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Krajník, Kulich, Mudrova, Ambrus, Ducktett: *Where's Waldo at time t ? Using Spatio-Temporal Models for Mobile Robot Search*, In International Conference on Robotics and Automation, Seattle, 2015.

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Where’s Waldo at time t ?

Using Spatio-Temporal Models for Mobile Robot Search

Tomáš Krajník¹ Miroslav Kulich² Lenka Mudrová³ Rares Ambrus⁴ Tom Duckett¹

Abstract—We present a novel approach to mobile robot search for non-stationary objects in partially known environments. We formulate the search as a path planning problem in an environment where the probability of object occurrences at particular locations is a function of time. We propose to explicitly model the dynamics of the object occurrences by their frequency spectra. Using the environment model proposed, our path planning algorithm can construct plans that reflect the likelihoods of object locations at the time the search is performed.

Three datasets collected over several months containing person and object occurrences in residential and office environments were chosen to evaluate the approach. Several types of spatio-temporal models are created for each of these datasets and the efficiency of the search method is assessed by measuring the time it took to locate a particular object. The experiments indicate that modeling the dynamics of objects’ occurrence reduces the average search time by 35% to 65% compared to maps that neglect these dynamics.

Index Terms—mobile robotics, long-term autonomy

I. INTRODUCTION

Searching for an object is a practical task of everyday life that would be trivial if we had perfect knowledge about our own environment - knowing the position of a searched object in advance means that the search itself does not have to be performed at all. Unlike in highly structured and well-defined worlds of factory assembly lines that are engineered to keep uncertainty of object positions minimal, the locations of most objects in human-populated environments are inherently uncertain. The uncertainty of human-populated environments is induced by the humans themselves, as they are not only changing their own locations, but also alter the positions of the objects they use. This motivates the need to understand (or at least represent) the dynamic processes that influence the locations of the humans and the items they use.

We assume that the search task is supposed to be carried out by a mobile robot that is able to move through the environment and detect the searched object using its on-board sensors. To perform the search efficiently, the robot has to be able to plan its motion through the environment. Better knowledge about possible object location means more efficient plans and hence, shorter times to locate the desired object. Most of the path-planning algorithms require this

knowledge in form of a probability distribution over possible object locations. This distribution is typically constructed by means of probabilistic inference that takes into account several factors including the history of the searched object locations.

We argue that in human-populated environments, the object locations are primarily influenced by human activities that tend to exhibit daily and weekly periodicities. In our approach, we show that identification and modeling of these periodicities leads to a more faithful representation of possible object locations and hence to a faster and more efficient search.

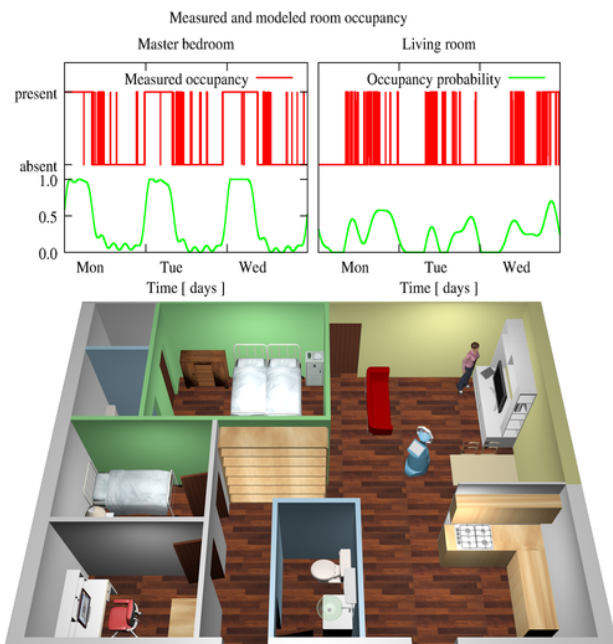


Fig. 1: Example environment with people presence probabilities in two rooms.

