

An individual based computational model of intestinal crypt fission and its application to predicting unrestrictive growth of the intestinal epithelium

| Journal: | Integrative Biology | |
|---|--|--|
| Manuscript ID: | Draft | |
| Article Type: | Paper | |
| Date Submitted by the Author: | n/a | |
| Complete List of Authors: | pin, carmen; institute of Food Research, Parker, Aimee; Institute of Food Research, Gut Health Food Safety gunning, allan; institute of food research, food and health Ohta, Yuki; Keio University, School of Medicine Johnson, Ian; Institute of Food Research, Carding, Simon; Institute of Food Research, Sato, Toshiro; Keio Univeristy, | |
| | | |
| Note: The following files were submitted by the author for peer review, but cannot be converted to PDF. You must view these files (e.g. movies) online. | | |
| Supplementary_Video S1.qt Supplementary_Video S2.qt | | |

SCHOLARONE[™] Manuscripts



Institute of Food Research Norwich Research Park Colney Norwich NR4 7UA UK www.ifr.ac.uk

Norwich, 10 March 2014

Intestinal crypt fission is a homeostatic phenomenon, observed rarely in healthy adult mucosa, which also plays a pathological role as the main mode of growth of intestinal polyps. Difficulties in observing experimentally crypt fission has limited its understanding. Recently developed experimental techniques have been integrated with theoretical models in order to gain novel insights into this process. An agent based model has been combined with measurements from *in vitro* culturing intestinal organoids to develop an innovative computational approach able to simulate the process of crypt fission and further to extrapolate predictions for the growth of adenomatous polyps in the intestinal epithelium.

The Institute of Food Research is a registered charity (No. 1058499) and a company limited by guarantee (registered in England and Wales No. 03009972). VAT registration No. GB 688 8914 52

Monday, 16 October 2014

Dear Dr Barcellos-Hoff:

Revised version of Manuscript ID IB-ART-03-2014-000055

Title: An individual based computational model of intestinal crypt fission and its application to predicting unrestrictive growth of the intestinal epithelium

We are very thankful for the opportunity of revising and resubmitting our manuscript and for the extra time given to address all reviewers' concerns.

We would like to thank the referees for their constructive comments and wise suggestions that in our opinion have contributed to strengthen the work presented here. As suggested, we have carried out additional experiments in order to verify the position of stem and Paneth cells in the organoids (point 2 reviewer 1) and to measure the biomechanical properties of stem and Paneth cells by Atomic Force Microscopy (AFM) in order to support our hypothesis with experimental evidences (Point 1 reviewer 2 and general concern of reviewer2). The generation of new data involving experiments with LGr5+ GFP mice, fluorescent labelling and imaging of grown organoids and AFM measurements were the reason for the extra time required to prepare this revised version.

The generation of new data also involved the addition of new co-authors in this paper: Yuki Ohta carried out the fluorescent labelling and imaging of stem and Paneth cells in organoids generated from Lgr5+ mice crypts at Keio University; Aimee Parker and A. Patrick Gunning carried out AFM measurements on stem and Paneth cells isolated from Lgr5+ mice crypts at the institute of Food Research.

We would be glad if you could consider the revised version of this manuscript for publication in the journal Integrative Biology. A point by point reply to the reviewers' comments is attached below.

Best regards Carmen Pin

Reviewer(s)' Comments to Author: <u>Referee: 1</u>

Comments to the Author

The article propose a very interesting and innovative theory, according to which the process of crypt fission is driven by a difference between the biomechanical properties of Paneth cells respect to stem cells.

This hypothesis is confirmed by the agreement between the computational model (built on the mentioned hypothesis) and the dynamics observed in an in vitro organoid model. The computational model looks complete and detailed. The fluid mechanic approach is innovative.

Nevertheless, there is no evidence that the claimed difference in biomechanical properties could be true, nor in vivo nor in vitro.

<u>Response.</u> We have measured mechanical properties of Lgr5+ stem cells and of nonfluorescent cells. Results explained below in response to question 1.

Also, it is not clear in the method how the difference in biomechanical properties is set in the computational model (a "force" is compared to a "size").

<u>Response.</u> The Model section has been rewritten and forces definition and all estimations clarified. See "Biomechanical model for the initiation of buds" in the Material and Methods section of the revised version of the paper

In my opinion, to be a reliable hypothesis there is the need of:

1) Experimental data on the biomechanical properties of paneth and stem cells (i.e., by atomic force microscopy).

We have measured the Young modulus of Lgr5+ stem cells and of non-fluorescent cells by AFM. Results are shown in Figure 3. The following paragraph has been added to the results

"In order to support this hypothesis, Atomic Force Microscopy (AFM) has been used to measure the Young modulus of Lgr5-eGFP positive cells and Lgr5-eGFP negative large granular crypt cells. The Young modulus is a measure of stiffness that quantifies the linear stress-strain relationship in the range of stress where Hook's law holds. Figure 3A shows that the Young modulus of all but one of the Lgr5-eGFP positive cells was significantly smaller than that of large granular cells by more than 3 times the standard deviation. Lgr5-eGFP positive cells, which were assumed to be stem cells, required significantly smaller forces to undergo deformation than large granular cells behave as viscous materials rather than the solid material behaviour described in previous models. Viscoelastic behaviour of cells was demonstrated in force curves. AFM measurements showed the typical separation, or hysteresis, between the approach and retract force curves resulting from viscous behaviour in all assessed cells (Figure 3B). "

2) Fluorescent labeling and imaging of paneth cells and stem cells on the organoids to verify their positions.

Fluorescent labelling and imaging of Paneth cells and stem cells on the organoids has been carried out and it is shown in Figure 1.

The following paragraph has been added to the manuscript:

"In mouse intestinal organoid cultures, bud formation takes place initially in regions of the primary cyst with high Paneth cell density; initial buds grow into crypts which contain Paneth and stem cells intermingling at their bases (Figure 1)."

3) Sensibility analysis on the parameters of the computational model, in particular on the value of the threshold "C", which has to be related to biologically relevant values of Young modulus.

Sensitivity analysis has been carried out for the shear stress threshold in Paneth cells. Results are presented in Figure 4 are described in the following paragraph:

"Figure 4A compares the time intervals between successive budding events observed in vitro with the intervals simulated using several values for the parameter α . This parameter governs the force threshold required for Paneth cell deformation. When α =0, Paneth cells have identical mechanical properties to stem cells. When $\alpha=1$, the force required to deform Paneth cells is equal to the force generated by a disequilibrium between available and required space equal to one average cell size; if α is smaller or greater than 1, Paneth cell deformation requires forces smaller or greater, respectively, than that generated by one extra cell. When crypts were simulated with $\alpha=0$ and $\alpha=0.1$, Paneth cells were deformed, and changes in cell size were translated in the flow of cell contents from crypt bottom to top without deformations of the crypt wall. This unimpeded flow was due to the non-stress boundary at the top of the crypt because of unrestrictive cell removal. As the value of α increased, Paneth cells became more resistant to deformation so that the increase in size and/or decrease of available space during the cell cycle was not accommodated by the nondeformable neighbouring Paneth cells, leading to protrusion of cell material out of the crypt wall and bud formation. In simulated crypts, the frequency of budding increased rapidly as the value of α increased from 0 to 1. The best agreement between simulated and observed distributions of frequencies for the time interval between successive budding events was observed for values of α slightly greater than 1. For instance, the smallest difference between the simulated and observed distribution was detected for α =1.3 (Figure 4B)."

Referee: 2

Comments to the Author

I found the individual based model of intestinal crypt fission to be quite interesting. However, below are suggestions for improvement.

The major weakness of the manuscript is that there is no experimental evidence to support their hypothesis underlying bud initiation, which is that bud initiation results from a difference in the biomechanical behavior of neighboring Paneth and stem cells. However, this is now a prediction from their model since it led to simulation results that matched experimental data at various levels. The manuscript would benefit significantly if they were able to validate this prediction, especially since this prediction is presented very early on in the manuscript and it sets the foundation for the rest of the experiments. Without this, it's unclear exactly what biological insights are gained from the current state of the model and the simulation results. There isn't a strong enough argument presented against modeling fission as a buckling process alone to support this new hypothesis.

We agree with the referee that the novelty of our work is showing an alternative mechanism for crypt fission based on differences on the mechanical features of stem and Paneth cells. To support experimentally our main hypothesis that Paneth cells are more resistant to deformation than Stem cells, we have measured the Young's modulus of Lgr5+ stem cells and of non-fluorescent cells by AFM. Results are shown in Figure 3 and the following paragraph has been added to the results:

"In order to support this hypothesis, Atomic Force Microscopy (AFM) has been used to measure the Young modulus of Lgr5-eGFP positive cells and Lgr5-eGFP negative large granular crypt cells. The Young modulus is a measure of stiffness that quantifies the linear stress-strain relationship in the range of stress where Hook's law holds. Figure 3A shows that the Young modulus of all but one of the Lgr5-eGFP positive cells was significantly smaller than that of large granular cells by more than 3 times the standard deviation. Lgr5-eGFP positive cells, which were assumed to be stem cells, required significantly smaller forces to undergo deformation than large granular cells, which were assumed to be Paneth cells. Moreover, we have assumed that cells behave as viscous materials rather than the solid material behaviour described in previous models. Viscoelastic behaviour of cells was

demonstrated in force curves. AFM measurements showed the typical separation, or hysteresis, between the approach and retract force curves resulting from viscous behaviour in all assessed cells (Figure 3B). "

We are proposing an alternative mechanism for crypt fission and we show that it is feasible by multiple validations between observed and simulated results. We model the epithelium as formed by individual viscous cells with different properties instead of as a solid beam/layer. The immediate improvement in our approach is that cells rae treated as viscous materials, which is what they are according to physical measurements; moreover in this revised version we present some evidence of the different biomechanical properties between stem cells and non-stem cells.

In addition, it could also be pointed out that previous studies modelling fission as a buckling process have been mainly theoretical articles with no experimental evidence supporting the solid mechanical behaviour of the epithelium, and very few –if any- comparisons between predictions and observations.

"(Figure 2E)" should be changed to "(Figure 2D)"

This has been corrected in the revised version of the manuscript. All figures are renumbered in the revised manuscript and Figure 2E is now Figure 4H which was the previous Figure 2D.

I felt that many details of the model were missing and should be included in supplementary. How many simulations were performed? With a monte carlo simulation, each will lead to a different result. From Fig 3 legend, it looks like 89 simulations were performed. Were the same 89 simulations used to create all of the results?

New simulations have been run in order to carry out a detailed analysis of the effect of the value of shear stress threshold of Paneth cells on model predictions. Fig 3 is now Fig 4, which merges previous Figs 2 and 3, and presents the comparison between fission measurements in simulated crypts and in cultured organoids. To do this, 30-40 crypts were simulated for 12 days, which matches the observation period in vitro, for each tested value of α . Twelve values were tested.

This is clarified in Figure 4 –former Fig 3- legend as follows

"Figure 4. Comparison between fission measurements in simulated crypts and in cultured organoids: (A) Observed (black bars; n=22 initial crypts) and simulated (red bars; n=30-40 initial crypts simulated during 12 days for each tested value of α) distributions for the time interval between successive budding processes per crypt. Plots show the results obtained with twelve values of the parameter α , from 0.1 to 2, which controls the force required to deform Paneth cells"

It is interesting that their model can recapitulate many features observed in vitro. For example, (1) time interval between consecutive budding events, (2) crypt growth rates, and (3) positioning of the secondary crypts. Hopefully, these results are from simulations using the same model parameter values. A table of the final parameter values used should be provided in supplementary. Are any of these parameters based on biological data.

Supplementary Table 1 with all parameters used in the simulations is provided in the revised manuscript. All simulations were run with the values presented in the Table, which are based on biological data.

As pointed out by the referee, many features observed in the simulations recapitulate observations in vivo. This is in part due to the fact that the value of the parameters of the individual based model has been chosen to minimize the error between predictions and

observations. For instance, α =1.3 minimize the error between the observed and simulated time interval between consecutive budding events.

In other cases, the good agreement between simulated and observed results indicates that hypotheses behind the individual based model are sufficient to describe crypt behaviour during fission. For example, the good agreement between the growth rates of the secondary crypt in simulated and in observed fission events indicates that the elongation of the secondary crypt is can be explained by cell proliferation which takes place at the same rate as in the primary crypt. The close agreement between simulated and observed migration rates of the secondary crypt are sufficient to explain the upward migration of the secondary crypt are sufficient to explain the upward migration of the secondary crypt.

This is now clarified in the text.

I question whether other computational models that simulate fission as a buckling process can also recapitulate these same features given the right parameter combination. Yes, it is possible.

Agreement between predictions and observations is necessary but not sufficient for model evaluation.

The essential difference between our approach and previous approaches, assuming a "solid beam" is that in those, cells are modelled as solid materials, whereas we treat them as viscous materials. AFM measurements confirmed the viscous nature of both LGR5-eGFP positive cells and large granular non-fluorescent cells isolated from crypts (Figure 3B). This indicates that our model is correct.

page 3 "became" should be "become"

Corrected in the new version of the manuscript.

In the discussion, the authors state that a distinctive feature of their model is that they do not model the process as the folding or buckling of a solid material like others before. Instead, fission results from modeling the fluid mechanics at the individual cell level. This feature should be emphasized more in the manuscript as it is a key advantage of the other models.

