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NOTE

DEPTH TO MATE AND THE 50-MOVE RULE

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1. INTRODUCTION

The first author's DTM₅₀ 'EGT' endgame tables (Huntington, 2013; Haworth, 2014a/b) provide 'DTM' Depth to Mate information as moderated by the FIDE (2014) '50mr' 50-move rule and the ply-count *pc*. This note puts that achievement in the context of earlier DTM computations (Nalimov et al., 2000/2001; Wu and Beal, 2001a/b; Bleicher, 2015) and data from previous studies of 50mr-impact (Tamplin and Haworth, 2004; Bourzutschky et al., 2005; Tamplin, 2015). It compares some DTM₅₀ statistics with the intrinsic, unmoderated DTM and DTZ₅₀ data.³ Datasets supporting these results are available (Huntington and Haworth, 2015) and include a pgn file, its annotation, and the fuller statistics which cannot be accommodated here.

When considering 50mr impact, the ply-count *pc* or rather the ply-remaining count pr = 100-*pc* must be borne in mind. A position's $dtm_{50,pc}$ may increase as *pc* increases until the win becomes a 'frustrated win', a '50mr-draw'. Even a mate in two ply will be frustrated if 99 ply have been expended, e.g., in KNNKP. These 'EM₅₀' DTM₅₀ EGTs are the first to provide depths for any value of *pc*. Clearly, maxDTM_{50,pc} $\ge \max DTM_{50,pc=0}$.

The FIDE 50-move rule is not an intrinsic rule of the game but a 'rule of play' introduced by Ruy López (1561) for the convenience of professional coffee house players. The results here show that it has major impact on KBBKN and KNNKP, and therefore on the upstream KBBKNN, KNNKNP and KNNKPP. For s6m, s7m and s8m chess, maxDTZ is greater than 80, 240 and 510 moves respectively (Haworth, 2014b). The 50mr, now backed by the 75-move-rule, will apparently frustrate ever more subtle wins as the number of men increases.

The perspective here is that these extreme cases of extended wins, rather than being denied by rules of play, should become part of the culture, experience, record and history of chess, at least when an EGT-armed computer-engine demonstrates infallible play.

2. COMPUTING DTM: ALGORITHM, LANGUAGE AND PROGRAM

When generating any EGT, the fundamental principles are that (a) successor endgames' EGTs are computed first, and (b) a position can be given a depth:

- temporarily when one of its immediate successors has been given a depth, but
- definitively only after enough of its successors have been given their definitive depth.

Any computation begins by identifying 'mated' (in 0 ply) positions. Positions which can be assigned a depth may be found by repeated, linear sweeps of the whole endgame and the first sweeps efficiently net many positions. Shortly though, the more selective and efficient method is to 'unmove' from the 'frontier' of positions which have just been given a depth in the last cycle of the algorithm.

The best known DTM computations are those of Nalimov (2000/2001) which created EGTs for the whole of sub-7-man (s7m) chess (Bleicher, 2015). Nalimov employed linear sweeps rather than the more retrograde 'unmove' algorithm, giving a position a depth at the earliest opportunity but lowering it later as required. As evid enced by the results here, this occurred many times in generating the KNNKP EGT. In contrast, Wu (2001a/b) worked exclusively in unmove mode. His key idea was to defer identifying 'mates in m+1' until all 'mates in m' had been identified. As each dtm is associated with one cycle of the algorithm, it only required two bits per position rather than one- or two-bytes, economising on memory by a factor of four or eight.

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 $^{^{3}}$ DTZ = minimaxed depth to the zeroing of the ply-count, i.e., to a pawn-push, capture and/or mate which end the current phase of play.

Huntington reverts to the principle of assigning depths as soon as possible. Each algorithm cycle corresponds to a specific number, pr, of ply remaining: pr effectively increases from 0 to 100 during the computation. Lower values of DTM₅₀ become possible when more ply are available. Table 3 shows that the highest variability of DTM₅₀ seen so far occurs in KNNKP with 25 different mate-depths. By noting on what cycle a DTM₅₀ value is set, the various ply-ranges corresponding to a specific dtm_{50} can be identified for each chess position.

