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# Comparison of methane combustion mechanisms using shock tube and rapid compression machine ignition delay time measurements

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ABSTRACT: Methane is the major component of natural gas, which is one of the most widely used fuels. Large amount of shock tube (ST) and rapid compression machine (RCM) ignition delay measurements are available in the literature for validating its detailed combustion mechanisms. A large set of experimental data was collected for methane combustion: ignition studies in STs (4939 data points in 574 datasets) and in RCMs (582/69). In total, 5521 data points in 643 datasets from 76 publications were collected covering wide ranges of temperature  $T$ , pressure  $p$ , equivalence

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3 ratio  $\phi$  and diluent concentration. For a quantitative assessment of methane combustion models, a  
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5 least-squares-function is used to show the agreement between measurements and simulations. 13  
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7 recent methane combustion mechanisms were tested against these experimental data, and the  
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9 dependence of their predictions on the types of experiments and the various experimental  
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11 conditions was investigated. The mechanism comparison results show that most mechanisms could  
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13 reproduce well the experimental ignition delay times (IDTs) measured in STs. IDTs measured in  
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15 RCMs and STs at low temperatures (below 1000 K) could also be well predicted by several  
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17 mechanisms. SanDiego-2014, Caltech-2015, Aramco-II-2016 and Glarborg-2018 were found to  
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19 be the most accurate mechanisms for the simulation of methane combustion under ST experimental  
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21 conditions, while Aramco-II-2016 had the smallest prediction error under RCM conditions. Local  
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23 sensitivity analysis was carried out to determine the effect of reactions on the simulation results  
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25 obtained under given experimental conditions and to identify the critical reaction steps for  
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27 improving the methane combustion models.  
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## 1. Introduction

Large amount of combustion experimental data was published in the last decades, with continuously improved measurement accuracy. However, most mechanisms were originally developed based on data obtained under narrow ranges of experimental conditions, and the subsequent validation studies of published mechanisms are rare. Therefore, we have investigated a series of detailed reaction mechanisms for the combustion of hydrogen <sup>1</sup>, synthesis gas <sup>2</sup>, methanol <sup>3</sup> and ethanol <sup>4</sup>. These studies led to building up a comprehensive experimental database <sup>5</sup>, and also these works demonstrated that there are excellent mechanisms for the combustion of these fuels. It was also shown that some of the widely used mechanisms poorly reproduce many of the experimental data points. Furthermore, even the best mechanisms may perform surprisingly badly under some specific conditions. This conclusion indicates that it is meaningful to systematically evaluate the combustion mechanisms also for further fuels.

Due to the accumulating knowledge and understanding in combustion chemistry and gas kinetics, and using the increasing power of computers and simulation codes, more and more mechanisms were generated in the recent decades. The study of Lu and Law <sup>6</sup> indicated that in the last twenty years not only the number of published combustion mechanisms increased, but also there was a significant increase in the numbers of species and reactions in the new mechanisms. However, in many cases the performance of these new mechanisms was not investigated under a wider range of conditions.

One of the most important fuels is natural gas, which is widely utilized for electricity production, heating and transport. The main ingredient of natural gas is methane, and therefore methane combustion is one of the practically most important chemical processes. Knowing the combustion kinetics of methane better, more efficient natural gas engines and gas turbines can be designed.

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3 Ignition delay time is one of the most important characteristic properties of the combustion of  
4 methane containing gas mixtures. Majority of such experiments was carried out in STs, but some  
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6 others also in RCMs. Jach et al.<sup>7</sup> recently published a paper on the comparison of the performance  
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8 of several hydrocarbon combustion mechanisms in reproduction of IDTs of C<sub>1</sub>–C<sub>4</sub> hydrocarbons,  
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10 but this study was not comprehensive for methane and the tests were based only on ST  
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12 measurements. Baigmohammadi et al.<sup>8</sup> collected experimental data on the ignition of C<sub>1</sub>–C<sub>2</sub>  
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14 hydrocarbons covering a wide range of experimental conditions (temperature ~800–2000K,  
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16 pressure ~1–80 bar, equivalence ratio ~0.5–2, dilution ~75–90%), and compared the simulation  
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18 results obtained by using the C<sub>3</sub>-NUIG mechanism with the experimental data. However, the  
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20 amount of data collected for methane ignition was limited and some regions of experimental  
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22 conditions were not covered, such as initial temperatures above 2000 K, equivalence ratios below  
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24 0.5 and above 2.0, and dilution ratios below 75%. Jach et al.<sup>9</sup> investigated the performance of 15  
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26 detailed reaction mechanisms for the reproduction of ignition delay times of C<sub>2</sub>–C<sub>6</sub> alkenes and  
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28 acetylene. Lee et al.<sup>10</sup> tested seven widely used syngas/biogas mechanisms based on a limited  
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30 amount of IDT experimental data in a wide condition range (907–2030K, 1.24–70 atm), and  
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32 suggested modified rate parameters for reactions  $H + O_2 (+CO_2) = HO_2 (+CO_2)$  and  $CH_4 + OH =$   
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34  $CH_3 + H_2O$ .  
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43 In this paper the general methodology that we have previously developed and applied for the  
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45 comparison of combustion mechanisms of other fuels<sup>1–4</sup> is employed for methane combustion  
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47 based on ST and RCM ignition delay measurements. To support related research in the future, a  
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49 large amount of experimental data from STs and RCMs was collected in the ReSpecTh database  
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51 <sup>5</sup>, using the latest version of ReSpecTh Kinetics Data Format. Improvement of the method for  
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53 calculating the standard deviations of experimental datasets was implemented by considering both  
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3 the statistical and experimental errors. The performance of 13 widely used detailed combustion  
4 mechanisms was compared according to the reproduction of the ignition delays of methane, and  
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6 four OHEX submechanisms were compared.  
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10 Engineering computational fluid dynamics simulations require accurate mechanisms under  
11 specific conditions. This is one of the reasons why in this paper a quantitative assessment of the  
12 accuracy of the combustion mechanisms was carried out separately in various ranges of pressure,  
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14 temperature, equivalence ratio and diluent ratio. Special attention was paid to the performance of  
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16 the mechanisms at low temperatures ( $<1000\text{K}$ ) and the reproducibility of IDTs with different  
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18 lengths. Local sensitivity analysis was carried out for identifying the most important reactions for  
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20 the reproduction of IDTs, and the rate coefficients of these reactions used in the best mechanisms  
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22 were compared.  
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## 2. Methodology

Agreement of experimental data and simulation results is investigated here by using the following objective function:

$$E = \frac{1}{N} \sum_{i=1}^N E_i$$

and

$$E_i = \frac{1}{N_i} \sum_{j=1}^{N_i} \left( \frac{Y_{ij}^{\text{sim}} - Y_{ij}^{\text{exp}}}{\sigma(Y_{ij}^{\text{exp}})} \right)^2$$

where

$$Y_{ij} = \begin{cases} y_{ij} & \text{if } \sigma(y_{ij}^{\text{exp}}) \approx \text{constant} \\ \ln y_{ij} & \text{if } \sigma(\ln y_{ij}^{\text{exp}}) \approx \text{constant} \end{cases}$$

Here  $N$  is the number of datasets and  $N_i$  is the number of data points in the  $i$ -th dataset. A dataset contains those data points that were measured on the same apparatus at the same time under similar conditions except for one that was systematically changed. Values  $y_{ij}^{\text{exp}}$  and  $\sigma(y_{ij}^{\text{exp}})$  are the  $j$ -th data point and its standard deviation, respectively, in the  $i$ -th dataset. The corresponding simulated (modeled) value is  $Y_{ij}^{\text{sim}}$  obtained from a simulation using an appropriate detailed mechanism and simulation method. IDT measurement errors are typically relative ones (the scatter is proportional to the value of  $y_{ij}$ ), therefore we used the option  $Y_{ij} = \ln y_{ij}$ .

Error function values  $E_i$  belonging to dataset  $i$ , and  $E$  belonging to all considered  $N$  datasets are expected to be near unity if the chemical kinetic model is accurate, and the deviations of the measured and simulated results are caused by the scatter of the experimental data only. Note that due to the squaring in the definition of  $E$ , a twice as high deviation of the simulated and experimental values leads to a four times higher value of  $E$ . This objective function has been used

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3 in our previous studies for assessing the performance of combustion mechanisms in the estimation  
4 of rate parameters from experimental data, comparison of reaction mechanisms and mechanism  
5 optimization<sup>1-4,11-19</sup>.  
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10 In addition to the average error function  $E$ , the mean  $\sigma$ -normalized signed deviation  $D$  was used  
11 to characterize the behavior of the mechanisms:  
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$$14 \quad D = \frac{1}{N} \sum_{i=1}^N \frac{1}{N_i} \sum_{j=1}^{N_i} \frac{Y_{ij}^{\text{sim}} - Y_{ij}^{\text{exp}}}{\sigma(Y_{ij}^{\text{exp}})}$$

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17 using the same transformation  $y_{ij} \rightarrow Y_{ij}$  as above. In contrast to  $E$ , the sign of the difference  
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22  $Y_{ij}^{\text{sim}} - Y_{ij}^{\text{exp}}$  is maintained in the definition of  $D$ , therefore trends such as systematic under- or over-  
23 prediction are captured in the  $D$  values. This is meaningful, if the investigated model results are of  
24 the same type, like ignition delay time in this paper. However, mean signed deviation  $D$  cannot be  
25 used for the characterization of accuracy, since positive and negative deviations belonging to  
26 different data points can cancel each other out and the resulting averaged value would erroneously  
27 suggest good overall agreement. The  $D$  value plots may deliver a better understanding of the trends  
28 associated with changes of certain operating conditions and should be interpreted alongside with  
29 the corresponding  $E$  value plots.  
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41 It is possible to characterize the similarity of simulation results for a given data series obtained  
42 using two different mechanisms by calculating the Pearson correlation coefficients of local  
43 absolute deviations ( $D_i(j)$ ), which are defined as:  
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$$47 \quad D_i^a(j) = Y_{ij}^{\text{sim}_a} - Y_{ij}^{\text{exp}}$$

$$48 \quad D_i^b(j) = Y_{ij}^{\text{sim}_b} - Y_{ij}^{\text{exp}}$$



where simulation results  $Y_{ij}^{\text{sim},a}$  and  $Y_{ij}^{\text{sim},b}$  are calculated using reaction mechanisms  $a$  and  $b$ , respectively. Let  $\overline{D_i^a}$  and  $\overline{D_i^b}$  denote the mean of values  $D_i^a(j)$  and  $D_i^b(j)$ . The Pearson correlation coefficient for dataset  $i$  can be calculated by the formula:

$$C_i^{ab} = \frac{\sum_j^{N_i} (D_i^a(j) - \overline{D_i^a})(D_i^b(j) - \overline{D_i^b})}{\sqrt{\sum_j^{N_i} (D_i^a(j) - \overline{D_i^a})^2} \sqrt{\sum_j^{N_i} (D_i^b(j) - \overline{D_i^b})^2}}$$

In the last step, the correlation coefficients calculated for all  $N$  datasets are averaged:

$$C^{ab} = \frac{1}{N} \sum_{i=1}^N C_i^{ab}$$

A discussion on the comparisons of the performance of mechanisms using these correlation coefficients can be found in references <sup>1, 2</sup> and <sup>9</sup>.

The standard deviation of a dataset was estimated based on the statistical scatter of the data ( $\sigma_{\text{stat},i}$ ) and the reported experimental uncertainty ( $\sigma_{\text{exp},i}$ ), in a way similar to the approach used in <sup>3</sup>:

$$\sigma_{ij} = \sqrt{\sigma_{\text{stat},i}^2 + \sigma_{\text{exp},ij}^2}$$

The statistical noise of a data series ( $\sigma_{\text{stat},i}$ ) was determined by finding an optimal trendline ( $Y^{\text{fit1}}(x)$ ) for the transformed experimental data series ( $Y_{ij}^{\text{exp}} = Y_i^{\text{exp}}(x_{ij}), j=1, \dots, N_j$ ) using code MinimalSplineFit <sup>20</sup>. The idea behind this method is that the transformed values of an experimental dataset ( $Y_{ij}^{\text{exp}}$ ) versus the changing condition variable ( $x$ , e.g. inverse temperature, equivalence ratio) can be considered as a smooth function with a symmetrically distributed noise added. If these data are fitted with flexible functions ( $y_i^{\text{fit1}}(x_j)$ ), such as polynomials or spline functions, of increasing complexity (*i.e.* with more parameters, e.g. higher order, more knots), the fits first reconstruct the underlying smooth function. This way the error reduces steeply, whereas later only the remaining noise is fitted, which cannot be captured efficiently. As a result, an optimal fitting

curve can be determined, which efficiently approximates the noise-free experimental data series, thus it can be used to give an unbiased estimate to the variance of the statistical noise ( $\sigma_{\text{stat}}^2$ ):

$$\sigma_{\text{stat},i}^2 = \frac{\sum_{j=1}^{N_i} (Y_{ij}^{\text{exp}} - Y_i^{\text{fit1}}(x_{ij}))^2}{N_{\text{DOF},i}}$$

Here  $Y_i^{\text{fit1}}(x_{ij})$  is the trendline value that corresponds to the experimental point  $Y_{ij}^{\text{exp}}$ ,  $N_{\text{DOF},i} = N_i - n_{\text{fit1},i}$  is the number of degrees of freedom, and  $n_{\text{fit1},i}$  is the number of parameters in the optimal fitting function. More details are available in ref. <sup>20</sup>.

For the ignition delay measurements, the experimental uncertainty could be expressed <sup>21</sup> as:

$$\sigma_{\text{exp},ij} = \frac{dy_{ij}^{\text{exp}}}{y_{ij}^{\text{exp}}}$$

Here  $y_{ij}^{\text{exp}}$  and  $dy_{ij}^{\text{exp}}$  are the experimental IDT and the corresponding uncertainty of  $i$ -th data point in  $j$ -th dataset.

In the present study, we used the reported experimental uncertainty of IDT whenever it was available in the original article. However, in several publications the uncertainty of IDT was not provided, but the authors indicated the uncertainty of temperature and pressure. In these cases, we derived the IDT uncertainty from the available  $P$  and  $T$  uncertainty. Usually the relationship between IDT, and pressure and temperature can be expressed by equation:

$$y_{ij}^{\text{fit2}} = A_{\text{fit2},i} P_{ij}^{a_{\text{fit2},i}} e^{\frac{b_{\text{fit2},i}}{T_{ij}}}$$

Here  $y_{ij}^{\text{fit2}}$  is the approximated IDT obtained by two-variate least squares fitting,  $P_{ij}$  and  $T_{ij}$  are the experimental pressure and temperature,  $A_{\text{fit2},i}$  is the fitted pre-exponential factor, while  $a_{\text{fit2},i}$  and  $b_{\text{fit2},i}$  are fitted parameters related to pressure and temperature, respectively. Description of the fitting process is available in Part 2 of the Supplementary Material. Derivation of the function above yields:

$$dy_{ij}^{\text{exp}} = \sqrt{(A_{\text{fit}2,i} a_{\text{fit}2,i} e^{\frac{b_{\text{fit}2,i}}{T_{ij}}} P_{ij}^{a_{\text{fit}2,i}-1})^2 + \frac{1}{T_{ij}^2} (A_{\text{fit}2,i} b_{\text{fit}2,i} e^{\frac{b_{\text{fit}2,i}}{T_{ij}}} P_{ij}^{a_{\text{fit}2,i}})^2}$$

If the uncertainty of either temperature or pressure is known, then the method can also be used for one variable only. The procedure described above follows the approach of Zhang et al.<sup>21</sup> for the calculation of the experimental uncertainty of IDT measurements. This procedure results in different standard deviation  $\sigma_i$  for each data point in some datasets, which is available in the Supplementary Material.

If the experimental uncertainty of IDT, temperature, or pressure was not reported by the authors for a dataset, then the standard deviation of the dataset was considered to be identical to  $\sigma_{\text{stat},i}$ . In the cases of some measurements, the standard deviation  $\sigma_{ij}$  calculated in this way was unrealistically low. Therefore, it was replaced by a minimal assumed standard deviation, which was 10% relative error for IDTs.

However, it is possible that some experimental data have large systematic uncertainty that could not be captured by either the reported experimental uncertainty or the statistical scatter. This is why data points that could not be reproduced within  $3\sigma$  error by any of the mechanisms were excluded from the mechanism comparison study, thus not all collected data were used at the assessment of the mechanisms. Also, the data were taken into account with different weights, since the equations for the calculation of  $E$  and  $D$  include that more uncertain data were considered with lower weight.

### 3. The investigated mechanisms

Our aim was to test widely used methane combustion mechanisms published in the last two decades. In the forthcoming discussions, an identifier of each mechanism is used, which combines the name of the author or research group and the year of publication.

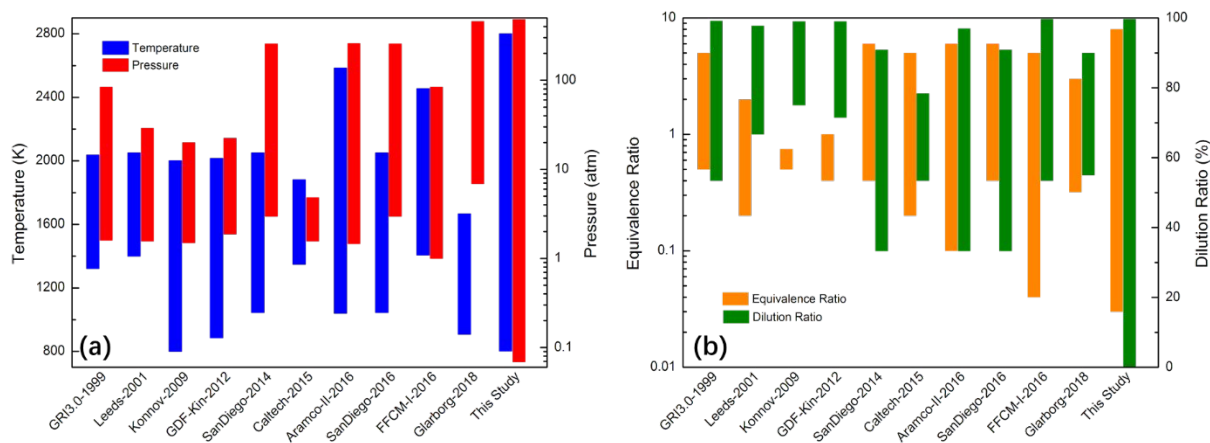
**Table 1.** General properties of the collected reaction mechanisms: number of species and reactions involved, the possible inert bath gas (aside from N<sub>2</sub>), and the conditions of methane ignition delay measurements at which the mechanisms were originally validated.