We have modified the following section to emphasize this point:

"A distinctive feature of our approach to modelling crypt fission is that we treat cells as viscous materials rather than assuming the solid material behaviour described in the models discussed above. In agreement with in vitro experimental observations, we have modelled fission as a budding process based on fluid mechanics at the individual cell level and not, as the folding or buckling of solid material. AFM measurements confirmed the viscous nature of both LGR5-eGFP positive and LGR5-eGFP negative large and granular single cells isolated from crypts (Figure 3B). Moreover, we modelled fission as a consequence of inequalities in the mechanical properties of viscoelastic cells which depend on cell lineage. This hypothesis was also supported experimentally by AFM measurements of single cells, which revealed that stem cells are less stiff than other granular large crypt cells."

An individual based computational model of intestinal crypt fission 1 and its application to predicting unrestrictive growth of the intestinal 2 3 epithelium 4 Carmen Pin^{1*}, Aimee Parker¹, A. Patrick Gunning², Yuki Ohta³, Ian T. Johnson², 5 Simon R. Carding^{1,4} and Toshiro Sato³ 6 7 ¹Gut Health and Food Safety Research Programme, ²Food and Health Research 8 9 Programme, Institute of Food Research, Norwich. NR4 7UA. UK ³School of Medicine, Keio University, Shinjuku-ku, Tokyo 160-8582 Japan 10 ⁴Norwich Medical School, University of East Anglia, Norwich. NR4 7TJ. UK. 11 12 13 14 *Corresponding author: 15 carmen.pin@ifr.ac.uk 16 Tel: +441603255000 17 Fax: +441603507723 18 19 20

21

22 Abstract

Intestinal crypt fission is a homeostatic phenomenon, observable in healthy adult mucosa, but which also plays a pathological role as the main mode of growth of some intestinal polyps. Building on our previous individual based model for the small intestinal crypt and on *in vitro* cultured intestinal organoids, we here model crypt fission as a budding process based on fluid mechanics at the individual cell level and extrapolated predictions for growth of the intestinal epithelium.

29 Budding was always observed in regions of organoids with abundant Paneth 30 cells. Our data support a model in which buds are biomechanically initiated by single 31 stem cells surrounded by Paneth cells which exhibit greater resistance to viscoelastic 32 deformation, a hypothesis supported by atomic force measurements of single cells. 33 Time intervals between consecutive budding events, as simulated by the model and 34 observed *in vitro*, were 2.84 and 2.62 days, respectively. Predicted cell dynamics was 35 unaffected within the original crypt which retained its full capability of providing 36 cells to the epithelium throughout fission. Mitotic pressure in simulated primary crypts forced upward migration of buds, which simultaneously grew into new 37 protruding crypts at a rate equal to 1.03 days⁻¹ in simulations and 0.99 days⁻¹ in 38 39 cultured organoids. Simulated crypts reached their final size in 4.6 days, and required 40 6.2 days to migrate to the top of the primary crypt. The growth of the secondary crypt 41 is independent of its migration along the original crypt. Assuming unrestricted crypt 42 fission and multiple budding events, a maximal growth rate of the intestinal 43 epithelium of 0.10 days⁻¹ is predicted and thus approximately 22 days are required for 44 a 10-fold increase of polyp size. These predictions are in agreement with the time 45 reported to develop macroscopic adenomas in mice after loss of Apc in intestinal stem 46 cells.

- 47
- 48
- 49

50 Introduction

51 The process of crypt fission, in which two functional crypts develop from one 52 single crypt, is a rare phenomenon in the healthy small intestinal or colorectal mucosa 53 of adults, but is essential for maintaining and recovering epithelial homeostasis following severe chemical-induced crypt injury¹, cytotoxic chemotherapy², or 54 irradiation³. Crypt fission is also responsible for increasing the number of crypts 55 required for postnatal development of the intestine ^{4, 5}, and for the sustained expansion 56 of the mucosal surface area following intestinal resection ⁶. Thus, this phenomenon 57 regulates mucosal morphology in the large intestine, and the balance between 58 59 population size of crypts and villi in the small intestine ⁷. It has also been reported that crypt fission is instrumental in the growth of epithelial tumours and in particular, in 60 61 the growth of adenomatous polyps bearing mutations of the adenomatous polyposis coli (APC) gene^{8,9}, colorectal adenomas and hyperplastic polyps¹⁰⁻¹² and in small 62 bowel polyposis syndromes including familial adenomatous and hamartomatous 63 64 syndromes such as juvenile polyposis^{13, 14}.

65 The mechanisms regulating the rate of crypt fission remain unclear. A crypt 66 cycle has been postulated in which a small alteration in the balance between cell loss 67 and cell proliferation results in a slow process of crypt enlargement and a gradual 68 compression of cells located in the lower part of the crypt, which is relieved by the 69 buckling of the cell layer out of the crypt base which initiates the fission event ¹⁵. 70 Stochastic models have been applied to explore the stability and asymptotic behaviour of the crypt cycle ¹⁶. In the human colon, calculations indicate a crypt cycle time of 71 between 17 and 30 years ¹², while in the mouse the length of the crypt cycle is 0.3-3.6 72 years ^{15, 17}. A simple model postulates that the threshold for triggering crypt fission is 73 the doubling of the stem cell number ¹⁸. Several biomechanical approaches, based on 74 75 the behaviour of solids, have been developed to model buckling configurations in the 76 intestinal epithelium as the result of the growth of the tissue and the elastic properties of the epithelium and/or underlying stroma ¹⁹⁻²³. 77

The main limitation to exploring crypt fission is its low frequency in the healthy mucosa combined with the difficulty of following the fission process in real time. Crypt fission is however frequently observed in cultures of intestinal organoids ²⁴⁻²⁶. Crypts growing *in vitro* are rapidly sealed, forming a cyst containing a lumen filled with apoptotic cells. The surface of the cyst undergoes continuous budding events that

83 grow into crypts, which after protruding from the cyst, undergo fission. Paneth cells present at the base of the crypts and at budding sites ²⁵ provide a crucial niche for 84 Lgr5⁺ stem cells by secreting Wingless/Int (Wnt) ligands ²⁷. Crypts deficient in Paneth 85 86 cells require exogenous Wnt molecules in order to grow ex vivo, while factors 87 compensating for the absence of Paneth cell-derived Wnt signals prevent stem cell exhaustion *in vivo*²⁸. Buske et al²³ modelled the biomechanics of the formation of 88 89 buds in the initial cyst, describing the surface of the continuously expanding cyst as an 90 epithelial cell layer provided with a flexible basal membrane whose mechanical 91 properties generate spontaneous proliferation-induced curvatures in the shape of the 92 epithelium. These spontaneous curvatures lead to buckling configurations by inducing 93 the specification into Paneth cells, which in a positive feedback fashion induce a more 94 pronounced curvature of the epithelium, leading to the formation of the bud on the surface of the cyst ²³. The authors identified a set of conditions that lead to the 95 96 formation of buds in a cyst in continuous expansion, but not for budding and fission in 97 non-expanding crypts.

98 The purpose of our study was to advance our understanding of crypt fission by 99 integrating biomechanical and cell-based computational models with measurements 100 from fission events in *in vitro* cultured intestinal organoids. Based on empirical 101 observations, we have extended the computational model previously developed for the 102 crypt ²⁹ by adopting an approach based on fluid mechanics that describes the 103 displacement of cell material out of the crypt plane to form buds that grow into crypts. 104 Our findings challenge the traditional belief that crypt fission is a process of crypt 105 base enlargement followed by buckling, proposing instead that bud initiation is 106 generated by the difference in the biomechanical behaviour of neighbouring Paneth 107 and stem cells. The model hypothesizes that the new crypt develops without affecting 108 cell dynamics within the original crypt. Under these conditions, the ability of the 109 original crypt to supply cells to neighbouring villi is not altered throughout the fission 110 process. Ultimately the model has been applied to predict maximal growth of the 111 epithelium by unrestricted crypt fission.

112 **Results**

113

114 **Biomechanical modelling of bud formation**

115 In mouse intestinal organoid cultures, bud formation takes place initially in 116 regions of the primary cyst with high Paneth cell density; initial buds grow into crypts 117 which contain Paneth and stem cells intermingling at their bases (Figure 1). The new 118 crypts undergo budding events that resemble the reported *in vivo* crypt fission 119 phenomena. Figure 2 shows that in organoids crypt fission is a budding phenomenon 120 that starts in regions of high Paneth cell density at the base of the crypts. The 121 mechanism underlying the association of bud formation and Paneth cells is unknown. 122 To circumvent this lack of knowledge, we have postulated that crypt fission is 123 initiated as a budding process by stem cells surrounded by Paneth cells or their 124 progenitors as a result of biomechanical forces.

The computational model previously developed for the crypt ²⁹ describes the 125 126 configuration of the crypt as a spiral in the crypt base and a helix forming a stack of 127 circular rings. As described in the Methods section we have extended this approach by 128 assuming that the crypt comprises viscoelastic epithelial cells adjacent to each other, 129 and able to deform if a threshold force, which varies depending on the type of cell, is 130 exceeded. Cell growth, division and migration affect the balance between the space 131 required by cell material and the available space in the crypt wall, generating forces 132 that act upon the cells. In response to these forces individual cells flow deforming the 133 shape of the crypt wall and leading eventually to budding initiation. We assume that 134 the proliferative condition of stem cells makes them deformable when subjected to 135 forces generated by changes in their size during growth and division and/or in the 136 available space in the crypt wall. For Paneth cells, deformation occurs when a critical 137 force threshold is exceeded. In order to support this hypothesis, Atomic Force 138 Microscopy (AFM) has been used to measure the Young's modulus of Lgr5-eGFP 139 positive cells and Lgr5-eGFP negative large granular crypt cells. The Young's 140 modulus is a measure of stiffness that quantifies the linear stress-strain relationship in 141 the range of stress where Hook's law holds. Figure 3A shows that the Young's 142 modulus of all but one of the Lgr5-eGFP positive cells was significantly smaller than 143 that of large granular cells by more than 3 times the standard deviation. Lgr5-eGFP 144 positive cells, which were assumed to be stem cells, required significantly smaller

forces to undergo deformation than large granular cells, which were assumed to be Paneth cells. Moreover, we have assumed that cells behave as viscous materials rather than the solid material behaviour described in previous models. Viscoelastic behaviour of cells was demonstrated in force curves. AFM measurements showed the typical separation, or hysteresis, between the approach and retract force curves resulting from viscous behaviour in all assessed cells (Figure 3B).

151 In order to parameterize our model, we have analysed the results in crypts 152 simulated with several values for the shear stress threshold required for Paneth cells 153 deformation.

154 Figure 4A compares the time intervals between successive budding events 155 observed *in vitro* with those simulated using several values for the parameter α . This 156 parameter governs the force threshold required for Paneth cell deformation. When 157 α =0, Paneth cells have identical mechanical properties to stem cells. When α =1, the 158 force required to deform Paneth cells is equal to the force generated by a 159 disequilibrium between available and required space equal to one average cell size; if 160 α is smaller or greater than 1. Paneth cell deformation requires forces smaller or 161 greater, respectively, than that generated by one extra cell. When crypts were 162 simulated with $\alpha=0$ and $\alpha=0.1$, Paneth cells were deformed with changes in cell size 163 translated in the flow of cell contents from crypt bottom to top without deformations 164 of the crypt wall. This unimpeded flow was due to the non-stress boundary at the top 165 of the crypt because of unrestrictive cell removal. As the value of α increased, Paneth 166 cells became more resistant to deformation so that the increase in size and/or decrease 167 of available space during the cell cycle was not accommodated by the non-deformable 168 neighbouring Paneth cells, leading to protrusion of cell material out of the crypt wall 169 and bud formation. In simulated crypts, the frequency of budding increased rapidly as 170 the value of α increased from 0 to 1 (Figure 4B). The best agreement between 171 simulated and observed distributions of frequencies for the time interval between 172 successive budding events was observed for values of α slightly greater than 1. For 173 instance, the smallest difference between the simulated and observed distribution was 174 detected for $\alpha = 1.3$ (Figure 4B). The median time interval between consecutive 175 budding events observed *in vitro* and simulated with α =1.3 was 2.62 and 2.84 days, 176 respectively. These medians were not significantly different (p > 0.05). Moreover, 177 under these assumptions bud formation was associated with single stem cells 178 surrounded by Paneth cells. Figure 4C shows that the probability of budding of one

stem cell surrounded by Paneth cells increases as the resistance to deformation of Paneth cells increases, reaching values of 0.95 for $\alpha > 1$, while the probability of budding for stem cells clusters with 2, 3 or 4 stem cells is very low (ca 0.04) and practically not affected by the resistance of Paneth cells to deformation (Figure 4C).