EGT generation, as a computation task, is challenging because the results are not self-evidently correct: the subtlety and toxicity of errors is well known (Hurd and Haworth, 2010). Where clarity of coding and correctness are particularly at risk, as has been argued in classic texts elsewhere (Hughes, 1990; Bird, 2014), 'FPL' functional programming languages, without side effects, may be preferred to imperative languages. The declarative style of FPLs, using higher levels of abstraction, creates programs which are more readable and understandable. Research in FPLs created an embarrassment of riches and ideas, and the best of these were brought together in the language HASKELL, 'standardised' in HASKELL 98 (Peyton-Jones, 2002) and then in HASKELL 2010 (Marlow, 2010). HASKELL is most liked for its elegance as a language, for its type system, and for the confidence it creates that compiled code is likely to be correct code (MacIver, 2015) and was the choice of the first author here.

FPLs once had a reputation for inefficiency but modern compilers have largely offset this and performance is competitive today. For example, FPLs allow new methods of whole-program optimisation made possible by the promise of purity. Also, code can be written much more compactly due to the expressive power of treating functions as ordinary values that can be built at runtime. Certainly, there are new kinds of pitfalls which programmers must contend with: the challenge of balancing use of space and time remains. Small changes can have a large effect on performance by, e.g., causing an optimization to become inapplicable. Worse, unexpected memory leaks are common, and measures must be taken to prevent overzealous time optimisation that causes excess space usage. Such snags plagued earlier versions of the DTM₅₀ EGT generator, and in general avoiding them is an active area of compiler research. The EGT itself consists internally of an array where each cell value stored the possible mate lengths for various ranges of PC, and an 'overflow' hash table to store values that do not fit in an array cell. The cell's size has to be fixed in advance and chosen with care. Too small, and the overflow structure becomes heavily used, which is much less space/time efficient than an array; too large, and much memory is wasted on unused array space.

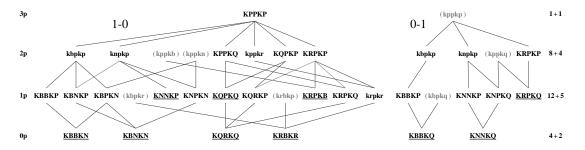


Figure 1.5-man endgame wins, 1-0 and 0-1, at first apparently DTZ-susceptible to the 50-move rule.

3. THE RESULTS

DTM endgame tables presume a ply-count of pc = 0 and therefore the DTM_{50,pc} results with pc = 0 provide a natural first focus. The later consideration of a free-ranging pc places emphasis on the cost of pc > 0 and the variability of $dtm_{50,pc}$.

3.1 DTM_{50,pc} with zero ply-count pc

For sub-5-man chess, no endgames are affected as maxDTM < 100 ply. Figure 1 shows those 5-man endgames, ranked by number of pawns, which appear at first to be susceptible to the 50mr, 1-0 and/or 0-1 wins⁴ perhaps being converted to 50mr-draws or lengthened in some sense. Tamplin and Haworth (2004) identified the actual 50mr impact in DTZ terms and this is annotated under four headings in Figure 1 and Table 1.

⁴ In fact, the 50mr only affects both 1-0 and 0-1 wins in the endgames KBBKP, KNNKP, KRPKQ and KRPKP of Figure 1.

