# **Optical Electrostriction**

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# ABSTRACT

It is well known that the forces which light imparts on micro- and nanoparticles arise due to intensity gradients and dielectric mismatch. For laser-irradiated atoms and molecules, optical forces primarily result from close resonance between the optical frequency and an electronic transition. Recently it has emerged that optically induced pair forces also arise, through a modification of Casimir-Polder interactions; preliminary assessments of the mechanism have largely centered on nanoparticle systems. In this paper, we show that a potentially very significant effect can be anticipated in the condensed phase, an optically induced modification of interatomic forces that is capable of generating anisotropic patterns of laser-induced compression and expansion. This phenomenon, termed optical electrostriction, should be measurable and significant when high intensity laser light is transmitted through even an essentially non-absorptive material. However, the full conditions for observation of the effect are such that some competing interactions might also arise. Key parameters that determine the size and character of optical electrostriction are delineated and possible applications are considered, including optical actuators for nanoscale electromechanical systems.

**Keywords**: Optomechanical forces, electrostriction, laser optics, Casimir-Polder interaction, quantum electrodynamics, nanoscale electromechanical systems

#### **1. INTRODUCTION**

The use of laser light to manipulate and guide small particles is an increasingly prominent research tool, finding applications in diverse laboratories. A variety of optomechanical mechanisms operate, across a spectrum of techniques that ranges from optical tweezers to laser cooling and trapping, though all are based on forces that operate directly on individual particles. Recently a wave of excitement has been created by a discovery of an entirely different class of optically induced forces, which operate *between* particles, over nanoscale dimensions.<sup>1-10</sup> Such forces offer a number of highly distinctive features which can be exploited for the controlled optical manipulation of matter. Through such interactions, new opportunities for creating optically ordered matter have already been demonstrated both theoretically and experimentally, leading to the introduction of terms such as 'optical binding' and 'optical matter' in the recent literature.<sup>11-13</sup> Though slightly misleading, these are terms that rightly draw attention to new, intriguing and distinctive phenomena.

The first demonstration of optically induced inter-particle forces occurred in 1980<sup>14</sup>, utilizing the theory of quantum electrodynamics (QED). This was followed by sporadic investigations involving different methods.<sup>15-20</sup> The advent of sufficient laser intensities to study these forces are now routinely available, encouraging new interest; indeed, there is now good reason to expect significant effects to be experimentally demonstrable at much lower intensity levels than originally expected. In 2005 the UEA quantum electrodynamics group published the first fully comprehensive theory of optically induced inter-particle force, based on QED.<sup>21</sup> Specific calculations were also performed for carbon nanotubes,<sup>22</sup> and the practicality of measuring significant laser-induced forces and torques was proven. It was also shown that the use of wavefront-structured light, such as Laguerre-Gaussian beams, offers further scope to tailor the pattern of such forces and torques; it can, for example, provide a means of achieving particle ring formations.<sup>23</sup>

In recently published material,<sup>24</sup> we have shown how the mechanism for optical binding owes its origin to a modification of Casimir-Polder forces. One of the possible manifestations that we have recently begun to consider is the effect of intense throughput optical radiation on optically transparent solids, where it is conceivable that effects

extending to the microscale might arise from the combined influence of light on the nearest-neighbor interactions between constituent particles of matter (atoms or molecules). It is the further exploration and quantification of this solid-state effect that we report below, as well as possible mechanisms for the detection of associated mechanical forces.