No.	Mechanisms ID	Ref.	Reactions/ Species Number	Diluents	Development and validation conditions			
					Temperature / K	Pressure / atm	$\phi$	Dilution Ratio / %
1	GRI3.0-1999	<sup>22</sup>	325 / 53	Ar/-	1323 - 2036	1.6 - 83.9	0.5 - 5.01	53.4 - 99.16
2	Leeds-2001	<sup>23</sup>	175 / 37	Ar/-	1400 - 2050	1.56 - 29	0.2 - 2	66.7 - 97.8
3	USC-II-2007	<sup>24</sup>	784 / 112	Ar/He	No validation based on CH <sub>4</sub> - IDT experiment.			
4	Konnov-2009	<sup>25</sup>	1231 / 129	Ar/-	800 - 2000	1.5 - 20	0.5 - 0.75	75.05 - 99
5	GDF-Kin-2012	<sup>26</sup>	1144 / 141	Ar/He	886.85 - 2015	1.87 - 22.38	0.4 - 1	71.5 - 99
6	SanDiego-2014	<sup>27</sup>	247 / 50	Ar/He	1045 - 2050	2.96 - 256.6	0.4 - 6	33.3 - 90.9
7	CRECK-2014	<sup>28</sup>	2642 / 107	Ar/He	No validation based on CH <sub>4</sub> - IDT experiment.			
8	Caltech-2015	<sup>29</sup>	1156 / 192	Ar/-	1348 - 1881	1.56 - 4.83	0.2 - 5	53.4 - 78.4
9	Aramco-II-2016	<sup>30</sup>	2716 / 502	Ar/He	1040 - 2584	1.46 - 260	0.1 - 6	33.3 - 97
10	SanDiego-2016	<sup>31</sup>	268 / 57	Ar/He	1045 - 2050	2.96 - 256.6	0.4 - 6	33.3 - 90.9
11	FFCM-I-2016	<sup>32</sup>	291 / 38	Ar/He	1408.1 - 2454	1 - 83.9	0.04 - 5.01	53.4 - 99.16
12	Konnov-2017	<sup>33</sup>	1236 / 107	Ar/He	No validation based on CH <sub>4</sub> - IDT experiment.			
13	Glarborg-2018	<sup>34</sup>	1407 / 154	Ar/He	908 - 1665	6.9 - 456	0.32 - 3	55 - 90

Two mechanisms (GRI3.0-1999<sup>22</sup> and Leeds-2001<sup>23</sup>) were originally developed for natural gas combustion, while the other mechanisms were elaborated for the combustion of hydrocarbons or oxygenates<sup>24-34</sup>, but have also been used to interpret methane combustion data. In the order of publishing year, **Table 1** lists all the 13 mechanisms and provides further information about size

and included diluents. Although the Aramco mechanism was continuously updated in the recent years, the methane part was updated in 2016 for the last time, therefore this version is used in the present study. **Figure 1** shows the condition ranges (temperature, pressure, equivalence ratio, and diluent ratio) of validating measurements of methane ignition delays used for the development of these mechanisms. **Fig.1** indicates that these mechanisms have not been validated under several specific conditions, such as at low pressure ( $< 1$  atm) and low diluent ratio ( $< 33.3\%$ ). The performance of the 13 mechanisms under these conditions will be presented in Section 6.1.

All mechanisms can handle  $N_2$  and Ar bath gases, while only four mechanisms do not include helium as a possible bath gas. For each mechanism, their own thermochemical data were used as published online and/or provided by the authors.



**Figure 1.** Condition (temperature, pressure, equivalence ratio, and diluent ratio) ranges of methane IDT experimental data originally used for the validation of the mechanisms. The last columns show the experimental condition ranges used for testing the mechanisms in this study. Mechanisms USC-II-2007, CRECK-2014, and Konnov-2017 are not included as they were not validated for methane ignition delay data by their developers

#### 4. Collection of experimental data

The combustion characteristics of mixtures containing methane have been studied extensively. In this work we consider only those experiments in which the reactant mixture contains methane, but no larger hydrocarbons or oxygenated species. This means that mixtures of methane and H<sub>2</sub> or CO are investigated in this paper, but no mixtures containing ethane or methanol. Having this restriction on the initial chemical composition, the datasets to be considered are still numerous, close to two thousand. Therefore, we decided to focus only on ignition delay time measurement in this study. An extensive literature review was performed, and 574 datasets were collected from ST and 69 datasets from RCM measurements, including 5521 data points in total.

The collection of IDT measurements in STs<sup>35–103</sup> covers a wide range of conditions. The initial temperature and pressure were varied in the range of 803–2800 K and 0.069–481.4 atm, respectively; the equivalence ratio was changed between 0.03 and 8.0; the mole fraction of diluent concentration was within the interval of 0–99.7%. In some cases, several different experimental IDTs were deduced from the same experiment in such a way that different profiles, such as pressure, excited OH radical, or other species profiles were measured simultaneously. In the present study, we added all these kinds of IDT measurements to the database but used only one of them for mechanism comparison. The priority order of IDT definitions was based on excited OH, excited CH, pressure, and other species. Therefore, less data were utilized here than actually collected and encoded in XML files, but the additional experimental data are also available for the combustion community for further studies. Also, measurements with helium bath gas were not used, because there were relatively few such measurements and also we wanted to make a comparison of all mechanisms using the same sets of measurements. Finally, 3403 data points in 484 datasets extracted from 69 publications were used for testing the mechanisms.

**Table 2.** A summary of methane experimental data used in the mechanism comparison by type of measurement and experimental facility. The table includes the numbers of datasets and data points used, ranges for pressure  $p$ , temperature  $T$ , equivalence ratio  $\phi$ , and the combinations of fuels and diluents together with the number of corresponding data points. PRR stands for pressure rise rate.

Type of measurement	No. of datasets	No. of data points	$T / \text{K}$	$p / \text{atm}$	$\phi$	Fuels	Diluents
ST without PRR	387	3557	803 – 2800	0.069 – 481.4	0.03 – 8	CH <sub>4</sub> - <b>2997</b> CH <sub>4</sub> /H <sub>2</sub> - <b>432</b> CH <sub>4</sub> /CO - <b>57</b> CH <sub>4</sub> /H <sub>2</sub> /CO - <b>71</b>	Ar - <b>2259</b> Ar/N <sub>2</sub> - <b>86</b> Ar/N <sub>2</sub> /CO <sub>2</sub> - <b>25</b> Ar/CO <sub>2</sub> - <b>53</b> Ar/CO <sub>2</sub> /H <sub>2</sub> O - <b>33</b> Ar/H <sub>2</sub> O - <b>7</b> N <sub>2</sub> - <b>879</b> N <sub>2</sub> /CO <sub>2</sub> - <b>27</b> N <sub>2</sub> /CO <sub>2</sub> /H <sub>2</sub> O - <b>39</b> N <sub>2</sub> /H <sub>2</sub> O - <b>23</b> CO <sub>2</sub> - <b>39</b> No diluent - <b>87</b>
ST with PRR	97	846	1020 - 2150	0.987 – 44	0.3 - 2.0	CH <sub>4</sub> - <b>595</b> CH <sub>4</sub> /H <sub>2</sub> - <b>251</b>	Ar - <b>514</b> N <sub>2</sub> - <b>258</b> N <sub>2</sub> /CO <sub>2</sub> - <b>74</b>
RCM	69	582	869.9 - 1200	9.87 – 156.62	0.3 – 2.0	CH <sub>4</sub> - <b>467</b> CH <sub>4</sub> /H <sub>2</sub> - <b>75</b> CH <sub>4</sub> /CO - <b>16</b> CH <sub>4</sub> /H <sub>2</sub> /CO - <b>24</b>	Ar - <b>257</b> N <sub>2</sub> - <b>21</b> Ar/N <sub>2</sub> - <b>304</b>

As for the conditions of RCM experiments<sup>26,43,63,104–107</sup>, the ranges of temperature and pressure were 869.9 – 1200 K, and 9.87 – 156.62 atm, respectively; equivalence ratio and diluent ratio were changed between 0.3 – 2.0 and 62.58 – 90%, respectively. All in all, 582 data points included in 68 datasets were extracted from 7 articles. All detailed information about the ST and RCM experiments can be found in **Tables A and B**, respectively, of the Supplementary.

An overview of the regions of initial conditions covered and diluents investigated is shown in **Table 2**. Although the conditions in the listed ranges are not represented uniformly, the provided numbers may serve as an outline for the ranges of conditions. The detailed list of data arranged in datasets with references is given in **Tables A and B** of the Supplementary Material.

## 5. Simulation of experiments

All the collected experimental data were encoded in ReSpecTh Kinetics Data Format v2.3 (RKDF2.3) <sup>108</sup> XML files. The RKD format is an XML data format for the storage of indirect combustion measurements and rate coefficient determinations by direct gas kinetics experiments and theoretical calculations. The RKD format is a modified and extended version of the PRIME Kinetics Data Format <sup>109</sup>. All the prepared XML files are available in the ReSpecTh Information System <sup>5</sup>.

The RKD files contain all information required for the simulation of the experiments, such as initial compositions, temperature, pressure and IDT definition. Usage of these files allowed the fully automatized run of thousands of simulations. In principle, the complete investigation of a mechanism against several thousand experimental data points can be carried out in a single run using these files and the Optima++ environment <sup>110</sup>. Both simulation packages FlameMaster <sup>111</sup> (FM) and OpenSMOKE++ <sup>112,113</sup> (OS) were used. For the ST data (shock tubes with constant pressure) all calculations were carried out with both simulation codes and the agreement of the calculated IDTs were always better than 1%. For the simulation of the experiments with pressure/volume profiles, *i.e.* for the ST-PRR and RCM experiments, FM simulations ran much slower and therefore OS was used routinely. In several points the OS results were checked with FM simulations and again good agreement (within 1%) was found.

### 5.1 Shock tube simulations

The IDT in a reflected ST experiment is interpreted as the time interval between the arrival of the reflected shock wave and the onset of a well measurable characteristic state. This state was extracted from the simulated pressure or concentration profiles. We found that in the experimental



papers dealing with ST methane ignition 37 different definitions of IDT have been used. These definitions, and the numbers of the related datasets and data points are listed in **Table 3**.

**Table 3.** A summary of various designations of IDTs as defined in the experiments. OHEX and CHEX denote electronically excited OH and CH species, respectively.

No.	The definition of IDT	Number of datasets	Number of data points
1	Root of the tangent line at the inflection point of $p(t)$	111	792
2	Root of the tangent line at the first inflection point of the [OH] profile	3	9
3	Root of the tangent line at the first inflection point of the [OHEX] profile	51	472
4	Root of the tangent line at the first inflection point of the [CH] profile	2	3
5	Root of the tangent line at the first inflection point of the [CHEX] profile	101	744
6	Root of the tangent line at the inflection point of the [CH <sub>4</sub> ] profile	35	201
7	Root of the tangent line at the first inflection point of the [CH <sub>3</sub> ] profile	2	24
8	Root of the tangent line at the inflection point of the [CO <sub>2</sub> ] profile	11	91
9	Root of the tangent line at the inflection point of the [O <sub>2</sub> ] profile	3	31
10	Root of the tangent line at the first inflection point of the [H <sub>2</sub> O] profile	2	14
11	Root of the tangent line at the inflection point of the [soot] profile *	1	6
12	Time of the first inflection point of $p(t)$	73	968
13	Time of the first inflection point of the [OHEX] profile	32	346
14	Time of the first inflection point of the [CHEX] profile	4	147
15	Time of maximum of [OH] profile	9	33
16	Time of maximum of [OHEX] profile	23	181
17	Time of maximum of [O] profile	6	44
18	Time of maximum of [O]×[CO] profile **	5	55
19	Time of maximum of [CH <sub>3</sub> ] profile	4	15
20	Time of maximum of [H <sub>2</sub> O] profile	2	20
21	Time of reaching 0.05×the maximum of $p(t)$	6	42
22	Time of reaching 0.25×the maximum value in [OH] profile	4	40
23	Time of reaching 0.50×the maximum value in [OH] profile	6	48
24	Time of reaching 0.75×the maximum value in [OH] profile	4	40
25	Time of reaching 0.05×the maximum value in [OHEX] profile	13	141
26	Time of reaching 0.10×the maximum value in [OHEX] profile	6	27
27	Time of reaching 0.50×the maximum value in [OHEX] profile	16	84
28	Time of reaching 0.05×the maximum value in [CHEX] profile	6	42
29	Time of reaching 0.25×the maximum value in [CO] profile **	4	40
30	Time of reaching 0.50×the maximum value in [CO] profile **	4	40
31	Time of reaching 0.75×the maximum value in [CO] profile **	4	40
32	Time of reaching 0.90×the maximum value in [CO] profile **	2	15
33	Time of reaching 0.25×the maximum value in [CO <sub>2</sub> ] profile	2	8
34	Time of reaching 0.90×the maximum value in [CO <sub>2</sub> ] profile	7	49
35	Time of reaching 0.90×the maximum value in [H <sub>2</sub> O] profile	2	14
36	Time of reaching 0.05×the maximum value in [C <sub>2</sub> ] profile *	6	38
37	Time of reaching [CO <sub>2</sub> ] = 1.6E14 molecule/cm <sup>3</sup> *	2	35

\* These data points were not used at the comparison of the mechanisms since these IDT definitions are not feasible in this study.

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3 \*\* These data points were not used at the comparison of the mechanisms, since only Ar was used as diluent gas in the measurements, thus the effect  
4 of vibration relaxation during CO production was not considered. According to the conclusion of the study of Mathieu et al. 114, if vibration  
5 relaxation is not considered, the measurements based on CO concentrations are not reproducible.  
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7 1251 IDTs in 141 datasets were determined from excited OH (OHEX) concentration profiles.  
8  
9 IDTs derived from simulated OH (ground state) and OHEX (excited state) concentration profiles  
10 may or may not agree with each other, and therefore if the experimental IDT was determined based  
11 on OHEX profile, then the simulated IDT also has to be based on the OHEX concentration profile.  
12  
13 However, only four of the thirteen mechanisms (Aramco-II-2016, FFCM-I-2016, Konnov-2017,  
14 Glarborg-2018) contain OHEX chemistry. The OHEX submechanism of the Aramco-II-2016  
15 mechanism was selected and it was added to the nine mechanisms that do not contain OHEX  
16 species. The detailed description is available in Part 3 of the Supplementary Material. It was  
17 verified that adding the OHEX submechanism to these mechanisms changed the calculation of the  
18 concentrations of all other species negligibly. If the IDT definition was based on the calculated  
19 OHEX profile, the original Aramco-II-2016, FFCM-I-2016, Konnov-2017, and Glarborg-2018  
20 mechanisms were used, whereas the other mechanisms were used together with the OHEX  
21 submechanism of Aramco-II-2016.  
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37 The IDTs in 933 data points (included in 111 datasets) were measured based on excited CH  
38 (CHEX) concentrations, from which 19 points of 8 datasets used helium as diluent. Similarly to  
39 the case of OH vs. OHEX, the calculated IDT has to be based on calculated CHEX profile, if the  
40 experimental IDT was obtained via monitoring the CHEX profile. However, only Aramco-II-2016  
41 and FFCM-I-2016 contain CHEX submechanisms. In a similar way, the CHEX submechanism of  
42 Aramco-II-2016 was selected and it was added to the mechanisms without CHEX chemistry.  
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44 Again, this addition negligibly affected the calculated concentrations of the other species. In the  
45 IDT simulations based on CHEX, the original CHEX submechanisms were used with Aramco-II-  
46 2016 and FFCM-I-2016, but CHEX submechanism of Aramco-II-2016 was added to all other  
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3 mechanisms. We also added the CHEX submechanism of FFCM-I-2016 (instead of Aramco-II-  
4 2016) to all other mechanisms and found that the calculated IDTs were practically identical to  
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6 using the Aramco-II-2016 CHEX submechanism.  
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10 We investigated the detailed description of experimental conditions in all articles containing ST  
11 experimental data. From all 71 articles without published pressure rise rates, 19 articles  
12 35,36,42,45,51,52,58,61,66,71,74,75,77,78,80,84,89,98,99 declared that the slightly increasing pressure observed  
13 before ignition can be neglected. These articles provided several reasons for it, such as (i) the used  
14 ST equipment had large diameter that minimized the boundary layer effects, (ii) the measured  
15 pressure rise rates before ignition were too small to be considered, (iii) the measured IDTs were  
16 very short, (iv) the pressure rise due to reactions could be reproduced by simulations, and (v) no  
17 pressure rise was found during the whole reacting process due to the high diluent ratio. Three  
18 articles <sup>54,68,88</sup> took into account the pressure rise at the estimation of the experimental error. The  
19 rest of the papers did not comment on the observed slight pressure change before ignition or they  
20 did not find pressure rise. For all shock tube measurements without published pressure rise rate  
21 the assumption of constant volume and adiabatic conditions was used.  
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38 Olm et al. simulated IDTs of hydrogen and syngas mixtures <sup>1,2</sup> and they excluded data points  
39 without detailed pressure–time history if the initial temperature was lower than 1000 K. In the  
40 present study, this procedure was not used for the following reasons. The performance of the  
41 mechanisms at low initial temperatures ( $T_5 \leq 900$  K) using ST measurements was investigated and  
42 six mechanisms (Aramco-II-2016, USC-II-2007, Glarborg-2018, Caltech-2015, Konnov-2017,  
43 GDF-Kin-2009) were found to have good performance (see **Fig. S3**). The error values belonging  
44 to the other seven mechanisms (FFCM-I-2016, GRI3.0-1999, Konnov-2009, CRECK-2014,  
45 Leeds-2001, SanDeigo-2014, and SanDiego-2016) were only slightly higher. Similarly, all data  
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3 points were sorted to five sets according to the length of IDT, and the results in **Fig. S4** show that  
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5 no clear trend of error function values  $E$  appear with increasing length of IDTs. The detailed  
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7 description and figures are available in Part 4 of the Supplementary Material.  
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10 In the shock tube measurements of Donohoe et al.<sup>43</sup>, Zhang et al.<sup>55,101</sup>, Burke et al.<sup>63</sup>, Zeng et  
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12 al.<sup>90</sup>, Merhubi et al.<sup>93</sup>, and Deng et al.<sup>95,96</sup>, pressure rise rates during ignition were reported. The  
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14 details of measurements including pressure rise rates was shown in “ST with PRR” part in **Table**  
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16 **2**. For the simulation of these ST data, we used the assumptions of constant volume and adiabatic  
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18 system with the measured pressure rise rate.  
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## 26 5.2 RCM simulations