In our original computational model²⁹, the ratio of Paneth to stem cells is 3:2 183 184 and they intermingle at the base of the crypt due to Notch signalling-driven 185 differentiation. In the crypt base, stem cell descendants differentiate into Paneth cell 186 progenitors or remain as pluripotent stem cells according to Notch signalling, which is 187 activated and inhibits the secretory cell fate if more than 50% of cells in contact 188 belong to the secretory lineage. In addition, cells in the crypt bottom are dynamically 189 relocated to adjust for cell growth and division. These events determine the 190 configuration of the crypt bottom. Figure 4D shows the relative frequency of stem 191 cells clusters with 1 (0.18 relative frequency), 2 (0.32), 3 (0.28) or 4 (0.22) stem cells 192 in simulated crypts, and how these frequencies were similar for all simulations and 193 not affected by the resistance of Paneth cells to deformation or values of parameter α . 194 Figures 4 E-H show an upper view of the displacement of the cell centres on a ring of 195 the crypt during cell deformation under selected mechanical scenarios. When all cells 196 are stem cells (Figure 4E), or intermingling Paneth and stem cells are deformable with 197 the same mechanical behaviour (α =0, Figure 4F) deformations of the ring are not 198 detected. When Paneth cells are more resistant to deformation than stem cells, for 199 instance for $\alpha = 1.3$, changes in the available space due to stem cells growth are not 200 accommodated and lead to protrusion of cell material out of the crypt wall (Figures 201 4G-H). We assume irreversible cell deformation if more than half of the cell material 202 is protruding out of the plane of the crypt. Irreversible deformations are observed in 203 areas where 1 stem cell is surrounded by Paneth cells alone (Figures 4G-H). In 204 general, irreversible deformations were not detected when 2 or more stem cells are 205 adjacent to each other because the threshold force for the viscoelastic behaviour of 206 Paneth cells is reached before the irreversible protrusion of cell contents (Figure 4H). 207 If the deformation is reversible, at division time, daughter cells locate out of the plane 208 of the crypt. Those stem cell descendants located outside the crypt plane together with 209 the surrounding Paneth cells, form an initial bud protruding from the original crypt 210 that will grow into a new crypt. We have observed *in vitro* that Paneth cells from the 211 original crypt appear to be incorporated into the new crypt (Figure 1) and it has been

demonstrated *in vivo* that crypts newly generated by fission contain numerous Paneth
 cells from the original crypts ³⁰.

We have assumed a fixed value for the limiting protruding cell material of irreversible deformations. Changing the protrusion threshold for budding would modify the probability of budding of stem cell clusters with different sizes. Should new experimental evidence in support of this mechanism be forthcoming, simulations could be run to fit jointly the parameters governing the force threshold for Paneth cell deformation and the protrusion threshold for bud initiation.

220

221 Cell dynamics within crypts during fission

222 Cell proliferation and differentiation takes place in the secondary crypt according to the hypotheses of the previously developed model ²⁹. We assumed that 223 224 mitotic pressure in the primary crypt forces the upward migration of the secondary 225 crypt, which simultaneously grows and protrudes out of the primary crypt. The 226 supplementary Video S1 shows a simulation of a crypt fission event and Figure 5A 227 shows good agreement between the specific growth rates of the new crypt observed 228 experimentally (0.99 days^{-1}) and in the simulations (1.03 days^{-1}) (Figure 5A). The 229 median values were not significantly different (p > 0.05). The good agreement 230 between the growth rates of the secondary crypt in simulated and in observed fission 231 events indicates that the elongation of the secondary crypt is likely based on cell 232 proliferation, which takes place at the same rate as in the primary crypt.

233 In simulated fission events the upward migration of the secondary crypt along 234 the original crypt has two periods. The first has a very slow migration rate, with the 235 new crypt located at the base of the original crypt, with a second period of rapid 236 upward migration along the primary crypt (Figure 5B). The duration of the first period 237 of very slow migration is highly variable and lasts until the new crypt reaches 238 positions above row 5 in the original crypt, which requires 4 ± 3.3 days. Thus, during 239 the first period some new crypts may fully develop at the base of the original crypt 240 without migrating upwards. This event, predicted by the model, is observed in 241 cultured organoids such as that captured in Figure 6 showing a fully developed crypt 242 at the base of the primary crypt and how this new crypt replaces the original crypt.

Once the secondary crypt reaches positions above the base of the original crypt, it rapidly migrates upwards to the top of the original crypt, which takes on average 1.7 ± 0.72 days. Our model therefore predicts that the bud is confined to the lower portion

of the crypt for approximately 70% of the duration of the fission process. In agreement with this prediction, between 70 to 90% of the observed fission events have been reported to be detected in the lower 1/4 of the crypts in infant rats ⁷. In a study of acid injury, most fission events were observed in the lower 2/3 of the crypt ¹.

250 The predicted increase in migration velocity after reaching positions above the 251 crypt base is in agreement with the observed dependency of the migration velocity along the crypt on mitotic pressure, which is greater at higher positions in the crypt ³¹. 252 253 Forces derived from cell growth and division in the primary crypt are sufficient to 254 explain the upward migration of the secondary crypt along the primary crypt, as seen 255 in the close agreement between simulated and observed migration rates (Figure 5A). 256 The Supplementary Video S2 shows a simulation of a crypt undergoing fission and an 257 in vitro fission event in an organoid during 1.3 days of the period of rapid migration 258 of the secondary crypt.

259 In our model, growth and migration of the secondary crypt are independent of 260 each other while cell proliferation and migration within the original crypt are not 261 affected during fission. This has important implications for the functionality of the 262 original crypt, which supplies cells to the *villi* at full capacity throughout the fission 263 process. Figure 7 shows the analysis of the simulation results regarding growth and 264 migration of the secondary crypt. The median time required for the new crypt to reach 265 its final size was 4.6 days (Figure 7A) while the median time to reach the top of the 266 primary crypt was 6.2 days (Figure 7B). These timings agree with the results of a 267 morphological study of the epithelium regeneration after acid injury ¹ in which crypt 268 fission was observed 7 days after the injury and the normal appearance of the mucosa 269 was recovered by 14 days post-injury.

270 Approximately 30% of the simulated crypts reached their final size before 271 reaching positions above row 5 on the primary crypt (Figure 7C). From these crypts, 272 the 5% located at row 0 of the original crypt have a small probability of migrating 273 upwards and could eventually replace the original crypt as observed in vitro (Figure 274 6). Some of the remaining 25% of crypts located at the bottom of the primary crypt 275 could ascend along the original crypt, generating lateral branches and resembling the 276 reported asymmetrical fission events commencing on the lateral crypt walls instead of at the crypt base^{8, 10}. Only 3% of the new crypts reach the top of the primary crypt 277 278 with a small size, equivalent to 10% of the final size of the crypt (Figure 7D). About

279 75% of the new crypts reach their final size before reaching the top of the primary280 crypt or the lumen (Figure 7D).

281

282 Cell composition in crypts during fission

283 During expansion of the new crypt, stem cell descendants generated at the crypt 284 base under high Wnt signalling give rise to stem cells and Paneth-secretory cells, 285 while the progeny of stem cells above the crypt base under low Wnt signalling will 286 specify into proliferative absorptive progenitors and secretory-goblet, enteroendocrine 287 and Tuft cells. Deciding between the two fates of secretory and stem/absorptive cells 288 depends on Notch signalling. Our model hypothesis for the crypt is that Notch 289 signalling inhibits secretory fate if more than 50% of the cells they are in contact with belong to the secretory lineage ²⁹. We have assumed that mature enterocytes are not 290 291 generated in the new crypt during its expansion.

292 Figure 8 shows that the simulated average proportions for each cell type in the 293 crypt remain fairly constant during fission. Around the third day after fission 294 commences, the model predicts a slight increase in the proportion of Paneth and stem 295 cells (Figure 8A). Acute activation of β -catenin has been reported to result in frequent 296 budding events at the bottom of colonic crypts *in vivo* accompanied by an increase of 297 the stem cell compartment³². Our model predicts that this increase is coincidental with 298 the formation of the bud or stem cell niche for the new crypt but it is rapidly averaged 299 out by the growth of the bud into a new crypt containing all cell types. Thus, the 300 predicted size of the proliferative compartment during fission is on average unaffected 301 (Figure 8B). The deletion of the adenomatous polyposis coli (*Apc*) gene in intestinal 302 stem cells of mice leads to an aggressive expansion of adenomatous polyps by crypt 303 fission. However the proportion of Lgr5⁺ stem cells in tumors remained unchanged 304 with respect to healthy crypts ⁹. Similarly, the number of mitotic cells and the size of 305 the cell proliferation compartment in human familial adenomatous polyposis (FAP) 306 crypts or in mouse multiple intestinal neoplasia (MIN) crypts did not differ from that of healthy crypts⁸. 307

308

309 Predicting growth of the intestinal epithelium by unrestricted crypt fission

The growth of the intestinal epithelium by crypt fission was predicted based upon the assumption that budding and fission always take place in crypts when a stem cell is surrounded by Paneth cells. Therefore, crypts undergo more than one budding

313 process simultaneously with budding taking place in the new crypts generated by 314 fission. These assumptions are based on *in vivo* observation of multiple buds arising 315 from the same crypt as reported after injury ³.

316 Figure 9 shows that the predicted value for the specific growth rate of the intestinal epithelium by crypt fission is approximately 0.10 days⁻¹. Thus, about 15.3 317 and 21.9 days are required to observe a 5 and 10-fold increase in size, respectively. 318 319 The predicted growth of the epithelium by unrestricted crypt fission agrees with *in* 320 vivo observations in mice after inducing the loss of the Apc gene in intestinal stem 321 cells⁹. After Apc loss, crypt branches were continuously formed resulting in 322 macroscopic epithelial formations 2-3 weeks post-induction⁹. However, the constant 323 specific growth rate observed in vitro and estimated for adenoma formation in Apc-324 mice seems to differ from the growth kinetics reported for human colonic adenomas. 325 These included relatively mitotically old populations of monoclonal crypts with 326 occasional newly generated subclones, indicating that colorectal tumourigenesis may 327 be characterized by relative stasis with occasional rapid growth of sub-clones ³³.

The predicted percentage of crypts undergoing fission in the epithelium was $\sim 37.6\%$ (Figure 9) comparable with prior*in vivo* studies reporting values of 35% and $\sim 22\%$ in mice ^{34, 35}, and 18% in humans at fission peaks seen during intestinal development in infants ³⁶. The percentage of crypt fission events observed in the proximal small bowel of MIN mice varied from 5% to 22% ⁸.

333

334 **Discussion**

335 Our individual cell-based approach to modelling the initiation of budding in the 336 intestinal crypt is based on fluid mechanics with cells having heterogeneous 337 viscoelastic properties depending on their lineage. Our model challenges the 338 traditional belief that crypt fission is a process of crypt base enlargement followed by 339 buckling. We propose the formation of a bud that progressively grows into a crypt, 340 migrating upwards along the primary crypt without affecting cell proliferation and 341 migration within the primary crypt, and without compromising the primary crypt 342 capability of providing cells to the epithelium.

343 Deformations are caused by the forced displacement of cell contents out of the 344 crypt plane forming a bud containing the stem cell niche that will grow into a new 345 crypt protruding from the primary crypt. Simulations under the hypothesis that Paneth

346 cells are more resistant to deformation than stem cells resulted in budding in regions 347 of stem cells surrounded by Paneth cells, as observed in crypt organoid cultures. In 348 our model, the location of buds depends on the local cell composition determined by 349 Wnt- and Notch-driven cell differentiation, proliferation and migration within the 350 crypt. Crypts with few Paneth cells are unlikely to undergo fission events, while an 351 increase in the ratio of Paneth cells to stem cells increases the predicted frequency of 352 budding. The model hypothesis could be generalized for the whole crypt by assuming 353 that proliferative absorptive progenitors behave mechanically as stem cells while 354 secretory cells have the same deformation threshold as Paneth cells. Budding takes 355 place only when proliferative cells are surrounded exclusively by secretory cells. In 356 normal conditions, this configuration would only be observed in the stem cell niche at 357 the base of the crypt.

The mechanisms responsible for the initiation of buds in the intestinal crypt, both *in vivo* and *in vitro*, are as yet unknown. Although the hypothesis underlying bud initiation in our fluid mechanics approach lacks experimental evidence, the good agreement between the observed budding frequency *in vitro* and the frequency predicted by our biomechanical approach for the normal ratio between Paneth and stem cells in the crypt validates its use to predict epithelial growth by crypt fission.

