

## Tilburg University

### A design and a code invariant under the simple group $Co_3$

Haemers, W.H.; Parker, C.; Pless, V.; Tonchev, V.D.

*Publication date:*  
1990

[Link to publication in Tilburg University Research Portal](#)

*Citation for published version (APA):*

Haemers, W. H., Parker, C., Pless, V., & Tonchev, V. D. (1990). *A design and a code invariant under the simple group  $Co_3$* . (Research memorandum / Tilburg University, Department of Economics; Vol. FEW 458). Unknown Publisher.

#### General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

#### Take down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

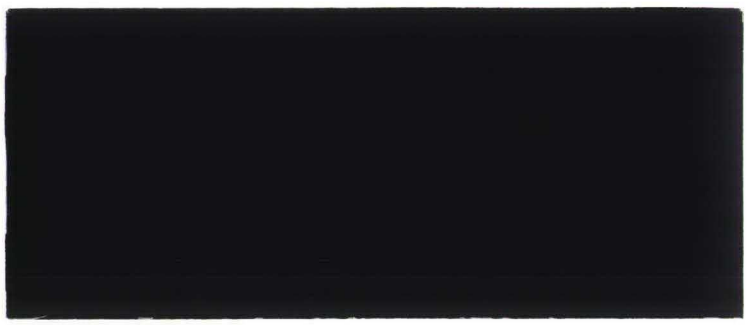
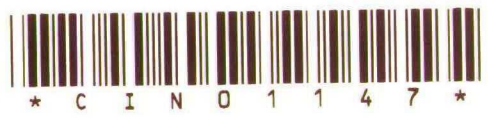
CBM

CBM  
R



POSTBOX 90153  
5000 LE TILBURG  
THE NETHERLANDS

7626  
1990  
458



DEPARTMENT OF ECONOMICS  
RESEARCH MEMORANDUM



A DESIGN AND A CODE INVARIANT UNDER  
THE SIMPLE GROUP  $C_{03}$

Willem H. Haemers, Christopher Parker  
Vera Pless and Vladimir D. Tonchev

FEW 458

R 83  
518. ~~71~~  
J

A DESIGN AND A CODE INVARIANT UNDER THE SIMPLE GROUP  $Co_3$

Willem H. Haemers

Department of Economics, Tilburg University, P.O.Box 90153,  
5000 LE Tilburg, The Netherlands,

Christopher Parker<sup>\*)</sup>

Department of Mathematics, University of Wisconsin-Parkside,  
Box 2000, Kenosha, Wisconsin 53141-2000, USA,

Vera Pless,

Department of Mathematics, University of Illinois at Chicago,  
Box 4348, Chicago, Illinois 60680, USA,

and

Vladimir D. Tonchev<sup>\*)</sup>

Institute of Mathematics, P.O. Box 373, 1090 Sofia, Bulgaria

In memory of Professor Marshall Hall

ABSTRACT

A self-orthogonal doubly-even  $(276,23)$  code invariant under the Conway simple group  $Co_3$  is constructed. The minimum weight codewords form a  $2-(276,100,2 \cdot 3^6)$  doubly-transitive block-primitive design with block stabilizer isomorphic to the Higman-Sims simple group HS. More generally, the codewords of any given weight are single orbits stabilized by maximal subgroups of  $Co_3$ . The restriction of the code on the complement of a minimum weight codeword is the  $(176,22)$  code discovered by Calderbank and Wales as a code invariant under HS.

---

\*) Part of this work was done while these two authors were at the University of Giessen, W. Germany, the first as a NATO Research Fellow, and the second as a Research Fellow of the Alexander von Humboldt Foundation.

## 1. The design

We assume that the reader is familiar with the basic notions and elementary facts from design and coding theory. Our notation follows that from [1], [3], [7], [12], [13], [15] and for groups [5]. We also use some ideas from the theory of strongly regular graphs and regular two-graphs [3], [6], [14].

The design we are going to discuss can be constructed in the spirit of the work by Marshall Hall, Lane and Wales [8], namely by using orbits under finite permutation groups.

The Conway simple group  $Co_3$  can be characterized as the full automorphism group acting 2-transitively on a unique two-graph  $\Omega$  on 276 vertices [4], [6], [14]. The Higman-Sims simple group HS [9] is a maximal subgroup of  $Co_3$  splitting the vertices of  $\Omega$  into two orbits of length 100 and 176 respectively, and acting 2-transitively on the orbit of length 176 and as a rank 3 group on the orbit of length 100. The orbit of the set of 100 vertices of  $G$  fixed by HS under  $Co_3$  is a 2-design  $D$  with 11178 blocks, i.e. a  $2-(276, 100, 2 \cdot 3^6)$  design on which  $Co_3$  acts doubly-transitively on points and primitively on blocks.