	-			maxDTM, ply				EZ						maxDTM ₅₀ , ply								
#	#P	Endgame	Res.					=	% wins % wins		wins	pc = 0					any pc					
					wtm		btm		frustrated		$dtz_{50} > dtz$		wtı			btr		n wtr				
				#	dtm	#	dtm	?	wtm	btm	wtm	btm		#	dtm	#	dtm		#	dtm	#	dtm
01	0	<u>KBBKN</u>	1-0	32	155	43	156	Δ	21.05	48.20	0	0	\downarrow	275	131	319	132	↓≡	275	131	319	132
02	1	KBBKP	1-0	1	147	15	146	Δ	З	З	0.01	3	\downarrow	1	131	4	132	↓↑	1	137	16	136
03		<u>KBNKN</u>	1-0	2	213	1	212	Δ	0.52	1.93	0	0	↓	11,204	159	5,140	160		11,204	159	5,140	160
04		KBNKP	1-0	9	207	9	208	Δ	3	3	3	3	+	5	161	10	162	↓↑	8	175	2	174
05		KBPKN	1-0	1	199	1	192	Δ	3	3	3	3	\downarrow	6	175	4	174	$\downarrow\uparrow$ $\uparrow\uparrow$	1	177	1	176
06 07		kbpkp	1-0 1-0	92 3	133 89	52 3	134 88	=	0	0	0	0 0	=	92 3	133 89	52 3	134 88	$\uparrow\uparrow$	3 5	145 89	3 5	146 90
07	*	(kbpkr) KNNKP	1-0 1-0	2	⁰⁹ 229	3 4	00 228	Δ	26.35	46.87	42.16	30.80		5 7	223	12	00 222	$\uparrow\uparrow$	28	89 255	3	90 256
09		KNPKN	1-0	5	194	12	193	Δ	20.55 ε	40.87 E	42.10 ε	30.80 S	¥	5	161	12	162	$\downarrow\uparrow$	28 5	163	13	162
10		knpkp	1-0	10	113	10	114	=	0	0	0	0	=	10	113	10	114	$\uparrow\uparrow$	1	129	2	130
11		(kppkb)	1-0	1	85	1	86	=	0	0	0	0	=	1	85	1	86	==	1	85	1	86
12	2	(kppkn)	1-0	2	99	1	100	=	0	0	0	0	=	2	99	1	100	==	1	99	1	100
13	3	KPPKP	1-0	6	253	7	254	Δ	з	3	3	3	\uparrow	4	281	4	282	$\uparrow =$	5	281	4	282
14	2	KPPKQ	1-0	7	247	2	200	Δ	0.01	0.01	0	0	↑	17	275	1	200	↑≡	17	275	1	200
15	1	kppkr	1-0	1	107	1	106	=	0	0	0	0	=	1	107	1	106	==	1	107	1	106
16		KQPKP	1-0	1	209	6	244	Δ	З	3	3	3	~	4	191	9	274	$\uparrow\uparrow$	4	233	9	274
17		<u>KOPKO</u>	1-0	5	247	13	246	Δ	0.02	0.08	0.03	0.10	1	36	273	30	274	$\uparrow\uparrow$	3	275	30	274
18		KQRKP	1-0	1	79	3	134	Δ	0	3	0	0	↓	1	79	3	122	~^	5	107	3	122
19		KORKO	1-0	3 1	133 55	31 4	134 72	$\Delta \equiv$	з 0	з 0	0	0	\downarrow	3 1	121 55	31 4	122 72	↓≡ ↑↑	3 1	121 73	31 1	122 74
20 21		(krbkp) KRBKR	1-0 1-0	1 28		4 19	128	Δ	0.01	0.02	0	0 0	\downarrow	939	111	4 162	112	↓≡	939	111	162	112
21		KRPKB	1-0	28 3	145	13	128	Δ	0.01 8	0.02 ε	о 8	ε	▼	3	145	13	146	\uparrow	5	149	102	112
23		KRPKP	1-0	3	111	3	136	Δ	0	с 3	3	с 2	\downarrow	3	111	23	118	~1	1	121	9	120
24		KRPKQ	1-0	45	135	1	108	Δ	ŝ	e 3	3	0	~	22	123	1	114	~=	48	123	1	114
25		krpkr	1-0	33	147	4	148	=	0	0	0	0	=	33	147	4	148	$\uparrow\uparrow$	2	161	1	162
26	1	KBBKP	0-1	54	164	82	165	Δ	5.85	8.47	0.07	0.02	\downarrow	3	134	7	135	↓↑	4	136	2	137
27		<u>KBBKO</u>	0-1	74	162	15	161	Δ	8.49	1.46	0	0	\downarrow	3,116	124	1,030	123	↓≡	3,116	124	1,030	123
28	2	kbpkp	0-1	2	100	3	101	=	0	0	0	0	=	2	100	3	101	==	2	100	3	101
29	1	(kbpkq)	0-1	3	100	2	99	=	0	0	0	0	=	3	100	2	99	$\uparrow\uparrow$	1	104	2	103
30		KNNKP	0-1	11	146	9	147	Δ	0.14	0.06	0.10	3	↓	12	130	13	131	↓=	16	130	13	131
31		<u>KNNKO</u>	0-1	10	144	2	143	Δ	0.05	0.01	0	0	\downarrow	162	124	104	123	↓≡	162	124	104	123
32		knpkp	0-1	3	114	3	115	=	0	0	0	0	=	3	114	3	115	==	3	114	3	115
33		KNPKQ	0-1	1	124	2	109	Δ	3	0	0	0	\downarrow	1	114	2	109	$\uparrow\uparrow$	1	146	1	145
34 35		(kppkp)	0-1 0-1	3 12	84 82	3 6	85 81	=	0	0	0	0 0	=	3 12	84 82	3 6	85 81	 ↑↑	3 3	84 86	3	85 87
36		(kppkq) KRPKP	0-1	5	200	6	205	Δ	0.14	0.05	0.10	е С	↓	3	02 188	2	193	↓≡	3	188	2	193
37	-	KRPKQ	0-1	3	200	1	203	Δ	0.14	0.03	0.10	3 3	¥	21	194	1	195	\uparrow	3 7	214	3	213
																		 ↑↑				
38		(kppkn)	0-1	12 3	32 140	31 4	33 139	=	0	0 0	0	0	=	12 3	32 140	31	33	 ↑↑	2 3	36 144	10 4	35 142
39	0	krbkq	0-1	3		4		=	0		U	0	=		140	4	139			144	4	143
40		KBBKNN	1-0	11	211	1	212	Δ	50.15	70.98	1.75	2.78	↓	1	179	1	178	↓↑	2	181	1	180
41		KNNKNP	1-0	198	275	30	274	Δ	?	?	?	?	↓	160	223	11	222	↓≡	160	223	11	222
42	2	KNNKPP	1-0	2	259	3	258	Δ	?	?	?	?	\downarrow	1	257	2	256	$\uparrow\uparrow$	2	269	2	268