364 Biomechanical approaches are commonly applied to modelling the buckling of a 365 growing epithelium. The analysis of the patterns created by buckling of a dividing 366 epithelial monolayer of cells lying on top of an elastic stroma results in a variety of possible conformations of crypts and villi along the small intestinal epithelium ^{21, 37}}. 367 368 Modelling a growing epithelium attached to a basement membrane has also been 369 demonstrated to be useful to study interactions between epithelium and stroma in the 370 crypt ³⁸. This kind of biomechanical approach has been applied specifically to model crypt fission ^{19, 20, 22, 39}. These models consider the epithelium as a solid beam formed 371 372 by adjacent cells subjected to stretching and compression forces generated by an 373 increase in the number of cells, leading to buckled conformations. The cell-based approach of Drasdo¹⁹ and Drasdo and Loeffler³⁹ describes the bending of the 374 375 epithelium in a two dimensional system and identifies cell proliferation as the main 376 reason for the onset of buckling. In the continuous approach modeling of Edwards and Chapman 20 , the epithelium is modeled as a growing beam attached to an underlying 377 378 lamina in 2 dimensions. In this model, the buckling of the tissue is in response to any 379 combination of an increase in cell proliferation, an enlargement of the proliferative

380 compartment and/or an increase in the strength of cellular attachment to the 381 underlying lamina. A further analysis of this approach shows that non-uniform growth 382 patterns along the epithelium have a much weaker influence on the buckled shapes 383 than non-uniformities in the mechanical properties of the material ²². The same 384 authors have recently claimed that in a three-dimensional system, growth patterning 385 has a greater impact on the distribution of crypts than does material inhomogeneity³⁷. 386 A distinctive feature of our approach to modelling crypt fission is that we treat cells as 387 viscous materials rather than assuming the solid material behaviour described in the 388 models discussed above. In agreement with *in vitro* experimental observations, we 389 have modelled fission as a budding process based on fluid mechanics at the individual 390 cell level and not, as the folding or buckling of solid material. AFM measurements 391 confirmed the viscous nature of both LGR5-eGFP positive and LGR5-eGFP negative 392 large and granular single cells isolated from crypts (Figure 3B). Moreover, we 393 modelled fission as a consequence of inequalities in the mechanical properties of 394 viscoelastic cells which depend on cell lineage. This hypothesis was also supported 395 experimentally by AFM measurements of single cells, which revealed that stem cells 396 are less stiff than other granular large crypt cells.

397 Another distinctive feature of our model is that, changes in the size of the 398 proliferative compartment or in the division rate are not associated with budding. 399 Although fission ultimately depends on cell division, there is uncertainty regarding 400 the relationship between changes in cell proliferation and crypt fission. The increase 401 in cell proliferation within the crypt, or in crypt volume, has been reported in several studies not to be associated with crypt fission^{10, 40-42}. Indeed, the administration of 402 403 epithelial growth factor to MIN mice resulted in an increased cell proliferation within 404 crypts with a significant reduction in the rate of fission ⁴¹. Similarly, studies on 405 intestinal development in infant rats and humans concluded that crypt fission is not always preceded by crypt hyperplasia^{36, 42}. Also, the administration of P-cadherin 406 results in enhancement of crypt fission in vivo while cell proliferation in crypts is 407 unaffected ⁴³. Similarly, in MIN mice the proportion of crypts in fission increases 408 409 dramatically but cell proliferation is not affected in dividing crypts compared to stable crypts⁸. In another study, a reduction in intestinal crypt fission was detected after the 410 411 administration of the negative regulator of Wnt signalling, dickkopf, although cell proliferation remained unchanged ⁴⁴. 412

413 Apc loss induces acute activation of Wnt/ β -catenin signalling pathway. The 414 activation of the Wnt pathway induces de novo specification of Paneth cells in the 415 mouse small intestine. Both murine colon polyps and human colonic tumours 416 resulting from Apc mutations express genes involved in Paneth cell differentiation ⁴⁵. 417 Although Paneth cells are absent from both mouse and human colon, a subset of 418 colonic secretory cells that share cKit⁺ expression with small intestinal Paneth cells, 419 and are essential for the maintenance of the stem cell niche and for organoid 420 formation *in vitro*, have been identified in the base of colonic crypts intermingled with 421 $Lgr5^+$ cells ⁴⁶.

422 In the small intestine, the relationship between Paneth cells and the two pools of 423 intestinal stem cells, slow cycling cells located at position +4 and actively cycling 424 stem cells at the bottom of crypt, is not well understood. It has been demonstrated that Paneth progenitor cells revert to stem cells upon crypt damage ^{47, 48}, and specifically 425 426 quiescent +4 stem cells have been identified with secretory progenitors expressing 427 Lgr5 and able to regain 'stemness' after intestinal injury ^{49, 50}. In mouse colonic crypts 428 Wnt activation has been demonstrated to induce crypt fission, accompanied by a 429 reduction in the cell proliferation rate and of activation of the Notch signalling pathway among progenitors ³². Therefore under Wnt activation, crypt fission could be 430 431 associated with enhancement of the slowly cycling secretory progenitors, which is in 432 agreement with the increase of budding linked to the increase in the ratio of secretory 433 cells to stem cells predicted by our model.

434 We have observed buds in regions with Paneth cells although we have not 435 experimentally determined the density of Paneth cells in budding regions. It has been 436 reported that numerous Paneth cells from the primary crypt are detected in newly generated crypts by fission *in vivo*³⁰. In this published study, crypt fission is assumed, 437 438 though not experimentally proven, to be a progressive longitudinal partition initiated 439 at the crypt base. However, if fission is a budding process as we propose here, the 440 abundance of original Paneth cells in the base of the new crypt indicates that Paneth 441 cells or their progenitors are present in high numbers in the region where the bud is 442 initiated and they form part of the initial bud. On the other hand, an essential role of Lgr5⁺ stem cells in crypt fission in the intestine ³⁰ and also in gland fission in the 443 stomach ⁵¹ has been demonstrated using *in vivo* clonal fate mapping strategies to 444 445 observe the lateral expansion of Lgr5-expressing stem cell derived clones, containing 446 clonal $Lgr5^+$ stem cells.

447 It should be noted however that ablation of Paneth cells does not affect 448 deregulation of crypt fission and intestinal tumourgenesis in Apc mice with intestinal stem cells deficiency ²⁸. Non-canonical Wnt signalling has also been associated with 449 450 crypt regeneration in the wounded epithelium of mice ⁵². Wnt5a molecules, which are 451 non-canonical Wnt ligands that inhibit intestinal cell proliferation in vitro, have been 452 detected in stromal mucosal cells localized to clefts in-between nascent crypts in vivo, 453 seemingly contributing to defining the shape of the new crypts in injured areas of the epithelium where crypts have been excised ⁵². A common denominator seen in 454 455 circumstances preceding non-tumour growth-associated crypt fission in vivo is a 456 diminished density of functional healthy crypts in the mucosa. For example, as seen during intestinal growth in infants ^{35, 36}, compensatory intestinal dilation following 457 intestinal resection 6 , and during recovery of wounded areas of the mucosa $^{1, 52}$. The 458 459 role of Wnt signalling and Paneth cells in the regulation of crypt fission in vivo is 460 therefore complex and other components, potentially of mesenchymal origin, are 461 likely to be involved.

462 In our simulated crypts, unrestricted crypt fission is associated with a 463 biomechanical instability generated by difference in the biomechanical properties of 464 Paneth and stem cells. We can hypothesize that the progression of the instability to 465 form an initial bud is inhibited *in vivo*, while the inhibitory mechanism is absent in the 466 *in vitro* culturing system. This hypothesis was developed to circumvent the lack of 467 information regarding the signalling and regulation of the fission process. Although 468 under this hypothesis the predicted and observed budding frequencies are in good 469 agreement (Figure 4A), further experimental validation is required. In addition, the 470 cellular Wnt and Notch signalling pathways function normally in both the simulated 471 crypts and in the *in vitro* cultured crypts. However, Apc⁻ mice have a severely altered 472 Wnt signalling pathway. Therefore, although the rates of fission appear to be similar, 473 the mechanisms behind unrestricted crypt fission *in vivo* and *in vitro* are likely to be 474 very different. One of the essential factors required to maintain intestinal stem cells and organoids in culture is R-spondin ⁵³. This protein strongly potentiates the Wnt 475 476 signalling pathway and, just as in the case of the deletion of the Wnt signalling inhibitor APC in vivo^{8, 12, 54}, this may account for the unimpeded epithelial growth by 477 478 crypt fission observed in vitro. Thus, crypts cultured in vitro under acute stimulation 479 of the Wnt signalling pathway, and *in vivo* crypts with a disinhibited Wnt target gene

480 programme, may achieve maximum crypt fission rates, which would explain the481 similarity of the epithelium growth kinetics in these two different systems.

482 In summary, the model we have presented shows how crypt budding can be 483 biomechanically initiated by stem cells surrounded by Paneth cells which accurately 484 predicts epithelial growth by unrestricted crypt fission as observed in cultured 485 organoids. The epithelial growth rate predicted by unrestricted crypt fission agrees 486 with the growth observed in vivo in intestinal adenomas associated with APC loss. We 487 have therefore integrated individual based models with *in vitro* culturing organoids to 488 develop an approach able to simulate the process of crypt fission and further 489 extrapolated predictions for the growth of adenomatous polyps in the mouse intestinal 490 epithelium. The generated modelling framework can be applied to test hypotheses on 491 regulation mechanisms in homeostatic crypts and to explore the impact of 492 perturbations on the progression of adenoma-carcinoma processes in the intestine.

493 Methods

Animal care and experimentation were performed in accordance with the Guidelines
established by the Committee on Animal Care and Use of Keio University and under
the authority of the UK Home Office (PPL 80/2355).

497 Preparation of *in vitro* crypt cultures

498 Small intestinal crypt preparations from 6 week old mice (strain C57/B6 or 499 Lgr5-EGFP-ires-CreERT2) were embedded in Matrigel (BDBioscience). After 500 polymerization of Matrigel, crypt culture medium (advanced DMEM/F12 501 supplemented with Penicillin/Streptomycin, 10 mM HEPES, Glutamax, 1x N2, 1x 502 B27 [Invitrogen], and 1 μ M N-acetylcysteine [Sigma] and containing 50 ng/ml EGF 503 [Peprotech], 100 ng/ml noggin [Peprotech], 1 μ g/ml R-spondin 1) was overlaid. 504 Cultures were maintained as previously described ⁵³.

The growth of organoids was imaged using a climate-controlled (37°C, 5% CO2) stage of an inverted motorised time-lapse microscopic system (Nikon) for periods of up to 10 days. Frames of ten movies including 1-3 organoids each were analysed to estimate budding frequency per crypt, the growth of the secondary crypt and its migration along the original crypt.

510

511 Fluorescent immunostaining and confocal microscopy

512 Organoids were isolated from Matrigel using Cell Recovery solution (BD 513 Biosciences) and fixed with 4% paraformaldehyde (PFA). After fixation, samples 514 were incubated with 0.2% Triton X-100 in PBS for permeabilization, and with 515 Universal Blocking Reagent (Biogenex) for blocking non-specific binding of 516 antibodies. To visualize Lgr5+ stem cells and lysozyme+ Paneth cells, samples were 517 incubated overnight at 4°C with antibodies specific for GFP (abcam; ab6673, 1:100) 518 and Lysozyme (Dako; A0099, 1:1000) in PBS. GFP and Lysozyme were labelled by 519 anti-Goat alexa488 conjugated antibody and anti-Rabbit alexa568 conjugated 520 antibody (Invitrogen) in PBS. Nucleus was counterstained with Hoechst33342. 521 Images were acquired by confocal microscopy (Leica SP8).

522

523 Crypt and epithelial cell isolation

524 Crypts were isolated from whole small intestine of C57BL/6-J or Lgr5-525 eGFP^{tm1(cre/ERT2)Cle/J} adult mice at 12-16 weeks of age. Whole intestines were flushed,

526 and dissected in PBS containing antibiotics and antimycotics. Samples were 527 incubated on ice in 2 x 5 mins 1mM DTT and 3 x 5 mins 2mM EDTA, with gentle 528 shaking to remove debris and sloughed epithelial cells. Remaining epithelial cells and 529 crypts were dislodged by 30 min incubation in 2mM EDTA at room temperature, then 530 vigorously shaken in successive fractions of ice-cold PBS. Crypts were spun down, 531 concentrated and incubated 35 min at 37°C with collagenase/dispase (Roche) and 532 DNase I (NEB) to generate a single-cell suspension. GFP-positive (Lgr5-eGFP stem 533 cells) and GFP-negative cells (non-stem epithelial cells) were separated using a Sony 534 SH-800 cell sorter. Cells were re-suspended in advanced DMEM containing B27, N2, 535 n-acetylcysteine (1 mM), HEPES (10 mM) penicillin/streptomycin (100 U/ml), L-536 Glutamine (2 mM), epidermal growth factor (50 ng/ml), Wnt-3A (100 ng/ml), Noggin 537 (100 ng/ml) SB202190 (20 μ M), seeded onto poly-lysine coated slides and allowed to 538 adhere overnight at 37°C / 5% CO2. Media was replaced with D-PBS with Ca^{2+}/Mg^{2+} , immediately prior to measurement by atomic force microscopy. 539 540

541 Atomic Force Microscopy AFM

The AFM used for this study was an MFP-3D-BIO (Asylum Research, Santa Barbara,
CA. USA). The deformability measurements were performed with a cantilever fitted
with 2.5 μm diameter silica bead in place of the AFM tip (CP-PNPL-SIO-A, sQUBE
Surface Science Support, Germany). This is necessary for two reasons; firstly to
prevent penetration of the cell membrane by the AFM tip during the measurements,
and secondly to allow proper quantification of the indenter shape for subsequent
modelling ⁵⁵.

549 Prior to the cell deformation measurements, the optical lever sensitivity of the 550 cantilevers was calibrated by pressing against a rigid surface (clean glass slide) The 551 spring constants of the cantilevers were determined using the thermal noise spectra method ⁵⁶. The AFM sits on top of an inverted optical microscope (IX-71, Olympus, 552 553 Japan) enabling the AFM tip to be accurately positioned on chosen cells. The optical 554 microscope was operated in epi-fluorescence mode to enable discrimination of the 555 Lgr5-eGFP+ stem cells. Deformability of the cells was measured by performing multiple force versus distance curves at a velocity of 2 μ m.s⁻¹ on the chosen cells. 556 557 Two controlled maximum load forces (600 pN and 1.2 nN) were applied to ensure 558 sufficient, but not excessive, deformation was achieved. The data was fitted to a

559 Hertzian elastic model featured in the instrument software which analyses it in terms

of force versus indentation (MFP-3D 111111+1610).