#### 2. PERTURBATIVE CALCULATIONS

We begin by defining the components of a simple system comprising a pair of particles A and B, each with distinct electronic integrity and electrical neutrality, together with the radiation field. As is appropriate for the subsequent applications detailed specifically, the term 'molecules' will be used in the following as a generic descriptor of these particles. Representing the system in quantum electrodynamical terms in the Coulomb gauge ensures that the coupling fields are duly retarded and satisfy causality.<sup>25</sup> In multipolar form the system Hamiltonian may be represented thus;

$$H = \sum_{\xi = A,B} H_{mol}^{\xi} + \sum_{\xi = A,B} H_{int}^{\xi} + H_{rad} \quad ,$$
(2.1)

Here  $H_{\text{mol}}^{\xi}$  is the field-free multipolar Hamiltonian for molecule  $\xi$ , operator  $H_{\text{int}}^{\xi}$  represents the interaction of  $\xi$  with the radiation field, and  $H_{\text{rad}}$  is the radiation Hamiltonian. The tripartite simplicity of equation (2.1) specifically results from adoption of the multipolar form of light-matter interaction, based on a well-known canonical transformation from the minimal-coupling interaction.<sup>26-28</sup> This procedure results in a precise cancellation from the system Hamiltonian of all Coulombic terms, save those intrinsic to the internal structure of the Hamiltonian operators for the component molecules. In the electric dipole approximation,  $H_{\text{int}}^{\xi}$  is given by;

$$H_{\rm int}^{\xi} = -\varepsilon_0^{-1} \sum_{\xi} \boldsymbol{\mu}(\xi) \cdot \boldsymbol{d}^{\perp}(\boldsymbol{R}_{\xi}) \quad , \qquad (2.2)$$

with  $\mu(\xi)$  and  $\mathbf{R}_{\xi}$  respectively denoting the electric-dipole moment operator and the position vector of molecule  $\xi$ . The operator  $\mathbf{d}^{\perp}(\mathbf{R}_{\xi})$ , representing the transverse electric displacement field at that location, is expressible in the following mode expansion involving summations over optical wave-vectors,  $\mathbf{p}$ , and polarizations,  $\varepsilon$ ,

$$\mathbf{d}^{\perp}(\mathbf{R}_{\xi}) = i \sum_{\mathbf{p},\varepsilon} \left( \frac{\hbar c p \varepsilon_0}{2V} \right)^{1/2} \left\{ \mathbf{e}^{(\varepsilon)}(\mathbf{p}) a^{(\varepsilon)}(\mathbf{p}) e^{\mathbf{i}(\mathbf{p}\cdot\mathbf{R}_{\xi})} - \overline{\mathbf{e}}^{(\varepsilon)}(\mathbf{p}) a^{\dagger(\varepsilon)}(\mathbf{p}) e^{-\mathbf{i}\left(\mathbf{p}\cdot\mathbf{R}_{\xi}\right)} \right\} .$$
(2.3)

Here  $\mathbf{e}^{(\varepsilon)}(\mathbf{p})$  is the polarization unit vector ( $\overline{\mathbf{e}}^{(\varepsilon)}(\mathbf{p})$  being its complex conjugate, the admission of complex polarizations allowing for circular or elliptical as well as plane polarization); V is an arbitrary quantization volume and  $a^{(\varepsilon)}(\mathbf{p})$ ,  $a^{\dagger(\varepsilon)}(\mathbf{p})$  are respectively the photon annihilation and creation operators for a radiation mode ( $\mathbf{p}, \varepsilon$ ).

To secure a general result for the optically induced energy-shift,  $\Delta E$ , and hence the associated force between A and B, requires the implementation of fourth-order perturbation theory – since the interaction entails four molecule-radiation field coupling events;

$$\Delta E = \operatorname{Re}\left\{\sum_{i,s,r} \frac{\langle i|H_{int}|t\rangle \langle t|H_{int}|s\rangle \langle s|H_{int}|r\rangle \langle r|H_{int}|i\rangle}{(E_i - E_i)(E_i - E_s)(E_i - E_r)}\right\} \quad .$$
(2.4)

