On Energy Processing with Linear–Assisted DC/DC Converters

Herminio Martínez-García
Barcelona College of Industrial Engineering
Department of Electronics Engineering
Technical University of Catalonia–BarcelonaTech (UPC)
c/ Comte de Urgell, 187, 08036, Barcelona (Spain)
herminio.martinez@upc.edu

Abstract—**Linear-assisted DC/DC converters (or linear-switching hybrid DC/DC converters) consist of a voltage linear regulator (classic NPN or nMOS topologies and LDO) connected in parallel with a switching DC/DC converter. In order to control these hybrid structures, different strategies exist, allowing to fix the switching frequency as a function of some parameters of the linear regulator. This article compares two control strategies that, although can be applied to the same circuital structure of linear-assisted converter, are sensibly different. The first one, reported in previous literature, cancels completely the average current through the linear regulator in steady state to achieve a reduction of the losses. Thus the efficiency of the whole system increases and almost equals the one of the standalone switching converter. The proposed approach, in spite of a slightly increment of linear regulator's losses, reduces the output ripple due to the crossover distortion of linear regulator output stage.**

Keywords—DC-DC Switching Converters; Voltage Linear Regulators; Linear-Assisted DC-DC Voltage Regulators.

I. INTRODUCTION

Two different alternatives have been widely used for decades to provide the necessary power supply voltage to electronics circuits and systems. These two alternatives are known largely: (1) the use of voltage series linear regulators (classic standard NPN –or nMOS– topologies and LDO) [1]-[3], and (2) DC/DC switching converters, thanks to which high current and high efficiency power supply systems can be obtained [4]-[6].

However, a third alternative, linear-assisted DC/DC converters (also known as linear-switching hybrid converters) is possible. They are circuital structures that present an increasing interest for the implementation of power supply systems that require two demanding design specifications: (1) high slew-rate of the output current and (2) high current consumption by the output load. This it is the case of the systems based on the modern microprocessors and DSPs, where both requirements converge [7], [8]. These linear-switching hybrid converters are able to combine the well-known advantages of the two existing typical alternatives for the implementation of DC/DC voltage regulators or converters, diminishing as well their disadvantages. Linear-assisted DC/DC converters can be implemented on printed circuits using discrete components. Nevertheless, they are also an attractive alternative susceptible to be integrated in on-chip power supply systems as a part of power management systems.

The basic scheme of a linear-assisted converter is shown in figure 1 [9], [10]. This structure consists, mainly, of a voltage linear regulator **in parallel** with a step-down switching DC/DC converter. In this type of converters, the value of the output voltage, supposed constant, is fixed with good precision by the voltage linear regulator. The current through this linear regulator is constantly sensed by the current sense element R_m. Based on its value, the controller activates or not the output of comparator CMP_1 that controls the switching element of the DC/DC converter. Notice that the current through the linear regulator constitutes a measurement of the error of the power supply system.
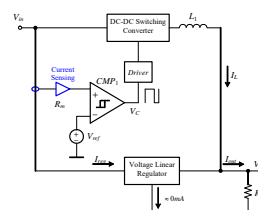

Fig. 1. Block diagram of a linear-assisted converter.

The power stage (that is, the switching converter) injects at the output the current required to force to a minimum value (not necessarily zero) the current through the linear regulator. As a consequence, it is obtained, altogether, a power supply system where the switching frequency comes fixed, among other parameters (such as the possible hysteresis of the analog comparator), by the value of the current through the linear regulator.

As an additional advantage of the structure shown in figure 1, and in contrast to which happens in other hybrid structures that work in open loop [11], it is possible to emphasize that the use of filters in the respective outputs of the linear and switching blocks (and, therefore, the possible optimization or equalization of its group propagation delays) is not, in this case, necessary. The present article allows to compare two strategies of control that can be applied to the same circuital structure of a linear-assisted converter. However, they are significantly different. The first one (that we will denominate *A* and is reported in previous literature [12],[13]), tries to cancel completely the current through the linear regulator in the steady state in order to achieve a reduction of the losses. Thus the efficiency of the whole system increases and almost

equals the one of the switching converter. It considers as a "main" block the switching DC/DC converter, and the linear regulator as an auxiliary module.

On the other hand, this proposal (strategy *B*) allows some average current flowing through the linear regulator. In spite of a slightly increasing of linear regulator's losses, this strategy reduces the output ripple due to the crossover distortion of its output stage. Thus, this approach considers as a "main" block the linear one, and the switching one as an auxiliary module.

