



# *Sensitivity of a hydraulic model to changes in channel erosion during extreme flooding*

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1 **Sensitivity analysis of a hydraulic model to changes in channel erosion during extreme flooding**

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6

7 **Abstract**

8 Recent research into flood modelling has primarily concentrated on the simulation of inundation  
9 flow without considering the influences of channel morphology. River channels are often represented  
10 by a simplified geometry that is implicitly assumed to remain unchanged during flood simulations.  
11 However, field evidence demonstrates that significant morphological changes can occur during  
12 floods to mobilise the boundary sediments. Despite this, the effect of channel morphology on model  
13 results has been largely unexplored. To address this issue, the impact of channel cross-section  
14 geometry and channel long-profile variability on flood dynamics is examined using an ensemble of a  
15 1D-2D hydraulic model (LISFLOOD-FP) of the 1:2102 year recurrence interval floods in  
16 Cockermouth, UK, within an uncertainty framework. A series of hypothetical scenarios of channel  
17 morphology were constructed based on a simple velocity based model of critical entrainment. A  
18 Monte-Carlo simulation framework was used to quantify the effects of channel morphology together  
19 with variations in the channel and floodplain roughness coefficients, grain size characteristics, and  
20 critical shear stress on measures of flood inundation. The results showed that the bed elevation  
21 modifications generated by the simplistic equations reflected a good approximation of the observed  
22 patterns of spatial erosion despite its overestimation of erosion depths. The effect of uncertainty on  
23 channel long-profile variability only affected the local flood dynamics and did not significantly  
24 affect the friction sensitivity and flood inundation mapping. The results imply that hydraulic models  
25 generally do not need to account for within event morphodynamic changes of the type and  
26 magnitude modelled, as these have a negligible impact that is smaller than other uncertainties, e.g.  
27 boundary conditions. Instead morphodynamic change needs to happen over a series of events to  
28 become large enough to change the hydrodynamics of floods in supply limited gravel-bed rivers like  
29 the one used in this research.

## 1 1. Introduction

2 River morphology is both a control and consequence of fluvial processes (Sear *et al.*, 2010). River  
3 channels subjected to morphological changes during a subset of flood events could have significant  
4 implications for floodplain inundation, flow depth, and floodwave propagation and the associated  
5 uncertainties. Numerous studies have addressed one or some of the types of the uncertainty in the  
6 modelling: model structural choice (e.g. Apel *et al.*, 2009), model friction and conveyance  
7 parameters (e.g. Aronica *et al.*, 1998; Romanowicz and Beven, 2003; Bates *et al.*, 2004; Werner *et*  
8 *al.*, 2005; Pappenberger *et al.*, 2007), and boundary conditions (e.g. Pappenberger *et al.*, 2006;  
9 Pappenberger *et al.*, 2007). The sensitivity of flood inundation predictions to uncertainty of the  
10 geometry of the floodplain (e.g. Werner *et al.*, 2005) and channel (e.g. Pappenberger *et al.*, 2006;  
11 Pappenberger *et al.*, 2007) (including the representation of natural and man-made flow control  
12 structures such as vegetation and buildings (e.g. Beven *et al.*, 2012)) have also been evaluated. In  
13 addition, others have presented methodology for the estimation of uncertainty of the models, which  
14 takes account of the uncertainty in the observed data (e.g. Pappenberger *et al.*, 2007; Di Baldassarre  
15 *et al.*, 2009; Stephens *et al.*, 2012; Stephens and Bates, In revision). Increased flooding is shown to  
16 be caused by either hydrologic changes that increase peak flows or geomorphic changes that reduce  
17 channel conveyance (Stover and Montgomery, 2001). Thus, how flood dynamics interact with  
18 morphological change is a topic of growing interest for hydraulic modelling (Fewtrell *et al.*, 2011).  
19 Driving this motivation has been the basic question that, given the uncertainty inherent in other  
20 sources like observation error and boundary conditions, is it important to account for uncertainty in  
21 morphodynamic changes within a flood event? The standard hydraulic models adopted for risk  
22 mapping use a static representation of channel geometry, but without studies that quantify the  
23 uncertainties associated with a changing channel geometry it is impossible to know whether this is a  
24 significant uncertainty that is missing from the quantification of risk. This paper therefore addresses  
25 this question by assessing the impact of changes in channel long-profile and cross-section during an  
26 extreme flood event on water surface elevation and subsequently the depth and extent of flood  
27 inundation.

28 Reviewing the development in the flood risk estimation and flood inundation mapping literature  
29 finds that most of the numerical hydraulic models (e.g. Galland *et al.*, 1991; Bates and De Roo, 2000;  
30 Brunner, 2002) are concentrated merely on the simulation of inundation flow without considering the  
31 influences of channel morphology and sediment delivery from upstream. In most cases  
32 hydrodynamic unsteady models are applied in which the river channels are considered as a means of  
33 access for flow conveyance rather than a device for controlling river flow patterns (Neuhold *et al.*,  
34 2009). It has been suggested that the complexity of channel geometry is not significant during large  
35 flood events as the whole floodplain and river channel can act as a single channel unit (Bates *et al.*,  
36 2005). River channels can then be represented by a simplified geometry that is implicitly assumed to  
37 remain unchanged during flood events and under long-term erosion and deposition. However,  
38 bedload may become highly mobile during floods, forces on the bed, banks and floodplain are  
39 sufficient to mobilise the boundary sediments resulting in significant changes in channel morphology  
40 (cross-section and long-profile) and even channel pattern (Kleinhans *et al.*, 2013), resulting in  
41 modification of form roughness (Hey, 1979). This suggests that the influence of sediment and

1 subsequent changes in bed elevation may be an important control on hydraulic and flood inundation  
2 modelling.

