

1 **METHODOLOGY ARTICLE** 12
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4 **Consistency of biological networks inferred from** 4
5
6 **microarray and sequencing data** 6
78 Veronica Vinciotti^{1*}, Ernst C. Wit², Rick Jansen³, Eco J.C.N. de Geus³, Brenda W.J.H. Penninx³, Dorret⁸
9 I. Boomsma³ and Peter A.C. 't Hoen⁴ 910
11 **Abstract** 1112
13 **Background:** Sparse Gaussian graphical models are popular for inferring biological networks, such as gene 13
14 regulatory networks. In this paper, we investigate the consistency of these models across different data 14
15 platforms, such as microarray and next generation sequencing, on the basis of a rich dataset containing 15
16 samples that are profiled under both techniques as well as a large set of independent samples. 1617
18 **Results:** Our analysis shows that individual node variances can have a remarkable effect on the connectivity of 17
19 the resulting network. Their inconsistency across platforms and the fact that the variability level of a node may 18
20 not be linked to its regulatory role mean that, failing to scale the data prior to the network analysis, leads to 19
21 networks that are not reproducible across different platforms and that may be misleading. Moreover, we show 20
22 how the reproducibility of networks across different platforms is significantly higher if networks are summarised 21
23 in terms of enrichment amongst functional groups of interest, such as pathways, rather than at the level of 22
24 individual edges. 2324
25 **Conclusions:** Careful pre-processing of transcriptional data and summaries of networks beyond individual edges 24
26 can improve the consistency of network inference across platforms. However, caution is needed at this stage in 25
27 the (over)interpretation of gene regulatory networks inferred from biological data. 2627
28 **Keywords:** Gaussian graphical models; gene regulatory network; microarray; next-generation sequencing 2829
30 **Introduction** 3031 One important direction in systems biology is to dis- 30
32 cover gene regulatory networks from transcriptional 31
33 data based on the observed mRNA levels of a large 32
34 number of genes. The nodes of the network are genes 33
35 and the edges are the corresponding interactions, such 34
36 as activation, repression or translation. Transcrip- 3536 tional data can be generated using two different high- 30
37 throughput technologies: gene expression microarrays³¹
38 [18] and tag-based sequencing methods, like Deep- 32
39 SAGE [12, 21] and RNA-seq [19]. 3334 Statistical models have been proposed in the lit- 34
35 erature for reverse engineering networks from data³⁵
36 and different adaptations have been developed to deal³⁶
37 with the high dimensionality and complexity of bi- 37
38 ological networks in particular, e.g. [8, 15, 22, 31].³⁸
39 Amongst these approaches, Gaussian graphical mod- 3937
38 *Correspondence: veronica.vinciotti@brunel.ac.uk38
39 ¹Department of Mathematics, Brunel University London, London, UK39
Full list of author information is available at the end of the article

els have shown to be particularly popular. The computationally efficient method introduced by [8] allowed the estimation of these models for the case of a large number of nodes relative to the sample size ($p \gg n$) via the use of an L_1 penalised likelihood approach. This approach is suited to microarray data, as the data are continuous and, after normalization, well approximated by a multivariate normal distribution. A number of papers have extended the original model to different cases, such as dynamic networks from microarray data [1], hub-type networks from microarray data [31], condition-specific networks from microarray data [7] and networks from next generation sequencing data, which are discrete, e.g. [4, 36].

After the advent of next generation sequencing technologies, a number of studies have evaluated the consistency between the two platforms, both at the level of expression values and at the level of differentially expressed genes, e.g. [12, 27, 30, 33, 37]. The general conclusion from these studies is that sequencing technologies not only allow to identify transcripts that have not been previously annotated, but they also allow to better quantify very low and very high expression transcripts, which would be masked by microarray's background noise and saturation effects, respectively. In the intermediate range, there is high replication and detection amongst the two platforms, although platform specific and dataset-specific effects can limit the level of consistency significantly [27]. A small number of studies has gone beyond expression and differential expression. In particular, [29] studied the consistency of clustering methods on microarray and RNA-seq data and [11] studied the consistency of co-expression networks on microarray and RNA-seq data, where the networks are inferred by Pearson correlation values.