An explicit construction of the design  $D$  is obtained by the following permutation presentation of  $Co_3$  which was found by computer using the group theory language CAYLEY. The following two permutations generate  $Co_3$  acting 2-transitively on 276 points:

$$\begin{aligned} \alpha = & (2\ 24\ 3)(4\ 5\ 7)(8\ 189\ 150)(9\ 184\ 144)(10\ 190\ 149)(11\ 183\ 143) \\ & (12\ 192\ 156)(13\ 191\ 153)(14\ 181\ 154)(15\ 182\ 155)(16\ 196\ 146) \\ & (17\ 194\ 148)(18\ 195\ 147)(19\ 193\ 145)(20\ 188\ 151)(21\ 186\ 152) \\ & (22\ 185\ 141)(23\ 187\ 142)(25\ 26\ 27)(29\ 49\ 200)(30\ 50\ 199)(31\ 51\ 198) \\ & (32\ 52\ 197)(33\ 57\ 226)(34\ 58\ 225)(35\ 59\ 228)(36\ 60\ 227)(37\ 55\ 204) \\ & (38\ 56\ 203)(39\ 53\ 202)(40\ 54\ 201)(41\ 47\ 206)(42\ 48\ 205)(43\ 45\ 208) \\ & (44\ 46\ 207)(61\ 121\ 172)(62\ 122\ 171)(63\ 123\ 169)(64\ 124\ 170) \\ & (65\ 127\ 158)(66\ 128\ 157)(67\ 125\ 160)(68\ 126\ 159)(69\ 138\ 162) \\ & (70\ 137\ 161)(71\ 139\ 164)(72\ 140\ 163)(73\ 118\ 174)(74\ 117\ 173) \\ & (75\ 120\ 176)(76\ 119\ 175)(77\ 131\ 177)(78\ 132\ 178)(79\ 130\ 180) \\ & (80\ 129\ 179)(81\ 134\ 168)(82\ 133\ 167)(83\ 136\ 166)(84\ 135\ 165) \end{aligned}$$

(85 91 97)(86 90 98)(89 100 95)(92 99 96)(101 107 113)(102 108 114)  
 (103 105 115)(104 106 116)(209 232 266)(210 236 268)(211 239 272)  
 (212 233 263)(213 231 271)(214 241 265)(215 244 275)(216 237 267)  
 (217 242 269)(218 235 274)(219 229 264)(220 234 273)(221 240 261)  
 (222 243 262)(223 230 270)(224 238 276)(245 255 248)(246 258 253)  
 (247 250 257)251 252 259);

$B = (1\ 117\ 120\ 125)(2\ 78\ 113\ 111)(4\ 167\ 166\ 89)(5\ 148\ 174\ 170)$   
 $(6\ 12\ 56\ 214)(7\ 33\ 250\ 141)(8\ 181\ 25\ 71)(9\ 136\ 124\ 119)$   
 $(10\ 20\ 132\ 178)(11\ 31\ 155\ 213)(13\ 35\ 187\ 264)(14\ 193\ 51\ 210)$   
 $(15\ 240\ 191\ 216)(16\ 152\ 59\ 212)(17\ 137\ 60\ 29)(18\ 134\ 46\ 55)$   
 $(19\ 231\ 233\ 61)(21\ 130\ 58\ 232)(22\ 199\ 189\ 222)(23\ 118\ 197\ 201)$   
 $(24\ 86\ 92\ 159)(26\ 112\ 70\ 267)(27\ 263\ 235\ 194)(28\ 198\ 62\ 228)$   
 $(30\ 224\ 266\ 218)(32\ 140\ 50\ 154)(34\ 40\ 47\ 248)(36\ 244\ 225\ 239)$   
 $(37\ 153)(38\ 176\ 249\ 87)(39\ 165\ 158\ 252)(41\ 150\ 145\ 234)$   
 $(42\ 256\ 162\ 99)(43\ 49\ 52\ 220)(44\ 259\ 192\ 67)(45\ 114\ 79\ 82)$   
 $(48\ 175\ 149\ 247)(53\ 223\ 202\ 207)(54\ 205\ 126\ 122)(57\ 188\ 274\ 138)$   
 $(63\ 80\ 275\ 237)(64\ 72\ 206\ 219)(65\ 236)(66\ 186\ 106\ 268)$   
 $(68\ 271\ 257\ 177)(69\ 273\ 171\ 217)(73\ 164\ 246\ 229)(74\ 102\ 103\ 93)$   
 $(76\ 183\ 258\ 243)(77\ 226\ 196\ 242)(81\ 251\ 168\ 115)(83\ 109)$   
 $(84\ 157\ 173\ 97)(88\ 238)(90\ 262\ 245\ 180)(91\ 95\ 104\ 108)$   
 $(94\ 253\ 116\ 98)(96\ 161\ 107\ 269)(110\ 270\ 215\ 241)(121\ 143\ 146\ 142)$   
 $(128\ 221)(131\ 190\ 139\ 151)(133\ 211)(135\ 200)(147\ 179\ 265\ 261)$   
 $(163\ 260)(169\ 276\ 272\ 185)(172\ 254)(182\ 184\ 208\ 227)(195\ 255).$