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30 In RCM experiments the compression is never truly adiabatic as from the beginning of the  
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32 compression stroke heat loss takes place to the walls. The most practical way to take such heat loss  
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34 into account in homogeneous simulations is based on the adiabatic core approximation<sup>115,116</sup>,  
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36 which assumes an inner adiabatic core in the chamber by mimicking heat loss with an equivalent  
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38 adiabatic expansion work. In order to experimentally determine heat loss rate before ignition, an  
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40 extra, non-reactive experimental measurement is done in an almost identical setup, in which  
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42 oxygen (O<sub>2</sub>) is replaced with nitrogen (N<sub>2</sub>), thus no chemical heat production can take place. From  
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44 the corresponding, non-reactive pressure trace the effective volume profile ( $V_{\text{eff}}(t)$ ), which also  
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46 takes heat loss into account within the adiabatic core and frozen-chemistry approximation (i.e.  
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48 isentropic process), is obtained by the following integral:  
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$$52 V_{\text{eff}}(t) = V(t_0) \exp \left( - \int_{p(t_0)}^{p(t)} \frac{1}{\gamma(T(p'))} \frac{dp'}{p'} \right)$$

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Here,  $p(t_0)$  and  $V(t_0)$  are the initial pressure and volume, respectively, and  $\gamma$  is the adiabatic index:

$$\gamma(T) = \frac{C_p(T)}{C_v(T)} = \frac{C_p(T)}{C_p(T) - R} ,$$

which can be calculated using the NASA polynomials of the constant-pressure molar heat capacity ( $C_p$ ). The momentary temperature ( $T(t')$ ) can be calculated from the initial temperature ( $T_0$ ), the initial and instantaneous pressures ( $p(t_0)$ ,  $p(t')$ ) and the effective volumes ( $V(t_0)$ ,  $V^{\text{eff}}(t')$ ) using the ideal gas law ( $pV/T = \text{constant}$ ). Applying this equation for the whole period, the simulation of the non-reactive mixture with the obtained volume profile under adiabatic conditions will always precisely follow the measured non-reactive pressure trace if frozen-chemistry approximation holds. This procedure was first applied in the work of Kérmonès et al.<sup>117</sup>, but it was not discussed in details there. Kérmonès et al.<sup>117</sup> used the code of T. Nagy and this code is available on request. The procedure proposed by He et al.<sup>118</sup> is very similar, but it determines the effective volume profile for the compression period using the reactive pressure trace. If chemistry (e.g. pyrolysis) takes place already during compression, these methods can provide more realistic simulation results than the procedure proposed by Mittal and Sung<sup>116</sup>, in which the matching of the pressure profile during compression is not achieved precisely. Transferring the determined volume profiles ( $V^{\text{eff}}(t)$ ) to reactive simulations, heat loss can be taken into account before ignition, which is necessary to capture the experimentally measured IDT.

For the uniform simulation of all considered RCM experiments, we derived effective volume histories from the non-reactive pressure histories whenever they were available. For the simulation of experiments in papers<sup>43,63,104,107</sup>, we used the provided volume–time profiles as no pressure histories were published. In refs.<sup>43,63,104</sup>, the volume–time profiles were determined based on the method of Mittal and Sung<sup>116</sup>, whereas in paper<sup>107</sup> they were calculated using the method of He

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3 et al.<sup>118</sup>. The authors of articles<sup>105</sup> and<sup>106</sup> published only reactive pressure histories and assessed  
4 heat loss based on them. For these experiments we proceeded in the same way as they did: they  
5 truncated each pressure history from when substantial heat release started taking place,  
6 extrapolated the preceding heat loss part to the removed period, and then derived the volume–time  
7 profile based on the discussed isentropic relations.  
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14       Adiabatic simulations of reactive experiments were carried out using the volume–time profiles  
15 and all RCM IDTs were defined, in accordance with the experimental papers, as the time of the  
16 steepest pressure rise (*i.e.* time of  $dp/dt$  maximum) after the end of the compression stroke ( $t = 0$   
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24       The experimental data used in the present study were obtained from published articles or  
25 personal communications with the authors. Some RCM experimental data were not accompanied  
26 with published pressure–time or volume–time histories<sup>94,119,120</sup> and these were excluded from the  
27 comparison.  
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## 6 Results and discussion

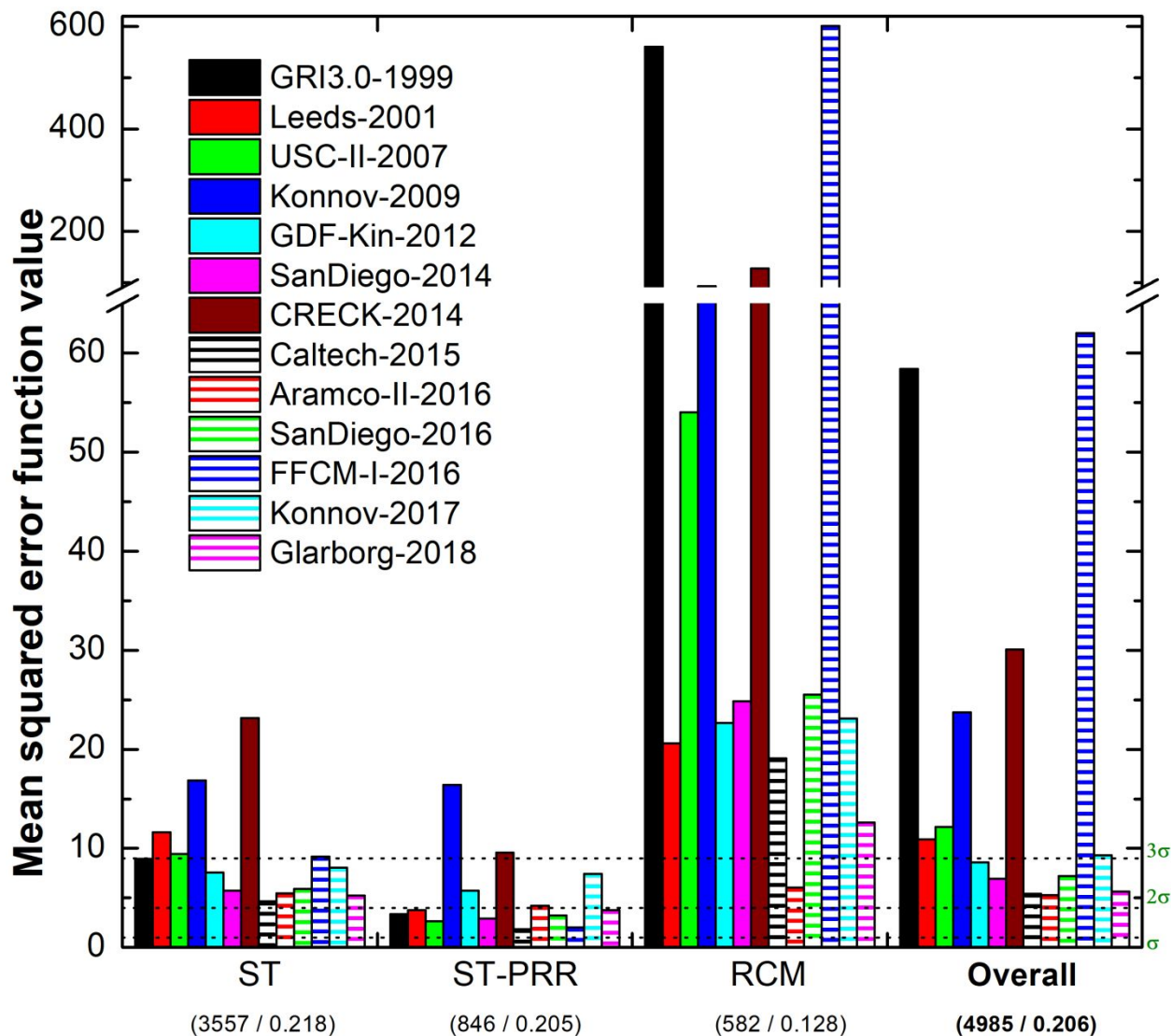
### 6.1 Ignition delay times

**Table 4** lists the mean squared error and the mean signed deviation function values of all mechanisms. These data are visualized in **Figs. 2** and **3**. **Fig. 2** shows the average error function values of all mechanisms for simulating the shock tube measurements with constant volume assumption (ST group), shock tube experiments with pressure rise rate (ST-PRR group), rapid compression machine measurements (RCM group) and the overall results (Overall group). There are six mechanisms with average error  $E$  lower than three times of the estimated experimental error ( $E < 9$ ); these are Aramco-II-2016, Caltech-2015, Glarborg-2018, SanDiego-2014, SanDiego-2016, and GDF-Kin-2012, in the order of increasing error. For the ST group, the simulation error values of Caltech-2015, Glarborg-2018, Aramco-II-2016, and SanDiego-2014 are the lowest. In the ST-PRR group, Caltech-2015 and FFCM-I-2016 have obviously lower error values, while for the RCM measurements, Aramco-II-2016 has significantly the best performance among all mechanisms. All mechanisms reproduce the ST-PRR experiments better than the ST experiments. This indicates that providing the pressure rise rate might be important in several cases for the accurate reproduction of the experimental conditions. Two mechanisms, GRI3.0-1999 and FFCM-I-2016 do not reproduce well the RCM experimental results, compared to other investigated mechanisms.

**Table 4.** The mean squared error function values  $E$  and the mean signed deviation function values  $D$  for all the mechanisms. The shaded cells indicate those up to six best performing mechanisms in each experimental type that reproduce the measured ignition delay times on average within  $3\sigma$  (i.e.  $E < 9$ ).

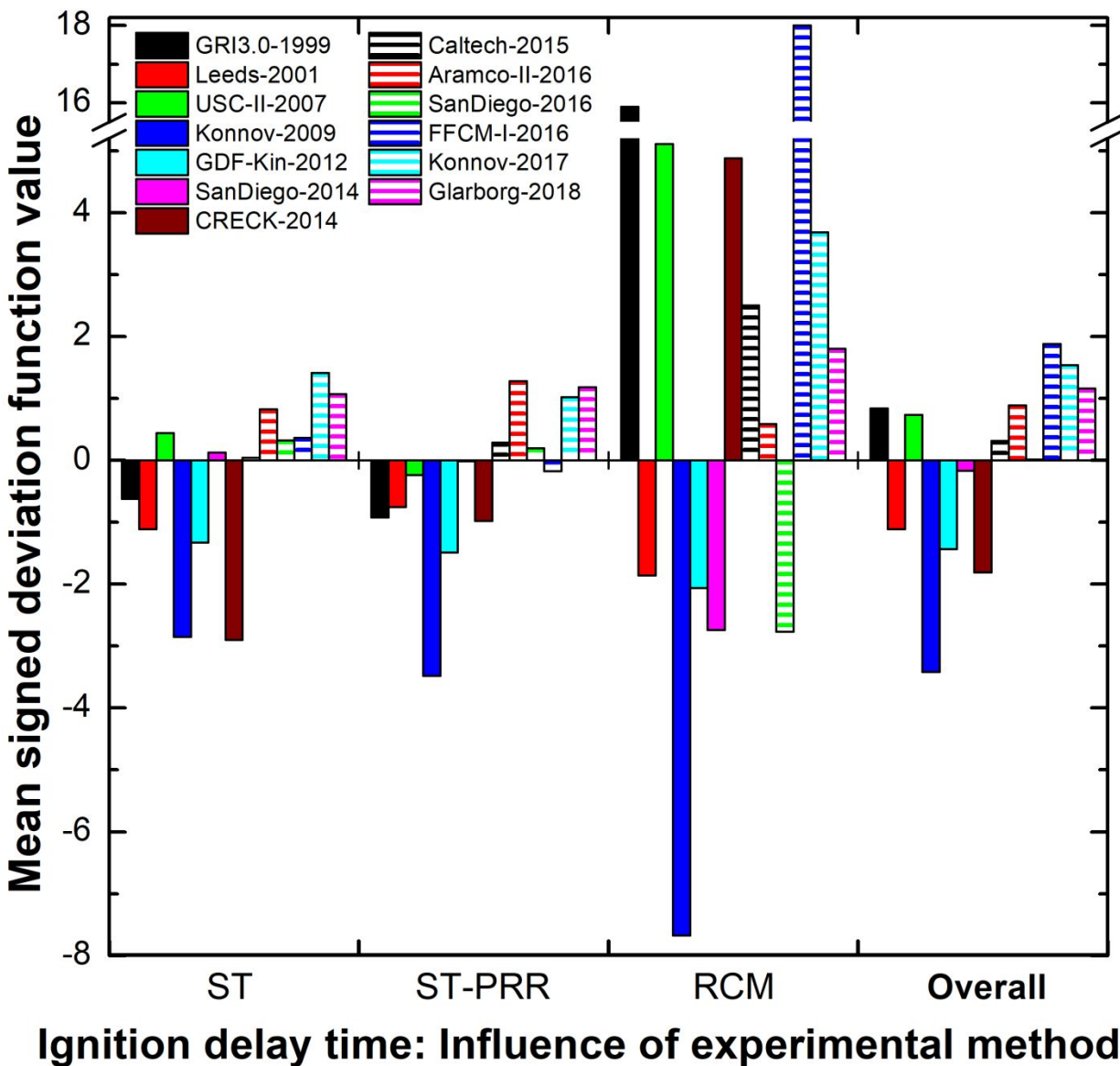
No.	Mechanisms ID	Mean squared error function values				Mean signed deviation function values			
		ST	ST-PRR	RCM	Overall	ST	ST-PRR	RCM	Overall
1	GRI30-1999	8.931	3.345	560.417	58.415	-0.620	-0.925	15.900	0.839
2	Leeds-2001	11.618	3.763	20.616	10.897	-1.110	-0.752	-1.860	-1.110
3	USC-II-2007	9.418	2.652	54.025	12.178	0.442	-0.236	5.110	0.737
4	Konnov-2009	16.861	16.411	92.951	23.751	-2.850	-3.480	-7.670	-3.420
5	GDF-Kin-2012	7.558	5.740	22.646	8.584	-1.330	-1.490	-2.060	-1.430
6	SanDiego-2014	5.742	2.932	24.848	6.941	0.128	-0.016	-2.740	-0.164
7	CRECK-2014	23.147	9.586	127.636	30.061	-2.900	-0.977	4.880	-1.810
8	Caltech-2015	4.644	1.851	19.099	5.420	0.044	0.285	2.500	0.317
9	Aramco-II-2016	5.458	4.205	6.029	5.264	0.823	1.280	0.589	0.891
10	SanDiego-2016	5.924	3.214	25.517	7.188	0.324	0.193	-2.770	0.015
11	FFCM-I-2016	9.160	2.016	600.867	62.026	0.366	-0.176	18.000	1.880
12	Konnov-2017	8.056	7.445	23.103	9.316	1.410	1.020	3.680	1.540
13	Glarborg-2018	5.258	3.786	12.613	5.643	1.070	1.180	1.800	1.160





### Ignition delay time: Influence of experimental method

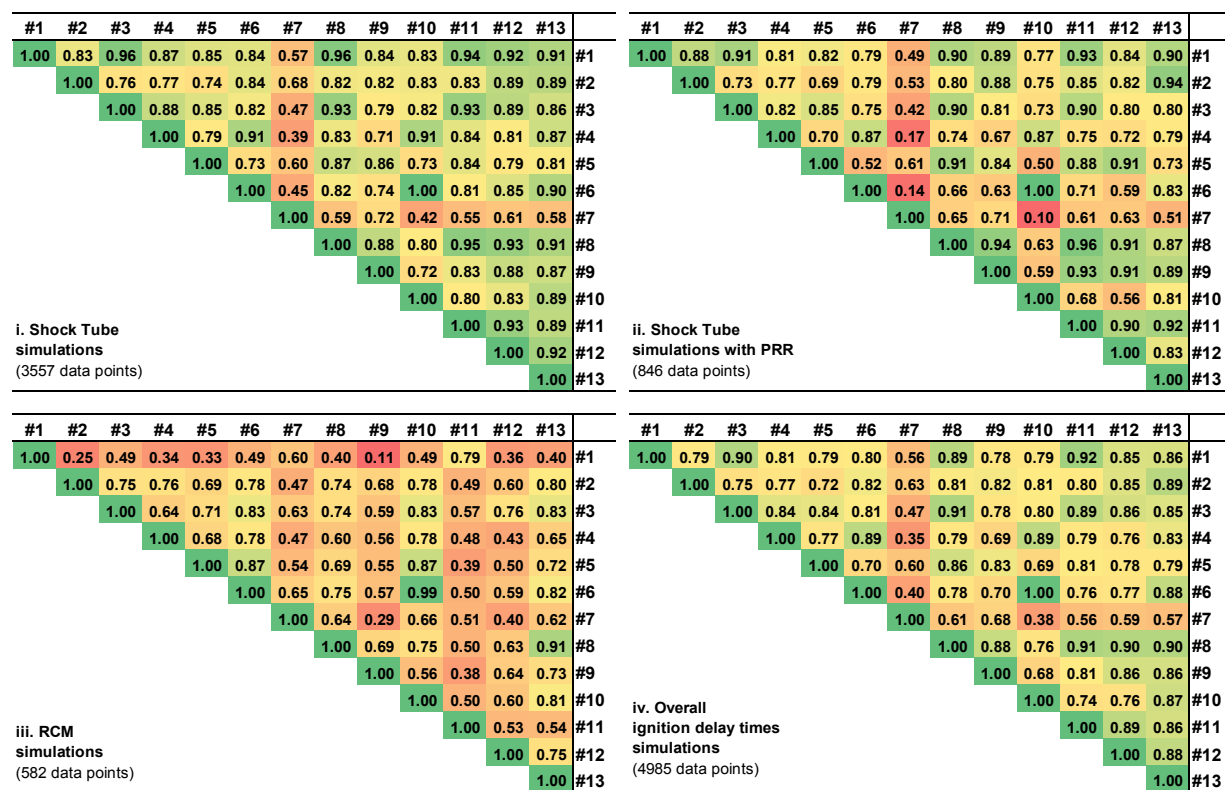
**Figure 2.** Errors of the reproductions of IDTs according to the different types of experiments. The number given in the parentheses are the number of data points used and the average of the estimated  $\sigma$  of the  $\ln \tau$  values.