To represent the probabilities of object locations we use a traditional topological map where each node is associated with a temporal model that captures the dynamics of the object occurrence at the particular location. These temporal models are based on Periodic Gaussian Mixtures similar to the approach proposed in [1] and the Frequency Map Enhancement (FreMEn) [2] technique that allows into introduce dynamics to static environment models. We evaluate the Gaussian- and Spectral- based temporal models on datasets gathered over several weeks and show that a search performed by a mobile robot is faster than when using purely

¹Lincoln Centre for Autonomous Systems, University of Lincoln, UK {tkrajnik, duckett}@lincoln.ac.uk

²Faculty of Electrical Engineering, Czech Technical University in Prague, Czech Republic {kulich}@fel.cvut.cz

³Intelligent Robotics Lab, University of Birmingham, UK {lxm210}@cs.bham.ac.uk

⁴KTH - Royal Institute of Technology, Sweden {raambrus}@kth.se

spatial models with probabilities that neglect environment dynamics.

II. RELATED WORK

The problem of finding a static object of interest has been studied from various perspectives. The operational research community defines the Minimum Latency problem (MLP, also known as the Traveling Deliveryman Problem or the Traveling Repairman Problem) as a problem of constructing a tour through all nodes in a graph that minimizes a sum of latencies to the nodes, where the latency of a node is a distance needed to travel to this node. The problem has been proven to be NP-hard [3], nevertheless several exact exponential time algorithms were introduced such as an integer linear programming approach [4] or a branch and bound algorithm [5]. Moreover, several approximate algorithms were presented recently. Salehipour et al. [6] present a meta-heuristic combining General Randomized Adaptive Search (GRASP) with Variable Neighborhood Descent (VNS). A meta-heuristic called GVNS (General Variable Neighborhood Search) is introduced in [7], while integer linear programming is used in [8].

Koutsoupias et al. [9] extend MLP by introducing the Graph Searching Problem (GSP), where the latency of each node is multiplied by a constant weight associated with each node and prove that GSP can be reduced to MLP under some conditions. Furthermore, Ausiello et al. [10] present a reduction algorithm for the metric GSP and the GSP on tree networks.

While the previous approaches are defined on a graph, Sarmiento et al. [11] formulates the problem in the polygonal domain, where the time required to find a static object is a random variable induced by a choice of search path and a uniform probability density function for the object's location. They propose a two-stage process to solve the problem: a set of locations (known as guards from the art gallery problem [12]) to be visited is determined first, followed by finding the order of visiting those locations minimizing the expected time to find an object. The optimal order is determined by a greedy algorithm in a reduced search space, which computes a utility function for several steps ahead. This approach is then used in [13], where robot control is assumed in order to generate smooth and locally optimal trajectories. Recently, Kulich et al. presented the search problem for a robot operating in an unknown environment [14].

Other approaches model spatial relations about objects in the scene and use these relations to constrain the possible objects locations. It has been shown that the refinement of the locations considered for search has a positive influence to search performance [15]. For example, object search based on the basis of Qualitative Spatial Relations is presented in [16], while five priors representing structure of the world and the specific scene are introduced and encoded into a probabilistic model and used to build consistent hypotheses about object locations in [17].

The idea of modeling the long-term dynamics of indoor environments been presented in [2] where the authors argue

that part of the environment variations exhibit periodicities and represent the environment states by their frequency spectra. The concept of Frequency-based Map Enhancement (FreMEn) has been applied to occupancy grids [18] to achieve compression of the observed environment variations and to landmark-based maps in order to increase robustness of robot localization [19]. In this paper, we show that usage of dynamic maps based on the same concept allows for better planning in the context of robotic search.

III. PROBLEM FORMULATION

The search problem can be generally understood as navigation through an environment in order to find an object with an unknown location. By finding an object we mean the situation when it is firstly detected by robot's sensors. A criterion to minimize is the time when this situation occurs. In this paper, we assume that the topology of the environment is a priori known and the object to be found remains stationary during the search.

