

# THE COLLEGE OF AERONAUTICS CRANFIELD

On a Theory of Sandwich Construction -by-

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#### SUMMARY

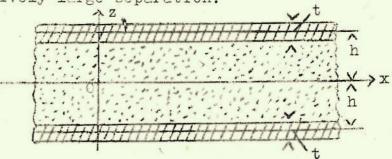
The theory of sandwich construction developed in this paper proceeds from the simple assumption that the filling has only transverse direct and shear stiffnesses, corresponding to its functional requirements (S1). This supposition permits integration of the equilibrium equations for the filling (32). The resulting integrals are used to study the compression buckling of a flat sandwich plate (§3). The formulae obtained are complex, but may be simplified in practical cases (\$4). A second approach to sandwich problems is made in \$5, where a theory of "bending" of plates is outlined. This generalises the usual theory, making allowance for flexibility in shear. This approach is applied to overall compression buckling of a plate in 36, and agreement with the previous calculations is found. This suggests the possibility of calculating buckling loads for curved sandwich shells. A simple example, the symmetrical buckling of a circular cylinder in compression is worked out in 87. The theory developed would seem applicable to all cases of buckling of not too short a wave length (\$8).

NOTE: This paper will be read at the VII International Congress of Applied Mechanics (1948).

#### 1 Assumptions

The construction of a plate built according to the principles of Sandwich Construction is shown in Fig.1.

Metal or plywood faces are glued to the surface of a low density filling. The faces are the principal load carrying agent. The function of the filling is to stabilise the faces against lateral buckling and to provide a shear connection between the faces without which the plate could not transmit bending actions. The filling may contribute to the load carrying capacity of the plate, but it is not essential that it should do so. The advantage of Sandwich Construction lies in the great flexural and torsional rigidity of plates constructed by this method. This rigidity arises from the stiffness of the faces in their planes combined with their relatively large separation.



#### Fig.1

The theory of Sandwich Construction developed in this paper proceeds from an ideal model in which the component parts fulfil their essential functions but play no other part at all. The faces are idealised as thin plates with a thickness t of isotropic material having Young's Modulus E and Poisson's ratio  $\sigma$ . The filling is assumed to extend between the middle surfaces of the faces with thickness 2h large compared with t. It will be assumed homogeneous, but anistropic, with direct stiffness at right angles to the faces and shear stiffness in planes at right angles to the faces.

Other kinds of stiffness of the filling will be taken as zero. If Cartesian axes are taken with Ox and Oy in the middle surface of the filling and Oz at right angles to the faces, the stress-strain relations for the filling can be written:-

$$X_X = 0, Y_y = 0, Z_Z = Ce_{ZZ},$$
  
 $Y_Z = Le_{yZ}, Z_X = Le_{ZX}, X_y = 0$  ... (1)

The notation for stress and strain components is that of Love's Treatise (Ref. 1). C is Young's Modulus in the Oz direction while L is the shear modulus in the Oyz and Ozx planes.

#### §2. The Displacement

The displacement in the filling can be calculated from equations (1) and the stress equations of equilibrium which can be written remembering (1) as:-

$$\frac{\partial Zx}{\partial z} = 0$$
,  $\frac{\partial Yz}{\partial z} = 0$ ,  $\frac{\partial Zx}{\partial x} + \frac{\partial Yz}{\partial y} + \frac{\partial Zz}{\partial z} = 0$  .. (2)

\_ 1 .

