non-parametric techniques for time series analysis. It decomposes a time series (i.e in this research a bearing vibration sub-signal) into a number of independent components. These components are generally interpreted as trend, periodic components and structure-less noise components. This technique is used widely for the analysis of climatic and meteorological time series[40, 41]. Recently, it has been used for health monitoring of tool wear[42], rotor rub problems [43] and fault diagnosis in rolling element bearings [44-46]. In [44] a number of statistical features are developed from the trend components and used as input to an artificial neural network classifier. Singular spectrum analysis is also applied as a multilevel analysis in [45]. A two level cascade singular spectrum analysis is applied and the number of the significant components for signal reconstruction is used as an indicator for the bearing condition monitoring. In [46] singular values and the energy of the first several principal components are used to form two feature vectors. Both of these feature vectors are used as input to the back propagation neural network (BPNN) classifier.

In the present work, SSA is used for the purpose of cleaning the structure-less noise before subjecting the signal to AR modelling. It helps in improving the goodness of fit of the linear time invariant autoregressive (LTIVAR) model.

As it was mentioned above there are several techniques that can be used for analysing / transforming a non stationary signal. In this study the simplest and most straightforward approach for making a signal stationary, the differencing technique is used. The differencing technique somehow has not been used before for stationarising bearing and in general machinery signals, although it is very popular in signal analysis and biomedical research [47-51].

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To the knowledge of the authors, no previous applications of the LTIVAR modelling for ball bearing fault diagnosis have applied a similar type of procedure to ensure that the signal can be modelled by an LTIVAR model. There are other studies that use linear autoregressive modelling, some of them also applying pretreatment of the signal, but this is done by different methods, e.g. empirical mode decomposition (EMD) [52] and amplitude demodulation (AD) [37]; which are generally more complicated than the procedure suggested here. Moreover signal stationarisation has not been taken as the basis of the pretreatment.

It is the opinion of the authors that the above mentioned two steps of signal pretreatment, namely SSA noise cleaning and stationarisation via differencing, represent an important improvement to the modelling precision and to the information contained by the signal, allowing much greater accuracy in the results of the detection and the classification of bearing condition.

The methodology presented in this work has been developed to achieve accurate and complete fault identification. The term 'complete' refers to the ability of the methodology to detect and identify the condition of the bearing (e.g healthy, IRF...etc) and eventually estimate its severity. To the best of the author's knowledge, the majority of previous studies using linear autoregressive modelling have not applied it to fault severity estimation.

The methodology suggested here can be divided into two main stages:

- signal pretreatment, which is based on several signal analysis procedures, including signal de-noising using SSA, signal stationarisation and the AR modelling
- 2. signal diagnosis, which is essentially based on a pattern-recognition process.
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In the first stage, signals are segmented into a number of equal-length segments, and each segment is then subjected to SSA to decompose into a number of components. The components of the higher singular values (i.e. higher contribution to the total signal variance) are used to reconstruct the new segment (i.e. sub-signal). When the new segments are reconstructed, they are subjected to a stationarity test. The non-stationary segments, i.e. those which fail to meet the test criterion, are stationarised using the differencing technique. The final step in the first stage of this methodology is to subject the segments to modelling, using the LTIVAR model and obtaining the model coefficients.

In the second stage (i.e. the signal diagnosis), the LTIVAR model coefficients are arranged into feature vectors, and a pattern-recognition approach is used to detect, and localise the fault and to estimate its size. The nearest neighbour (NN) classification rule, based on the Mahalanobis distance, is suggested for this purpose. In this classification approach, the distance of each new feature vector from a testing sample to the corresponding signal categories from training sample is checked to assign the feature vector to the category to which its nearest neighbour belongs. If for any reason, the lengths of the new testing feature vector and that made from the training sample are different, they should be equalized to measure the Mahlanobis distance properly. Three different possibilities are investigated in this study to see whether vectors length equalization may affect the performance of the methodology or not. Eventually, the technique which ensures best classification results is adopted.

The paper is organised into the following sections: Section 2 presents the pretreatment of the data, including signal segmentation, noise suppression using singular spectrum analysis SSA, stationarisation and linear AR modelling. Section 3 describes the diagnosis method, based on the pattern-recognition process. In Section 4, three case studies for the validation of the method are introduced. In Section 5, the results and discussion are presented. Section 6 provides a comparison of the performance of the method suggested here with some recent previous works. Finally, concluding remarks and proposals for further development of the suggested methodology are given in Section 7.

2. Signal pretreatment

2.1 Signal segmentation

Signals are segmented to provide more samples and to overcome the difficulty of obtaining repetitive measurements from the machine. For each bearing condition, each signal is segmented into a number of non-overlapping sub-signals of equal-length. With regard to autoregressive modelling, it is generally recommended that the segment length should follow the ratio p/n < 0.1, where p is the model order and n is the segment length [53]. This ratio is recommended because it is known that a greater ratio can affect the model's goodness of fit.

2.2 Singular Spectrum Analysis (SSA)

SSA is a statistical procedure which has been used extensively for climate and meteorology analysis, but has not yet gained popularity for machinery analysis. It is simply principal components analysis applied to the lagged components of a time series. SSA is used to decompose the original signal into a number of independent components; the principal components (PCs). The initial time series can be then reconstructed by using a number of PCs. The primary aim of SSA is to uncover the

trend in a signal, particularly its oscillatory patterns. SSA can, however, also be used as a noise-cleaning procedure; it is known to clean structure-less noise by transforming it into low singular value components [54]. This is the purpose for which SSA is used in this study. Only the independent principal components that explain a large proportion of the variance of the sub-signal were selected for the reconstruction step. This resulted in a considerable improvement in the LTIVAR model's goodness of fit. In this study, SSA was used for decomposing the segmented signals, after which they were reconstructed using a number of the principal components. Thus, the procedure has two stages: decomposition and reconstruction [55].