**Figure 3.** Mean signed deviation values for all mechanisms according to the different types of experiments.

**Fig. 3** displays the mean signed deviations for all mechanisms for the different types of experiments. Four mechanisms (Caltech-2015, Aramco-II-2016, Konnov-2017 and Glarborg-2018) generally overpredict the IDTs, which means that the simulated IDTs are longer than the experimental ones. Three mechanisms (Leeds-2001, Konnov-2009, and GDF-Kin-2012)

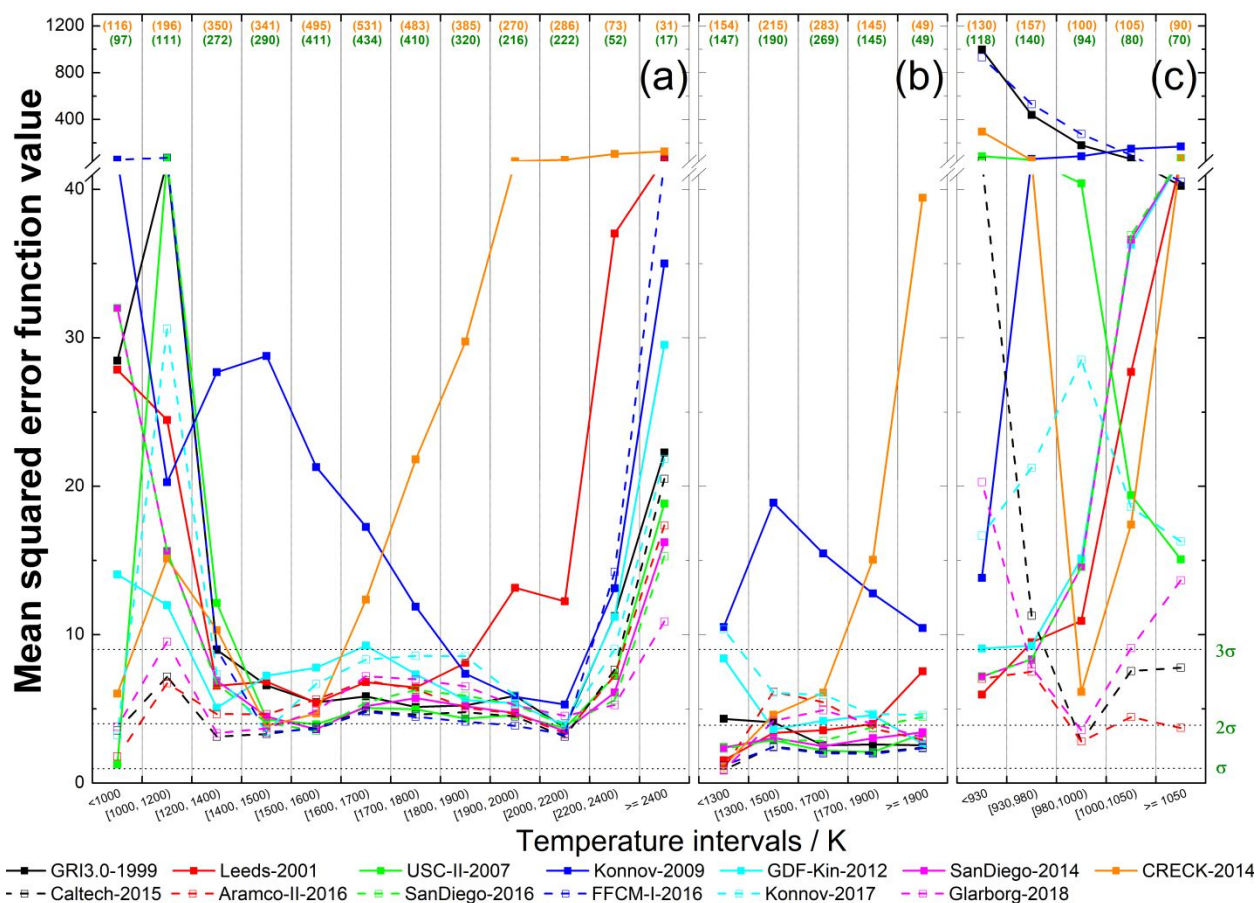
underpredict IDTs. The other mechanisms do not show an obvious trend in the signed deviation values.



**Figure 4.** Matrix of Pearson correlation coefficients for all types of simulations. The #*n* numbers refer to the mechanism indices shown in **Table 1**.

In **Fig. 4**, the average Pearson correlation coefficients between the IDTs calculated by each two mechanisms are displayed. Among the weak correlations, CRECK-2014 (#7) has small correlation coefficients with all other 12 mechanisms in all the four groups, and GRI3.0-1999 (#1) has this feature only for the RCM measurements. In **Fig. 4 panel iii** (RCM experiments), FFCM-I-2016 (#11) and Konnov-2017 (#12) have weak correlations with the other mechanisms overall. SanDiego-2014 (#6) and SanDiego-2016 (#10) have the highest correlation at all types of measurements, since the latter was developed from the former one, and their simulated values for most of the data points are very close. Except for the two San Diego mechanisms, the highest

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3 correlations exist for mechanism pairs GRI3.0-1999 (#1) / USC-II-2007 (#3) and GRI3.0-1999  
4 (#1) / Caltech-2015 (#8) in the ST subset, Caltech-2015 (#8) / FFCM-I-2016 (#11) in the ST-PRR  
5 subset, Caltech-2015 (#8) / Glarborg-2018 (#13) in the RCM subset, and GRI3.0-1999 (#1) /  
6 FFCM-I-2016 (#11) for all IDTs. In ST and ST-PRR parts, any of the pairs between GRI3.0-1999  
7 (#1), USC-II-2007 (#3), Caltech-2015 (#8), FFCM-I-2016 (#11) has a correlation coefficient  
8 higher than or equal to 0.9. In addition, simulation results of Caltech-2015 (#8) and Glarborg-2018  
9 (#13) have correlation higher than average with several mechanisms in the four panels. The  
10 correlation coefficients of each two mechanisms are larger for ST experiments than for the ST-  
11 PRR and RCM ones. The correlation coefficients indicate that most mechanisms were calibrated  
12 considering the ST without PRR datasets, while the generally more recent ST-PRR and RCM  
13 datasets were less used. High correlation coefficients are usually in good accordance with the  
14 known development history of the mechanisms. Olm et al. had a similar observation for the  
15 hydrogen <sup>1</sup> and syngas <sup>2</sup> mechanisms.  
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**Figure 5.** Performance of the mechanisms in the various intervals of temperature with respect to IDT. The panels show the results for STs without PRR (a), STs with PRR (b) and RCM (c). The orange and green numbers at the top of the figure give the number of data points in each interval before and after excluding data points that could not be reproduced within  $3\sigma$  error by any of the mechanisms were not used.

In **Figs. 5 to 10**, the performance of the mechanisms in reproducing IDTs is shown in the various intervals of experimental conditions, like temperature, pressure, equivalence ratio, and diluent ratio. In these figures, the intervals were selected by ensuring statistically enough data points within each interval. The number of data points used in each range is shown at the top of the corresponding intervals.

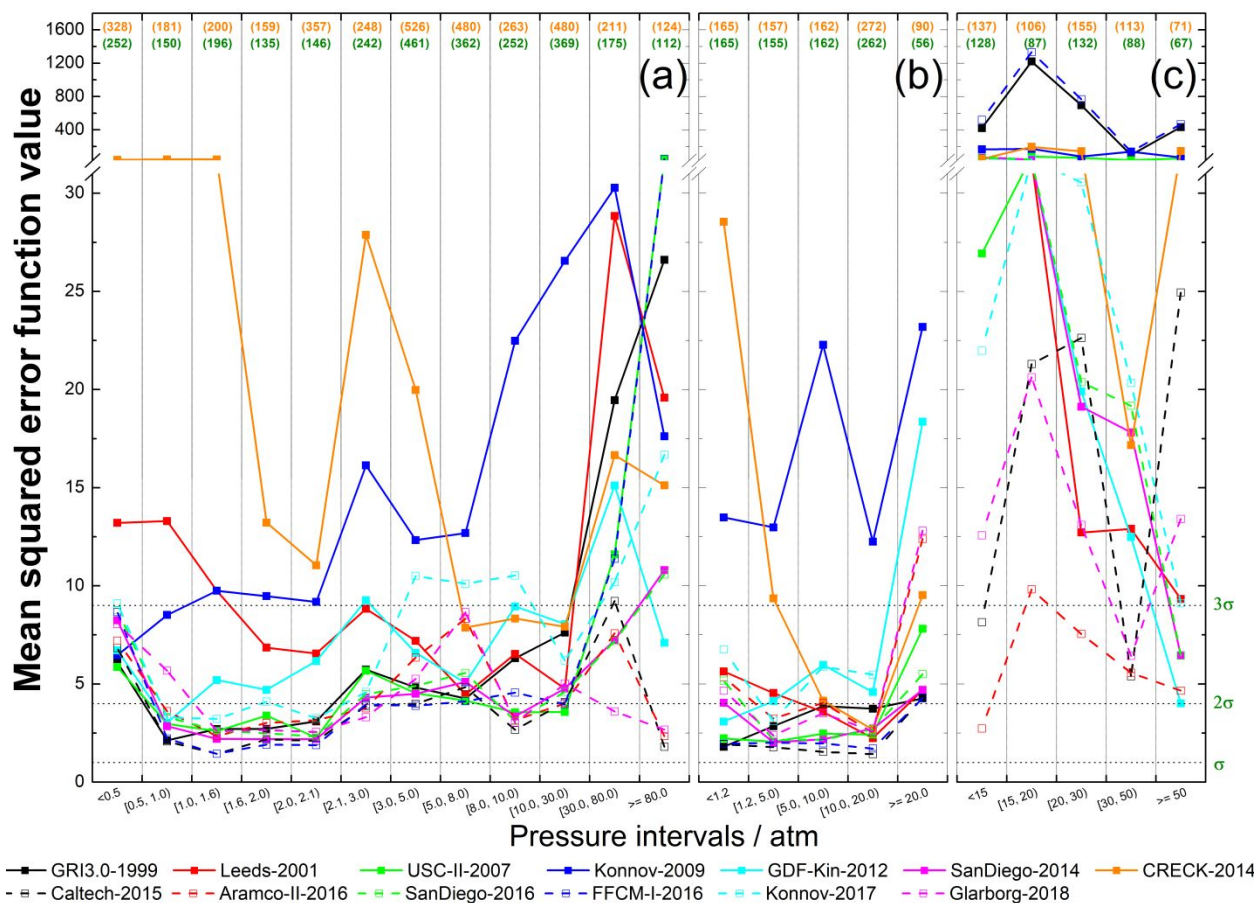
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3 **Fig. 5** shows the dependence of  $E$  values of the mechanisms on the initial temperature. In **Fig.**  
4 **5(a)** for ST measurements without PRR, the overall trend is that most mechanisms can reproduce  
5 the experiments with better accuracy in the middle temperature range, (1200K – 2200K) except  
6 for mechanisms Leeds-2001, Konnov-2009, and CRECK-2014. The  $E$  values of these three  
7 mechanisms follow a similar trend, but with higher values. In this middle temperature range,  
8 Caltech-2015 and FFCM-I-2017 have the lowest error values. However, the  $E$  values of FFCM-I-  
9 2017 increase dramatically towards lower and higher temperatures, while Caltech-2015 has stable  
10 performance in the whole temperature range. Similarly, Aramco-II-2016 and Glarborg-2018 are  
11 accurate at all initial temperatures.

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24 As **Fig. 5(b)** shows, for the reproduction of the ST with PRR experimental data, five mechanisms  
25 (Leeds-2001, Konnov-2009, GDF-Kin-2012, CRECK-2014, and Konnov-2017) have large errors  
26 in all or in some temperature ranges. Surprisingly, Aramco-II-2016 has a somewhat larger error in  
27 the temperature range of 1300K to 1700K, where most other mechanisms have very low error.

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33 According to **Fig. 5(c)**, the majority of mechanisms reproduce the RCM experimental data  
34 poorly, while Aramco-II-2016 is the only one which has  $E$  values lower than 9 (*i.e.* below on  
35 average  $3\sigma$  deviation) at all initial temperatures. Konnov-2017 and Glarborg-2018 have error  
36 values larger than those of Aramco-II-2016, but these are better than the other mechanisms. The  
37 error value  $E$  of Caltech-2015 is less than 9 above 980K, while below this temperature  $E$  is  
38 increasing significantly with decreasing temperature.

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47 **Fig. S5** (panels (a) and (b) for initial temperature and pressure, respectively) in the  
48 Supplementary Material shows that there is no trend for under- or overprediction of the ST  
49 experimental data (with or without PRR) for most of the mechanisms. At high temperature,  
50 CRECK-2014 and Leeds-2001 strongly underpredicts the ignition delay times. At low temperature,  
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Konnov-2009 underpredicts the IDTs. Konnov-2017 overpredicts IDTs in the whole pressure range, while CRECK-2014 and Konnov-2009 underpredicts the ignition delay times at low and high pressures, respectively. For the RCM experimental data (see Fig. S5 (c)) all mechanisms, except for Konnov-2009, trend to predict relatively longer IDTs at lower initial temperatures, while simulate relatively shorter IDTs at higher temperatures.

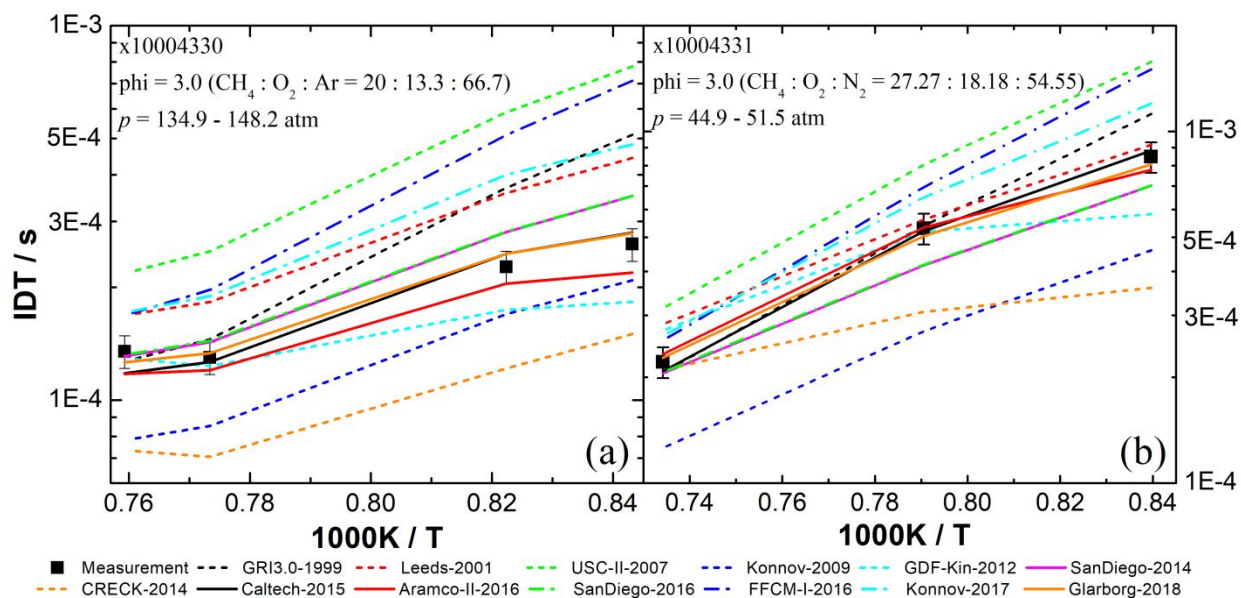


**Figure 6.** Performance of the mechanisms for various intervals of pressure with respect to IDT. Each plot shows the results for STs without PRR (a), STs with PRR (b) and RCM (c).

Although Table 1 and Fig. 1 show that the mechanisms have not been validated considering the low pressure ( $< 1$  atm) experiments, Fig. 6(a) shows that all mechanisms can reproduce the ST experiments without PRR data well in the low and middle pressure range, but their performance

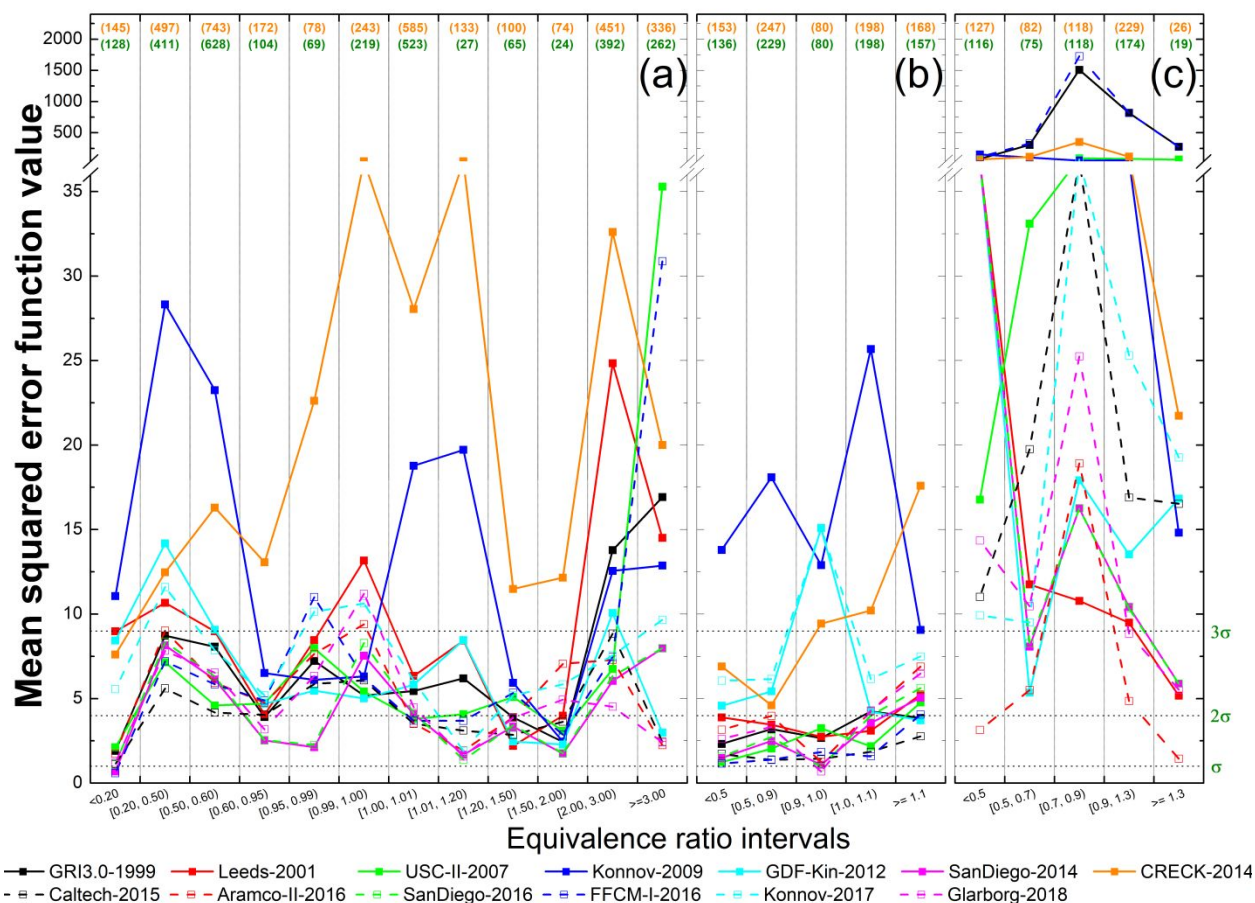
is not as good at pressures higher than 30 atm, except for Glarborg-2018, Aramco-II-2016 and Clatech-2015. As shown in **Fig. 6(b)** for the ST-PRR data, Konnov-2009, GDF-Kin-2012, and CRECK-2014 have significant change of  $E$  values for all ranges of pressure, while the other mechanisms are satisfactory for reproducing all datasets. In **Fig. 6(c)**, Aramco-II-2016 is the most accurate mechanism for the reproduction of the RCM data in all pressure ranges and the deviations of Caltech-2015 and Glarborg-2018 are also within the reasonable range. However, the predicting capability of all other mechanisms are much poorer.

