Symmetry-Related Transitions in the Spectrum of Nanosized Cubic Y_2O_3:Tb^{3+}

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Herein the preparation and cathodoluminescence of nanoparticles of cubic Y_2O_3:Tb^{3+} having Tb^{3+} concentration varying between 0.1 and 10 Mol% are described. The cathodoluminescence spectra were recorded with a high resolution spectrometer, which enabled the identification of Tb^{3+} lines with C_2 and S_6 symmetry: the lines at 542.8 nm and 544.4 nm were designated as $^5D_4 \rightarrow {}^7F_5$ (C_2) and $^5D_4 \rightarrow {}^7F_5$ (S_6) respectively. The critical distance for energy transfer from Tb^{3+} ions at S_6 lattice sites to Tb^{3+} ions at C_2 lattice sites was found to be >1.7 nm. At the greater distances which prevail at low Tb^{3+} concentration, this energy transfer virtually stops. From cathodoluminescence spectra recorded in a scanning transmission electron microscope it was concluded that this energy transfer also did not take place if the temperature was reduced below 102 K. The efficiency of the cathodoluminescence of 1% Y_2O_3:Tb^{3+} was 6 lm/w at a beam voltage of 15 kV. The decay time of the $^5D_4 \rightarrow {}^7F_5$ (C_2) transition was substantially shorter than that of the $^5D_4 \rightarrow {}^7F_5$ (S_6) transition at low Tb^{3+} concentrations. The decay behavior of the cathodoluminescence images in a field emission scanning electron microscope has been explained in terms of phosphor saturation.

Recently we have published a study on the cathodoluminescence (CL) of nanosized Y_2O_3:Eu^{3+} particles.[1] The methods described in that report enabled a detailed analysis of the symmetry-related spectral transitions in the CL spectrum of Y_2O_3:Eu^{3+}. In the present report we describe a study on the cathodoluminescence of nanosized Y_2O_3:Tb^{3+} particles using the same methods as developed for analyzing the spectra of Y_2O_3:Eu^{3+}. Although the industrial importance of Y_2O_3:Tb^{3+} is smaller than that of Y_2O_3:Eu^{3+}, the strong green fluorescence of Tb^{3+} doped Y_2O_3 crystals has attracted much attention and many scientists studied the PL and CL spectra of Y_2O_3:Tb^{3+} particles, both micrometre and nanometre sized. The CL spectra of nine rare earth ions in Y_2O_3 host crystals were published by Ozawa.[2] The idiosyncrasy of the luminescence spectra of Tb^{3+} doped phosphors was nicely summarized by Blasse and Grabmaier: domination by the $^5D_4 \rightarrow {}^7F_J$ (J = 2, 3, 4, 5 and 6) transitions, contribution of (weak) $^5D_3 \rightarrow {}^7F_J$ transitions in the blue and a complicated structure of the crystal field splitting because of the rather high J quantum numbers.[3]

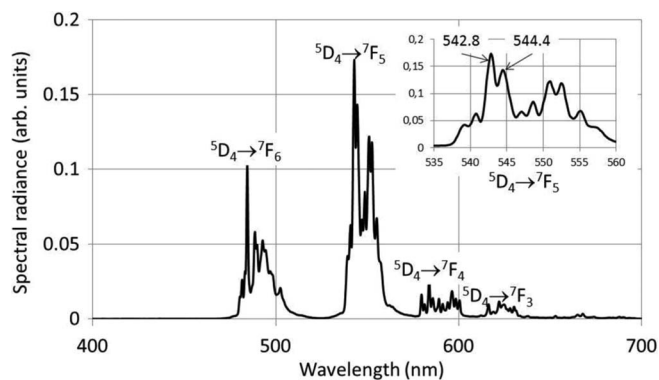Figure 1 shows the high resolution CL spectrum of cubic nanosized Y_2O_3:Tb^{3+} with 1% Tb^{3+} recorded by us at an electron energy of 15 keV, current density of 2 μA/cm^2 and room temperature. The spectral radiance of the $^5D_3 \rightarrow {}^7F_J$ transitions in the blue region of the spectrum is very small and cannot be observed in Figure 1. The inset shows a detail of the spectrum between 535 nm and 560 nm: 10 peaks can be observed at these conditions. Because of the complicated configuration of the peaks in the various $^5D_4 \rightarrow {}^7F_J$ transition clusters, a detailed designation of the lines to specific crystal-field-splitting levels has not been established. A second complication in identifying the spectral lines of Y_2O_3:Tb^{3+} is related to the crystal structure of the Y_2O_3-host. It has been well established that Y_2O_3 doped with various concentrations of Tb^{3+} and annealed at temperatures above 900°C has the cubic structure of the mineral bixbyite;[4–10] moreover, the cell constant of the unit cell, 1.060 nm, does not change upon doping.[6] This cubic structure has two different Y^{3+} lattice sites, which possess the point symmetries C_2 and S_6: 24 lattice sites have C_2 symmetry, while the other 8 have S_6 symmetry.[11] These sites are shown in Figure 2. Upon doping Y_2O_3 with Tb^{3+} the two sites are occupied with Tb^{3+} with almost equal probability, because the Tb^{3+} ion is only slightly smaller than the Y^{3+} ion: hence, the concentration of Tb^{3+} at C_2 sites will be three times larger than the concentration of Tb^{3+} at S_6 sites. It can be seen that the S_6 sites have inversion symmetry, whereas the C_2 sites exhibit a "small deviation" from the inversion symmetry according to Blasse and Grabmaier.[3] Unlike the situation

for the Y_2O_3:Eu^{3+} spectrum, in which various S_6 and C_2 lines have been identified, an identification of symmetry-related peaks in the spectrum of Y_2O_3:Tb^{3+} is missing. As we have shown in our study of the CL-spectrum of Y_2O_3:Eu^{3+}, the relation between C_2 and S_6 transitions gave valuable information on the energy transfer between levels in Eu^{3+}. In order to make a similar analysis for Y_2O_3:Tb^{3+}, we need to identify C_2 and S_6 transitions in the spectrum.

In spite of the absence of any assignment of the lines in the various $^5D_4 \rightarrow {}^7F_J$ transition clusters, the scientific work on nanosized Y_2O_3:Tb^{3+} is progressing.[5–10,12–16] The majority of these recent studies have dealt with photoluminescence (PL) of Y_2O_3:Tb^{3+}; however, Alarcón-Flores et al.[12] and Cho et al.[13] have used cathodoluminescence (CL), while Cress et al.[14] have applied alpha particles (radioluminescence) to excite the phosphor. In the PL studies the effects of annealing temperature, particle size and Tb^{3+} concentration in the Y_2O_3 host have been described. Most authors discussed the cross relaxation of the 5d and 4f levels of Tb^{3+}; however, Withnall et al.[15] suggested also the possibility of energy transfer between Tb^{3+} at an S_6 and a C_2 site in cubic Y_2O_3. Meng et al.[7] attributed the differences between excitation spectra to surface versus bulk effects upon changing the Y_2O_3:Tb^{3+} particle size. Goldburt et al.[16] found that the PL efficiency decreased by a factor of 5 when the size of the nano particles increased from 4 to 9 nm. Liu et al.[8] studied the effect of Eu^{3+}, Tb^{3+} co-doping on the luminescent properties of Y_2O_3 nanorods as a function of the Tb^{3+} concentration. Chien et al.[5] found that 1 Mol% Tb^{3+} in Y_2O_3 has the highest PL efficiency, Jiu et al.[9] found that a concentration of 3% was optimum whereas Park et al.[10] concluded that 8% Tb^{3+} was most efficient. Sotiriou et al.[4] described the effect of the lattice on the PL efficiency. They found that monoclinic Y_2O_3:Tb^{3+} has a higher efficiency than the cubic phase, which needs a higher annealing temperature. This brief review of recent work on the luminescence of nanosized Y_2O_3:Tb^{3+} is in no way exhaustive; however, it does illustrate the widespread interest in this material.

