

1                   **UPGRADING THE PREDICTION OF JET GROUTING COLUMN DIAMETER**  
2                   **USING DEEP LEARNING WITH AN EMPHASIS ON HIGH ENERGIES**

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9  
10                  **Abstract**

11                  In this article is proposed a new method to estimate the diameter of jet grouting columns. The  
12                  method uses the largest data collection of column diameters measured to date and includes a large  
13                  amount of new data that fills the existing gap of data for high injection energies. The dataset was  
14                  analysed using a deep neural network that took into account the problem's key parameters (i.e.  
15                  type of soil, soil resistance, type of jet and specific energy in the nozzle). As a result, three  
16                  different neural networks were selected, one for each type of jet, according to the errors and  
17                  consistency associated with each. Finally, using the trained networks, a number of design charts  
18                  were developed to determine the diameter of a jet grouting column as a function of the soil  
19                  properties and the jet system. These charts allow generating an optimal jet grouting design,  
20                  improving the prediction of the diameter of jet columns especially in the high energy triple fluid.

21  
22                  **Keywords:** Jet grouting; ground improvement; column diameter; deep learning; neural networks.

23 **1. Introduction.**

24

25 Jet grouting [38] is the most powerful, versatile and studied technique among existing ground  
26 improvement methods. The technology uses radial fluid injection at very high speeds to erode the  
27 ground, partially replacing the eroded material and mixing it with a grouting agent (grout) to  
28 create a new material [6,5,22]. Jet grouting has led to wide-ranging applications including  
29 foundations, underpinnings, excavation supports, soil improvements, among others [21,19,11].

30

31 Currently, there are a large number of jet grouting procedures [8]. However, there are three  
32 traditional systems according to the number of fluids injected: single fluid (only grout is injected),  
33 double fluid (grout enshrouded by air or water is used) and triple fluid (grout and water  
34 enshrouded by air is used) [11,14]. Other systems also exist, such as enhanced triple fluid and  
35 superjet grouting, widely used nowadays, which are essentially improvements of the traditional  
36 methods [8,37]. The final product obtained with a jet grouting treatment depends on many factors  
37 [15], which in turn reside both in the parameters of the system itself (type of jet, injection pressure,  
38 flow rate, injected material, lifting and rotational speed of the monitor) and the soil to improve  
39 (particle size distribution, density, structure and phreatic level location). According to Modoni et  
40 al. [22] the column diameter depends on the jet's capacity to propagate its erosive action at greater  
41 distances from the nozzle, which is determined by the combination of the energy given by the  
42 injection and the soil's resistance. The way in which the grout interacts with the soil differs  
43 depending on the soil's permeability and therefore the fine particle content influences the soil's  
44 resistance to erosion, as recognised by Shen et al. [33]. Thus, there are three major types of grout–  
45 soil interaction according to the soil's permeability: seepage, sand erosion and clay erosion [22].

46

47 Consequently, predicting the diameter of a jet grouting column is a key parameter of major  
48 importance in engineering design and it has piqued the interest of many researchers. Atangana  
49 Njock et al. [3] reviewed the different existing methods to estimate the diameter of jet grouting  
50 columns based on the work published by Ribeiro and Cardoso [27] introducing the methods based

51 on artificial intelligence (AI) as a new category. In this way, they classified the methods to  
52 estimate jet grouting column diameters into the following five categories: (1) empirical, (2)  
53 conceptual, (3) theoretical, (4) semitheoretical and (5) based on artificial intelligence. The  
54 empirical [9] and conceptual methods [23,10,1] are mainly based on single fluid jet, as are most  
55 of the theoretical methods [22,36,17], except that of Shen et al. [33]. Among the semitheoretical  
56 methods, it should be underlined the work of Flora et al. [15] who collected data from field trials  
57 and established what is probably the most widely used jet grouting column estimation method to  
58 date for all types of jet grouting. However, the main drawback of this latter work is that the data  
59 of only 18 columns were used to validate the method in the triple fluid jet. Methods based on  
60 artificial intelligence predict the diameters of new columns using measured column diameter data.  
61 A key point to remember is that these methods are dependent on the amount of training data, so  
62 the larger the database used, the more accurate the predictions will be. Among these methods, we  
63 can highlight that proposed by Tinoco et al. [35] who collected column data mainly from double  
64 fluid systems and clayey soils; the authors conclude that the method is only suitable under these  
65 conditions and therefore much caution should be taken when applying under different conditions.  
66 Ochmański et al. [25] compiled the largest known database to date, with the data of 131 measured  
67 diameters of jet grouting columns corresponding to the three jet types (50 single, 43 double and  
68 38 triple). These authors created design charts derived from neural networks that significantly  
69 improve the predictions proposed by other authors [32,15] and that are applicable to all types of  
70 jet grouting and in all types of soils. Finally, a work based on neural networks [31] should be  
71 highlighted, in this case bidirectional long short-term memory networks, based on data from 7  
72 columns, all built with the single fluid jet system and in the same type of soil (pyroclastic soil).  
73 The work provides a novel tool to determine the real-time variations in jet grout column diameter  
74 with the depth.