In section II, the strategy of control *A* is discussed and shows its advantages and drawbacks. In section III the strategy of control *B* is compared with the first one. In section IV the linear-assisted converter is modified to improve its transient response. The article concludes with the main conclusions in section V.

II. STRATEGY OF CONTROL *A*

The first of the two strategies of control that is considered in the current article is implemented on the converter of figure 2, where the implementation of the linear-assisted converter consists of a linear regulator (including transistors Q_{2a} and Q_{2b}, which form an output complementary push-pull stage) and a switching DC/DC converter connected in parallel with the first one. In this case, the switching converter is a step-down type (buck converter) without the output capacitance. With this strategy, the switching converter is considered as a "main" block, whereas the linear regulator is considered as the auxiliary block that "assists" the first one when it is not able to provide output currents with high variations (that is to say, with high slew rate of the load current).
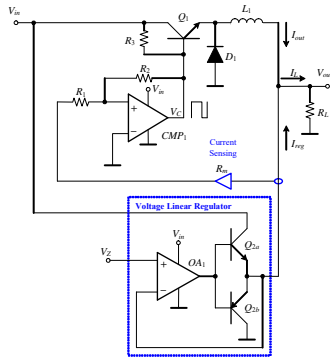

Fig. 2. Basic structure of a linear-assisted converter to implement the control strategy *A*.

The control strategy consists of sensing the current through the linear regulator and, transforming it into a voltage (thanks to the current sensing element R_m), controlling the switching frequency of the DC/DC switching converter. The main objective of this one is to provide ***all*** the load current in steady-state conditions (to obtain high efficiency of the whole system). Thus, in steady state the linear regulator does not provide current to the load, although it maintains the output voltage to an acceptable DC value. However, when variable output loads are driven, the linear regulator provides high transitory changes of the current in order to maintain constant the output voltage of the whole structure (figure 3).

Therefore, we can name to this type of control as ***strategy control with null average linear regulator current***. Resistors R_1 and R_2 of the Schmitt trigger determine the width of its hysteresis cycle and, thus, the maximum value of the switching frequency of the DC/DC converter.
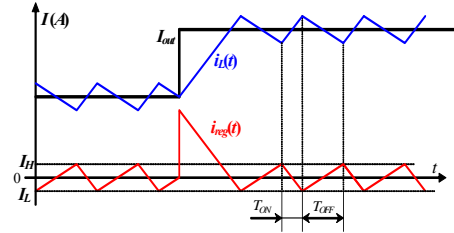

Fig. 3. Principle of operation of a linear-assisted converter with control strategy *A*.

This strategy of control allows to obtain an efficiency almost equal to the switching converter, because the current by the linear block and, thus, the dissipation in its pass transistors is, practically, neglected. Nevertheless, it suffers from a limitation referring to maintaining the output voltage free of significant ripples due to the well-known crossover distortion inherently present in push-pull amplifiers.

Let us consider the linear-assisted converter shown in figure 2, where the desired output voltage (fixed by the voltage V_Z) is equal to 5 *V*. Figure 4 shows the start-up transient response of the regulator with V_{in}=10 *V*. In addition, in the same figure is observed the response of the circuit for a step of the input voltage of the converter from 10 *V* to 13 *V* at *t*=20 µ*s*, and a decrease in the resistance of the load resistance of 50%, from 5 Ω to 2.5 Ω at *t*=40 µ*s*. On the other hand, figure 5 shows in detail the operation in the steady state of the considered linear-assisted converter. Notice that although the output voltage remains, in average, around the 5 *V* prefixed by means of the reference V_Z, the ripple is approximately 0.6 *V* (figure 6). The reason of this ripple is due to the output complementary transistors in the linear regulator. In fact, in every switching period, they pass from their cut region to their linear zone and vice versa. As a consequence, during the transitions of cut to conduction and vice versa, due to the well-known crossover distortion, a lack of regulation of the output voltage takes place, originating a ripple that, in certain applications, can not be tolerated.

