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# Soft Morphological Filter Optimization Using a Genetic Algorithm for Noise Elimination

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**Abstract**—Digital image quality is of importance in almost all image processing applications. Many different approaches have been proposed for restoring the image quality depending on the nature of the degradation. One of the most common problems that cause such degradation is impulse noise. In general, well known median filters are preferred for eliminating different types of noise. Soft morphological filters are recently introduced and have been in use for many purposes. In this study, we present a Genetic Algorithm (GA) which combines different objectives as a weighted sum under a single evaluation function and generates a soft morphological filter to deal with impulse noise, after a training process with small images. The automatically generated filter performs better than the median filter and achieves comparable results to the best known filters from the literature over a set of benchmark instances that are larger than the training instances. Moreover, although the training process involves only impulse noise added images, the same evolved filter performs better than the median filter for eliminating Gaussian noise as well.

**Keywords**—Filter Design, Supervised Learning, Genetic Algorithm, Image Processing.

## I. INTRODUCTION

Noise reduction is an essential concern in image processing. There are many sources of noise in digital images. For example, transmitting or scanning an image can boost up the noise due to electrical interference from the devices used. There are different types of noises dealt with in image processing such as Gaussian noise, periodic noise or impulsive noise. Many studies have proposed a variety of approaches for the removal of such types of noise. Impulsive noise is often encountered during the image transmission process [21], malfunctioning in camera sensors or faulty memory locations in hardware [3]. There are two common types of impulse noise; salt and pepper and random-valued noise. In this study, impulsive noise elimination problem that requires restoration of the image quality which is reduced by white and black (salt and pepper) spots spread over the images is tackled. There are some previous studies on this topic using different search methods. In most of the previous studies, search methodologies are used as training approaches to optimize filters, then the candidate filters are applied on corrupted images. During the search process the original non-corrupted images are compared to the images produced after filtering. By minimizing the difference between filtered and original images, it is expected that an optimized filter will be obtained.

Initially, well known search methodologies, such as, standard GAs [9] and adaptive immune algorithms [26] were used in the design of standard morphological filters [9] for noise filtering. After soft morphological filters were discovered, soft flat morphological filters were optimized for the same purpose. Approaches, such as simulated annealing and tabu search [7], [6] were employed to this end. Direct mathematical approaches such as median filtering [15] and non-linear filters [22] were also favoured by researchers. Indeed, median filtering is regarded as the standard approach to deal with impulsive noise. More sophisticated methods such as Neural Networks combined with fuzzy logic [8], noise removal using B-Splines [10] and use of directional filters [31] were also proposed to tackle the same problem. In this study, a Genetic Algorithm (GA) for optimizing a multi-stage non-flat soft morphological filter is presented. The aim is to eliminate salt and pepper noise on images while preserving the quality as much as possible. Different objectives are combined in a fitness function and an appropriate representation scheme is designed to cover a broad range of filter parameters.

The paper is organized as follows: In the next section (Section II), background information about soft mathematical morphology is given. In Section III, the representation scheme and other relevant components of GA, designed for automatically creating a noise elimination filter is explained in detail. In Section IV-A, the experimental settings used to obtain the best filter are explained and performance comparison of the generated filter and median filter is provided over 10 different benchmark images in Section IV. Also, the filters generated for different levels of noise are compared with the latest filters presented in the literature and the improvement of the GA and the fitness function is shown visually and mathematically. Finally, conclusions are provided in Section V.

## II. SOFT MATHEMATICAL MORPHOLOGY

Mathematical morphology was first introduced as an image processing methodology for binary images [16]. The basic operators used in mathematical morphology are *erosion* and *dilation* operators that accept the image itself and a *structuring element* (SE), also referred to as *kernel*, as input. For more details on mathematical morphology, readers can refer to [24] and [25]. Dilation causes regions of foreground pixels grow in size and holes within those areas shrink, while erosion has a reverse effect.