Linked to the work of [11], the aim of this paper is to quantify the consistency, across platforms and samples, of biological networks inferred by sparse Gaussian

graphical models. We consider a rich dataset containing samples that are profiled under both microarray and sequencing techniques as well as a large set of independent samples [39]. We assess the consistency of networks both at the level of individual edges and at the level of enrichment among pathways extracted from the Kyoto Encyclopedia of Genes and Genomes (KEGG) database (<http://www.genome.jp/kegg>). For the latter, we make use of a recently developed test for network enrichment [28].

Method

Data

The data used in this study contain DeepSAGE (DS) sequencing of 21bp tags and corresponding Affymetrix expression data from total blood RNA samples from unrelated individuals from the Netherlands Twin Register (NTR) [5] and the Netherlands Study of Depression and Anxiety (NESDA) [24]. From the NTR/NESDA cohorts, we selected healthy (and thus non-diabetic) individuals at the extremes of the fasting glucose serum level distribution: 41 individuals with fasting glucose concentrations ≤ 4.8 mmol/l; 53 individuals with fasting glucose concentrations ≥ 5.9 mmol/l. This selection comprised 28 males and 66 female individuals. Microarray and DeepSAGE data generation, processing and quality control have been described previously [13, 35, 39]. In addition, we used Affymetrix-profiled blood samples of 1272 additional participants of the NTR and NESDA studies, selected using the same glucose based criterion as above. In particular, of these there are 418 high glucose and 854 low glucose samples. We later refer to the three datasets as DS (the 94 DeepSAGE samples), MA(DS) (the 94 corresponding microarray samples) and MA(Add) (the 1272 additional microarray samples). Together with gene expression data, a number of corresponding covariates are used: age (in years), sex, Body Mass Index (BMI), glucose level and smoking (yes and no). These

1 were obtained during the interview at the time of blood
 2 draw. Glucose was measured in blood plasma using the
 3 Vitros 250 glucose assay (Johnson and Johnson). The
 4 DS samples are corrected for GC content.

5 For the analysis, we select the 1500 most highly ex-
 6 pressed genes for which there are concept profiles, i.e.
 7 for which there is information in the literature in at
 8 least 5 papers. This group of genes is expected to be
 9 least affected by observational noise in their expres-
 10 sion measurements and, therefore, to be most consis-
 11 tent across platforms. This aids in focussing on the
 12 actual contribution of network modelling to the con-
 13 sistency across platforms, which is the focus of this
 14 paper. From these 1500 genes, we select 1435 genes
 15 that are common to both DS and microarray data.
 16 For microarray data, we take the average expression
 17 of all probes targeting the same gene. Figure 1 (left)
 18 shows the correspondence between count data and ex-
 19 pression data for the 1435 genes, averaged over the
 20 94 samples. The correlation between the two is 0.49,
 21 suggesting a moderate reproducibility across the two
 22 platforms at the level of expression data. The right
 23 plot shows a very high reproducibility for the microar-
 24 ray experiments between the 94 samples and the 1272
 25 independent samples.

27 Sparse Gaussian graphical models

28 In this paper, we use Gaussian graphical models for
 29 inferring networks from data. A Gaussian graphical
 30 model makes the assumption that the vector of nodes
 31 D follows a multivariate Gaussian distribution, so

$$32 \quad D \sim N(\mu, \Sigma),$$

33 with mean vector μ and variance-covariance matrix Σ .