The problem is formally defined as a variant of the Graph Searching Problem [9]: That is, given

- an undirected graph $G(V, E)$, where V is a finite set of vertices and E is a set of edges between these vertices,
- $d : E \rightarrow \mathbb{R}$ the time needed to traverse the edge, and
- $p : V \rightarrow \langle 0, 1 \rangle$ a probability of presence of the searched object at the given vertex,

the objective is to find a walk $\omega = \langle \omega_0, \omega_1, \dots, \omega_k \rangle$ in G , which visits all nodes of V at least once (i.e. $\forall v \in V \exists \omega_j \in \omega : \omega_j = v$) and which minimizes the expected time to find the object:

$$\omega = \arg \min_{w \in \Omega} \mathbb{E}(T|w) = \sum_{i=0}^{|\omega|} \tau^w(i) p(w_i), \text{ where} \quad (1)$$

$$\tau^w(i) = \sum_{\iota=0}^i d(w_\iota, w_{\iota+1})$$

is the time when w_i , the i -th vertex of the walk w is visited and Ω is a set of all possible walks in G . The minimal expected time is then

$$T_{exp} = \mathbb{E}(T|\omega) = \sum_{i=0}^{|\omega|} \tau^\omega(i) p(\omega_i). \quad (2)$$

IV. TEMPORAL MODELS

The underlying environment representation used in our approach is a topological map, where nodes represent distinct areas and edges represent the robot's ability to move between them. Each node of our map is associated with a probability of person presence and each edge contains information about the time it takes to move between the map's nodes. Unlike traditional maps, the probabilities associated with particular nodes are not constant, but are functions of time. These functions are estimated through long-term observation of the person or object presence at the particular locations.

A. Frequency map enhancement

The Frequency Map Enhancement (FreMEn) is a method that can introduce dynamics into static environment models. Its primary application domain is mobile robotic mapping and localization in scenarios where the robots are required to operate autonomously for long periods of time. The FreMEn assumes that most of the indoor environment states are influenced by humans that perform their regular daily activities. The regularity and influence of these activities on the environment states is obtained by means of frequency transforms. Specifically, the FreMEn extracts the frequency spectra of binary functions that represent long-term observations of environment states, discards non-essential components of these spectra and uses the remaining spectral components to represent probabilities of the corresponding binary states in time. The authors of the FreMEn have shown that introducing dynamics into (volumetric, topological and landmark) environment models causes these to represent the world more faithfully [2], [18], which results in increased robustness of robot self-localization [19].

So let us assume that the presence of an object at a particular area of the environment is represented by a binary function of time $s(t)$. Let us represent the uncertainty of $s(t)$ by the presence probability $p(t)$. Then, the main idea of the FreMEn is to represent a (temporal) sequence of states $s(t)$ by the most prominent components of its frequency spectrum $S(\omega) = \mathcal{F}(s(t))$. The advantage of this representation is that each spectral component of $P(\omega)$ is represented by three numbers only which leads to high compression rates of the observed sequence $s(t)$.

To create the FreMEn model, the frequency spectrum $S(\omega)$ of the sequence $s(t)$ is first calculated. The first spectral component a_0 , that represents an average value of $s(t)$ is stored. The remaining spectral components of $S(\omega)$ are ordered according to their absolute value and the n highest components are selected. Each component represents a harmonic function that is described by three parameters: amplitude a_j , phase shift φ_j and frequency ω_j . The superposition of these components, i.e.

$$p(t) = a_0 + \sum_{j=1}^n a_j \cos(\omega_j t + \varphi_j), \quad (3)$$

allows to estimate the probability $p(t)$ of the state $s(t)$ for any given time t . Since t is not limited to the interval when $s(t)$ was actually measured, Eq. (3) can be used not only to interpolate, but also to predict the state of a particular model component. In our case, we use Eq. (3) to predict the presence of the searched object in a particular room.

While the aforementioned representation deals well with periodicities, it suffers from two disadvantages:

- it allows to model only one process per one frequency,
- it poorly models regular, but short-duration events.