Later, in gray-scale morphology erosion and dilation operators are replaced with *minimum* and *maximum* operators as the fundamental morphological operators, respectively. There are also *opening* and *closing* operators which requires application of dilation and erosion using the same structuring element in a specified order. Up to now, mathematical morphology has been used in many different image processing applications, ranging from noise suppression, feature extraction to object recognition. Soft mathematical morphology was introduced by Koskinen, Astola, and Neuvo [12] in 1991. In this approach, weighted order statistics is used instead of the minimum or maximum. The main difference from the standard morphology is the division of the structuring element into two parts; *hard centre* and *soft boundary*. The numbers in the hard centre part have weights greater than one, which is set by a parameter called *rank* or *repetition parameter*. The numbers in the soft boundary part of the SE have weights equal to one.

Given a structural element  $B$ , it is divided into two subsets: the hard centre structural element  $A$  and the soft structural element  $B \setminus A$ , where  $A, B \subseteq Z^2, B \setminus A \neq \emptyset$ , and  $\setminus$  denotes the set difference. Let  $\oplus$  and  $\ominus$  represent *soft dilation* and *soft erosion* operations. Soft dilation and soft erosion of an image  $f$  with rank-order  $i$  are defined as:

$$\oplus_{B,A,i}(f) = \max^i \{ i \diamond (f(Z - \epsilon) + A(\epsilon)) \mid \epsilon \in F_A \} \cup \{ f(Z - \delta) + B(\delta) \mid \delta \in F_{B \setminus A} \} \quad (1)$$

$$\ominus_{B,A,i}(f) = \min^i \{ i \diamond (f(Z + \epsilon) - A(\epsilon)) \mid \epsilon \in F_A \} \cup \{ f(Z + \delta) - B(\delta) \mid \delta \in F_{B \setminus A} \} \quad (2)$$

where  $\max^i$  and  $\min^i$  denote the  $i$ th largest and smallest value in the set respectively;  $\diamond$  is the repetition operator and  $i \diamond f(v) = \{f(v), f(v), \dots, f(v)\}$  ( $i$  times);  $F_A$  and  $F_{B \setminus A}$  represent the field of definition of  $A$  and  $B \setminus A$ , respectively. Consequently, soft opening ( $\Lambda$ ) and soft closing ( $\Delta$ ) of an image  $f$  are defined as:

$$\Lambda_{B,A,i}(f) = \oplus_{B,A,i}(\ominus_{B,A,i}(f)) \quad (3)$$

$$\Delta_{B,A,i}(f) = \ominus_{B,A,i}(\oplus_{B,A,i}(f)) \quad (4)$$

It has been shown that soft morphological operations are more robust in noisy conditions and are less sensitive to additive noise and to small variations in object shape [13].

### III. GENETIC ALGORITHMS FOR GENERATING SOFT MORPHOLOGICAL FILTER

Genetic Algorithm (GA) is a well known population-based metaheuristic approach used for solving difficult optimization problems [18], [19], [20]. The need to search and try different combinations of operations, structuring elements and parameters expands the search space dramatically and makes the search for the best soft morphological filter well suited for GAs. In this study, GAs are used as a supervised learning mechanism to generate a filter for impulsive noise removal, automatically. Our approach uses GA to optimize the parameters of the soft morphological filter using a set of noisy small training images, then the best found filter is applied to a

set of large test instances corrupted by noise for performance evaluation.

#### A. Representation

Each candidate solution encoded by a chromosome represents a different filter. In this representation scheme, a soft morphological filter that has up to four stages can be encoded. Each of these four stages can have different morphological operations, parameters and structuring elements. It is shown in a previous study [11] that having multiple stages gives better results compared to a one-staged morphological filter. In the first four genes of the chromosome, the type of the morphological operations for each stage are coded ( 0-No Operator, 1-Erosion, 2-Dilation, 3-Opening, 4-Closing ). By using a *No Operator* type, the corresponding stage can be eliminated, or by using one of the other operations, the operator can be selected for the corresponding stage.

In the next four genes, the neighbourhood type is encoded. In this study, 4 and 8 neighbourhood types are allowed. In a 4 neighbourhood type, the corners of the SE are not used, but in an 8 neighbourhood type, all the nine elements in the SE are used. First of all, these are the most common ones and some prior tests done showed that, enlarging the search space by allowing all types of SE shapes does not give better results. For this part of the chromosome, zero means a 4-connected type neighbourhood; one means an 8-connected type neighbourhood.