34 Of particular importance is the inverse of the variance-
 35 covariance matrix, also called precision or concentra-
 36 tion matrix, which is usually denoted by

$$37 \quad \Theta = (\theta_{ij}) = \Sigma^{-1}.$$

This matrix holds a special role in Gaussian graphical
 models: in fact, zeros in the precision matrix corre-
 spond to conditional independence between the corre-
 sponding variables, i.e. the absence of an edge in the
 corresponding graph. In particular, there is a direct
 link between the precision value θ_{ij} and the partial
 correlation ρ_{ij} between D_i and D_j conditioning on all
 other nodes, as

$$38 \quad \rho_{ij} = -\frac{\theta_{ij}}{\sqrt{\theta_{ii}\theta_{jj}}}. \quad (1)$$

39 Thus inferring the network of interactions can be re-
 40 casted into the problem of estimating the precision
 41 matrix Θ and extracting its zero structure. Of par-
 42 ticular importance for the analysis in this paper is
 43 the fact that the diagonal of the matrix Θ is given
 44 by the inverse of the conditional variances, i.e. $\theta_{ii} =$
 $\frac{1}{\text{var}(D_i|D_j, j \neq i)}$ [34]. Thus, the scale of individual
 nodes can play a significant role in the dependency
 structure.

45 In the case of high-dimensional networks, that is
 46 where the sample size n (number of experiments) is
 47 smaller than the number of nodes p (number of genes),
 48 a sparse estimate of the precision matrix Θ can be ob-
 49 tained by imposing an L_1 -penalty constraint on the
 50 entries of the precision matrix. This results in the pe-
 51 nalisised likelihood optimization

$$52 \quad \max_{\Theta} [\log |\Theta| - \text{Trace}(S\Theta) - \lambda \|\Theta\|_1],$$

53 with S the sample covariance matrix and λ the penalty
 54 parameter controlling sparsity. [8] provide an efficient
 55 optimization procedure for this problem, by maximis-
 56 ing the penalised log-likelihood iteratively for each
 57 node and, at each step, by re-writing the problem into
 58 an equivalent lasso regression problem. The latter is es-
 59 timated efficiently using coordinate descent methods.

¹Network Inference

²We adopt a Poisson regression model for the Deep-
³SAGE data to correct for spurious confounders in mea-
⁴suring the interaction between the genes. Let $Y_i =$
⁵ (Y_{i1}, \dots, Y_{ip}) be the count data for gene i under p ex-
⁶periments. Let $X = (X_1, \dots, X_c)$ be a vector of covari-
⁷ates. Then

$$\begin{aligned}
 & Y_{ij} \sim \text{Poisson}(\lambda_{ij}) \\
 & \log(\lambda_{ij}) = \log(n_j) + \sum_{c=1}^C x_{jc}^T \beta_{ic},
 \end{aligned}$$

¹²with n_j the total number of counts in experiment j ,
¹³ $x_j = (x_{j1}, \dots, x_{jC})$ the vector of covariates for sample
¹⁴(experiment) j and β_i the vector of parameters for gene
¹⁵ i . For microarray data, a multiple regression model
¹⁶is used to correct for the same covariates, with the
¹⁷exception of GC content and total number of counts
¹⁸which are specific to count data.

¹⁹We then extract the residuals of the regression mod-
²⁰els. For the Poisson regression, we take the deviance
²¹residuals defined by

$$d_{ij} = \text{sign}(y_{ij} - \hat{\lambda}_{ij}) \sqrt{2y_{ij} \log \frac{y_{ij}}{\hat{\lambda}_{ij}} - 2(y_{ij} - \hat{\lambda}_{ij})}.$$

²⁵These are approximately normally distributed [20] and
²⁶are used for network modelling.

²⁷This two-step method does not take into account the
²⁸uncertainty of the regression estimates and could, es-
²⁹pecially when the number of samples is similar to the
³⁰number of regressors, lead to biased estimates. We ac-
³¹count for this uncertainty by non-parametrically boot-
³²strapping the data and repeating the analyses on the
³³bootstrap samples. This provides typically asymmet-
³⁴ric confidence intervals of the quantities of interest that
³⁵will account both for the bias and the under-estimated
³⁶variance of the original two-step estimation procedure.