Here all states are those of the *system*, i.e. the two molecules plus the radiation field;  $|i\rangle$  is the unperturbed system state in which both molecules are in their electronic ground state,  $|r\rangle$ ,  $|s\rangle$  and  $|t\rangle$  are virtual states, and  $E_n$  is the energy of state  $|n\rangle$ . The latter signifies one of the basis states for the perturbative development, expressible in the form;

$$|n\rangle = |\operatorname{mol}_n\rangle |\operatorname{rad}_n\rangle \equiv |\operatorname{mol}_n; \operatorname{rad}_n\rangle , \qquad (2.5)$$

with  $|mol_n\rangle$  and  $|rad_n\rangle$  defining states of the molecular pair and the radiation, respectively. In equation (2.4), each operation of  $H_{int}$  on the state to its right effects the annihilation or creation of a photon, as follows from (2.2) and (2.3). The laser-induced interaction involves the annihilation of a throughput photon at one molecule and the stimulated emission of an equivalent 'real' photon into the radiation mode; this is mediated by inter-molecular energy transfer through a virtual photon created at one site and annihilated at the other. The molecules and the throughput radiation suffer no overall change in state; the term 'real' applied to photons of the input mode denotes quanta of electromagnetic radiation with a propagation time that is long compared to the optical cycle, and correspondingly 'real' characteristics.<sup>29</sup> In performing energy shift calculations based on (2.4), detailed representations of all contributory terms are provided by a set of 48 time-ordered diagrams, one of which is exhibited in figure 1.



Figure 1: Time-ordered diagram depicting the annihilation of a real photon at molecule A and the creation of a corresponding real photon at molecule B, coupled by the transfer of a virtual photon between the pair. This diagram is one of 48 generated by eqn. 2.4

When such a large number of time-orderings is involved, a recently devised alternative based on *state-sequence* diagrams<sup>30</sup> proves advantageous. All the time-orderings are in fact accommodated in just two state-sequence diagrams, (one for the case where the real photon absorption occurs at A and the stimulated emission at B, the other where the opposite applies), one of which is shown in figure 2.



Figure 2: State-sequence diagram containing 24 of the time-ordered diagrams generated by eqn. 2.4. Figure 1 is incorporated as the highlighted pathway. Filled circles represent molecules in the ground state and empty circles virtual transition states. The symbols  $\omega$  and  $\phi$  represent real and virtual photons, respectively.

The explicit result for  $\Delta E$  follows the substitution of equations (2.2) and (2.3) in (2.4), recognizing that  $\mu(\xi)$  and  $\mathbf{d}^{\perp}(\mathbf{R}_{\xi})$  operate on  $|\mathrm{mol}_n\rangle$  and  $|\mathrm{rad}_n\rangle$ , respectively – the latter through the following expressions:  $a^{(\varepsilon)}(\mathbf{p})|n(\mathbf{p},\varepsilon)\rangle = \sqrt{n}|(n-1)(\mathbf{p},\varepsilon)\rangle$  and  $a^{\dagger(\varepsilon)}(\mathbf{p})|n(\mathbf{p},\varepsilon)\rangle = \sqrt{n+1}|(n+1)(\mathbf{p},\varepsilon)\rangle$ . Details of the complete calculation are given in a recent paper.<sup>21</sup> The following result thereby emerges, concisely expressible using the implied summation convention for repeated Cartesian tensor indices;

$$\Delta E(k,\mathbf{R}) = \left(\frac{n\hbar ck}{\varepsilon_0 V}\right) \operatorname{Re}\left\{e_i^{(\lambda)} \overline{e}_i^{(\lambda)} \alpha_{ij}^{\mathrm{A}}(k) V_{jk}^{\pm}(k,\mathbf{R}) \alpha_{kl}^{\mathrm{B}}(k) \exp(\mathrm{i}\mathbf{k}.\mathbf{R})\right\} \quad .$$
(2.6)