It follows that  $\mathbf{Z}_{\mathbf{X}}$  and  $\mathbf{Y}_{\mathbf{Z}}$  are functions of  $\mathbf{x}$  and  $\mathbf{y}$  alone, and that

$$Z_{z} = -z(\frac{\partial Z_{x}}{\partial x} + \frac{\partial Y_{z}}{\partial y}) + Z_{zo} \qquad ... \qquad (3)$$

where  $Z_{ZO}$  is  $(Z_{Z})_{Z=0}$ , a function of x and .y. Using the formulae expressing the strain components in terms of the displacement (u, v, w),

$$\frac{\partial w}{\partial z} = e_{ZZ}$$

$$\frac{\partial w}{\partial y} + \frac{\partial v}{\partial z} = e_{yZ}, \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} = e_{zX}$$

$$(4)$$

we obtain by substitution from (1) and simple integration the formulae:-

$$u = \frac{z^{3}}{\varepsilon C} \frac{\partial}{\partial x} \left( \frac{\partial^{2}x}{\partial x} + \frac{\partial^{2}z}{\partial y} \right) - \frac{z^{2}}{2C} \frac{\partial^{2}z}{\partial x} + z \left( \frac{Z_{x}}{L} - \frac{\partial w_{0}}{\partial x} \right) + u_{0} \right)$$

$$v = \frac{z^{3}}{6C} \frac{\partial}{\partial y} \left( \frac{\partial^{2}x}{\partial x} + \frac{\partial^{2}z}{\partial y} \right) - \frac{z^{2}}{2C} \frac{\partial^{2}z}{\partial y} + z \left( \frac{Y_{z}}{L} - \frac{\partial w_{0}}{\partial y} \right) + v_{0} \right) ... (5)$$

$$w = -\frac{z^{2}}{2C} \left( \frac{\partial^{2}x}{\partial x} + \frac{\partial^{2}x}{\partial y} \right) + \frac{z^{2}z}{C} + w_{0}$$

where (u<sub>0</sub>, v<sub>0</sub>, w<sub>0</sub>) is the displacement of the plane z=0. Equation (5) expresses the displacement in terms of six arbitrary functions of x and y, namely  $Z_x$ ,  $Y_z$ ,  $Z_{z0}$ , u<sub>0</sub>, v<sub>0</sub> and w<sub>0</sub>.

#### §3. Buckling in Compression

A sandwich plate, occupying the region  $-\infty < x < + \infty$ , os y so, h so z + h, is compressed in the x direction by a uniform load P per unit length. The edges y = o, b are simply supported. The plate will become unstable at a certain critical value of P. To find this value, a small displacement (u, v, w) is imposed upon the uniform compression and the examination of the possibility of equilibrium in this buckled form is carried out in the usual way. The displacement (u, v, w) is given by (5). This satisfies equilibrium conditions in the filling. The six unknown functions involved are determined by the boundary conditions at the faces.

The calculations are simplified somewhat by introducing the arcal dilatation  $\Delta$  of the faces. This is related to the applied forces per unit area  $\mathbb{Z}_X$  and  $\mathbb{Y}_Z$  by the equation

$$\nabla^2 \Delta = \pm \frac{(1 - \sigma^2)}{Et} \left( \frac{\partial Z_X}{\partial x} + \frac{\partial Y_Z}{\partial y} \right) .. \quad (6)$$

where in this, as in subsequent equations, the upper sign

refers to z = h and the lower to z = -h. From (5) it follows that

$$\Delta = \nabla^{2} \left\{ \pm \frac{h^{3}}{60} \left\{ \frac{\partial Z_{X}}{\partial x} + \frac{\partial Y_{Z}}{\partial y} \right\} - \frac{h^{2}}{20} Z_{ZO} + hw_{0} \right\}$$

$$\pm \frac{h}{L} \left( \frac{\partial Z_{X}}{\partial x} + \frac{\partial Y_{Z}}{\partial y} \right) + \left( \frac{\partial u_{0}}{\partial x} + \frac{\partial v_{0}}{\partial y} \right) \dots$$
 (7)