³⁷In order to assess the impact of individual node
³⁸variances and of correction for confounding effects on
³⁹the resulting inferred network and on the consistency

of network models across different samples and plat-
forms, we fit sparse Gaussian graphical models in the
following three cases:

- ⁴1 Residuals standardised to have mean zero and
⁵variance one per node.
- ⁶2 Residuals not standardised.
- ⁷3 Normalised expression data standardised to have
⁸mean zero and variance one but not corrected for
⁹confounding effects.

For the first and the third case, we use the package
huge [38], which automatically scales the data prior to
network inference. In terms of the choice of the penalty
parameter λ , we select this based on the rotation infor-
mation criterion (`ric`) approach, which is available in
the R function `huge.select`. We take the optimal net-
work for the case of standardised residuals from the 94
DS samples. This returns a network with 1435 nodes
and 29865 edges. We then select λ for all other net-
works in such a way that all networks in the compar-
ative study are of similar size. For the second case,
we use the function `glasso` in the package `glasso` [9],
which does not automatically scale the data.

Given the estimated networks, the test developed by
[28], and implemented in the R package `neat`, is used
to detect enrichment of the networks among KEGG
pathways. In particular, the test detects whether the
number of edges between two pathways in the inferred
network is larger than what is expected by chance. For
this, we download all human KEGG pathways using
the R package `KEGGREST` [32]. Out of the total 299
pathways, we filter 62 pathways as those that contain
at least 20 of the selected genes and test for enrich-
ment amongst any pair of pathways. Finally, we rank
the p-values and build a network with 62 nodes (the
pathways) and with edges corresponding to the top
enrichments.

Throughout the analysis, the agreement between any
two networks is measured using the product-moment

¹correlation between the corresponding adjacency ma-
²trices. This is implemented in the function `gcor` of
³the R package `sna`. The function `qaptest` in the same
⁴package is used to compute the p-values under a re-
⁵labelling of the nodes of the network.

⁶

⁷

⁸Results and Discussion

⁹The Confounders Effect

¹⁰In a first set of experiments, we evaluate the impact
¹¹of confounders on network inference and thus justify
¹²the choice of performing the network modelling on the
¹³residuals. In order to do this, we fit networks under
¹⁴two cases. In the first case the data are scaled but not
¹⁵corrected for confounders (with the exception of GC
¹⁶and number of experiments for DS data). In the second
¹⁷case, the data are scaled and corrected for confounders
¹⁸as explained before.

¹⁹ The results on our data show a high correlation
²⁰between the networks in the two cases, with 95%
²¹bootstrapped confidence intervals (0.56, 0.94) for DS,
²²(0.68, 0.75) for MA(DS) and (0.95, 0.98) for MA(Add).
²³The agreement is particularly high in the MA(Add)
²⁴case due to the larger sample size. However, looking at
²⁵the difference between the two networks for each of the
²⁶three datasets, we can see how genuine regulatory in-
²⁷teractions, when one transcript directly regulates the
²⁸expression of another transcript, may be masked by
²⁹confounding effects. Figure 2 shows two examples of
³⁰edges that are found in the MA(DS) network when not
³¹correcting for confounders but they are not found when
³²correcting for confounders. In general, any two differ-
³³entially expressed genes may be highly correlated, but
³⁴they may not be directly interacting, i.e. this may be a
³⁵spurious correlation caused by a third factor. One way
³⁶of distinguishing between direct and indirect interac-
³⁷tions is by correcting for confounders: if the correlation
³⁸is still at the the level of residuals (i.e. partial correla-
³⁹tion), then it may be a sign of a genuine relationship.

In conclusion, regulatory interactions between genes¹
 may be masked by confounders effects. Although their²
 effect in the network reconstruction is found to be³
 small for our particularly study, performing this step⁴
 increases the chances of detecting genuine regulatory⁵
 mechanisms. For the remaining of the paper, we there-⁶
 fore fit networks to the residuals, after correcting for⁷
 the confounders mentioned in the description of the⁸
 data.