Here **k** and  $\hbar ck$  denote the input wave-vector and photon energy, respectively, and **R** is the inter-particle displacement vector,  $\mathbf{R} \equiv \mathbf{R}_B - \mathbf{R}_A$ . Also  $V_{jk}^{\pm}$  signifies the fully retarded resonance electric dipole - electric dipole interaction tensor of the form;<sup>31</sup>

$$V_{jk}^{\pm}(k,\mathbf{R}) = \frac{e^{\mp ikR}}{4\pi\varepsilon_0 R^3} \left\{ (1\pm ikR) \left( \delta_{jk} - 3\hat{R}_j \hat{R}_k \right) - (kR)^2 \left( \delta_{jk} - \hat{R}_j \hat{R}_k \right) \right\} , \qquad (2.7)$$

and  $\alpha_{ii}^{\xi}(k)$  is the dynamic polarizability tensor given as;

$$\alpha_{ij}^{\xi}\left(k\right) = \sum_{s} \left\{ \frac{\mu_{i}^{is} \mu_{j}^{si}}{\tilde{E}_{si} - \hbar ck} + \frac{\mu_{j}^{is} \mu_{i}^{si}}{\tilde{E}_{si} + \hbar ck} \right\} \quad , \tag{2.8}$$

where  $\mathbf{\mu}^{xy} = \langle x | \mathbf{\mu} | y \rangle$  and  $\tilde{E}_{xy} \equiv \tilde{E}_x - \tilde{E}_y$ , the tilde denoting the inclusion of damping factors as appropriate.

Before proceeding further, we note that the above result in principle holds for two particles in a vacuum, each with properties expressible in terms of wavefunctions that extend over the whole particle – as is essentially the case for the molecules of a gas. In the condensed phase – the case of molecular solids, or for example particles optically trapped in a host liquid, dissipative and refractive corrections due to the electronic properties of the local environment should be applied to both the inter-particle coupling (which is thereby cast in terms of virtual polaritons rather than photons) and also the interactions with the optical beam. The procedure for introducing such corrections is intricate but the outcome is known<sup>32, 33</sup> and the necessary reformulation of the above result produces the following equation:

$$\Delta E(k,\mathbf{R}) = \operatorname{Re}\left(\frac{n\varepsilon_0 \hbar v_k k}{n_k^3 V}\right) \left(\frac{n_k^2 + 2}{3}\right) \left\{ e_l^{(\lambda)} \overline{e}_l^{(\lambda)} \chi_{ij}^{\prime A}(k) V_{jk}^{\pm}(n_k k,\mathbf{R}) \chi_{kl}^{\prime B}(k) \exp(\mathrm{i}\mathbf{k}.\mathbf{R}) \right\},$$
(2.9)

where  $\chi'$  denotes a linear susceptibility tensor scaled by the corresponding particle volume,  $v_k$  is the group velocity for the medium at optical frequency ck, and  $n_k$  is the corresponding complex refractive index. Although we do not pursue it here, it could be a matter of considerable interest to further develop this equation for nanoparticles such as quantum dots with distinctive dispersion characteristics.

### **3. APPLICATIONS**

In order to observe meaningful shifts in inter-particle forces, a basic requirement is pairs of highly polarizable particles in close proximity to each other, with suitably intense laser radiation present. In previous publications we have focused on interactions between nanoparticles, in one case specifically addressing carbon nanotubes.<sup>22</sup> The latter are particularly

well suited as candidates for observing and exploiting laser-induced pair forces, because of their exceptional electronic properties. At first, it may appear unlikely that similar effects will be observed in smaller molecules due to their reduced polarizability. Two possible approaches can be taken to overcome this problem – either choose a system that is amenable to extremely high resolution mechanical or spectroscopic analysis, so that very small geometric adaptations to an optical pair force can be determined, or probe a system in which small mechanical effects are amplified by scale. In the following we entertain detailed examples of these two distinct cases.

