

1 **eLS A26071**

## 2 **Supercoiled DNA: Structure**

3 Richard Peter Bowater, University of East Anglia, Norwich, UK

4

5 Based in part on the previous version of this eLS article 'Supercoiled DNA: Structure' (2005)

6

### 7 **Advanced Article**

8 **(Advanced articles are aimed at advanced undergraduates, graduate students, postgraduates,**  
9 **and researchers reading outside their field of expertise.)**

## 10 **Abstract**

11 Supercoiling is introduced into DNA molecules when the double helix is twisted around its  
12 own axis in three-dimensional space. Experimental techniques that are sensitive to  
13 molecular shape can be used to analyse the topological states of DNA, but the approaches  
14 used most successfully are high-speed centrifugation, high-resolution microscopy and gel  
15 electrophoresis. Generally, DNA molecules are negatively supercoiled inside cells, although  
16 the level of supercoiling is not equal throughout the genome and many supercoils may be  
17 constrained by bound proteins. Supercoiling increases the free energy of DNA and  
18 influences DNA metabolism by promoting or hindering specific enzymatic processes. DNA  
19 topoisomerases are the main enzymes that regulate DNA topology and several different  
20 types of enzymes are present in all cells.

21 **Keywords:** DNA; linking number; supercoiling; topology; twist; writhe

22

## 23 **Key Concepts**

- 24 • Double stranded DNA helices can wind in three-dimensional space to form further  
25 helices of higher order, forming *supercoiled* DNA.
- 26 • Since the early 1960s the importance of DNA supercoiling to cellular processes has  
27 been apparent, with its most obvious consequence being that it aids compaction of  
28 large DNA molecules into the relatively small volume of cells.
- 29 • The extent of supercoiling in a DNA molecule is influenced by environmental  
30 conditions, such as ionic strength and temperature; since supercoiling of DNA  
31 influences the biological pathways in which it is involved, the level of DNA  
32 supercoiling inside cells is tightly regulated.
- 33 • Supercoiling provides a significant amount of free energy to DNA molecules and,  
34 inside cells, this can be used to drive structural transitions and other metabolic  
35 processes that would normally be thermodynamically unfavourable, such as opening  
36 of the DNA helix during replication and transcription.

- 1 • Mathematical and modelling studies have provided insight for quantitative analyses  
2 of DNA supercoiling, leading to definitions for *twist*, which describes how the  
3 individual strands of DNA coil around its axis, and *writhe*, which describes how the  
4 helix axis coils in three-dimensional space.
- 5 • DNA inside cells contains supercoils of two types: interwound, which is when circular  
6 DNA winds around its own axis; toroidal supercoiling occurs when the DNA helix  
7 forms a series of spirals around an imaginary ring.
- 8 • Any technique that is sensitive to molecular shape will be useful for experimental  
9 analysis of supercoiled DNA, but the large size of the molecules mean few  
10 techniques have been used successfully; those that have been widely used include  
11 high-speed centrifugation, high-resolution microscopy (e.g. electron microscopy and  
12 scanning-force microscopy) and agarose gel electrophoresis.
- 13 • A wide variety of proteins that bind to DNA alter the local geometry of its helix and  
14 influence DNA topology; an important characterised example of this effect is the  
15 winding of DNA around the eukaryotic histone octamer to form the nucleosome.
- 16 • A fundamental feature of closed domains of DNA, such as a circular molecule, is that  
17 the two strands of DNA are topologically linked and strand separation can be  
18 achieved only by breakage of one of the strands; the main enzymes that regulate  
19 DNA topology are DNA topoisomerases and they may act to remove or introduce  
20 negative supercoils or they may remove both positive and negative supercoils.
- 21 • Cellular processes that move macromolecular assemblies along DNA may generate  
22 localized DNA supercoiling since, as the large protein complex moves along the  
23 DNA, its rotation around the DNA may be inhibited.

24

25

## Introduction

26 Normally, DNA occurs as a helical, double-stranded molecule in which the two strands pair  
27 up in antiparallel fashion; this is the classical B-type helical structure first solved in 1953 by  
28 Watson and Crick (Watson and Crick, 1953) using a range of experimental data obtained by  
29 many other scientists (Chargaff *et al*, 1950; Franklin and Gosling, 1953; Wilkins *et al*, 1953).  
30 The DNA helix is usually visualized in a linear form, but, frequently, the helix axis is curved  
31 and numerous 'unusual DNA structures' form under specific sequence and environmental  
32 conditions. See also: DNA Structure, DOI: 10.1002/9780470015902.a0006002.pub2; DNA  
33 Structure: A-, B- and Z-DNA Helix Families, DOI: 10.1038/npg.els.0003122; DNA Structure:  
34 Sequence Effects, DOI: 10.1002/9780470015902.a0002976.pub2; Non-B DNA Structure  
35 and Mutations Causing Human Genetic Disease, DOI: 10.1002/9780470015902.a0022657;  
36 Crick, Francis Harry Compton, DOI: 10.1038/npg.els.0002392; Watson, James Dewey, DOI:

1 10.1038/npg.els.0002445; Franklin, Rosalind Elsie, DOI: 10.1038/npg.els.0003559; Wilkins,  
2 Maurice Hugh Frederick, DOI: 10.1038/npg.els.0002954.

3 Notably, since the B-form of DNA is a configuration of minimum energy, any bending or  
4 twisting of the DNA molecule will increase its free energy. In addition to varying secondary  
5 structures, the DNA helix can wind in three-dimensional space to form further helices of  
6 higher order. DNA in this conformation is termed supercoiled and changes to this tertiary  
7 structure of a DNA molecule have dramatic consequences for the free energy and biology of  
8 the molecule. See also: Nucleic Acids: General Properties, DOI: 10.1038/npg.els.0001335;  
9 DNA Topology: Fundamentals, DOI: 10.1038/npg.els.0001038; DNA Topology: Supercoiling  
10 and Linking, DOI: 10.1038/npg.els.0003904.

11 In a linear double-stranded DNA molecule, the two strands of the helix are free to rotate  
12 around each other and, indeed, may unwind completely to give two separate strands.  
13 Complete separation is unlikely to happen inside cells because of the large number of base  
14 pairs contained within genomic DNA. Complete separation of the DNA helix may also be  
15 prevented because the molecule may exist within closed domains, for example by covalent  
16 joining of the DNA strands to give a circular molecule. The binding of proteins may also  
17 separate the DNA molecule into different domains, particularly if a loop of DNA is formed  
18 due to the same protein complex binding at two distinct sites on the DNA. A fundamental  
19 feature of closed domains in DNA is that the strands are topologically linked and strand  
20 separation can be achieved only by breakage of one of the strands. Unlike the open-ended  
21 DNA molecule, within closed domains of DNA the three-dimensional conformation of any  
22 base pair cannot be changed without influencing the structure of the remainder of the  
23 domain.

24 Studies of topological isoforms (topoisomers) of DNA began during the early 1960s with the  
25 demonstration that polyomavirus DNA was consistently isolated in linear and closed-circular  
26 forms. When Vinograd's laboratory showed that DNA extracted from cells was negatively  
27 supercoiled, the importance of DNA supercoiling to cellular processes became apparent  
28 (Lebowitz, 1990). Supercoiling of DNA has dramatic consequences for the biological  
29 pathways in which it is involved and, thus, the level of DNA supercoiling inside cells is tightly  
30 regulated.

## 31 **Definition of Supercoiling**

32 Quantitative measurements and analyses of DNA supercoiling have been defined.  
33 Mathematical studies have provided enormous insight for these definitions and are

1 discussed in more detail in other reviews and monographs (Bates and Maxwell, 2005; Bauer  
2 *et al*, 1980; Benham and Mielke, 2005; Schlick, 1995). The basic ideas are described below  
3 (Table [1](#)) in relation to covalently closed-circular DNA (cccDNA) molecules, but similar  
4 principles apply to any closed domain of DNA. See also: DNA Topology: Fundamentals,  
5 DOI: 10.1038/npg.els.0001038; DNA Topology: Supercoiling and Linking, DOI:  
6 10.1038/npg.els.0003904.