⁹

¹⁰

¹¹The Node Variance Effect

The fact that the variance of a node has an impact on¹²
 the dependency structure is natural for models that are¹³
 based on estimating the inverse of covariances, as ex-¹⁴
 plained in the description of Gaussian graphical mod-¹⁵
 els. Due to computational stability of the estimation¹⁶
 procedure, in most cases the variables are standard-¹⁷
 ized prior to the estimation of the dependency struc-¹⁸
 ture. However, this is not always included in the im-¹⁹
 plementations that are made available. For example,²⁰
 the original implementation of sparse Gaussian graph-²¹
 ical models in the `glasso` package [9] does not auto-²²
 matically standardize the variables. Of 44 citations of²³
 the package in Google scholar, we found that 14 use²⁴
`glasso` for inferring biological networks, and only 3²⁵
 of these make explicit mentioning to standardization²⁶
 of the data. This is the same for JGL [6], where the²⁷
 variables are only centralised per condition, and for²⁸
`SparseTSCGM` [2], where the variables are not standard-²⁹
 ized. Amongst other implementations of sparse Gaus-³⁰
 sian graphical models, `huge` [38] automatically scales³¹
 the data, and similarly, the function `sugm` in the `flare`³²
 R package [16] is based on estimation of the inverse of³³
 the correlation matrix and, thus, is scale independent.³⁴
 These are only few examples of the most popular im-³⁵
 plementations. In general, the decision as to whether³⁶
 to scale the data or not is not always done automati-³⁷
 cally by the software, so it is important to appreciate³⁸
 the impact of this choice on the resulting network and³⁹

the implications when interpreting the network for biological findings.

Figure 3 plots the connectivity of each node versus its variance (both in the log scale) for the networks inferred from non-scaled data (case 2). Figure 3 (a) is for the case of DS data, whereas (b) is for the case of MA(DS) data. A similar relationship exists for the MA(Add) data. The plots show how the connectivity of a node is strongly linked with its variance. The panel (c) of the figure shows how the variance of a node is not consistent across platforms. Thus the conclusion is that the networks inferred in this analysis from non-scaled data will mainly reflect measurement scale and platform specific effects rather than biological effects.

In addition, Figure 4 shows how the residuals with the largest variances tend to correspond to the highly expressed genes. Looking at the list of these genes, we find various markers for cellular composition. In particular, as the data come from blood samples, many of the highly expressed genes are related to blood markers, e.g. HBB is the gene with the highest variance and is the most connected gene of the DS network (1307 edges), whereas HLA-C is the highest connected gene in the MA(DS) network (811 edges). Markers for cellular composition are in general not expected to have also a regulatory role, thus the network on non-scaled data may show features that, in some cases, may be consistent across platform but they may not necessarily be linked to regulation.

In general, the connectivity of a network inferred from non-scaled data is strongly influenced by the individual node variances. As shown by Figure 5, the network on non-scaled data has a very pronounced right tail, i.e. a small number of highly connected nodes (hubs), whereas the network on scaled data has a more uniform level of connectivity. The plots show how the effect is more pronounced for the DS than for the MA(DS) network, as in count data the variance

scales with the mean and there is therefore a larger variability in node variances.

If networks on non-scaled data exhibit a gene variance effect and if the measurement scales are not consistent across platforms, then one would expect a lower consistency of networks across samples and platforms if the data are not standardized. Table 1 shows the correlations of networks across different samples and platforms, distinguishing the case of scaled and not-scaled data. The correlation between adjacency matrices is computed using the function `gcor` of the R package `sna`. Firstly, the table shows varying levels of correlations, which all tested significant using the `qaptest` function (p-values < 0.001). Secondly, the networks on the same data, but scaled versus non-scaled, are rather different, particularly for the DS case, where the correlation is only 0.18. This is less pronounced for the MA(Add) case, due to the larger sample size. Thirdly, the correlation across samples improves when the data are scaled, e.g. 0.26 between MA(DS) and MA(Add) when they are both scaled versus 0.22 when they are not scaled, and 0.06 between DS and MA(Add) when they are both scaled versus 0.04 when they are not. The correlations between the scaled networks tested significantly larger than those between the non-scaled networks (p-values < 0.001). Fourthly, the correlation across platforms is significant, but generally very low (top second and third quadrant), even when the data are scaled. We will expand on this point in the next section.