As a base block of our design  $D$  we can take the first 100 points  $1, 2, \dots, 100$  since the set-wise stabilizer of this 100-subset turns out to be precisely a group isomorphic to  $HS$ .

Since  $Co_3$  has rank 5 presentation on the blocks of  $D$ , there are at most four (in fact precisely four) intersection numbers: 34, 36, 44, 50. The numbers  $n_i$  ( $i = 34, 36, 44, 50$ ) of blocks intersecting a given block in precisely  $i$  points are listed in Table 1.

Let  $X$  denote the set of 276 points of  $D$  and let  $B$  be a block of  $D$ . Since the stabiliser of  $B$ , a  $HS$ , acts 2-transitively on  $X \setminus B$ , the blocks intersecting  $B$  in a constant number  $i$  of points form a 2-design on  $X \setminus B$

$i$	$n_i$
34	5600
36	4125
44	1100
50	352

Table 1. Block intersection numbers of  $D$

with 176 points and  $n_i$  blocks. The values of  $n_i$  for  $i = 34, 36, 44$  from Table 1 correspond to indices of maximal subgroups of HS (cf. [5]). Therefore, the designs obtained in this way are block primitive under HS. In the case  $i=50$  the 352 blocks intersecting  $B$  in 50 points split into two classes of 176 blocks each in such a way that if  $B_1$  and  $B_2$  intersect  $B$  in 50 points and are disjoint on  $B$  then  $B_1$  and  $B_2$  coincide on  $X \setminus B$ . Therefore, the restrictions of the blocks intersecting  $B$  in 50 points on  $X \setminus B$  form the well-known symmetric  $2$ - $(176, 50, 14)$  design discovered first by G. Higman [10].

## 2. The code

Since the block size is  $100 \equiv 0 \pmod{4}$  and all block intersection numbers are even (i.e., the design  $D$  is self-orthogonal in the terminology of [16]), the rows of the block-point incidence matrix of  $D$  generate a self-orthogonal binary code  $C_{276}$  of length 276 with all weights divisible by 4, i.e.  $C_{276}$  is a doubly-even code. Consequently, the dimension of  $C_{276}$  is at most  $276/2 = 138$ . However, the actual dimension turns out to be as small as 23. A generator matrix for the code is obtained by taking the images of the vector of length 276 and weight 100 with the first 100 positions equal to 1 under the cyclic group of order 23 generated by the following element  $y$  of  $Co_3$ :