In the decomposition stage, a sub-signal **x** of length n , x(1),x(2),...,x(n), is mapped onto a window of length (L) to form the so-called trajectory matrix **Y** (LxK) where K=n-L+1 (see Eq. (2)).

$$\mathbf{Y} = \begin{bmatrix} x(1) & x(2) & x(3) & \dots & x(K) \\ x(2) & x(3) & x(4) & \dots & x(K+1) \\ x(3) & x(4) & x(5) & \dots & x(K+2) \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x(L) & x(L+1) & x(L+2) & \dots & x(n) \end{bmatrix}$$
(2)

The trajectory matrix (**Y**) is then subjected to singular value decomposition to obtain (L) eigenvectors ($\mathbf{U}_{i}, i = 1, 2.., L$) corresponding to (L) eigenvalues ($\lambda_{i}, i = 1, 2.., L$). Each λ_{i} represents the partial variance of the original time series in the direction of the \mathbf{U}_{i} . Projecting the trajectory matrix onto each eigenvector provides the corresponding principal components (**PC**_i.):

$$PC_{i}(m) = \sum_{j=1}^{L} Y^{T}(m+j-1) * U_{i}(m)$$
(3)

where

i=1, 2....L;

m=1, 2...n;

j=1, 2...L.

Then, L elementary matrices $(\mathbf{El}_i = \mathbf{U}_i \mathbf{PC}'_i \text{ where } i = 1,2, \dots L \text{ and the prime means transpose})$ can be created by the projection of the PCs on the Eigenvectors U.

The contribution of these elementary matrices norms to the original trajectory matrix norm follows the trend of the singular values, which is the first matrices have the highest contribution while the last ones have the lowest.

As was mentioned above, the signals can be reconstructed by a linear combination of all or a number of the PCs. Different criteria can be used to select the number of PCs [45]. In this study, a number (w) of PCs was selected so that 90% of the original sub-signal variance is contained in the new reconstructed signal (\mathbf{xr}). The reconstruction process is done by the diagonal averaging technique which is described below[56]:

$$xr(m) = \frac{1}{N_m} \sum_{i \in w} \sum_{j=Lm}^{Um} PC_i (m-j+1) * U_i(m) , m = 1, 2, ..., n-1$$
(4)

The Normalisation factor (N_m) and the lower (Lm) and upper (Um) bounds of sums differ for the edges and the centre of the signal. They are defined as follows:

$$\left(\frac{1}{N_{m}},Lm,Um\right) = \begin{cases} \left(\frac{1}{m},1,m\right), & for \quad 1 \le m \le L-1\\ \left(\frac{1}{L},1,K\right), & for \quad L \le m \le K\\ \left(\frac{1}{n-m+1},m-n+L,L\right), & for \quad K+1 \le m \le n \end{cases}$$
(5)

The new reconstructed signals **xr** will be used for the further analysis.

2.3 Stationarisation

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Basically, the property of a stationarity of a signal is defined as the consistency of the first four statistical moments over the time. Conversely, non stationarity occurs when these statistical moments are changing with time. However, since the above definition is too strict and difficult to achieve, a second order or weak stationarity is usually meant by the term ''stationary''. And it refers to the case when the first two statistical moments are constant over the time [57].

The suggested procedure uses linear autoregressive modelling as a method for extracting the information needed for the diagnosis process. Linear autoregressive modelling is a process which has been developed primarily for stationary time series. As it was mentioned above differencing is applied to bring the non stationary sub-signal to stationarity. However, applying further differencing can introduce high frequency noise, it is suggested to check the signal for stationarity and then apply the differencing to the nonstationary sub-signals just once. A number of tests have been developed for testing the stationarity of a signal. In this study, each reconstructed sub-signal was first tested for stationarity using the Kwiatkowski–Phillips–Schmidt–Shin (KPSS) test [58]. This test is used for testing the null hypothesis that the sub-signal is stationary around a deterministic trend. If the sub-signal is recognised as non-stationary then it is subjected to stationarisation. After applying the test, the differencing technique is applied for the purpose of stationarisation only to those signals which were recognized as non-stationary. The differencing technique be described using the following equation [57]:

$$xr^{dif}(m) = xr(m) - xr(m-1)$$
, where $m = 2,3, ... n$ (6)

 xr^{dif} is the new stationarised sub-signal. The primary aim of differencing is to remove the stochastic trends responsible for the sub-signal non-stationarity (i.e. to stabilise the mean of a non-stationary sub- signal [59]). This is the simplest method that can be used for the purposes of stationarisation. It is clear that the new transformed sub-signal (i.e. xr^{dif}) is shorter than the original one.

The order of differencing depends on the complexity of the signals. More specifically, if a signal lacks a tendency to return to its mean value then higher order of differencing might be required. In general the differencing method is a rather simple but powerful process so on most occasions quite high stationarity is achieved through just one application. In most studies which apply differencing for other purposes not related to fault diagnosis and machinery dynamics the process is applied just once [60-62].

In this work, one application of differencing was sufficient to bring the sub-signals to stationary ones.

The differencing technique has been used for purposes of stationarisation in climate research [63]; to the knowledge of the authors, however, it has not been used in the field of machinery fault diagnosis.

2.4 Linear AR Modelling

Once the sub-signals (i.e. bearing vibration signals) are stationarised they can be represented by the linear autoregressive (AR) model.

The structure of a linear AR model can be described as follows [64]:

$$xr(m) = a_0 + a_1 \cdot xr(m-1) + a_3 \cdot xr(m-2) + \dots + a_p \cdot xr(m-p) + \varepsilon(m)$$
(7)

where

xr(m) is the predicted signal value at time m which is linearly related to (p) previous values;

p is the order of the model;

 a_i (i =0,1,2...,p) are weighting coefficients (i.e. model coefficients);

 $\varepsilon(m)$ is the error term, which represents the difference between the actual and linearly predicted values.