Many of the daily activities that occur in an apartment or an office exhibit both of the aforementioned characteristics. Examples include preparing a hot drink, brushing teeth or taking a shower - these activities typically occur on a

regular basis and take a short time. Moreover, some of the aforementioned activities influence objects' presence in the same room.

Application of the Fourier Transform to temporal sequences that possess the aforementioned characteristics causes it to approximate these functions with high-frequency harmonic components. However, these components do not correspond to any regular patterns that actually occur in the environment and therefore decrease the predictive capabilities of the frequency-based temporal model. The results presented in [2], [19] suggest that the best predictive capabilities are achieved by FreMEn models of the 2^{nd} or 3^{rd} order. Such low-order models are not able to represent short-duration events.

B. Gaussian Mixture Models

Gaussian Mixture Models that can approximate multi-dimensional functions as a weighted sum of Gaussian component densities are a well-established method of function approximation. A Gaussian Mixture Model of a function $f(t)$ is a weighted sum of m Gaussian functions:

$$f(t) = \frac{1}{\sqrt{2\pi}} \sum_{j=1}^m \frac{w_j}{\sigma_j} e^{-\frac{(t-\mu_j)^2}{2\sigma_j^2}}. \quad (4)$$

GMMs find their applications in numerous fields ranging from Botany to Psychology [20]. The parameters of individual components of GMMs, i.e. the weights w_k , means μ_j and variances σ_j are typically estimated from training data using the iterative Expectation Maximization (EM) or Maximum A-Posteriori (MAP) algorithms. While the GMMs can model arbitrarily-shaped functions, their limitation rests in the fact that they cannot naturally represent functions that are periodic.

To deal with this issue, we simply assume that people perform most of their activities on a daily basis and thus we consider the object presence in the individual areas as being the same for every day. While this assumption is not entirely correct (as working days will be different from weekends), such a temporal model might be still better than the 'static' model where the probability of object presence is a constant.

Prior knowledge of the periodicity allows to transform the measured sequence of states $s(t)$ into a sequence $p'(t)$ by the following formula

$$p'(t) = \frac{k}{\tau} \sum_{i=1}^{k/\tau} s(t + i\tau), \quad (5)$$

where τ is the assumed periodicity and k is the $s(t)$ sequence length. After calculating $p'(t)$, we employ the Expectation Maximization algorithm to find the means μ_j , variances σ_j and weights w_j of its Gaussian Mixture approximation. Thus, the probability of occupancy of a room at a time t is given by

$$p(t) = \frac{1}{\sqrt{2\pi}} \sum_{j=1}^m \frac{w_j}{\sigma_j} e^{-\frac{(\text{mod}(t,\tau) - \mu_j)^2}{2\sigma_j^2}}, \quad (6)$$

where τ is the a priori known period of the function $p(t)$ and mod is a modulo operator. The advantages of this periodic-GMM-based (PerGaM) model are complementary to the weaknesses of the FFT-based one. It can approximate even short, multiple events, but it can represent only one periodicity that has to be known a priori.

An example comparison of the PerGaM and FreMEn models of a week-long occupancy of an office is shown on Figure 2. The figure 2 demonstrates that while the PerGaM

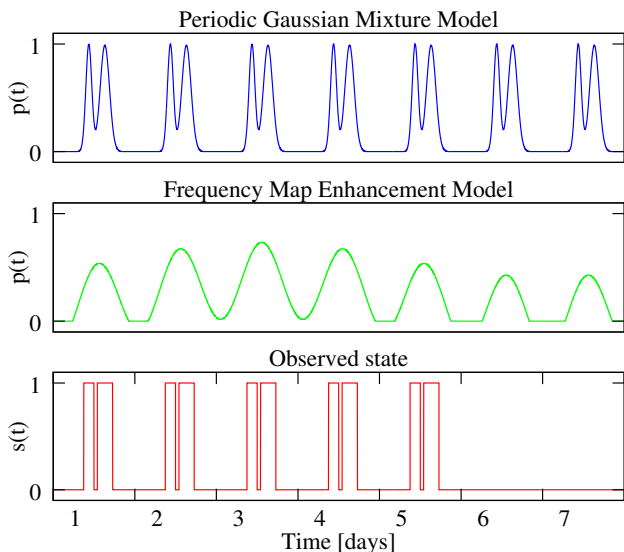


Fig. 2: PerGaM and FreMEn models example/comparison.

can model short-term event like lunch-breaks, it fails to capture the week-long dynamics.