7 [<Table 1 near here>](#)

8 Linear double-stranded DNA molecules can be closed into a circle by the formation of 5'–3'  
9 phosphodiester bonds to seal each strand. Due to the helical nature of the DNA backbone,  
10 after circularization the two strands of the helix cannot be separated without breaking one of  
11 them; the backbone strands are linked topologically. The number of links between the  
12 strands corresponds to the number of double-helical turns (twists) in the original DNA  
13 molecule (Figure [1](#)). Upon circularization, this number must be an integer and is known as  
14 the linking number of the cccDNA molecule, abbreviated as *Lk*. (Note that earlier literature  
15 refers to the topological winding number of DNA,  $\alpha$ , which is identical to *Lk*. Previously this  
16 term has also been abbreviated to *L*.) *Lk* is a topological property of cccDNA that does not  
17 depend on its particular conformation.

18 [<Figure 1 near here>](#)

19 Linking number is a fundamental property of any two closed curves in three-dimensional  
20 space and is equal to the number of times that one strand intersects the plane of the other.  
21 An intersection may act to increase or decrease the number of links between the two  
22 strands. By convention, positive values are given to links arising from forming a closed circle  
23 with a completely right-handed double helix (such as B-DNA). Consequently, links with a  
24 negative value arise from the formation of a cccDNA molecule from a left-handed DNA helix  
25 (such as Z-DNA). The overall *Lk* of a DNA molecule is equal to the sum of the sign-  
26 dependent intersections.

27 A given length of DNA has an inherent number of double-helical turns, which is equivalent to  
28 the length of the DNA (defined as *N* base pairs) divided by the number of base pairs per turn  
29 of the helix (defined as *h*). Values of *h* depend upon environmental conditions and  
30 sequence, but an average value is specified from standard conditions and is usually taken to  
31 be 10.5 bp per turn for B-DNA. The linking number corresponding to an unconstrained state  
32 is termed  $Lk^0$  and, for any DNA:

33 •  $Lk^0 = N/h$  (1)

1 Since  $N/h$  need not necessarily be an integer,  $Lk^0$  is not a true linking number (it is  
2 sometimes called the 'hypothetical linking number'). For DNA with  $N/h$  that is not an integer,  
3 some deformation of the molecule's conformation will be required to line up the strands to  
4 allow their closure into a circle, which leads to torsional stress within the cccDNA. In this  
5 situation, the most unconstrained DNA circle is referred to as the relaxed topoisomer,  
6 defined  $Lk_m$ . Note that, if  $N/h$  is an integer, when the linear DNA is bent to form a simple,  
7 planar circle, the strands will line up precisely and  $Lk = Lk^0 = Lk_m$ .

8 It is also possible to add or remove turns to the DNA helix before it is closed into a circle,  
9 leading to the molecule having  $Lk$  that deviates from  $Lk_m$  (Figure 1). Since the average  
10 conformation of DNA (B-type helix) is defined to have positive  $Lk$ , twisting up of the helix  
11 before closure leads to an increase in linking number above  $Lk_m$  and is defined as positive  
12 supercoiling. Analogously, unwinding of the helix before closure is defined as negative  
13 supercoiling. DNA molecules with positive and negative supercoiling may also be referred to  
14 as helices that are over- or underwound, respectively. Note that an underwound helix has an  
15 increased value of  $h$ .

16 It is clear that  $Lk$  is related to the number of turns of the helix, but these two parameters are  
17 not equivalent. This can be shown using mathematical analysis, which defines supercoiling  
18 in the form of topological and geometric parameters.  $Lk$  is a topological property and its  
19 value can only be applied to the complete DNA molecule. The twist ( $Tw$ ) of DNA is a  
20 geometric parameter and its values have importance for local regions of the molecule;  
21 indeed, the value of  $Tw$  of the whole molecule is equal to the sum of individual sections of  
22 the molecule. There is a geometrical significance to any difference between  $Lk$  and  $Tw$  and  
23 this is named the writhe ( $Wr$ ) of the molecule.

24 In terms of cccDNA,  $Tw$  and  $Wr$  are complementary geometric parameters, and each may  
25 be defined and described (Table 1):  $Tw$  describes how the individual strands of DNA coil  
26 around the axis of the DNA helix and  $Wr$  describes how the helix axis coils in space. Both  
27 are complex geometric functions whose values need not be an integer. The important finding  
28 in relation to studies of DNA supercoiling is that:

29 •  $Lk = Tw + Wr$  (2)

30 The main consequence of this equation is that because  $Lk$  is invariant for a given cccDNA,  
31 any change in  $Tw$  of the molecule must be accompanied by an equal and opposite change in  
32  $Wr$ , and vice versa.

1 Supercoiling of DNA can occur in two forms that produce different overall shapes for the  
2 molecule. Circular DNA that winds around itself, as shown in Figure 1, is called interwound  
3 (also referred to as plectonemic supercoils) and purified cccDNA in solution usually has this  
4 type of supercoiling (Benham and Mielke, 2005). Note that the sense of interwinding is right-  
5 handed in the case of negatively supercoiled DNA. Supercoiling can also be achieved if the  
6 DNA helix forms a series of spirals around an imaginary ring, taking a shape similar to a  
7 telephone flex. This kind of supercoiling is known as toroidal (Hud and Vilfan, 2005; Schlick,  
8 1995). It corresponds most closely to the term 'superhelix' since a left-handed untwisting of  
9 the DNA helix (i.e. negative supercoiling) is manifested as a left-handed helix of higher order  
10 wound around the torus. Toroidal supercoiling is formed when DNA is wrapped around  
11 proteins, as in nucleosomes (Luger and Richmond, 1998; Richmond and Davey, 2003). In  
12 reality, DNA inside cells contains supercoils of both interwound and toroidal geometries. See  
13 also: Cell Biophysics, DOI: 10.1038/npg.els.0001271; DNA Topology: Fundamentals, DOI:  
14 10.1038/npg.els.0001038; DNA Topology: Supercoiling and Linking, DOI:  
15 10.1038/npg.els.0003904.

## 16 Specific Linking Difference, Superhelical 17 Density

18 Changes in  $Lk$  of a DNA produce alterations to the level of supercoiling of the molecule. The  
19 change in linking number from  $Lk_m$  is a measurement of the extent of supercoiling of the  
20 molecule and is termed the linking difference of the DNA, or  $\Delta Lk$ . The addition of turns to the  
21 DNA helix (positive supercoiling) leads to an increase in  $Lk$  over  $Lk_m$ , giving a positive  $\Delta Lk$ .  
22 Conversely, the removal of turns from the DNA helix (negative supercoiling) gives a value of  
23  $Lk$  lower than  $Lk_m$ , giving a negative  $\Delta Lk$ .

24 If  $Lk_m$  is not equal to  $Lk^0$ , the 'relaxed' topoisomer will contain a small amount of torsional  
25 strain, which should really be counted towards the total supercoiling of the DNA. Thus, an  
26 exact definition of  $\Delta Lk$  is:

27 •  $\Delta Lk = Lk - Lk^0$  (3)

28 Furthermore, since changes in  $Lk$  produce corresponding changes in  $Tw$  and/or  $Wr$ ,

29 •  $\Delta Lk = \Delta Wr + \Delta Tw$  (4)

30 Specific values of  $\Delta Lk$  produce more torsional stress in small DNA molecules than in large  
31 ones because they comprise a larger proportion of the overall  $Lk$ . To allow comparison of the

1 degree of supercoiling in molecules of different sizes, it is useful to normalize measurements  
2 of supercoiling to give the specific linking difference ( $\sigma$ ); frequently, this is referred to as  
3 superhelical density (Muskhelishvili and Travers, 2003). Since cccDNA molecules of  $Lk^0$  do  
4 not contain supercoils, this serves as a good reference point for such normalization:

5 • 
$$\sigma = \frac{Lk - Lk^0}{Lk^0} = \frac{\Delta Lk}{Lk^0} \quad (5)$$

6 The specific linking difference allows meaningful comparison between DNA molecules. For  
7 example, natural cccDNA molecules, such as bacterial plasmids, vary widely in size, but,  
8 when isolated *in vitro*, the majority have values for  $\sigma$  of  $-0.05$  to  $-0.06$ .

## 9 Energetics of Supercoiled DNA

10 Like all molecules, DNA will assume a configuration of minimum energy, and this is usually a  
11 helix of the B-form. Upon bending or twisting of the molecule, its energy is increased. For a  
12 cccDNA with a surplus or deficit in  $Lk$ , conformational modifications introduce specific  
13 changes to the free energy of the molecule. For example, to accommodate the same length  
14 of DNA in fewer helical turns, the double helix must be untwisted, leading to a substantial  
15 increase in the deformation energy of the molecule. By taking an appropriate writhed  
16 configuration, the cccDNA minimizes the amount by which it departs from the B configuration  
17 and reduces its deformation energy. On the other hand, writhing always introduces some  
18 curvature, and so it increases the bending contribution to the energy of the molecule. Since  
19  $Wr$  and  $Tw$  are interconvertible, it is apparent that the underwound DNA molecule will  
20 assume a configuration that optimizes twist while introducing the smallest possible amount  
21 of bending (Benham and Mielke, 2005; Vologodskii and Cozzarelli, 1994a).