The model coefficients can be estimated using different algorithms. In this research, the least square algorithm was used. The performance of the model (i.e. goodness of fit) in representing the experimental signal data is measured by calculating normalised loss function based on the normalised mean square error (NMSE), as given by the equation below:

Goodness of Fit|_{NMSE} =
$$\left(1 - \frac{\sqrt{\sum_{i=1}^{i=n} \left(xr_{pr}(i) - xr_{ms}(i)\right)^2}}{\sum_{i=1}^{i=n} xr_{pr}(i) - \overline{xr_{ms}}}\right) * 100\%$$
 (8)

where:

*xr*_{pr} is predicted sub-signal;

 xr_{ms} is the real time measured sub-signal;

 \overline{xr}_{ms} is the mean value of real time sub-signal;

n is the number of data points (i.e. sub-signal length).

The calculations for the least square algorithm and the NMSE values mentioned above were carried out using MATLAB.

2.5 Model order selection

The determination of the optimum model order is of great importance, as an incorrect model order can lead to either over-fitting or under-fitting, which both give poor model prediction and result in a poor and/or false diagnosis [34, 65] Thus, a proper order selection can reduce the errors of over-fitting or under-fitting considerably. Several methods, based on increasing the model order and calculating an error criterion function of model prediction, have been developed for determining the optimum model order. This function is primarily based on the calculations of the residual sum of squared errors between the predicted and measured data. The optimum model order minimises the error criterion function. In this research, the final prediction error (FPE) criterion is used. This FPE criterion can be defined in the following way (Eq. (9)):

$$FPE = V. (1 + p/n)/(1 - p/n)$$
(9)

where

V is the loss function which is the variance of the residuals (i.e. the difference between the predicted and the actual signal);

p is the model order;

n is the number of data points.

According to this criterion, the model order corresponding to the minimum value of FPE is selected as the optimum order

2.6 Dealing with model orders

There might be some cases where the model orders for different signals/signal categories are not the same as some fault types may require a different model order. As these model orders will represent the lengths of the feature vectors formed for the diagnosis stage, it means the lengths of the feature vectors will not be the same. In this case, the equalising step is necessary in order to apply the NN rule properly in the fault diagnosis stage. Three different possibilities are investigated to see whether the way of equalising can affect the performance of the methodology or not. Assuming that the minimum and maximum optimum orders for several signals/categories are (p_{min}) and (p_{max}) respectively, the equalising possibilities are:-

2.6.1 **Zero padding.** In this procedure the feature lower order vectors ($l < p_{max}$) are transformed by adding ($p_{max} - l$) zero elements at the ends (see Figure 1). Eventually all the feature vectors acquire the maximum length p_{max} .

 $(p_{\max} - l) \text{ elements}$ $[a_o \ a_1 \ a_2 \ \dots \ a_l \ 0 \ 0 \ 0 \ 0]$ $[a_o \ a_1 \ a_2 \ \dots \ \dots \ a_{p_{max}}]$

Figure 1: Illustration of zero padding.

2.6.2 **Variance Threshold Method**: In this method, it is proposed to select the model coefficients which have the highest variance contribution among the feature vectors. This can be done using the variance threshold method

(VTM), which proposes to select only the model coefficients with a variance higher than the mean value of all the features vectors variances.

2.6.3 **Trimming**. It is proposed to trim/cut the features vectors of length 1, where $l > p_{min}$, to length (p_{min}) . If $[a_0 \ a_1 \ a_2 \dots a_l]$ is a longer feature vector (i.e. $l > p_{min}$), then its last 1- p_{min} components are removed and the new vector is $[a_0 \ a_1 \ a_2 \dots a_{Pmin}]$ (see Figure 2).

 $\begin{bmatrix} a_o & a_1 & a_2 & \dots & a_{l-3} & \overline{a_{l-2} & a_{l-1} & a_l} \end{bmatrix}$ $\begin{bmatrix} a_o & a_1 & a_2 & \dots & a_{p_{min}} \end{bmatrix}$

Figure 2: Illustration of trimming.

In this research, all the three possibilities above were applied during the detection and the fault identification stage. The best one in terms of highest correct classification rate was selected and used further for the next stage of fault severity estimation.

3 Diagnosis Method

In this study feature vectors, which are made of the coefficients of the autoregressive models (see Section 2.4) of the sub-signals, are used in the diagnosis stages. The coefficients of each LTIVAR model, after being subjected to one of the above procedures in order to equalise their numbers, are ordered to form the feature vectors. Thus each feature vector is made of the coefficients corresponding to a certain sub-signal. In the first stage, the sub-signal is assigned to one of the categories corresponding to different bearing conditions mentioned above. Once a signal was identified as faulty in the first stage, it is further classified in the second stage into one

of the fault severity levels (small, medium and large). According to the introduced stages the following signal categories are adopted. For the first stage four categories are used, namely healthy bearings signals (H), Inner race fault signals (IRF),Outer race fault signals (ORF) and ball bearing fault signals (BF). For the second stage of the severity estimation only three categories are used, namely small faults (S), medium faults (M) and large faults (L). For both stages, the identification and the severity estimation, the feature vectors are divided into two samples: a training and a testing sample. The feature vectors from the training sample were used to define the matrices corresponding to each signal category (\mathbf{K}_a matrices for the first stage and \mathbf{K}_b for the second stage). Each of these matrices is formed by arranging the corresponding feature vectors in rows, (see Eq (10)). $\mathbf{K}_a = 1, 2...4$ and $\mathbf{K}_b = 1, 2, 3$)

For each matrix, the number of columns equals the number of model coefficients which is the optimum model order (p), while the number of rows (N) equals number of subsignals in that category:

$$\mathbf{H}_{K_{i}} = \begin{bmatrix} a_{K_{i}11} & a_{K_{i}12} & \dots & a_{K_{i}1p} \\ a_{K_{i}21} & a_{K_{i}22} & \dots & a_{K_{i}2p} \\ \vdots & \vdots & \ddots & \vdots \\ a_{K_{i}N1} & a_{K_{i}N2} & \dots & a_{K_{i}Np} \end{bmatrix}$$
(10)

where K_i corresponds to one of the categories in the diagnosis stages (i.e. fault identification $K_i \in K_a$ and quantification $K_i \in K_b$).