$y = (1\ 191\ 184\ 195\ 28\ 63\ 50\ 245\ 5\ 100\ 11\ 97\ 33\ 135\ 218\ 58\ 84\ 76\ 43\ 181\ 130$   
 $151\ 231)(2\ 196\ 246\ 222\ 40\ 36\ 203\ 41\ 83\ 68\ 177\ 260\ 47\ 129\ 263\ 34\ 77\ 228$   
 $85\ 10\ 79\ 150\ 13)(3\ 22\ 271\ 70\ 143\ 145\ 19\ 193\ 138\ 82\ 257\ 221\ 148\ 20\ 4\ 9$   
 $241\ 103\ 205\ 105\ 242\ 157\ 37)(6\ 175\ 171\ 206\ 252\ 87\ 266\ 140\ 39\ 88\ 155\ 119$   
 $229\ 185\ 66\ 94\ 136\ 227\ 247\ 152\ 115\ 256\ 7)(8\ 51\ 240\ 108\ 134\ 170\ 192\ 81$   
 $158\ 189\ 52\ 176\ 141\ 264\ 249\ 212\ 200\ 235\ 166\ 29\ 111\ 96\ 12)(14\ 60\ 210\ 262$   
 $179\ 118\ 174\ 30\ 42\ 75\ 232\ 54\ 99\ 64\ 202\ 214\ 217\ 46\ 122\ 215\ 188\ 194\ 234)$   
 $(15\ 244\ 107\ 38\ 71\ 104\ 123\ 163\ 137\ 258\ 144\ 219\ 182\ 153\ 49\ 265\ 261\ 259$   
 $16\ 272\ 55\ 156\ 35)(17\ 243\ 173\ 61\ 268\ 147\ 48\ 238\ 159\ 124\ 91\ 213\ 236\ 113$   
 $102\ 109\ 169\ 274\ 216\ 207\ 201\ 31\ 237)(18\ 95\ 160\ 65\ 270\ 230\ 116\ 142\ 44$   
 $225\ 255\ 226\ 56\ 110\ 89\ 233\ 167\ 23\ 276\ 199\ 187\ 198\ 132)(21\ 121\ 93\ 57\ 25$   
 $275\ 172\ 220\ 139\ 114\ 209\ 73\ 223\ 248\ 90\ 128\ 146\ 204\ 178\ 133\ 208\ 127\ 74)$   
 $(24\ 101\ 269\ 53\ 98\ 251\ 186\ 273\ 164\ 92\ 27\ 80\ 131\ 62\ 67\ 86\ 72\ 211\ 190\ 168$   
 $125\ 45\ 161)(26\ 162\ 197\ 149\ 254\ 32\ 78\ 180\ 165\ 117\ 267\ 112\ 239\ 183\ 224$   
 $106\ 59\ 126\ 120\ 250\ 154\ 69\ 253).$

The weight distribution of this code was computed by Jesse Nemoier and is listed in Table 2.

$i$	$A_i = A_{276-i}$
0	1
100	11178
112	37950
128	1536975
132	2608200

Table 2. The weight distribution of the code  $C_{276}$ .

#### Notes

(i) It is remarkable that the possible weights are determined by the block intersection numbers (cf. Table 1) and the all-one vector. Furthermore, the minimum weight codewords are precisely the blocks of the design  $D$ .

(ii) By the 2-transitivity of  $Co_3$  on the code coordinates, the codewords of any fixed weight  $w$  form a 2-design. As seen from the list of maximal groups of  $Co_3$  [5], the stabilizer of any (non-zero) codeword is a maximal subgroup of  $Co_3$ :

$$w = 100: HS;$$

$$w = 112: U_4(3): (2^2)_{133};$$

$$w = 128: 2^4.A_8;$$

$$w = 132: 2 \times M_{12}.$$

Therefore, for all designs the group  $Co_3$  acts primitively on blocks.

(iii) Removing a codeword  $x$  of minimum weight and deleting the 100 code coordinates corresponding to the support of  $x$  leads to a  $(176,22)$  code  $C_{176}$  invariant under the Higman-Sims simple group with weight distribution listed in Table 3. In fact this is precisely the code discovered by Calderbank and Wales [2]. This gives a natural embedding of the Higman-Sims group into the Conway group  $Co_3$ .

$i$	$A_i = A_{176-i}$
0	1
50	176
56	1100
64	4125
66	5600
70	17600
72	15400
78	193600
80	604450
82	462000
86	369600
88	847000

Table 3. The weight distribution of the code  $C$

The stabilizers of codewords of weight 50, 56, 64, 66 and 72 are maximal subgroups of HS. The codewords in  $C_{176}$  of the first four non-zero weights are precisely the restrictions of the blocks of D distinct from x on the complement of x (cf. Table 1).

### 3. A construction from the McLaughlin graph

In this section we give a computer-free argument for the dimension of the row space of the incidence matrix of the design D, i.e. the dimension of the code  $C_{276}$ , as well as a construction of D and  $C_{276}$  based on the McLaughlin simple group [11] and the related rank 3 graph on 275 vertices and regular two-graph on 276 vertices [4], [6], [14].

Theorem. Let A be the (0,1)-adjacency matrix of the McLaughlin strongly regular graph with parameters (in the notation of [3])  $n=275$ ,  $a=112$ ,  $c=30$ ,  $d=56$ , and eigenvalues  $r=2$ ,  $s=-28$ . Then the binary code C generated by the columns of the following matrix G,

$$G = \begin{pmatrix} 1 & 0 & \dots & 0 \\ \vdots & & & \\ \cdot & & A & \\ 1 & & & \end{pmatrix}$$

has dimension 23 and is equivalent to  $C_{276}$ .