22 Experimental studies during the 1970s established that the free energy of a supercoiled DNA  
23 sample ( $\Delta G_{sc}$ ) has a quadratic dependence on  $\Delta Lk$ :

24 • 
$$\Delta G_{sc} = K \cdot \Delta Lk^2 \quad (6)$$

25 where  $K$  is a DNA length-dependent constant. Thus, samples of cccDNA exist in a normal  
26 (Gaussian) distribution of topoisomers (i.e. molecules have a continuous, symmetrical  
27 distribution of  $Lk$  around the most intensely populated topoisomer – see Figure 2).

28 Theoretical simulations suggest it is likely that  $\Delta G_{sc}$  varies with ionic conditions and, in fact, it  
29 may not be a quadratic function of  $\Delta Lk$  under all conditions (Schlick, 1995; Vologodskii and  
30 Cozzarelli, 1994a). The influence of environmental conditions on DNA supercoiling is due, at

1 least in part, to the fact that ionic strength and temperature alter  $T_w$  of double-helical DNA.  
2 Effects of ionic environment on the three-dimensional structure of DNA are to be expected  
3 because DNA is a polyelectrolyte with a net negative charge at every nucleotide residue.

4 <Figure 2 near here>

5 The free energy of supercoiling can be normalized to circle size in the same manner as  
6 described for  $\Delta Lk$ . Hence:

7 • 
$$\Delta G_{sc}/N = NK(\Delta Lk/N)^2 \quad (7)$$

8 For DNA circles of 3–10 kb, it was shown that  $NK$  is independent of DNA circle size, and that  
9  $NK \approx 1100RT$ , where  $R$  is the gas constant and  $T$  is the temperature. Since  $\Delta Lk/N$  is  
10 proportional to  $\sigma$ , the free energy of supercoiling per base pair is proportional to  $\sigma^2$ , and is  
11 independent of circle size. Studies with small DNA molecules showed that  $NK$  increases  
12 gradually with decreasing DNA size, with a value of about  $4000RT$  for a 300-bp circle. The  
13 interpretation of this finding was that, for small molecules, writhing of the DNA becomes  
14 increasingly unfavourable relative to twisting. Due to these energy considerations, it is  
15 thought that a higher proportion of supercoiling is partitioned into twisting rather than writhing  
16 for small DNA circles.

17

## 18 Intercalation

19 Intercalators contain a planar, usually polycyclic, aromatic ring structure, which allows them  
20 to insert between two base pairs of a double-stranded DNA helix. The best-known examples  
21 of intercalating molecules are chloroquine and ethidium bromide (EtdBr) (Wu *et al*, 1988).  
22 While these molecules bind similarly to most DNA sequences, other intercalators prefer to  
23 bind to specific sequences. For example, actinomycin D binds most avidly between  
24 neighbouring G–C base pairs. A consequence of intercalators binding to DNA is that they  
25 will increase the distance between the adjacent base pairs. This causes a local unwinding of  
26 the DNA helix, resulting in an overall increase in the helical repeat and a decrease in  $T_w$ . For  
27 a closed domain of DNA, this will produce a corresponding increase in  $W_r$ .

28 Intercalators have been of enormous value in the experimental measurements of plasmid  
29 supercoiling (Liu and Wang, 1975; Wang, 1974). EtdBr exhibits a large increase in  
30 fluorescence upon binding to DNA, making it particularly useful to molecular biologists  
31 through its use as a stain for DNA. Furthermore, as outlined in Figure 2, this intercalator has  
32 been widely used during the preparation of topoisomers at different levels of supercoiling



1 and in agarose gel electrophoresis analysis of *Lk* (Bowater *et al*, 1992). See also: Staining,  
2 Viewing and Photography of Gels and Estimation of Fragment Sizes, DOI:  
3 10.1038/npg.els.0003777.

4 Intercalation of one molecule of EtdBr to DNA causes a local unwinding of adjacent base  
5 pairs of 26°. Some classes of intercalator affect the helix in the opposite manner, leading to  
6 a localized increase in the twist of the helix. The best-characterized example of such a  
7 molecule is netropsin, which binds to the minor groove of AT-rich DNA and increases  
8 winding of the helix by approximately 9° for each molecule bound (Schlick and Olson, 1992).

## 9 **Assays**

10 In principle, any technique that is sensitive to molecular shape will be useful for experimental  
11 analysis of supercoiled DNA. However, because of the large size of these molecules, few  
12 techniques have been used successfully to provide direct structural information.

13 Of central importance to the discovery and initial characterization of supercoiled DNA was  
14 the use of high-speed centrifugation (Lebowitz, 1990). The sedimentation velocity and  
15 buoyant density of polyoma viral DNA was monitored after various treatments that induce  
16 strand separation or cleavage of the DNA helix. These experiments clearly identified that  
17 DNA molecules could exist in a variety of forms that differed only by their shape, and the  
18 concept of supercoiled DNA was founded.

19 High-resolution microscopy provides explicit analysis of molecular structure and electron  
20 microscopy (EM), cryo-EM and scanning-force microscopy have been used to analyse  
21 supercoiled forms of DNA (Vologodskii and Cozzarelli, 1994a). Each of these techniques  
22 has confirmed that supercoiled DNA has a compact shape and that the interwound form  
23 predominates in naked DNA. Moreover, high-resolution microscopy clearly shows that  
24 supercoiled DNA is often branched and that its conformational and thermodynamic  
25 properties depend on ionic conditions (Vologodskii and Cozzarelli, 1994a).

26 The other main technique that has been used to analyse DNA supercoiling is agarose gel  
27 electrophoresis. Smaller and/or more compact molecules migrate more rapidly during  
28 electrophoresis and, thus, DNA molecules that are linear, nicked circles or supercoiled  
29 circles can be separated (Figure 2) (Bowater *et al*, 1992; Keller, 1975). Compared with high-  
30 speed centrifugation, this technique provides a higher resolution for distinction between  
31 molecules with different shape and it is cheaper and easier to use. Incorporation of  
32 intercalators into electrophoresis running buffers allows topoisomers of high  $\sigma$  to be resolved

1 (Figure 2a,b) and their exploitation in two-dimensional gel electrophoresis allows a wide  
2 range of topoisomers to be analysed on a single gel (Figure 2c) (Bowater *et al*, 1992). See  
3 also: Gel Electrophoresis, DOI: 10.1002/9780470015902.a0005335.pub2; Staining, Viewing  
4 and Photography of Gels and Estimation of Fragment Sizes, DOI: 10.1038/npg.els.0003777.

5 Other experimental techniques have been used to provide less direct information about the  
6 structure of supercoiled DNA, including a variety of spectroscopic methods (circular  
7 dichroism, static and dynamic light scattering) (Lilley and Dahlberg, 1992; Vologodskii and  
8 Cozzarelli, 1994a). Utilization of complementary techniques, particularly in combination with  
9 theoretical methods, has provided significant information on the three-dimensional structure  
10 of supercoiled DNA.

## 11 **Catenanes and Knots**

12 Knots and catenanes (Figure 3) occur frequently in DNA, primarily as a consequence of the  
13 complex biochemical reactions that take place within closed topological domains. These  
14 structures can influence processes occurring on the DNA molecule, such as replication and  
15 transcription, and they are also utilized as intermediates in some types of genetic  
16 recombination (Wasserman and Cozzarelli, 1986). See also: DNA Topology: Fundamentals,  
17 DOI: 10.1038/npg.els.0001038; DNA Topology: Supercoiling and Linking, DOI:  
18 10.1038/npg.els.0003904.

19 <Figure 3 near here>

20 Knots were first detected in DNA treated with topoisomerases *in vitro* (Wasserman and  
21 Cozzarelli, 1986). They have also been observed in native DNA, although they are not  
22 particularly common. Catenanes are more prevalent and are utilized in a number of diverse  
23 biological systems. Catenated molecules were first observed in mitochondrial DNA from  
24 human cells (Wasserman and Cozzarelli, 1986) and their most common occurrence is as  
25 intermediates during the replication of circular DNA.