**Figure 7** shows the  $\log \tau - 1000/T$  plots and indicates the deviations of the various simulation results compared to the experimental IDT uncertainty. Note that neither the experimental data nor the simulation results fit to a straight line, because pressure was not identical in these experiments.



**Figure. 7.** Measured and simulated ignition delay times of methane mixtures at high pressures. The detailed information on experimental data x10004330 and x10004331<sup>71</sup> is shown in Table A in the Supplementary Material.

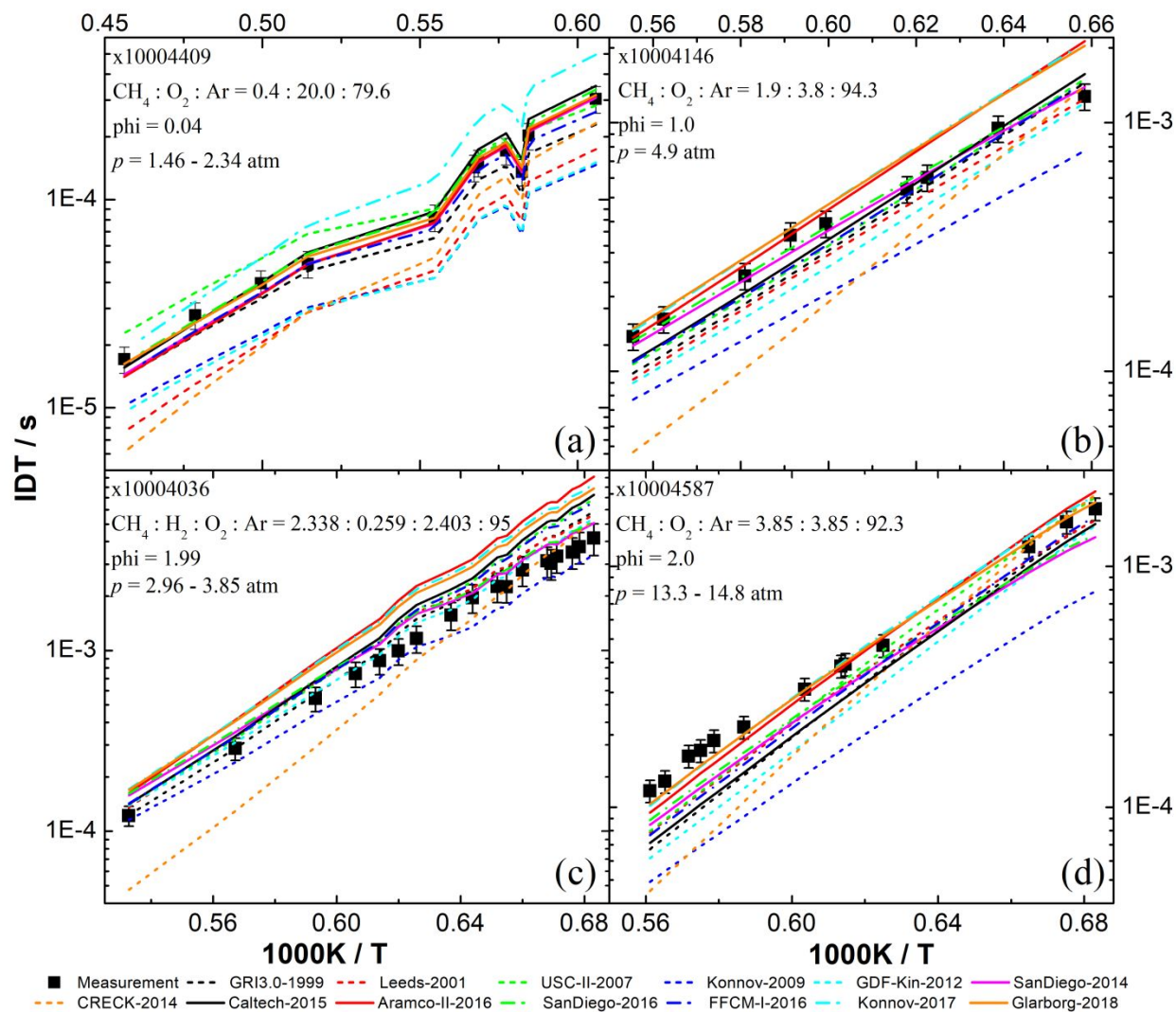




**Figure 8.** Performance of the mechanisms for various intervals of equivalence ratio with respect to IDT. Each plot shows the results for STs without PRR (a), STs with PRR (b) and RCM (c).

**Fig. 8(a)** shows that at the reproduction of ST data without PRR there is no clear trend for changing the error function values with equivalence ratios. However, in the low equivalence ratio range SanDiego-2014, SanDiego-2016, and Caltech-2015 have the lowest error. **Table 1** and **Fig. 1** indicate that all mechanisms but FFCM-I-2016 were validated only at equivalence ratios larger than 0.1. In **Fig. 8(a)** it is shown that all mechanisms can predict the experiments within  $2\sigma$  at low equivalence ratio  $\phi < 0.2$ , except for Leeds-2001, GDF-Kin-2012, CRECK-2014 and the two Konnov mechanisms. For the reproduction of ST data with PRR (**Fig. 8(b)**), Caltech-2015 and FFCM-I-2016 are the most accurate mechanisms, and Glarborg-2018 has low error (less than  $1\sigma$ )

at stoichiometric equivalence ratio. For reproducing the RCM data (**Fig. 8(c)**), most mechanisms are less accurate under slightly lean ( $0.7 < \phi < 0.9$ ) conditions compared to both the lean and rich mixtures. Aramco-II-2016 has the same trend, but its error is the lowest at most equivalence intervals.



**Figure 9.** Measured and simulated ignition delay times of the methane mixtures with various equivalence ratios. The detailed information of the experimental data (x10004036<sup>91</sup>, x10004146<sup>52</sup>, x10004409<sup>81</sup>, x10004587<sup>100</sup>) is shown on the Table A in the Supplementary Material.

Figure 9(a) provides a related comparison of the experimental data and the simulation results on a  $\log \tau - 1000K/T$  plot. Near the stoichiometric equivalence ratio, the errors of most mechanisms are low, except for CRECK-2014 and Konnov-2009, as seen in Figure 9(b). In the range of moderately rich equivalence ratio ( $1.2 < \phi < 2.0$ ), the GDF-Kin-2012 mechanism has relatively lower error compared to other mechanisms, as shown in Figure 9(c). For mixtures even richer in fuel ( $2.0 \leq \phi$ ), Glarborg-2018 could reproduce the experimental data the best, as shown in Figure 9(d).

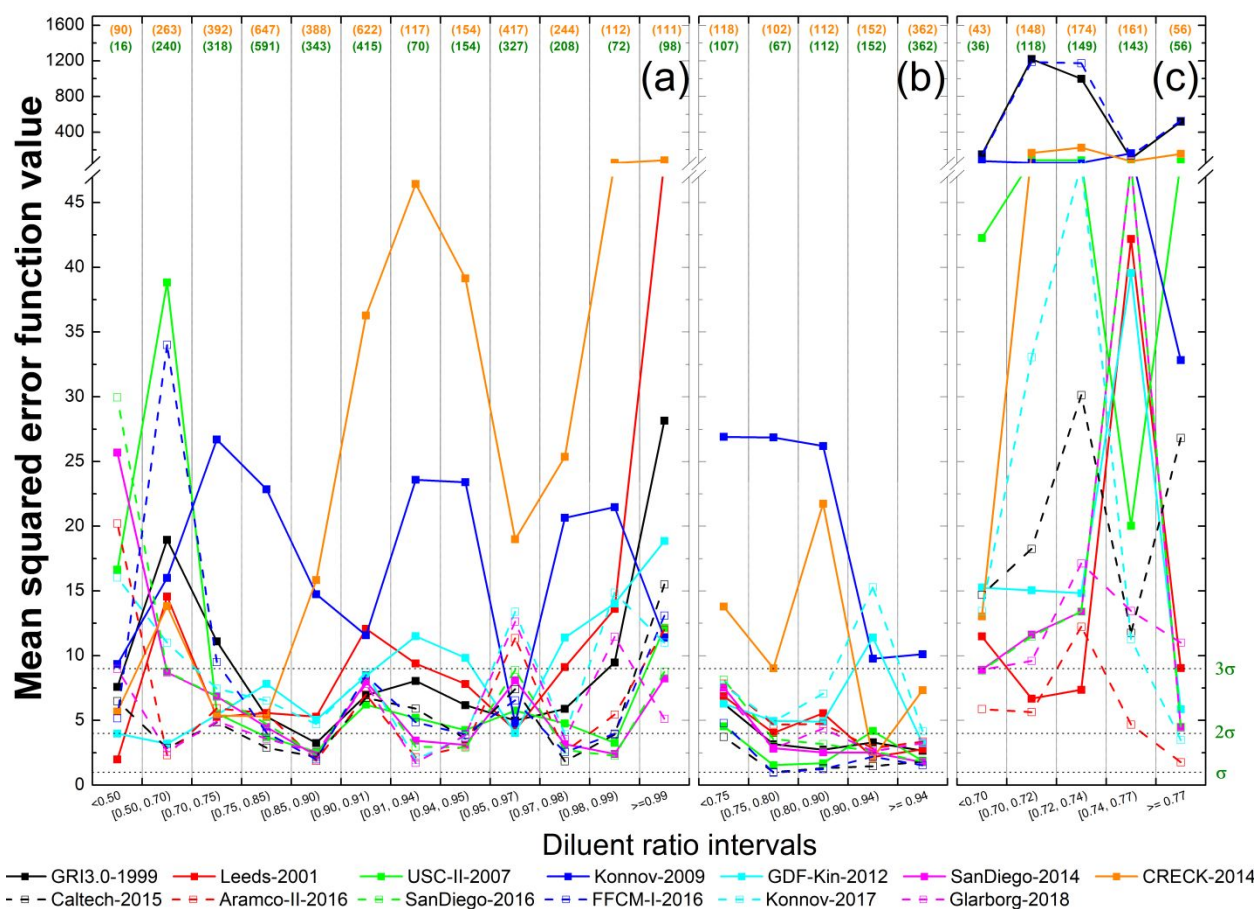


Figure 10. Performance of the mechanisms for various intervals of diluent ratio with respect to IDT. Each plot shows the results for STs without PRR (a), STs with PRR (b) and RCM (c).

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3 The lowest diluent ratio used for the original validation of mechanisms is 33.3% (see **Table 1**),  
4 which means that the performance of these mechanisms below diluent ratio 33.3% was not  
5 investigated. In the present study, however, even combustion of undiluted mixtures was also  
6 considered (diluent ratio 0, oxy-fuel combustion). **Figure 10** shows the performance of the  
7 mechanisms for various intervals of diluent ratio. For the ST data without PRR (**Fig. 10(a)**),  
8 Glarborg-2018 and Caltech-2015 are advantageous in predicting experiments in the full condition  
9 range. Caltech-2015 and FFCM-I-2016 are the most accurate mechanisms for reproducing the ST  
10 experimental data with PRR, as shown in **Fig. 10(b)**. **Fig. 10, panels (a), (b), and (c)** show that  
11 Leeds-2001, Caltech-2015 and Aramco-II-2016 are the best performing mechanisms, respectively,  
12 under low diluent ratio conditions.  
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26 For the prediction of RCM data (**Fig. 10(c)**), Aramco-II-2016 is the best mechanism again,  
27 although its error is slightly higher in the diluent ratio range 72% to 74%. As shown in **Fig. S6 (f)**  
28 of the Supplementary Material, Aramco-II-2016 overpredicts the IDTs measured with RCM in  
29 most ranges of diluent ratio.  
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## 6.2 Sensitivity analysis results

Sensitivity analysis was carried out using the four mechanisms with the best predicting ability (SanDiego-2014, Clatech-2015, Aramco-II-2016 and Glarborg-2018) under each of the conditions of the collected IDT measurements. The local sensitivity coefficients were calculated in such a way that Arrhenius parameters  $A$  of the reactions were increased by 5% and the ignition delay times were recalculated. Sensitivity coefficients  $d\tau/dA_j$  were calculated by finite differences and then converted to normalized sensitivities  $d\ln\tau/d\ln A_j = (A_j/\tau) d\tau/dA_j$ . The normalized sensitivity coefficients were scaled to values between  $-1$  and  $+1$  by dividing them by the largest absolute sensitivity coefficients. The most sensitive reactions were identified based on the order of the average of the absolute values of the scaled sensitivity coefficient obtained in the investigated intervals. Furthermore, range  $[-1, +1]$  was divided to ten equidistant intervals, and the relative frequency of the reactions in each interval was counted. This analysis was carried out for each experimental type (ST, ST with PRR, RCM).

In **Table 5**, for the selected four mechanisms the fifteen most sensitive reactions and their mean absolute scaled sensitivity coefficients  $\overline{S}_{abs}$  are shown. The order of the sensitivity is meaningful within one mechanism, and the values belonging to different mechanisms cannot be compared.

**Table 5.** The top 15 most sensitive reactions for the selected four mechanisms based on the average absolute values  $\overline{S_{abs}}$  (scale: 0 - 1)