V. SEARCH ALGORITHM

The proposed path-planning search algorithm is a variant of branch-and-bound based on a recursive version of depth first search (DFS).

Procedure BranchAndBound(walk)

```

1 if all vertices visited then
2   if current walk faster than the fastest one then
3     set the current walk as the fastest one;
4 else if estimated walk time exceeds fastest walk then
5   return
6 else
7   foreach not visited vertex do
8     backup the current state;
9     append the shortest path  $P$  to the last vertex;
10    update the cost (duration) of walk;
11    mark all vertices in  $P$  as visited;
12    call BranchAndBound(walk);
13    restore the state;

```

The algorithm systematically constructs all possible walks (see **Procedure** BranchAndBound) in G by calling

BranchAndBound($start$), where $start$ is the vertex where the robot starts searching. The procedure starts with testing whether the current walk contains all vertices of G . If this is the case and the walk w is faster than the current fastest solution $fastest$ (i.e., $\mathbb{E}(T|w) < \mathbb{E}(T|fastest)$) then w becomes the new fastest solution (lines 2-3). If w is worse than $fastest$ the procedure is finished leading to a backtracking of the BFS (line 5). Remaining vertices to visit are sequentially processed at lines 7-13. For each unvisited vertex v , the shortest (in time) path P is determined from the last vertex in w to v and appended to w : $w = w \cup P$ (line 9). Moreover, the new cost of w according to Eq.(2) is computed and all vertices in P are labeled as visited (lines 10-11). The BranchAndBound is then called on the new walk at line 12. Note that backing up and restoring of the current state (walk, its cost, and the marking of visited vertices) at lines 8 and 13 allows for an efficient backtracking.

To achieve an effective branching and thus low computational times, several improvements to the original algorithm were made. Firstly, vertices in the *foreach* cycle at line 7 are processed in increasing distance to the last vertex in w , i.e. more promising shorter edges are processed first. Secondly, Johnson’s algorithm [21] is run in the preprocessing phase to find the shortest paths between all pairs of vertices, which are used at line 9. Finally, the estimated cost (i.e. the lower bound of all walks with a prefix w) $T^{exp}(w)$ at line 4 is determined as

$$T^{exp}(w) = \mathbb{E}(T|w) + \sum_{i=0}^K p_i D_i, \text{ where}$$

$$D_i = D(w) + \sum_{l=0}^i d_l,$$

where K is the number of unvisited vertices, $D(w)$ stands for the length of w , and d is an array containing the shortest edges incident to unvisited vertices sorted in ascending order. Similarly, p is a descendingly sorted array of weights (presence probabilities) of unvisited vertices.

The algorithm is exact and solves small-size instances in a reasonable time, i.e. the ‘Brayford’ problem with 11 vertices (see section VI) in less than 1 ms, a graph with 20 vertices in 6 sec and a graph with 25 vertices in 60 sec on a standard computer.

VI. METHOD EVALUATION

To evaluate the utility of temporal models to speed-up the robotic search, we have performed an extensive comparison of the proposed methods on two long-term datasets where the searched object is a human and one dataset with several objects of everyday use. Each dataset was divided into separate training and testing sets. The training sets were used to establish the temporal models of the nodes’ occupancy and edge traversals times. The testing sets were used to establish the time statistics of the search.

The first, ‘Aruba’ dataset [22] was collected by the Center for Advanced Studies in Adaptive Systems (CASAS) to support their research concerning smart environments. The

second ‘Brayford’ dataset [19] was created by the Lincoln Centre for Autonomous System (LCAS) as a part of the STRANDS project that is aimed at researching methods that enable long-term autonomous operation of intelligent robots in human-populated environments. The third ‘KTH’ dataset was created by the Royal Institute of Technology in Stockholm as a part of the STRANDS project.