Agreement of Enrichment Networks

Table 1 shows a very small agreement of network models, particularly across different platforms. The question could therefore be asked whether the overlap between the two networks is at all biologically relevant. In this section, we aim to summarise the networks at the higher level of functional groups and interactions between these. In particular, we summarise the networks

¹in terms of interactions among 62 KEGG pathways.
²The test `neat` [28] is used to detect enrichment among
³any pair of pathways. Figure 6 shows the quantile-
⁴quantile plots (q-q plots) of the p-values for all pair-
⁵wise comparisons. Under no enrichment, the p-values
⁶should follow a uniform distribution. In that case, the
⁷q-q plot would follow the diagonal line. For the case
⁸of DS and MA(DS), it is obvious how scaling the data
⁹returns networks that are enriched of biological edges,
¹⁰as the q-q plots are those of right-skewed distributions.
¹¹The node variance effect of the networks on non-scaled
¹²data may therefore mask biological facts and the de-
¹³tection of biologically meaningful interactions. For the
¹⁴case of MA(Add), there is detection of interactions
¹⁵among pathways both for the networks on scaled and
¹⁶non-scaled data. In fact, Table 1 showed a relatively
¹⁷large agreement between the two networks (correlation
¹⁸0.54). This is most likely due to the significantly larger
¹⁹sample size of MA(Add) (1272 versus 94), which limits
²⁰the effect of the variances of individual nodes on the
²¹network inference.

²²
²³ Considering the case of scaled data, we build net-
²⁴works among pathways testing for "Overenrichment"
²⁵at a 10% significance level. The resulting networks
²⁶have 240 edges in the case of DS, 240 edges for MA(DS)
²⁷and 427 edges for MA(Add). Figure 7 shows the in-
²⁸tersection of the three networks. The network reveals
²⁹some links between pathways that are supported by
³⁰existing literature. For example, the link between the
³¹Focal Adhesion and Calcium pathways is found signif-
³²icant in the DS network (p-value 0.006, 34 links be-
³³tween the two pathways), MA(DS) (p-value 0.041, 32
³⁴links) and MA(Add) (p-value 0.009, 39 links). Look-
³⁵ing closely at the links, there are many connections
³⁶between the protein tyrosine kinase 2 (PTK2B) from
³⁷the calcium pathway with genes in the focal adhe-
³⁸sion pathway, for example a link between VAV1 and
³⁹PTK2B in the DS network that was found previously

by [10]. In the other direction, AKT2 from the focal¹
adhesion pathway was found to be regulated by cal-²
cium signalling [26] and the link between AKT2 and³
calcium-dependent regulators such as CALM3, which⁴
is found in the microarray networks, is supported by⁵
[23, 25].⁶

Table 2 shows the agreement among the three net-⁷
works in terms of correlation. Comparing this table⁸
with Table 1, we observe the same agreement between⁹
MA(DS) and MA(Add) (p-value 0.532), but a signifi-¹⁰
cantly higher agreement across platforms: 0.11 versus¹¹
0.04 for DS-MA(DS) (p-value 0.019) and 0.12 versus¹²
0.06 for DS-MA(Add) (p-value 0.017). Overall, this¹³
suggests a higher level of consistency at the level of in-¹⁴
teractions between pathways, rather than at the level¹⁵
of individual edges.¹⁶