26 Topological knots of a wide degree of complexity can be formed (Wasserman and  
27 Cozzarelli, 1986; Witz and Stasiak, 2010). Mathematical methods allow unique description of  
28 different knots and catenanes, although these descriptions become complex for highly  
29 knotted structures and for catenanes involving many loops. Theoretical analyses of these  
30 types of DNA conformations have been particularly valuable in the development of molecular  
31 models of supercoiled DNA (Benham and Mielke, 2005; Schlick, 1995; Vologodskii and  
32 Cozzarelli, 1994b).

# Protein Binding and DNA Topology

A wide variety of proteins that bind to DNA alter the local geometry of its helix and influence DNA topology. The best-known example of this effect is the winding of DNA around the eukaryotic histone octamer to form the nucleosome (Luger and Richmond, 1998; Richmond and Davey, 2003). Histone proteins are positively charged and have no enzymatic activity, but they allow extremely large DNAs to be compacted to fit within each eukaryotic cell. Each histone core envelops approximately 1.8 left-handed turns of DNA and stabilizes negative writhing within the complex. Supercoiling of this type is constrained because it is not available to influence the structure of the remainder of the DNA. See also: Chromosomes and Chromatin, DOI: 10.1002/9780470015902.a0005766.pub2; Chromosome Structure, DOI: 10.1002/9780470015902.a0001486.pub2; DNA Coiling and Unwinding, DOI: 10.1038/npg.els.0005967; Nucleosomes: Structure and Function, DOI: 10.1038/npg.els.0001155.

Prokaryotes do not contain histone proteins, but they do harbour proteins that influence DNA architecture. The two most abundant of these in the nucleoid of *Escherichia coli* are H-NS (H1) and HU (Drlica and Rouviere-Yaniv, 1987). These proteins constrain supercoils and have highly pleotropic effects, affecting genome stability, and recombination- and transcription-related events (Dillon and Dorman, 2010). Proteins that have more specific cellular functions also exhibit differential binding to DNA templates at various levels of supercoiling. Included among these are polypeptides that bind to specific DNA sequences, such as integration host factor (IHF), which is involved in site-specific recombination (Swinger and Rice, 2004), and factor for inversion stimulation (FIS), which influences transcription at certain promoters (Travers *et al*, 2001). Other proteins that bind to DNA independent of its sequence become abundant under specific growth conditions. For example, Dps is induced upon starvation of *E. coli* and is important for coordinating cellular responses to such stress (Chiancone and Ceci, 2010). See also: Chromosomes: Nonhistone Proteins, DOI: 10.1038/npg.els.0001158.

## Enzymatic Modulations of DNA Topology: Global and Local DNA Supercoiling

As a fundamental component of the three-dimensional structure of DNA, it is essential that cells regulate the overall amount of supercoiling that persists within chromatin – frequently referred to as the global level. The main enzymes involved in control mechanisms are the DNA topoisomerases, which can alter  $Lk$  of DNA (Schoeffler and Berger, 2008; Vos *et al*,

1 2011). General DNA topoisomerases function with little regard for DNA sequence. Additional  
2 enzymes that are involved in site-specific recombination reactions have considerable amino  
3 acid homology to some topoisomerases and have similar reaction mechanisms (Wasserman  
4 and Cozzarelli, 1986).

5 Topoisomerases with a wide variety of activities have been identified (Corbett and Berger,  
6 2004; Schoeffler and Berger, 2008): they may act to remove or introduce negative supercoils  
7 or they may remove both positive and negative supercoils. In some cases these topological  
8 changes are coupled to the hydrolysis of ATP, as is the case for DNA gyrase and reverse  
9 gyrase (Gubaev and Klostermeier, 2014; Lulchev and Klostermeier, 2014). DNA gyrases are  
10 well-characterised essential enzymes in bacteria that are able to add negative supercoils to  
11 DNA. By contrast, reverse gyrases are able to positively supercoil a circular DNA; these  
12 atypical topoisomerases are present in some hyperthermophilic organisms (Forterre *et al*,  
13 2007). See also: DNA Coiling and Unwinding, DOI: 10.1038/npg.els.0005967;  
14 Topoisomerases, DOI: 10.1038/npg.els.0001039.

15 Topoisomerases are classed as type I or II, according to the mechanism by which they  
16 produce topological changes of DNA (Schoeffler and Berger, 2008). Type I topoisomerases  
17 are further subdivided into two groups, types IA and IB, which exhibit dissimilar structures  
18 and distinct reaction characteristics. Type I enzymes transiently cleave one strand of the  
19 helix, pass the intact strand through and seal the break. Type II enzymes also make  
20 transient breaks in the helix, but they cleave both complementary strands of the molecule  
21 before passing another intact double-stranded molecule through the break. A consequence  
22 of these different reaction mechanisms is that type I enzymes change  $Lk$  in steps of 1,  
23 whereas type II enzymes change  $Lk$  in multiples of two.

24 Global DNA supercoiling varies for different cell types and growth conditions and DNA  
25 topoisomerases maintain levels within strict physiological boundaries (Baranello *et al*, 2012;  
26 Gilbert and Allan, 2014; Roca, 2011). Cellular processes that involve movement of  
27 macromolecular assemblies along DNA may also generate localized DNA supercoiling. As a  
28 large protein complex moves along the DNA, its rotation around the DNA may be inhibited  
29 (Liu and Wang, 1987). Instead, the DNA will rotate upon its axis, causing an increase in twist  
30 ahead of the complex and a reduction in twist behind; these twist changes are equivalent to  
31 positive and negative DNA supercoiling, respectively. This process is named 'twin domains  
32 of supercoiling', in recognition of the two regions of supercoiling that border the large protein  
33 complex. This phenomenon is best characterized for transcription (Figure 4), although it is  
34 also likely to occur during the action of DNA polymerases and DNA helicases. Such local  
35 topological changes *in vivo* have been shown to have a significant impact on the

1 conformation and function of important DNA sequence elements, such as promoters and  
2 DNA replication origins (Travers and Muskhelishvili, 2005; Wu and Fang, 2003).

3 <Figure 4 near here>

4 Since DNA strands are not broken during processes generating twin domains of  
5 supercoiling, there is no overall change of  $Lk$ . In a linear molecule such transient  
6 supercoiling will diffuse away and on a circular molecule the negative and positive supercoils  
7 will cancel out by diffusion around the circle. However, since chromatin is organized into  
8 discrete domains that are topologically independent, the diffusion of supercoils may be  
9 blocked and elevated levels of DNA supercoiling may build up (Gilbert and Allan, 2014). The  
10 relative orientation of neighbouring promoters may also influence the formation of  
11 transcription-induced supercoiling. For example, highly negatively supercoiled DNA may  
12 form between two divergent promoters that transcribe away from each other, whereas DNA  
13 that is between two convergent promoters may be positively supercoiled. DNA  
14 topoisomerases prevent increases in localized DNA supercoiling: in bacteria, negative and  
15 positive supercoils are removed by topoisomerase I and DNA gyrase, respectively (Corbett  
16 and Berger, 2004; Schoeffler and Berger, 2008). Inhibition of the activity of either of these  
17 enzymes, for example, by mutation, can lead to significant changes to cellular DNA topology  
18 (Hatfield and Benham, 2002; Wu and Fang, 2003). See also: DNA Coiling and Unwinding,  
19 DOI: 10.1038/npg.els.0005967; DNA Topology: Fundamentals, DOI:  
20 10.1038/npg.els.0001038; DNA Topology: Supercoiling and Linking, DOI:  
21 10.1038/npg.els.0003904; Topoisomerases, DOI: 10.1038/npg.els.0001039.

## 22 **Biological Functions**

23 The unconstrained  $\sigma$  of chromatin is believed to be about  $-0.02$  to  $-0.03$  in prokaryotic cells  
24 and is probably less negatively supercoiled in eukaryotes (Drlica, 1992). When localized  
25 variations to DNA topology are considered, it is clear that supercoiling provides a significant  
26 amount of free energy to DNA molecules inside cells. This increase in free energy can be  
27 used to drive structural transitions and other metabolic processes that would normally be  
28 thermodynamically unfavourable. For example, DNA can adopt a wide range of “unusual”  
29 structures that are different to the standard B-form helix, and many of these are more likely  
30 to form in molecules that negatively supercoiled (Kouzine and Levens, 2007). Importantly,  
31 some of these non-B-DNA structures have been linked with physiological consequences,  
32 including some types of human diseases. See also: Base Pairing in DNA: Unusual Patterns,  
33 DOI: 10.1038/npg.els.0003127; DNA Structure, DOI:

1 10.1002/9780470015902.a0006002.pub2; Non-B DNA Structure and Mutations Causing  
2 Human Genetic Disease, DOI: 10.1002/9780470015902.a0022657.