III. STRATEGY OF CONTROL *B*

The proposed strategy is analyzed using the step-down switching converter shown in figure 7 [14], [15]. The linear regulator consists of a push-pull output stage (transistors Q_{2a} and Q_{2b}). In this strategy, the main objective of the DC-DC switching converter is to provide ***most of*** the load current in steady-state conditions to obtain also a good efficiency of the whole system. Thus, thanks to the incorporation of the reference voltage V_{ref} at the inverting input of the analog comparator, the linear regulator provides a small part of the load current in steady state, maintaining the output voltage to an acceptable constant value.
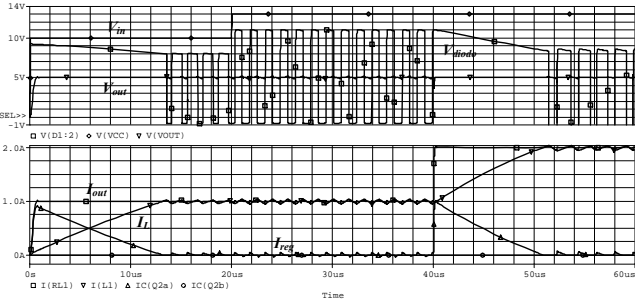
Fig. 4. Start-up transient of the converter in figure 2 with V_{in}=10 V. In addition, the response of the circuit to an input voltage step from 10 V to 13 V at t=20 μs, and to a variation in the load resistance from 5 Ω to 2.5 Ω at t=40 μs.
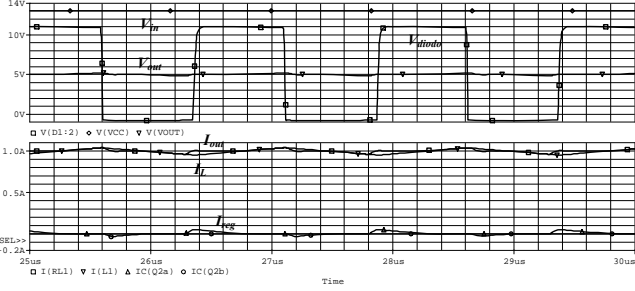

Fig. 5. Detail of operation in the steady state of the converter shown in figure 2.
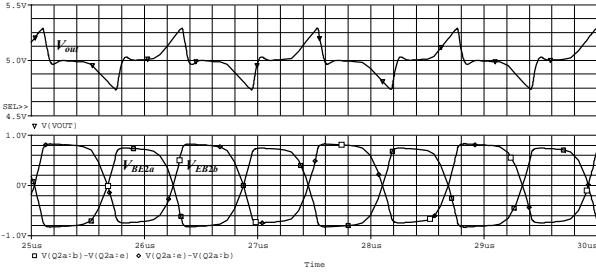

Fig. 6. Detail of the output voltage ripple and base-emitter voltage of transistors Q_{2a} and Q_{2b} of the linear regulator in the steady state for the linear-assisted converter in figure 2.

As a matter of fact, if the current demanded by the load is inferior to a maximum value of current, which we will denominate **switching threshold current**, I_γ, the output of comparator CMP_1 will be at low level, disabling the DC/DC switching converter and, thus, the current through inductor L_1 will be zero. Therefore, the voltage linear regulator supplies the load R_L, providing **all** the output current ($I_{reg}=I_{out}$).

When the current demanded by the load overpasses this current limit I_γ, automatically the output of the comparator will pass to high level, causing that the current through the inductance L_1 grows linearly according to:

$$i_L(t) = \frac{V_{in} - V_{out}}{L_1} t + I_L(\tau_1) \qquad (1)$$

In that expression, the conduction collector-emitter voltage of transistor Q_1 is ignored. $I_L(\tau_1)$ is the initial value of the current through inductor L_1 at the time instant T_{ON}. Considering that the output current $I_{out}=I_{reg}+I_L$, and is assumed to be constant (equal to V_{out}/R_L), the linear regulator current I_{reg} will decrease linearly, until becoming slightly smaller than I_γ. At this moment, the comparator will change

its output to low level, cutting the transistor Q_1 and causing that the current through the inductor decreases according to equation (2)

$$i_L(t) = -\frac{V_{out}}{L_1} t + I_L(\tau_2) \qquad (2)$$

In this expression it is considered that the diode D_1 is ideal (with zero direct voltage). $I_L(\tau_2)$ is the maximum value reached by the current flowing through the inductor (just at the beginning of the interval T_{OFF}). When the inductor current decreases to a value in which $I_{reg}>I_\gamma$, the comparator changes its state to high level, repeating the cycle again.
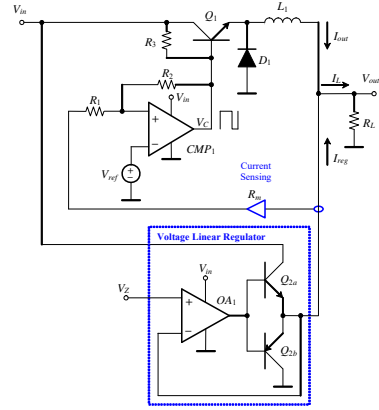

Fig. 7. Basic structure of linear-assisted converter with strategy of control B.