The objective of this study is analyzing the CL-spectra and decay behavior of some transitions of nanosized Y_2O_3:Tb^{3+} in the hope to find evidence for a symmetry-related route of energy transfer beside the well-known relaxation between the $^5D_3$ and $^7F_6$ levels.[17] In our previous study[1] on the energy transfer in nanosized Y_2O_3:Eu^{3+} we could confirm the results obtained with micrometer-sized particles.[18] So, we assume that the size of the particles is not the determining parameter for this study, but rather the concentration of Tb^{3+} in the Y_2O_3 lattice. To make a fair comparison between the spectra of different Tb^{3+} concentrations in Y_2O_3, temperature, current density and e-beam energy were kept constant. Deviations from this principle are indicated in the text.

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Figure 1. High resolution CL spectrum of cubic nanosized Y_2O_3:Tb^{3+} with 1 Mol% Tb^{3+} recorded at a beam energy of 15 keV, current density of 2 $\mu A/cm^2$ and room temperature. Inset: $^5D_4 \rightarrow {}^7F_4$ transition cluster in wide wavelength scale. The wavelengths (in nm) of the two strongest peaks in the spectrum are indicated.

Materials and Methods

Materials and synthesis.— Yttrium oxide (99.99%, Ampere Industrie, France) and terbium oxide (99.99%, Neo performance materials, UK) were used to prepare the terbium-doped yttrium nitrate stock solutions. Urea, nitric acid and isopropanol (IPA) were supplied by Fisher Scientific, UK; all chemicals were used as received. Glass substrates (1 cm^2) coated with an indium tin oxide (ITO) film (85 Ω/sq) were obtained from Visiontek Ltd., UK. The ITO-coated slides were carefully cleaned in de-ionized water and IPA using ultrasonic cavitation. Conductive carbon tabs coated with adhesive on both sides were used as substrate for recording the spectra and the imaging studies in the field emission scanning electron microscope (FESEM). For the transmission electron microscope (TEM) special C-grid substrates were used. The synthesis of Y_2O_3:Eu^{3+} nanoparticles by the urea method has been described extensively in our earlier work;[1,19–21] the synthesis of nanosized Y_2O_3:Tb^{3+} was done identically. The aging of the turbid suspensions after the onset of precipitation was continued for one hour at a temperature above 85°C (which is the temperature at which urea slowly decomposes in aqueous media). After this aging period the precipitate was filtered, washed three times with de-ionized water and dried in an oven at 80°C. The phosphor precursor particles were then annealed at 980°C in a furnace in air for four hours to yield cubic nanosized Y_2O_3:Tb^{3+} phosphor particles. This annealing temperature guarantees cubic crystallites that yield optimum CL characteristics.[20] The Y_2O_3:Tb^{3+} powders after annealing looked slightly yellow-brown, due to the presence of a small quantity of Tb^{4+}.[22] The possible reduction of this very small quantity of Tb^{4+} will be discussed in the CL spectrum section.
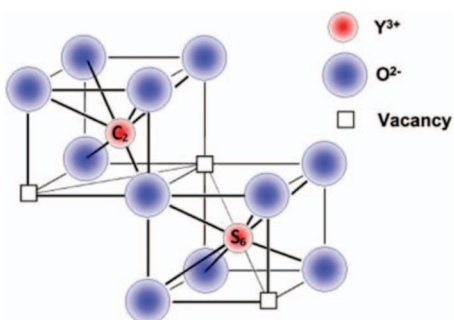

Figure 2. C_2 and S_6 sites of the Y^{3+} cation in cubic Y_2O_3. S_6 has inversion symmetry, whereas C_2 has 180° rotation symmetry.
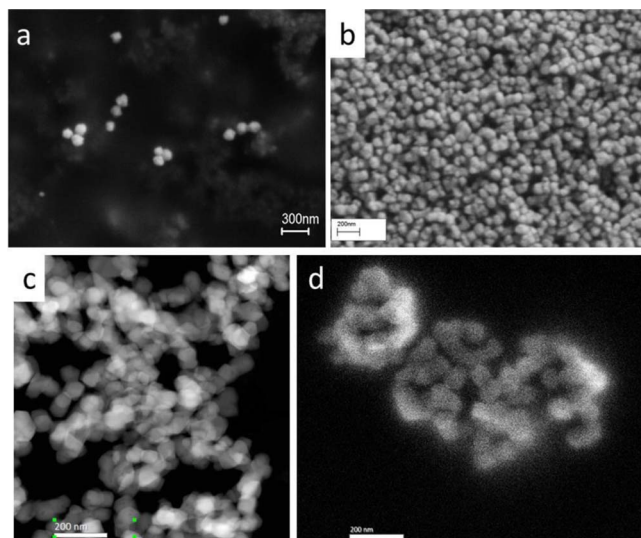
Figure 3. (a) FESEM image of Y_2O_3:Tb^{3+} (0.3% Tb^{3+}) particles on C-substrate (10 kV). (b) FESEM image of dense layer of Y_2O_3:Tb^{3+} (10% Tb^{3+}) on Si substrate. (c) STEM image of Y_2O_3:Tb^{3+} (3% Tb^{3+}) at 200 kV on C-substrate. (d) Panchromatic cathodoluminescence STEM image of Y_2O_3:Tb^{3+} (3% Tb^{3+}) at 200 kV on C-substrate.

Phosphor layers were deposited onto ITO-coated glass slides by electrophoresis from isopropanol suspensions containing various phosphor concentrations; however, it was difficult to obtain uniform layers with an area of 1 cm^2. Only layers with 3 and 1% Tb^{3+} had sufficient uniformity and could be used for the measurements of the luminous efficiency. Figure 3a shows a SEM image of Y_2O_3:Tb^{3+} (0.3% Tb^{3+}) particles on a C-substrate. The scarce coverage of particles on the C-substrate in Figure 3a was made on purpose to enable decay measurements in the SEM, to be discussed in Decay analysis with FESEM section. Figure 3b shows an image of a settled layer of Y_2O_3:Tb^{3+} on a Si substrate, while Figures 3c and 3d show TEM images of Y_2O_3:Tb^{3+} with 3% Tb^{3+}. From Figures 3b, 3c and 3d it can be derived that the average diameter of the Y_2O_3:Tb^{3+} particles varied between 50 and 80 nm, which did not depend on the concentration of Tb^{3+}, it was virtually equal for all concentrations. This particle diameter is much smaller than the identically synthesized Y_2O_3:Eu^{3+} particles, which showed spherical shapes with diameters ranging from 200 nm up to 350 nm.[1,19,20] These differences in size and shape could be caused by a (small) difference between the pH of the stock solutions of $Tb(NO_3)_3$ and $Eu(NO_3)_3$: this will be the topic of a future study in our laboratory.

Equipment and methods.— The CL measurements were carried out using two high vacuum chamber systems. The first system, called herein as 5 kV rig, was equipped with an EFG-7 electron gun with a maximum voltage of 5 kV and a EGPS-7 power supply (both Kimball Physics Inc., USA) worked at a pressure of 4×10^{-6} mbar. In this system decay measurements at current densities of typically 0.5 mA/cm^2 were conducted and some high resolution spectra as a function of current density up to 5 mA/cm^2 were recorded as well. On the second high vacuum chamber system, called 15 kV rig, CL spectra were collected over a range of electron beam accelerating voltages from 3 to 15 kV using an EFG-12 electron gun and EGPS-12 power supply (both Kimball Physics Inc., USA). The luminous efficiency measurements and recording of the CL spectra were done on the 15 kV rig at current densities of 1–5 $\mu A/cm^2$ and pressure of 2×10^{-6} mbar. Deflection plates enabled optimum positioning of the electron beam on the sample and a ZnO:Zn standard. The latter being a non-charging thin film of ZnO:Zn powder on ITO-coated glass to adjust the current density on the charging Y_2O_3:Tb^{3+} samples as explained in our previous work.[1,19] High resolution CL emission spectra of the samples were
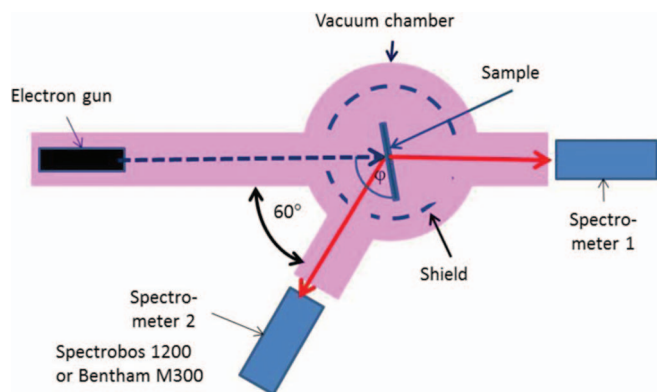
Figure 4. Equipment for CL measurements using two spectrometers. Recording of high resolution spectra with the Bentham monochromator was only done in reflection mode.

collected using a Bentham phosphor spectrometer system (Bentham Instruments Ltd., Reading, UK.), configured with M300 excitation and emission monochromators, to which the emission monochromator was connected via a fibre optic bundle positioned at the window of the vacuum chamber. The absolute wavelength calibration of this emission monochromator could be off by maximally 0.4 nm; however, relative wavelength values were accurate within 0.03 nm.