The next four genes are also binary like the previous four genes. They encode the information whether the SE is symmetric or not. In a symmetric SE, the numbers are symmetrically placed in all planes (horizontally, vertically and diagonally). However, in a non-symmetric SE, all the numbers can be different. The next 36 genes represent the numbers in the structuring elements of the four stages. 3x3 sized SEs are used in this study; which means each Structuring Element has nine numbers in them. Each slot in an SE has a range of [-255, 255]. In a previous work [11], this range is used and it is shown that [9], [11] expanding the range of the number in the SEs gives better results. A gray scale image has a range of [0, 255]; in order to change a black pixel (255) into a white pixel -255 have to be added, and a value of 255 have to be added for the opposite. Therefore, to cover all the values of a gray scale image, this range is used.

The last two parts are the parameters only used in soft morphology. The next 36 genes represent the *hard* and *soft* elements in the SEs. This part of the chromosome is also binary. Each gene works for a single number in an SE. When encoding, a zero maps to a soft element, and a one maps to a hard element. The last four genes in a chromosome represent the *repetition parameter of the rank parameter* for each stage. An allele for each gene in this part is in  $\{1, \dots, 9\}$ . An allele value of 1 in this field indicates a standard morphological filter, while another value changes the operation according to the rules defined in soft mathematical morphology. The values above eight give the same results, as the SEs used in this study have nine numbers in them.

#### B. Evaluation Function

The GA in this study is used as a training method; a filter trainer for a specific purpose which is noise elimination. The

fitness calculation (evaluation) gives us a value that represents the difference between the filtered noisy image and the original non-noisy image. Therefore, the lower the difference, the better the filter will be. There are different measures in the literature. In this study, we combine four measures (functions/criteria). Mean Absolute Error (MAE) (Eq.5) and Mean Squared Error (MSE) (Eq.6), are two commonly used criteria in the literature. MSE strengthens the influence of differences on the result, however none of those functions has precedence over the other. Shape Error (Eq.7) is a relatively new measure as compared to MAE and MSE. In contrast to the other functions, this criteria takes the whole image into account, which is useful for reconstruction [14].

Those three measures presented so far, are good in smoothing the noise and preserving the shape details. Nonetheless, the non-flat structuring elements used in our method tend to change the average pixel value of the image, leading to a different brightness in the resulting image when compared to the original image. In order to overcome this difficulty, the brightness error measure (Eq.8), a method mostly ignored in the literature, is additionally used to bias the search to a direction where the brightness of the resulting image will be close to the original image's brightness value.

$$f_1 = \frac{1}{M \times N} \sum_{i=1}^M \sum_{j=1}^N |X(i, j) - Y(i, j)| \quad (5)$$

$$f_2 = \frac{1}{M \times N} \sum_{i=1}^M \sum_{j=1}^N (X(i, j) - Y(i, j))^2 \quad (6)$$

$$f_3 = \frac{1}{M \times N} \sum_{i=1}^M \sum_{j=1}^N \sum_{(i', j') \in w} (X(i, j) - x(i', j') - (Y(i, j) - Y(i', j')))^2 |^y \quad (7)$$

$$f_4 = \left( \frac{1}{M \times N} \sum_{i=1}^M \sum_{j=1}^N X(i, j) \right) - \left( \frac{1}{M \times N} \sum_{i=1}^M \sum_{j=1}^N Y(i, j) \right) \quad (8)$$

In the equations above,  $X$  and  $Y$  are the noisy and restored gray scale images respectively, each of size  $M \times N$  pixels. Also, in Eq.7,  $y = 2$  and  $(i', j')$  specifies the floating windows around  $(i, j)$  with the masking element  $w$ , which is a  $3 \times 3$  window in this case. The objective functions discussed above are all scaled and combined to form a single fitness function. Scaling the contribution of each function is necessary to equalize the contribution of the objective components on the fitness value. To scale these components, each objective is divided by the maximum possible value they can give in an extreme case. Subsequently, the scaled fitness function emerges which is given in Eq.9.