Substituting from (7) into (6) and adding and subtracting the resulting equations:-

$$\left\{ \begin{array}{ccc} \frac{h^{3}}{60} & \nabla^{4} & + \frac{h}{L} & \nabla^{2} - \frac{(1 - \sigma^{2})}{Et} \end{array} \right\} \left\{ \frac{\partial Z_{X}}{\partial x} + \frac{\partial Y_{Z}}{\partial y} \right\}$$

$$= h \nabla^{4} w_{O} ... (8)$$

$$\nabla^{2}(\frac{\partial u_{0}}{\partial x} + \frac{\partial v_{0}}{\partial y}) = \frac{h^{2}}{2C} \nabla^{4} z_{z_{0}} \qquad (9)$$

The remaining condition of equilibrium at the faces is that of balance of normal forces. Here the effects of the initial compression P must be introduced as well as the external force  $\mathbf{Z}_{\mathbf{Z}}.$  The resulting equations are:-

$$(\mathbb{D}\nabla^4 + \frac{\mathbb{P}}{\mathbb{Z}} \frac{2^2}{2^{\times 2}}) (w)_{z=\pm h} \pm (\mathbb{Z}_z)_{z=\pm h} = 0 \qquad .. \quad (10)$$

where 
$$D = \frac{Et^3}{12(1-5^2)}$$
 .... (11)

Substituting from (3) and (5) into (10) and again adding and subtracting the resulting equations:-

$$(D\nabla^4 : \frac{P}{2} \frac{\partial^2}{\partial x^2} + \frac{C}{h}) Z_{zo} = 0 \qquad ... \qquad (13)$$

Equations (8), (9), (12) and (13) involve only the four unknowns

$$\frac{\partial Z_x}{\partial x} + \frac{\partial Y_z}{\partial y}$$
,  $Z_{zo}$ ,  $\frac{\partial u_0}{\partial x} + \frac{\partial v_0}{\partial y}$  and  $w_0$ 

This relative simplicity is due to the use of  $\triangle$ . The calculation of critical loads is unaffected by this artifice. The equations fall into two sets. Equations (8)

and (12) involve only  $\frac{\partial Z_x}{\partial x} + \frac{\partial Y_z}{\partial y}$  and  $w_0$ , while equations (9) and (13) involve  $Z_{z0}$  and  $\frac{\partial u_0}{\partial x} + \frac{\partial v_0}{\partial y}$ .

There are thus two distinct types of buckling:-

- (a) Symmetric. Here  $\frac{\partial Z_X}{\partial x} + \frac{\partial Y_Z}{\partial y} = w_0 = 0$  and so w is an odd function of z. The critical loads follow from (13).
- (b) Anti-symmetric. Here  $Z_{ZO} = \frac{\partial u_O}{\partial x} + \frac{\partial v_O}{\partial y} = 0$  and w is an even function of z. The critical loads follow from (8) and (12) which yield when  $\frac{\partial Z_X}{\partial x} + \frac{\partial Y_Z}{\partial y}$  is eliminated:-

$$-\frac{hP}{2L} \frac{\partial^{2}}{\partial x^{2}} \nabla^{2} + \frac{(1-\sigma^{2})P}{2Et} \frac{\partial^{2}}{\partial x^{2}} \qquad w_{0} = 0 .. (14)$$

The critical values of P follow from (13) and (14) by assuming that w and hence  $Z_{ZO}$  and  $W_{O}$ , vary as  $\sin \frac{\pi_{X}}{\lambda} \sin \frac{\pi_{Y}}{b}$ , where  $\lambda$  is the, as yet unknown, half-wave length. The formulae are:-

Type (a) 
$$P = \frac{2\pi^2 D}{b^2} \left(\frac{b}{\lambda} + \frac{\lambda}{b}\right)^2 + \frac{2b^2 C}{\pi^2 c} \left(\frac{\lambda}{b}\right)^2 \qquad \dots \qquad (3.5)$$