75

76 Nowadays, due to a lack of reliable methods, uncertainty persists during the design stage  
77 regarding the prediction of the final grouted body's diameter. In this sense, analytical methods  
78 are unreliable due to the complexity of jet grouting mechanisms [22]. Mathematical models that

79 attempt to emulate the behaviour of the human brain have been developed over several decades.  
80 One class of these models are artificial neural networks (ANN) first introduced by McCulloch  
81 and Pitts [20]. ANNs have been widely applied to solve and/or understand many geotechnical  
82 engineering problems [39,7,34,13,16]. Specifically, ANNs have been used to predict the diameter  
83 of jet grouting columns [25,24], offering satisfactory results and even achieving lower levels of  
84 prediction errors than other analytical or empirical methods. A neural network having more than  
85 one hidden layer is generally referred to as a deep neural network (DNN) [30]. It uses multiple-  
86 layer architectures to extract the inherent features of the data from the lowest to the highest layer  
87 making it one of the most efficient AI tools for solving very complex problems, being widely  
88 used in geotechnical engineering [e.g. 4,18].

89

90 In the present study, DNNs were employed to predict jet grouting column diameter based on the  
91 problem's key parameters. Prior to the training of the DNN, a comprehensive set of data on jet  
92 grouting column diameters was collected. This database included column diameter measurements  
93 of all types of jet grouting and soils worldwide, thus, completing previous databases and methods,  
94 especially in the triple fluid jet grouting technique high energy range, where most of AI-based  
95 studies lack actual diameter data measured, leading to greater uncertainties regarding diameter  
96 predictions. It is worth noting that the evolution of this technique has been directed towards the  
97 increase of the columns' diameter, particularly for ground improvement works [12], therefore, an  
98 enhancement in the prediction of the diameter will lead to more accurate designs. Finally, the  
99 performed analysis allowed the plot of design charts to determine the diameter of a jet grouting  
100 column based on key input variables.

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102 The paper is organised as follows: Section 2 gives a detailed description of the field data database  
103 compiled. The input variables used and the adopted DNNs are addressed in detail in Section 3.  
104 Section 4 describes the main results of the analysis and presents the design charts proposed to  
105 design jet grouting columns. The main conclusions of the paper are summarised in section 5.

106

107 **2. Database.**

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109 To train the DNN was used a set of test field data in which the diameter of the jet grouting column  
110 was measured by different methods (such as visual inspection, sounding pipes or boreholes). The  
111 database developed by Ochmański et al. [25] was taken as basis, which in turn complements that  
112 elaborated by Flora et al. [15]. This database compiles diameter measurements in columns built  
113 in all types of soils and with the three jet grouting techniques. Therefore, it can be considered as  
114 a universal database, which can be used as a starting point to cover the objectives of this work.  
115 This database was completed with data directly extracted from the scientific literature and other  
116 data recovered from the experience of the authors. The data were classified according to the type  
117 of jet grouting (single fluid, double fluid or triple fluid). The database also contained data  
118 belonging to super jet grouting and other types of high energy jet. These inputs were included as  
119 cases corresponding to the triple fluid jet because of their similarities in terms of energy diameter  
120 ratio.