Without hysteresis in the comparator, the switching point of the DC/DC switching converter is given by the switching threshold current, I_γ, of the linear regulator. This one can be adjusted to a value thanks to the gain of the current sensing element, R_m, and the reference voltage V_{ref}, according to the expression:

$$I_\gamma = \frac{V_{ref}}{R_m} \qquad (3)$$

In case of a comparator without hysteresis, intrinsic delays of the electronic circuits determine a small hysteresis that limits the maximum value of the linear-assisted converter switching frequency (figure 8). However, with the objective of fixing this switching frequency to a practical value, in order not to increase significantly losses by the switching process, it is important to add the aforementioned hysteresis to the comparator CMP_1. Denoting V_H and V_L as the superior and inferior levels switching of this comparator, the value of this frequency can be determined as:

$$f = \frac{R_m}{L_1} \frac{V_{out}}{V_H - V_L} \left(1 - \frac{V_{out}}{V_{in}}\right) \qquad (4)$$

where (from equations (1) and (2)) T_{ON} and T_{OFF} time intervals (charge and discharge of the inductor L_1, respectively) in every switching period are given by:

$$T_{ON} = \frac{L_1}{R_m} \frac{V_H - V_L}{V_{in} - V_{out}} \quad ; \quad T_{OFF} = \frac{L_1}{R_m} \frac{V_H - V_L}{V_{out}} \qquad (5)$$

The graphs in figure 9 show how the switching frequency (normalized to the maximum frequency) varies as a function of the output voltage (normalized to the input voltage V_{out}/V_{in}) and as a function of the input voltage (normalized to the

output voltage V_{in}/V_{out}). Notice that, on the one hand, fixing the input voltage V_{in}, the maximum switching frequency is given when $V_{out}=V_{in}/2$. On the other, for a given output voltage, whatever greater is the input voltage, greater is the switching frequency.
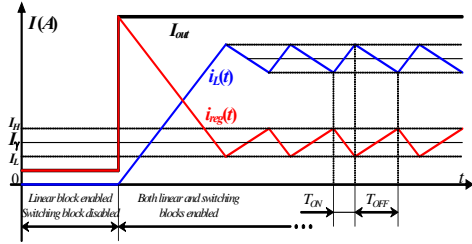

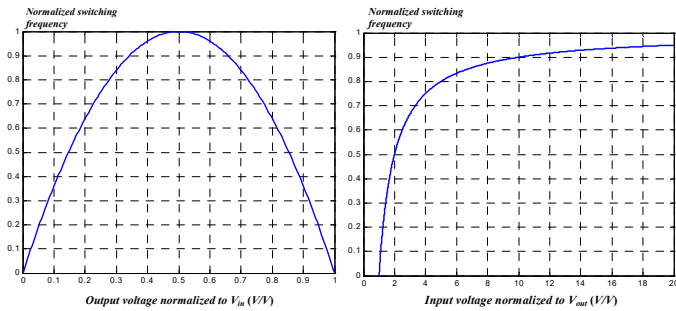Fig. 8. Principle of operation of a linear-assisted converter with strategy of control B.

Fig. 9. Switching frequency normalized to the maximum frequency as a function of the output voltage (normalized to the input voltage, V_{out}/V_{in}) and as a function of the input voltage (normalized to the output voltage, V_{in}/V_{out}).

Note that, in contrast to the strategy A, with this new strategy, the linear regulator can be considered as the "main" block, and the switching converter as the auxiliary block. This one "assists" to the first one when an excess current bigger than the threshold I_{γ} circulates through the linear regulator.