The electron gun set-up and viewing port geometries of the 15 kV rig are shown in Figure 4. The sample was positioned in the centre of the vacuum chamber. For the determination of the luminous efficiency, spectral radiance and luminance were recorded with two Spectrobos 1200 spectroradiometers manufactured by JETI (Germany) between 380 nm and 780 nm in reflection and transmission mode, indicated in Figure 4 by spectrometers 2 and 1 respectively. Spectrometer 2 was replaced with the Bentham fibre optic bundle for recording the high resolution CL spectra.

The shield is a high transmission grid (transmission > 99%) which is biased at −50 V to collect all secondary electrons on the sample plate. By blanking the e-beam of the Kimball electron gun of the 5 kV rig we could measure the persistence of the luminescence of various spectral transitions in Y_2O_3:Tb^{3+}. The high resolution Bentham monochromator was used to adjust the wavelength to the maximum of a spectral peak. This measuring method has been described in detail in our previous report.[1]

The morphology and particle size assessment of the phosphor powders and CL-microscopy analyses were conducted in both a SEM and TEM. The SEM was a FESEM, Supra 35 VP, Carl Zeiss, Germany. Besides three detectors for secondary and backscattered electrons, this microscope was also equipped with a detector for CL. This facility enabled luminescence decay studies of individual phosphor particles, as we have recently described.[1,23] Image analysis of the panchromatic CL-micrographs was performed using ImageJ (Public Domain) software.

The nanosized Y_2O_3:Tb^{3+} samples with 0.3 and 3% Tb^{3+} were also analyzed with a TEM, model 2100F, JEOL, Japan. This microscope was operated in scanning mode with a spot size of 0.2 nm or 1.5 nm. The TEM was equipped with a Vulcan CL detector, Gatan, USA, for imaging and spectroscopic purposes. This system used a Czerny-Turner spectrometer with back-illuminated CCD and a grating with 1200 lines/mm (blazed at 500 nm) for collection of CL emission spectra. A cooled photo-multiplier tube (PMT) was utilized for collection of the total light flux from the sample. By collecting the visible light with the Vulcan system simultaneously with the JEOL high angle annular dark field detector it was possible to observe the visible light that was emitted from the particles. A small cryostat connected to the sample holder enabled cooling of the samples in the TEM down to 103 K (−170°C); adjustment of the sample temperature anywhere between 102 K and 303 K could be made.

Results

CL spectrum.— Figure 1 is the high resolution CL spectrum of nanosized Y_2O_3:Tb^{3+} with 1% Tb^{3+}, recorded at the 15 kV rig at low current density. The inset of this Figure shows the $^5D_4 \rightarrow ^7F_4$ transition cluster at a wide wavelength scale. The two strongest peaks reach their maximum values at 542.8 nm and 544.4 nm. Figure 5 shows normalized CL spectra of nanosized Y_2O_3:Tb^{3+} with 0.3, 0.7, 1 and 3% Tb^{3+}, recorded at an electron energy of 15 keV, current density of 2 μA/cm² and room temperature For reasons of clarity the spectra of the 0.1, 0.6 and 10% Tb^{3+} have not been included in Figure 5; the spectra for 0.1 and 10% Tb^{3+} are presented in Figure 6. Normalization was done versus the strongest peak in the spectra, viz. the 542.8 nm peak was set to unity in all spectra: this facilitated the comparison between the spectra. Figure 5a refers to the $^5D_4 \rightarrow ^7F_5$ the transition cluster, Figure 5b to $^5D_4 \rightarrow ^7F_6$, Figure 5c to $^5D_4 \rightarrow ^7F_3$ and Figure 5d to $^5D_4 \rightarrow ^7F_4$. It can be seen that only Figures 5a and 5c show pronounced concentration effects; the concentration effects in the $^5D_4 \rightarrow ^7F_6$ and $^5D_4 \rightarrow ^7F_4$ transitions clusters are rather small, but cannot be neglected either. The isolated peak at 637.8 nm in the $^5D_4 \rightarrow ^7F_3$ transition cluster, indicated by an arrow in Fig. 5c, shows a particularly large effect: the 3% Tb^{3+} concentration has the lowest spectral radiance and the 0.3% Tb^{3+} the highest. The other concentrations have intermediate radiances. The same trend can be observed in the $^5D_4 \rightarrow ^7F_5$ transition cluster notably for the peak at 544.4 nm. Because of the low spectral radiance of the $^5D_4 \rightarrow ^7F_3$ transitions cluster we did not analyze this part of the spectrum in detail and focussed on the high radiance $^5D_4 \rightarrow ^7F_5$ peaks at 542.8 nm and 544.4 nm. The normalized spectra did not change between 5 and 15 kV.

Figure 6 shows the CL spectra of the $^5D_4 \rightarrow ^7F_5$ the transition cluster of Y_2O_3:Tb^{3+} with 0.1 and 10% Tb^{3+}. The radiance was small for these samples because of considerable concentration quenching for the 10% sample and low concentration for the 0.1% sample. The spectra shown in Figure 6 are also normalized to unity at 542.8 nm. For the 0.1% sample the 544.4 nm peak is now larger than the 542.8 nm peak. The spectrum of 6% Tb^{3+} is not shown, because it almost coincides with that of the 10% sample. The height difference of the 544.4 nm peak between 0.1 and 10% Tb^{3+} is very pronounced in this Figure. However, some peaks at λ > 544.4 nm show also substantial concentration effects.

The spectra shown in Figures 5 and 6 were recorded at a low current density between 2 μA/cm² and 5 μA/cm², in which the effect of saturation can be excluded. For the spectra shown in Figure 6 we used 5 μA/cm² to increase the signal to noise ratio. We have also recorded CL-spectra of Y_2O_3:Tb^{3+} at much higher current density on the 5 kV rig, in which the effect of current density becomes quite noticeable. An example is shown in Figure 7 for the $^5D_4 \rightarrow ^7F_5$ transition cluster of 1% Y_2O_3:Tb^{3+}, in which the 542.8 nm peak has again been normalized to unity. It can be seen that the peak at 544.4 nm suffers more from saturation than the peak at 542.8 nm.