Proof. Since all columns of G have even weights and the scalar product of any pair of columns is even, the column space of G is a binary self-orthogonal code of length 276. In view of the preceding observations, it is enough to show that the dimension of this column space is at most 23, and the blocks of D are among the codewords of weight 100.

Put  $E = A - 10I - 2J$  (I is the identity and J the all-one matrix). Then  $\text{rank } E = 22$  (the multiplicity of  $-28$  in A). Hence  $\text{rank}_2 E \leq 22$ , so  $\text{rank}_2 A \leq 22$  and  $\dim C \leq 23$ .

Let McL denote the McLaughlin graph on 275 vertices. The graph McL extended by an isolated vertex  $\infty$  is in the switching class of the regular two-graph  $\Omega$  on 276 vertices for which  $\text{Co}_3$  is the full automorphism group. Then  $\Omega$  can be represented by the following graph in its switching class:

$$A^* = \begin{bmatrix} 0 & N_0 \\ N_0^T & B_0 \end{bmatrix} = \begin{bmatrix} 0 & \dots & 0 & 1 & \dots & 1 & 0 & \dots & 0 \\ \vdots & 0 & & N_1 & & N_2 & & & \\ \vdots & & & & & & & & \\ 0 & & & & & & & & \\ 1 & & & & & & & & \\ \vdots & N_1^T & & B_1 & & B_{12} & & & \\ \vdots & & & & & & & & \\ 1 & & & & & & & & \\ 0 & & & & & & & & \\ \vdots & N_2^T & & B_{12}^T & & B_2 & & & \\ \vdots & & & & & & & & \\ 0 & & & & & & & & \end{bmatrix},$$

$\xleftrightarrow{23}$        $\xleftrightarrow{253}$

$\xleftrightarrow{77}$        $\xleftrightarrow{176}$

where:  $N_0$  is an incidence matrix of the unique quasi-symmetric  $4-(23,7,1)$  design;  $N_1$  is its derived and  $N_2$  its residual design; and  $B_i$  ( $i = 0,1,2$ ) is the adjacency matrix of the block graph of  $N_i$ . The group  $HS < Co_3$  has an orbit  $O_1$  of size 100 and an orbit  $O_2$  of size 176 on  $\Omega$ . The sub two-graph induced by  $O_2$  is the Higman-Sims regular two-graph  $\Omega'$ . In the representation above  $\Omega'$  is represented by  $B_2$ , and  $O_1$  induces

$$C = \begin{bmatrix} 0 & \dots & 0 & 1 & \dots & 1 \\ \vdots & 0 & & N_1 & & \\ \vdots & & & & & \\ 0 & & & & & \\ 1 & & & & & \\ \vdots & N_1^T & & B_1 & & \\ \vdots & & & & & \\ 1 & & & & & \end{bmatrix}.$$

Note that if we switch with respect to the upper left entry,  $C$  becomes the adjacency matrix of the Higman-Sims strongly regular graph on 100 vertices with valency 22.

If  $\infty$  does not belong to  $O_2$ , we can choose to isolate, by switching, the upper left entry of  $A^*$  in order to obtain  $A$ . Then

$$A = \begin{bmatrix} 0 & J-N_1 & N_2 \\ J-N_1^T & B_1 & J-B_{12} \\ N_2^T & J-B_{12}^T & B_2 \end{bmatrix}.$$

The row sum matrix is then

$$\begin{bmatrix} 0 & 56 & 56 \\ 16 & 16 & 80 \\ 7 & 35 & 70 \end{bmatrix}.$$

Thus the 77 columns in the middle add up to  $O_2$ .

If  $\omega \in O_2$ , then isolate, by switching, a vertex of  $B_2$ . The remaining vertices of  $O_2$  represent a strongly regular graph  $H$  with 175 vertices and valency 72. After the switching  $O_1$  induces a switched Higman-Sims graph, and thus we have the following structure for  $A$ .

$$A = \begin{bmatrix} B_3 & B_{34} & N_3 \\ B_{34}^T & B_4 & N_4 \\ N_3^T & N_4^T & B_2^* \end{bmatrix},$$

$$\begin{array}{ccc} \longleftrightarrow & \longleftrightarrow & \longleftrightarrow \\ 50 & 50 & 175 \end{array}$$

where  $B_2^*$  is the adjacency matrix of  $H$ , the matrix

$$\begin{bmatrix} B_3 & J-B_{34} \\ J-B_{34}^T & B_4 \end{bmatrix}$$

represents the Higman-Sims graph and  $B_3$  and  $B_4$  are regular with valency 7 (in fact,  $B_3$  and  $B_4$  are Hoffman-Singleton graphs). The row sum matrix now is

$$\begin{bmatrix} 7 & 35 & 70 \\ 35 & 7 & 70 \\ 20 & 20 & 72 \end{bmatrix}.$$

Hence, the first 51 columns of  $C$  add up to  $0_2$ .