It is important to emphasize that reducing the value of the power dissipated in the pass transistor of the linear regulator increases the efficiency of the set, even with significant output currents. Therefore, it is important to fix the current limit I_{γ} to a commitment value between the minimum necessary to operate the regulator properly but without penalizing its good characteristics of regulation. Thus, considering commercial model of voltage linear regulators, this value is around few mA. For example, for the LM317 from National Semiconductor, this value goes up to around 3.5 mA typically (minimum load current). What is more, with the purpose of obtaining a good regulation of the output, without significant ripple in it, it is mandatory that the current provided by the linear regulator is bigger than zero. In fact, in figure 10 we can appreciate the output current and the current flowing through the inductor and the linear regulator when the switching threshold current I_{γ} is adjusted to 50 mA. In this simulation the reference voltage $V_Z=5$ V. Transient response of the converter can be observed with $V_{in}=10$ V. It is also shown the circuit response to a step of the converter input voltage from 10 V to 13 V at $t=20$ µs, as well as the transient from a reduction of the load resistance of the 100%, from 5 Ω

to 2.5 Ω at $t=40$ µs. Notice that the regulation of the output voltage is excellent.
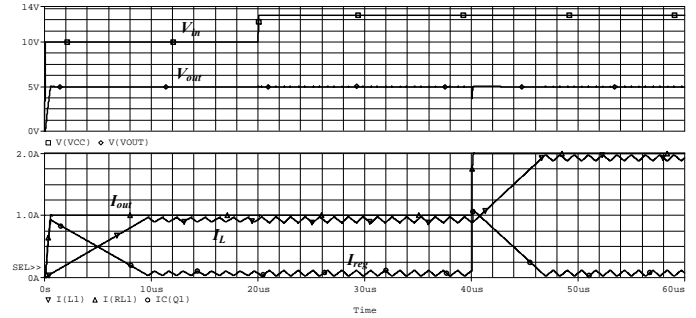

Fig. 10. Response of the converter shown in figure 7 with $V_{in}=10$ V. In addition, it can be seen the circuit response to a step of the input voltage from 10 V to 13 V at $t=20$ µs, and a variation in the load resistance from 5 Ω to 2.5 Ω at $t=40$ µs. The switching threshold current I_{γ} has been adjusted to 50 mA.

The output voltage and the base-emitter voltage of transistors Q_{2a} y Q_{2b} at steady state are shown in figure 11. Comparing these graphs with those in figure 6, shown in the same conditions, it becomes evident that with the proposed approach (realization B) the output ripple is reduced significantly.
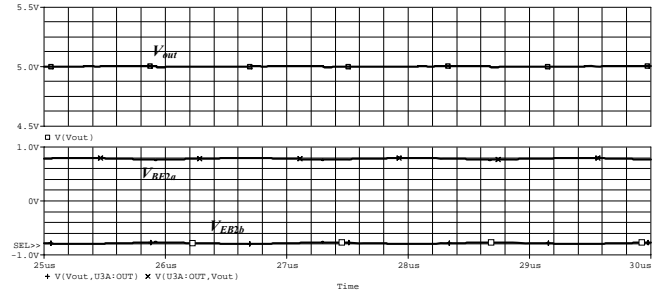

Fig. 11. Detail of the output voltage ripple and base-emitter voltage of transistors Q_{2a} y Q_{2b} of the linear regulator in the steady state in figure 7.

In figure 12 we can appreciate the system behavior when the threshold current I_{γ} is 5 mA. Notice that the regulation of the output voltage gets worse significantly. It is accentuated when I_{γ} is reduced down to a value near to zero. Therefore, the switching current threshold must be a value such that: (1) It significantly does not increase the power dissipation of the pass transistor in the linear regulator and does not diminish excessively the efficiency of the regulator, and (2) It does not significantly deteriorate the regulation of the output voltage.

Thus, we can denominate this type of control as a ***strategy control with nonnull average linear regulator current***. For instance, for a practical implementation of a linear-assisted converter using discrete components on board, for load currents lower than 10 A, the suitable value of I_{γ} that fulfills the two previous conditions is found to be between 10 mA and 50 mA.

Finally, notice that if the load current is below I_{γ}, the switching block (the DC/DC converter) is disabled in order to minimize its losses. Thus, only the linear regulator provides the output current for slight load conditions. Figure 13 shows the experimental efficiency versus the load current for the two strategies. It is shown the comparison of the control