Because of the substantial overlapping of peaks in the spectra, comparing the peak values at 542.8 nm and 544.4 nm may yield inaccurate information; therefore, it was decided to calculate the ratio of the peaks at 542.8 nm and 544.4 nm, indicated by $I_{542.8}/I_{544.4}$, from the deconvoluted spectra. The deconvolution was done in the same way as we did for the spectra of Y_2O_3:Eu^{3+} as described in Ref. 1. It was assumed that the spectral transitions have Gaussian shapes. The spectral radiance SR(λ), where λ represents the wavelength, can be written as:

$$SR(\lambda) = \sum_i A_i e^{\frac{-(\lambda - \lambda_i)^2}{s_i}}, \qquad [1]$$

where A_i is the maximum spectral radiance of the ith peak, λ_i is the wavelength for the maximum and s_i is a parameter related to the width of the ith peak. The full width at half maximum (FWHM) is

$$FWHM_i = 1.665\sqrt{s_i}, \qquad [2]$$
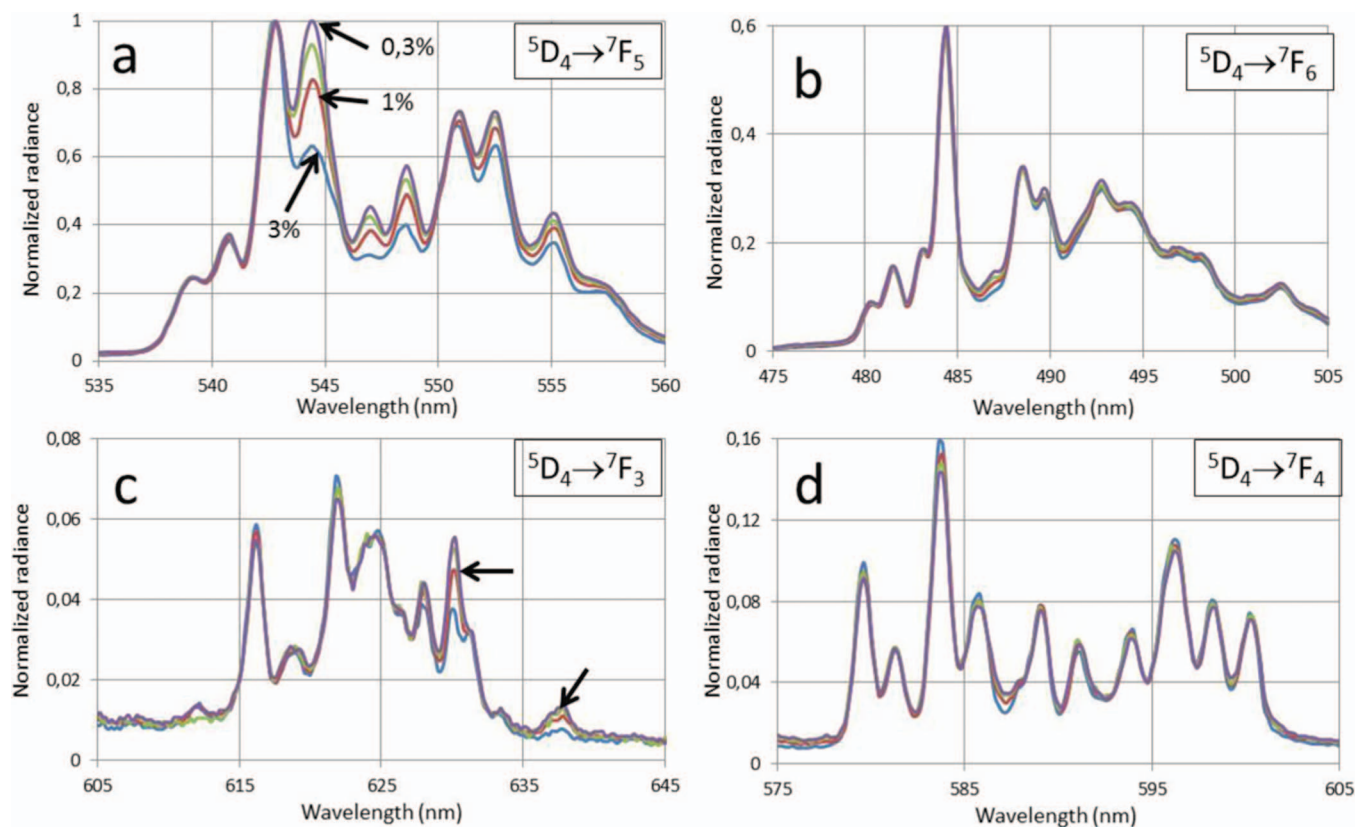
Figure 5. Normalized CL spectra of Y_2O_3:Tb^{3+} at 0.3, 0.7, 1 and 3%Tb^{3+}; a: $^5D_4 \rightarrow ^7F_5$ cluster; b: $^5D_4 \rightarrow ^7F_6$ cluster; c: $^5D_4 \rightarrow ^7F_3$ cluster; d: $^5D_4 \rightarrow ^7F_4$ cluster. Radiance of 542.8 nm peak set to unity for all spectra.

and the radiance of the ith transition is

$$R_i = \int_{-\infty}^{\infty} A_i e^{\frac{-(\lambda - \lambda_i)^2}{s_i}} d\lambda = A_i \sqrt{\pi s_i}. \qquad [3]$$

An example of the deconvolution of the $^5D_4 \rightarrow ^7F_5$ peaks at 542.8 nm and 544.4 nm is depicted in Figure 8 for 0.3% Y_2O_3:Tb^{3+}. In this deconvolution four Gaussian profiles were used; Lorentzian profiles did not yield satisfactory results. These four Gaussians were fitted to the experimental spectrum with a least squares algorithm using Microsoft's Excel solver.

The radiance ratio $I_{542.8}/I_{544.4}$ is plotted in Figure 9a as function of Tb^{3+} concentration and as a function of the average distance between Tb^{3+} ions in the Y_2O_3 lattice in Figure 9b. This average distance D_{Tb}

can be written as[1]:

$$D_{Tb} = \sqrt[3]{\frac{100M}{2\rho N_{av}c}}, \qquad [4]$$

where M is the molecular weight of Y_2O_3, ρ is the density of Y_2O_3, being 5.01 g/cm^3, and N_{av} is Avogadro's number. The factor 100 appears in Eq. 4, because the concentration c is expressed in %.

The correspondence between Figure 9, derived from the spectra recorded at low current density, and the equivalent Figure in our report on Y_2O_3:Eu^{3+} is striking;[1] so, we conclude that the 542.8 nm peak refers to Tb^{3+} at a C_2 site and the 544.4 nm peak refers to Tb^{3+} at
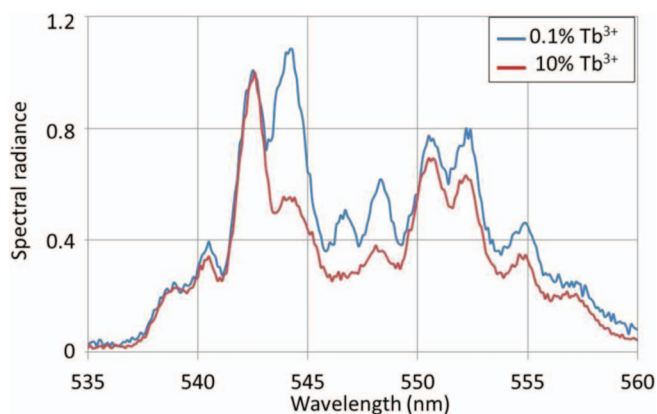
Figure 6. Normalized CL spectra of the $^5D_4 \rightarrow ^7F_5$ transition cluster of nanosized Y_2O_3:Tb^{3+} with 0.1 and 10% Tb^{3+}, recorded at 15 keV and 5 μA/cm^2.
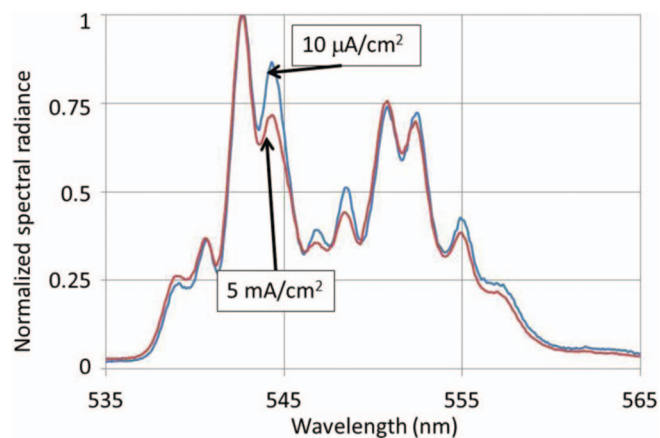
Figure 7. Normalized CL spectra of nanosized Y_2O_3:Tb^{3+} with 1% Tb^{3+} at 5 kV of $^5D_4 \rightarrow ^7F_5$ the transition cluster at low (10 μA/cm^2) and high (5 mA/cm^2) current density.
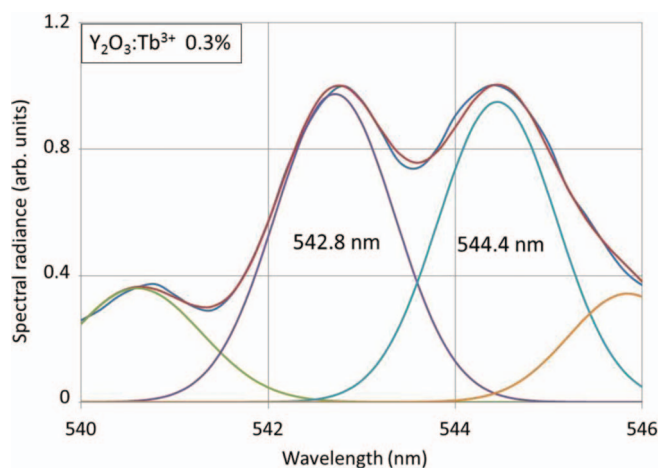
Figure 8. Deconvolution of a part of the $^5D_4 \rightarrow {}^7F_5$ spectrum between 540 and 546 nm with four Gaussian profiles.