561

562 Biomechanical model for the initiation of buds

563 Cells are modelled as spherical shapes of incompressible homogenous viscous 564 material which are packed to form the walls of the crypt. Cells maintain their shape in 565 the absence of stress, but under an applied sufficient stress, cell material flows and 566 changes cell shape, accumulating stress in return. When the accumulated stress and 567 the applied stress have the same magnitude, the cell material is no longer displaced. 568 When the applied stress is removed, cells could partially return to their original form 569 (viscoelastic behaviour) or maintain some degree of deformation (viscoplastic 570 behaviour); constant cell proliferation generates a certain compression force in the 571 system that prevents the absolute relaxation of the system.

572 We describe the crypt as a cylindrical structure organized in 3 dimensions with 573 rings of cells in the XY horizontal plane and a vertical axis, Z, from the base to the 574 top of the crypt (Figure 10). Proliferative cells, which include stem cells, are assumed 575 to behave as Newtonian fluids under forces derived from cell growth; however mature 576 cells including Paneth cells, behave as Bingham plastics. With these assumptions, the 577 viscoelastic behaviour of stem cells is defined by one parameter, the dynamic 578 viscosity coefficient, μ , derived from the linear relationship between the shear force, 579 τ , and the shear rate, $\partial v/\partial x$. For laminar flows this can be expressed as: $\tau = \mu (\partial v/\partial x)$ 580 where v is the velocity and x the orthogonal dimension to the direction of the flow. 581 The behaviour of Paneth cells is described by two parameters, the apparent viscosity 582 coefficient, η , and the shear stress threshold or yield point, τ_T , i.e. $\tau = \tau_T + \eta (\partial v / \partial x)$. 583 Paneth cells exhibit linear shear stress, shear rate behaviour only after the shear stress 584 threshold, τ_T has been reached. Hence, to deform Paneth cells, the driving shear stress 585 has to be larger than τ_{T_i} and because of this threshold, Paneth cell deformation differs 586 from stem cell deformation. The shear rate or velocity gradient, $\partial v/\partial x$, of Newtonian 587 fluids decreases gradually towards the cell centre and reaches a value of 0 at the axis 588 of symmetry or x = 0 giving place to a gradual deformation of the shape of the edge 589 (Figure 10). Bingham plastics behave as solids when the force is below the shear 590 stress threshold which results in the formation of a solid plug at the front of the

591 deformed edge of the cell moving with the flow (Figure 10), i.e $\partial v/\partial x = 0$ at $x = x_T$, 592 which is the radio of the solid plug.

Assuming zero-stress boundary conditions at the top of the crypt because of the unrestrictive removal of cells, when all cells have the same mechanical properties, cell growth is translated in the flow of cells in the parallel direction to the Z axis within the crypt wall. Flow within the crypt wall in other directions is also possible, but not frequent, due to the fully packed condition of the crypt walls. The other direction that the flow may take is the orthogonal direction to the Z axis, out of the crypt wall (Figure 10).

When Paneth cells behave as Bingham plastics, the flow may be disturbed by the presence of these cells with higher resistance to deformation which are obstacles to the flow of the viscous cells, and eventually they may force the change of the direction of the flow towards the X and Y directions, i.e. deforming the external side of the crypt wall (Figure 10).

605 The deformation of the external side of the cells occurs when one or more 606 adjacent viscous, i.e. deformable, cells, whose geometric centres form a convex set, 607 are delimited by cells that will exhibit viscous behaviour only after a given threshold 608 force is reached. Flow analysis in three dimensions can be carried out under the 609 assumption of laminar flow. To analyse the deformation of the external side of the 610 cell, it is sufficient to analyse the flow in two dimensions in either the XZ plane or of 611 the XY plane as described in Figure 10. The analysis of the deformation in these two 612 planes is equivalent under the hypothesis of axial symmetric flow (Figure 10). As an 613 example, we describe below the deformation of rings formed by two- dimensional 614 cells in the XY plane (Figure 10). The analysis is exactly the same for a two-615 dimensional longitudinal section of the crypt.

616 The Navier-Stokes general equations for an incompressible two-dimensional 617 flow are:

618
$$\frac{\partial v_y}{\partial t} + v_x \frac{\partial v_y}{\partial x} + v_y \frac{\partial v_y}{\partial y} = -\frac{1}{\rho} \frac{\partial P}{\partial y} + \nu \left(\frac{\partial^2 v_y}{\partial x^2} + \frac{\partial^2 v_y}{\partial y^2} \right)$$
(1)

619
$$\frac{\partial v_x}{\partial t} + v_x \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} = -\frac{1}{\rho} \frac{\partial P}{\partial x} + v \left(\frac{\partial^2 v_x}{\partial x^2} + \frac{\partial^2 v_x}{\partial y^2} \right)$$
(2)

620 And the continuity condition for incompressible flow,

20

621
$$\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} = 0$$
(3)

622 In equations (1) through (3), v_x and v_y are the velocity components of the flow in the x 623 and y direction, respectively, t is time, ρ is density, v is the kinematic viscosity and P 624 is the pressure per unit length, which is uniformly applied to the edges of a two 625 dimensional cell in the direction of the motion of the liquid due to compression 626 (Figure 10). Cell compression is derived from the difference between cell size and 627 available space. We have described the deformation of free external cell sides only. 628 The deformation of free internal cell sides facing the crypt lumen could be similarly 629 analysed. With a perfect laminar flow, the pressure in both internal and external cell 630 sides and therefore cell content displacement in each direction will be proportional to 631 the area of each cell side. Due to the organization of cells in rings the area of the 632 internal cell side is smaller than the area of the external side. For instance, in our 633 crypt, cell protrusion towards the lumen will be in average only 20% of the external 634 cell protrusion. In addition, it is likely that cell structural properties perturb the flow 635 and decrease cell displacement towards the lumen. For these reasons, we have 636 disregarded the analysis of cell protrusion towards the lumen of the crypt.

As described in Figure 10, the laminar flow in two dimensions driven by a constant pressure gradient, $-\partial P / \partial y = K$, takes place essentially in the *y* direction and hence, $v_x = 0$ which when replaced into equation (3), produces $\partial v_y / \partial y = 0$. These two conditions, $v_x = 0$ and $\partial v_y / \partial y = 0$, simplify equations (1) and (2) to the following:

641
$$\frac{\partial v_y}{\partial t} = -\frac{1}{\rho} \frac{\partial P}{\partial y} + v \frac{\partial^2 v_y}{\partial x^2}$$
(4)

$$642 0 = -\frac{1}{\rho} \frac{\partial P}{\partial x} (5)$$

643 Equation (5) indicates that *P* is not a function of *x*, then $\partial P / \partial y = dP / dy = -K$ 644 which combined with in equation 4 results in the governing equation:

645
$$\frac{\partial v_y}{\partial t} = \frac{K}{\rho} + v \frac{\partial^2 v_y}{\partial x^2}$$
(6)

646 Assuming that the flow is in steady state, i.e. $\partial v_v / \partial t = 0$, equation (6) becomes:

$$647 \qquad \qquad \frac{d^2 v_y}{dx^2} = -\frac{K}{\mu} \tag{7}$$

For stem cells behaving as a Newtonian fluid, $\mu = \rho v$ is the dynamic viscosity of the fluid. The *x* variable describes the distance of the cell content being displace from the cell centre in the XY plane and hence takes values in the interval (-*R*, *R*) (Figure 10). With the condition, $dv_y/dx = 0$ at x = 0 derived from the axial symmetry assumption, and the no-slip condition at the boundaries, i.e. v = 0 at x = R, equation 7 has solution:

654
$$v_y(x) = \frac{dy}{dt} = -\frac{K}{2\mu}(x^2 - R^2)$$
 (8)

Equation 8 is the Poiseuille law for a two-dimensional fluid and it describes the velocity of cell material located at a distance x from the cell centre in the XY plane The area of the surface, S, displaced in dt, or flow rate, can be estimated by integrating equation 8 on x from -0 to R and multiplying the result by 2:

$$\frac{dS}{dt} = \frac{2}{3}aR^3 \tag{9}$$

660 Where $a = \frac{K}{\mu}$

661 For Paneth cells behaving as Bingham plastics, $\eta = \rho v$ is the apparent viscosity 662 of the fluid and equation 6 is as follows

663
$$\frac{d^2 v_y}{dx^2} = -\frac{K}{\eta}$$
(10)

664 With the condition, $dv_y/dx = 0$ at $x = X_T$, which is the radio of the symmetric 665 solid plug at the center of the flow (Figure 10) and the no-slip condition at the 666 boundaries, i.e. v = 0 at x = R and at x = -R, equation 7 has solution:

667
$$v_{y}(x) = \frac{dy}{dt} = -\frac{K}{\eta} \frac{(x^{2} - R^{2})}{2} + \frac{K}{\eta} X_{T}(x - R)$$
(11)

668 The corresponding flow rate is:

669
$$\frac{dS}{dt} = 2\left(\int_{X_T}^R -\frac{K}{2\eta}(x^2 - R^2) + \frac{K}{\eta}X_T(x - R)dx + X_Tv_y(X_T)\right) =$$

670
$$= b \left(\frac{2}{3} R^3 + \frac{1}{3} X_T^3 - R^2 X_T \right)$$
(12)

671 Where $b = \frac{K}{\eta}$

672 As the cell material is incompressible, the value dS/dt, can be estimated from 673 the change in cell size and available space as follows:

674
$$\frac{d\hat{S}}{dt} = \sum_{k \in I} \frac{dA(cell_k)}{dt} - \frac{dA(space available for I set)}{dt}$$
(13)

675 where *I* is the set of adjacent cells forming a convex set with identical viscous 676 behaviour and *A* the area of surface.

677 Equation 9 and 12 are identical when the shear stress threshold in Paneth cells is 678 equal to zero and Paneth and stem cells have the same coefficient of viscosity, $\mu = \eta$. 679 Under these conditions, the values of the parameters *a* and *b*, can be estimated from 680 equation 9 or 12 and 13, respectively. The assumption of equal coefficient of viscosity 681 for stem and Paneth cells also simplifies the description of the shear stress threshold 682 in Paneth cells as described below.

In order to quantify the formation of buds with different values for the shear stress threshold in Paneth cells, τ_T , and to provide a rough biological interpretation, the relationship between the shear stress and the pressure gradient due to cell growth can be described as

$$\epsilon_{0} = -x \frac{dP}{dy} \tag{14}$$

688 And the shear stress threshold in Paneth cells can be expressed as:

690 By substituting in equation 11:

691
$$v_{y}(x) = \frac{dy}{dt} = -\frac{K}{2\eta}(x^{2} - R^{2}) + \frac{\tau_{T}}{\eta}(x - R)$$
(16)

692 From equation 9 for the flow rate in stem cells, an average pressure gradient can 693 be estimated as a function of the average growth rate of the surface area of stem cells, 694 r_{av} , and an average stem cell ratio at birth, R_{av} , as follows:

695
$$K_{av} = \frac{3}{2} \frac{\mu}{R_{av}^3} r_{av}$$
(17)

696 From equation 14 and 17, the average force exerted by the compression due to697 one extra cell can be described as follows;

698
$$\tau_{av} = R_{av} K_{av} = \frac{3}{2} \frac{\eta}{R_{av}^2} r_{av}$$
(18)

From equation 18 and under the assumption that $\eta = \mu$, values for the ratio τ_T / η in equation (16) can be chosen to be proportional to the average shear rate in stem cells

702
$$\frac{\hat{\tau}_T}{\eta} = \alpha \frac{\tau_{av}}{\mu} = \frac{3}{2} \frac{r_{av}}{R_{av}^2}$$

703 And therefore,

704

 $\hat{\tau}_{\tau} = \alpha \tau_{av} \tag{19}$

705 Where α is a factor of proportionally between the shear force threshold required 706 to deform Paneth cells and the compressive forces generated by a disequilibrium 707 between the required and the available space equal to one cell size; α takes values 708 equal to or greater than zero. If $\alpha=0$, Paneth cells behave as a Newtonian fluid and its 709 deformability is identical to that of stem cells. If $\alpha = 1$, the shear force threshold 710 required to deform Paneth cells is equal to the compressive forces generated by one 711 extra cell; if α is smaller or greater than 1, Paneth cells deformation requires forces 712 smaller or greater, respectively, than those generated by one extra cell. The initiation 713 of budding and fission takes place because of the instability of the cell shape. We 714 assume irreversible cell deformation, if more than half of the cell material is 715 protruding out of the plane of the crypt. Less extreme deformations of the cell are 716 considered reversible. Thus, when the protrusion of cell material is significant, at 717 division time, daughter cells will locate out of the plane of the crypt, initiating a bud 718 that grows into a new crypt.

In order to study how budding depends on the shear force threshold of Paneth cells, the probability of budding within a period of 12 and the time intervals between successive budding events in a single crypt were quantified in simulations run with α values equal to 0.1, 0.3, 0.5, 0.7, 0.8, 0.9, 1, 1.1, 1.2, 1.3, 1.5, 2.