For both fault classification stages, the nearest neighbour (NN) method [66]was used. According to this method, a feature vector is assigned to its nearest category. In this study, the distances of a feature vector to each of the categories (represented by matrix \mathbf{H}_{K_i} (see Eq. (10)) were measured by using the Mahalanobis distance. The Mahalanobis distance measures the distance between a vector and a set of vectors. Here it was used to measure the distance between a feature vector and a matrix \mathbf{H}_{K_i} . The mean of the row feature vectors for each of the matrices \mathbf{H}_{K_i} is calculated as follows:

$$\mathbf{E}_{K_{i}} = \frac{\sum_{j=1}^{N} \left(a_{K_{i}j1....a_{K_{i}}jp} \right)}{N}$$
(11)

The Mahalanobis distance to the mean vectors $\mathbf{E}_{\mathbf{K}}$ is measured according to:

$$D_{K_i}(\mathbf{f}\mathbf{v}, \mathbf{E}_{K_i}) = (\mathbf{f}\mathbf{v} - \mathbf{E}_{K_i}) \cdot \mathbf{S}^{-1} \cdot (\mathbf{f}\mathbf{v} - \mathbf{E}_{K_i})'$$
(12)

where

 D_K is Mahalanobis distance;

fv is a feature vector from the testing sample;

 \mathbf{S}^{-1} is the inverse of the category covariance matrix \mathbf{H}_{K_i} .

The prime (') denotes the transpose of the vector $(\mathbf{fv} - \mathbf{E}_{K_i})$.

It is important to mention that both $(\mathbf{fv}, \mathbf{E}_{K_i})$ lengths are already equalised using one of the procedures described in Section 2.6.

When the distances of a new feature vector to each of the categories are obtained, the vector is classified to the category for which the distance above (see Eq. (12)) has a minimum; that is, **fv** belongs to the category for which $D_{K_i}(\mathbf{fv}, \mathbf{E}_{K_i})$ has minimum over all K_i.

Figure 3 shows the stages of the diagnosis procedure. It is clear from the figure that in a case in which the new feature vector is assigned as healthy, it will not go further for the second stage of diagnosis.

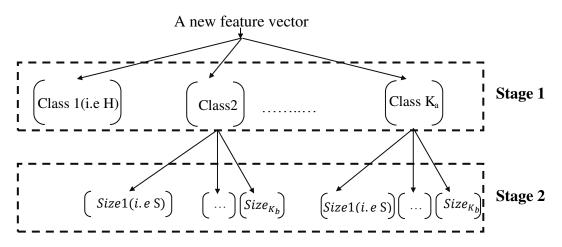


Figure 3: A scheme illustrating the bearing condition categories for both the diagnosis stages

Figure 4 shows the block diagram of the whole process of the methodology. There are three main blocks in the flow chart (1, 2 and 3), each bordered by a dashed rectangle.

- Block 1: the stages of signal pretreatment.
- Block 2: Fault identification.
- Block 3: Fault severity estimation.

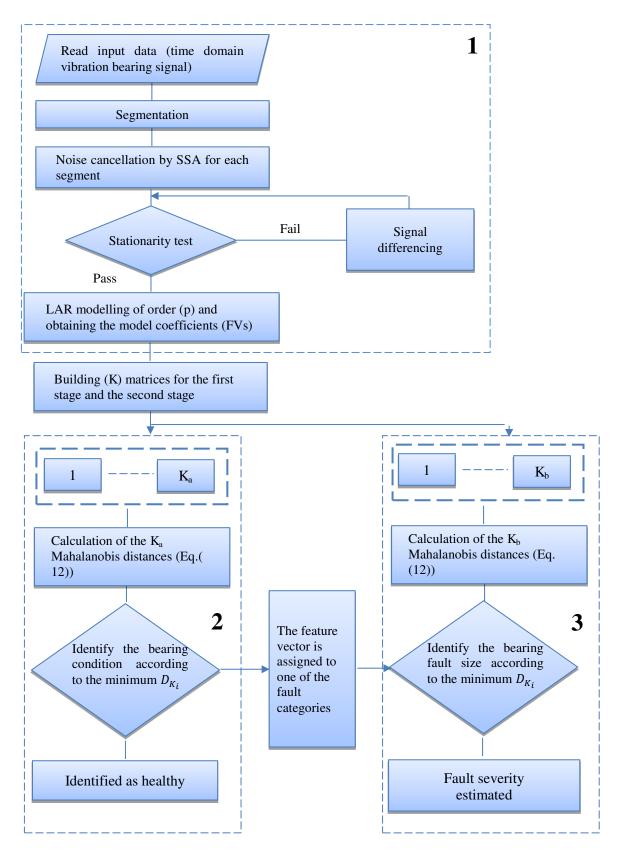


Figure 4: A block diagram illustrating the proposed classification method

The performance of the methodology was estimated by using the so-called confusion matrix. The confusion matrix is a square ($K_k x K_k$) matrix, where K_k (i.e, either K_a or K_b) is the number of sub-signal categories. The columns represent the predicted classes, while the rows represent the actual classes. Thus, the main diagonal represents the correctly categorised signals, while all the other elements represent the miscategorised signals. The name 'confusion' stems from the fact that this matrix makes it easy to evaluate whether the proposed methodology confuses two or more classes (i.e. mislabelling one category as another). Table 1 shows the structure of a confusion matrix:

Actual				
class/predicted	1	2		K _k
class				
1	C11%	C12%		C1K _k %
2	C21%	C22%		C2K _k %
•	•	•	•	•
	•	•	•	•
K _k	CK _k 1%	CK _k 2%		CK _k K _k %
ıx _k		$CIX_{K}2$ /0		CIX _K IX _K /0

Table 1: An example of a confusion matrix

Cij (i and j =1,2...K_k) refers to the percentage of vectors from class i which are classified as class j. It is clear that if i=j, then Cij represents the percentage of correct classification. If $i \neq j$, then Cij represents the percentage ratio of the misclassification.