Type (b)
$$P = \frac{2 \pi^2 \text{Eth}^2}{(1 - \sigma^2)b^2} \left( \frac{b}{\lambda} + \frac{\lambda}{b} \right)^2 \left\{ \frac{1 + \frac{D(1 - \sigma^2)}{\text{Eth}^2} + \frac{\pi^2 D}{\text{Lhb}^2} (1 + \frac{b^2}{\lambda^2}) + \frac{\pi^4 \text{hD}}{3\text{Cb}^4} (1 + \frac{b^2}{\lambda^2})^2}{\left(1 + \frac{\pi^2 \text{Eth}}{\text{Lb}^2 (1 - \sigma^2)} (1 + \frac{b^2}{\lambda^2}) + \frac{\pi^4 \text{Eth}^3}{3\text{Cb}^4 (1 - \sigma^2)} (1 + \frac{b^2}{\lambda^2})^2} \right\} \dots (16)$$

#### §4. Discussion of the Buckling Formulae

The value of the smallest critical load follows from (15) and (16) by chosing  $\lambda$  to make P a minimum. This is easy in the case of symmetrical buckling and yields

In practice  ${}^{b^4C}/_{\pi^4hD} >> 1$  and so

$$\lambda = \pi ({}^{hD}/_{C})^{\frac{1}{4}}$$
 .... (18)

which shows that symmetric buckling occurs in short wavelengths of the order of the sandwich thickness 2h\*\*. The corresponding critical load is given by:-

$$P_{\text{crit}} = 4(\frac{CD}{h})^{\frac{1}{2}}$$
 .... (19)

The formula (16) for anti-symmetrical buckling is much more difficult to interpret. If the filling is so rigid that the effects of C and L can be disregarded, the problem reduces to that of an ordinary plate and so for minimum P, which will be written  $P_{\mathbb{R}}$ , the condition is  $\lambda = b$ . This gives

$$P_{\rm E} = \frac{8 \, \pi^2 E th^2}{(1 - \sigma^2) b^2} \qquad . \qquad . \qquad . \qquad (20)$$

Now so long as  $\lambda$  is of the same order as b, inspection of (16) shows that of the various terms of the correcting fraction only the unities and the term involving L in the denominator need be retained. Under these conditions equation (16) can be written

$$P/P_{E} = \frac{1}{4} (\frac{b}{\lambda} + \frac{\lambda}{b})^{2} / \left\{ 1 + \frac{P_{E}}{4P_{S}} (1 + \frac{b^{2}}{\lambda^{2}}) \right\} ... (21)$$

where, 
$$P_{S} = 2hL$$
 .... (22)

The minimum value of P occurs when

and this yields for Perit the formula

$$\frac{1}{P_{\text{crit}}} = \frac{1}{P_{\text{E}}} + \frac{1}{2P_{\text{S}}} + \frac{P_{\text{E}}}{16P_{\text{g}}2} \dots \dots (24)$$

where  $P_{\rm E}$  is now the Euler load per unit length.

<sup>\*\*</sup>  $\lambda_h$  is proportional to  $(Et^3/_{ch}3)^{\frac{1}{4}}$  which in practice is of the order of unity.

The relation (16) gives a further minimum value of Nhen  $\lambda/b <<$  1. Expansion in powers of  $\lambda/b$  up to gives a formula with a minimum at

The corresponding critical value of P is:-

Comparison with equation (19) shows that the critical load for anti-symmetrical wrinkling is larger than that for the symmetrical variety.

#### \$5. Bending

The problem of the overall buckling of a sandwich panel may be approached via a theory of bending of sandwich plates. This may be developed from the displacement formulae (5) by taking that part of the displacement which is antisymmetric about z=0. The displacement at the face z=h, written (u', v', w'), is then given by

$$u' = \frac{h^{3}}{60} \frac{\partial}{\partial x} \left( \frac{\partial Z_{x}}{\partial x} + \frac{\partial Y_{z}}{\partial y} \right) + h\left( \frac{Z_{x}}{L} - \frac{\partial w_{0}}{\partial x} \right)$$