3 Following recent large flood events, during which significant and damaging morphological change  
4 occurred, both in the UK and other parts of the world (e.g. River Derwent in UK 2009, 2012; River  
5 Indus in Pakistan 2010), there is an increasing need to evaluate the impact and uncertainties  
6 introduced by morphological change on the accuracy of flood inundation modelling. Hydraulic  
7 models are not only sensitive to model parameters and the representation of hydraulic structures, but  
8 also the geometric description (Merwade *et al.*, 2008). Fewtrell *et al.* (2011), for instance, showed  
9 that cross-section variability is less important than the channel long-profile in the calibration process  
10 with the use of a coupled dynamic 1D-2D hydraulic model (ESTRY-TUFLOW) of the Carlisle  
11 floods of January 2005. Other studies have addressed the intricacy of channel geometry  
12 representation and showed the flood inundation area will be influenced by the number and location  
13 of cross-sections (e.g. Cook and Merwade, 2009). Implementation of hydraulic models also requires  
14 the specification of suitable roughness parameters. Channel and floodplain roughness used in many  
15 studies (e.g. Aronica *et al.*, 2002) are commonly examined in a calibration process based on  
16 observed flood inundation extent and flow depth. Roughness values, and the way in which they  
17 change with depth, are needed to compensate for the restrictions in the model representation of  
18 channel geometry, floodplain topography and energy dissipation at the scale of model resolution as  
19 such these roughness values are often referred to as 'effective' (e.g. Pappenberger *et al.*, 2005;  
20 Werner *et al.*, 2005). Therefore, reach scale effective values of roughness are required, but little  
21 attention is paid to the impact of geometric description on model sensitivity to roughness parameter  
22 values which can be highly uncertain.

23 Knowing the effect of uncertainty in channel geometry on roughness parameter values is not  
24 sufficient and the challenge is to, perhaps more importantly, assess the effect that such uncertainty  
25 may have on model performance. Channel geometry and floodplain topography are the principal  
26 variables that affect the flood wave propagation and are therefore critical to the prediction of flood  
27 dynamics. A small degree of uncertainty in bed elevation may have a relatively large effect on model  
28 predictions (Wilson and Atkinson, 2005). In a study of a 5.6km reach of the Upper River Wharfe,  
29 UK, Raven *et al.* (2009) showed that a mean bed level rise of 0.17m over the six-year monitoring  
30 period had a significant effect on increasing the flood frequency by 2.6 times on average, and  
31 overbank flow time by 12.8 hours. Similarly, Stover and Montgomery (2001) concluded that whilst  
32 the requisite discharge for overbank flow and peak discharge had reduced, the frequency of flooding  
33 had increased as a result of aggradation on the mainstem Skokomish River, Washington State, USA.  
34 Furthermore, recent research that incorporates the implications of sediment delivery and river bed  
35 level changes on flood risk (Lane *et al.*, 2007; Lane *et al.*, 2008; Neuhold *et al.*, 2009), have  
36 highlighted the fact that an effective flood inundation modelling strategy should be built on how  
37 sensitive the flood dynamics are to the changes not only in hydrological but also morphological  
38 processes.

39 In the light of current interest and recent research, the objectives of this paper are therefore 1) to  
40 develop an approach that reconstructs realistic changes (in terms of spatial patterns) in channel  
41 erosion during flood events; 2) to examine the impact of modelled bed elevation changes during a  
42 flood event on model sensitivity to roughness parameter values; 3) to assess the significance of

1 modelled bed elevation changes on the prediction of flood depths; and, 4) to explore and quantify the  
2 differences arising from cross-section geometry and long-profile variability on flood inundation  
3 mapping. The recent extreme flooding in Cockermouth, UK provides a useful test because of the  
4 availability of high quality hydrological, flood inundation and morphological data for before and  
5 after flood conditions.

## 6 **2. Test Site and Data Availability**

7 The town of Cockermouth in North West Cumbria, UK, is situated at the confluence of one major  
8 river (River Derwent) and the River Cocker, with the River Marron joining the main River Derwent  
9 further downstream (Figure 1). This study reach, 32.27km in length, was selected because: a) an  
10 extreme flood event in November 2009 caused significant morphological changes to the river  
11 channels and floodplain and, b) a data-rich case study that has multiple datasets of the observed flood  
12 extent at different times during the flood for evaluation of model performance was available.

13 The November 2009 event followed a prolonged period of rainfall over the catchment. A rain gauge  
14 at Seathwaite Farm in Borrowdale, about 24.1km southeast of Cockermouth, recorded the highest  
15 24hr total ever recorded in the UK of 316.4mm. Furthermore, major lakes and reservoirs within the  
16 region were already full and with the waterlogged upland catchment soil conditions, this resulted in a  
17 large amount of runoff into the river network. The resulting peak flow at Camerton gauging station  
18 on the Derwent was estimated by the Environment Agency of England and Wales (hereafter the EA)  
19 as  $700\text{m}^3\text{s}^{-1}$  and historic flood marks indicated that it was the largest event since at least 1899. The  
20 flood event was estimated to have a return period of 2102 years, with 95% confidence limits of 507  
21 and 17706 years (Miller *et al.*, 2013). These high river flows destroyed six bridges and flooded 855  
22 properties in Cockermouth and Workington. Sediment transport processes resulted in the largest  
23 changes in channel width since at least 1867, the date of the first accurate surveys of the river  
24 planform. Bank erosion, including the collapse of river cliffs up to 30m in height, injected substantial  
25 quantities of sediment into the flooded river. Much of that material was then deposited on the  
26 floodplain and infilled pools within the river channels. In one area, the channel avulsed across the  
27 floodplain to create a new planform for the water flow.

28 The EA provided a digital elevation model (DEM) at 2m resolution of the study site, generated from  
29 an airborne laser altimetry (LiDAR) survey flown in 1998 and April/May 2009. The majority of the  
30 data was from 1998 and had a vertical Root Mean Square Error (RMSE) of approximately 0.25m .  
31 Three different datasets of the observed flood extent were taken at different times during the flood: 1)  
32 aerial photography of the flood, which had a horizontal resolution of 0.15m, taken between 13:10  
33 and 14:50 on 20<sup>th</sup> November; 2) well defined wrack marks, which were visible along much of the  
34 extent of the flood in the aerial photograph and represent the maximum flood extent; and, 3)  
35 TERRASAR-X imagery, which had a 1m horizontal resolution, captured at 18:02 on 21<sup>st</sup> November.  
36 Water level measurements at 15-min intervals were provided for three gauges around Cockermouth:  
37 upstream on River Derwent at Ouse Bridge and downstream at Camerton, and upstream on the River  
38 Cocker at Southwaite Bridge (See Figures 1 & 2). The Ouse Bridge gauge was bypassed during the  
39 flood. Yet, the EA had provided metadata to advise that the stage at the peak of the flood has been  
40 edited using estimates of the maximum flood level from a wrack survey, with the time of peak and  
41 the infilled data estimated using correlation techniques. The Camerton gauge was severely damaged

1 during the flood event, the dataset with ‘Good’ readings only recorded up to 19th November 2009 at  
2 20:30. After this, the only available data are through correlation with the Southwaite gauge. Flow  
3 data for the River Marron was provided by rescaling the flows in the Cocker using the comparative  
4 size of the catchments. Data to quantify the river channel geometry and bed material grain size of the  
5 River Derwent were also available. Some 234 and 191 channel cross-sections were surveyed for the  
6 study reach of the River Derwent in 1998 and 2010 respectively. The 1998 dataset were provided by  
7 the EA and was based on a composite of ISIS Section 105 model total station cross-section surveys,  
8 and repeat cross-sections within the town of Cockermouth. The 2010 data was based on cross-  
9 sections surveyed by the EA in December 2009 from Workington to immediately upstream of  
10 Cockermouth. In addition, 127 repeat cross-sections were surveyed for the whole river in May and  
11 August 2010 by this study (See Table 1 for summary). The 2010 cross-sections were taken at  
12 locations close to those made in 1998, of which 93 could be paired as they were within 10m of each  
13 other.