3 The most obvious consequence of DNA supercoiling is that it aids compaction of very large  
4 DNA molecules into the relatively small volume of cells. The most efficient form of length  
5 reduction arises from toroidal winding. Notably, size problems are particularly acute in  
6 eukaryotic cells and are overcome by the binding of DNA into toroids (nucleosomes and  
7 higher order structures). In addition to these effects, DNA supercoiling has a direct influence  
8 on many aspects of DNA metabolism *in vivo*. The binding of proteins to DNA is often  
9 influenced by supercoiling. Conversely, the binding of proteins that remove DNA supercoils  
10 can be used to relieve excess energy associated with supercoiling and prevent unfavourable  
11 deformations within the DNA. See also: Cell Biophysics, DOI: 10.1038/npg.els.0001271;  
12 Protein–DNA Interactions: Structure and Energetics, DOI: 10.1038/npg.els.0001349.

13 DNA topology plays a fundamental role in facilitating site-specific recombination reactions.  
14 Furthermore, analysis of the topology of reaction products has provided significant  
15 information towards understanding the recombination reaction, particularly for processes  
16 involving IHF and resolvases (Swinger and Rice, 2004; Wasserman and Cozzarelli, 1986).

17 Increased free energy associated with negative supercoiling can also be used to separate  
18 the strands of the DNA helix (Figure 1), which is usually unfavourable under physiological  
19 conditions. Thus, negatively supercoiled DNA templates assist processes that require  
20 opening of the DNA helix, such as replication and transcription. In general, these processes  
21 are increased at higher levels of negative supercoiling, but the relationship between  $\sigma$  and  
22 efficiency of transcription is complex. Some promoters are inhibited by increases in negative  
23 DNA supercoiling, suggesting that sequence or chromatin context are also important (Gilbert  
24 and Allan, 2014).

## 25 **Current Research Topics**

26 The influence of supercoiling upon the three-dimensional structure of DNA is well  
27 understood *in vitro*. The relationship of these observations to the structure of DNA *in vivo* is  
28 less clear. For example, many experiments show that twin domains of supercoiling can be  
29 generated when macromolecular protein assemblies translocate along DNA, and these  
30 could have profound effects on DNA metabolism inside cells. Although localized levels of  
31 DNA supercoiling are observed to vary *in vivo*, it seems that DNA topoisomerases normally  
32 keep these variations within well-defined limits (Baranello *et al*, 2012; Gilbert and Allan,  
33 2014; Roca, 2011). Evidence is growing to show that variable levels of supercoiling may

1 impact on specific reactions that involve DNA metabolism. Ongoing research is evaluating  
2 the extent by which DNA topology exerts regulatory influences over DNA metabolism.  
3 Developments of new scientific technologies have been particularly useful for visualising  
4 how proteins influence DNA topology inside cells and at the single-molecule level *in vitro* (De  
5 Vlaminck and Dekker, 2012; Koster *et al*, 2010; Neuman, 2010). See also: Magnetic  
6 Tweezers, DOI: 10.1002/9780470015902.a0023173.

7 There are reciprocal interactions between virtually every reaction involving DNA and DNA  
8 topology. In other words, DNA topology influences its metabolism and DNA metabolism  
9 influences its topology (Fogg *et al*, 2012). Thus, there is obvious potential for DNA topology  
10 to be used in the regulation of gene expression (Ptacin and Shapiro, 2013). There is  
11 significant evidence that this occurs under some physiological conditions, but the extent to  
12 which this happens remains unclear. It seems likely that because global DNA supercoiling is  
13 an intrinsic property of the DNA template, it may be too universal to provide the fine control  
14 of expression of all genes. Perhaps the cell has evolved mechanisms that sever the links  
15 between DNA topology and transcription in some circumstances? The situation could be  
16 dramatically different for local DNA supercoiling where the surrounding DNA determines the  
17 topological changes. The manner by which these interactions take place are still unresolved.  
18 Well-characterized experimental systems are now available to monitor reactions such as  
19 replication, transcription and recombination, from both pro- and eukaryotes. Continued  
20 development and application of *in vitro* and *in vivo* approaches will provide significant  
21 advances in our understanding of how the three-dimensional structure of DNA integrates  
22 within cellular metabolism.

23

## 24 **Glossary**

### 25 **Catenane**

26 Interlinked double-stranded DNA circles, i.e. that cannot be unlinked without  
27 breakage of both strands of one double-stranded helix.

### 28 **Closed-circular DNA**

29 Double-helical DNA with no free ends, i.e. both strands are closed circles with no  
30 discontinuities in their phosphodiester backbones.

### 31 **Linking difference**

32 Difference between the linking number of a particular topoisomer of closed-circular  
33 DNA and the average linking number of relaxed DNA; can have positive or negative  
34 values.

1 **Linking number**

2 Number of times two strands of closed-circular DNA are connected. It is distributed  
3 between the two geometric parameters twist and writhe.

4 **Open-circular DNA**

5 Double-helical DNA with one strand containing a broken phosphodiester bond; also  
6 referred to as 'nicked DNA'.

7 **Relaxed DNA**

8 Closed-circular DNA formed with minimal torsional strain of the DNA helix.

9 **Supercoiled DNA**

10 DNA containing coiling in addition to its normal helical path; closed-circular DNA  
11 molecules formed under torsional stress have average linking difference not equal to  
12 zero – can be positive or negative.

13 **Topoisomer**

14 (from *topological isomer*) Closed-circular DNA molecule of unique linking number.

15 **Topoisomerase**

16 Enzyme that catalyses changes in the linking number of closed-circular DNA.

17 **Twist**

18 Number of double-helical turns in a given length of DNA, measured relative to the  
19 DNA helix axis.

20 **Writhe**

21 Geometric parameter that describes the path of a DNA helix in three-dimensional  
22 space.

23

24 **References**

25 Baranello L, Levens D, Gupta A and Kouzine F (2012) The importance of being supercoiled:  
26 how DNA mechanics regulate dynamic processes. *Biochim Biophys Acta* **1819**: 632-638

27

28 Bates AD and Maxwell A (2005) *DNA topology, Chapter 2, pp. 25-81*, Oxford: IRL Press.

29

30 Bauer WR, Crick FHC and White JH (1980) Supercoiled DNA. *Sci Amer* **243**: 100-113

31

32 Benham CJ and Mielke SP (2005) DNA mechanics. *Annu Rev Biomed Eng* **7**: 21-53

33



1 Bowater R, Aboul-Ela F and Lilley DMJ (1992) Two-dimensional gel electrophoresis of  
2 circular DNA topoisomers. *Meth Enzymol* **212**: 105-120

3

4 Chargaff E, Zamenhof S and Green C (1950) Composition of human desoxyribose nucleic  
5 acid. *Nature* **165**: 756-757

6

7 Chiancone E and Ceci P (2010) The multifaceted capacity of Dps proteins to combat  
8 bacterial stress conditions: Detoxification of iron and hydrogen peroxide and DNA binding.  
9 *Biochim Biophys Acta* **1800**: 798-805

10

11 Corbett KD and Berger JM (2004) Structure, molecular mechanisms, and evolutionary  
12 relationships in DNA topoisomerases. *Annu Rev Biophys Biomol Struct* **33**: 95-118

13

14 De Vlaminck I and Dekker C (2012) Recent advances in magnetic tweezers. *Annu Rev*  
15 *Biophys* **41**: 453-472

16

17 Dillon SC and Dorman CJ (2010) Bacterial nucleoid-associated proteins, nucleoid structure  
18 and gene expression. *Nat Rev Microbiol* **8**: 185-195

19

20 Drlica K (1992) Control of bacterial DNA supercoiling. *Mol Microbiol* **6**: 425-433

21

22 Drlica K and Rouviere-Yaniv J (1987) Histone like proteins of bacteria. *Microbiol Reviews*  
23 **51**: 301-319

24

25 Fogg JM, Randall GL, Pettitt BM *et al* (2012) Bullied no more: when and how DNA shoves  
26 proteins around. *Q Rev Biophys* **45**: 257-299