121

122 Tables S1, S2 and S3 detail all the considered cases, with 89 cases for the single fluid jet, 69 cases  
123 for the double fluid jet and 91 cases for the triple fluid jet. It is worth noting that this is the largest  
124 jet column diameter database to date, covering all the ranges of energy as well as different types  
125 of soils and jet grouting systems. They were compiled from papers published in the scientific  
126 literature as well as the authors' technical experience, complementing existing databases. The  
127 dataset processed in this work actually represents double the number of records considered in  
128 previous works. More specifically, the number of triple fluid system records represents a threefold  
129 increase with respect to the amount of data considered in previous works. Additionally, if we  
130 focus on the high energy range ( $E'_n > 100$  MJ/m), a total of 56 diameter records were used in this  
131 work compared to 3 used in previous works.

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### 135 **3. Deep Neural Networks.**

136

#### 137 **3.1. Input variables.**

138 To define the input variables, the same considerations adopted in previous works [e.g. 25,15]  
139 were followed and only four input variables were considered: (1) jet grouting injection system,  
140 (2) soil type, (3) soil value of the standard penetration test (SPT) and (4) specific energy at the  
141 nozzle. Regarding the type of jet grouting, three types were considered (single fluid, double fluid  
142 or triple fluid) according to the definitions given in EN:12716 [14]. In relation to the soil type,  
143 the data were grouped according to their classification in the standard ASTM:D2487 [2], which  
144 divides soils into coarse-grained without fine (less than 5% fine grains), coarse-grained with fine  
145 and fine-grained, as stated by different authors [22,32] who demonstrated that erosion  
146 mechanisms varied according to the type of soil. The resistance of these three classes of soil to  
147 erosion was quantified based on the value of the SPT. In the records where there was no SPT  
148 value but resistance to static penetration ( $q_c$ ), both were correlated following the guidelines given  
149 in Schmertmann [29] and Robertson et al. [28]. The last input variable considered was the specific  
150 energy at the nozzle ( $E'_n$ ), which was calculated according to the methods proposed by Flora et  
151 al. [15].

152

#### 153 **3.2. Adopted DNNs.**

154

155 A DNN with different architectures and parameters was trained for each type of jet grouting. Two  
156 scoring indicators, mean absolute percentage error (MAPE) and root mean square error (RMSE),  
157 were used to quantify the prediction performance and accuracy of the developed models among  
158 the different architecture and parameter options. The sample size of the training and validation  
159 sets was determined using the cross-validation technique, considering different fractions (70/30,  
160 75/25, 80/20 and 85/15 and 90/10) and the 80/20 ratio produced the best results. Thus, the  
161 available data were divided into two sets, a training set representing 80% of the total data and a  
162 validation set representing the remaining 20%. An important issue to bear in mind regards the

163 input variables considered in the analysis: these variables vary in their scales because they  
164 measure different quantities. In this way, to improve the predictive power, it is necessary to carry  
165 out a feature scaling process. In this case, the data were standardised by removing the mean and  
166 scaling to unit variance.

167

168 Baseline models of the DNNs were initially built and later optimised through model parameter  
169 tuning. There are no established, infallible rules for developing baseline DNN models, and  
170 previous experiences clearly demonstrate the importance of empirical testing when it comes to  
171 developing neural network models. However, the denominated grid search technique [26] can be  
172 used for tuning deep learning models. Therefore, the optimum values of the DNN parameters  
173 considered were determined by using a grid search strategy with five-fold cross-validation. Table  
174 S4 shows the parameters involved in the grid search along with a brief description.

175

176 Once the parameters were chosen, they were refined in their environment in order to maximise  
177 each DNN's performance. The final results for each jet grouting type considered are shown in  
178 Table 1, and Figure S1 shows a graphical scheme of the neural network adopted in the case of the  
179 double fluid.

180

181 The process of choosing the architecture and DNN parameters came to an end once the lowest  
182 MAPE and RMSE values were found, while constantly checking that the predictions were  
183 consistent. During this process, the absence of overfitting was verified by checking the errors  
184 gained in the training and validation processes; in all cases, the errors obtained were similar.  
185 Learning curves (errors depending on the epochs in the training and validation sets) were  
186 inspected to determine the appropriate number of epochs and diagnose the model's performance.  
187 These curves also helped us to determine the absence of overfitting in the adopted networks.