14 As there were five major flood events between 2003 and 2008 (Figure 3) the 1998 DEM was updated  
15 and modified to provide a better representation of topography before the 2009 flood event. The 1998  
16 DEM was built from a combination of datasets: 1998 LiDAR 2m DEM, 1998 cross-section survey,  
17 2005 repeat cross-section survey for the reach through the town of Cockermouth, and bank outlines  
18 derived from the latest aerial photographs (1:3000) taken in 2004. <5% of the total cross-sections,  
19 where bank migration had occurred between 1998 and 2004, were linearly interpolated out to the  
20 position of the 2004 bankline. In the area of wetted channel, 1998 (adjusted to 2004 banklines) and  
21 post-2005 flood cross-sections were interpolated to generate cross-sections at 5m spacing throughout  
22 the whole channel using the method of Merwade *et al.* (2008) and Cook and Merwade (2009), with a  
23 RMSE of 0.235m. Using the 2004 banklines as 3D breaklines (Wheaton *et al.*, 2010), the cross-  
24 section nodes were combined with the LiDAR 2m DEM data within the 2004 bankline mask to  
25 create a 2m DEM for the wetted and non-wetted valley floor. Comparison of cross-sections surveyed  
26 post the 2005 flood in the reach through Cockermouth with those taken in 1998 show minor changes  
27 in bed elevation associated with submerged bars (0.15 +/- 0.08m) and localised changes in bank  
28 outline. Therefore, the modified DEM was assumed to closely reflect the river morphology and  
29 topographic conditions at the time of the 2009 flood event.

### 30 **3. Methodology**

#### 31 3.1. Model setup

32 The LISFLOOD-FP model was considered appropriate and was used in this paper for three reasons.  
33 Firstly, the model was relatively straightforward to implement (in terms of data requirement) and edit  
34 (in terms of changing river geometry). Secondly, the model code has been extensively validated and  
35 benchmarked, and is routinely employed in industrial applications (Hunter *et al.*, 2008). Lastly, the  
36 model was not limited by computational burden given the large number of simulations required to  
37 fully examine the model sensitivities.

38 A 1D-2D LISFLOOD-FP model was then set up with the river channel represented by a diffusive  
39 wave solver as described by Trigg *et al.* (2009) and the floodplain represented by the inertial  
40 formulation of the shallow water equations as described by Bates *et al.* (2010). The location and  
41 structure of the channel in the channel component is specified as a series of XY coordinates that can

1 be matched to a corresponding cell in the floodplain component and is represented using variables  
 2 for channel width and bed elevation at each XY coordinate. In the model, water is routed through the  
 3 channel component until flows exceed the channel capacity, at which point the excess flow divided  
 4 between the two grid cells adjacent to the channel cell and entered the floodplain component.

5 The floodplain topography in the model was described using the modified DEM, rescaled to 20m  
 6 resolution to enable multiple simulations to be run for computational efficiency. The 1D channel  
 7 model was driven by the 234 channel cross-section points extracted from the mid-points of each  
 8 1998 surveyed cross-section (Figure 4). The channel geometry was assumed to be a rectangular  
 9 shape due to the inability of LISFLOOD-FP to represent complex irregular channels. The channel  
 10 slopes were taken from the survey by allowing the channel bed to slope both positively and  
 11 negatively. The channel widths were extracted by measuring the distance between two end points of  
 12 each cross-section and the bed elevations of the channel were adjusted such that bank-full cross-  
 13 sectional flow area matched the surveyed bank-full flow area along the reach.

14 Instead of using the gauged data for Camerton as a downstream stage-varying boundary condition on  
 15 account of the failure of the gauge during the event, a free boundary condition has been imposed.  
 16 The River Derwent catchment is characterised as a gravel-bedded river ( $D_{50}$   $0.058 \pm 0.017$ m) with  
 17 pastoral (grazed grass) land use dominating the floodplain across the catchment. According to Chow  
 18 (1959) pasture with short grass would have a minimum Manning's  $n$  of 0.025, and a gravel bed  
 19 would have a minimum of 0.030. Some areas of the catchment are heavily forested or have medium  
 20 to dense brush, which might expect a maximum Manning's  $n$  value of 0.120 (Chow, 1959). To  
 21 ensure that the entire range of potential friction values were sampled, and also accepting that friction  
 22 as specified in LISFLOOD-FP acts as an effective value to parameterise un-modelled process and  
 23 features such as sub-grid scale topography and three dimensional flow structures, a range of channel  
 24 ( $n_{ch}$ ) and floodplain ( $n_{fp}$ ) friction values of between 0.020 and 0.140 were explored.

### 25 3.2. Evaluation of model performance

26 The two observed datasets (wrack marks and aerial photography) were processed by Stephens and  
 27 Bates (In revision) to provide a total of 177 maximum water elevations and 3724 observed data  
 28 points for model assessment. The outline of the flood in the TERRASAR-X image was also  
 29 manually digitised and converted to 3353 data points from which known erroneous points, such as in  
 30 vegetated areas, were removed.

31 Based on the analysis procedure described in Aronica *et al.* (2002), Monte-Carlo simulation using  
 32 the GLUE technique (Beven and Binley, 1992) was adopted. 300 parameter sets were randomly  
 33 sampled from the parameter space to evaluate model performance at the time steps when the  
 34 observed datasets were collected. Mason *et al.* (2009) described two water surface elevation  
 35 comparison methods (RMSE and paired  $t$  test) to assess the acceptability of parameter sets. The use  
 36 of paired  $t$  test might be problematic as mentioned in Stephens *et al.* (2012) and therefore the RMSE  
 37 will only be used in this study. The equation is defined as the square root of the mean square error  
 38 and is given as

$$39 \quad RMSE = \sqrt{E((sim_i - obs_i)^2)} \quad (1)$$



1 where  $i$  is the number of data points,  $sim$  the simulated nearest water surface elevation in the model,  
 2 and  $obs$  the observed flood margin on DEM elevation.