In many cases, the biological objective of the analysis¹⁷
is to detect differences in regulatory patterns among¹⁸
biological conditions. Then the interest is in the dif-¹⁹
ferential networks, that is in the edges that are found²⁰
only in one of the conditions. Consistency of differ-²¹
ential network analyses among different samples and²²
platforms is therefore also important. In order to assess²³
this, we fitted networks on high glucose and low glu-²⁴
cose samples separately. A similar agreement to that in²⁵
Table 1 was found across platforms, both for high and²⁶
low glucose networks. We then considered the networks²⁷
containing the edges that are in high glucose but not in²⁸
low glucose. We found 18686 edges unique to high glu-²⁹
cose from the networks inferred from DS data, 25522³⁰
edges in the networks inferred from MA(DS) data and³¹
15974 edges in the networks inferred from MA(Add)³²
data. But the three networks altogether have only 100³³
edges in common, suggesting that the detection of dif-³⁴
ferences at the level of individual edges is not robust.³⁵
In contrast to this, when enrichment among pathways³⁶
is considered, Figure 8 shows a low level of pathway³⁷
enrichment for all three networks, particularly for the³⁸
³⁹

network from the DS data. Similar results are obtained when considering the networks unique to low glucose. For example, there are 21218 edges unique to high glucose from the networks inferred from DS data, 24684 edges in the networks inferred from MA(DS) data and 13489 edges in the networks inferred from MA(Add) data, but the three networks altogether have only 98 edges in common. This means that the networks, across samples and platforms, have little signature of differences between high and low glucose conditions. Of course, there may be genuine differences, but there is not enough evidence in the data to pick these up. These examples show that consistency across platforms can be particularly low for differential networks, since one is looking for a robust detection of edges that are in one condition but not in the other condition, so sensitivity as well as specificity of sparse Gaussian graphical models play a role in this case.

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Discussion and Conclusion

The aim of this paper was to assess the consistency of networks inferred by sparse Gaussian graphical models across different samples and data platforms. To this aim, we used a rich dataset containing samples that are profiled under both techniques as well as a large set of independent samples. We first of all showed the impact of confounding effects (such as age and gender) on the network reconstruction. The effect was not very strong in our study. Nevertheless, we show how confounding effects may return spurious interactions amongst genes and may mask the search for genuine regulatory interactions. Although the inference method does not correspond to any generative model of the data, i.e., it is impossible to set up a sampling scheme that exactly correspond to the two-step inference procedure, we have investigated how realistic sampling schemes for genetic networks are affected by confounding variables. The results, included in the supplementary materials, show that the inferred precision matrix in the two-

step procedure relates closely the underlying network in all kind of confounding scenarios. Moreover, [3] show that the precision matrix can approximately be interpreted in terms of conditional odds ratios, which are more natural ways to interpret conditional independence for count data. Given these considerations, we recommend to devise an appropriate regression model and fit networks to the residuals of this model, i.e. to data adjusted for confounders.

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Our analysis of the inferred networks shows that individual node variances can have a remarkable effect on the connectivity of the resulting network. In particular, they result in hub-type networks with hubs made of the nodes with the highest variances. The inconsistency of node variances across platforms and the fact that the variability level of a node may not be linked to its regulatory role mean that, failing to scale the data prior to the network analysis, leads to networks that are not reproducible across different platforms and that may be misleading. This point is of particular importance given that not all available implementations of sparse Gaussian graphical models automatically scale the data and thus this step is often left to the user. Failure to scale the data prior to network modelling may in part explain the belief, particularly in the early days of network modelling of biological systems, that biological networks are scale-free and the later contributions which questioned this assumption, e.g. [14, 17] and references therein.

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However, even after scaling of the data, our analysis shows that a large number of edges are not replicated across platforms. We then show how the reproducibility of networks across different samples and platforms is notably higher if networks are summarised in terms of enrichment amongst functional groups of interest, such as KEGG pathways, rather than at the level of individual edges. In particular, we show, for the case of differential networks, how conclusions from individ-

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ual edges are not consistent across platforms and, once again, how conclusions drawn from analyses of individual edges may be misleading.

Overall, while the field of network modelling makes steady advances and new network models with higher specificity, sensitivity and computational efficiency are proposed in the literature, this study shows that caution is needed at this stage in the (over)interpretation of the inferred networks for biological findings. In particular, we show how summarising the networks at the level of functional groups of interest, such as KEGG pathways, provides a more robust representation of the underlying network and allows to reach conclusions that are most consistent across platforms. The network of functional groups is also of a significantly smaller scale than the network of genes and, thus, it can be more easily interrogated to generate hypotheses that can be tested by further biological experiments.