4 Method verification-case studies

The methodology was tested and validated using several bearing vibration datasets obtained from different test rigs.

4.1 Case Study 1

The bearing vibration data were obtained from the test rig of Case Western Reserve University (CWRU). The data-bearing centre [67] shown in Figure 5 consists of a 2 HP three-phase induction motor: a dynamometer. The drive end bearing (SKF 6025 deep grove ball bearing) data were used in this analysis. An electrical discharge machine was used to introduce single point faults in the bearing raceways and ball elements of different bearings with fault diameters of 0.007, 0.014, and 0.021 inches and a depth of 0.011 inches. The bearing vibration data were obtained at a sampling rate of 12 kHz for different fault sizes, with speed varying from 1797 rpm (0 HP) to 1730 rpm (3 HP). The data for the outer race fault were taken with the fault position centred at the 6 o'clock position with respect to the load zone.

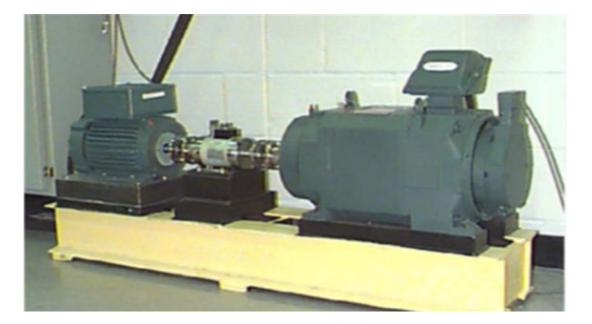


Figure 5: The bearing test rig [65]

4.2 Case Study 2

The test data for this case study was acquired from a bearing test rig at Strathclyde University/Department of Mechanical and Aerospace Engineering, shown in Figure 6. The test rig consists of a 1Hp shunt DC motor, bearing assembly and a mechanical loading system. The bearings used in the experiment are SKF deep grooves 6308. The motor shaft's torque is transmitted to the test bearing assembly by a pinion-toothed belt mechanism. As the pinions at the motor and the entrance of the bearing assembly are of different diameters, the rotational speed of the test bearing shaft is measured by a contactless tachometer. Faults were introduced using an electrical discharge machine on the inner raceway and outer raceway using different bearings with a fault diameter of 0.05 inches. The bearing vibration data were obtained for healthy, inner raceway and outer raceway fault conditions at two rotational speeds (350 and 500 rpm). Signals were obtained at a 2.5 kHz sampling rate.



Figure 6: Bearing test rig at Strathclyde University

4.3 Case Study 3

The data were acquired from a test assembled at the Department of Mechanical and Aerospace Engineering of Politecnico di Torino by the Dynamics & Identification Research Group (DIRG) (Figure 7) [68]. The signals were acquired at a 102.4 kHz sampling frequency for both healthy, defective inner raceway and defective roller bearings at 500 Hz speed and 1.8 kN load. The fault diameters were 0.006, 0.0098 and 0.0178 inches.



Figure 7: DIRG test rig, the triaxial accelerometers (X, Y, Z) and the damaged roller used in the tests [56]

5 Results and discussion

The bearing vibration signal sets that were considered in the validation of the methodology are labelled as (CW) for the data corresponding to Case Study 1 (i.e. CWRU), (ST) for those data corresponding to Case Study 2 (i.e. Strathclyde) and (PT) for those corresponding to Case Study 3 (i.e. Politecnico di Torino)

5.1 Signal pretreatment

In this section, the steps of the signal pretreatment stage are illustrated visually. A sub-signal from a bearing with a small fault on the inner race (e.g case study3) is used as an example. Figure 8 shows the raw sub-signal in the time domain. The x-axis represents the number of points (2048) and the y axis represents the acceleration of the bearing vibration in m/s^2 .

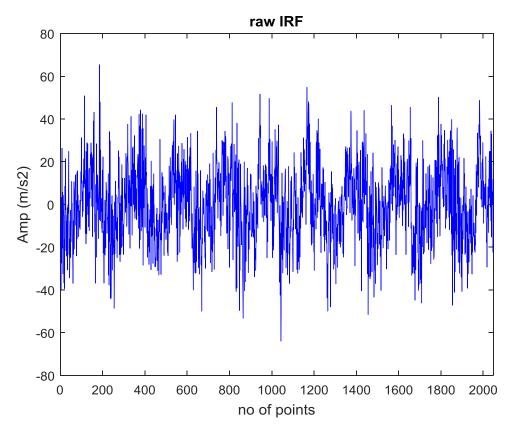


Figure 8: A signal from data set 3, a bearing with inner race fault

As mentioned in Section (2.2), the signal is decomposed by the singular spectrum analysis into a number of components. Figure 9 shows the original sub-signal as well as the first five components obtained by the SSA. It is clear that the first component corresponds to the trend of the signal.