3 According to their RMSE performances, the parameter sets were ranked and normalised into  
 4 generalised likelihoods (Wagener *et al.*, 2002). This measure could only be treated as analogous to a  
 5 true probability as it could not be used for formal statistical inference (Wagener *et al.*, 2002).  
 6 Because of the unavoidably subjective process when no consistent error structure could be assumed  
 7 (Freer *et al.*, 2003), the top 20% of parameter sets were used to classify as behavioural simulations,  
 8 the rest were rejected and their likelihoods were set to zero. Each parameter set was then weighted  
 9 and assigned a value corresponding to how well the simulations reproduced the result in a global  
 10 sense. The observed datasets were combined by evaluating on one dataset, then using another to  
 11 update the weights assigned to each parameter set with the use of a recursive form of Bayes'  
 12 equation (Lamb *et al.*, 1998). The combined likelihood values associated with behavioural parameter  
 13 sets were used to calculate and then map the relative probability ( $P_i^{flood}$ ) that a given pixel is  
 14 inundated, using the following equation

$$15 \quad P_i^{flood} = \frac{\sum_j f_i W_j}{\sum_j W_j} \quad (2)$$

16 where  $j$  is the number of model simulations,  $f_i$  represents the numerical model result at a pixel  $i$  for  
 17 each parameter set, and takes a value of 1 for a flooded pixel and is 0 otherwise.  $W_j$  acts as a  
 18 generalised relative measure for each simulation.

### 19 3.3. Generation of bed elevation scenarios

20 A simplified method was adopted to statically adjust the channel geometry at the beginning of the  
 21 simulation due to the inability of LISFLOOD-FP to represent any morphodynamic processes and  
 22 complicated technical demand to incorporate all processes (e.g. erosion, deposition, bank failure,  
 23 etc.). Erosion during the flood peak was chosen as the focus of this paper because this is the point of  
 24 the flood where flood extent and depths are greatest, and therefore has the highest risk as well as  
 25 potential for geomorphological change. It is also the period when the largest sensitivities and  
 26 uncertainties were most likely to be found. In addition, the majority of channel change was erosional,  
 27 with deposition occurring as extensive gravel and sand sheets, on floodplains immediately  
 28 downstream of river cliff failures. Lateral erosion (bank failure) was excluded in the erosion process  
 29 to further reduce the complexity of parameter uncertainties. Therefore, changes in bed elevations at  
 30 each cross-section were used as a simplified representation of changes in river morphology during  
 31 the flood event.

32 The construction of hypothetical bed elevation scenarios was derived from a simplified duBoys-type  
 33 sediment transport formulae (DuBoys, 1879) that have a shear stress relationship, which was  
 34 developed by relating sediment transport to the threshold of incipient motion of sediments. For a  
 35 fluid to begin transporting sediment that is currently at rest on a surface, the bed shear stress  $\tau_b$   
 36 exerted by the fluid must exceed the critical shear stress  $\tau_{cr}$  for the initiation motion of grains at the  
 37 bed (Buffington and Montgomery, 1997). The bed shear stress  $\tau_b$  is expressed as a force per unit  
 38 area of the bed ( $Nm^{-2}$ ) and increases with flow depth and water surface slope while the critical shear

1 stress  $\tau_{cr}$  is defined in a dimensionless form (Shields *et al.*, 1936) and increases with particle size  
2 and bed roughness. They are defined as

$$3 \quad \tau_b = \rho g R_h S \quad (3)$$

$$4 \quad \tau_{cr} = \theta_{cr}(\rho_s - \rho)gD \quad (4)$$

5 where  $g$  is acceleration due to gravity (assumed to be  $9.8\text{ms}^{-2}$ ),  $R_h$  hydraulic radius,  $S$  water surface  
6 slope ( $\text{mm}^{-1}$ ),  $\rho$  water density (assumed to be  $1000\text{kgm}^{-3}$ ),  $\rho_s$  the sediment density (assumed to be  
7  $2650\text{kgm}^{-3}$ ),  $\theta_{cr}$  the dimensionless shear stress, and  $D$  a characteristic grain size (m). Equation (4)  
8 represents the moment at which sediment movement begins. Equation (3) was converted in terms of  
9 velocity  $v$  using the Manning equation ( $v = \frac{1}{n}R_h^{2/3}S^{1/2}$ ). Combining the two equations and  
10 rewriting the terms, Equation (4) was converted into critical velocity  $v_{cr}$ , defined as

$$11 \quad v_{cr} = (\theta_{cr}GR_h^{1/3}D)^{1/2}/n \quad (5)$$

12 where  $G = \frac{(\rho_s - \rho)}{\rho}$  is the dimensionless submerged specific gravity of the sediment, and  $n$  the  
13 Manning's  $n$  which is estimated by the Strickler equation ( $n = D^{1/6}/21$ ) (Strickler, 1923).  
14 Rewriting the Manning's  $n$  and Equation (5) became

$$15 \quad v_{cr} = 21R_h^{1/6}D^{1/3}(\theta_{cr}G)^{1/2} \quad (5.1)$$

16 Given a 1D channel with steady and uniform flow, at each cross-section, the relationship between  
17 velocity and critical velocity is defined as

$$18 \quad vh = v_{cr}(h + e) \quad (6)$$

19 where  $e$  is the erosion depth (m), and  $h$  the water depth (m). Re-arranging the equation, the  
20 following equation can be used to calculate the maximum possible bed elevation change, defined as

$$21 \quad e = \begin{cases} h\left(\frac{v}{v_{cr}} - 1\right) & \text{if } v > v_{cr} \\ 0 & \text{if } v \leq v_{cr} \end{cases} \quad (7)$$