723

Integration of the bud initiation process in the individual based model for the crypt of Pin et al ²⁹ and analysis of forces.

The model of Pin et al ²⁹ has been adapted to describe crypt fission in a three 726 727 dimensional crypt. Model parameters are summarized in Supplementary Table S1. In 728 the original model, the structure of the bottom of the crypt is modelled as a three-729 dimensional spiral followed by the crypt body, which is a three-dimensional helix, 730 constructed from single cells organized in a one-dimensional chain. The position of 731 any cell in the spiral or helix is determined by the coordinates of the cells organized in 732 rings in the XY plane and the vertical coordinate Z, which describes the height 733 reached by cells in columns perpendicular to the XY plane. At each interval time of

the simulation, the three dimensional spiral and helix are re-built according to the change in cell, and division or deletion events. Growing cells expand homogenously in all directions. The increase in cell size in the vertical direction creates a force translated mostly in upward migration. Cell size changes in the horizontal plane are accommodated by changing the perimeter of the ring in the XY plane perpendicular to the crypt-villus axis.

740 In the new version of the model, growing cells expand in the vertical Z 741 direction, unless the force generated by growth is not enough to deform neighbouring 742 Paneth cells, which in that case are obstacles to the flow that force cell shape 743 deformation in the XY plane protruding out of the crypt wall.

The Monte Carlo simulation previously described ²⁹ has been extended by updating the cell viscous behaviour and accordingly cell position at each time-step. Time-steps include division times. All other cell properties such as size, type, age are updated as previously described ²⁹. A summary of the extended approach is as follows:

Proliferative and stem cells grow, increasing their size to reach twice their
 original size by division time according to the proliferation rates previously described
 ²⁹. Non-proliferative cells also grow at those rates until they reach their final size.

752 2) The viscous behaviour of non-growing cells, such as mature Paneth cells, and 753 the sets of deformable cells are evaluated by comparing the ratio between the overall 754 size of neighbouring deformable cells and the available space. Paneth cells subjected 755 to forces that are not greater than the threshold and are not deformable and remain in 756 their original position. The deformation out of the crypt plane of growing stem cells 757 surrounded by non-deformable Paneth cells is quantified as described in the section 758 above. When the protrusion of cell material is significant, at division time, the 759 daughter cells will form a bud located out of the plane of the crypt.

760 3) In regions where all cells are deformable, the increase of cell size takes place 761 within the crypt wall and the cell deforms mainly in the direction of the crypt 762 longitudinal, or Z, axis. At each time step, the crypt is reorganized to accommodate 763 changes in cell size, which are translated in changes in the Z coordinate for the 764 majority of cells, while cell coordinates in the XY plane practically do not change. 765 Dividing cells partition into two daughter cells with similar size which is randomly apportioned ²⁹. The division event does not imply any increase of cell size, however, 766 767 in practice, after division the one dimensional chain used to build the three

25

768 dimensional helix has to be reorganized to assign an index to the new cell as 769 previously described²⁹. One of the daughter cells is assigned with the index of the cell 770 located in the ring immediately above. The vertical adjustment of indices spreads 771 upwards along the crypt until the cell in the last ring. The position and shape of the 772 relocated cell are accommodated to fit the space occupied by the cell immediately 773 above and this has an impact on cell displacement. To quantify this impact, we have 774 measured the velocity of cells during time intervals that include index rearrangement 775 and compared it with velocities of cells that do not change the ring. Supplementary 776 Figure S1 shows the comparison of the total distance and the distance in each 777 dimension travelled by cells during time intervals with and without index 778 reassignment. We have estimated that on average index reassignment takes place in 779 the crypt in 20% of the cell movements and it generally causes a small increase of the 780 total travelled distance by the cell by affecting mainly cell displacement on the XY 781 plane (Supplementary Figure S1); this is because cells are not aligned along the crypt 782 wall. Despite the impact of the index reassignment process on cell displacement, our 783 approach is a good approximation to describe continuous cell growth and migration and cellular compaction within the crypt in a similar way to lattice free models ⁵⁷⁻⁶⁰ 784 and therefore, it differs from automota cell models using rigid lattices ^{61, 62} in which 785 786 cells migrate by discontinuous large movements.

787 In our approach, cell migration is exactly modelled as the result of the balance 788 of forces during the process of cell deformation out of the crypt plane. However, cell 789 migration within the crypt plane is simulated by a Monte Carlo approach without 790 applying explicit energy balance equations. This is possible because inertial forces are 791 neglected and cell displacement is assumed to be the consequence of cell growth only, 792 that are common assumptions when modelling cell dynamics in the crypt ^{59, 63}. To 793 evaluate the applicability of our model, we have compared simulated cell velocities 794 with theoretical cell velocities resulting from the total force exerted by neighbouring cells as the consequence of cell growth and migration ⁶³. Supplementary Figure S2 795 796 shows that the simulated and theoretical velocity is practically the same for a high 797 percentage (\sim 70%) of cells when they do not change index position in the helix. 798 During cell relocation in the helix, the balance of forces is maintained only in $\sim 40\%$ 799 of the cases while for the rest, the simulated velocity is greater than the theoretical 800 velocity (Supplementary Figure S2). Therefore, a proportion of punctual cell 801 velocities with our modelling approach could be slighted overestimated.

26

| 802 |
|-----|
|-----|

803 Computational model for the development of a new crypt from the crypt 804 partition process.

805 The biomechanics of the progression of the initial deformation towards a new 806 crypt is currently unknown and we have therefore adopted a simple descriptive 807 geometrical approach. The initial bud is assumed to be formed by the newly generated 808 cells after division and the surrounding Paneth cells from the original crypt; with 809 practically no displacement of Paneth cells, the initial spiral is located orthogonally to 810 the tangent plane to the original stem cell centre. The new crypt is developed from the 811 bud by proliferation and differentiation of cells that progressively form a new spiral 812 and helix according to a given final number of crypt cells as previously described ²⁹. 813 The final size of the new crypt is assumed to be equal to the size of the primary crypt.

814 We assume that cells in the bud proliferate and generate a new crypt, protruding 815 from the primary crypt independently of the primary crypt. In the primary crypt the 816 insertion of the new crypt is represented by a disk of a diameter equal to the 817 secondary crypt mouth. The new crypt is located orthogonally to the tangent plane to 818 the central point of the crypt insertion disk and therefore, the lumens of both crypts 819 are assumed to be connected from the earliest stage (Supplementary Figure S3). Cell 820 differentiation and proliferation in the primary crypt is not affected by the presence of 821 the bud so that the primary crypt deals with the area of insertion of the new crypt in 822 the same way as with no budding regions.

823 Mitotic pressure in the primary crypt forces the upward migration of the 824 secondary crypt, which simultaneously grows and protrudes out of the primary crypt. 825 Thus, the growth and migration of the secondary crypt are independent processes. We 826 assumed that when the secondary crypt reaches its final size its length stops increasing 827 and cell proliferation forces either cell shedding into the lumen, or cell migration to 828 any adjacent villus structures or to the walls of the primary crypt, whilst the secondary 829 crypt has not yet reached the top of the primary crypt. Crypt fission or partition occurs 830 when the secondary crypt reaches the top of the primary crypt.

831

832 Stochastic simulation of the growth of the intestinal epithelium by crypt fission

We developed a Monte-Carlo simulation algorithm to simulate the growth of the intestinal epithelium. The time for the following budding event in a crypt is generated by randomly sampling from the histogram of the time intervals between budding events in Figure 4A; the specific growth rate is assigned to each crypt by
randomly sampling from the simulated histogram in Figure 5A. Budding times are
used as time steps. At each time step, a new crypt formed by 1 cell is added into the
epithelium and the size of all growing crypts is updated. Crypts stop growing after
reaching their final size. Simulations were started from a single crypt.

841
842
Statistical Analysis

- 843 Growth rates were estimated by lineal regression after the logarithmic
- transformation of the dependent variable when required. Median values were
- 845 compared by a Wilcoxon-Mann-Whitney test.
- 846

847 Acknowledgments

- 848 Authors kindly acknowledge the help of Gary Barker with modelling the
- 849 behaviour of viscoelastic material.

850

| 851 852 | | |
|-------------------|-----|---|
| 853 854 | 1. | L. Cheng, K. Araki, Y. Furuya, T. Matsuoka, K. Mashima, M. Kobayashi and K. Matsuura, <i>Med Electron Microsc</i> , 2000, 33, 165-171. |
| 855 | 2. | N. A. Wright and A. Al-Nafussi, Cell Tissue Kinet, 1982, 15, 611-621. |
| 856 | 3. | A. B. Cairnie and B. H. Millen, Cell Tissue Kinet, 1975, 8, 189-196. |
| 857 858 | 4. | N. A. Wright and M. R. Alison, <i>The biology of epithelial cell populations</i> . <i>Volume 2</i> , Clarendon Press, Oxford, 1984. |
| 859 | 5. | R. M. Clarke, J Anat, 1972, 112, 27-33. |
| 860 861 862 | 6. | C. M. Dekaney, J. J. Fong, R. J. Rigby, P. K. Lund, S. J. Henning and M. A. Helmrath, <i>American journal of physiology. Gastrointestinal and liver physiology</i> , 2007, 293, G1013-1022. |
| 863 | 7. | W. H. St Clair and J. W. Osborne, Cell Tissue Kinet, 1985, 18, 255-262. |
| 864 865 | 8. | H. S. Wasan, H. S. Park, K. C. Liu, N. K. Mandir, A. Winnett, P. Sasieni, W. F. Bodmer, R. A. Goodlad and N. A. Wright, <i>J Pathol</i> , 1998, 185, 246-255. |
| 866 867 868 | 9. | N. Barker, R. A. Ridgway, J. H. van Es, M. van de Wetering, H. Begthel, M. van den Born, E. Danenberg, A. R. Clarke, O. J. Sansom and H. Clevers, <i>Nature</i> , 2009, 457, 608-611. |
| 869 | 10. | N. A. Wright, Int J Exp Pathol, 2000, 81, 117-143. |
| 870 871 | 11. | W. M. Wong, N. Mandir, R. A. Goodlad, B. C. Wong, S. B. Garcia, S. K. Lam and N. A. Wright, <i>Gut</i> , 2002, 50, 212-217. |
| 872 | 12. | A. Humphries and N. A. Wright, Nat Rev Cancer, 2008, 8, 415-424. |
| 873 874 | 13. | A. P. Haramis, H. Begthel, M. van den Born, J. van Es, S. Jonkheer, G. J. Offerhaus and H. Clevers, <i>Science</i> , 2004, 303, 1684-1686. |
| 875 | 14. | N. Arber and M. Moshkowitz, Curr Gastroenterol Rep, 2011, 13, 435-441. |
| 876 | 15. | J. Totafurno, M. Bjerknes and H. Cheng, Biophys J, 1987, 52, 279-294. |
| 877 | 16. | M. Loeffler and B. Grossmann, J Theor Biol, 1991, 150, 175-191. |
| 878 879 | 17. | Y. Q. Li, S. A. Roberts, U. Paulus, M. Loeffler and C. S. Potten, <i>J Cell Sci</i> , 1994, 107 (Pt 12), 3271-3279. |
| 880 881 | 18. | M. Loeffler, T. Bratke, U. Paulus, Y. Q. Li and C. S. Potten, J Theor Biol, 1997, 186, 41-54. |

- 882 19. D. Drasdo, Phys Rev Lett, 2000, 84, 4244-4247.
- 883 20. C. M. Edwards and S. J. Chapman, *B Math Biol*, 2007, 69, 1927-1942.
- 884 21. E. Hannezo, J. Prost and J. F. Joanny, *Phys Rev Lett*, 2011, 107, 078104.
- 885 22. M. R. Nelson, D. Howard, O. E. Jensen, J. R. King, F. R. Rose and S. L.
 886 Waters, *Biomech Model Mechanobiol*, 2011, 10, 883-900.
- P. Buske, J. Przybilla, M. Loeffler, N. Sachs, T. Sato, H. Clevers and J. Galle, *FEBS J*, 2012, DOI: 10.1111/j.1742-4658.2012.08646.x.
- T. Sato, D. E. Stange, M. Ferrante, R. G. Vries, J. H. Van Es, S. Van den Brink, W. J. Van Houdt, A. Pronk, J. Van Gorp, P. D. Siersema and H. Clevers, *Gastroenterology*, 2011, 141, 1762-1772.
- T. Sato, R. G. Vries, H. J. Snippert, M. van de Wetering, N. Barker, D. E.
 Stange, J. H. van Es, A. Abo, P. Kujala, P. J. Peters and H. Clevers, *Nature*,
 2009, 459, 262-U147.
- A. Ootani, X. Li, E. Sangiorgi, Q. T. Ho, H. Ueno, S. Toda, H. Sugihara, K.
 Fujimoto, I. L. Weissman, M. R. Capecchi and C. J. Kuo, *Nat Med*, 2009, 15, 701-706.
- T. Sato, J. H. van Es, H. J. Snippert, D. E. Stange, R. G. Vries, M. van den Born, N. Barker, N. F. Shroyer, M. van de Wetering and H. Clevers, *Nature*, 2011, 469, 415-+.
- 901 28. A. Durand, B. Donahue, G. Peignon, F. Letourneur, N. Cagnard, C.
 902 Slomianny, C. Perret, N. F. Shroyer and B. Romagnolo, *PNAS USA*, 2012, 109, 8965-8970.
- 904 29. C. Pin, A. J. Watson and S. R. Carding, *Plos One*, 2012, 7, e37115.
- 905 30. H. J. Snippert, A. G. Schepers, J. H. van Es, B. D. Simons and H. Clevers,
 906 *EMBO reports*, 2014, 15, 62-69.
- 907 31. C. S. Potten, *Philosophical Transactions of the Royal Society B-Biological*908 Sciences, 1998, 353, 821-830.
- A. Hirata, J. Utikal, S. Yamashita, H. Aoki, A. Watanabe, T. Yamamoto, H.
 Okano, N. Bardeesy, T. Kunisada, T. Ushijima, A. Hara, R. Jaenisch, K.
 Hochedlinger and Y. Yamada, *Development*, 2013, 140, 66-75.
- 33. A. Humphries, B. Cereser, L. J. Gay, D. S. Miller, B. Das, A. Gutteridge, G.
 Elia, E. Nye, R. Jeffery, R. Poulsom, M. R. Novelli, M. Rodriguez-Justo, S. A.
 McDonald, N. A. Wright and T. A. Graham, *Proc Natl Acad Sci U S A*, 2013, 110, E2490-2499.
- 916 34. H. Cheng and M. Bjerknes, Anat Rec, 1985, 211, 420-426.