#### 3.1 Van der Waals molecules

Van der Waals molecules are weakly bound, usually dimeric molecular structures. Having significantly larger moments of inertia than their monomer parents – this difference enhanced by the unusually long 'bond' holding the component units together – such dimers are readily identifiable by high resolution microwave spectroscopy. The model system to be examined in more detail below consists of two linear molecules lying end-to-end, with the intermolecular separation vector **R** identified with the Z-axis and the plane-polarized throughput radiation defined by  $\phi$  i.e. the angle between the **e** and **R** vectors. The polarization vector can thus be written in cylindrical form as  $\mathbf{e} = \sin \phi \, \hat{\mathbf{i}} + \cos \phi \, \hat{\mathbf{k}}$ . From eqn (2.6), and acknowledging that  $I(k) = n\hbar c^2 k/V$  is the irradiance of the throughput radiation, the energy shift is;

$$\Delta E(R) = \frac{I}{\varepsilon_0 c} \operatorname{Re} \left\{ \sum_{J,K} \sin^2 \phi \, \alpha_{XJ}^{A} V_{JK}^{\pm} \alpha_{KX}^{B} + \sin \phi \cos \phi \left( \alpha_{XJ}^{A} V_{JK}^{\pm} \alpha_{KZ}^{B} + \alpha_{ZJ}^{A} V_{JK}^{\pm} \alpha_{KX}^{B} \right) + \cos^2 \phi \, \alpha_{ZJ}^{A} V_{JK}^{\pm} \alpha_{KZ}^{B} \right\} \cos(\mathbf{k} \cdot \mathbf{R})$$
(3.1)

where the *k* and **R** dependences are henceforth suppressed and the indices *I*, *J* and *K* are in the laboratory frame. Employing the explicit form of the  $V_{JK}^{\pm}$  tensor from (2.7), and writing  $\alpha_{XX} = \alpha_{\perp}, \alpha_{ZZ} = \alpha_{\parallel}$  for each molecule, equation (3.1) is expressible as;

$$\Delta E(R) = \frac{I}{4\pi\varepsilon_0^2 c} \left[ \left( \sin^2 \phi . \alpha_{\perp}^A \alpha_{\perp}^B - 2\cos^2 \phi . \alpha_{\parallel}^A \alpha_{\parallel}^B \right) . \left( \frac{\cos kR}{R^3} + \frac{k\sin kR}{R^2} \right) - \sin^2 \phi . \alpha_{\perp}^A \alpha_{\perp}^B \left( \frac{k^2 \cos kR}{R} \right) \right] \cos(\mathbf{k} \cdot \mathbf{R})$$
(3.2)

In the short-range region  $(kR \ll 1)$  the leading term of equation (3.2),  $\Delta E^0$ , is found by taking the leading terms in the Taylor series expansions of sin *kR*, cos *kR* and cos (**k.R**) to give;

$$\Delta E^{0}(R) = \frac{I}{4\pi\varepsilon_{0}^{2}cR^{3}} \left(\sin^{2}\phi.\alpha_{\perp}^{A}\alpha_{\perp}^{B} - 2\cos^{2}\phi.\alpha_{\parallel}^{A}\alpha_{\parallel}^{B}\right) \quad .$$
(3.3)

On isotropically averaging the system with respect to the incoming light, the energy-shift of equation (3.3) is written as;

$$\Delta E^{0}(R) = \frac{I}{6\pi\varepsilon_{0}^{2}cR^{3}} \left(\alpha_{\perp}^{A}\alpha_{\perp}^{B} - \alpha_{\parallel}^{A}\alpha_{\parallel}^{B}\right) \quad .$$

$$(3.4)$$

The result (3.4) vanishes if  $\alpha_{\perp}^{A} \alpha_{\perp}^{B} = \alpha_{\parallel}^{A} \alpha_{\parallel}^{B}$  (i.e. if the molecules are spherically symmetric); otherwise it is non-zero and its sign signifies a force that is either attractive or repulsive, as determined by the relative magnitudes of the polarizability components.