$$f'(X, Y) = \sum_{i=1}^4 s_i f_i \quad (9)$$

Using a single image results in a filter that is best suitable for an image with similar attributes like the training image. So, it is seen that to achieve a generalized filter, more than one image is needed for the training phase. In this study, three different  $100 \times 100$  sized images are used for the fitness calculation. The fitness of each candidate filter is calculated with the same way described before, and the average value of these calculations made up the final fitness value as shown in Eq.10. Using multiple images for the fitness calculation also helps in reducing the difference in the brightness between the original and restored image.

$$f = \frac{\sum_{i=1}^3 f'(X_i, Y_i)}{3} \quad (10)$$

## IV. EXPERIMENTAL RESULTS

### A. Experimental Design

An arbitrarily chosen small square subregion of three images are used during the training to generate high quality filters via GA to reduce the training time. The training images are cropped from the Lena, Flower and Mandrill images as original (basis) images (Figure 1) and exposed to random noise at a given level before each training process.

An initial population with a size of 50 individuals is randomly generated according to the value ranges of each gene. Uniform crossover is used for recombination after choosing 2 parents using tournament selection with a tour size of 4. The traditional mutation operator randomly perturbs an allele with a probability of  $1/\text{individual-length}$ . The best individual is maintained while the rest of the population is replaced by the new individuals. A run is terminated after 1000 generations. To obtain the best filter, GA is run with the same parameters and with the same training images for 30 trials. At each trial, a different set of training images is used. Each training image used at a trial is obtained by exposing the basis image to random noise generated using a different random seed at the given level of noise. After termination, the best filter generated having the best fitness from all 30 trials is tested over ten "unseen" images (Fig 2). During the testing phase, each test image is corrupted with various levels of noise ranging from 10% to 90% for each trial in a similar manner as the training images.

We performed 3 different sets of experiments. In the first set of experiments, level of salt and pepper noise is fixed and the performance of different median filters are compared along with the generated filter. In the second set of experiments, the best filter achieved for various noise levels is tested on test images and the results are compared to those of well-known filters from the literature. Finally, an entirely different type of noise, namely Gaussian noise, is handled with the filter which was trained to eliminate impulse noise. The goal is to evaluate the generality level of the filter evolved by GA.

### B. Comparison of Filters at a Fixed Noise Level

In the first set of our experiments, level of noise is fixed as 20% and the performance of the generated filter and the median filters of sizes  $3 \times 3$ ,  $4 \times 4$  and  $5 \times 5$  are compared. Table I summarizes the results which shows that, according to MSE

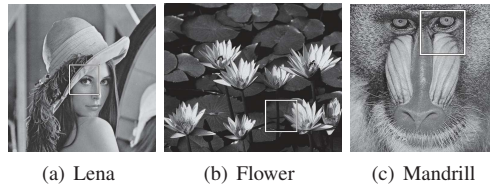


Fig. 1. Cropped part of each image that is taken to form the training set.

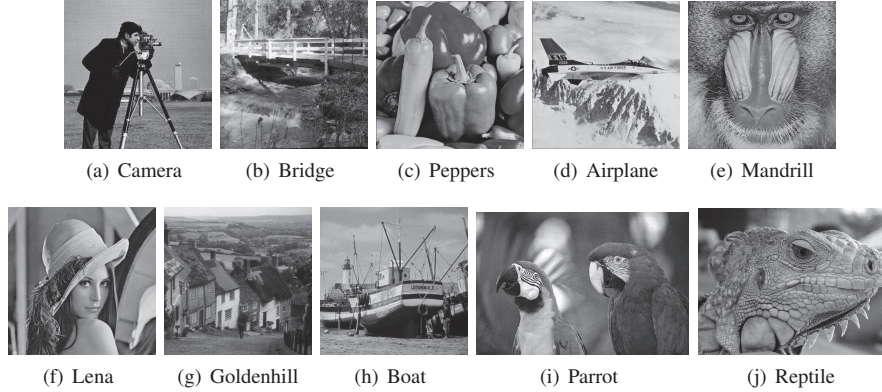


Fig. 2. Test images.