22 This equation only accounts for the erosion caused by flow at the time that maximum velocity  
23 occurred, and makes a couple of assumptions: 1) there were no sediment transported and deposited  
24 from upstream; 2) there were no lateral erosion (bank failure) during the flood event; 3)  
25 consequences that caused by deposition within the channel such as avulsion, increased lateral erosion,  
26 channel instability were neglected; 4) the channel was in rectangular shape along the long profile;  
27 and 5) local features such as presence of bedrock and bridges were ignored. In other words, the paper  
28 only focusses on the scouring effect of the flood event during the peak caused by the changes in  
29 mean bed elevation, before any sediment could deposit downstream as the flood proceeded. Similar  
30 with other applications in sediment transport formulae (Gomez and Church, 1989), one calculation is  
31 undertaken for each cross-section with the mean depth being input into the equation and such a  
32 simple approach may reduce the capability of the equation. The equation is also affected the different  
33 sources of error arising from the propagation of error in the measured variables (e.g. McLean *et al.*,  
34 1999) and the spatial variability of bed shear stress (Wilcock, 1996). Moreover, the uncertainty

1 involved in the equation is evident in the fact that the values of the dimensionless critical shear stress  
2 differ from a variety of roughly a factor of two (Buffington and Montgomery, 1997). Additionally,  
3 the equation is sensitive to grain size distribution due to patch dynamics or topographic variability  
4 across the channel. Regardless of well-documented limitations in using such formulae approach  
5 (Gomez and Church, 1989), sediment transport formulae continue to be widely used and reasonably  
6 accepted in geomorphological studies. It is acknowledged that the accuracies of the formulae  
7 approach could be improved by building an empirical relationship between transport rate and flow  
8 discharge from field measurements (Wilcock, 2001), but effort required to determine this input can  
9 be very large, becoming impractical as it involves knowledge of the bed grain size and topography  
10 throughout the reach. A balance must then be found between the overall ease of the implementation  
11 of the approach and the complexity involved in the equation.

12 The dimensionless critical shear stress  $\theta_{cr}$  and grain size  $D$  were believed to be the main source of  
13 uncertainty in the equation and thereby considered in this study. The range of values of  $\theta_{cr}$  0.03 to  
14 0.06, which cover different flow conditions (Reynolds numbers ranging from  $\approx 10$  to  $\geq 400$ ),  
15 previously reported in the literature (Graf, 1971) were adopted here. Regarding  $D$ , the simplest and  
16 most common approximation was to treat the bed material as a single size fraction (e.g. the median  
17  $D_{50}$ ) (Wilcock, 2001). Based on the surveyed grain size data which were sampled at four locations  
18 (Isel, Cockermouth, Papcastle, and Great Broughton) along the River Derwent (see Figure 1), the  
19 grain size distribution was computed at each site using the Wolman method (Wolman, 1954),  
20 whereby grains are blindly selected from the channel every few walks in a rough grid pattern. The  
21 Wolman method uses the percentile system to characterise the grain size variability and errors  
22 involved in estimating the percentiles using this methods are mainly because of the influence of  
23 fluctuations in sampling (Green, 2003). However, assuming that the grain size distribution is log-  
24 normal, the precision reduces with distance from the median percentile,  $D_{50}$ , and only decreases  
25 noticeably beyond the 5th and 95th percentiles (Inman, 1952). The 5th (0.048) and 95th (0.082)  
26 percentiles were reasonably to be used to represent the entire bed size distribution, while remaining  
27 simple enough to permit a practical integral description of the sediment. 300 parameter sets for  $\theta_{cr}$   
28 and  $D$  were randomly sampled and generated from the range specified accordingly. Despite the  
29 rectangular channel assumption, it is expected that the model would perform equally well in terms of  
30 optimum RMSE as compared with model with channels of higher complexity (Fewtrell *et al.*, 2011).  
31 The results of Fewtrell *et al.* (2011) also suggested that in order to obtain a good prediction of  
32 maximum water levels, it is essential to configure a channel approximation that maintains an  
33 estimate of bank-full capacity that is consistent with field observations, as was the case in this study.

34 The velocities in Equation (7) and critical velocities in Equation (5.1) were determined by running a  
35 steady state flow simulation of LISFLOOD-FP. 300 bed elevation scenario cases were then  
36 generated by Equation (7) for each behavioural friction parameter set. The 5th and 95th percentiles  
37 were extracted to save computational cost and used as inputs in LISFLOOD-FP for re-evaluation of  
38 model performance. The two percentile cases represented two extreme scenarios in which the 5th  
39 percentile portrayed the least amount of possible erosion while the 95th described the greatest. The  
40 same procedure applied and the probabilistic map was again generated for comparison.

41 In addition, the simulated bed elevation changes were compared with the 93 pairs of observed data  
42 points where both pre- and post-flood surveys were taken. The aim of the comparison was to provide

1 a general idea of how well the hypothetical erosion changes reflected the observed spatial  
2 geomorphic changes. The 2010 surveyed cross-section data, in which ten of them had to be modified  
3 to account for sediment management undertaken by riparian owners in the intervening period  
4 following the flood, were assumed to reflect the nearest river geometry after the 2009 flood event  
5 because: 1) comparison between ground based photographs taken immediately after the flood with  
6 those taken during the surveys showed no obvious evidence of bar or bank changes in reaches  
7 without major sediment management; and, 2) the morphological changes resulting from the  
8 November 2009 flood were clearly far greater than any subsequent re-sculpting, or any channel bank  
9 migration since the first accurate surveys of the bank line undertaken by the Ordnance Survey in  
10 1867. The data were then used to compute the observed changes in bed elevation for comparison.

## 11 **4. Results**

### 12 4.1. Modification of river bed elevations

13 Because of the inability of LISFLOOD-FP to dynamically change the channel geometry during  
14 simulations, Equation (7) was used to account for the erosion processes during the flood peak and to  
15 statically adjust the channel geometry at the start of the simulation. Figure 5a illustrates the  
16 hypothetical changes of river bed elevations along River Derwent from downstream. The two dash  
17 lines represent the 5th (black) and 95th (grey) percentile calculated erosion depth. Figure 5b displays  
18 the 5th percentile bed elevation scenario on subsection of the domain covering the downstream area  
19 near Camerton while Figure 5c and 5d show the 95th percentile scenario on subsections of the  
20 domain covering area near Great Broughton and the vicinity of Cockermouth and Papacastle  
21 respectively. White represents areas of channel where there has been no erosion, and increasing  
22 erosion depths (m) are represented by an increase in saturation of red. The 95th percentile scenario  
23 displays discontinuous erosion along the reach with little or almost no scouring for the last 5km  
24 measuring from downstream. Both scenarios showed three major erosion zones: (1) between BNG  
25 311572E 530696N and BNG 311295E 531137N where Cockermouth and Papacastle lie (Figure 5d);  
26 (2) at BNG 307774E 531170N near Great Broughton (Figure 5c); and (3) downstream near  
27 Camerton at BNG 303832E 530554N and BNG 303623E 530044N (Figure 5b). Yet, care should be  
28 taken when looking at the erosion depth at the tight bend in Papacastle as the river floor and width are  
29 confined by bedrock, in which the presence of bedrock was not represented in the model. The real  
30 values of vertical changes are likely to have been lower than modelled. Local erosion was also  
31 predicted to occur at BNG 309795E 530900N and BNG 308295E 530900N respectively due to the  
32 presence of two bridges. The bridge structure was not represented explicitly in the model but its  
33 effect was simulated by a reduction in channel cross-sectional area at cross-sections co-incident with  
34 the bridge resulting in an increase in velocities and subsequent erosion.