strategy *A* and the proposed by authors (strategy *B*) for V_{out}=5 *V*. It is shown four different I_γ values: 0 *mA* (strategy *A*), and 10 *mA*, 50 *mA* and 100 *mA* (all three for strategy *B*). Note that, if I_γ is low, the efficiency is not almost affected, reducing the output ripple too.
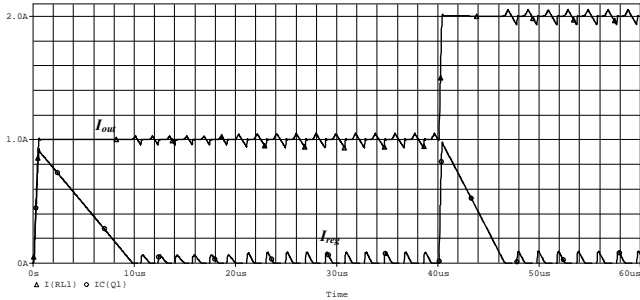
Fig. 12. Detail of the output current I_{out} and the linear regulator current I_{reg} at the start transient of the converter in figure 7 with V_{in}=10 *V*. It can also be observed the response of the circuit to an input voltage step from 10 *V* to 13 *V* at *t*=20 µ*s*, and a variation in the load resistance from 5 Ω a 2.5 Ω at *t*=40 µ*s*. The switching threshold current I_γ is fixed at 5 *mA*.
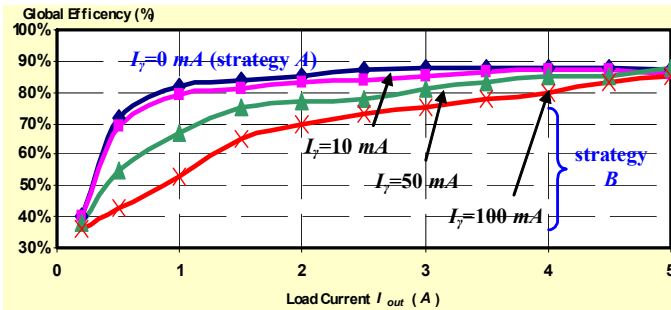
Fig. 13. Experimental efficiency for the control strategy *A* and the proposed by the authors (strategy *B*) with V_{out}=5 *V*. It is shown four different I_γ values: 0 *mA* (strategy *A*), and 10 *mA*, 50 *mA* and 100 *mA* (all three for strategy *B*).

IV. IMPROVEMENT OF THE LINEAR-ASSISTED CONVERTER WITH CONTROL STRATEGY *B*

Studying the preceding figures, it is possible to ask for the necessity or not of using the transistor PNP Q_{2b} in the scheme of figure 7, since this one, in steady state (and unlike the strategy *A*), always remains in cut. However, the inclusion of the same one is necessary to increase the response speed of the linear regulator from decremental variations of the load current. In fact, since it has been reflected in the preceding figures, one of the objectives of the linear regulator, besides obtaining an excellent regulation of the output voltage, frees of ripples, is to provide fast current responses when abrupt variations of the load consumption exist. In this way, the switching DC/DC converter cannot respond to those variations of the output current. Thus, this current transients must be provided (or absorbed, depending on if the variation of the load current is incremental or decremental) by the linear regulator.

In the previous figures this can be appreciated when the consumption of the load increases from an initial value (in this case 1 *A*) to another end value greater (equal to 2 *A*). Nevertheless, it is important to notice that, if the response wants also to be maintained for descendent variations of the

load current, the voltage linear regulator must incorporate necessarily the transistor Q_{2b} (in both figure 2 and figure 7) to allow bidirectional output currents.

In figure 14 we can appreciate the response of the proposed hybrid convert in figure 7 without the Q_{2b} transistor, when we have an increasing step of the load current at *t*=40 µ*s* and a decreasing variation at *t*=60 µ*s*. Note that the answer provided by the linear regulator for ascending variations of the load current is good enough, and allows, therefore, to maintain the output voltage of the set constant during the transient. However, the response of the set is not appropriate for descendent variations, being the response time of the set marked by the switching converter, losing the load regulation at that time interval.
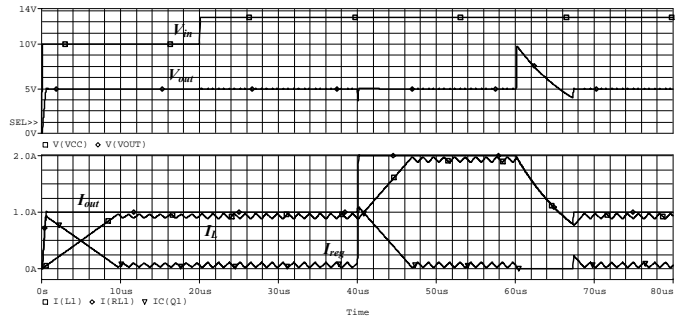
Fig. 14. Detail of the lack of load regulation when the load current changes from 2 *A* to 1 *A* at *t*=60 µ*s* for the converter in figure 7 without the transistor Q_{2b} (variation in the load resistance from 2.5 Ω to 5 Ω). The switching threshold current is adjusted to 50 *mA*.