$$v' = \frac{h^{3}}{60} \frac{\partial}{\partial y} \left( \frac{\partial Z_{x}}{\partial x} + \frac{\partial Y_{z}}{\partial y} \right) + h\left( \frac{Y_{z}}{L} - \frac{\partial w_{0}}{\partial y} \right)$$

$$w' = \frac{-h^{2}}{20} \left( \frac{\partial Z_{x}}{\partial x} + \frac{\partial Y_{z}}{\partial y} \right) + w_{0}$$

$$(28)$$

The stress resultants  $T_1'$ ,  $T_2'$  and S' in the face z = h are given by

$$T_{1}' = \frac{Et}{(1-\sigma^{2})} \left( \frac{\partial u'}{\partial x} + \sigma \frac{\partial v'}{\partial y} \right)$$

$$T_{2}' = \frac{Et}{(1-\sigma^{2})} \left( \frac{\partial v'}{\partial y} + \sigma \frac{\partial u'}{\partial x} \right)$$

$$S' = \frac{Et}{2(1+\sigma)} \left( \frac{\partial v'}{\partial x} + \frac{\partial u'}{\partial y} \right)$$

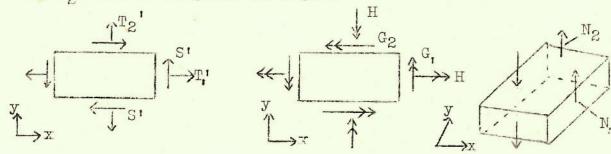
$$(29)$$

Neglecting the contribution from the bending of the faces, the formulae for the normal stress resultants N, and N<sub>2</sub> and the stress couples G, G, and H for the sandwich plate as a whole can be written:-

$$N_1 = 2hZ_X$$
,  $N_2 = 2hY_Z$  ... (30)

$$G_1 = 2hT_1', G_2 = 2hT_2', H = -2hS' ... (31)$$

The sign convention for the quantities  $T_1$ ,  $T_2$ ,  $S_1$ ,  $N_1$ ,  $N_2$ ,  $G_1$ ,  $G_2$  and H is given in Fig.2.



Face z = h

Sandwich as a whole

#### Fig. 2

The quantities  $Z_{x}$  and  $Y_{z}$  may be eliminated using (30). Relations between  $G_{t}$ ,  $G_{2}$ , and H and the normal displacement of the middle surface  $w_{0}$  can be obtained by substituting from (28) into (29) and thence into (31). The result may be written:

$$G_{1} = -D_{1} \left\{ K_{1} + \sigma K_{2} - \frac{1}{2hL} \left( \frac{\partial N_{1}}{\partial x} + \sigma \frac{\partial N_{2}}{\partial y} \right) + \frac{h}{12C} \left( \frac{\partial^{2} p}{\partial x^{2}} + \sigma \frac{\partial^{2} p}{\partial y^{2}} \right) \right\}$$

$$G_{2} = -D_{1} \left\{ K_{2} + \sigma K_{1} - \frac{1}{2hL} \left( \frac{\partial Ng}{\partial y} + \sigma \frac{\partial N_{1}}{\partial x} \right) + \frac{h}{12C} \left( \frac{\partial^{2} p}{\partial y^{2}} + \sigma \frac{\partial^{2} p}{\partial x^{2}} \right) \right\}$$

$$H = D_{1} \left( 1 - \sigma \right) \left\{ \Upsilon - \frac{1}{4hL} \left( \frac{\partial Ng}{\partial x} + \frac{\partial N_{1}}{\partial y} \right) + \frac{h}{12C} \frac{\partial^{2} p}{\partial x \partial y} \right\}$$

$$Where \qquad D_{1} = \frac{2E th^{2}}{(1 - \sigma^{2})} \qquad ... \qquad (33)$$

$$K_1 = \frac{\partial^2 w_0}{\partial x^2}, \quad K_2 = \frac{\partial^2 w_0}{\partial y^2}, \quad T = \frac{\partial^2 w_0}{\partial x \partial y} \quad ... \quad (34)$$

and p is the transverse load per unit area of the plate, which is given by equation (35) below. Equations (32) generalise the usual bending moment - curvature relations to allow for flexibility of the filling in shear and transverse tension and compression. In practice the terms in p are usually small and may therefore be omitted.