Subset 1: Shock tube ignition delay times with constant pressure								
Rank	SanDiego-2014	$\overline{S_{abs}}$	Caltech-2015	$\overline{S_{abs}}$	Aramco-II-2016	$\overline{S_{abs}}$	Glarborg-2018	$\overline{S_{abs}}$
1	H + O <sub>2</sub> = O + OH	0.738	H + O <sub>2</sub> = O + OH	0.678	H + O <sub>2</sub> = O + OH	0.836	H + O <sub>2</sub> = O + OH	0.855
2	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.650	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.362	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.506	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.413
3	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.467	CH <sub>4</sub> + H = CH <sub>3</sub> + H <sub>2</sub>	0.356	CH <sub>4</sub> + H = CH <sub>3</sub> + H <sub>2</sub>	0.441	CH <sub>4</sub> + H = CH <sub>3</sub> + H <sub>2</sub>	0.410
4	CH <sub>4</sub> + H = CH <sub>3</sub> + H <sub>2</sub>	0.412	CH <sub>3</sub> + CH <sub>3</sub> = C <sub>2</sub> H <sub>5</sub> + H	0.279	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>3</sub> O + OH	0.344	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>3</sub> O + OH	0.389
5	CH <sub>3</sub> + H + M = CH <sub>4</sub> + M <sup>LP</sup>	0.361	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>3</sub> O + OH	0.253	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.299	CH <sub>3</sub> + CH <sub>3</sub> = C <sub>2</sub> H <sub>5</sub> + H	0.282
6	CH <sub>3</sub> + CH <sub>3</sub> = C <sub>2</sub> H <sub>5</sub> + H	0.213	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.205	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M	0.254	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.279
7	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M	0.193	C <sub>2</sub> H <sub>6</sub> + M = CH <sub>3</sub> + CH <sub>3</sub> + M	0.203	CH <sub>3</sub> + H + M = CH <sub>4</sub> + M <sup>LP</sup>	0.226	CH <sub>4</sub> + O <sub>2</sub> = CH <sub>3</sub> + HO <sub>2</sub>	0.192
8	CH <sub>4</sub> + OH = CH <sub>3</sub> + H <sub>2</sub> O	0.173	CH <sub>3</sub> + H + M = CH <sub>4</sub> + M <sup>LP</sup>	0.163	CH <sub>4</sub> + OH = CH <sub>3</sub> + H <sub>2</sub> O	0.179	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M	0.184
9	CH <sub>2</sub> O + O <sub>2</sub> = HCO + HO <sub>2</sub>	0.152	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>4</sub> + O <sub>2</sub>	0.151	CH <sub>2</sub> O + O <sub>2</sub> = HCO + HO <sub>2</sub>	0.178	CH <sub>3</sub> + H + M = CH <sub>4</sub> + M <sup>LP</sup>	0.182
10	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M <sup>LP</sup>	0.127	CH <sub>3</sub> + H <sub>2</sub> O <sub>2</sub> = CH <sub>4</sub> + HO <sub>2</sub>	0.124	CH <sub>4</sub> + HO <sub>2</sub> = CH <sub>3</sub> + H <sub>2</sub> O <sub>2</sub>	0.171	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M <sup>LP</sup>	0.129
11	CH <sub>2</sub> O + OH = HCO + H <sub>2</sub> O	0.111	CH <sub>2</sub> O + O <sub>2</sub> = HCO + HO <sub>2</sub>	0.114	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>4</sub> + O <sub>2</sub>	0.161	HCO + O <sub>2</sub> = CO + HO <sub>2</sub>	0.120
12	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>3</sub> O + OH	0.111	C <sub>2</sub> H <sub>6</sub> + M = CH <sub>3</sub> + CH <sub>3</sub> + M <sup>LP</sup>	0.105	HCO + M = H + CO + M	0.107	CH <sub>4</sub> + OH = CH <sub>3</sub> + H <sub>2</sub> O	0.116
13	CH <sub>3</sub> + O = CH <sub>2</sub> O + H	0.105	CH <sub>4</sub> + OH = CH <sub>3</sub> + H <sub>2</sub> O	0.101	CH <sub>3</sub> + O = CH <sub>2</sub> O + H	0.093	HCO + M = H + CO + M <sup>LP</sup>	0.102
14	HCO + M = CO + H + M	0.092	HCO + M = CO + H + M	0.098	HCO + O <sub>2</sub> = CO + HO <sub>2</sub>	0.092	CH <sub>4</sub> + HO <sub>2</sub> = CH <sub>3</sub> + H <sub>2</sub> O <sub>2</sub>	0.101
15	CH <sub>2</sub> O + HO <sub>2</sub> = HCO + H <sub>2</sub> O <sub>2</sub>	0.089	HCO + O <sub>2</sub> = CO + HO <sub>2</sub>	0.083	CH <sub>4</sub> + O = CH <sub>3</sub> + OH	0.085	CH <sub>3</sub> + O = CH <sub>2</sub> O + H	0.095
Subset 2: Shock tube ignition delay times with pressure rise rate								
Rank	SanDiego-2014	$\overline{S_{abs}}$	Caltech-2015	$\overline{S_{abs}}$	Aramco-II-2016	$\overline{S_{abs}}$	Glarborg-2018	$\overline{S_{abs}}$
1	H + O <sub>2</sub> = O + OH	0.858	H + O <sub>2</sub> = O + OH	0.964	H + O <sub>2</sub> = O + OH	0.963	H + O <sub>2</sub> = O + OH	0.903
2	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.652	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.438	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.509	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>2</sub> O + OH	0.394
3	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.416	CH <sub>4</sub> + H = CH <sub>3</sub> + H <sub>2</sub>	0.413	CH <sub>4</sub> + H = CH <sub>3</sub> + H <sub>2</sub>	0.388	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>3</sub> O + OH	0.374
4	CH <sub>4</sub> + H = H <sub>2</sub> + CH <sub>3</sub>	0.378	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>3</sub> O + OH	0.297	CH <sub>3</sub> + HO <sub>2</sub> = CH <sub>3</sub> O + OH	0.335	CH <sub>4</sub> + H = CH <sub>3</sub> + H <sub>2</sub>	0.337
5	CH <sub>3</sub> + H + M = CH <sub>4</sub> + M <sup>LP</sup>	0.216	CH <sub>3</sub> + CH <sub>3</sub> = C <sub>2</sub> H <sub>5</sub> + H	0.280	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.262	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.213
6	CH <sub>4</sub> + OH = H <sub>2</sub> O + CH <sub>3</sub>	0.213	C <sub>2</sub> H <sub>6</sub> + M = CH <sub>3</sub> + CH <sub>3</sub> + M	0.214	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M	0.236	CH <sub>3</sub> + CH <sub>3</sub> = C <sub>2</sub> H <sub>5</sub> + H	0.188
7	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M	0.196	CH <sub>3</sub> + O <sub>2</sub> = CH <sub>3</sub> O + O	0.208	CH <sub>4</sub> + OH = CH <sub>3</sub> + H <sub>2</sub> O	0.207	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M	0.170
8	CH <sub>3</sub> + CH <sub>3</sub> = C <sub>2</sub> H <sub>5</sub> + H	0.163	CH <sub>4</sub> + OH = CH <sub>3</sub> + H <sub>2</sub> O	0.184	CH <sub>2</sub> O + O <sub>2</sub> = HCO + HO <sub>2</sub>	0.160	CH <sub>4</sub> + OH = CH <sub>3</sub> + H <sub>2</sub> O	0.159
9	CH <sub>3</sub> + CH <sub>3</sub> + M = C <sub>2</sub> H <sub>6</sub> + M <sup>LP</sup>	0.150	OH + H <sub>2</sub> = H + H <sub>2</sub> O	0.147	H <sub>2</sub> + OH = H + H <sub>2</sub> O	0.124	CH <sub>4</sub> + O <sub>2</sub> = CH <sub>3</sub> + HO <sub>2</sub>	0.136

10	$\text{CH}_2\text{O} + \text{O}_2 = \text{HCO} + \text{HO}_2$	0.137	$\text{CH}_3 + \text{HO}_2 = \text{CH}_4 + \text{O}_2$	0.143	$\text{CH}_3 + \text{HO}_2 = \text{CH}_4 + \text{O}_2$	0.104	$\text{CH}_3 + \text{CH}_3 + \text{M} = \text{C}_2\text{H}_6 + \text{M}^{\text{LP}}$	0.129
11	$\text{CH}_3 + \text{HO}_2 = \text{CH}_3\text{O} + \text{OH}$	0.123	$\text{C}_2\text{H}_6 + \text{M} = \text{CH}_3 + \text{CH}_3 + \text{M}^{\text{LP}}$	0.138	$\text{CH}_3 + \text{H} + \text{M} = \text{CH}_4 + \text{M}^{\text{LP}}$	0.104	$\text{OH} + \text{H}_2 = \text{H} + \text{H}_2\text{O}$	0.128
12	$\text{H}_2 + \text{OH} = \text{H}_2\text{O} + \text{H}$	0.111	$\text{CH}_2\text{O} + \text{O}_2 = \text{HCO} + \text{HO}_2$	0.113	$\text{CH}_4 + \text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$	0.101	$\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 + \text{M}^{\text{LP}}$	0.112
13	$\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 + \text{M}^{\text{LP}}$	0.104	$\text{CH}_3 + \text{H}_2\text{O}_2 = \text{CH}_4 + \text{HO}_2$	0.100	$\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 + \text{M}^{\text{LP}}$	0.097	$\text{CH}_3 + \text{H} + \text{M} = \text{CH}_4 + \text{M}^{\text{LP}}$	0.081
14	$\text{CH}_2\text{O} + \text{OH} = \text{HCO} + \text{H}_2\text{O}$	0.096	$\text{CH}_3 + \text{H} + \text{M} = \text{CH}_4 + \text{M}^{\text{LP}}$	0.095	$\text{HCO} + \text{M} = \text{H} + \text{CO} + \text{M}$	0.073	$\text{HCO} + \text{O}_2 = \text{CO} + \text{HO}_2$	0.078
15	$\text{CH}_3 + \text{O} = \text{CH}_2\text{O} + \text{H}$	0.088	$\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 + \text{M}^{\text{LP}}$	0.092	$\text{CH}_2\text{O} + \text{H} = \text{HCO} + \text{H}_2$	0.065	$\text{HCO} + \text{M} = \text{H} + \text{CO} + \text{M}^{\text{LP}}$	0.076

Subset 3: RCM measurements

Rank	SanDiego-2014	$\overline{S}_{abs}$	Caltech-2015	$\overline{S}_{abs}$	Aramco-II-2016	$\overline{S}_{abs}$	Glarborg-2018	$\overline{S}_{abs}$
1	$\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$	0.720	$\text{OH} + \text{OH} + \text{M} = \text{H}_2\text{O}_2 + \text{M}^{\text{LP}}$	0.623	$\text{CH}_4 + \text{O} = \text{CH}_3 + \text{OH}$	0.761	$\text{CH}_3 + \text{H} = \text{CH}_2 + \text{H}_2$	0.733
2	$\text{OH} + \text{OH} + \text{M} = \text{H}_2\text{O}_2 + \text{M}^{\text{LP}}$	0.398	$\text{CH}_3 + \text{H}_2\text{O}_2 = \text{CH}_4 + \text{HO}_2$	0.619	$\text{C}_2\text{H}_5\text{OH} + \text{CH}_3\text{O}_2 = \text{C}_2\text{H}_5\text{O} + \text{CH}_3\text{O}_2\text{H}$	0.699	$\text{CH}_2\text{CHO} + \text{CH}_2 = \text{C}_2\text{H}_4 + \text{HCO}$	0.682
3	$\text{CH}_2\text{O} + \text{HO}_2 = \text{HCO} + \text{H}_2\text{O}_2$	0.398	$\text{C}_2\text{H}_6 + \text{M} = \text{CH}_3 + \text{CH}_3 + \text{M}$	0.467	$\text{CH}_4 + \text{OH} = \text{CH}_3 + \text{H}_2\text{O}$	0.579	$\text{HCO} + \text{O}_2 = \text{CO} + \text{HO}_2$	0.653
4	$\text{CH}_4 + \text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$	0.362	$\text{CH}_2\text{O} + \text{HO}_2 = \text{HCO} + \text{H}_2\text{O}_2$	0.356	$\text{CH}_4 + \text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$	0.554	$\text{HCO} + \text{HO}_2 = \text{CO}_2 + \text{OH} + \text{H}$	0.644
5	$\text{CH}_3 + \text{CH}_3 + \text{M} = \text{C}_2\text{H}_6 + \text{M}$	0.344	$\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$	0.343	$\text{HOCHO} + \text{H} \Rightarrow \text{H}_2 + \text{CO} + \text{OH}$	0.469	$\text{CH}_2\text{O} + \text{H} = \text{HCO} + \text{H}_2^{\text{DUP2}}$	0.554
6	$\text{CH}_2\text{O} + \text{O}_2 = \text{HCO} + \text{HO}_2$	0.208	$\text{CH}_3\text{O}_2 + \text{CH}_3 = \text{CH}_3\text{O} + \text{CH}_3\text{O}$	0.341	$\text{HCOH} + \text{OH} = \text{HCO} + \text{H}_2\text{O}$	0.464	$\text{CH}_3\text{OOH} + \text{H} = \text{CH}_2\text{OOH} + \text{H}_2$	0.474
7	$\text{OH} + \text{OH} + \text{M} = \text{H}_2\text{O}_2 + \text{M}$	0.192	$\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2^{\text{DUP2}}$	0.340	$\text{CH}_3 + \text{O} = \text{CH}_2\text{O} + \text{H}$	0.452	$\text{HCO} + \text{OH} = \text{CO} + \text{H}_2\text{O}$	0.457
8	$\text{CH}_4 + \text{OH} = \text{H}_2\text{O} + \text{CH}_3$	0.184	$\text{H} + \text{O}_2 = \text{O} + \text{OH}$	0.320	$\text{H} + \text{O}_2 = \text{O} + \text{OH}$	0.349	$\text{CH}_3 + \text{M} = \text{CH} + \text{H}_2 + \text{M}$	0.398
9	$\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2^{\text{DUP2}}$	0.164	$\text{CH}_3 + \text{HO}_2 = \text{CH}_3\text{O} + \text{OH}$	0.301	$\text{CH}_2\text{O} + \text{H} = \text{HCO} + \text{H}_2$	0.346	$\text{CH}_3\text{O} + \text{CH}_3 = \text{CH}_2\text{O} + \text{CH}_4$	0.391
10	$\text{CH}_2\text{O} + \text{OH} = \text{HCO} + \text{H}_2\text{O}$	0.148	$\text{OH} + \text{OH} + \text{M} = \text{H}_2\text{O}_2 + \text{M}$	0.254	$\text{CH}_3 + \text{OH} = \text{CH}_2 + \text{H}_2\text{O}$	0.315	$\text{H} + \text{O}_2 = \text{O} + \text{OH}$	0.372
11	$\text{H} + \text{O}_2 = \text{OH} + \text{O}$	0.132	$\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 + \text{M}^{\text{LP}}$	0.232	$\text{H}_2\text{O}_2 + \text{M} = \text{OH} + \text{OH} + \text{M}$	0.280	$\text{CH}_3\text{OO} + \text{CH}_2\text{O} = \text{CH}_3\text{OOH} + \text{HCO}$	0.351
12	$\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2^{\text{DUP1}}$	0.123	$\text{CH}_3\text{O}_2 + \text{CH}_2\text{O} \Rightarrow \text{CH}_3\text{O} + \text{OH} + \text{HCO}$	0.216	$\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2^{\text{DUP2}}$	0.275	$\text{H}_2\text{O}_2 + \text{M} = \text{OH} + \text{OH} + \text{M}$	0.303
13	$\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 + \text{M}^{\text{LP}}$	0.104	$\text{CH}_3 + \text{HO}_2 = \text{CH}_4 + \text{O}_2$	0.193	$\text{C}_2\text{H}_5\text{OH} + \text{C}_2\text{H}_5 = \text{P-C}_2\text{H}_4\text{OH} + \text{C}_2\text{H}_6$	0.255	$\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2^{\text{DUP1}}$	0.294
14	$\text{CH}_3 + \text{O}_2 = \text{CH}_3\text{O} + \text{O}$	0.104	$\text{CH}_2\text{O} + \text{O}_2 = \text{HCO} + \text{HO}_2$	0.160	$\text{CH}_3 + \text{O}_2 + \text{M} = \text{CH}_3\text{O}_2 + \text{M}$	0.246	$\text{CH}_2\text{CHO} + \text{O}_2 = \text{CH}_2\text{O} + \text{CO} + \text{OH}$	0.274
15	$\text{CH}_3 + \text{HO}_2 = \text{CH}_3\text{O} + \text{OH}$	0.093	$\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2^{\text{DUP1}}$	0.151	$\text{CH}_4 + \text{H} = \text{CH}_3 + \text{H}_2$	0.242	$\text{HCCO} + \text{HCCO} = \text{C}_2\text{H}_2 + \text{CO} + \text{CO}$	0.213

<sup>LP</sup> Low-pressure limit rate parameters.<sup>DUP1-2</sup> Duplicate reaction; the numbering is in the order of the reactions in the mechanism.

Red shading: six reactions with the highest average absolute scaled sensitivity coefficients.

Yellow shading: six reactions with the next highest average absolute scaled sensitivity coefficients.

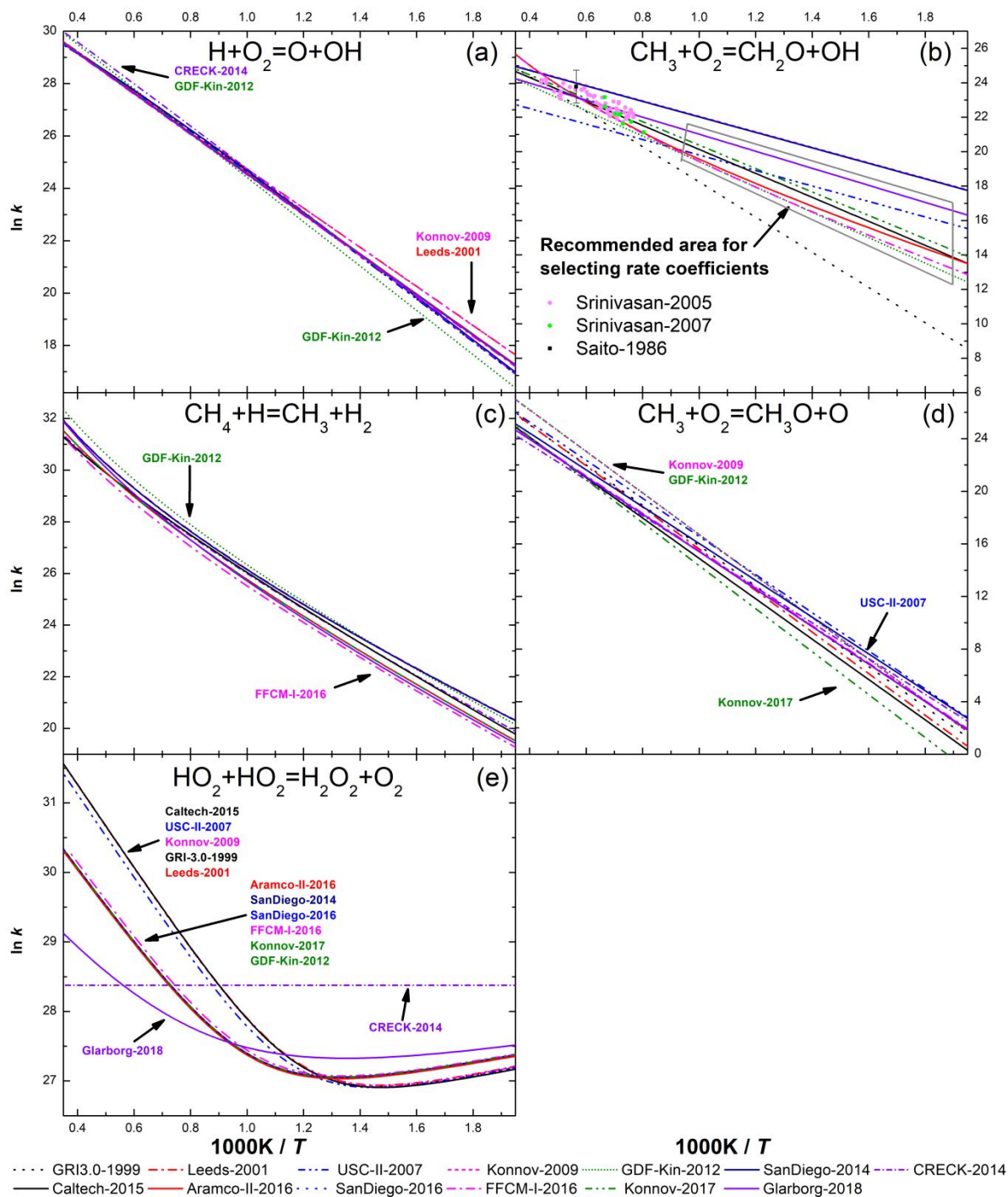
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3 Six reactions, R1:  $\text{H} + \text{O}_2 = \text{O} + \text{OH}$ , R2:  $\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$ , R3:  $\text{CH}_4 + \text{H} = \text{CH}_3 + \text{H}_2$ ,  
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5 R4:  $\text{CH}_3 + \text{O}_2 = \text{CH}_3\text{O} + \text{O}$ , R5:  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2$  (Duplicate 1), R6:  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2$   
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7 +  $\text{O}_2$  (Duplicate 2), are the most sensitive elementary reactions. This list indicates that both  
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9 channels of reaction  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2$  are important. The following analysis investigates  
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11 the sum of the rate coefficients of channels R5 and R6. These six reactions are highlighted by red  
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13 in **Table 5**. The first four reaction steps, R1 to R4, were defined as the most sensitive elementary  
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15 reactions since they have the highest average absolute scaled sensitivity coefficients ( $\overline{(S_{abs})_{avg}}$ ) in  
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17 the two shock tube subsets of **Table 5**. The two channels of the elementary reaction,  $\text{HO}_2 + \text{HO}_2$   
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19 =  $\text{H}_2\text{O}_2 + \text{O}_2$ , were further identified as the most sensitive reaction steps by the RCM subset of  
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24 **Table 5**.