A. Aruba dataset

The ‘Aruba’ dataset contains measurements collected by 50 different sensors spread over a 12×10 m, seven-room apartment for 16 weeks. The apartment is occupied by a single person who is occasionally visited by other people. To estimate the people presence in the individual rooms of the apartment, we processed the ON/OFF events from the dataset’s motion detectors. A room is considered to be occupied if any of its motion sensors report movement. In case no motion is detected by any of the sensors, the occupancy is unchanged, i.e. the last room reported to be occupied retains its state.

The apartment was partitioned into nine different areas, seven represent the rooms and two correspond to corridors - see Figures 1 and 3. Thus, we have obtained nine sequences that represent the occupancies of individual areas second-by-second for 16 weeks. The first 4 weeks of the data were used to train the temporal models of room occupancy and the remaining 12 weeks of the data were used as a testing set, i.e. for the evaluation itself. Thus, each areas’ occupancy model was trained and tested with more than 2.4 million and 7.2 million samples respectively. Note that the occupancy probabilities of the individual areas do not have to sum to one, because the apartment is sometimes completely empty and the inhabitant is occasionally visited by relatives. To

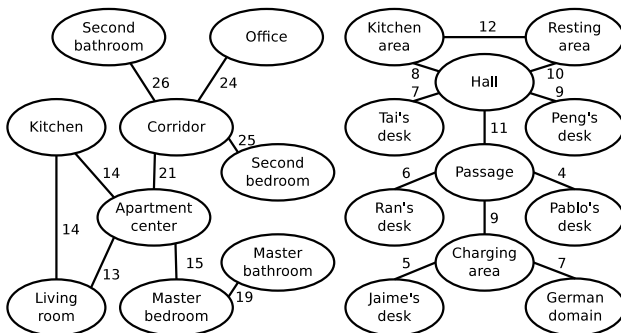


Fig. 3: Aruba and Brayford datasets - topological maps.

establish the times it takes to move between individual areas, a simulated environment based on the ‘Aruba’ apartment layout was created, see Figure 1. A virtual SCITOS-G5 mobile robot was placed in the apartment model and set up to autonomously navigate between the individual rooms. The robot’s trajectory was recorded, and the average times it took to traverse between the individual areas were calculated and used as an edge times of the topological map used by the planning algorithm. The average times (in seconds) are shown on the Aruba topological map, see Figure 3. Thus, the

resulting topological representation is based on both real-world (room occupancies) and simulated (time to navigate between rooms) data.

B. Brayford dataset

The Brayford dataset was collected by a SCITOS-G5 mobile robot (see Figure 4) equipped with an RGB-D camera mounted on a pan-tilt unit and a laser rangefinder. The robot has been set to patrol a large, open-space office of the Lincoln Centre for Autonomous Systems. Its autonomous navigation has been based on an improved ROS navigation stack and a visual-based method for precise docking with the charging station [23]. While the robot’s laser rangefinder was used primarily for autonomous navigation, the robot’s Asus Xtion RGB-D camera was primarily used for data gathering. The



Fig. 4: The SCITOS-G5 robot and example images of the Brayford dataset.

robot was set-up to capture RGB images of eight designated areas of the Witham Wharf office at Brayford street every ten minutes for two weeks of November 2013 and one week of February 2014. While the first week of November data were used as a training set, the testing set consisted of two days - one captured during November 2013 and one on February 2014. The training and testing datasets consisted of approximately 10000 images that were manually checked for people presence. Representative examples of the captured images are shown in Figure 4. To establish the times for the edges of the LCAS topological map, the trajectory recorded during the data gathering was analysed similarly to the Aruba dataset.