Figure 10. Lumen efficacy of nanosized Y_2O_3:Tb^{3+} versus beam voltage.

an S_6 site. The knee of the curve in Figure 9b is at 1.7 nm, which implies that the critical distance, $D_{Tb^{3+}}^{Crit}$, for interaction between the S_6 and C_2 sites is 1.7 nm. This value is identical to the critical distance in Y_2O_3:Eu^{3+1}. We have argued that $D_{Tb^{3+}}^{Crit}$ is two times larger than the distance R_0, being the critical transfer distance for which the transfer rate of energy from S_6 to C_2 is equal to the radiative decay rate;[24] consequently, R_0 for Y_2O_3:Tb^{3+} is 0.85 nm and the same as R_0 for Y_2O_3:Eu^{3+}. Ozawa mentioned the change of the relative radiance of lines in the CL spectrum of Y_2O_3:Tb^{3+} upon varying the dopant concentration,[2] but he did not specify which peaks were changing. Without splitting the $^5D_4 \rightarrow {}^7F_5$ transition into a doublet consisting of a C_2 and S_6 part the concentration effects in the spectrum are modest, let alone that it would be possible to designate overlapping peaks in a low resolution spectrum.

Beside the high resolution spectra shown in Fig. 5 we have also recorded low resolution spectra at various e-beam voltages and a current density of 1 µA/cm² with the Spectrobos 1200 spectrora-diometers, which enable a direct evaluation of the color coordinate of the emitted light. This measurement was primarily carried out for the determination of the lumen efficiency, to be discussed in Luminous efficiency section; however, it allowed also a check on the possible reduction of Tb^{4+} ions in the Y_2O_3 lattice upon electron bombardment. Adjustment and measurement took about 2 minutes for each spectrum; the spectra were recorded in succession with spectrometer 2 at increasing e-beam voltages of 3, 6, 9, 12 and 15 kV. The color coordinates of the CL-spectra were constant, namely x = 0.3280 and y = 0.5750 (CIE-1931). These color coordinates have not been checked via a calibration procedure of the spectrometers; however, for the present purpose the comparison is justified, because spectrometer and
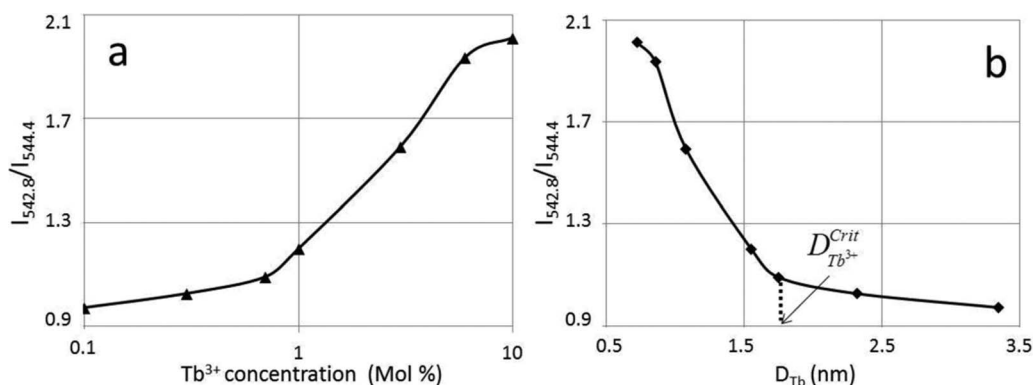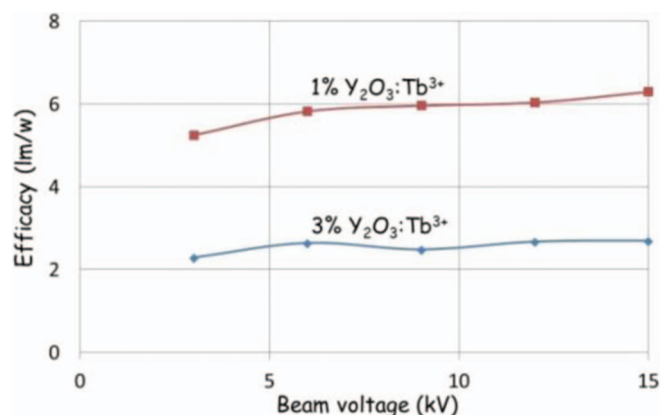
electron gun were not touched during the measurements. The invariance of the color coordinates versus time and beam voltage indicates that a possible reduction of a small quantity of Tb^{4+} ions to Tb^{3+} in the Y_2O_3 lattice upon electron bombardment can be neglected. There is another reason why we assume that a possible reduction of Tb^{4+} can be neglected in the present study, viz. the considerations on the ratio $I_{542.8}/I_{544.4}$, refer to wavelengths, which are so close, that an effect of a small change in the absorption due to a variation in the Tb^{4+} would have been detected in the deconvolutions discussed afore.

Luminous efficiency.— Thin layers of Y_2O_3:Tb^{3+} particles deposited on ITO coated glass slides were used for measuring the luminance and spectral radiance. The weight of the Y_2O_3:Tb^{3+} layers was 2 mg/cm² for the 1% Tb^{3+} sample, yielding a layer thickness 6.2 µm.[1] In the case of 3% Tb^{3+} the weight of the layer was less and the thickness was therefore smaller. The measurement method of the luminance and the evaluation of the luminous efficiency have been described extensively in our previous papers;[1,19] hence, we may suffice in presenting the results only in Figure 10. The measurements were conducted in the 15 kV rig at a current density of 1 µA/cm². It can be seen that the luminous efficiency is almost constant between 6 and 15 kV. Since it was impossible to prepare layers of sufficient uniformity for the other Tb^{3+} concentrations, the optimum Tb^{3+} concentration could not be determined. Obviously, Y_2O_3:Tb^{3+} with 3% Tb^{3+} is already suffering from concentration quenching; so, the optimum concentration must be lower than 3%.

The lumen efficacy of Y_2O_3:Tb^{3+} is smaller than that Y_2O_3:Eu^{3+1}. This result is contrary to luminance data published by Cho et al.[13]

Decay.— Thin layers of nanosized Y_2O_3:Tb^{3+} particles on C-substrates were excited with a partially focussed electron beam of 5 kV rig and current densities between 100 µA/cm² and 500 µA/cm².

Figure 9. a. Plot of $I_{542.8}/I_{544.4}$ as a function of Tb^{3+} concentration. b. $I_{542.8}/I_{544.4}$ versus D_{Tb}.