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26 Another group of six reactions is listed as second-level sensitive reactions: R7:  $\text{CH}_4 + \text{OH} = \text{CH}_3$   
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28 +  $\text{H}_2\text{O}$ , R8:  $\text{CH}_3 + \text{H} + \text{M} = \text{CH}_4 + \text{M}$  (LP), R9:  $\text{OH} + \text{H}_2 = \text{H} + \text{H}_2\text{O}$ , R10:  $\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 +$   
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M (LP), R11:  $\text{CH}_4 + \text{O} = \text{CH}_3 + \text{OH}$ , R12:  $\text{CH}_4 + \text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$ . These are highlighted by  
yellow in **Table 5**. The  $\overline{(S_{abs})_{avg}}$  values of R7 and R8 in ST measurements and R7-R10 in ST-PRR  
experiments are between 0.1 and 0.25.

For the most sensitive reactions of the RCM subset, the inconsistency between the four best mechanisms is significant, as shown in **Table 5**. Since Aramco-II-2016 is the only mechanism that had a good performance under RCM conditions, the top four sensitive reactions of Aramco-II-2016 for RCM subset ( $\overline{(S_{abs})_{avg}} > 0.5$ ) are definitely important. However, reaction  $\text{C}_2\text{H}_5\text{OH} + \text{CH}_3\text{O}_2 = \text{C}_2\text{H}_5\text{O} + \text{CH}_3\text{O}_2\text{H}$  is not present in the other mechanisms, therefore the rate coefficient of this reaction cannot be used in comparisons. Considering that reaction  $\text{CH}_4 + \text{OH} = \text{CH}_3 + \text{H}_2\text{O}$  has been identified as the most important reaction in the two subsets of the shock tube measurements,



reactions  $\text{CH}_4 + \text{O} = \text{CH}_3 + \text{OH}$  (R11) and  $\text{CH}_4 + \text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$  (R12) are added to the list of the second-level sensitive reactions.



**Figure 11.** Comparison of the rate coefficients of the five most sensitive reactions: R1:  $\text{H} + \text{O}_2 = \text{O} + \text{OH}$  (a), R2:  $\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$  (b), R3:  $\text{CH}_4 + \text{H} = \text{CH}_3 + \text{H}_2$  (c), R4:  $\text{CH}_3 + \text{O}_2 = \text{CH}_3\text{O}$

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3 + O (d), R5 + R6:  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2$  (e). Panel (b) contains the direct measurement results  
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5 of the R2 rate coefficients from the studies of Srinivasan<sup>121 122</sup> and Saito<sup>123</sup> (only a single point  
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7 with error bar). The units of the rate coefficients are in cm, mol, s.  
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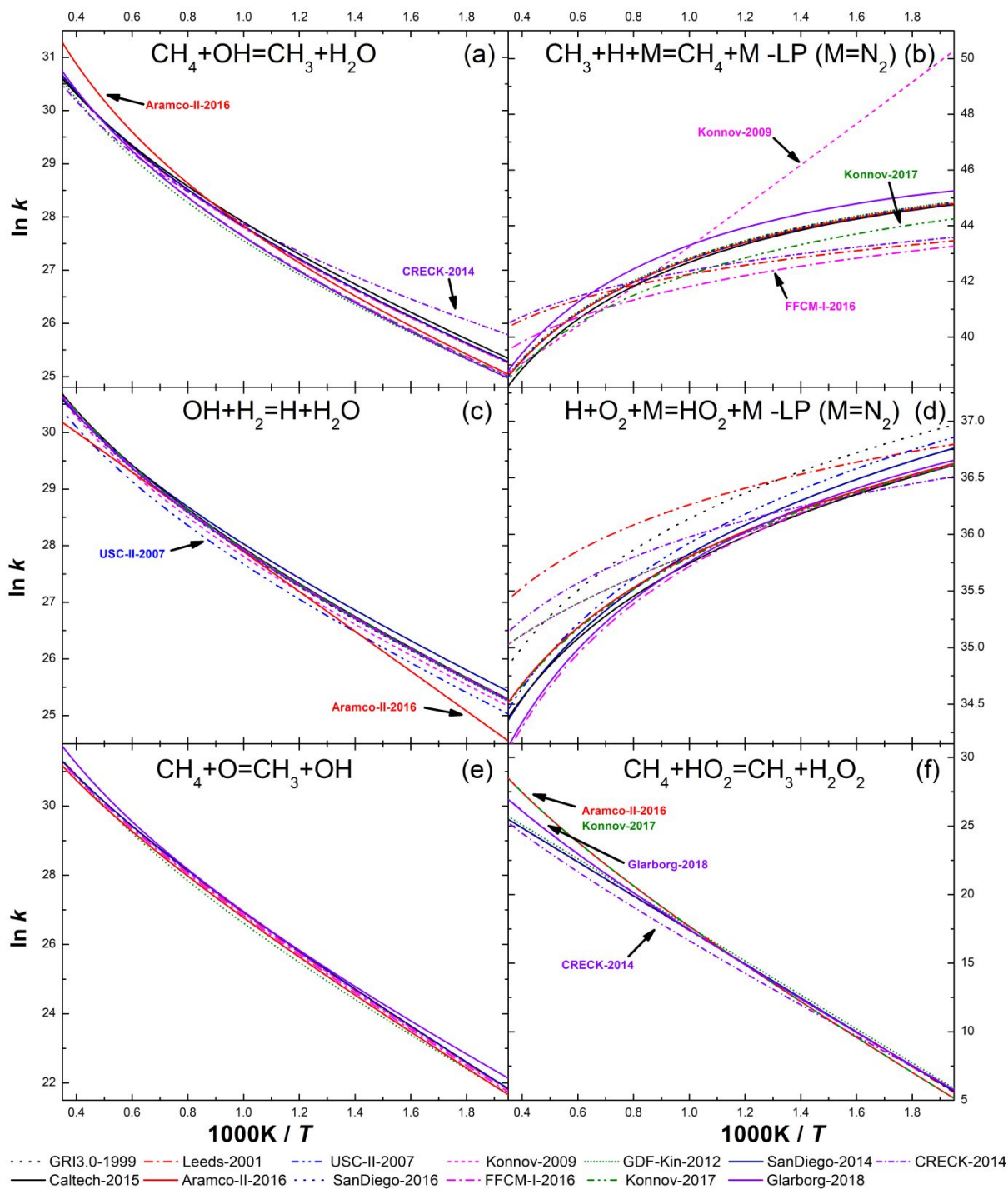
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11 **Figure 11** gives the Arrhenius plots of the five most sensitive reactions as used in the 13  
12 mechanisms. Rate coefficients of the four best mechanisms are drawn by solid lines for an added  
13 emphasis. For R1,  $\text{H} + \text{O}_2 = \text{O} + \text{OH}$  (**Fig. 11(a)**), most mechanisms have similar trends, except  
14 for CRECK-2014 at middle and high temperatures ( $>1100\text{K}$ ) and Leeds-2001 and Konnov-2009  
15 at low temperature ( $<890\text{K}$ ). GDF-Kin-2012 has slight deviation from the other mechanisms in  
16 the whole temperature range. In the case of R2,  $\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$  (b), the rate coefficients  
17 used in the various mechanisms are very different. The  $\ln k$  curves of the four best mechanisms  
18 have four different trends, although Caltech-2015 and Aramco-II-2016 are close to each other.  
19 Considering that the Arrhenius parameters of reaction R2 are very different in the various  
20 mechanisms, we investigated the origin of the Arrhenius parameters of this reaction in each  
21 mechanism. The findings are given in **Table E** of the Supplementary Material. Srinivasan et al.<sup>121</sup>  
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122 and Saito et al.<sup>123</sup> published direct measurement results for the R2 rate coefficient. These  
experimental data are also plotted in the **Fig. 11**. The available direct measurement data are in the  
high temperature range (above 1250 K) and such data are not available at lower temperatures which  
are more critical for the modelling. For reaction R3,  $\text{CH}_4 + \text{H} = \text{CH}_3 + \text{H}_2$  (c), the rate coefficients  
for all the mechanisms have a similar trend. The rate coefficients of GDF-Kin-2012 and FFCM-I-  
2016 are the highest and lowest ones, respectively. R4,  $\text{CH}_3 + \text{O}_2 = \text{CH}_3\text{O} + \text{O}$  (d), is the second  
channel of the reaction between  $\text{CH}_3$  and  $\text{O}_2$  in the present study. Unlike of the first channel, R2,  
the rate coefficients of R4 for all mechanisms have a similar Arrhenius curve. For the four best  
mechanisms, only the rate coefficient of Caltech-2015 deviates significantly at low temperatures

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3 (<820K). R5 and R6 are two duplicate channels of reaction  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2$ . The sum of  
4 these two rate coefficients is plotted in **Fig 11(e)**. At high temperatures channel R5 dominates the  
5 rate coefficient. Caltech-2015, USC-II-2007, Konnov-2009, GRI3.0-1999, Leed-2001 have the  
6 highest R5 rate coefficients and thus the highest overall  $k$  of this reaction, while these mechanisms  
7 have the lowest R6 rate coefficients and thus the lowest overall  $k$  at low temperatures. The  
8 Arrhenius plot of (R5+R6) of Glarborg-2018 is significantly different from all other mechanisms.  
9 CRECK-2014 uses temperature independent rate coefficient for reaction (R5+R6)  $\text{HO}_2 + \text{HO}_2 =$   
10  $\text{H}_2\text{O}_2 + \text{O}_2$ .

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12 Similarly, the Arrhenius plots of the second-level sensitive reactions, R7–R12, are displayed in  
13 **Fig. 12**. For R7,  $\text{CH}_4 + \text{OH} = \text{CH}_3 + \text{H}_2\text{O}$ , the rate coefficient of Aramco-II-2016 is significantly  
14 higher than those of other mechanisms at high temperature, while it decreases rapidly with  
15 decreasing temperature. The Arrhenius plot of reaction R8  $\text{CH}_3 + \text{H} + \text{M} = \text{CH}_4 + \text{M}$  (LP) shows  
16 that mechanisms GRI3.0-1999, USC-II-2007, GDF-Kin-2012, SanDiego-2014, Caltech-2015,  
17 Aramco-II-2016, SanDiego-2016 have identical rate coefficients, while all the other mechanisms  
18 use alternative ones. Konnov-2009 used significantly higher rate coefficient for R8 at low  
19 temperature than the other mechanisms, and in the newer version (Konnov-2017) the rate  
20 coefficient was shifted to a lower level below 1000 K. R9 is a sensitive reaction for ST-PRR  
21 measurements and the Arrhenius plots for all mechanisms are similar, except for Aramco-II-2016;  
22 its rate coefficient is significantly lower than those of other mechanisms. Reaction R10,  $\text{H} + \text{O}_2 +$   
23  $\text{M} = \text{HO}_2 + \text{M}$  (LP), is relatively sensitive in Caltech-2015 at the simulation of RCM measurements,  
24 and the R10 rate coefficient of Caltech-2015 is among the lowest ones in the whole temperature  
25 range. For R11,  $\text{CH}_4 + \text{O} = \text{CH}_3 + \text{OH}$ , the Arrhenius plots are close to each other, while the rate  
26 coefficient of Glarborg-2018 is slightly higher at both lower and higher temperatures. At low  
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temperature, the rate coefficients of R12,  $\text{CH}_4 + \text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$ , are close to each other for all mechanisms, while there are significant differences at high temperatures.



**Figure 12.** Comparison of the rate coefficients of second-level sensitive reactions: R7:  $\text{CH}_4 + \text{OH} = \text{CH}_3 + \text{H}_2\text{O}$  (a), R8:  $\text{CH}_3 + \text{H} + \text{M} = \text{CH}_4 + \text{M}$  (LP) (b), R9:  $\text{OH} + \text{H}_2 = \text{H} + \text{H}_2\text{O}$  (c), R10:  $\text{H} + \text{O}_2 + \text{M} = \text{HO}_2 + \text{M}$  (LP) (d), R11:  $\text{CH}_4 + \text{O} = \text{CH}_3 + \text{OH}$  (e), R12:  $\text{CH}_4 + \text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$  (f).

The units of the rate coefficients are expressed in cm, mol, s.

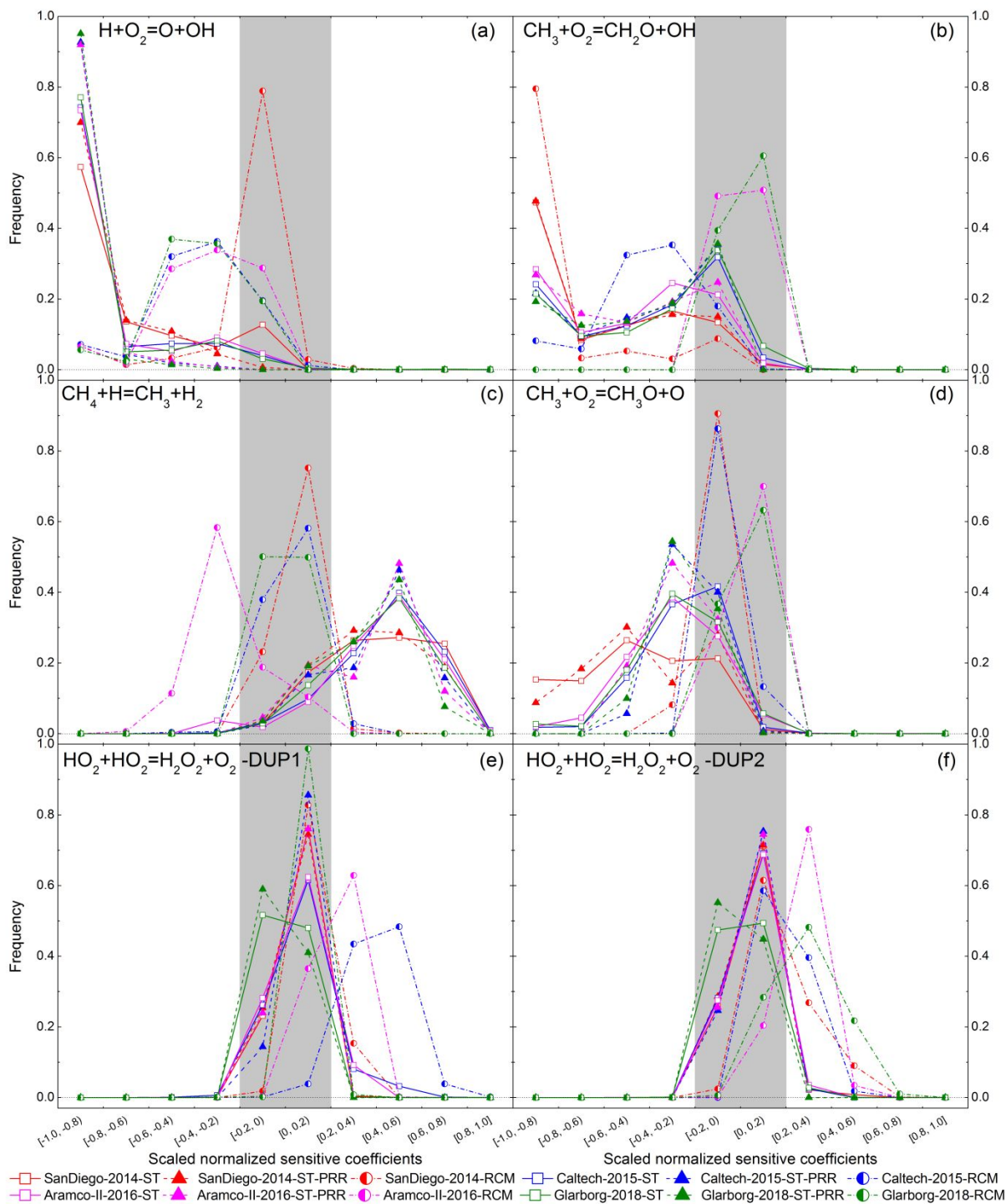
**Figure 13** shows the frequencies of the sensitivity coefficients from R1 to R6. The sensitivity coefficients have little variation for the shock tube measurements (ST and ST-PRR), while for the RCM experiments, the highly sensitive coefficients of identical reactions in different mechanisms have significant discrepancy.

It can be seen from **Fig. 13(a)** that reaction R1 have strong promoting effect for most cases, but the promoting effect in SanDiego-2014 on RCM ignition is very weak. **Fig. 13(b)** shows that reaction R2 shortens the simulated RCM ignition delays in SanDiego-2014; R2 basically performs the role of R1 in this mechanism via the generation of OH from  $\text{O}_2$ . Correspondingly, **Fig. 11(b)** indicates that the rate coefficient of R2 for SanDiego-2014 is large, and **Table 5** shows that R2 has the highest average value of the absolute scaled sensitivity coefficients for the SanDiego-2014 mechanism under RCM conditions. This suggests that the role of reaction R2 at RCM ignition (that is at lower temperatures) deserves further investigations. Performances of mechanisms Caltech-2015, Aramco-II-2016, Glarborg-2018 are good for reproducing ST-IDT (see **Fig. 5(a)**), and Aramco-II-2016, Glarborg-2018 and Konnov-2017 well reproduce RCM-IDT (see **Fig. 5(c)**). Reaction R2 is the only reaction that exhibits much inconsistency at low temperatures (<1200K) among the mechanisms, which indicates that the  $\ln k$  curves for reaction R2 must be within the framed region in **Fig. 11(b)** in the corresponding temperature region.