The theory of the bending of sandwich plates is completed by the usual equilibrium equations:-

$$\frac{\partial N_1}{\partial x} + \frac{\partial N_2}{\partial y} + p = 0$$

$$\frac{\partial G_1}{\partial x} - \frac{\partial H}{\partial y} - N_1 = 0$$

$$\frac{\partial H}{\partial x} + \frac{\partial G_2}{\partial y} - N_2 = 0$$
(35)

#### \$6. Alternative Calculation of Overall Compression Buckling

A calculation of the buckling load for compression buckling with half-wave length  $\lambda$  of the order of b can be based upon the bending theory of §5. Allowance for the initial compression p is made by writing

$$p = -P \frac{\partial^2 w_0}{\partial x^2} \qquad \dots \qquad (36)$$

The equations (32) and (35) are solved by writing

$$w_{0} = W \sin \frac{\pi_{X}}{\lambda} \sin \frac{\pi_{Y}}{b}$$

$$N_{1} = n_{1} \cos \frac{\pi_{X}}{\lambda} \sin \frac{\pi_{Y}}{b}$$

$$N_{2} = n_{2} \sin \frac{\pi_{X}}{\lambda} \cos \frac{\pi_{Y}}{b}$$

$$G_{1} = g_{1} \sin \frac{\pi_{X}}{\lambda} \sin \frac{\pi_{Y}}{b}$$

$$G_{2} = g_{2} \sin \frac{\pi_{X}}{\lambda} \sin \frac{\pi_{Y}}{b}$$

$$H = h_{1} \cos \frac{\pi_{X}}{\lambda} \cos \frac{\pi_{Y}}{b}$$

$$(37)$$

where  $W_1$ ,  $n_1$ ,  $n_2$ ,  $g_1$ ,  $g_2$ , and  $h_1$  are constants. Substitution from (37) and the elimination of these constants yields the following formula for P:-

$$P = \frac{\pi^{2}D_{1}}{b^{2}} \left\{ \frac{b}{\lambda} + \frac{\lambda}{b} \right\}^{2} \left\{ 1 + \frac{\pi^{2}D_{1}}{2hLb^{2}} \left\{ 1 + \frac{b^{2}}{\lambda^{2}} \right\} \right\} \qquad (38)$$

It is to be remarked that the terms in p in (32) have been omitted. Inspection of (33) and (20) shows that equation (38) is identical with equation (21). The approach via the bending theory of 35 yields the same result for overall buckling as the more exact calculations of \$3. This suggests the possible application of the formulae (32) to more difficult problems, such as those of the buckling of curved shells.

## 87. Symmetrical Buckling of a Circular Cylinder in Compression

The application of the formulae (32) to problems of curved shells may be exemplified by the simple case of the buckling of a circular cylinder in a symmetric mode. The assumed cross-sectional deformation is shown in Fig. 3. "w" the radial displacement is a function of x the distance along the axis of the cylinder. The hoop tensile strain  $\xi_2$ 

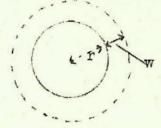


Fig. 3

is w/r. Assuming no change in direct stress parallel to the axis, it follows that the x-wise strain  $\mathcal{E}$ , has the value  $-\sigma w$ .