However, if in the hybrid converter in figure 7 transistor PNP Q_{2b} is added, the response of the converter improves significantly when the load current decreases. In figure 15 we can appreciate that, when a decreasing step of the output current takes place from 2 *A* to a 1 *A* at *t*=60 µ*s*, the transistor Q_{2b} included in the linear regulator can absorb the excess of current that, provided by the inductor L_1, the load no longer accepts. Thus, the linear regulator can maintain an output voltage with good regulation (and, therefore, free of ripples) even with decreasing transients. Finally, figure 16 shows experimental details of the load regulation when the load current changes from 5 *A* to 1.4 *A* for the implemented converter in figure 7 without (figure 15.*a*) and with (figure 15.*b*) the transistor Q_{2b}. The switching threshold current is adjusted to 50 *mA*.
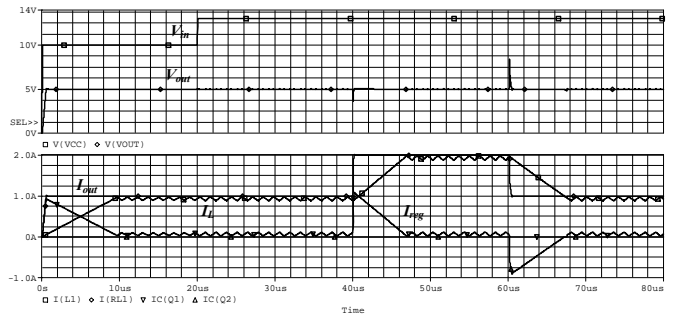
Fig. 15. Detail of the improvement obtained in the load regulation when the load current changes from 2 *A* to 1 *A* at the time instant *t*=60 µ*s* for the converter in figure 7 with the transistor Q_{2b} (variation in the load resistance from 2.5 Ω to 5 Ω). The switching threshold current is adjusted to 50 *mA*.

V. Conclusions

The present article has shown the comparative of two strategies of control sensibly different for power DC/DC linear-assisted (or hybrid) converters based on the association of a linear regulator in parallel with a switching converter. The first of the two strategies (strategy *A* or with **null average value in the linear regulator current**) allows to obtain a high efficiency, similar to switching converters because, in the steady state, the power dissipated in the linear regulator is practically zero. However, it has as inconvenient the presence of a ripple output voltage because the pass transistor of the output linear stage is switching between the cut and the conduction in every switching period.

The proposal presented in the article (strategy of control *B* or **nonnull average value in the linear regulator current**), allows a little current through the linear stage that causes that the efficiency of the set diminishes slightly. However, it allows to obtain an output voltage practically free of spurious ripples.

The article allows to affirm that, the maximum value of the current that circulates through the linear regulator (switching threshold current), must be fixed to a value of commitment so that it does not increase the power dissipation in the pass transistor of the linear regulator significantly and does not make excessively diminish the efficiency of the set, but does not deteriorate significantly the regulation of the output voltage.

Finally, note, as an additional advantage of linear-assisted converters with this second strategy, that typical low pass filter capacitors, which are required in switching converters (and whose values, in certain applications, can get to be important), in this case can be suppressed, since the own linear regulator already makes the low pass filter function. Therefore, from this point of view, it can be said that, in an effective form, the voltage linear regulator acts as an active low pass filter, removing high frequency components generated in the modulation process.

Acknowledgment

References

[1] C. K. Chava, J. Silva-Martínez. "A Frequency Compensation Scheme for LDO Voltage Regulators". *IEEE Transactions on Circuits and Systems–I: Regular Papers*, vol. 51 (nº 6): pp. 1041-1050, June 2004.

[2] R. J. Milliken, J. Silva-Martínez, E. Sánchez-Sinencio. "Full On-Chip CMOS Low-Dropout Voltage Regulator". *IEEE Transactions on Circuits and Systems–I: Regular Papers*, vol. 54 (nº 9): pp. 1879-1890, September 2007.

[3] V. Grupta, G. A. Rincón–Mora, P. Raha. 'Analysis and Design of Monolithic, High PSR, Linear Regulator for SoC Applications'. *Proceedings of the IEEE International SoC Conference*: pp. 311–315, 2004.

[4] R. W. Erickson, D. Maksimovic. '*Fundamentals of Power Electronics*'. 2nd edition, Ed. Kluwer Academic Publishers, 2001.

[5] J. G. Kassakian, M. F. Schlecht, G. C. Verghese. '*Principles of Power Electronics*'. Ed. Addison–Wesley, 1991.