and shape error criteria, the generated filter gave better results across all images. According to MAE criteria, generated filter is always better than almost all median filters, except for the Reptile image, for which the  $3 \times 3$  median filter gave a better result. According to brightness error criterion, performance of the generated filter is the worse. The  $3 \times 3$  median filter performs well with respect to this criterion as compared to the other median filters of size  $4 \times 4$  and  $5 \times 5$ . In most of the cases, the generated filter is better than the large size median filters but slightly worse than the  $3 \times 3$  median filter. In the overall, the generated filter delivers a better performance than the median filters of different sizes and the best performing median filter is of size  $3 \times 3$ .

### C. Comparison to Previously Proposed Approaches

The second set of experiments is organized with the goal of comparing the performance of our approach to the previously proposed ones. In the literature, performance of most of the approaches are reported with respect to the MSE values on 3 images: Lena, Mandrill and Peppers. The performance of generated filters are evaluated on the corrupted versions of those images with 9 different levels of noise:  $\{10\%, 20\%, \dots, 80\%, 90\%\}$ . The same noise levels are used during the training process. The performance of each filter produced for a given noise level during the training is also tested across images corrupted with other noise levels. In general, the noise level is not known prior to reconstruction of an image. On average, it has been observed that the filter obtained by using training instances with 60% noise yields a better performance (Fig 3). Please note that, the results for all noise levels are not shown due to lack of space. However, Table III summarizes the results for the filter trained on images with 60% noise (the best performing evolved filter) are presented and compared to other well established methods from the literature: Anfis-based Impulsive

noise removing Filter (AIF) [2], Spatial Median Filter(SMF) [27], Iterative Median Filter (IMF) [29], Progressive Switching Median Filter (PSM) [29], Signal Dependent Rank Order Mean Filter (SDROM) [1], Two-state Recursive Signal Dependent Rank Order Mean Filter (SDROMR) [1], Impulse Rejecting Filter (IRF) [4], Non-Recursive Adaptive-Center Weighted Median Filter (ACWM) [5] Recursive Adaptive-Center Weighted Median Filter (ACWMR) [5], Center Weighted Median Filter (CWM) [17], Yüksel's Anfis based filter (YÜKSEL) [30], Russo's fuzzy filter (RUSSO) [23] and Histogram Based adaptive fuzzy filter (HAF) [28].

Each approach is ranked from 1 (best) to 14 (worst) based on the MSE values for each resultant image, then the average ranking of each approach is provided. As expected, in most of the cases, a filter obtained after training on instances from a given noise level is more successful in eliminating noise from an image corrupted at the same noise level. Our filter does not give the best results among all the filters, but if we look at the results of each for their generated noise level, it can be observed that our method gets a rank in the top 3 or 4 filters among the state-of-the-art filters from the literature.

### D. Eliminating Gaussian Noise

Although our filter is trained using impulsive noise added images (60%), in this part, it is tested on images exposed to a different type of noise, that is Gaussian noise. Considering salt and pepper noise, pixels in the image are very different in color or intensity from their surrounding pixels. The defining characteristic is that the value of a noisy pixel bears no relation to the color of surrounding pixels. Generally, this type of noise will only affect a small number of image pixels. Whereas considering Gaussian noise, each pixel in the image will be changed from its original value by a (usually) small amount.

TABLE I. PERFORMANCE COMPARISON OF OUR FILTER (OBTAINED AFTER TRAINING USING THE SMALL IMAGES WITH 20% SALT AND PEPPER NOISE) AND MEDIAN FILTERS WITH RESPECT TO DIFFERENT METRICS BASED ON MEAN VALUES (AVERAGED OVER 30 RUNS). MAE: MEAN ABSOLUTE ERROR, MSE: MEAN SQUARED ERROR, SE: SHAPE ERROR, BE: BRIGHTNESS ERROR