35 The modification of river bed elevations based on Equation (7) was further compared with the 93  
36 pairs of observed data points where both pre- and post-flood surveys were taken. The black dots in  
37 Figure 6 show the net differences in observed data points between pre- and post- surveys along the  
38 River Derwent from downstream and the envelopes indicate the 5th and 95th percentiles of simulated  
39 erosion depth at the observed locations. Negative values mean net erosion and positives net  
40 deposition. Referring to the locations where erosion was seen to be the dominant process (between  
41 23.5km and 31.3km), the observed bed elevation changes ranged from -0.06m to -0.84m while the  
42 5th and 95th percentile envelope covered similar ranges (from -0.02m to -0.75m). Estimated by a

1 wide range of percentile envelopes by Equation (7), two locations between 14.8km and 17.4km and  
2 between 2.9km and 4.9km matched the areas where dynamic geomorphic processes, both erosion  
3 and deposition, were observed. The observed bed elevation changes ranged from -0.54m to +1.00m  
4 and from -1.45m to +1.16m respectively. Even though the wide range of percentile envelopes  
5 provided unrealistic erosion depths (especially between 2.9km and 4.9km where the 95th percentile  
6 erosion depth could be up to 2.9m), the envelopes do indicate the potential erosive power of the  
7 flood at these locations and reveal the areas where dynamic changes could potentially occur.

#### 8 4.2. Model sensitivity to parameter roughness values

9 After identifying the possible ranges of erosion process during the flood event, the 5th and 95th  
10 percentile bed elevation scenarios were then used as inputs in LISFLOOD-FP for re-evaluation of  
11 model performance. Figure 6 present the sensitivity of the RMSE between the 300 simulated and  
12 observed water levels obtained from the three datasets before and after applying the bed elevation  
13 changes using Equation (1). It is immediately noticeable that the model showed no real sensitivity to  
14 channel friction, only floodplain friction (Figure 7 left) for all three datasets. This suggests that the  
15 channel friction had little effect on flow conveyance as the floodplain and river channel acted as a  
16 single channel unit during the flood event. Even taking the river bed channel changes into  
17 consideration, the sensitivity remained similar (Figure 7 middle & right). However, differences  
18 between the parameter spaces were still witnessed. There were noticeable changes in the region for  
19 the floodplain optimum. In general, the region for the floodplain optimum for all scenarios moved  
20 gradually to a lower floodplain friction value after the flood peak, but a slightly higher region for the  
21 peak flood wrack marks dataset and the time of aerial photography in the case of 95th percentile bed  
22 elevation scenario.

23 To further examine the changes in parameter spaces, the optimal friction parameter sets and their  
24 RMSEs for each scenario and each dataset are shown in Table 2. Generally, the RMSEs were the  
25 lowest for all scenarios at peak flood (wrack marks) and gradually increased when the flood receded  
26 (aerial photos and TERRASAR-X image). Applying the bed elevation changes did not improve the  
27 RMSE for both 5th and 95th percentile scenarios. The parameter sets of channel and floodplain  
28 friction for the peak flood wrack marks dataset and the time of aerial photography varied  
29 considerably. Specifically, the value of optimal floodplain friction decreased on the falling limb of  
30 the event while that of optimal channel friction appeared to have an increasing trend despite its poor  
31 sensitivity. Conversely, the optimal parameter set ( $n_{ch}$ : 0.047;  $n_{fp}$ : 0.020) for the TERRASAR-X  
32 image remained the same for all scenarios. All this suggests that the complexity of channel geometry  
33 and long-profile variability is noticeable during and shortly after the flood peak but becomes  
34 negligible when the flood further recedes. Given the significant geomorphological change in the river  
35 channel and deposition of sediments on the floodplain, the uncertainty in bed elevation changes  
36 during this extreme flood event is evident, although the effect of this uncertainty is not dominant  
37 compared to other uncertainties. This is perhaps more likely (or largely) to be due to boundary  
38 condition uncertainty than any physical change in surface roughness such as through scouring of  
39 river beds.

#### 40 4.3. Effects of bed elevation changes on prediction of flood depths

1 The similar behaviour of the RMSE performance measure and parameter spaces, despite differences  
2 in bed elevation scenarios, suggests the modifications due to bed elevation changes are not  
3 remarkable in the global friction sensitivity. However, the local dynamics of in-channel and  
4 floodplain flows, flood depth and extent may still be affected by the changes in channel geometry  
5 and long-profile variability both temporally and spatially. To investigate the influence of bed  
6 elevation changes on flood dynamics, the 50th percentile, standard deviation (SD) and coefficient of  
7 variation (CV) of inundation depth at the flood peak were computed for three scenarios. Only  
8 flooded cells were included in the calculations in order to prevent non-flood cells from skewing the  
9 results, as cells which were not flooded in some simulations would have decreased both SD and CV.  
10 The 50th percentile inundation depth at the flood peak of the no change scenario is shown in Figure  
11 8a and two subsections of the domain (Camerton in Figure 8b and Cockermouth and Papcastle in  
12 Figure 8c) are zoomed in as areas of interest for better illustration of variability (This also applies to  
13 Figure 9). The inundation depth ranged from 0.11m at the edge of the floodplain to 5.76m in the  
14 channel. However, the variations in SD were very different from the inundation depth pattern in  
15 which the channel and the surrounding floodplain both had the same variations (Figure 10a(ii)).  
16 When mean depth was taken into account using CV, it was the shallowest areas, especially at the  
17 edge of the flood, which exhibited the greatest variation in depth (Figure 11a(ii)). The no change  
18 scenario was compared with the 5th and 95th percentile bed change scenarios and the differences in  
19 inundation depth are shown in Figures 9a(i) and 9b(i) respectively. Increase in mean depth is  
20 indicated as green, decrease as red, and no change in white. Overall, the 5th percentile change  
21 scenario did not produce much change in the inundation depth of the whole reach, except for the  
22 areas (BNG 303800E 530764N) where erosion took place (See Figure 9a(ii)). For instance, the  
23 maximum decrease in floodplain water depth was 0.103m, accompanied with an increase in channel  
24 water depth of 0.469m at BNG 303935E 530690N. This implies that the effects are localised and do  
25 not propagate through the whole model in this case. The result of the 95th percentile change scenario  
26 showed a strong association of increase in channel water depth with decrease in its surrounding  
27 floodplain water depth (Figure 9b(ii) & 9b(iii)). The effects in this case, however, propagate  
28 downstream as both channel and floodplain water depth increased in the areas after the sections  
29 where channels were modified (Figure 9b(i)). This could be due to the fact that where more erosion  
30 took place in the channel it led to an increase in channel capacity, which resulted in a delay in time  
31 and a shift in location of overbank flow to the floodplain when the flood wave progressed  
32 downstream. The variations in SD and CV in the 5th percentile change scenario were similar to that  
33 of the no change scenario, excluding an average increase of 0.015m and 0.063% at BNG 303935E  
34 530690N (Figure 10b(i) & 11b(i)). The 95th percentile change scenario had a general decrease in  
35 variations in both SD and CV, except for the areas at BNG 303935E 530690N and BNG 311630E  
36 531175N where the SD (0.053m and 0.076m) and CVs (0.306% and 0.248%) remained high (Figure  
37 10c(ii) & 11c(ii)).