27

28 Forterre P, Gribaldo S, Gadelle D and Serre MC (2007) Origin and evolution of DNA  
29 topoisomerases. *Biochimie* **89**: 427-446

30

31 Franklin RE and Gosling RG (1953) Molecular configuration in sodium thymonucleate.  
32 *Nature* **171**: 740-741

33

34 Gilbert N and Allan J (2014) Supercoiling in DNA and chromatin. *Curr Opin Genet Dev* **25**:  
35 15-21

36

37 Gubaev A and Klostermeier D (2014) The mechanism of negative DNA supercoiling: a  
38 cascade of DNA-induced conformational changes prepares gyrase for strand passage. *DNA*  
39 *Repair (Amst)* **16**: 23-34

40

41 Hatfield GW and Benham CJ (2002) DNA topology-mediated control of global gene  
42 expression in *Escherichia coli*. *Annu Rev Genet* **36**: 175-203

43

1 Hud NV and Vilfan ID (2005) Toroidal DNA condensates: unraveling the fine structure and  
2 the role of nucleation in determining size. *Annu Rev Biophys Biomol Struct* **34**: 295-318

3

4 Keller W (1975) Determination of the number of superhelical turns in simian virus 40 DNA by  
5 gel electrophoresis. *Proc Natl Acad Sci U S A* **72**: 4876-4880

6

7 Koster DA, Crut A, Shuman S, Bjornsti MA and Dekker NH (2010) Cellular strategies for  
8 regulating DNA supercoiling: a single-molecule perspective. *Cell* **142**: 519-530

9

10 Kouzine F and Levens D (2007) Supercoil-driven DNA structures regulate genetic  
11 transactions. *Front Biosci* **12**: 4409-4423

12

13 Lebowitz J (1990) Through the looking glass: the discovery of supercoiled DNA. *Trends*  
14 *Biochem Sci* **15**: 202-207

15

16 Lilley DMJ and Dahlberg JE (1992) DNA structures. *Meth Enzymol* **211 and 212**

17

18 Liu LF and Wang JC (1975) On the degree of unwinding of the DNA helix by ethidium. II.  
19 Studies by electron microscopy. *Biochim Biophys Acta* **395**: 401-412

20

21 Liu LF and Wang JC (1987) Supercoiling of the DNA template during transcription. *Proc*  
22 *Natl Acad Sci USA* **84**: 7024-7027

23

24 Luger K and Richmond TJ (1998) DNA binding within the nucleosome core. *Curr Opinion*  
25 *Struct Biol* **8**: 33-40

26

27 Lulchev P and Klostermeier D (2014) Reverse gyrase--recent advances and current  
28 mechanistic understanding of positive DNA supercoiling. *Nucleic Acids Res* **42**: 8200-8213

29

30 Muskhelishvili G and Travers A (2003) Transcription factor as a topological homeostat.  
31 *Front Biosci* **8**: d279-285

32

33 Neuman KC (2010) Single-molecule measurements of DNA topology and topoisomerases. *J*  
34 *Biol Chem* **285**: 18967-18971

35

36 Ptacin JL and Shapiro L (2013) Chromosome architecture is a key element of bacterial  
37 cellular organization. *Cell Microbiol* **15**: 45-52

38

39 Richmond TJ and Davey CA (2003) The structure of DNA in the nucleosome core. *Nature*  
40 **423**: 145-150

41

42 Roca J (2011) The torsional state of DNA within the chromosome. *Chromosoma* **120**: 323-  
43 334

1  
2 Schlick T (1995) Modeling superhelical DNA: recent analytical and dynamic approaches.  
3 *Curr Opin Struct Biol* **5**: 245-262

4  
5 Schlick T and Olson WK (1992) Supercoiled DNA energetics and dynamics by computer  
6 simulation. *J Mol Biol* **223**: 1089-1119

7  
8 Schoeffler AJ and Berger JM (2008) DNA topoisomerases: harnessing and constraining  
9 energy to govern chromosome topology. *Q Rev Biophys* **41**: 41-101

10  
11 Swinger KK and Rice PA (2004) IHF and HU: flexible architects of bent DNA. *Curr Opin*  
12 *Struct Biol* **14**: 28-35

13  
14 Travers A and Muskhelishvili G (2005) DNA supercoiling - a global transcriptional regulator  
15 for enterobacterial growth? *Nat Rev Microbiol* **3**: 157-169

16  
17 Travers A, Schneider R and Muskhelishvili G (2001) DNA supercoiling and transcription in  
18 *Escherichia coli*: The FIS connection. *Biochimie* **83**: 213-217

19  
20 Vologodskii AV and Cozzarelli NR (1994a) Conformational and thermodynamic properties of  
21 supercoiled DNA. *Annu Rev Biophys Biomol Struct* **23**: 609-643

22  
23 Vologodskii AV and Cozzarelli NR (1994b) Supercoiling, knotting, looping and other large-  
24 scale conformational properties of DNA. *Curr Opinion Struct Biol* **4**: 372-375

25  
26 Vos SM, Tretter EM, Schmidt BH and Berger JM (2011) All tangled up: how cells direct,  
27 manage and exploit topoisomerase function. *Nat Rev Mol Cell Biol* **12**: 827-841

28  
29 Wang JC (1974) The degree of unwinding of the DNA helix by ethidium. I. Titration of twisted  
30 PM2 DNA molecules in alkaline cesium chloride density gradients. *J Mol Biol* **89**: 783-801

31  
32 Wasserman SA and Cozzarelli NR (1986) Biochemical topology: applications to DNA  
33 recombination and replication. *Science* **232**: 951-960

34  
35 Watson JD and Crick FC (1953) Molecular structure of nucleic acids: a structure for  
36 deoxyribose nucleic acids. *Nature* **171**: 737-738

37  
38 Wilkins MH, Stokes AR and Wilson HR (1953) Molecular structure of deoxypentose nucleic  
39 acids. *Nature* **171**: 738-740

40  
41 Witz G and Stasiak A (2010) DNA supercoiling and its role in DNA decatenation and  
42 unknotting. *Nucleic Acids Res* **38**: 2119-2133

43

1 Wu HY and Fang M (2003) DNA supercoiling and transcription control: a model from the  
2 study of suppression of the leu-500 mutation in *Salmonella typhimurium* topA- strains. *Prog*  
3 *Nucleic Acid Res Mol Biol* **73**: 43-68

4  
5 Wu P, Song L, Clendenning JB *et al* (1988) Interaction of chloroquine with linear and  
6 supercoiled DNAs. Effect on the torsional dynamics, rigidity, and twist energy parameter.  
7 *Biochemistry* **27**: 8128 - 8144

8

## 9 **Further Reading**

10 • Calladine CR, Drew HR, Luisi B and Travers AA (2004) *Understanding DNA:*  
11 *The Molecule and How it Works*, 3<sup>rd</sup> edn. Academic Press: London.

12 • Cozzarelli NR and Wang JC (eds) (1990) *DNA Topology and its Biological*  
13 *Effects*, Cold Spring Harbor, NY: Cold Spring Harbor Press.

14 • Frank-Kamenetskii MD (1997) *Unraveling DNA: The Most Important*  
15 *Molecules of Life*, Reading, USA: Addison Wesley.

16 • Neidle S (2008) *Principles of Nucleic Acid Structure*, UK: Academic Press:  
17 London.

18 • Saenger W (1984) *Principles of Nucleic Acid Structure*. New York, NY:  
19 Springer-Verlag.

20 • Sinden RR (1994) *DNA Structure and Function*. San Diego, USA: Academic  
21 Press.

22 • Travers A (1993) *DNA-Protein Interactions*. UK: Chapman & Hall.

23 • Wang JC (1994) Appendix I: an introduction to DNA supercoiling and DNA  
24 topoisomerase-catalyzed linking number changes of supercoiled DNA. In: Liu LF (ed.)  
25 *DNA Topoisomerases: Topoisomerase-targeting Drugs*, pp. 257–270. San Diego:  
26 Academic Press.

27 • Vologodskii A (1992) *Topology and Physics of Circular DNA*. Boca Raton,  
28 USA: CRC Press.