Table 1. Data for some endgame wins, the first 37 being those of Figure 1.⁵

The four-way DTZ-based taxonomy is indicated as follows:

- obviously unaffected wins (7) (bracketed 'lower case'), e.g., KBPKR (1-0), KPPK(Q/P) (0-1): maxDTM ≤ 100 ply ⇒ EM₅₀ = EM ⇒ there need be no 50mr-effect here or 'downstream',
- perhaps affected wins (6) (unbracketed lower case), e.g., K(B/N)PKP (1-0 and 0-1): the DTZ₅₀ and DTZ EGTs, i.e., $EZ_{50} \equiv EZ$, are identical but perhaps $dtm_{50} > dtm$ somewhere,
- affected wins (14) (upper case), e.g., KBBKP and KRPKP (both, 1-0 and 0-1), KPPK(Q/P) (1-0): maxDTZ ≤ 100 ply but there are 50mr draws, i.e., EM₅₀ ≠ EM,
- obviously affected wins (10) (underlined, upper case), e.g., KNNKP (1-0) and KRPKQ (0-1): maxDTZ > 100 ply ⇒ 50mr-draws ⇒ EM₅₀ ≠ EM.

Beyond the scope of Figure 1, Table 1 provides DTM_{50} data for a number of other endgames which are affected. A second DTZ/Z_{50} review (Bourzutschky et al., 2005) provides further context for Pawnless 6-man endgames.

⁵ maxDTM_{50,0} is compared with maxDTM. maxDTM $_{50,pc}$ is compared with maxDTM and then maxDTM $_{50,0}$. ' \downarrow ', ' \equiv ', ' \uparrow ' and ' \sim ' mean, respectively, 'if anything, less than', 'identical', 'if anything, more than' and 'considering wtm/btm, both less than and more than'. '=' rather than ' \equiv ' indicate that the number of maximal positions has changed.