| 917 918 | 35. | J. J. Dehmer, A. P. Garrison, K. E. Speck, C. M. Dekaney, L. Van Landeghem, X. F. Sun, S. J. Henning and M. A. Helmrath, <i>Plos One</i> , 2011, 6. | | | |
|---------------------------------|-----|---|--|--|--|
| 919 920 921 | 36. | A. G. Cummins, A. G. Catto-Smith, D. J. Cameron, R. T. Couper, G. P. Davidson, A. S. Day, P. D. Hammond, D. J. Moore and F. M. Thompson, <i>J Pediatr Gastroenterol Nutr</i> , 2008, 47, 153-157. | | | |
| 922 923 | 37. | M. R. Nelson, J. R. King and O. E. Jensen, <i>Mathematical biosciences</i> , 2013, 246, 229-241. | | | |
| 924 925 | 38. | S. J. Dunn, A. G. Fletcher, S. J. Chapman, D. J. Gavaghan and J. M. Osborne, <i>J Theor Biol</i> , 2012, 298, 82-91. | | | |
| 926 927 | 39. | D. Drasdo and M. Loeffler, Nonlinear Analysis-Theory Methods & Applications, 2001, 47, 245-256. | | | |
| 928 929 | 40. | J. Berlanga-Acosta, R. J. Playford, N. Mandir and R. A. Goodlad, <i>Gut</i> , 2001, 48, 803-807. | | | |
| 930 931 | 41. | O. Bashir, A. J. Fitzgerald, J. Berlanga-Acosta, R. J. Playford and R. A. Goodlad, <i>Clin Sci (Lond)</i> , 2003, 105, 323-330. | | | |
| 932 933 | 42. | A. G. Cummins, B. J. Jones and F. M. Thompson, <i>Digest Dis Sci</i> , 2006, 51, 718-723. | | | |
| 934 935 936 937 938 | 43. | A. Milicic, L. A. Harrison, R. A. Goodlad, R. G. Hardy, A. M. Nicholson, M. Presz, O. Sieber, S. Santander, J. H. Pringle, N. Mandir, P. East, J. Obszynska, S. Sanders, E. Piazuelo, J. Shaw, R. Harrison, I. P. Tomlinson, S. A. McDonald, N. A. Wright and J. A. Jankowski, <i>Cancer Res</i> , 2008, 68, 7760-7768. | | | |
| 939 940 941 | 44. | J. K. Fauser, R. P. Donato, J. A. Woenig, S. J. Proctor, A. P. Trotta, P. K. Grover, G. S. Howarth, I. A. Penttila and A. G. Cummins, <i>J Pediatr Gastroenterol Nutr</i> , 2012, 55, 26-31. | | | |
| 942 943 944 | 45. | P. Andreu, S. Colnot, C. Godard, S. Gad, P. Chafey, M. Niwa-Kawakita, P. Laurent-Puig, A. Kahn, S. Robine, C. Perret and B. Romagnolo, <i>Development</i> , 2005, 132, 1443-1451. | | | |
| 945 946 947 | 46. | M. E. Rothenberg, Y. Nusse, T. Kalisky, J. J. Lee, P. Dalerba, F. Scheeren, N. Lobo, S. Kulkarni, S. Sim, D. Qian, P. A. Beachy, P. J. Pasricha, S. R. Quake and M. F. Clarke, <i>Gastroenterology</i> , 2012, 142, 1195-1205 e1196. | | | |
| 948 949 | 47. | S. Roth, P. Franken, A. Sacchetti, A. Kremer, K. Anderson, O. Sansom and R. Fodde, <i>Plos One</i> , 2012, 7, e38965. | | | |
| 950 951 952 953 | 48. | J. H. van Es, T. Sato, M. van de Wetering, A. Lyubimova, A. N. Nee, A. Gregorieff, N. Sasaki, L. Zeinstra, M. van den Born, J. Korving, A. C. Martens, N. Barker, A. van Oudenaarden and H. Clevers, <i>Nature cell biology</i> , 2012, 14, 1099-1104. | | | |

- 954 49. S. J. Buczacki, H. I. Zecchini, A. M. Nicholson, R. Russell, L. Vermeulen, R.
 955 Kemp and D. J. Winton, *Nature*, 2013, 495, 65-69.
- 956 50. H. Clevers, *Nature*, 2013, 495, 53-54.
- 957 51. M. Leushacke, A. Ng, J. Galle, M. Loeffler and N. Barker, Cell, 2013, 5, 1-8.
- 958 52. H. Miyoshi, R. Ajima, C. T. Luo, T. P. Yamaguchi and T. S. Stappenbeck,
 959 Science, 2012, 338, 108-113.
- 53. T. Sato, R. G. Vries, H. J. Snippert, M. van de Wetering, N. Barker, D. E.
 Stange, J. H. van Es, A. Abo, P. Kujala, P. J. Peters and H. Clevers, *Nature*, 2009, 459, 262-265.
- 963 54. N. Barker, J. H. van Es, J. Kuipers, P. Kujala, M. van den Born, M. Cozijnsen,
 964 A. Haegebarth, J. Korving, H. Begthel, P. J. Peters and H. Clevers, *Nature*,
 965 2007, 449, 1003-U1001.
- 966 55. Q. S. Li, G. Y. Lee, C. N. Ong and C. T. Lim, *Biochem Biophys Res Commun*, 2008, 374, 609-613.
- 968 56. J. L. Hutter and J. Bechhoefer, *Rev Sci Instrum*, 1993, 64, 1868-1873.
- 969 57. F. A. Meineke, C. S. Potten and M. Loeffler, *Cell Proliferat*, 2001, 34, 253970 266.
- 971 58. J. Galle, M. Hoffmann and G. Aust, J Math Biol, 2009, 58, 261-283.
- 972 59. P. Buske, J. Galle, N. Barker, G. Aust, H. Clevers and M. Loeffler, *PLoS computational biology*, 2011, 7, e1001045.
- 974 60. J. M. Osborne, A. Walter, S. K. Kershaw, G. R. Mirams, A. G. Fletcher, P.
 975 Pathmanathan, D. Gavaghan, O. E. Jensen, P. K. Maini and H. M. Byrne,
 976 *Philos T Roy Soc A*, 2010, 368, 5013-5028.
- 977 61. M. Loeffler, R. Stein, H. E. Wichmann, C. S. Potten, P. Kaur and S.
 978 Chwalinski, *Cell Tissue Kinet*, 1986, 19, 627-645.
- 979 62. M. Loeffler, C. S. Potten, U. Paulus, J. Glatzer and S. Chwalinski, *Cell Tissue Kinet*, 1988, 21, 247-258.
- 981 63. J. Pitt-Francis, P. Pathmanathan, M. O. Bernabeu, R. Bordas, J. Cooper, A. G.
 982 Fletcher, G. R. Mirams, P. Murray, J. M. Osborne, A. Walter, S. J. Chapman,
 983 A. Garny, I. M. M. van Leeuwen, P. K. Maini, B. Rodriguez, S. L. Waters, J.
 984 P. Whiteley, H. M. Byrne and D. J. Gavaghan, *Comput Phys Commun*, 2009,
 985 180, 2452-2471.
- 986

987 Figure Legends

| 0 | 0 | 0 | |
|---|---|---|--|
| 9 | х | x | |

989 Figure 1. Fluorescent microscopy of small intestinal organoids undergoing budding 990 events. Lgr5+ stem cells are labelled in green. Lysozyme granules in Paneth cells are 991 in red and cell nuclei in blue. Yellow arrows point at Paneth and stem cells 992 intermingling at the base of the crypts. Red arrows indicate the initiation of buds in 993 regions where Paneth cells are located. Green arrows point at stem cells located in 994 between Paneth cells.

Figure 2. Crypt fission in cultured murine small intestinal organoids. Budding isinitiated in areas rich in Paneth cells (asterisk).

Figure 3. (A) Comparison of the Young's modulus measured by Atomic Force
Microscopy (AFM) of Lgr5-eGFP positive stem cells (red lines) and Paneth cells
identified visually as non-fluorescent large granular cells (black lines). The Young's
modulus reflects cell stiffness. (B) AFM force approach and retract curves showing
hysteresis characteristic to viscous material. Colour codes as in 3A.

1002 Figure 4. Comparison between fission measurements in simulated crypts and in 1003 cultured organoids: (A) Observed (black bars; n=22 initial crypts) and simulated (red 1004 bars; n=30-40 initial crypts simulated during 12 days for each tested value of α) 1005 distributions for the time interval between successive budding processes per crypt. 1006 Plots show the results obtained with twelve values of the parameter α , from 0.1 to 2, 1007 which controls the force required to deform Paneth cells. (B) Square difference 1008 between the observed and simulated frequencies plotted in Figure 4A; the smallest 1009 difference was detected with $\alpha = 1.3$. (C) Simulated probability of budding -within a 1010 12 days period- of stem cells clusters surrounded by Paneth cells with several values 1011 for the parameter α and for cluster sizes of 1 (•), 2 (\Diamond), 3 (+) and 4 (\circ) stem cells. (D) 1012 Percentage of clusters of stem cells surrounded by Paneth cells of size of 1 (\bullet), 2 (\diamond), 1013 3 (+) and 4 (\circ) stem cells in simulated crypts. (E-H) Schematic representation of the 1014 location of the cell centres on the ring of the crypt formed by stem, S, and Paneth, P, 1015 cells when (E) all cells are deformable stem cells; (F) Paneth and stem cells have the 1016 same viscoelastic behaviour and (G) Paneth cells are more resistant to deformation 1017 $(\alpha=1.3)$ than stem cells. The simulated location of cell centres occurs over a period of 1018 20 days. For all hypotheses the duration of the stem cell division cycle is a normal 1019 distributed random variable with a mean value of 21.5 h and standard deviation of 1020 2.15 h. Stem cells divide asynchronously. (H) Location of cell centres (dots) and cell 1021 boundaries (lines) at the beginning of the division cycle (discontinuous lines) of a

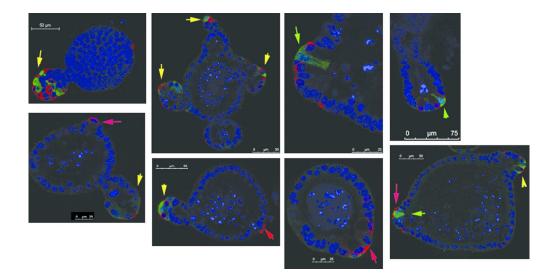
1022 stem cell (marked with an asterisk) surrounded by Paneth cells and ~ 21 h later 1023 immediately before division (continuous lines) under the hypothesis that Paneth cells 1024 are more resistance to deformation (α =1.3). 1025 1026 Figure 5. (A) Observed (black bars; n=17) and simulated (red bars; n=89) 1027 distributions for the for the specific growth rate of the crypt length. (B) Observed 1028 (black) and simulated (red) migration curves of the secondary crypt along the length 1029 of the primary crypt expressed in percentage. 1030 1031 Figure 6. Appearance of a secondary crypt completely developed at the base of the 1032 original crypt without migrating upwards and which replaces the original crypt. 1033 1034 **Figure 7**. Simulated growth of the new crypt and migration along the original crypt: 1035 (A) Simulated distributions of the time for the secondary crypt to reach its final size 1036 and (B) to reach the top of the original crypt. (C) Distribution of the position of the 1037 secondary crypt when reaching the final size and (D) of the size -number of cells- of 1038 the secondary crypt when reaching the top of the original crypt. 1039 1040 Figure 8. Average proportions of each cell type during crypt fission. A) Proportion of 1041 stem and secretory cells and B) of proliferative cells and absorptive progenitors per 1042 crypt. 1043 1044 Figure 9. Predicting growth of the intestinal epithelium by crypt fission. The 1045 predicted number of crypts and cells in the newly formed tissue assumes that budding 1046 and fission always take place in a crypt when a stem cell is surrounded by Paneth 1047 cells.