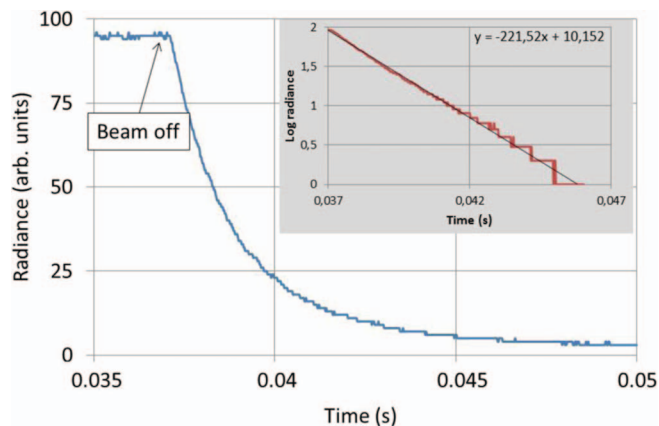**Figure 11.** Decay of radiance of 542.8 nm peak of Y_2O_3:Tb^{3+} (0.3%Tb^{3+}); beam energy 5 keV, current density is $\approx 500\ \mu A/cm^2$.
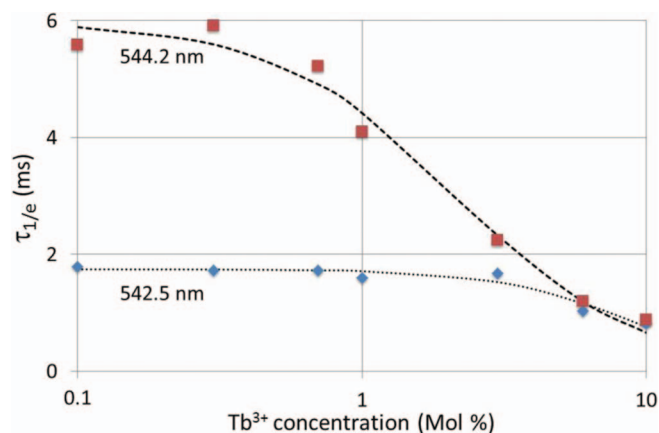
Figure 12. Decay times of 542.8 nm and 544.4 nm peaks of Y_2O_3:Tb^{3+} versus Tb^{3+} concentration. Points: experimental values, curves are fitted to the experimental results.

Some saturation of the 544.4 nm could occur at these conditions as can be seen in Figure 7. Since we did not observe differences upon lowering the current density to 10 $\mu A/cm^2$ for this peak, we did not investigate this issue in more detail. The high resolution Bentham spectrometer was used to adjust the wavelength to be analyzed, which helped to minimize the interference from partially overlapping transitions. A typical decay curve for the $^5D_4 \rightarrow ^7F_5$ (C_2) transition at 542.8 nm is presented in Figure 11. These decay curves showed exponential behavior in most cases; decay times, $\tau_{1/e}$, were calculated from log plots as shown in Figure 11, including a small instrumental correction.

Figure 12 is a plot of the decay times ($\tau_{1/e}$) as a function of the Tb^{3+} concentration in Y_2O_3.

The decay times of the experimental points represented in Figure 12 are also listed in Table I.

Table I. $\tau_{1/e}$ (ms) for 542.8 nm, 544.4 nm, 550.7 nm and 552.3 nm peaks of Y_2O_3:Tb^{3+}.

Conc. Tb^{3+} (Mol %)	C_2 542.8 nm	S_6 544.4 nm	550.7 nm	552.3 nm
0.1	1.8	5.6	2.0	2.7
0.3	1.7	5.2	2.1	2.6
0.7	1.7	5.8	2.0	2.3
1	1.6	4.1		
3	1.7	2.2		
6	1.0	1.2		
10	0.8	0.9		

Table II. Parameters for decay curves represented in Figure 11.

Parameter	542.8 nm (C_2)	544.4 nm (S_6)
τ_r (ms)	1.74	5.98
A	0.020	0.353
γ	1.83	1.36

The experimental results for 542.8 nm and 544.4 nm peaks shown in Fig. 12 were fitted to curves, which can be written as:[1,18]

$$\tau_{1/e} = \frac{\tau_r}{1 + A\tau_r c^\gamma}, \qquad [5]$$

where τ_r is the radiative decay time (in ms) and the second term in the denominator representing the radiationless decay, in which c is the concentration of Tb^{3+} in % and A and γ are parameters that were fitted to the measured time constants. The parameters that were obtained by a least squares fit are listed in Table II.

The results presented in Figure 12 and Tables I and II indicate that the radiative decay time of the 544.4 nm peak is 3.4 times longer than that for the 542.8 nm peak (at low Tb^{3+} concentrations). This is what one might expect if the 544.4 nm peak refers to Tb^{3+} at an S_6 site and the 542.8 nm peak refers to Tb^{3+} at a C_2 site. The S_6 site has inversion symmetry, which forbids direct electric dipole transitions, but magnetic dipole transitions are possible for this symmetry, which yield usually longer decay times. We conclude therefore that the decay measurements support the assignment of the 542.8 nm and 544.4 nm peaks to $^5D_4 \rightarrow ^7F_5$ (C_2) and $^5D_4 \rightarrow ^7F_5$ (S_6) transitions respectively.

Table I also lists decay times for the other two strong peaks in the $^5D_4 \rightarrow ^7F_5$ transition cluster of Y_2O_3:Tb^{3+}, viz. the doublet at 550.7 nm and 552.3 nm. The decay times are between the values obtained for the peaks at 542.8 nm and 544.4 nm, indicating that the first mentioned doublet is a mixture of C_2 and S_6 type transitions. This is also confirmed in Figure 5a, showing that the concentration effect is stronger for the 552.3 nm peak than that for the 550.7 nm peak. So, the S_6-content in the 552.3 nm peak is higher and thus leads to a somewhat longer decay time.

Analysis with STEM.— As mentioned in the Experimental section, the TEM in our laboratory has the possibility to record panchromatic images as represented in Figure 3d and to measure CL spectra. These spectra can be recorded at temperatures from 102 K to 303 K. Figure 13 shows the CL spectra of 3% Y_2O_3:Tb^{3+} at 102 K and 303 K recorded at 200 keV.

Figure 13 indicates that the spectrum at 102 K has sharper peaks because of less vibronic broadening; moreover, the ratio $I_{542.8}/I_{544.4}$
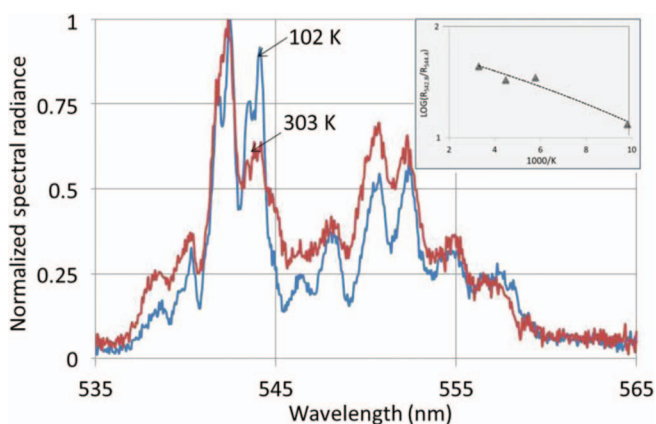
Figure 13. CL spectra of 3% Y_2O_3:Tb^{3+} at 102 K and 303 K in TEM. Spectra have been normalized to unity at 542.8 nm. For reasons of clarity, spectra at 173 K and 223 K with intermediate radiance values have been omitted: the peak values of the 544.4 nm line were between those of 102 K and 303 K. The inset is a plot of LOG($I_{542.8}/I_{544.4}$) versus 1000/K.
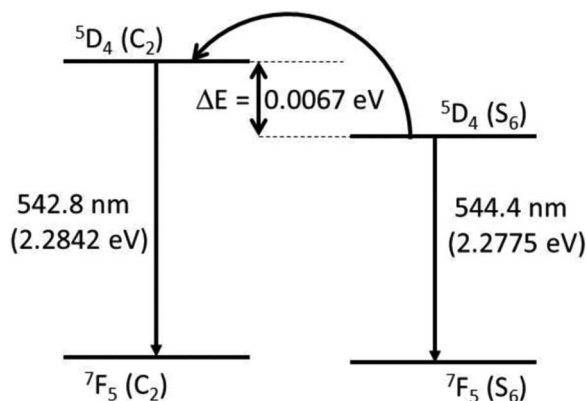
Figure 14. Mechanism of electron transfer from $^5D_4$ (S_6) to $^5D_4$ (C_2); energy levels are not on scale for reasons of clarity.