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Jet type	Hidden layers	Architecture	Activation function	Epochs	Optimizer	Batch size	Learning rate
Single fluid	4	128/64/32/16/1	ReLU	30	Adadelata	10	0.80
Double fluid	3	64/32/16/1	ReLU	70	Adadelata	3	1.05
Triple fluid	5	64/32/16/8/4/1	ReLU	120	Adadelata	3	0.35

191

192

*Table 1. Summary of the main features of the adopted DNNs.*

193

#### 194 **4. Results: Design charts.**

195

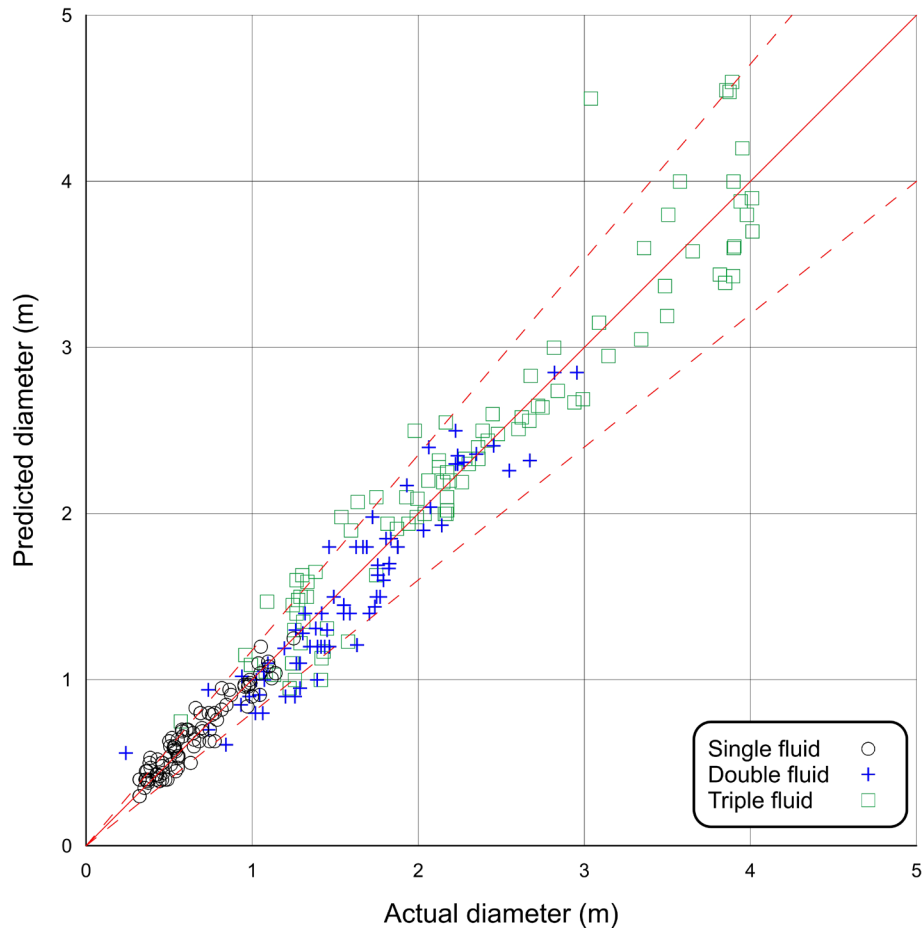
196 Once the most appropriate network architectures and configurations were selected, their  
 197 predictions were checked by comparing the measured and predicted diameters with the whole  
 198 dataset. Figure 1 shows the point clouds of the three types of jet grouting systems considered.  
 199 Table 2 shows the most significant performance metrics obtained for each type of jet.

200

201 Compared to the existing common and universal methods to predict jet column diameters  
 202 [33,25,15], the present work contributes to a significant improvement mainly for the triple fluid  
 203 jet. A summary of the metrics obtained in these works are described in Ochmański et al. [25], and  
 204 the highest performance is found in the study of Ochmański et al. [25], achieving MSE values of  
 205 0.007, 0.05 and 0.106 m<sup>2</sup> and MAPE values of 11.93, 12.97 and 15.49%, for the single double  
 206 and triple jet, respectively. If these results are compared with those shown in Table 2, the present  
 207 work offers considerable improvements regarding the diameter prediction, mainly for the triple  
 208 fluid jet.