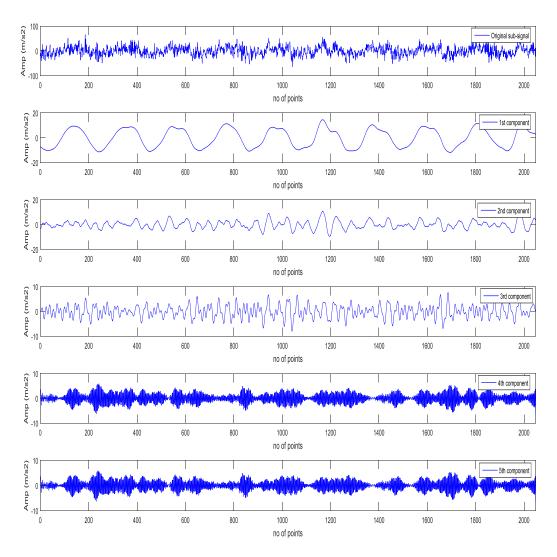


Figure 9: Original sub-signal and the first five components obtained from the singular spectrum analysis

As mentioned above in Section 2.2, a number of the PCs are selected so that at least 90% of the original sub-signal variance is recovered in the new reconstructed signal. In this example 19 out of the 43 components (e.g contains nearly 90%) are selected. The structure-less noise is removed by rejecting the low contribution components.

In the Figure 10 shows the effect of the noise cleaning by SSA. The blue and red lines refer to the raw and noise cleaned signal respectively where the signal becomes smoother due to removing the structure-less noise.

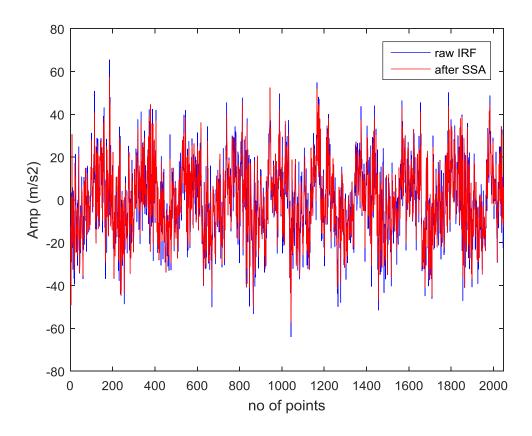


Figure 10: Raw signal verses noise cleaned signal by singular spectrum analysis (SSA)

When the sub-signal fails at the test of stationarity (Section 2 .3), it is then subjected to differencing to stabilize its mean and to be transformed to a stationary. It is important to know that not all the sub-signals are differenced, but only those which fail in the test of stationarity. The differenced sub-signals are subjected again to the test of stationarity to see whether one differencing is sufficient to bring it to stationarity. For all the cases, differencing was applied once. Figure 11 shows the signal after differencing. It can be seen from the figure that the sub-signal mean is less fluctuated compared to the sub-signal shown in the Figure 10.

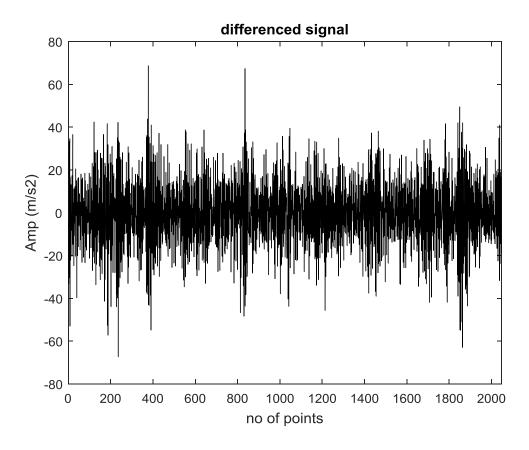


Figure 11: A differenced sub-signal

The sub-signal is then subjected to modelling by the LTIVAR model (Eq.7).

Figure 12 shows both the differenced (black line) and the modelled sub-signal (red line). It can be seen that the model is accurately representing the differenced sub-signal (e.g NMSE is 97.6% see Eq.(8)).

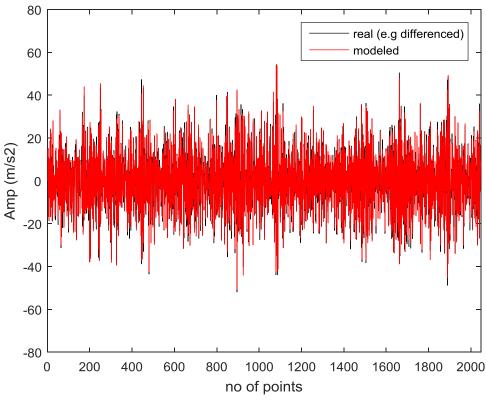


Figure 12: a differenced sub-signal versus modelled sub-signal

5.2 Signal Diagnosis

5.2.1 Case Study 1

The data obtained from the drive end bearing and used for validating the methodology for fault type identification and fault severity estimation are shown in Table 2. The notations are as follows: H - healthy bearing; IRF - bearing with a fault on the inner raceway; BF - bearing with a fault on the rolling element; ORF - bearing with a fault on the outer raceway; S - small fault (0.007 inch diameter); M – medium-size fault (0.014 inch diameter) and L - large fault (0.021 inch diameter).

Case no.	Motor speed(rpm)	Signal Category
CW1	1797	Healthy, (IRF, BF and ORF) small fault 0.007"
CW2	1772	Healthy, (IRF, BF and ORF) small fault 0.007"
CW3	1750	Healthy, (IRF, BF and ORF) small fault 0.007"
CW4	1730	Healthy, (IRF, BF and ORF) small fault 0.007"
CW5	1797	IRF (S,M and L)
CW6	1797	BF (S,M and L)
CW7	1797	ORF (S,M and L)
CW8	1772	IRF (S,M and L)
CW9	1772	BF (S,M and L)
CW10	1772	ORF (S,M and L)
CW11	1750	IRF (S,M and L)
CW12	1750	BF (S,M and L)
CW13	1750	ORF (S,M and L)
CW14	1730	IRF (S,M and L)
CW15	1730	BF (S,M and L)
CW16	1730	ORF (S,M and L)

Table 2: The drive end bearing vibration datasets obtained from case study 1used in the bearing condition diagnosis

The cases (from CW1 to CW4) were used in the first stage of classification (fault identification), while the others were used in the second stage of diagnosis (fault estimation).