38 Regarding the temporal change of flood inundation area (Figure 12 left) all three scenarios followed  
39 the same pattern that the total inundation area increased to a maximum of 6.44km<sup>2</sup> at 77hours and  
40 gradually decreased after reaching the peak. The 5th and 95th percentile bed elevation scenarios  
41 simulated smaller flood inundation areas of 6.44km<sup>2</sup> and 6.39km<sup>2</sup> at the later times of 77.25hours  
42 and 78.25hours respectively. Maximum SD occurred 19.5hours and 21.25hours after the time of  
43 maximum flood inundation extent in no change and 5th percentile scenarios while that of 95th

1 percentile scenario came shortly (9.75hours) after the time of maximum flood area. Although the SD  
2 in area decreased as the flood moved downstream, the CVs continued to rise to a maximum of 1.50%,  
3 1.50%, and 0.43% and tended to stabilise as the flood wave receded. These figures suggested that the  
4 variation increased through time. However, with the consideration of bed elevation changes, the  
5 variations were smaller throughout the simulation even though all scenarios produced similar  
6 temporal patterns in total inundation area and time of maximum flood extent.

7 On the other hand, a different trend in SD and CV was observed in the mean channel and floodplain  
8 depth of flooding (Figure 12 middle & right). The greatest variation occurred during the rising limb  
9 of the hydrograph, before falling back to a relatively low level. This higher variation in depth during  
10 the rising limb than falling limb was expected because this was when flood inundation commenced.  
11 However, the variation was restricted to a shorter period of time as flood inundation occurred at a  
12 faster rate than flood recession. The maximum SDs of the mean floodplain water depth in three  
13 scenarios (0.0370m, 0.037m, and 0.009m) were smaller than that of the mean channel water depth  
14 (0.053m, 0.0543m, and 0.0135m) (Figures 12 middle b & 12 right b) but the maximum CVs of the  
15 former were double (3.172%, 3.192%, and 0.765%) than that of the latter (1.572%, 1.603%, and  
16 0.383%) (Figures 12 middle c & 12 right c). This meant that the variations in mean floodplain water  
17 depth in each scenario were larger than that of the mean channel water depth.

#### 18 4.4. Effects of bed elevation changes on flood inundation mapping

19 Deriving flood inundation maps is important for subsequent decision making for local planning or  
20 insurance industry. Accordingly, the effect of bed elevation changes on the mapping of flood  
21 inundation was assessed. Based on the RMSE analysis and Equation (2), 31 parameter sets out of  
22 300 were classified as behavioural in the no change bed elevation scenario and were used to generate  
23 the probabilistic flood inundation maps at the three observed time intervals. The same procedure was  
24 applied to the 5th and 95th percentile scenarios in which 31 and 10 parameter sets were used. The  
25 model simulated water depths were converted into a discrete binary format. Adopting the approach  
26 in previous studies (e.g. Aronica *et al.*, 2002), only cells with simulated water depths greater than  
27 0.1m were assumed to be inundated so as to reflect uncertainties in the exact shoreline location, e.g.  
28 caused by emergent vegetation. Figure 13 provides subsections from flood inundation probability  
29 maps for the time of maximum flood extent. Generally speaking, the flood margins along the whole  
30 reach had a high degree of certainty in flood extent at all three time intervals (refer to Figure 13 top  
31 for illustration). This could be due to the fact that it was a valley-fill flood event in which the flood  
32 margins were constrained by the both side of the valley, resulting in a highly certain flood boundary.  
33 Not surprisingly, the flood margins were more or less as certain as before even taking the bed  
34 elevation change scenarios into consideration (Figure 13 bottom). The flood extent of the bed change  
35 scenario produced a similar pattern and area with that of the no change scenario despite an increase  
36 of channel volume following erosion.

### 37 5. Discussion

38 In this study, the effect of bed elevation changes on flood dynamics was explored using a simplified  
39 1D-2D hydraulic model, LISFLOOD-FP, within an uncertainty analysis framework applied to  
40 modelling of the November 2009 flooding in Cockermouth, North West England. The 5th and 95th

1 percentiles bed elevation change scenarios were extracted to represent the range of possible erosion  
2 that were derived from a simple velocity based model of critical entrainment. There were numerous  
3 sources of uncertainty stemming from morphodynamic processes and from assumptions made that  
4 undermined the capability of Equation (7). Since erosion goes with deposition most of the time, on  
5 one hand these two effects partially offset one another, on the other channel instability due to  
6 braiding caused by deposition can further enhance erosion. More often the effects of deposition are  
7 far greater on channel behaviour and thus hydraulics than erosion. Neglecting deposition may result  
8 in an overestimation of erosion depths, especially in locations where dynamic geomorphic processes  
9 occurred. The model did not incorporate deposition changes, is therefore acknowledged to be a major  
10 limitation. However, the model did simulate the range of erosional channel adjustments which are  
11 typical of supply limited reaches of river networks. Although no rigorous statistical comparison  
12 between observed and estimated erosion depths could be made, the bed elevation modifications  
13 generated by Equation (7) reflected a good approximation of realistic spatial erosion pattern when  
14 compared with the observed erosion data points. 62 out of 93 pairs of observed data points were  
15 recorded as net erosion. Among them there were 23 data points fall within the 5th and 95th percentile  
16 envelopes. In other words, 37.1% was estimated within the bed change scenarios. Given the  
17 numerous factors that can cause erosion within the channel, the equation that is driven by water  
18 depth and indirectly grain size through critical velocity could still be able to capture areas of  
19 significant erosional channel changes. The approach was, therefore, good enough for an initial  
20 assessment of the erosional impact on flood modelling.