With increasing likelihood, maxDTM_{50,pc=0} is greater than, less than or equal to maxDTM as indicated in Table 1:

 $maxDTM_{50, pc=0} > maxDTM:$

(1-0) KPPKP, KPPKQ, KQPKP btm, KQPKQ, KRPKQ btm

 $maxDTM_{50, pc=0} < maxDTM:$

(1-0) KB(B/N)K(N/P), KBPKN, KNNKP, KNPKN, KQPKP btm, KQRK(P/Q), KRBKR, KRPKP, KRPKQ wtm (and 6-man) KBBKNN, KNNKPP;

(0-1) KBBK(P/Q), KNNK(P/Q), KNPKQ, KRPK(P/Q)

		Value depths in ply						lv			
id	Endgame	FEN	1-0?	5-way	dtc	dtm	dtm50	dtz	dtz50	dtz50r	Notes: annotations to the DTZ_{50}' metric
01	KBNKN	8/8/1N6/8/6B1/1K3n2/8/k7 b 0 1	1-0	-2	100	158	160	100	100	100	maxDTM ₅₀ s6m_P-less pos for $pc \ge 0$
02	KPPKP	8/8/8/1p3K2/3P4/3P4/7k/8 b 0 1	1-0	-2	8	248	282	2	2	2	maxDTM ₅₀ s 6m pos for $pc \ge 0$
03	KRBKQ	k4B2/8/8/8/6q1/8/K3R3/8 w 01	0-1	-2	82	140	140	82	82	82	maxDTM ₅₀ P-less 2-man win for $pc = 0$
04	KRBKQ	k4B2/8/8/8/6q1/8/K3R3/8 w 11 1	0-1	-2	82	140	144	82	82	82	maxDTM ₅₀ P-less 2-man win for $pc \ge 0$
05	KRPKQ	4q3/1R6/8/8/k7/1PK5/8/8 b 0 1	0-1	2	137	193	195	77	77	77	maxDTM ₅₀ 2-man win for $pc = 0$
06	KRPKQ	2k5/8/8/R7/8/3K4/1P4q1/8 w 33 1	0-1	-2	126	182	214	64	64	64	maxDTM ₅₀ 2-man win for $pc \ge 0$
07	KNNKP	6k1/p7/8/8/7N/7K/2N5/8 w 0 1	1-0	2	178	181	223	30	56	56	maxDTM ₅₀ KNNKP pos for $pc = 0$
08	KNNKP	8/8/5N2/p7/8/k1K5/8/1N6 b 4 1	1-0	-2	167	190	256	43	93	93	maxDTM ₅₀ KNNKP pos for $pc \ge 0$
09	KQPKQ	3Q4/8/8/5K2/8/3P4/7k/1q6b01	1-0	-2	220	240	274	100	100	100	maxDTM ₅₀ KQPKQ pos for $pc = 0$
10	KQPKQ	3Q4/8/8/5K2/8/8/3P3k/1q6 w 88 1	1-0	2	141	163	275	1	1	1	maxDTM ₅₀ KQPKQ pos for $pc \ge 0$
11	KBBKNN	7k/7B/8/2B5/3K4/2n5/8/5n2 w 0 1	1-0	2	9	133	179	9	55	55	maxDTM ₅₀ KBBKNN pos for $pc = 0$
12	KBBKNN	$2n5/8/3B4/8/3K4/1B6/6n1/2k5 \ w \ - \ - \ 43\ 1$	1-0	2	21	139	181	21	55	55	maxDTM ₅₀ KBBKNN pos for $pc \ge 0$
13	KBBKN	8/8/7B/4k3/4B3/3K4/1n6 w 0 1	'1-0'	1	119	143	_	119	_	119	
14	KBBKP	8/8/8/7B/4k3/4B3/1p1K4/8b01	'1-0'	-1	6	144	_	6	_	1	1 b1=N+'''', 50mr-draw