The van der Waals dimer  $(HCN)_2$  is one widely-known example of such a molecular system. The intermolecular bond is well modeled by the Stockmayer potential;<sup>34, 35</sup>

$$U(\mathbf{R}, \boldsymbol{\mu}^{A}, \boldsymbol{\mu}^{B}) = 4\varepsilon \left[ \left( \sigma / R \right)^{12} - \left( \sigma / R \right)^{6} \right] + \boldsymbol{\mu}^{A} \cdot \boldsymbol{\mu}^{B} / 4\pi\varepsilon_{0} R^{3} - 3 \left( \boldsymbol{\mu}^{A} \cdot \mathbf{R} \right) \left( \boldsymbol{\mu}^{B} \cdot \mathbf{R} \right) / 4\pi\varepsilon_{0} R^{5}$$
(3.5)

where *R* is the intermolecular separation,  $\sigma$  is the usual Lennard-Jones parameter,  $\varepsilon$  is the well-depth and the  $\mu$  terms are dipole moments. The effect of intense throughput laser radiation is to introduce a laser-induced energy shift which can be included in an effective potential, writing;

$$U(R) + \Delta E^{0}(R) = U(R) + K/R^{3} \quad , \tag{3.6}$$

where, from eqn (3.4),  $K = I\left(\alpha_{\perp}^{A}\alpha_{\perp}^{B} - \alpha_{\parallel}^{A}\alpha_{\parallel}^{B}\right)/6\pi\varepsilon_{0}^{2}c$ . The modification to the potential energy surface changes the equilibrium position of the bond, relating to a contraction or expansion – depending on the attractive or repulsive nature, respectively, of the laser-induced energy shift. Differentiating eqn (3.6) with respect to *R* gives the following at the new equilibrium position  $R'_{0} = R_{0} + \delta R_{0}$ ;

$$U'(R_0 + \delta R_0) - 3K / (R_0 + \delta R_0)^4 = 0 \quad . \tag{3.7}$$

Taking the leading term in Taylor series expansions of both terms in the above equation leads to an expression for  $\delta R_0$  as follows;

$$\delta R_0 = \frac{3K}{R_0^4 U''(R_0)} \quad . \tag{3.8}$$

Differentiating eqn (3.5) twice with respect to *R* gives the following expression for the change in equilibrium bond length;

$$\delta R_{0} = \frac{\pi I(k) (\alpha_{\perp}^{\prime 2} - \alpha_{\parallel}^{\prime 2}) R/9c}{\varepsilon \left[ 26 \,\sigma^{12}/R^{9} - 7 \,\sigma^{6}/R^{3} \right] - \left|\mu\right|^{2} / 4\pi\varepsilon_{0}} \quad , \tag{3.9}$$

recognizing that  $\alpha^{A} = \alpha^{B} = \alpha$  and  $\mu^{A} = \mu^{B} = \mu$ . In the above,  $\alpha'$  refers to volume polarizabilities ( $\alpha$  scaled by  $1/4\pi\epsilon_{0}$ ).

The  $(HCN)_2$  dimer is a particularly suitable example of a van der Waals molecule. Its centre of mass lies 0.605 Å from the central H atom, along the intermolecular bond. From the moment of inertia *I* about the centre of mass, the rotational constant *B* of the dimer can be calculated from;

$$B = h/8\pi^2 Ic$$
 , (3.10)

with a reported value<sup>36</sup> of 0.0584 cm<sup>-1</sup>. The change in equilibrium bond length induced by the laser field will modify the moment of inertia and hence the rotational constant of the dimer. Substituting data from previous studies<sup>35-37</sup> into eqn (3.9), it is readily determined that an irradiance of  $10^{16}$  W m<sup>-2</sup> will cause the dimer bond to extend by 1.72 pm. It is important to note that, despite this bond length being measured between the centers of each molecule, the linear expansion will be almost entirely operative through extension of the N-H hydrogen bond. [The principle of laserinduced bond extension could be applied to individual bonds in either HCN molecule, but the polarizability of each HCN molecule is much larger than that of any individual atomic component; also the N-H intermolecular bond has a much lower force constant than the intramolecular bonds.] The change in equilibrium bond length can be applied to eqn (3.10), giving a new rotational constant of  $0.0579 \text{ cm}^{-1}$  – a difference of about 1%. This is experimentally very significant, well above the bounds of error in microwave spectroscopic measurements. Taking account of the distribution of intensity across a typical laser beam, it is clear that the effect would be manifest in a broadening as well as a shift in spectral lines.