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Figure 1. Predicted vs measured jet grouting column diameter for all types of jet grouting considered.

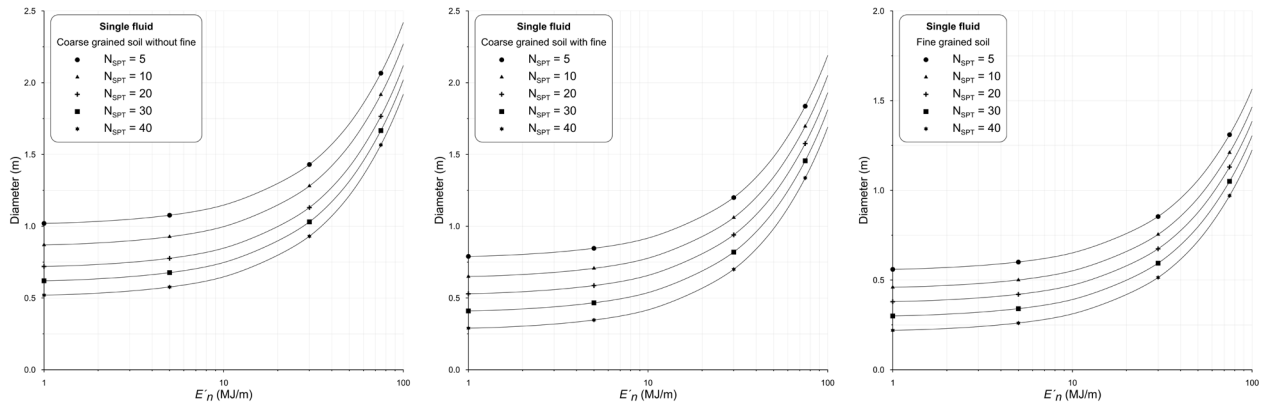
Jet type	$R^2$	MAPE (%)	MAE (m)	MSE ( $m^2$ )
Single fluid	0.91	9.71	0.058	0.005
Double fluid	0.90	12.51	0.157	0.037
Triple fluid	0.91	9.99	0.214	0.087

213 Table 2. Summary of accuracy parameters of the adopted DNNs.  $R^2$  is the coefficient of determination, MAPE is the  
214 mean absolute percentage error, MAE is the mean absolute error and MSE is the mean squared error.

215

216 Finally, once the DNNs were trained and tested, they were fed using different input datasets (i.e.  
217 SPT blow counts, soil types and energies) strategically prepared to predict the associated  
218 diameters. These data were plotted in three main design charts, providing the present work with  
219 greater practical usefulness. The proposed design charts are shown in Figures 2, 3 and 4.

220



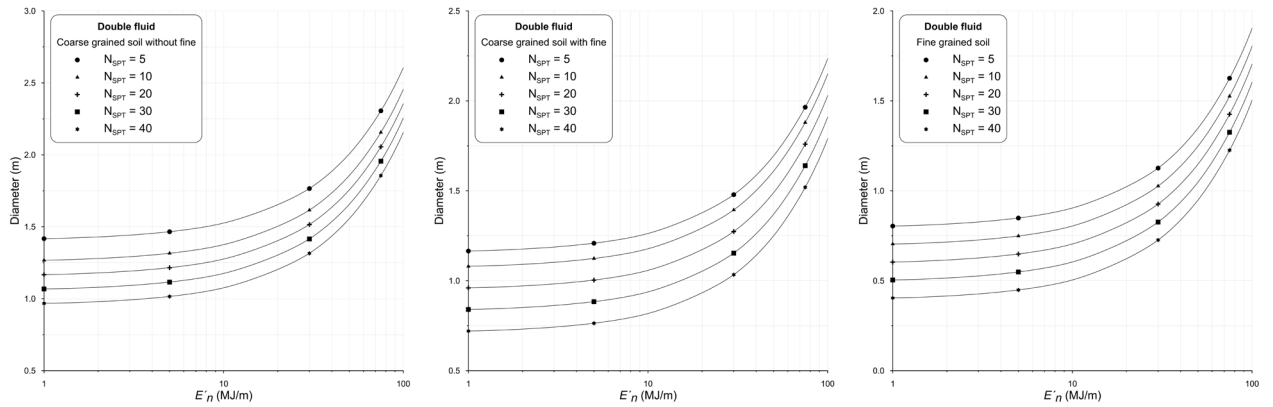
221

222

Figure 2. Design charts to predict the column diameter for jet grouting single fluid. From left to right, coarse-grained without fine soils, coarse-grained with fine soils and fine-grained soils.