21 When evaluating the model performance, the three scenarios (no change, 5th and 95th percentiles)  
22 displayed similar friction sensitivity for channel and floodplain Manning's  $n$ . The inclusion of bed  
23 elevation changes did not improve the performance of behavioural models, however the use of the  
24 RMSE global performance measure will average out local errors, and so therefore might not be the  
25 best indicator of where the model performance has improved as a result of accounting for the  
26 uncertainty in channel morphology. The regions of behavioural friction parameter sets were  
27 reasonably different considering that the only thing being changed was erosional changes to the bed  
28 elevation. Greater changes in parameter spaces might be seen if it were two different rivers or events.  
29 Constrained by the valley sides and due to the fact that the entire valley floor acted as a single  
30 channel unit to convey the flood, the edge of the floodplain along the whole reach had a high degree  
31 of certainty in flood extent even though changes in bed elevation were considered. The flood  
32 inundation extent was thus not a sensitive measure in this case. It may be argued that larger effect of  
33 erosion on flood extent might be seen for smaller flood events as the channel capacity becomes more  
34 important when the majority of flow is still held within the channel. However, for this reach these  
35 events did no create significant morphological changes, as shown by the evidence that cross-section  
36 surveys in the post 2005 flood in the reach through Cockermouth showed minor changes in bed  
37 elevation and localised changes in bank outline when compared to those taken in 1998. In addition,  
38 since the change in flood extent is dependent on the size of the flood event due to topographic  
39 gradient, evaluation of model performance should be achieved using comparison of water surface  
40 elevations not spatial patterns of the flood (Stephens *et al.*, In press).

41 Referring to the changes in water depths within the inundation area, the uncertainty in the simulated  
42 mean depth of flooding throughout the flood event, however, had an average increase of 0.68% to



1 4.31% in 5th and 95th percentile bed change scenarios. The effects of uncertainty in bed elevation  
2 changes on flood dynamics were also observed both through time and with distance downstream.  
3 Temporally speaking, variations in mean channel and floodplain depth of flooding were greater but  
4 shorter during rising limb than falling limb. Despite its negligible change in water depth, the  
5 variations in mean floodplain water depth were larger than that of the mean channel water depth.  
6 Referring to the spatial patterns, local bed elevation changes became the principal control over where  
7 flood water initially flowed. Regions furthest away from the channel generally tended to have a  
8 higher degree of variability, areas where calculated erosion took place, however, also caused the  
9 near-channel floodplain to have greater variations in the time of initial flooding. Perhaps it would be  
10 interesting to look at the probability of localised channel breaching and its impact would have on  
11 floodplain inundation, but this is outside the scope of the data that is available as it would need to  
12 include some prior knowledge of the condition of the banks to get the probabilities of breaching  
13 remotely correct.

## 14 **6. Conclusion**

15 Overall, the inclusion of bed elevation changes appeared to alter the flood dynamics locally, and  
16 although this effect was noticeable in the global friction sensitivity, it was not significant for the  
17 flood inundation mapping. Given that the November 2009 flooding in Cockermouth was an extreme  
18 flood event with significant geomorphological changes, the effects of uncertainty in the bed elevation  
19 changes on flood dynamics were noticeable but relatively small. It is more likely that the boundary  
20 conditions or errors in observed data could have a larger impact on the model performance as well as  
21 on acceptable effective roughness values. For instance, an analysis of rating curve uncertainties  
22 could lead to an uncertainty in the input of 18-25% at peak discharge (Pappenberger *et al.*, 2006). It  
23 is highly possible that the rating curve uncertainties arising from the extrapolation of the rating curve  
24 and errors in estimating the peak discharge are even greater for this flood event. Therefore, this study  
25 has shown that hydraulic models might not need to account for within event morphodynamic  
26 changes as these can have a negligible impact compared to other uncertainties. However, the  
27 conclusions of this study are limited in that they only represent simplified and erosional cross-section  
28 changes and did not account for the significant changes in cross-section (bank erosion) and  
29 deposition. Similarly, in catchments with much larger sediment supply, changes may well include  
30 channel blocking and avulsion, neither of which were included within this model. While we  
31 conclude that morphodynamic change needs to happen over a series of events to become large  
32 enough to change the hydrodynamics of floods in the UK, given the assumptions in this study future  
33 work should be undertaken to concentrate on two areas: 1) the effects of the full range of  
34 morphological adjustments and, 2) the agglomerative changes in channel morphology resulting from  
35 flood sequences and how the uncertainties of each flood event propagate to the next; the latter  
36 becoming more significant with increased flood frequency.

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**Table 1 Summary statistics of cross-section survey**

	<b>Pre-flood survey</b>	<b>Post-flood survey</b>
Date of survey	1998 by EA	December 2009 by EA May and August 2010 by this study
No. of cross-section	234	191
Mean spacing (m)	124	151
Mean point spacing (m)	1.09	3.35
Minimum elevation (m)	4.20	3.03
Maximum elevation (m)	67.44	69.72

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**Table 2 Optimal parameter sets of channel and floodplain friction identified using RMSE for three bed elevation scenarios and for three datasets.**

	Bed Elevation Scenario	Channel Friction	Floodplain Friction	RMSE (m)
Wrack Marks	No change	0.022 – 0.042	0.044	0.2751
	5% percentile	0.067	0.045	0.2759
	95% percentile	0.067 – 0.132	0.05	0.3059
Aerial Photos	No change	0.038 – 0.135	0.029	0.4187
	5% percentile	0.036 – 0.061	0.028	0.4187
	95% percentile	0.05 – 0.067	0.038	0.4311
TERRASAR-X Image	No change	0.047	0.020	0.6303
	5% percentile	0.047	0.020	0.6281
	95% percentile	0.047	0.020	0.6084

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