Additional Files

Additional file 1: Simulation showing the effect of confounders on network reconstruction.

List of abbreviations

SAGE: Serial Analysis of Gene Expression; MA: MicroArray; DS: DeepSAGE; KEGG: Kyoto Encyclopedia of Genes and Genomes; q-q plot: quantile-quantile plot; NTR: Netherlands Twin Register; NESDA: Netherlands Study of Depression and Anxiety; Body Mass Index (BMI).

Ethics approval and consent to participate

The research protocol was approved by the Ethical Committees of the participating universities and all subjects have provided written informed consent.

Consent for publication

Not applicable.

Availability of data and materials

Gene expression data used for this study are available at dbGaP, accession number phs000486.v1.p1 (http://www.ncbi.nlm.nih.gov/projects/gap/cgi-bin/study.cgi?study_id=phs000486.v1.p1).

Competing interests

The authors declare that they have no competing interests.

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Authors' contributions

VV, EW and PH conceived the study, discussed the methodology and interpreted the results. VV and EW performed the data analysis. RJ, EG, BP, DB provided the NTR and NESDA data. PH assisted in the biological interpretation of the results. VV wrote the manuscript. All authors read and approved the final manuscript.

Author details

¹Department of Mathematics, Brunel University London, London, UK.

²Johann Bernoulli Institute of Mathematics and Computer Science, University of Groningen, Groningen, The Netherlands. ³VU University Medical Center, Amsterdam, The Netherlands. ⁴Leiden University Medical Center, Leiden University, Leiden, The Netherlands.

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Figure 1 DS versus Microarray Expression. Left: Average (log) expression for the 1435 genes from the 94 DS samples (x-axis) and the 94 microarray samples (y-axis). Right: Average gene expression from the 94 microarray samples versus the 1272 additional microarray samples.

Figure 2 Confounders Effect. Two examples of the effect of confounders on the MA(DS) network: the two links are found when not correcting for confounders, but not after correction.

Figure 3 Node Variance Effect. Node connectivity versus node variance for DS network (a), MA(DS) network (b) and node variance from DS data versus node variance from MA data (b).

Figure 4 Node Connectivity versus Expression Node connectivity of DS network versus node expression level (measured as number of transcripts per million (tpm)).

Figure 5 Scaling Effect on Node Connectivity Node degree distributions of DS (left) and MA(DS) (right) networks on scaled (red) and non-scaled (blue) data. The networks have similar size (about 30000 edges).

Figure 6 Enrichment of Links between Pathways q-q plot of p-values of the enrichment test for all pairwise comparisons of 62 KEGG pathways for DS, MA(DS) and MA(Add) and distinguishing the case of scaled and not-scaled data.

Figure 7 Network of Pathways Overlap Overlap of Pathway Networks from DS, MA(DS) and MA(Add) at 10% significance level.

Figure 8 High versus Low Glucose Networks q-q plot of the enrichment test for all pairwise comparisons of 62 KEGG pathways for the differential networks between high and low glucose.

Table 1 Correlation among the 6 networks from expression data (DS, MA(DS) and MA(Add)) and two cases (SCALED - data centered to mean zero and variance one for each gene and NOT SCALED.)

		DS		MA(DS)		MA(Add)	
		SCALED	NOT SCALED	SCALED	NOT SCALED	SCALED	NOT SCALED
DS	SCALED	1.00	0.18	0.04	0.02	0.06	0.05
	NOT SCALED		1.00	0.03	0.03	0.04	0.04
MA(DS)	SCALED			1.00	0.36	0.26	0.21
	NOT SCALED				1.00	0.14	0.22
MA(Add)	SCALED					1.00	0.54

Table 2 Correlation among the networks at the level of KEGG pathways.

	DS	MA(DS)	MA(Add)
DS	1.00	0.11	0.12
MA(DS)		1.00	0.26
MA(Add)			1.00