15	KBNKN	8/8/3K4/8/8/3B4/k7/1n1N4 w 0 1	'1-0'	1	139	199	_	139	_	139	
16	KBNKP	8/8/3K4/8/8/3B4/kp6/3N4 b 0 1	'1-0'	-1	9	200	_	9	_	1	1 b1=N'''', 50mr-draw
17	KBPKN	1n6/3P4/8/8/1K6/7B/8/k7 w 0 1	'1-0'	1	1	199	_	1	_	1	1. d8=N'''', 50mr-draw
18	KNNKP	K1k5/3N1N2/8/8/4p3/8/8/8 w 0 1	'1-0'	1	169	169	_	164	_	164	
19	KNPKN	kn6/3P4/1K6/8/8/8/3N4/8 w 0 1	'1-0'	1	1	191	_	1	_	1	1. d8=B'''', 50mr-draw
20	KPPKP	8/4P3/8/8/8/4P3/kp1K4/8 b 0 1	'1-0'	-1	2	244	_	2	_	1	1 b1=Q'''', 50mr-draw
21	KPPKQ	8/4P3/8/8/8/4P3/k2K4/1q6 w 0 1	'1-0'	1	1	243	_	1	_	1	1. $e8=Q''''$, 50mr-draw ($dtz = 102p$)
22	KQPKP	8/4Q3/8/8/8/K7/6Pp/5k2 w 0 1	'1-0'	1	5	191	_	1	_	1	1. g4'''', 50mr-draw
23	KQPKQ	4Q3/8/8/8/8/4P3/k2K4/1q6b 01	'1-0'	-1	222	242	_	102	—	102	
24	KQRKP	Q7/2k5/8/8/8/8/R2p4/K7 b 0 1	'1-0'	-1	2	134	_	2	_	1	1d1=Q'''', 50mr-draw
25	KQRKQ	Q7/2k5/8/8/8/8/R7/K2q4 w 0 1	'1-0'	1	119	133	_	119	_	119	
26	KRBKR	8/3B4/8/1R6/5r2/8/3K4/5k2 w 0 1	'1-0'	1	117	129	_	117	—	117	
27	KRPKB	K1R5/8/3k4/3P4/8/8/1b6/8 w 0 1	'1-0'	1	113	131	_	105	_	105	
28	KRPKP	6R1/P6K/1k6/8/8/8/3p4/8 b 0 1	'1-0'	-1	2	136	_	2	—	1	1d1=Q'''', 50mr-draw
29	KRPKQ	6R1/P7/2q5/2k5/8/8/8/6K1 b 0 1	'1-0'	-1	2	118	_	2	—	2	1Kb6'''' 2. a8=Q'''', 50mr-draw
30	KBBKNN	8/6B1/8/8/2B1n3/6K1/3k3n/8 w 0 1	'1-0'	1	1	147	_	1	_	1	1. Kxh2'''', 50mr-draw
31	KBBKP	8/8/6B1/3K4/5B2/8/p7/3k4 b 0 1	'0-1'	1	1	157	_	1	—	1	1a1=Q'''', 50mr-draw
32	KBBKQ	8/8/6B1/3K4/5B2/8/8/q2k4 w 0 1	'0-1'	-1	136	156	_	136	_	136	
33	KNNKP	3k3N/3N4/3K4/8/8/8/7p/8 b 0 1	'0-1'	1	1	145	_	1	—	1	1h1=Q'''', 50mr-draw
34	KNNKQ	3k3N/3N4/3K4/8/8/8/8/7q w 0 1	'0-1'	-1	126	144	_	126	—	126	q.v., KNNKP '0-1'
35	KNPKQ	1k1K4/4P1N1/8/8/8/6q1/8/8 w 0 1	'0-1'	-1	6	124	_	6	—	1	1. e8=N'''', 50mr-draw
36	KRPKP	8/8/8/5PR1/8/2K5/5p2/k7 w 0 1	'0-1'	-1	2	188	_	2	—	2	1. Kd4'''', f1=Q'''', 50mr-draw
37	KRPKQ	8/7R/6K1/8/5P2/8/8/k6q b 0 1	'0-1'	1	116	165	-	3	-	2	1 Qe4+'' 2. f5'''', 50mr-draw