Figure 15. CL image of 1% Y_2O_3:Tb^{3+} recorded in FESEM at 10 kV. The scan speed of this image was 20.2 s/frame.

increases with temperature. This phenomenon indicates that the electron transfer from Tb^{3+} at S_6 to Tb^{3+} at C_2 is much less at low temperature than at room temperature. Another interesting feature of Figure 13 is the increase of the spectral radiance between 545 nm and 552 nm with temperature. This may also be attributed to vibronic broadening and thus, it is another indication that detection of the many hidden lines in the $^5D_4 \rightarrow ^7F_4$ transition cluster will be impossible without further lowering of the temperature. Finally, the low temperature spectrum in Figure 13 indicates that the peaks at 542.8 nm and 544.4 nm are doublets. This feature has not been analyzed in the present study. Since our equipment does not enable lower temperatures than 102 K, we are currently trying to improve the signal to noise ratio. Results of this study will be published as soon as they have been completed.

The inset of Figure 13 is an Arrhenius plot of the ratio $I_{542.8}/I_{544.4}$, in which $LOG(I_{542.8}/I_{544.4})$ is plotted against 1000/K. Such an analysis is obvious, because the ratio $I_{542.8}/I_{544.4}$ refers to the rate of populating and depopulating energy levels. The activation energy calculated from this plot is 0.005 eV. The accuracy of this value is not particularly high, but the order of magnitude is equal to the energy difference between the 542.8 nm and 544.4 peaks, shown in Figure 14, which visualizes the mechanism of the above mentioned electron transfer from the S_6 to C_2 Tb^{3+} ion.

The energy difference between the $^5D_4$ (S_6) and $^5D_4$ (C_2) levels, being 0.0067 eV, has been calculated from the wavelengths of the indicated spectral transitions. When the temperature of the crystal is 78 K, the energy gap of 0.0067 eV can be bridged and electrons can be promoted via phonon assistance from the $^5D_4$ (S_6) to the $^5D_4$ (C_2) level. The higher the temperature the more electrons will be promoted. This mechanism explains the change of the spectra with temperature in Figure 13. The low temperature spectrum in Figure 13 was recorded at 102 K, which is slightly higher than the theoretical onset of 78 K. In other words, it is to be expected that at 102 K already a few electron have been promoted. This may also be concluded from Figures 6 and 9, because for a concentration of 0.1% Tb^{3+} electron transfer from Tb^{3+} (S_6) to Tb^{3+} (C_2) is virtually impossible. At that condition $I_{542.8}/I_{544.4}$ would be 0.97, whereas Figure 13 already indicates a larger value of about 1.1 for this ratio.

Decay analysis with FESEM.— Figure 15 is a CL-image of nanosized Y_2O_3:Tb^{3+} particles on a C-substrate. The smearing of the image is due to the rather long decay time of the Tb^{3+} ions. The CL-detector only enables the recording of panchromatic images, which implies that the decay times evaluated with the FESEM are "overall" decay times.

The bright comets in Figure 15 refer to small clusters of nano particles while the faint comets are from individual particles as shown in Figure 3a. For Tb^{3+} concentrations > 0.3% the gray scale in the tail of a comet varied exponentially. In the case of low Tb^{3+} concentrations
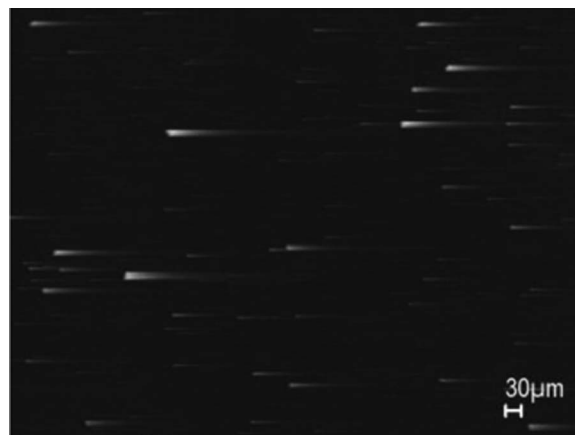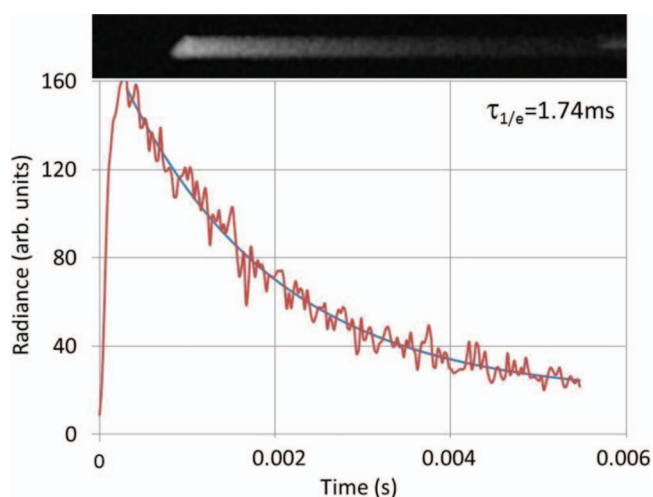
Figure 16. Brightness decay of small cluster of Y_2O_3:Tb^{3+} particles with 0.7% Tb^{3+}; CL-image on top. Beam voltage of FESEM 10 kV.

deviations were observed, which are caused by different degrees of saturation of excited levels. This has been explained in our previous reports.[1,23] By using the Image J software the overall decay times of the FESEM images were determined. An example is shown in Figure 16.

Curve fitting to a one-exponential function was done with a least squares algorithm, in which the background brightness was accounted for. Results for the various concentration of Tb^{3+} are summarized in Table III.

In the case of Y_2O_3:Tb^{3+} with 0.1% Tb^{3+} the saturation was particularly strong. For this Tb^{3+} concentration the light distribution in the comets could be represented by two exponentials with

Table III. Decay times of Y_2O_3:Tb^{3+} particles evaluated form CL-images recorded with FESEM.

Conc. Tb^{3+} (Mol %)	$\tau_{1/e}$ (ms)
0.1	0.13 & 1.8*
0.3	1.7
0.7	1.8
1	1.7
3	1.7

*Comets were represented by two exponentials.

Table IV. Published decay times ($\tau_{1/e}$) of $^5D_4 \rightarrow {}^7F_5$ transition of Y_2O_3:Tb^{3+}.

$\tau_{1/e}$ (ms)	Conc. Tb^{3+} (Mol %)	Level/transition	Excitation method	Reference
2.19	0.1	$^5D_4 \rightarrow {}^7F_5$	PL: 266 nm	7
2.15	1	$^5D_4 \rightarrow {}^7F_5$	PL: 266 nm	7
2.67	1	545 nm	PL: 276 nm	4
1.09	5	545 nm	PL: 276 nm	4
1.16	1	549 nm	laser	28
1.13	2	549 nm	laser	28
0.85	4	549 nm	laser	28
0.84	1	$^5D_4$ level	PL: 270 nm	27
1.44	5	$^5D_4$ level	PL: 270 nm	27
0.77	10	$^5D_4$ level	PL: 270 nm	27
2.8	2	544.5 nm	PL: 310 nm	26
0.8	6.8	544.5 nm	PL: 310 nm	26
1.02 & 2.15	8	543 nm	PL: 254 nm	10
0.92	3?	544 nm	PL: 305 nm	9
1.11	3	542 nm	Laser	29

decay times as indicated in Table III. The "overall" decay times in Table III determined from the FESEM-images match with the decay times determined for the $^5D_4 \rightarrow {}^7F_5$ (C_2) at 542.8 nm, listed in Table I. In other words, the contribution of the S_6 transitions with longer persistence can be neglected in the CL-images, because of the stronger saturation of the $^5D_4$ (S_6) level(s) in Y_2O_3:Tb^{3+}. We shall discuss this issue in more detail in the next section.