For each case in Table 2, the signals were segmented into a number of segments of 2048 points each. Each segment was then decomposed by the singular spectrum analysis into

a number of components equal to the ratio of sampling rate to the minimum bearing fault frequency. For example, in case CW2 (speed=1772 rpm; see Table 2) the minimum bearing fault frequency was that of the fault on the outer race, which equals 3.5848*rotational speed (in Hz) [67]. The number of decomposed components therefore equals (12000 / (3.5848*1772/60)) = 114 components. The number of the selected components for reconstruction purposes was determined so that at least 90% of the original signal variance was contained by the reconstructed signal. The model optimum order and goodness of fit values for CW2 are given in Table 3.

Signal Category	Model optimum order (p)	NMSE (Eq. (8))
Н	5	99.96%
IRF	12	99.2%
BF	8	98.96%
ORF	6	99.94%

Table 3: The model optimum order and NMSE values for dataobtained at 1772 rpm

It can be seen from Table 3 how well the model predicts the majority of de-noised subsignals.

Samples of the confusion matrices (CW2) described in Section 3 are shown below in Tables 4-6, based on the different possibilities of equalisation of feature vector length discussed in Section 2.6. The number of the feature vectors used in the first stage of diagnosis is 232 (4 signal categories*58 segments for each category, made by dividing the length of original signal by the segment length (2048)). Half of them (116) are used for forming the signal category matrices (see Section 3) while the remaining 116 are used as testing feature vectors.

		Н	IRF	BF	ORF
Actual	Н	100%	100%	0%	0%
	IRF	0%	100%	0%	0%
	BF	0%	0%	100%	0%
	ORF	0%	0%	0%	100%

Prediction

Table 4 : The confusion matrix using feature vectors modified by
zero padding: 116 feature vectors at 1772 RPM

		Н	IRF	BF	ORF
	Н	100%	0%	0%	0%
IRF BF ORF	IRF	0%	100	0%	0%
	BF	0%	0%	89.65%	10.35%
	ORF	0%	0%	79.3%	20.7%

Prediction

Table (5) : The confusion matrix using feature vectors modified by variance threshold method : 116 feature vectors at 1772 RPM

		Н	IRF	BF	ORF
	Н	100%	0%	0%	0%
Actual	IRF	0%	100%	0%	0%
Act	BF	0%	0%	100%	0%
	ORF	0%	0%	0%	100%

Prediction

Table (6) : The confusion matrix using feature vectors modified using trimming: 116 feature vectors at 1772 RPM For the data used in this analysis, it is found that using any of the zero padding and trimming ensures a very high correct classification rate. Accordingly, one of these two methods was selected (e.g trimming) and all subsequent results shown in this paper were obtained following it.

An example of the confusion matrix for fault size estimation (CW8) using trimming is shown in Table 7. In the stage for fault severity diagnosis, the number of feature vectors was 174 (3 categories*58). The number of the feature vectors from the testing sample was 87 (0.5*174).

		predicted		
		S	М	L
	S	100%	0%	0%
Actual	М	0%	100%	0%
	L	0%	0%	100%

Table 7: Correct classification rate using features vectors based on trimming method for estimation of different fault sizes on the inner raceway at 1772 rpm.

In order to present the correct classification rates (%), the average of the values on the diagonal on each confusion matrix are shown rather than the entire confusion matrix, as the values on the diagonals represent those of correct classification (see Table 1).

For example, for the confusion matrix in Table 7, corresponding to the case CW8, the average of diagonal values is (100%+100%+100%)/3 = 100%. Table 8 shows the correct classification rates (in percent) for all the cases mentioned in Table 2.

Case no.	Motor speed (rpm)	Signal Category	No of testing FVs	Average % correct classification rate	
CW1	1797	Healthy, (IRF, BF and ORF) _{small} fault 0.007" diameter	116	100%	
CW2	1772	Healthy, (IRF, BF and ORF) _{small} fault 0.007" diameter	116	100%	
CW3	1750	Healthy, (IRF, BF and ORF) _{small} fault 0.007" diameter	116	100%	
CW4	1730	Healthy, (IRF, BF,ORF) small fault 0.007'' diameter	116	100%	
CW5	1797	IRF (S,M and L)	87	100%	
CW6	1797	BF (S,M and L)	87	100%	
CW7	1797	ORF (S,M and L)	87	100%	
CW8	1772	IRF (S,M and L)	87	100%	
CW9	1772	BF (S,M and L)	87	100%	
CW10	1772	ORF (S,M and L)	87	100%	
CW11	1750	IRF (S,M and L)	87	100%	
CW12	1750	BF (S,M and L)	87	98.8%	
CW13	1750	ORF (S,M and L)	87	100%	
CW14	1730	IRF (S,M and L)	87	100%	
CW15	1730	BF (S,M and L)	87	100%	
CW16	1730	ORF (S,M and L)	87	100%	

Table 8: The average correct classification rates based on trimming as equalisation of feature vectors for case study 1

It can be seen that the average correct classification rates are 100% for all of the cases except one, CW12, in which one feature vectors has been misclassified.

Case Study 2

The data obtained from the test rig presented in Section 4.2 are also used for validating the methodology for fault type identification. The data considered are shown in the Table 9.

Case no.	Motor speed (rpm)	Signal Category	
ST1	350	Healthy, IRF, ORF	
ST2	500	Healthy, IRF, ORF	

Table 9: The bearing vibration datasets obtained from case study 2 used for faulttype identification

The notation (ST) refers to the test rig at Strathclyde University from which the test data were acquired.