**Fig. 13(c)** shows that increasing the rate coefficient of reaction R3 extends the shock tube ignition delays, while under RCM conditions it shortens the ignition delays, especially for Aramco-

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3 II-2016. Reaction R4 is able to accelerate the shock tube ignition, while for RCM ignitions the  
4 effect is negligible, as seen from **Fig. 13(d)**. Based on **Fig. 13(e)** and **Fig. 13(f)**, the two channels  
5 of the reaction  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2$  have inhibiting ability to ignition on various extent for all  
6 the mechanisms in RCM simulations, while the scaled sensitivity coefficients for shock tube  
7 ignitions are very low.  
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14 Similar results of sensitivity analysis for reactions R7–R12 are shown in **Fig. S7** in the  
15 Supplementary Material. For reactions R8, R9 and R10 in **Figs. S7 (b), (c), and (d)**, respectively,  
16 it is easy to see that these reactions have slight promoting or depressing influence, in good  
17 accordance for all mechanisms and reaction types. However, it is interesting that reaction R7 ( $\text{CH}_4$   
18 +  $\text{OH} = \text{CH}_3 + \text{H}_2\text{O}$ ) has an opposite effect for ignitions in RCM and shock tube. It is worth noting  
19 that increasing the rate coefficient of R7 (see **Fig. S7(a)**) and R11 (**Fig. S7(e)**) can accelerate the  
20 ignition in the RCM simulations using Aramco-II-2016, while this effect is insignificant in the  
21 other mechanisms. Moreover, **Fig. S7(f)** shows that increasing the rate coefficient of R12 ( $\text{CH}_4 +$   
22  $\text{HO}_2 = \text{CH}_3 + \text{H}_2\text{O}_2$ ) have opposite effect on the RCM ignition delay times using SanDiego-2014  
23 and Aramco-II-2016.  
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**Figure 13.** Frequencies of sensitivity coefficients of R1:  $\text{H} + \text{O}_2 = \text{O} + \text{OH}$  (a), R2:  $\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$  (b), R3:  $\text{CH}_4 + \text{H} = \text{CH}_3 + \text{H}_2$  (c), R4:  $\text{CH}_3 + \text{O}_2 = \text{CH}_3\text{O} + \text{O}$  (d), R5:  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2$  (Duplicate 1) (e), R6:  $\text{HO}_2 + \text{HO}_2 = \text{H}_2\text{O}_2 + \text{O}_2$  (Duplicate 2) (f), for the three types of

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3 measurements (ST, ST-PRR, RCM). The sensitivity analyses were carried out using mechanisms  
4 SanDiego-2014, Caltech-2015, Aramco-II-2016 and Glarborg-2018. The experimental conditions  
5 are given for each type of measurements. The grey shaded rectangle is the domain of low  
6 sensitivity of reactions.  
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13 To sum up, at high temperatures (*i.e.* for shock tube measurements), the sensitivity analysis  
14 results obtained from the four best performing mechanisms have significant consistency. The rate  
15 coefficients of the most sensitive reactions of all mechanisms are similar with each other. The only  
16 significant exception is reaction R2 ( $\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$ ). Based on the performance of the  
17 various mechanisms, the present study indicated that the proper selection of the rate parameters of  
18 R2 reaction is important and the rate coefficient of this reaction has to be determined in further  
19 experimental and theoretical studies at low temperatures.  
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29 The case of low temperature conditions (corresponding mainly to RCM measurements) is very  
30 different. There is an inconsistency of sensitivity analysis results among the various mechanisms  
31 and there are only a few reactions which have high sensitivity according to all the mechanisms. A  
32 better description of the low temperature ignition of methane requires a more accurate  
33 determination of the rate parameters of several reaction steps. As the sensitivity analysis results  
34 indicate, these are mainly the reactions of  $\text{HO}_2$ ,  $\text{H}_2\text{O}_2$ , and alkylperoxides.  
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### 45 6.3 Main differences between the four best mechanisms

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48 The four best mechanisms are Aramco-II-2016, Caltech-2015, Glarborg-2018 and SanDiego-  
49 2014 (in the order of increasing error) on average for the reproduction of ignition delay times of  
50 methane combustion, noting that Aramco-II-2016 was the only one that reproduced well the RCM  
51 measurements. In this section these four mechanisms are compared, using **Figs. S8 to S11** in the  
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Supplementary Material. These figures summarize the simulation and sensitivity analysis results in various intervals of temperature, pressure, equivalence ratio and diluent ratio in measurement categories ST without PRR, ST with PRR and RCM. The bottom of each figure shows the error function value  $E$  for these four mechanisms, averaged for each interval. The upper four rows of panels plot the scaled normalized sensitivity coefficients, calculated by using each of the four mechanisms. The sensitivity coefficients are given for those 99 reactions for which the absolute scaled normalized sensitive coefficient is larger than 0.1 in any condition interval. The same reaction step is indicated with the same legend in each figure and each panel, which allows a transparent comparison of the sensitivity analysis results. **Figures S8 to S11** have a common legend table after **Fig. S11**. It is immediately obvious, that even if the performance of the four mechanisms is very similar in some intervals, the indicated important reactions may be different.

**Fig. S8** shows that the performance of the four mechanisms is similarly good for the ST with PRR measurements in the whole temperature range. Considering the ST without PRR measurements, all mechanisms have a good performance, except for SanDiego-2014 at low temperatures. For SanDiego-2014 at low temperatures, reaction R2:  $\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$  has a considerable promoting effect on ignition (the scaled sensitivity coefficient is nearly  $-1$ , see panel (a)) and this reaction has low sensitivity for the other mechanisms. **Fig. S5(a)** shows that the SanDiego-2014 mechanism tends to estimate shorter IDTs if the temperature is lower than 1400K. The rate coefficient of this reaction in SanDiego-2014 is much higher than in the other mechanisms (see **Fig. 11(b)**) in the whole temperature range. However, decreasing this rate coefficient alone does not improve the performance of the SanDiego-2014 mechanism at low temperatures.

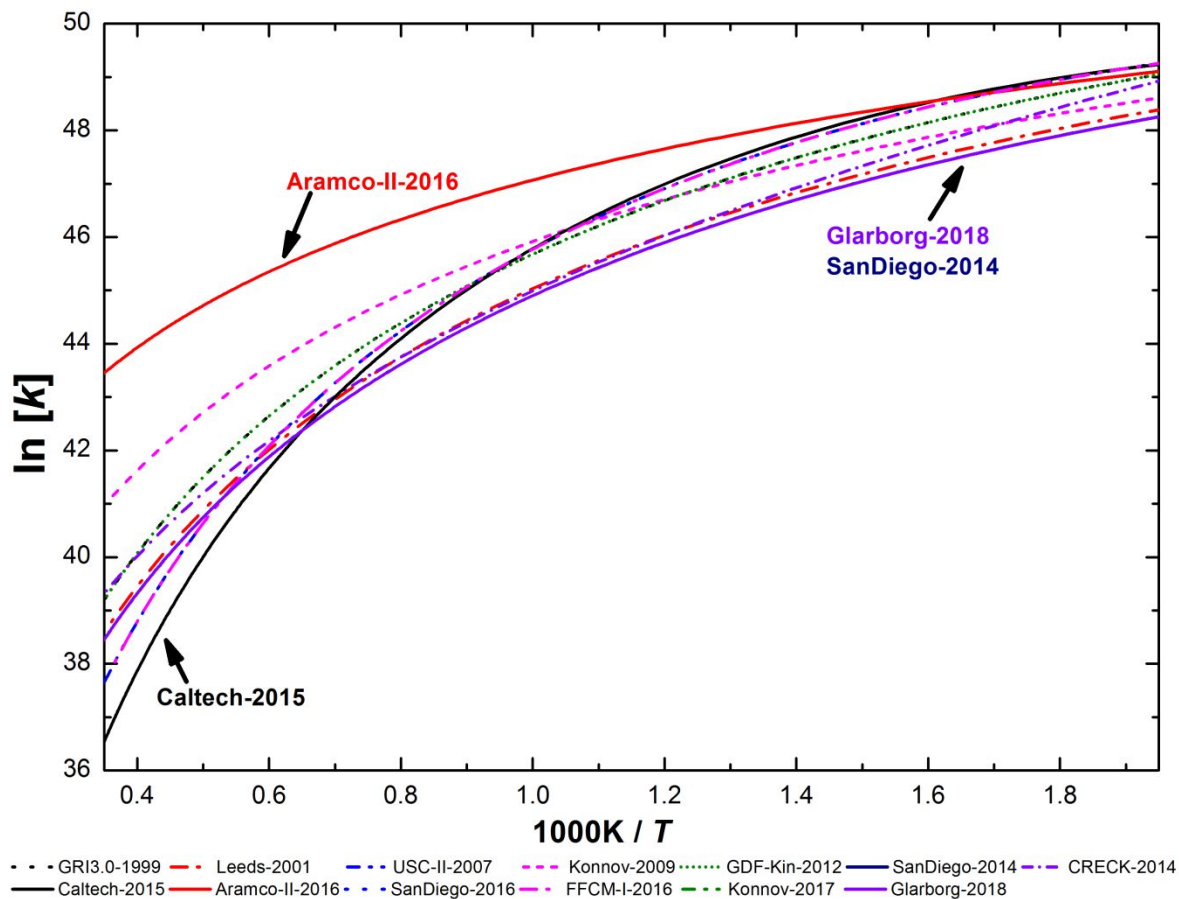
Under high temperature conditions ( $T > 2200\text{K}$ ), all the four mechanisms are relatively inaccurate. Reaction R8:  $\text{CH}_3 + \text{H} + \text{M} = \text{CH}_4 + \text{M}$  (LP) is the only reaction that has large sensitivity

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3 above 2200 K, but much lower sensitivity under other conditions. The rate parameters of this  
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5 reaction deserve a closer look.  
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8 **Fig. S8(o)** shows that only Aramco-II-2016 simulates well the low temperature RCM  
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10 measurements. Aramco-II-2016 is different from the other three mechanisms, since the sensitivity  
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12 analysis results show (see panel (i)) that four reactions,  $\text{CH}_4 + \text{O} = \text{CH}_3 + \text{OH}$  (R11),  $\text{CH}_4 + \text{OH} =$   
13  
14  $\text{CH}_3 + \text{H}_2\text{O}$  (R7),  $\text{C}_2\text{H}_5\text{OH} + \text{CH}_3\text{O}_2 = \text{C}_2\text{H}_5\text{O} + \text{CH}_3\text{O}_2\text{H}$  (\*), and  $\text{CH}_3 + \text{O} = \text{CH}_2\text{O} + \text{H}$  are the  
15  
16 main ignition promoting reactions under RCM conditions. Also,  $\text{HOCHO} + \text{H} \Rightarrow \text{H}_2 + \text{CO} + \text{OH}$   
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18 (\*) is an important ignition hindering reaction in Aramco-II-2016. These reaction steps either do  
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20 not exist in the other three mechanisms (indicated by asterisk), or have a minor role in them.  
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24 Regarding different pressure conditions, **Fig. S9** shows that the four mechanisms reproduce well  
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26 the shock tube experimental data, except for the SanDiego-2014 mechanism above 80 atm for the  
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28 ST data, and the Aramco-II-2016 mechanism near 20 atm for all ST data. In ST measurements  
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30 with PRR, Aramco-II-2016 has the poorest performance. Again, Aramco-II-2016 is the best  
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32 performing mechanism at all pressures under RCM conditions.  
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35 **Figures S10** and **S11** present that the performance of the four mechanisms changes in good  
36  
37 accordance with changing equivalence ratio and dilution, respectively. **Figure S10(m)** shows that  
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39 in the equivalence ratio range [0.60, 0.99), SanDiego-2014 is apparently better than the other  
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41 mechanisms. According to **Fig. S11(m)**, the errors of Aramco-II-2016 and SanDiego-214 are much  
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43 higher than that of Caltech-2015, if the diluent ratio is less than 0.5. The obvious difference among  
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45 all mechanisms is that the sensitivity coefficient of  $\text{CH}_3 + \text{CH}_3 + \text{M} = \text{C}_2\text{H}_6 + \text{M}$  is higher in  
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47 Aramco-II-2016 than in Caltech-2015, and the origin of it is that Aramco-II-2016 uses higher rate  
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49 coefficient for this reaction than the other mechanisms (see **Fig. 14**).  
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**Figure 14.** Comparison of the rate coefficients for reaction  $\text{CH}_3 + \text{CH}_3 + \text{M} = \text{C}_2\text{H}_6 + \text{M}$  ( $\text{M} = \text{N}_2$ ). The units of the rate coefficients are expressed in  $\text{cm}^3 \text{mol}^{-1} \text{s}^{-1}$ .

## 7 Conclusion

Methane is the main component of natural gas, which is a widely used clean fuel, thus accurate simulation of its combustion is of paramount importance. Furthermore, its kinetic mechanism is also an important part of the combustion mechanisms of larger hydrocarbons. Having reviewed the related experimental papers, large amount of measurements of ignition delay times in shock tubes (4939 data points in 574 datasets) and rapid compression machines (582/69) were collected from 73 publications. The initial mixtures included oxygen, diluent ( $N_2$ , Ar, He,  $CO_2$  or  $H_2O$ ), and neat methane or blends of  $CH_4$  with  $H_2$  and/or CO. The details of the experimental datasets are given in the Supplementary Material. All the experimental data were encoded in ReSpecTh Kinetics Data Format v2.3 (RKDF 2.3) XML files, which are freely available at the ReSpecTh Information Site <sup>5</sup>. From this site one can also download code Optima++ <sup>110</sup>, a simulation framework that allows convenient automatic testing of reaction mechanisms against large amount of experimental data by using simulation packages FlameMaster <sup>111</sup> and OpenSMOKE++ <sup>112,113</sup>. The collected ignition delay data were used for mechanism comparison in this study, and these data files may also promote methane mechanism development studies in the future.

We found that 37 different ignition delay time (IDT) definitions have been applied in shock tube measurements. The corresponding IDT definitions were stored in the RKD data files and Optima++ can employ the appropriate IDT definition at the simulations. The only exception was when the experimental ignition delay time was determined based on the vibration relaxation of the produced CO, which would have required the inclusion of an additional detailed submodel, thus the related experimental data were omitted from the comparison.

The shock tube measurement data were published with or without measured pressure rise rate. These were considered as two separate categories of measurements in our investigations and in

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3 general the IDTs of the latter group could be reproduced better. When slightly increasing pressure  
4 was detected but neglected by the experimentalist, we categorized the reasons. For the RCM  
5 measurements, in the various papers we found several different handlings of heat loss during the  
6 compression period, and we recalculated it based on the nonreactive pressure–time histories  
7 whenever these raw data were available. The obtained revised volume–time profiles are published  
8 in the corresponding RKD files.  
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17 We selected 13 widely used methane combustion mechanisms and presented the ranges of  
18 conditions at which these mechanisms had been validated by the original authors. In this study all  
19 mechanisms were tested under much wider ranges of conditions. We compared four excited OH  
20 submechanisms and two excited CH submechanisms that have been published as parts of methane  
21 combustion mechanisms. The excited OH submechanism of Aramco-II-2016 could significantly  
22 improve the performance of several mechanisms, thus it was selected and coupled with those  
23 mechanisms that did not contain such a reaction block. Also, the excited CH submechanism of  
24 Aramco-II-2016 was used in a similar way for the related shock tube experiments.  
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35 Agreement between the experimental data and the simulation results was investigated using the  
36 mean squared and the mean signed errors. Furthermore, Pearson correlation coefficients were used  
37 to characterize the pairwise similarity of the simulation results obtained by the mechanisms.  
38 Whenever it was possible, the published experimental uncertainties were used for the calculation  
39 of the metrics above. In the lack of such information, the uncertainty of the ignition delay time  
40 was estimated from the published uncertainties of temperature and/or pressure using error  
41 propagation. Also, the statistical scatter of the data points in each data series was taken into  
42 account. The derived uncertainty of the experimental data was stored in the RKD data files.  
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3 The results of mechanism comparison studies show that almost all mechanisms reproduced the  
4 high-temperature ignition delay times well, while ignition delay times measured in shock tubes  
5 and rapid compression machines at low temperatures (below 1000 K) could also be well-  
6 reproduced by several mechanisms. It should be noted that Olm et al.<sup>1 2</sup> excluded the low  
7 temperature ( $T < 1000\text{K}$ )  $\text{H}_2$  and  $\text{H}_2/\text{CO}$  shock tube ignition delay data without measured  
8 pressure–time profiles since the mechanisms could reproduce these data poorly. However, in the  
9 present work we found that most mechanisms were able to give reasonable prediction of even the  
10 low temperature ignition delay times. The error function values of Aramco-II-2016 and Glarborg-  
11 2018 were lower than  $E=9$  (i.e. agreement within  $3\sigma$  on average) for the low initial temperature ( $T$   
12  $< 900\text{K}$ ) shock tube measurements. On the other hand, almost half of the mechanisms could  
13 reproduce the long ignition delays ( $> 10^5 \mu\text{s}$ ) measured in shock tubes accurately.  
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29 The performance of the mechanisms was investigated in various ranges of temperature, pressure,  
30 equivalence ratio and diluent ratio. Four mechanisms, Aramco-II-2016, Caltech-2015, Glarborg-  
31 2018 and SanDiego-2014 proved to be generally the best mechanisms, and additionally Aramco-  
32 II-2016 had the smallest prediction error under RCM conditions. We recommend Aramco-II-2016  
33 as the most robust mechanism as it performs reliably under wide range of conditions. However, it  
34 does not mean that Aramco-II-2016 has the best performance under all conditions, since for  
35 example Caltech-2015 has the lowest error in the initial temperature range 1300-1900 K. Therefore,  
36 if an accurate methane combustion mechanism is needed under a specific range of conditions, it  
37 can be selected based on the content of Figs. 5 to 8.  
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49 Local sensitivity analysis was carried out for the best four mechanisms. The 15 most sensitive  
50 reactions of each mechanism in each measurement category were identified and compared. For  
51 high temperature ignitions, the results of sensitivity analysis of the best performing mechanisms  
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3 were similar and the rate coefficients of the most sensitive reactions of all the four mechanisms  
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5 were close to each other. The only exception was reaction  $\text{CH}_3 + \text{O}_2 = \text{CH}_2\text{O} + \text{OH}$ , which was  
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7 highly sensitive according to all mechanisms, but used with very different rate parameters. In the  
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9 case of RCM measurements, there is an inconsistency among the sensitivity analysis results  
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11 obtained for the various mechanisms. The sensitivity analysis results of RCM simulations show  
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13 that the rate parameters of reactions involving peroxides,  $\text{HO}_2$  and  $\text{H}_2\text{O}_2$  have to be known more  
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15 accurately in order to improve the performance of the mechanisms at low temperatures.  
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## 23 ASSOCIATED CONTENT

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26 The following files are available free of charge.

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30 Lists for the details of all collected experimental data collected in this study, method for deriving  
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32 experimental IDT uncertainty, comparison results for OHEX submechanisms, relevant figures and  
33  
34 tables for sensitivity analysis result. (IDT\_R1\_Supp1\_v01.docx)

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38 Detailed estimated standard deviations for some experimental data points used for mechanism  
39  
40 comparison (IDT\_R1\_Supp2\_v01.txt)

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### 43 **Author Contributions** 44

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46 The manuscript was written through contributions from all authors. All authors have given  
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48 approval to the final version of the manuscript.  
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