[6] N. Mohan, T. M. Underland, W. P. Robbins. '*Power Electronics: Converters, Applications and Design*'. Ed. John Wiley & Sons, 1989.

[7] X. Zhou, P. L. Wong, P. Xu, F. C. Lee, A. Q. Huang. 'Investigation of Candidate VRM Topologies for Future Microprocessors'. *IEEE Transactions on Power Electronics*, vol. 15 (nº 6): pp. 1172–1182, November 2000.

[8] B. Arbetter, D. Maksimovic. 'DC–DC Converter with Fast Transient Response and High Efficiency for Low–Voltage Microprocessor Loads'. *IEEE Applied Power Electronics Conference*, pp. 156-162. 1998.

[9] P. Midya, F. H. Schlereth. 'Dual Switched Mode Power Converter'. *IECON. Industrial Electronics Society*: pp. 155–158, 1989.

[10] F. H. Schlereth, P. Midya. 'Modified Switched Power Convertor with Zero Ripple'. *Proceedings of the 32nd IEEE Midwest Symposium on Circuits and Systems (MWSCAS'90)*: pp. 517–520, 1990.

[11] V. Yousefzadeh, E. Alarcón, D. Maksimovic. 'Band Separation and Efficiency Optimization in Linear–Assisted Switching Power Amplifiers'. *Proceedings of the 37th IEEE Power Electronics Specialists Conference, 2006* (PESC'06), pp. 1-7, 18-22 June 2006.

[12] R. Vázquez, A. Barrado, E. Olías, A. Lázaro. 'Theoretical Study and Implementation of a High Dynamic Performance, High Efficiency and Low Voltage Hybrid Power Supply'. *Proceedings of the IEEE 32nd Annual Power Electronics Specialists Conference, 2001* (PESC 2001), vol. 3: pp. 1517–1522. 17-21 June 2001.

[13] A. Barrado, R. Vázquez, E. Olías, A. Lázaro, J. Pleite. 'Theoretical Study and Implementation of a Fast Transient Response Hybrid Power Supply'. *IEEE Transactions on Power Electronics*, vol. 19 (nº 4): pp. 1003-1009, July 2004.

[14] X. XXX, X. XXX. "Modeling of Linear-Assisted DC–DC Converters". European Conference on Circuit Theory and Design 2007 (ECCTD 2007), 26th-30th August 2007.

[15] X. XXX, X. XXX, X. XXX. "Modeling of Linear & Switching Hybrid DC–DC Converters". 12th European Conference on Power Electronics and Applications (EPE 2007), September 2007.
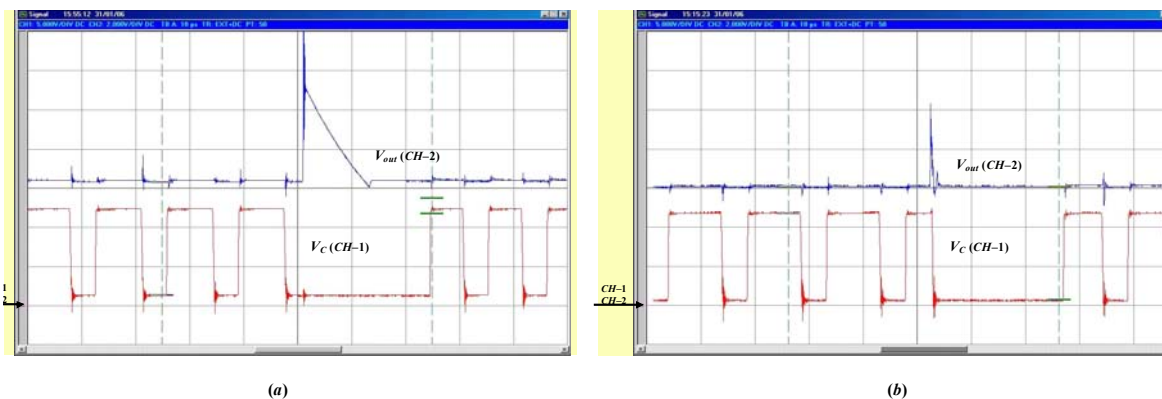
(a)   *(b)*

Fig. 15. Experimental results of the load regulation when the load current changes from 5 *A* to 1.4 *A* for the implemented converter in figure 7 without and with the transistor Q_{2b}. The switching threshold current is adjusted to 50 *mA*.