#### **3.2 Molecular Solids**

To apply the theory we consider a regular solid comprising close-packed, electrically neutral quasi-linear molecules. Focusing on one neighboring pair of molecules in detail, we consider specifically a pair of parallel, cylindrically symmetric molecules with a mutual separation vector **R** orthogonal to their 'long' molecular axes. Identifying **R** with the Z-axis and the molecular axis with the X-direction, and assuming the system is irradiated with plane-polarized light, we define the polarization vector of throughput radiation in cylindrical coordinates as  $\mathbf{e} = \sin \phi \cos \theta \, \hat{\mathbf{i}} + \sin \phi \sin \theta \, \hat{\mathbf{j}} + \cos \phi \, \hat{\mathbf{k}}$ , where  $\phi$  and  $\theta$  are the angles made by **e** with **R** and the molecular axis, respectively. From (5), the laser-induced energy shift experienced by this pair is;

$$\Delta E(R) = \frac{I}{\varepsilon_0 c} \operatorname{Re} \left\{ \sin^2 \phi \cos^2 \theta \, \alpha_{XX}^A V_{XX} \alpha_{XX}^B + \sin^2 \phi \sin^2 \theta \alpha_{YY}^A V_{YY} \alpha_{YY}^B + \cos^2 \phi \, \alpha_{ZZ}^A V_{ZZ} \alpha_{ZZ}^B \right\} \cos(\mathbf{k} \cdot \mathbf{R})$$
(3.11)

On differentiating (3.11) with respect to distance, after taking the leading terms in the Taylor series expansions of cos kR, sin kR and cos **k.R** (effecting a correction to the result given in ref. 21) we obtain the following expression for the force induced between the particles,  $\mathbf{F}_{ind} = -\partial \Delta E_{ind} / \partial \mathbf{R}$ ;

$$\mathbf{F}_{ind}\left(R\right) = \frac{3I}{4\pi\varepsilon_{0}^{2}cR^{4}} \left[\alpha_{\perp}^{A}\alpha_{\perp}^{B}\left(\sin^{2}\phi\left(2+\sin^{2}\theta\right)-2\right) + \alpha_{\parallel}^{A}\alpha_{\parallel}^{B}\sin^{2}\phi\cos^{2}\theta\right],\tag{3.12}$$

where  $\alpha_{\perp} = \alpha_{YY} = \alpha_{ZZ}$ ,  $\alpha_{\parallel} = \alpha_{XX}$ . This is effectively the *only* mechanically operative pair force, since other interparticle forces in the solid are balanced at equilibrium. It is instructive to consider special geometric cases.

#### Parallel pair

The following results emerge for cases in which the polarization vector of the incident light is: (*i*) parallel to the molecular axis; (*ii*) parallel to the separation vector, (*iii*) orthogonal to both;

$$\mathbf{F}_{ind}\left(R\right) = \begin{cases} \frac{3I\left(\alpha_{\parallel}^{A}\alpha_{\parallel}^{B}\right)}{4\pi\varepsilon_{0}^{2}cR^{4}}, & (i) \ (\phi = \pi/2, \ \theta = 0) \\ -\frac{3I\left(\alpha_{\perp}^{A}\alpha_{\perp}^{B}\right)}{2\pi\varepsilon_{0}^{2}cR^{4}}, & (ii) \ (\phi = 0, \ \theta = \pi/2) \\ \frac{3I\left(\alpha_{\perp}^{A}\alpha_{\perp}^{B}\right)}{4\pi\varepsilon_{0}^{2}cR^{4}}, & (iii) \ (\phi = 0, \ \theta = 0) \end{cases}$$
(3.13)

The positive sign for results (*i*) and (*iii*) signifies a repulsion tending to increase the pair separation, leading to expansion; in case (*ii*) the attractive force will generate a contraction. The strengths of the forces depends on the magnitudes of  $\alpha_{\parallel}^{\xi}$  and  $\alpha_{\perp}^{\xi}$ , and for electronically prolate molecules, ( $\alpha_{\parallel}^{\xi} > \alpha_{\perp}^{\xi}$ ), the repulsion (*i*) is the largest force.