Discussion

In CL spectrum section we have already noticed that the variation of the Tb^{3+} concentration is clearly observable in the $^5D_4 \rightarrow {}^7F_5$ (Figure 5a) and $^5D_4 \rightarrow {}^7F_3$ (Figure 5c) transition clusters, but hardly in the $^5D_4 \rightarrow {}^7F_4$ (Figure 5d) and $^5D_4 \rightarrow {}^7F_6$ (Figure 5b) clusters. For the first two transition clusters $\Delta J = +1$ and $\Delta J = -1$ respectively, whereas $\Delta J = 0$ for $^5D_4 \rightarrow {}^7F_4$ and $\Delta J = +2$ for $^5D_4 \rightarrow {}^7F_6$. The latter transition cluster is a so-called forced electric-dipole transition, which is magnetically forbidden.[3] A small concentration effect is noticeable for the peak at 583.2 nm in the $^5D_4 \rightarrow {}^7F_4$ transition cluster (Figure 5d). When Tb^{3+} is at an S_6 site it may display magnetic dipole transitions with $\Delta J = 0, \pm 1$. So, it can be concluded that assigning the 544.4 nm peak in the $^5D_4 \rightarrow {}^7F_5$ cluster and the 630.1 nm and 637.8 nm peaks in the $^5D_4 \rightarrow {}^7F_3$ transitions cluster as S_6 transitions and the virtual absence of S_6 transitions in the $^5D_4 \rightarrow {}^7F_6$ transition cluster are in line with the selection rules. The 547.0 nm and 548.6 nm peaks in the $^5D_4 \rightarrow {}^7F_5$ transition cluster (Figure 5a and Figure 6) may also be assigned as S_6 transitions. Due to substantial overlapping of neighboring peaks, we did not investigate these peaks in detail. Figure 13 shows a pronounced sharpening of these peaks by lowering the temperature to 102 K. As mentioned in Decay section the longer $\tau_{1/e}$ decay time for the S_6 transition at 544.4 nm as compared to the C_2 transition at 542.8 nm is in line with what may be expected from magnetic- and electric-dipole transitions respectively. Further support for the above assignment can be deduced from Figure 7, which shows a stronger saturation effect for the 544.4 nm peak than that for the 542.8 nm peak. From our findings, which are summarized in Figure 14, it can be concluded that the phonon assisted transition from $^5D_4$ (S_6) to $^5D_4$ (C_2) is symmetry-allowed, whereas the reverse route, which is energetically favorable and does not need phonon assistance, is symmetry-forbidden.

We mentioned in the introduction section that because of the equivalence of ion radii between Y^{3+} and Tb^{3+} it is obvious to assume that there are three times less Tb^{3+} ions at S_6 than at C_2 sites in the Y_2O_3 lattice. The saturation effect at continuous irradiance with an electron beam having a current density j can be estimated by using a simple equation that has been derived by Bril and Kröger[25]:

$$R_i = \frac{j\eta_i}{1 + j\eta_i\tau_i/N_i}, \qquad [6]$$

where R_i is the radiance of transition i ($= {}^5D_4 \rightarrow {}^7F_5$ (C_2) or $^5D_4 \rightarrow {}^7F_5$ (S_6)), η_i is the efficiency of transition i at low current density and N_i is the number of Tb^{3+} ions per cm^3 at C_2 or S_6. If $\eta_{C2} \approx \eta_{S6}$ and because $N_{C2} = 3N_{S6}$ and moreover $\tau_{C2} < \tau_{S6}$, then it is clear from Eq. 6 that the effect of saturation by increasing j is more pronounced for the S_6 transition. This consideration also explains that the CL images of the FESEM, in which effective current densities of about 1A/cm^2 are rife,[1] lack longer persistence S_6-light.

In spite of the extensive literature on the luminescence of Y_2O_3:Tb^{3+}, it is not easy to make a comparison between the results of this work and those of other authors. An important reason is the resolution of the spectrometer. The published spectra of bulk and nanosized Y_2O_3:Tb^{3+} show usually only two peaks for the various $^5D_4 \rightarrow {}^7F_J$ transition clusters.[4–10,12–14,26,27] As can be seen in Figure 5a for the $^5D_4 \rightarrow {}^7F_5$ cluster, these two peaks must be (1) a fusion between the 542.8 nm and 544.4 nm peaks, being named here "peak A", in the literature sometimes indicated by wavelength (543 nm, 544 nm, 545 nm or even 549 nm) or as the $^5D_4 \rightarrow {}^7F_5$ transition, and (2) a fusion of the peaks at 551.0 nm and 552.6 nm, being named "peak B". The ratio of the maximum radiance (A/B) of these fused peaks is found to be 1.2–1.4 in the literature. The same ratio is found by us after the fusing procedure: this ratio decreases slightly upon increasing the Tb^{3+} concentration. The fusion peak A is thus a mixture of the C_2 and S_4 transitions. Figure 5a and Table I indicate that there is also S_6 content in the fusion peak B.

Table IV summarizes decay times of the $^5D_4 \rightarrow {}^7F_5$ transition of Y_2O_3:Tb^{3+} published by other authors.

The data listed in Table IV show that $\tau_{1/e}$ decreases when the Tb^{3+} concentration is increased and that there are substantial deviations between the various authors. The decrease of the decay time at larger concentration is also shown in Figure 12: for the 544.4 nm peak more pronounced than for the 542.8 nm peak. The decay data of Table IV do not refer to the 542.8 nm or 544.4 nm peaks of Fig. 5a, but rather to the fusion peak A, defined above. The data can therefore not be compared directly to our results as summarized in Table I, but indirectly it is possible. From Figure 9a it can be derived that $I_{542.8}/I_{544.4}$ is 1.6 for 3% Y_2O_3:Tb^{3+}, which implies that when the peaks are fused together, the C_2 content is 1.6 times larger than the S_6 content. For 3% Y_2O_3:Tb^{3+} the overall decay time of this fusion peak would be 1.8 ms, which agrees quite well with the data in Table IV.

Conclusions

Recording the CL spectra of nanosized cubic Y_2O_3:Tb^{3+} with a high resolution spectrometer enabled the identification of peaks that are related to Tb^{3+} at C_2 and S_6 sites in the Y_2O_3 crystal. From our literature search we could not find that others have assigned this previously. The critical distance for energy transfer from Tb^{3+} ions

at S_6 lattice sites to Tb^{3+} ions at C_2 lattice sites, $D_{Tb^{3+}}^{Crit}$, was found to be 1.7 nm. This distance is identical to that in Y_2O_3:Eu^{3+}, which is not unexpected, because Eu^{3+} and Tb^{3+} have the same ion size and corresponding 4f-4f and 4f-5d (in Tb^{3+}) relaxations. At a temperature <78 K the phonon assisted transfer of energy from $^5D_4$ (S_6) to $^5D_4$ (C_2) stops in Y_2O_3:Tb^{3+} with a high concentration of Tb^{3+}; when the temperature is >78 K, this transfer is enabled due to phonon assistance.

The decay times of the $^5D_4 \rightarrow ^7F_5$ (C_2) and the $^5D_4 \rightarrow ^7F_5$ (S_6) transitions decrease at high Tb^{3+} concentration; this effect starts for S_6 at lower concentrations than for C_2. Decay times determined with the FESEM at very high current density of about 1 A/cm^2 are equal to the decay times of the $^5D_4 \rightarrow ^7F_5$ C_2 transition determined at a current density of about 0.5 mA/cm^2. The contribution of longer persistence S_6 transitions to CL-images in the FESEM is minimized because of the strong saturation of these transitions.

Finally, we would like to stress that the conclusions obtained from this study are of a preliminary character and need to be updated with more detailed studies at low temperature, i.e. is the splitting of the lines at 542.8 nm and 544.4 nm at low temperature shown in Figure 13 real? Currently we are studying the PL and CL from nanosized Y_2O_3:Tb^{3+} particles at room temperature and low temperature to answer this question and to get a better insight into the transfer of energy after excitation of the lattice (CL) or target levels (PL) in this phosphor.

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