C. KTH dataset

One might argue that the Aruba and Brayford datasets are not related to object search since the robot searches for people. To verify the locations of objects of everyday use also exhibit periodicities, a specialized dataset was created at another site. The KTH dataset was collected by a SCITOS-G5 mobile robot (see Figure 4), in the Computer Vision and Active Perception lab at KTH Stockholm, over the course of five weeks. During this time the robot conducted between two and six autonomous patrol runs per day (weekends were excluded), visiting three specific waypoints during each run. Upon reaching a waypoint, the robot would execute a pan-tilt

sweep and collect data from the RGB-D sensor; the RGB-D frames collected during one sweep are registered spatially to form an observation of that particular waypoint at the particular time. The KTH dataset contains approximately 100 observations per waypoint, and at each waypoint we have extracted the dynamic elements of the environment by the ‘MetaRoom’ method presented in [24].

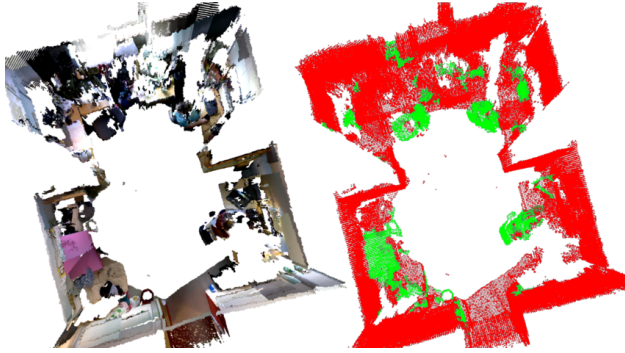


Fig. 5: Example observations with identified static (red) and dynamic (green) structures.

These dynamic elements correspond to movable objects such as jackets, backpacks, laptops, chairs, bottles, mugs, etc. For the experiments presented in this paper, we have manually labeled these dynamic clusters obtaining 37 different objects, out of which 14 tend to appear and disappear periodically. Using the first weeks of the KTH dataset, dynamic models of these objects’ presence were created. The remaining week was used as testing data.

VII. RESULTS

A. Aruba and Brayford datasets

To evaluate the influence of the temporal models on the time of the robotic search, we have first built seven temporal models of each of the two environments and used these as an input for the search algorithm described in Section V. Three temporal models were based on the FreMEn concept and they differed in the number (one to three) of spectral components included in the model. Another three ‘PerGaM’ temporal models consisted of the Periodic Gaussian Mixtures, where the daily occupancy was modeled by a combination of one-to-three Gaussians. Finally, a reference, ‘Static’ model represented the occupancy of each area by a constant probability. Each of these models has been used to predict the probabilities of area occupancies for every minute of the Aruba and every 10 minutes of the Brayford testing sets. Each of the topological maps generated was used as an input for the planning algorithm V that calculated an optimal (in the sense of criterion 1) robot path. Using the ground truth data of the testing sets, we determined the time it would take for the robot to find a person at a particular time using a given temporal model. The testing set of the Aruba environment allowed us to perform over $\sim 850\,000$ searching runs (7 evaluations every minute for 12 weeks) and the Brayford results are based on ~ 2000 testing runs (7 evaluations

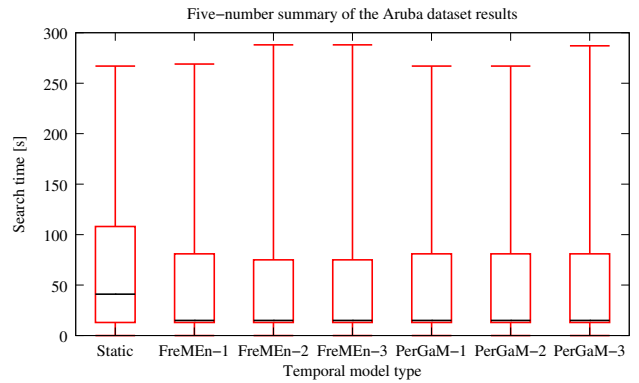


Fig. 6: Five-point summary of search times for different temporal models - Aruba dataset.