1048

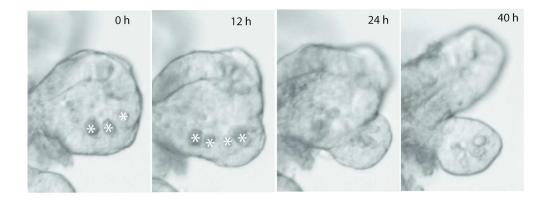
Figure 10. Geometry of the viscoelastic behavior of cells within the crypt. The deformation of the external side of the cell can be monitored by measuring the deformation of either the central vertical, i, or central horizontal, ii, axis. The pressure per unit length, P, derives from the difference between cell size and available space and it is uniformly applied to the external edge of a cell of width equal to 2R. The length of the cell external edge is equal to L. v_y is the velocity of the flow in the Y direction.

34

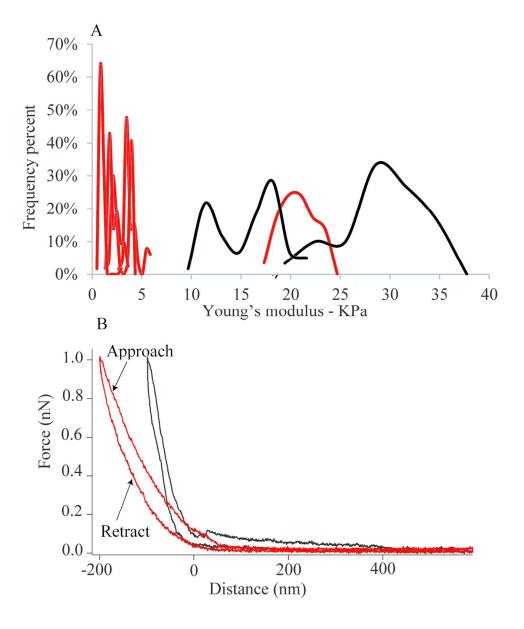
| 1056 | | |
|------|---|--|
| 1057 | Supplementary data | |
| 1058 | | |
| 1059 | Table S1. Individual based model parameters | |
| 1060 | | |
| 1061 | Figure S1. Frequency of cell velocities (cell positions/h) along the crypt during index | |
| 1062 | reassignment process, i.e. moving to the ring immediately above (blue columns), and | |
| 1063 | during time intervals in which cells do not change rings (red columns). Velocities are | |
| 1064 | estimated in the three-dimensional space (A) as well as in each of the dimensions, Z | |
| 1065 | (B), X (C) and Y (D). Velocities were estimated from 14.000 cells located in the | |
| 1066 | upper half of a simulated crypt during one week. Numbers represent the average | |
| 1067 | velocities and their standard errors for each group of cells according to colour. | |
| 1068 | | |
| 1069 | Figure S2. Comparison of the theoretical velocity derived from the balance of forces | |
| 1070 | within the crypt and the simulated velocity in our model. The difference between the | |
| 1071 | theoretical and simulated velocity was measured in 40,000 cells evolving in a | |
| 1072 | simulated crypt during one week. Blue columns represent velocity frequencies for | |
| 1073 | cells undertaking index reassignment and therefore moving to the ring immediately | |
| 1074 | above, while red columns are for cells that do not change ring. Numbers represent the | |
| 1075 | average velocities for each group of cells according to colour. | |
| 1076 | | |
| 1077 | Figure S3. Longitudinal view of a simulated fission event. The white arrow marks the | |
| 1078 | initial location of the bud in the primary crypt at the time of fission initiation. The bud | |
| 1079 | grows into a crypt that migrates upwards the primary crypt in the following days. The | |
| 1080 | lumen (red) of both crypts is connected during this process. | |
| 1081 | | |
| 1082 | Video S1. Simulation of a crypt fission event. Cells are represented by spherical | |
| 1083 | shapes unrelated to the modelled cell shape. | |
| 1084 | | |
| 1085 | Video S2. Simulation of a crypt fission event coupled with the observation of a crypt | |
| 1086 | undergoing fission in a cultured organoid - period of observation is 1.2 days. Cells are | |
| 1087 | represented by spherical shapes unrelated to the modelled cell shape. | |



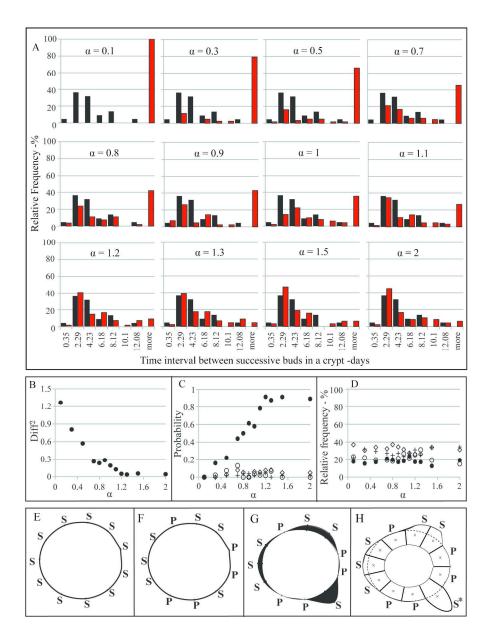
329x168mm (72 x 72 DPI)



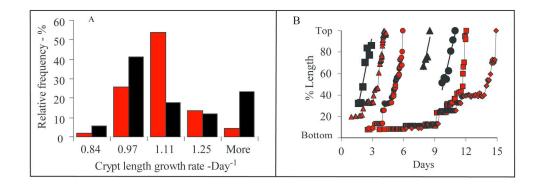
179x66mm (300 x 300 DPI)



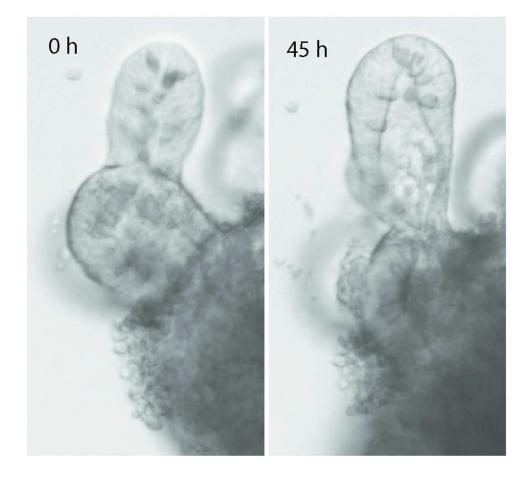
123x148mm (300 x 300 DPI)



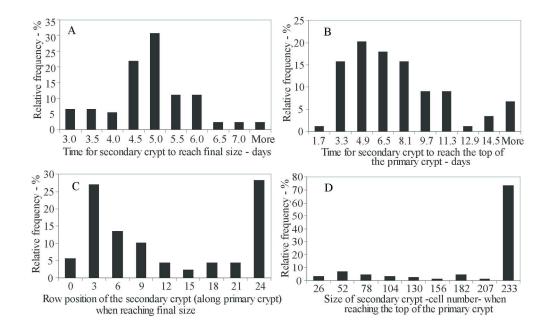
182x243mm (300 x 300 DPI)



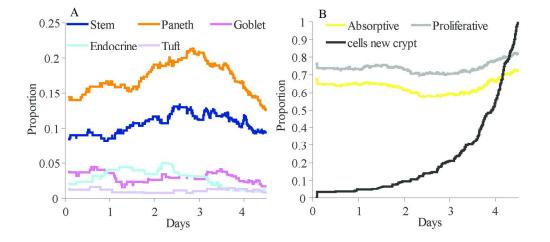
185x67mm (300 x 300 DPI)



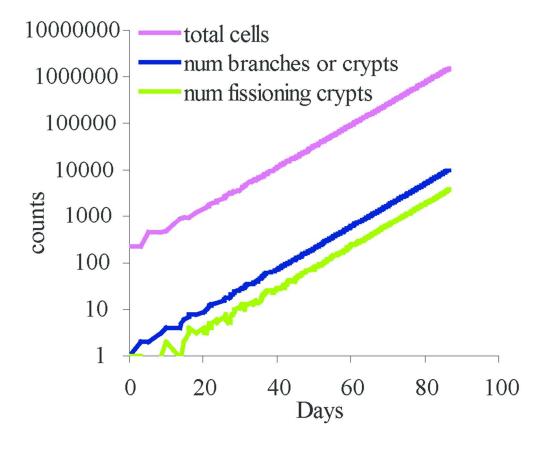
90x82mm (300 x 300 DPI)



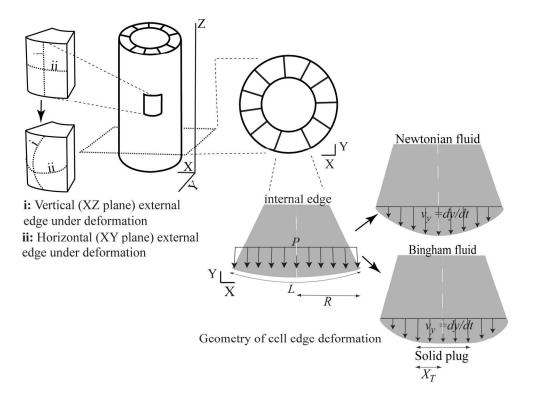
180x109mm (300 x 300 DPI)



172x78mm (300 x 300 DPI)



87x71mm (300 x 300 DPI)



163x123mm (300 x 300 DPI)

| Parameter | Value | source | definition |
|----------------------------|---|------------------------|--|
| ncells | 235 | data ²⁹ | Number of cells in the crypt |
| <i>n</i> _{spiral} | 33 | data ²⁹ | Number of Paneth and Stem cells in the stem cell niche |
| $Diff_{Secr}$ | >50% | data ²⁹ | Percentage of secretory neighbouring cells that inhibit differentiation into secretory lineage |
| D _c | -5.7091 <i>N</i> _d + 21.449 | data ^{29, 62} | Duration of division cycle (hours). N_d is the number of undertaken divisions by the cell: its value is fixed to 0 for stem cells and for transit cells the maximum value is 2. |
| n | 6 | data ²⁹ | Maximum number of division cycles in transit amplifying cells |
| R_{av} | 5 | data | Average cell radius at birth (µm) |
| r _{av} | $\frac{\pi R_{av}^{2}}{D_{c}}$ | data | Average growth rate of the surface area of cells $(\mu m^2 h^{-1})$ |
| α | 1.3 | data | Parameter governing the shear stress threshold in Paneth cells |

Table S1. Individual based model parameters

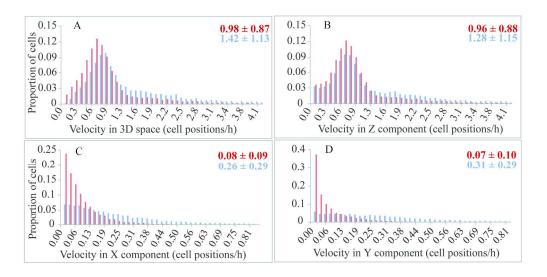


Figure S1. Frequency of cell velocities (cell positions/h) along the crypt during index reassignment process, i.e. moving to the ring immediately above (blue columns), and during time intervals in which cells do not change rings (red columns). Velocities are estimated in the three-dimensional space (A) as well as in each of the dimensions, Z (B), X (C) and Y (D). Velocities were estimated from 14.000 cells located in the upper half of a simulated crypt during one week. Numbers represent the average velocities and their standard errors for each group of cells according to colour. 193x96mm (300 x 300 DPI)

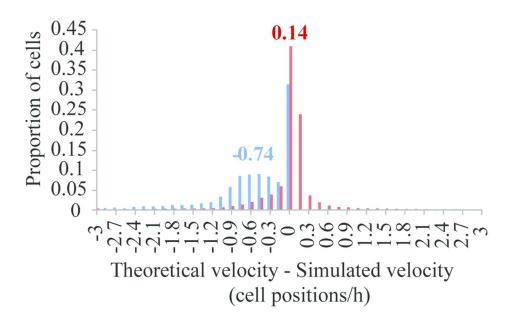


Figure S2. Comparison of the theoretical velocity derived from the balance of forces within the crypt and the simulated velocity in our model. The difference between the theoretical and simulated velocity was measured in 40,000 cells evolving in a simulated crypt during one week. Blue columns represent velocity frequencies for cells undertaking index reassignment and therefore moving to the ring immediately above, while red columns are for cells that do not change ring. Numbers represent the average velocities for each group of cells according to colour. 101x61mm (300 x 300 DPI)

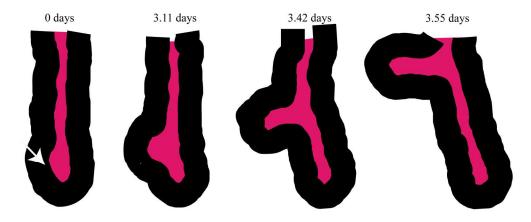


Figure S3. Longitudinal view of a simulated fission event. The white arrow marks the initial location of the bud in the primary crypt at the time of fission initiation. The bud grows into a crypt that migrates upwards the primary crypt in the following days. The lumen (red) of both crypts is connected during this process. 185x76mm (300 x 300 DPI)