The hoop tension T2 is then given by

$$T_{2} = \frac{2Et}{(1 - \sigma^{2})} (\boldsymbol{\xi}_{2} + \boldsymbol{\sigma}\boldsymbol{\xi}_{1}) = 2Et_{\underline{\mathbf{r}}}^{\underline{\mathbf{w}}} \dots \dots \dots \dots (39)$$

The equations of equilibrium are: -

$$\frac{\partial N_{1}}{\partial x} - \frac{T_{2}}{r} + p = 0$$

$$\frac{\partial G_{1}}{\partial x} - N_{1} = 0$$

$$(40)$$

where N, and G, are the shear and bending moment. The pressure p arises from the initial compression P and is given by:-

Finally the bending moment - curvature relation follows from (32):-

$$G_{1} = -D_{1} \left( \frac{\partial^{2} w}{\partial x^{2}} - \frac{1}{2hL} \frac{\partial N_{1}}{\partial x} \right) \qquad (42)$$

Elimination of  $T_2$ ,  $N_1$ , p and  $G_1$  from (39), (40), (41) and (42) yields:-

$$\left(1 - \frac{D_1}{2hL} \frac{\partial^2}{\partial x^2}\right) \left(P \frac{\partial^2 w}{\partial x^2} + \frac{2Et}{r^2} w\right) + D_1 \frac{\partial^4 w}{\partial x^4} = 0 .. \quad (43)$$

The critical load is obtained from (43) by assuming w proportional to  $\sin \pi x/\lambda$ . This yields the result:-

$$\mathbb{P}/\mathbb{P}_{\mathbb{E}} = \left\{ \left( \frac{\lambda \mathbb{E}}{\lambda} \right)^{2} + \left( \frac{\lambda}{\lambda \mathbb{E}} \right)^{2} + \frac{1}{2} \frac{\mathbb{P}_{\mathbb{E}}}{\mathbb{P}_{S}} \right\} / \left\{ 2 + \frac{\mathbb{P}_{\mathbb{E}}}{\mathbb{P}_{S}} \left( \frac{\lambda \mathbb{E}}{\lambda} \right)^{2} \right\} \dots (44)$$

where, 
$$P_{E} = \frac{2}{r} (2EtD_{t})^{\frac{1}{2}}$$
)
$$\lambda_{E} = \pi (\frac{D_{t}r^{2}}{2Et})^{\frac{1}{4}}$$
) .... (45)

 $P_{\rm E}$  and  $\lambda_{\rm E}$  are the buckling load and half-wave length for the case where shear flexibility of the filling is small.  $P_{\rm S}$  is given by (22). The minimum value of P in equation (44) occurs when

$$\left(\frac{\lambda}{\lambda_{\rm E}}\right)^2 = 1 - \frac{1}{2} \frac{P_{\rm E}}{P_{\rm S}}$$
 .... (46)

This gives for Pcrit the formula:-

0

Equation (47) is valid so long as (46) yields a wave length sufficiently long to justify the use of the bending theory of §5. For practical application  $P_{\rm E} < \frac{3}{2} P_{\rm S}$  would seem quite a reasonable limitation.

### S8. The Field of Application of the Theory

The type of construction to which the theory of this paper is directly applicable is that class of sandwich in which the filling consists of resin impregnated paper honeycomb. In this case the stiffnesses of the filling conform almost exactly to the equations (1). The formulae for the buckling loads (19), (24) and (47) would seem then to be appropriate to this type of construction.

The formula (19) which covers the case of wrinkling will certainly not apply to other kinds of filling, whose comprehensive elastic properties induce a dying away of surface waves at points distant from the surface and so lead to a buckling formula which is approximately independent of the filling thickness \*\*. On the other hand the formulae (24) and (47) which apply to overall buckling in wave lengths large compared with the plate thickness may reasonably be expected to apply to all practical fillings.

#### References

- 1. "The Mathematical Theory of Elasticity". Love.
- 2. "Theory of Elastic Stability". Timoshenko.
- 3. "Instability of Sandwich Struts and Beams". H.L. Cox. (R & M.2125)

<sup>\*\*</sup> See Reference 3.