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224



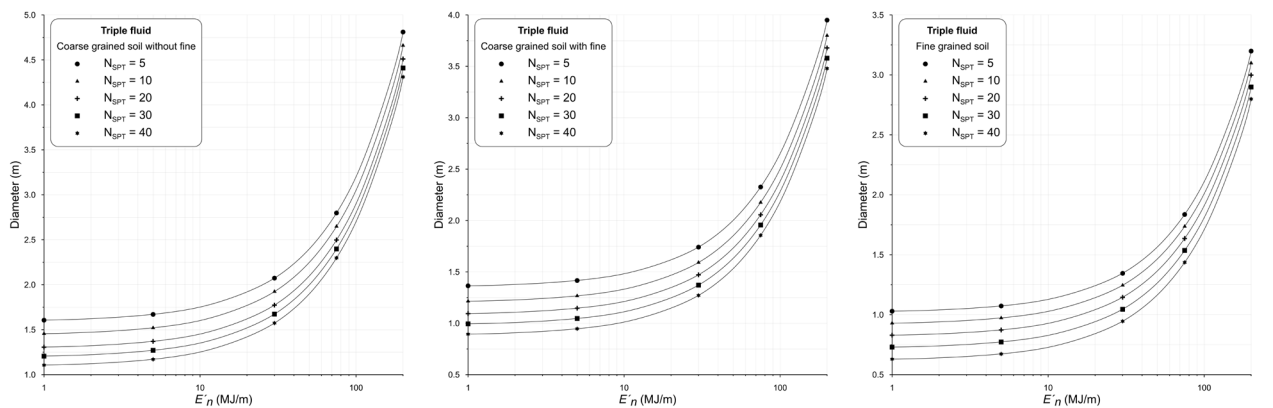
225

226

Figure 3. Design charts to predict the column diameter jet grouting double fluid. From left to right, coarse-grained without fine soils, coarse-grained with fine soils and fine-grained soils.

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229

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Figure 4. Design charts to predict the column diameter for jet grouting triple fluid. From left to right, coarse-grained without fine soils, coarse-grained with fine soils and fine-grained soils.

231

232

233 When comparing to previously published design charts [e.g. 15,25] some differences are observed  
234 and these are manifested more notably in the triple fluid jet, reaching very significant differences  
235 (up to 20-30%) in the zone of high energies.

236

## 237 **5. Conclusions.**

238

239 In this paper, deep learning was applied to estimate the diameter of jet grouting columns. To this  
240 end, the largest dataset to date of jet grouting column diameter measurements was collected.  
241 These data complement existing works, especially regarding the high energy zone of the triple  
242 fluid system, which is the most widespread today because the technology's evolution largely  
243 focuses on high energies (increases in diameter).

244 Once the data were collected, the key variable inputs were selected and different DNN  
245 configurations (architectures and parameters) were tested in order to select the most appropriate  
246 DNNs to explain the problem (those with a lower value in error function and prediction  
247 consistency). This process ended with the adoption of three DNNs, one for each type of jet  
248 grouting, producing better performance metrics than those offered by existing methods, mainly  
249 for the prediction of triple fluid high energy columns diameters.

250 To improve the practical applications of this work, the trained DNNs were used to plot a series of  
251 design charts to allow a quick and easy prediction of a jet grouting column's diameter, based on  
252 the specific energy in the nozzle, the type of soil and its strength expressed through the soil SPT  
253 value. These charts will contribute to more accurate and reliable designs of jet grouting columns,  
254 although the networks trained in this study are likely to be improved in the future as more diameter  
255 data are obtained.

256

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258

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269

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272

273 **Availability of data and material:** The data used in this paper are available upon request by  
274 contacting the correspondence author.

275

276 **Code availability:** (software application or custom code) not applicable.

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