29

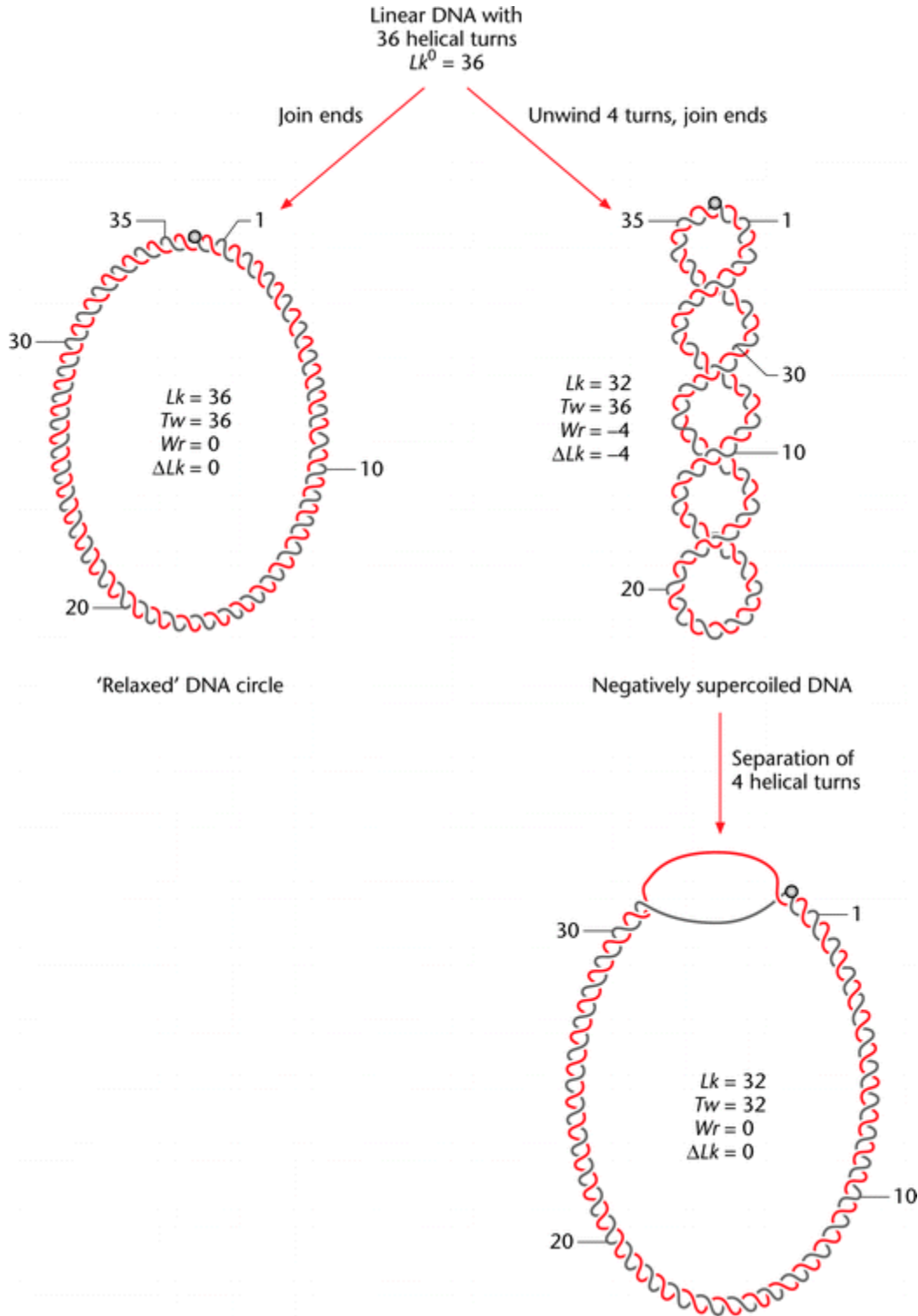
1  
2  
3

**Table 1.** Definitions of abbreviation of DNA topological parameters

Abbreviation	Term	Definition
cccDNA	Covalently closed circular DNA	Double-helical DNA without free ends, i.e. both strands are closed circles
$N$	Length	Total number of base pairs in DNA
$h$	Helical repeat (helical pitch)	Number of base pairs per turn of DNA helix
$Lk$	Linking number	For cccDNA, number of times one DNA strand intersects the plane of the other
$Lk^0$	Hypothetical linking number	cccDNA without torsional strain (equal to $N/h$ )
$Lk_m$	Relaxed linking number	Linking number of topoisomer with least torsional strain (may not be equal to $N/h$ )
$\Delta Lk$	Linking difference	For supercoiled DNA, difference between $Lk$ and $Lk^0$
$\sigma$	Specific linking difference	$\Delta Lk$ normalized to length of DNA (equal to $\Delta Lk/Lk^0$ )
$Tw$	Twist	Number of turns within DNA double helix
$Wr$	Writhe	Number of times DNA double helix crosses its own path
$\Delta G_{sc}$	Free energy of supercoiling	Additional free energy contained within DNA due to presence of supercoils

4

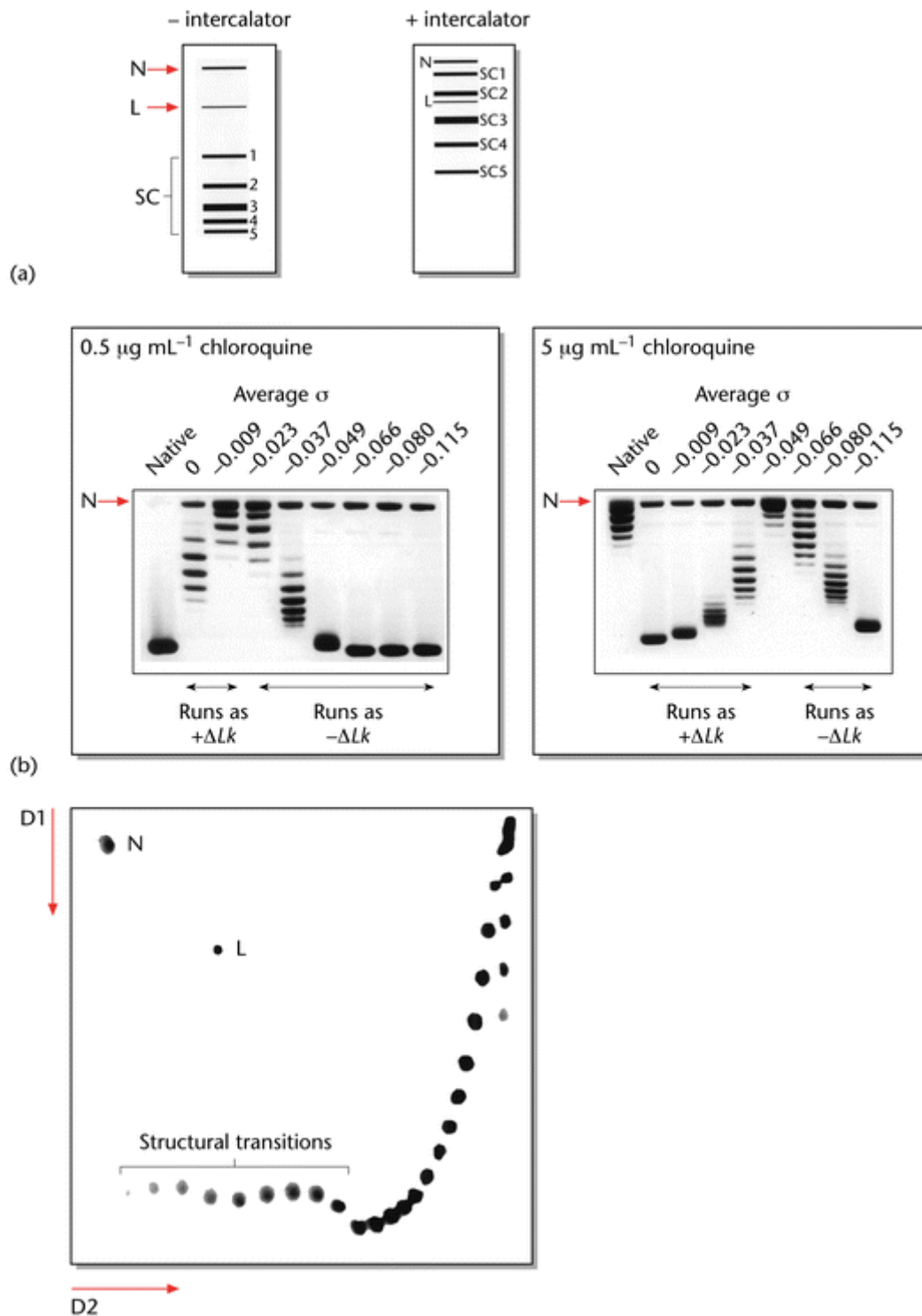
1



2  
3

4 **Figure 1.** Relationship of linking number, twist and writhe of closed circular forms of  
5 DNA. Closed DNA circles can be made by formation of covalent 5'-3'  
6 phosphodiester bonds on each strand of a linear molecule. For a linear molecule  
7 with 36 helical turns, the linking number of this unconstrained state ( $Lk^0$ ) is 36.