Table 2. Positions p01-p37: example maxDTM₅₀ wins and 50mr-draws.⁶

3.2 DTM_{pc} with free-ranging ply-count

With pc being allowed to range over all values 0-99, each endgame will have:

- a maxDTM_{50, $pc \ge 0$} and a set of positions and a set of pc-values for which $dtm_{50,pc} = maxDTM_{50,pc \ge 0}$,
- 'maximum penalty' positions for which ply-count pc produces max dtm50,pc-dtm,
- 'maximum variety' positions for which varying pc gives most values of $dtm_{50,pc}$.

Five 5m endgames have maxDTM_{50, pc=0} > maxDTM and sixteen more have maxDTM_{50, $pc\geq0$} > maxDTM:

- within Figure 1: (1-0) KBPK(P/R), KNNKP, KNPKP, KQPKP, KQRKP wtm, KRPKB, KRPKP wtm, KRPKQ btm, KRPKR and (0-1) K(B/N/P)PKQ, KRPKQ,

- beyond Figure 1: (0-1) KPPKN, KRBKQ and (6 man) KNNKPP.

⁶ "" = absolutely unique value-preserving move; " = unique metric-optimal move; ' = metric-equi-optimal move

Tables 2 and 3 provide a list of positions^{7,8} illustrating 50mr-impact:

- p01-p06: zonal maxDTM_{50, pc=0} and maxDTM_{50, $pc\geq 0$} positions,
- p07-p12: endgame-specific maxDTM_{50, pc=0} and maxDTM_{50, $pc\geq 0$} positions,
- p13-p37: '50mr-draw' frustrated wins or saved losses,
- p38-p46: DTM-lengthened wins or losses with pc = 0,
- p47-p50: zonal 'maximum *pc*/DTM-penalty' positions,
- p51-p56: endgame-specific 'maximum pc/DTM-penalty' positions,
- p57-p60: zonal maximum of the number of *pc*-determined mate-depths DTM_{50,pc},
- p61-p63: endgame-specific maximum number of mate-depths, nmd.