#### End-to-end pair

The above results account for only two dimensions of molecular packing in these anisotropic solids; it is also necessary to consider the forces on a pair of adjacent particles placed end-to-end. Again the results differ according to whether the polarization vector of the incident radiation is: (v) parallel to, or (vi) orthogonal to the intermolecular separation vector. Explicitly, the ensuing forces are as follows;

$$\mathbf{F}_{ind}^{0}\left(R\right) = \begin{cases} -\frac{3I\left(\alpha_{\parallel}^{A}\alpha_{\parallel}^{B}\right)}{2\pi\varepsilon_{0}^{2}cR^{4}}, & (v)\left(\mathbf{e} \parallel \mathbf{R}\right) \\ \frac{3I\left(\alpha_{\perp}^{A}\alpha_{\perp}^{B}\right)}{4\pi\varepsilon_{0}^{2}cR^{4}}, & (vi)\left(\mathbf{e} \perp \mathbf{R}\right) \end{cases}$$
(3.14)

Thus, irradiating such a solid with plane-polarized light effects a contraction in the direction of the solid parallel to the polarization of the laser beam, and an expansion in the other two orthogonal dimensions, both linearly dependent on the irradiance of the laser.

In summary, a compression parallel to  $\mathbf{e}$  together with an expansion in directions perpendicular to  $\mathbf{e}$  produces a solid deformation characterized by an overall increase in volume that scales linearly with the irradiance *I*. This in turn signifies a change in the local density – and hence in the local refractive index – that can also be expected to scale linearly with *I*. Optical electrostriction thus leads to an optomechanically induced intensity-dependence in the refractive index.

#### 4. DISCUSSION

Detection of the process of optical electrostriction is fraught with experimental difficulty, and this is undoubtedly why it has not been characterized before. Such difficulties should not prove insurmountable, but they need to be taken into account in planning practicable experiments. Because the effect of interest leads to optical changes, there is an obvious temptation to seek an optical proof. However it is clear that the optical electrostrictive effect, in solids, will usually be dominated by much more widely known electronic mechanisms such as the optical Kerr effect<sup>38</sup> – and, in absorbing regions, other photothermal effects due to spatially inhomogeneous heating. Intriguingly, electrostriction was indeed considered in connection with an intensity-dependent refractive index in the early days of laser physics,<sup>39</sup> but it subsequently emerged that other mechanisms play a more direct and significant role.

With the problems envisaged with optical means of detecting this effect, consideration of mechanical methods may be met with more success. As seen in the previous section, the relatively modest change in inter-particle separation is magnified when considering a molecular solid transparent to the applied radiation field. Although the induced force and corresponding separation modification will be limited orthogonal to the propagation direction due to the width of the laser beam, if the radiation field propagates along the length of the solid, a much greater effect can be expected. This will result in an expansion of the material parallel to the propagation direction of the beam, since this is necessarily perpendicular to its polarization. A system that seems particularly suited to measure small changes in size is one recently decribed<sup>40</sup> – the pertinent part being two mirrors set up opposite each other, of known separation such that a light wave propagating between the two has a known interference pattern. In their system the activation of a mechanical switch causes the position of one of the mirrors to shift slightly, altering the interference pattern. If instead the mirror were attached to a thin rod of material transparent to a given laser frequency, an intense laser pulse along the length of this rod would cause it to expand, altering the position of the mirror resulting in the modification of the interference pattern, the detection and quantification of which would allow the optical electrostriction effect to be detailed.

Although we have focused on the intrinsic interest of the subject, it is worth considering the applicability of this effect to optomechanical devices. In the context of dramatically accelerating developments in the field of nanoelectromechanical systems, any mechanism that can reproducibly deliver a reversible and ultrafast mechanical

response, actuated by light, appears to be of considerable merit. It is hoped the mechanism described herein will provide many opportunities and challenges in this burgeoning field.

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