Error Type	Method	Camera	Bridge	Peppers	Airplane	Mandrill	Lena	Goldenhill	Boat	Parrot	Reptile
MAE	GA(20%)	5.27	8.55	2.53	2.90	10.72	2.52	3.95	3.67	3.05	4.68
	3 × 3	5.94	9.76	2.80	3.21	11.74	2.79	4.58	4.22	3.36	4.01
	4 × 4	8.19	12.48	4.41	5.20	14.43	4.53	6.15	6.17	4.69	5.99
	5 × 5	7.77	12.47	3.55	4.52	14.69	3.81	5.99	5.76	4.29	5.44
MSE	GA(20%)	169.86	184.34	31.21	47.02	300.25	31.91	49.56	58.84	77.08	79.06
	3 × 3	276.02	289.72	78.96	110.46	392.60	79.87	111.79	123.17	125.00	119.74
	4 × 4	414.40	374.73	131.34	191.47	491.62	120.77	122.13	176.19	150.92	160.71
	5 × 5	373.53	373.07	67.40	128.10	502.10	79.73	121.17	151.44	141.83	131.49
SE	GA(20%)	46.61	49.64	18.21	21.77	64.66	18.34	25.04	26.18	31.40	28.14
	3 × 3	59.91	62.90	31.03	35.58	75.18	30.59	37.89	38.74	40.50	38.60
	4 × 4	64.48	64.32	30.40	36.24	77.68	29.15	34.36	38.81	39.89	37.24
	5 × 5	62.85	64.06	24.68	32.54	79.06	25.94	34.97	37.84	40.10	35.19
BE	GA(20%)	0.16	0.23	0.16	0.23	0.32	0.03	0.06	0.20	0.13	1.16
	3 × 3	0.58	0.39	0.11	0.20	0.43	0.17	0.21	0.12	0.09	0.09
	4 × 4	1.28	0.78	0.12	0.21	0.64	0.31	0.41	0.17	0.29	0.21
	5 × 5	1.20	0.90	0.25	0.14	0.72	0.40	0.51	0.04	0.26	0.49

TABLE II. AVERAGE RANK OF EACH FILTER OVER ALL NOISY IMAGES

Method	Lena	Mandrill	Peppers	Method	Lena	Mandrill	Peppers
Our Method (10%)	15,44	15,00	14,11	SMF(3 × 3)	17,56	17,11	16,44
Our Method (20%)	12,56	12,33	11,11	PSM	12,22	10,89	10,89
Our Method (30%)	10,78	11,33	9,44	SDROM	18,78	17,33	19,11
Our Method (40%)	8,33	9,67	7,67	SDROMR	11,56	11,33	12,33
Our Method (50%)	9,44	9,89	8,78	IRF	17,11	16,11	17,11
Our Method (60%)	7,56	8,67	6,67	ACWM	17,22	15,22	17,56
Our Method (70%)	10,67	10,56	9,56	ACWMR	9,78	7,89	10,11
Our Method (80%)	9,11	9,33	10,22	CWM	20,89	19,89	20,78
Our Method (90%)	11,44	10,67	13,22	YÜKSEL	7,56	7,56	13,00
AIF	1,00	1,00	1,00	RUSSO	11,56	18,44	12,22
IMF	10,44	10,78	9,67	HAF	2,00	2,00	2,00

TABLE III. AVERAGE RANK OF DIFFERENT FILTERS, WHICH ARE OBTAINED USING DIFFERENT APPROACHES, BASED ON THEIR PERFORMANCES WITH RESPECT TO MSE OVER DIFFERENT LEVELS OF NOISE. EACH FILTER IS USED TO ELIMINATE SALT AND PEPPER NOISE FROM THE LENA, MANDRILL AND PEPPERS IMAGES, EACH CORRUPTED WITH NINE DIFFERENT LEVELS OF NOISE FROM 10%-90% AND RANKED ACCORDINGLY.