			Va	lue		de	pths	in p			
id	Endgame	FEN	1-0?	5-way	dtc	dtm	dtm50	dtz	dtz50	dtz50r	Notes: annotations to the DTZ_{50}' metric
38	KNNKP	6k1/p7/8/8/7N/7K/2N5/8 w 0 1	1-0	2	180	181	223	32	58	58	$dtm_{so} = dtm + 42p; \max DTM_{so, pc} = 0 \text{ pos.}$
39	KPPKP	8/8/8/2K4p/4P3/4P3/k7/8 b 0 1	1-0	-2	8	248	282	2	2	2	$dtm_{so} = dtm + 34p; maxDTM_{so, pc} = 0 pos.$
40	KPPKQ	8/4P3/8/8/1q6/3KP3/k7/8 w 0 1	1-0	2	1	241	275	1	1	1	$dtm_{so} = dtm + 34p; maxDTM_{so, pc} = 0 pos.$
41	KQPKQ	8/K7/8/8/7q/4PQ2/8/k7 b 0 1	1-0	-2	220	240	274	100	100	100	$dtm_{so} = dtm + 34p; maxDTM_{so, pc} = 0 pos.$
42	KRPKQ	1K4R1/P7/8/8/8/8/1k6/q7b01	1-0	-2	4	112	114	4	4	4	$dtm_{so} = dtm + 2p; \max DTM_{so, pc} = btm pos.$
43	KBBKNN	8/8/6n1/8/k3BB2/8/n1K5/8 w 0 1	1-0	2	1	133	149	1	55	55	$dtm_{so} = dtm + 16p$
44	KBBKP	8/8/8/1k6/8/8/p4BB1/3K4 b 0 1	0-1	2	1	123	125	1	13	13	$dtm_{50} = dtm + 2p$
45	KRPKP	8/8/5K2/8/2R2P2/8/6p1/k7b 01	0-1	2	1	159	163	1	11	11	$dtm_{so} = dtm + 4p$
46	KRPKQ	8/4q2R/k5K1/8/5P2/8/8/8 b 0 1	0-1	2	113	163	167	3	41	41	$dtm_{so} = dtm + 4p$
47	KPPKP	8/4P3/8/8/8/2K1P3/k3p3/8 w 99 1	1-0	2	1	17	275	1	1	1	$\max 5m_{vin} pc/DTM_{cost} = 258p$
48	KRRKN	k7/3R4/8/8/8/K2R4/8/4n3 w 97 1	1-0	2	4	5	81	4	4	4	$max 5m_P$ -less_win pc/DTM-cost = 76p
49	KNNKR	5r2/5N2/8/8/2N5/K1k5/8/8 b 98 1	0-1	2	1	3	73	1	1	1	max 2-3m_P-less_win pc/DTM-cost = $70p$
50	KRPKQ	8/8/8/8/2K5/4k3/RP6/4q3 b 88 1	0-1	2	13	29	191	7	7	7	max 2-3m_win pc/DTM-cost = 162p
51	KBBKN	k7/8/B2B4/8/3K4/8/8/6n1 w 90 1	1-0	2	9	11	45	9	9	9	max KBBKN pc/DTM-cost = 34p
52	KNNKP	7k/2K3Np/3N4/8/8/8/8/8 w 91 1	1-0	2	17	17	207	8	8	8	max KNNKP pc/DTM-cost = 190p
53	KQPKQ	8/1K6/8/8/q7/5Q2/4P3/k7 w 96 1	1-0	2	7	33	275	1	1	1	max KQPKQ pc/DTM-cost = 242p
54	KRBKR	8/8/B7/1R6/8/1K6/6r1/k7 w 90 1	1-0	2	9	11	37	9	9	9	max KRBKR (1-0) pc/DTM-cost = 26p
55	KRBKR	5r2/B7/8/8/2R5/1k6/8/K7 b 98 1	0-1	2	1	3	57	1	1	1	max KRBKR (0-1) pc/DTM-cost = 54p
56	KBNKNN	8/4B3/4N3/7n/k1K4n/8/8/8 w 98 1	1-0	2	1	3	161	1	1	1	max KBNKNN pc/DTM-cost = 158p
57	KNNKP	8/p7/2N3K1/8/8/8/2N1k3/8 w pc 1	1-0	2	120	121	→223	42	44	44	$\max \text{sub-6-man } nmd = 25$
58	KQNKR	7N/6rk/8/8/K7/8/8/6Q1 w pc 1	1-0	2	11	29	$\rightarrow 61$	11	11	11	$\max \text{sub-6-man}_P\text{-less } nmd = 12$
59	KRNKQ	7N/8/6R1/k7/8/8/K7/2q5 w pc 1	0-1	-2	8	42	→66	8	8	8	$\max 2-3m_P$ -less win $nmd = 11$
60	KRPKQ	8/8/4R3/3K2q1/2P5/8/7k/8 w pc 1	0-1	-2	58	104	→164	31	31	31	$\max 2-3m \min \max nmd = 14$
61	KBBKN	5n2/1BB5/8/8/8/2K5/8/3k4 w pc 1	1-0	2	17	37	$\rightarrow 51$	17	17	17	KBBKN max $nmd = 8$
62	KQPKQ	8/8/8/3P4/6k1/3K2q1/3Q4/8 w pc 1	1-0	2	99	115	→159	29	29	29	KQPKQ max $nmd = 13$
63	KRBKR	6B1/8/5r2/8/1K6/7R/8/1k6 w pc 1	1-0	2	23	33	→ 41	23	23	23	KRBKR max nmd = 5

Table 3. Positions p38-p63: example elongated wins, and maximum penalty/variety positions.

4 SUMMARY AND VIEW FORWARD

The impact of the 50-move rule on sub-6-man chess, including the effect of the ply count pc, has been identified. Given a shortage of remaining ply, the winning strategy is more adaptable in some endgames than in others. The 50mr impact increases as the number of men increases, and has been observed in key 6- and 7-man endgames of interest. This impact should be measured as the 50mr, now backed up by a mandatory 75-move rule, truncates chess as experienced over the board, whether played by man or machine. The evolving data files associated with this note (Huntington and Haworth, 2014) provide:

- extended versions of Tables 1-3,
- (annotated) pgn files illustrating various positions and lines mentioned here, and
- a set of spreadsheets of the first author's complete data.

The maxDTZ₅₀ figures inferred from these DTM₅₀ EGTs confirm previous figures (Tamplin and Haworth, 2004). Some maxDTM_{50, pc} positions and lines have been published in an evolving collection of chess records (Haworth, 2014b) which facilitates the comparison of DTM, DTM₅₀, DTZ and DTZ₅₀ lines.

⁷ The 5-way value-scale is ± 2 for unconditional '50mr-wins/losses', ± 1 for '50mr-draws' and 0 for unconditional draws.

⁸ The list includes a frustrated win but not necessarily a DTM-elongated win for every affected endgame.

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