The number of signals used for classification was 375 (125 signals*3 classes). Each of these signals is made of 2048 points. Table 10 illustrates how the performance of the methodology for Case Study 2.

Case no.	Motor speed (rpm)	Signal Category	No of testing FVs	Average % correct classification rate
ST1	350	Healthy, IRF and ORF	375	98.4%
ST2	500	Healthy, IRF and ORF	375	98%

Table 10: The average correct classification rates based on trimming as equalisation of feature vectors for case study 2

It can be seen from Table 10 that very few signals have been misclassified. At 350 rpm, only 6 feature vectors from faulty inner race (IRF) category were misclassified as healthy (H) category. At 500 rpm, only 8 feature vectors from the healthy (H) category were misclassified as faulty outer race (ORF) category faulty (outer raceway fault).

5.3. Case Study 3

Table 11 shows the data acquired from the test rig introduced in Section 4.3.

Case no.	Motor speed (rpm)	Signal Category		
PT1 30000 (Healthy, IRF and BF) small fault 0.006 i		(Healthy, IRF and BF) small fault 0.006 inch diameter		
PT2	30000	IRF (S, M and L)		
PT3	30000	BF (S, M and L)		

Table 11: The bearing vibration datasets obtained from case study 3 used for the bearing condition diagnosis

The number of feature vectors (FVs) used for classification in any case (PT1, PT2 and PT3) was 597 (3 signal categories*199 FVs).Table 12 illustrates the performance of the methodology for the data from Case Study 3.

Case no.	Motor speed (rpm)	Signal Category	No of testing FVs	Average % correct classification rate
PT1	30000	Healthy, IRF and BF	597	100%
PT2	30000	IRF (S, M and B)	597	100%
PT3	30000	BF (S, M and B)	597	99.8%

Table 12: The average correct classification rates based on trimming as equalisation of feature vectors for case study 3

It can be seen from Table 12 that all the 597 feature vectors corresponding to the cases PT1 &PT2 were correctly classified. For the case PT3 only one feature vector from the small fault signal category was classified as a medium fault signal category.

6 Comparison with published work

The Table 13 shows the precision of the present method as compared to some other recent methods which are based on different time series analysis but they use the same part of datasets of CWRU. Several information regarding such as the datasets details, number of testing and training FVs and average correct classification rates are presented in Table 13 presented for these methods and for the method suggested here.

The methods are listed below:

1) Difference histograms (DHs) and feed forward neural network (FFNN) [69]: The difference histograms (DHs) based method includes the formation of scaled representation for histograms of increased segment lengths. Some of the first histogram bins are used as inputs to a FFNN for classification purpose of faults.

2) SSA and back propagation neural network (BPNN) [46]:In this study two sets of feature vectors are developed using SSA. The first FV includes the singular values of some of the first several principal components and the other FV uses the energy of the time domain of sub-signal components corresponding to these principal components. These feature vectors are used as input to the BPNN classifier.

3) In [70], signals from two different accelerometers are used to create a two dimensional representation of the bearing condition. The minimum volume ellipsoid (MVE) method is used to extract the features. Principal component analysis (PCA) is used for selecting the most important features. The last step is to input the selected features to the nonlinear nearest neighbour classifier.

It can be seen from Table 13 that all the compared methods achieve a rather good classification rate. From all the four methods compared it can be seen that the method suggested here demonstrates the best classification rate, which is between 98.8-100%

Method	Dataset (single point defect size width; load; signal length)	Training and testing datasets	Condition classified	Average testing accuracy (%)	Fault features
1)DH and FFNN[69]	0.18, 0.36,0.53mm; 0–3 HP load;30000 data points	Both 144	(IF, OF and BF classification only)	92-95	First 6 histogram bins
2)SSA and BPNN [46]	0.18, 0.36, 0.53, 0.71 mm; 0– 3 HP load;6100 data points	Train—336 test—144	H, IF,OF and BF	96.53–100 95–100	4 singular values 3 energy features
3)MVE, PCA and nonlinear neighbour classifier [70]	0.18, 0.36,0.53mm , 0-3 HP, 2000 data points		Healthy and faulty. It was reported by the author that there is some overlapping among some fault classes	94.68-99.98	-
4)Differencing, SSA and AR [present work]	0.18, 0.36,0.53 mm; 0-3 HP loads; 2048 data points	Train-464 Test-464	H, IF, OF and BF	98.8-100	coefficients of LTIVAR model

7 Conclusions

The present work suggests a new methodology for rolling element bearing fault diagnosis based on linear time invariant autoregressive modelling and pattern recognition. The suggested method is relatively simple in the sense that it uses a combination of simple processes to first transform the signal and then determine the condition of the bearing. A new signal pretreatment process is applied before subjecting the signals to modelling. This process includes noise cleaning, using singular spectrum analysis (SSA), and stationarisation of the bearing vibration signal by the differencing procedures. The methodology aims to transform the signal to bring it close to a stationary one, rather than complicating the model to bring it closer to the signal. The signal pretretment proposed enhances the precision of the model prediction, which is influenced by the presence of noise and non-stationary parts in the signal. The LTIVAR model coefficients are extracted using the least squares method and used as FVs for signal classification purpose. The FVs are then presented to the 1-NN algorithm based on the Mahalanobis distance. The signals were assigned to the category of their nearest neighbour. The performance of the methodology is then assessed on the basis of confusion matrices, which provide the percentage of correctly- and incorrectlyclassified signals.

The methodology suggested encompasses several relatively simple procedures, which facilitates its potential practical application and its possible automation.

The developed methodology is intended to serve as a stepping-stone towards the development of a new process for bearing fault diagnosis which will not require the availability of sample signal data from the different categories. This will be based on a study of the behaviour of the AR coefficients with the presence and the growth of different faults, which the authors are currently conducting.

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