### References

1. Th. Beth, D. Jungnickel and H. Lenz. "Design Theory", B.I. Wissenschaftsverlag, Mannheim 1985, and Cambridge University Press, Cambridge 1986.
2. A.R. Calderbank and D.B. Wales, A global Code Invariant under the Higman-Sims group, *J. Algebra*, 75 (1982), 233-260.
3. P.J. Cameron and J.H. van Lint. "Graphs, Codes and Designs", Cambridge Univ. Press, Cambridge 1980.
4. J.H. Conway, Three lectures on exceptional groups, in: M.B. Powell and G. Higman, eds., *Finite Simple Groups* (Academic Press, New York 1971), 215-247.
5. J.H. Conway, R.T. Curtis, S.P. Norton, R.A. Parker, R.A. Wilson, "Atlas of Finite Groups", Clarendon Press, Oxford 1985.
6. J.M. Goethals and J.J. Seidel, The regular two-graph on 276 vertices, *Discr. Math.* 12 (1975) 143-158.
7. M. Hall, Jr. "Combinatorial Theory", 2nd ed., Wiley 1986.
8. M. Hall, Jr., R. Lane, and D. Wales, Designs derived from permutation groups, *J. Combin. Theory* 8 (1970), 12-22.
9. D. Higman and C. Sims, A simple group of order 44, 353, 000, *Math. Z.* 105 (1968), 110-113.
10. G. Higman, On the simple group of D.G. Higman and C.C Sims, *Illinois J. Math.* 13 (1969), 74-80.
11. J. McLaughlin, A simple group of order 898,128,000, in: R. Brauer and C.H. Sah, eds., *Theory of Finite Groups* (Benjamin, New York, 1969), 109-111.
12. F.J. MacWilliams and N.J.A. Sloane. "The Theory of Error-Correcting Codes", North-Holland, Amsterdam 1977.
13. V. Pless, "Introduction to Coding Theory", Wiley, New York 1986.

14. D.E. Taylor, Regular 2-graphs, Proc. London Math. Soc., Ser. 3, 35 (1977), 257-274.
15. V.D. Tonchev. "Combinatorial Configurations", Longman Scientific and Technical, J. Wiley&Sons, New York 1988.
16. V.D. Tonchev, Self-orthogonal designs, Contemporary Math. 101 (1990) (to appear).

## IN 1989 REEDS VERSCHENEN

- 368 Ed Nijssen, Will Reijnders  
"Macht als strategisch en tactisch marketinginstrument binnen de distributieketen"
- 369 Raymond Gradus  
Optimal dynamic taxation with respect to firms
- 370 Theo Nijman  
The optimal choice of controls and pre-experimental observations
- 371 Robert P. Gilles, Pieter H.M. Ruys  
Relational constraints in coalition formation
- 372 F.A. van der Duyn Schouten, S.G. Vanneste  
Analysis and computation of  $(n,N)$ -strategies for maintenance of a two-component system
- 373 Drs. R. Hamers, Drs. P. Verstappen  
Het company ranking model: a means for evaluating the competition
- 374 Rommert J. Casimir  
Infogame Final Report
- 375 Christian B. Mulder  
Efficient and inefficient institutional arrangements between governments and trade unions; an explanation of high unemployment, corporatism and union bashing
- 376 Marno Verbeek  
On the estimation of a fixed effects model with selective non-response
- 377 J. Engwerda  
Admissible target paths in economic models
- 378 Jack P.C. Kleijnen and Nabil Adams  
Pseudorandom number generation on supercomputers
- 379 J.P.C. Blanc  
The power-series algorithm applied to the shortest-queue model
- 380 Prof. Dr. Robert Bannink  
Management's information needs and the definition of costs, with special regard to the cost of interest
- 381 Bert Bettonvil  
Sequential bifurcation: the design of a factor screening method
- 382 Bert Bettonvil  
Sequential bifurcation for observations with random errors