Method	Lena	Mandrill	Peppers	Method	Lena	Mandrill	Peppers
GA(60%)	5.33	6.00	4.56	IRF[4]	10.44	9.78	10.33
AIF[2]	1.00	1.00	1.00	ACWM[5]	10.67	9.11	10.89
IMF[29]	6.78	6.89	5.67	ACWMR[5]	5.67	5.11	5.67
SMF - 3x3 [27]	10.44	10.11	9.67	CWM[17]	13.67	13.11	13.56
PSM[29]	7.56	6.89	6.33	YÜKSEL[30]	5.00	4.56	8.22
SDROM[1]	12.11	11.00	12.33	RUSSO[23]	7.11	12.11	7.33
SDROMR[1]	7.22	7.33	7.44	HAF[28]	2.00	2.00	2.00

Gaussian noise is applied on all images. The variance of the Gaussian noise is varied from 10% to 90%. Subsequently, the 3 by 3 median filter and the selected filter which is trained at 60% noise level is applied to all those images and the results are recorded according to mean-squared-error criteria. The test results show that, our method also can eliminate Gaussian noise and achieves significantly better results than the median filter for all images and noise levels (Table IV).

## V. CONCLUSION

In this study, an evolutionary approach is used to generate a noise filter which is based on soft mathematical morphology. Elimination of noise while preserving details as much as possible is achieved by using a representation which allows multi-stage filters with a wide range of structuring elements and by combining four different objectives in the fitness function. We generated a filter which is enabled to handle different levels of noise and compared its performance to the best known filters from the literature. Our filter turned out to

be one of the top filters with respect to the MSE criterion. Although that filter was specifically tailored for impulsive noise, tests over Gaussian noise added images showed that it is also successful in eliminating this type of noise regardless of its level. The evolved filter outperformed the Median filter almost for all images and noise levels tested. This work shows that using evolution to generate “reusable” filters to eliminate noise is a viable approach. Moreover, the evolutionary process is capable of learning from small instances how to eliminate noise which then can be applied to large unseen instances.

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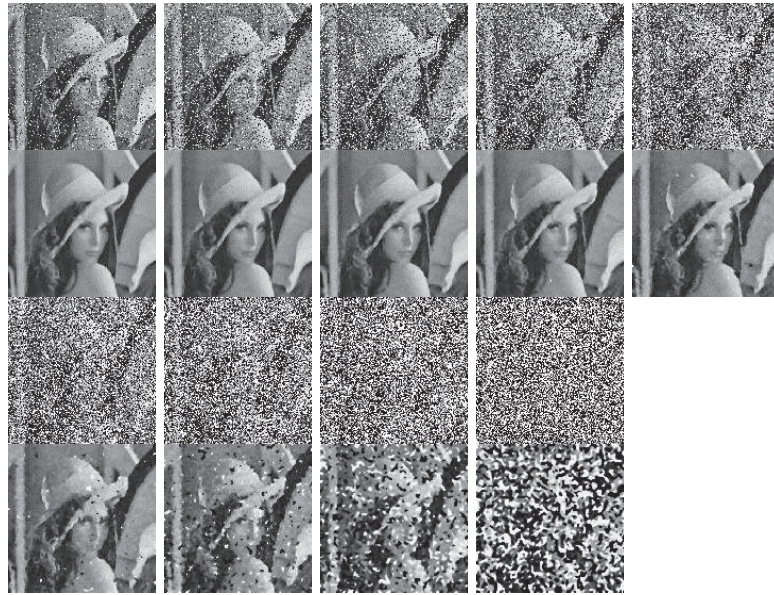


Fig. 3. Pairs of Lena images, corrupted with noise levels from 10% – 90% (up) and reconstructed using an evolved filter trained at a 60% noise level (down).

TABLE IV. COMPARISON OF THE AVERAGE VALUES OF MEDIAN FILTER ( $3 \times 3$ ) AND SELECTED FILTER RESULTS FOR EACH IMAGE (MSE CRITERIA) GIVEN A GAUSSIAN NOISE

Image	Our Method	Median Filter	Image	Our Method	Median Filter
Camera	1345.01	3895.39	Lena	1104.35	3783.05
Bridge	1409.56	3921.38	Goldhill	1110.90	3771.69
Peppers	1104.59	3690.05	Boat	1168.55	3786.48
Airplane	1070.35	3472.62	Parrots	1159.43	3817.20
Mandrill	1527.03	4208.30	Reptile	1297.67	4020.27

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