1 Closure into an unconstrained planar circle, as shown on the left side of the figure,  
2 produces a molecule with twist ( $Tw$ ) = 36 and writhe ( $Wr$ ) = 0. If the number of helical  
3 turns is altered before closure, the DNA molecule adopts a supercoiled  
4 conformation. On the right side of the figure, four helical turns are removed from the  
5 molecule, reducing the linking number ( $Lk$ ) to 32. For simplicity, the figure shows all  
6 unwinding partitioned as  $Wr$ , although such changes are usually partitioned between  
7  $Tw$  and  $Wr$ . Unwinding of helical turns produces negatively supercoiled DNA (or  
8  $-\Delta Lk$ ) as shown, whereas the inclusion of additional turns produces positively  
9 supercoiled DNA. For DNA with  $-\Delta Lk$  in the interwound form, the superhelical turns  
10 are right-handed. Note that separation of DNA strands removes negative supercoils  
11 (equivalent to the addition of positive supercoils).



1 (c)

2 **Figure 2.** Measurement of linking number by gel electrophoresis. (a) Schematic

3 illustration of a DNA sample separated by electrophoresis through an agarose gel

4 with and without an intercalator. DNA isolated from bacterial cells contains molecules

5 with different topology: some have their backbones unbroken and are negatively

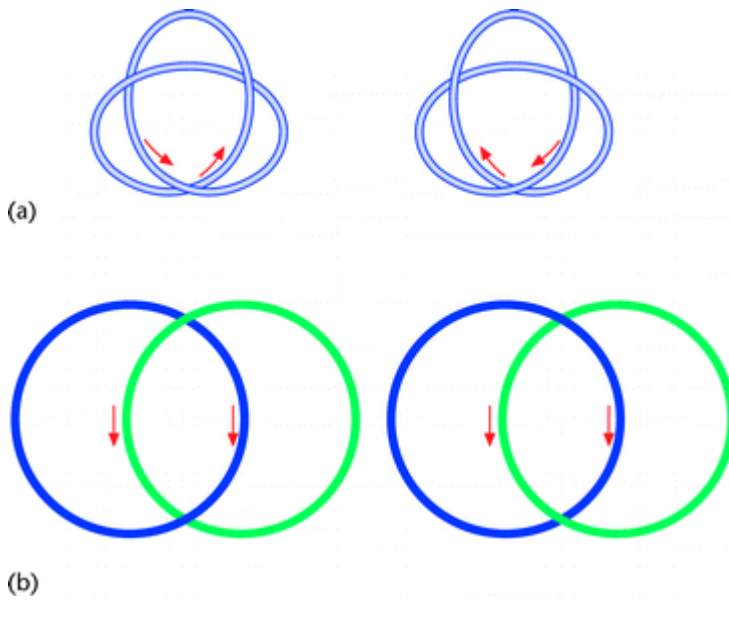
6 supercoiled (SC), some have one strand broken and referred to as 'nicked' (N) and



1 some have both strands broken to produce a linear molecule (L). Note that the  
2 supercoiled DNA consists of a Gaussian distribution of different topoisomers. Upon  
3 addition of intercalator, the migration of intact molecules is altered, but that of nicked  
4 and linear molecules is not changed. (b) Enzymatic relaxation of plasmid DNA in the  
5 presence of varying concentrations of intercalator produces samples containing  
6 topoisomers at different levels of supercoiling. Utilization of multiple gels with  
7 different concentrations of intercalator allows measurement of  $\Delta Lk$ . For each sample,  
8 average superhelical density ( $\sigma$ ) is shown above the lane. Note that in each gel,  
9 samples can have positively or negatively supercoiled topoisomers. The inclusion of  
10 intercalator in the running buffer alters the electrophoretic mobility of all topoisomers  
11 equivalently. Superhelical density can be measured for experimental samples  
12 ('native') by comparison with those of known  $\sigma$ . (c) Two-dimensional agarose gel  
13 electrophoresis of topoisomers ranging from high negative  $\sigma$  to moderate positive  $\sigma$ .  
14 A DNA sample is loaded in a single well in a large agarose gel and electrophoresis is  
15 performed under specific conditions (usually without intercalator) in direction D1.  
16 After soaking of the gel in buffer containing intercalator, electrophoresis is continued  
17 in direction D2 (90° to D1). The gel shown contained 20  $\mu\text{g mL}^{-1}$  chloroquine during  
18 the second electrophoresis, resulting in all topoisomers having positive  $\sigma$ . Deviation  
19 of topoisomers from a smooth curve indicates that structural transitions in the DNA  
20 molecules reduced their negative  $\sigma$  during the first direction of electrophoresis. Spots  
21 marked 'N' and 'L' indicate the position of migration of 'nicked' and 'linear' DNA  
22 molecules, respectively.

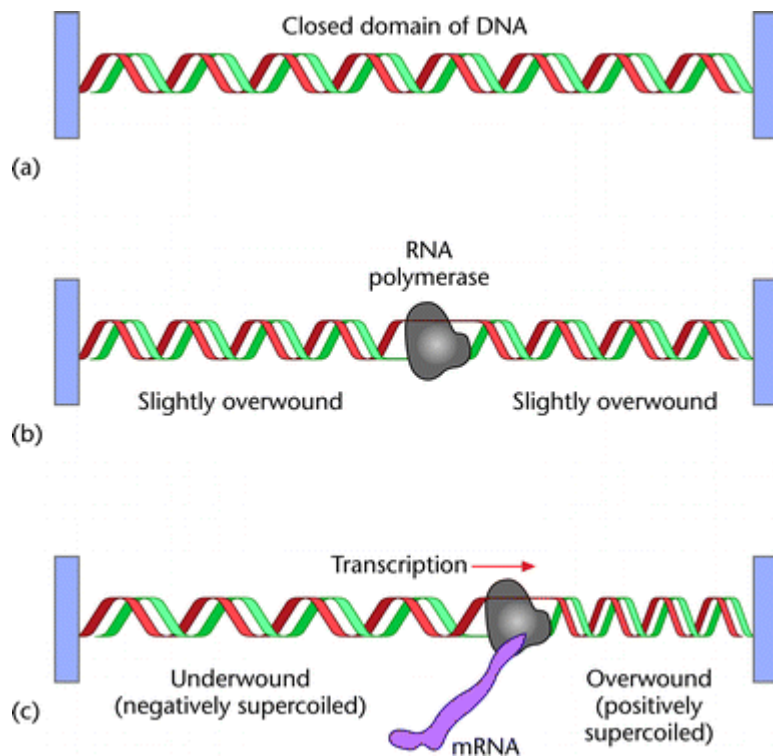
23

1



2  
3

4 **Figure 3.** Representation of knots and catenanes. (a) Topological knots may be  
5 formed in closed circles of DNA. The simplest knot that can be formed is called a  
6 trefoil because there are three lobes to the structure when it is laid flat. Two isomers  
7 of the trefoil knot are shown. Many other more complex knots may be formed within  
8 cccDNA molecules. (b) Catenanes are formed when two circular DNA molecules are  
9 interlocked. Catenanes containing complex, multiple links and involving many DNA  
10 circles have been observed in naturally occurring DNA. The arrows indicate that the  
11 polarity of a knot or catenane is influenced by the directionality of the sequence in  
12 the DNA molecule.



1

2

3

4

5

6

7

8

9

10

11

**Figure 4.** Twin domains of supercoiling are generated during transcription. (a) The shaded cylinders flank a closed domain of DNA containing eight helical turns. (b) To accommodate the transcriptional complex, some unwinding of the DNA helix occurs producing slight overwinding of the remaining DNA within each closed domain. (c) During transcription elongation, rotation of the large transcriptional complex around the DNA is hindered and positive and negative supercoiling are generated ahead and behind the polymerase, respectively. In this diagram, positive and negative supercoiling is represented by the presence of the same number of helical turns over a shorter and longer distance of DNA, respectively. Several biological mechanisms exist to remove these supercoils.

12

13

14

15

16

17

18

### Permissions

Figures 1-4 have been published in the previous version of this eLS article, so no permissions are required.