- 383 Harold Houba and Hans Kremers  
Correction of the material balance equation in dynamic input-output models
- 384 T.M. Doup, A.H. van den Elzen, A.J.J. Talman  
Homotopy interpretation of price adjustment processes
- 385 Drs. R.T. Frambach, Prof. Dr. W.H.J. de Freytas  
Technologische ontwikkeling en marketing. Een oriënterende beschouwing
- 386 A.L.P.M. Hendrikx, R.M.J. Heuts, L.G. Hoving  
Comparison of automatic monitoring systems in automatic forecasting
- 387 Drs. J.G.L.M. Willems  
Enkele opmerkingen over het inversificerend gedrag van multinationale ondernemingen
- 388 Jack P.C. Kleijnen and Ben Annink  
Pseudorandom number generators revisited
- 389 Dr. G.W.J. Hendrikse  
Speltheorie en strategisch management
- 390 Dr. A.W.A. Boot en Dr. M.F.C.M. Wijn  
Liquiditeit, insolventie en vermogensstructuur
- 391 Antoon van den Elzen, Gerard van der Laan  
Price adjustment in a two-country model
- 392 Martin F.C.M. Wijn, Emanuel J. Bijnen  
Prediction of failure in industry  
An analysis of income statements
- 393 Dr. S.C.W. Eijffinger and Drs. A.P.D. Gruijters  
On the short term objectives of daily intervention by the Deutsche Bundesbank and the Federal Reserve System in the U.S. Dollar - Deutsche Mark exchange market
- 394 Dr. S.C.W. Eijffinger and Drs. A.P.D. Gruijters  
On the effectiveness of daily interventions by the Deutsche Bundesbank and the Federal Reserve System in the U.S. Dollar - Deutsche Mark exchange market
- 395 A.E.M. Meijer and J.W.A. Vingerhoets  
Structural adjustment and diversification in mineral exporting developing countries
- 396 R. Gradus  
About Tobin's marginal and average  $q$   
A Note
- 397 Jacob C. Engwerda  
On the existence of a positive definite solution of the matrix equation  $X + A^T X^{-1} A = I$

- 398 Paul C. van Batenburg and J. Kriens  
Bayesian discovery sampling: a simple model of Bayesian inference in auditing
- 399 Hans Kremers and Dolf Talman  
Solving the nonlinear complementarity problem
- 400 Raymond Gradus  
Optimal dynamic taxation, savings and investment
- 401 W.H. Haemers  
Regular two-graphs and extensions of partial geometries
- 402 Jack P.C. Kleijnen, Ben Annink  
Supercomputers, Monte Carlo simulation and regression analysis
- 403 Ruud T. Frambach, Ed J. Nijssen, William H.J. Freytas  
Technologie, Strategisch management en marketing
- 404 Theo Nijman  
A natural approach to optimal forecasting in case of preliminary observations
- 405 Harry Barkema  
An empirical test of Holmström's principal-agent model that tax and signally hypotheses explicitly into account
- 406 Drs. W.J. van Braband  
De begrotingsvoorbereiding bij het Rijk
- 407 Marco Wilke  
Societal bargaining and stability
- 408 Willem van Groenendaal and Aart de Zeeuw  
Control, coordination and conflict on international commodity markets
- 409 Prof. Dr. W. de Freytas, Drs. L. Arts  
Tourism to Curacao: a new deal based on visitors' experiences
- 410 Drs. C.H. Veld  
The use of the implied standard deviation as a predictor of future stock price variability: a review of empirical tests
- 411 Drs. J.C. Caanen en Dr. E.N. Kertzman  
Inflatieneutrale belastingheffing van ondernemingen
- 412 Prof. Dr. B.B. van der Genugten  
A weak law of large numbers for  $m$ -dependent random variables with unbounded  $m$
- 413 R.M.J. Heuts, H.P. Seidel, W.J. Selen  
A comparison of two lot sizing-sequencing heuristics for the process industry

- 414 C.B. Mulder en A.B.T.M. van Schaik  
Een nieuwe kijk op structuurwerkloosheid
- 415 Drs. Ch. Caanen  
De hefboomwerking en de vermogens- en voorraadaf trek
- 416 Guido W. Imbens  
Duration models with time-varying coefficients
- 417 Guido W. Imbens  
Efficient estimation of choice-based sample models with the method of moments
- 418 Harry H. Tigelaar  
On monotone linear operators on linear spaces of square matrices