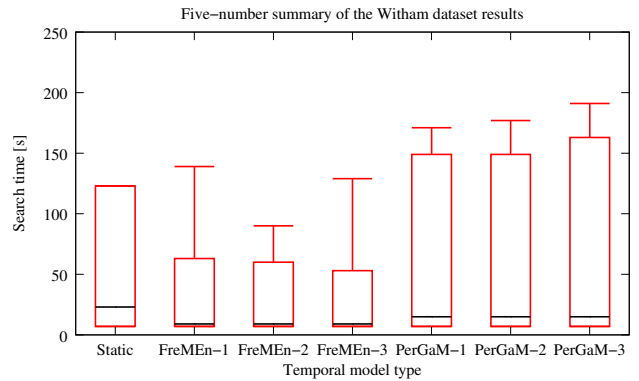


Fig. 7: Five-point summary of search times for different temporal models - Brayford dataset.

every 10 minutes for two days). To indicate the impact of using the temporal models for the robot search, we provide five-point characteristics extracted from the aforementioned testing runs. Figures 6 and 7 show that in general, usage of the temporal models allows to construct plans that are more likely to find a person in a given environment faster than in cases when the temporal information is neglected (the ‘Static’ models). Compared to the stationary models, the median time of the dynamic models’ testing runs is lower by 35-65%. However, the Figure 6 also indicates that in some cases - about 6%, the plan that takes into account the temporal models might perform worse than the one using a static model. This is typically caused by short-term absences at the expected locations and cases when the environment is completely vacant.

To further evaluate the results, we have calculated the mean times it takes to find the person when the environment is not empty. The mean time of finding a person along with the median time to complete the search is shown in Table I.

B. KTH dataset

The KTH dataset does not offer the same evaluation as the Aruba and Brayford ones, because the objects (sometimes) appear at a particular waypoint only. Instead of having the

TABLE I: Mean (μ) and median (\tilde{t}) time of finding a person

Model		Dataset			
		Aruba		Brayford	
type	order	$\mu[s]$	$\tilde{t}[s]$	$\mu[s]$	$\tilde{t}[s]$
Static	-	44	41	19	23
FreMEn	1	36	15	14	9
FreMEn	2	33	15	14	9
FreMEn	3	34	15	16	9
PerGaM	1	34	15	14	15
PerGaM	2	33	15	14	15
PerGaM	3	33	15	14	15

robot to plan a sequence of rooms to move through, we want it to find a set of the objects at that location and let it decide when to visit the location. The robot calculates the joint probability of the objects' presence for the time of intended patrol and decides to visit the place only when the probability is at least 0.5. This test has shown that the number of visits decreased by 33% compared to visiting the place on a regular basis.

VIII. CONCLUSION

We have presented a novel approach to the robotic search problem based on spatio-temporal environment modeling and efficient probabilistic path planning. We assume that the topology of the robot operational environment is known and that the searched object locations are influenced by human activities which tend to exhibit a certain degree of periodicity. This assumption allows to model the likelihood of object occurrences at particular locations by combination of periodic functions which are identified from the long-term observations of object occurrences. These function constitute dynamic probability distribution of the searched objects' locations which allows to create different search plans for different times of day. In other words, our approach allows to integrate several observations of the same environment in a spatio-temporal model that captures the periodic aspects of object occurrences and uses this knowledge to construct time-dependent plans for the object search.

The experimental evaluation performed on datasets gathered over several weeks show that explicit representation of the long-term periodicities of environment dynamics speeds up the search process. Compared to traditional probabilistic models that neglect long-term environment dynamics, using the proposed spatio-temporal models for path planning resulted in a 25% - 65% reduction of time needed to locate the searched object. The tests have shown that the Spectral-based dynamic modeling methods speed up the search slightly more than the Gaussian-based ones, though the difference was not statistically significant in our experiments.

ACKNOWLEDGMENTS

The work has been supported by the EU ICT project 600623 'STRANDS' and by the Technology Agency of the

Czech Republic under the project no. TE01020197 'Centre for Applied Cybernetics'

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