## IN 1990 REEDS VERSCHENEN

- 419 Bertrand Melenberg, Rob Alessie  
A method to construct moments in the multi-good life cycle consumption model
- 420 J. Kriens  
On the differentiability of the set of efficient  $(\mu, \sigma^2)$  combinations in the Markowitz portfolio selection method
- 421 Steffen Jørgensen, Peter M. Kort  
Optimal dynamic investment policies under concave-convex adjustment costs
- 422 J.P.C. Blanc  
Cyclic polling systems: limited service versus Bernoulli schedules
- 423 M.H.C. Paardekooper  
Parallel normreducing transformations for the algebraic eigenvalue problem
- 424 Hans Gremmen  
On the political (ir)relevance of classical customs union theory
- 425 Ed Nijssen  
Marketingstrategie in Machtspectief
- 426 Jack P.C. Kleijnen  
Regression Metamodels for Simulation with Common Random Numbers: Comparison of Techniques
- 427 Harry H. Tigelaar  
The correlation structure of stationary bilinear processes
- 428 Drs. C.H. Veld en Drs. A.H.F. Verboven  
De waardering van aandelenwarrants en langlopende call-opties
- 429 Theo van de Klundert en Anton B. van Schaik  
Liquidity Constraints and the Keynesian Corridor
- 430 Gert Nieuwenhuis  
Central limit theorems for sequences with  $m(n)$ -dependent main part
- 431 Hans J. Gremmen  
Macro-Economic Implications of Profit Optimizing Investment Behaviour
- 432 J.M. Schumacher  
System-Theoretic Trends in Econometrics
- 433 Peter M. Kort, Paul M.J.J. van Loon, Mikuláš Luptacik  
Optimal Dynamic Environmental Policies of a Profit Maximizing Firm
- 434 Raymond Gradus  
Optimal Dynamic Profit Taxation: The Derivation of Feedback Stackelberg Equilibria

- 435 Jack P.C. Kleijnen  
Statistics and Deterministic Simulation Models: Why Not?
- 436 M.J.G. van Eijs, R.J.M. Heuts, J.P.C. Kleijnen  
Analysis and comparison of two strategies for multi-item inventory systems with joint replenishment costs
- 437 Jan A. Weststrate  
Waiting times in a two-queue model with exhaustive and Bernoulli service
- 438 Alfons Daems  
Typologie van non-profit organisaties
- 439 Drs. C.H. Veld en Drs. J. Grazell  
Motieven voor de uitgifte van converteerbare obligatieleningen en warrantobligatieleningen
- 440 Jack P.C. Kleijnen  
Sensitivity analysis of simulation experiments: regression analysis and statistical design
- 441 C.H. Veld en A.H.F. Verboven  
De waardering van conversierechten van Nederlandse converteerbare obligaties
- 442 Drs. C.H. Veld en Drs. P.J.W. Duffhues  
Verslaggevingsaspecten van aandelenwarrants
- 443 Jack P.C. Kleijnen and Ben Annink  
Vector computers, Monte Carlo simulation, and regression analysis: an introduction
- 444 Alfons Daems  
"Non-market failures": Imperfecties in de budgetsector
- 445 J.P.C. Blanc  
The power-series algorithm applied to cyclic polling systems
- 446 L.W.G. Strijbosch and R.M.J. Heuts  
Modelling (s,Q) inventory systems: parametric versus non-parametric approximations for the lead time demand distribution
- 447 Jack P.C. Kleijnen  
Supercomputers for Monte Carlo simulation: cross-validation versus Rao's test in multivariate regression
- 448 Jack P.C. Kleijnen, Greet van Ham and Jan Rotmans  
Techniques for sensitivity analysis of simulation models: a case study of the CO<sub>2</sub> greenhouse effect
- 449 Harrie A.A. Verbon and Marijn J.M. Verhoeven  
Decision-making on pension schemes: expectation-formation under demographic change

- 450 Drs. W. Reijnders en Drs. P. Verstappen  
Logistiek management marketinginstrument van de jaren negentig
- 451 Alfons J. Daems  
Budgeting the non-profit organization  
An agency theoretic approach
- 452 W.H. Haemers, D.G. Higman, S.A. Hobart  
Strongly regular graphs induced by polarities of symmetric designs
- 453 M.J.G. van Eijs  
Two notes on the joint replenishment problem under constant demand
- 454 B.B. van der Genugten  
Iterated WLS using residuals for improved efficiency in the linear  
model with completely unknown heteroskedasticity
- 455 F.A. van der Duyn Schouten and S.G. Vanneste  
Two Simple Control Policies for a Multicomponent Maintenance System
- 456 Geert J. Almekinders and Sylvester C.W. Eijffinger  
Objectives and effectiveness of foreign exchange market intervention  
A survey of the empirical literature
- 457 Saskia Oortwijn, Peter Borm, Hans Keiding and Stef Tijs  
Extensions of the  $\tau$ -value to NTU-games

Bibliotheek K. U. Brabant



17 000 01086043 6