# Optimal Design of a Three-Phase AFPM for In-Wheel Electrical Traction

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Abstract—Sinusoidally fed permanent magnet synchronous motors (PMSM) fulfill the special features required for traction motors to be applied in electric vehicles (EV). Among them, axial flux permanent magnet (AFPM) synchronous motors are especially suited for in-wheel applications. Electric motors used in such applications must meet two main requirements, i.e. high power density and fault tolerance. This paper deals with the optimal design of an AFPM for in-wheel applications used to drive an electrical scooter. The single-objective optimization process carried out in this paper is based on designing the AFPM to obtain an optimized power density while ensuring appropriate fault tolerance requirements. For this purpose a set of analytical equations are applied to obtain the geometrical, electric and mechanical parameters of the optimized AFPM and several design restrictions are applied to ensure fault tolerance capability. The optimization process is based on a genetic algorithm and two more constrained nonlinear optimization algorithms in which the objective function is the power density. Comparisons with available data found in the technical bibliography show the appropriateness of the approach developed in this work.

Keywords—Permanent fault tolerance; magnet: optimization; genetic algorithm.

## NOMENCLATURE

$P_R$ :	Rated power
<i>m</i> :	Number of phases
$m_1$ :	Phases per stator. It is unity in the case of one stator
<i>p</i> :	Number of pole pairs
f:	Electric frequency
Q:	Number of slots in the stator
$K_e$ :	EMF factor incorporating the winding distribution
	factor and the radio between the area spanned by the salient poles and the total air gap area
$K_i$ :	Form factor of the electric current wave = $I_{pk}/I_{RMS}$
$K_p$ :	Form factor of the electric power wave

Slot fill factor  $K_{cu}$ : Carter coefficient  $K_c$ : Overall machine efficiency  $\eta$ : Air gap flux density  $B_g$ : Stator core flux density  $B_{cs}$ :

 $A_s$ : Stator electrical loading

 $f_b$ : Rated or base converter frequency

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Base angular electrical frequency =  $2\pi f_b$  $\omega_b$ : Pole pairs number  $N_{ph}$ : Number of turns per phase Effective stack length  $L_r$ : Rotor axial length Rotor core axial length  $L_s$ : Stator axial length  $L_{cs}$ : Stator core axial length Permanent magnets axial length  $L_{PM}$ :

Air gap length g:

 $B_r$ : Remanent flux density of the permanent magnets  $B_{\nu}$ : Attainable flux density on the surface of the permanent magnets

 $B_{cr}$ : Flux density in the rotor core

 $B_{cs}$ : Flux density in the stator core

 $J_s$ : Current density

 $\mu_{r.PM}$ : Relative permeability of the permanent magnets

Flux leakage factor

 $W_{cuo}$ : Outer protrusion in the radial direction of the end

winding

 $W_{cui}$ : Inner protrusion in the radial direction of the end

winding

 $D_o$ : Outer surface diameter of the AFPM

 $D_t$ : Total outer diameter  $D_g$ : Average diameter  $D_i$ : Inner diameter

 $K_l$ : Aspect ratio coefficient =  $D_g/L_e$ 

λ: Ratio between the inner and outer diameters =  $D_i/D_o$ 

 $I_{s.N}$ : Rated stator current

 $V_{ph,N}$ : Rated phase-to-neutral voltage

Nominal flux linkage  $\psi_N$ :

## I. INTRODUCTION

Electric vehicles (EVs) are attractive due to several benefits compared to internal combustion engine powered vehicles, including low emissions, higher efficiency, quieter operation, less maintenance costs, stronger acceleration or lower fuel price, among others. However, their main drawbacks are associated to batteries, which have a limited driving range, long recharge time and high cost [1].

In part due to the limitations of the battery pack, EVs require traction motors with especial features, including high efficiency [2], high power and torque density, compactness, precise torque control, extended speed range [3,4]. Sinusoidally fed PMSMs are also compatible with adjustable speed ac inverter drives since they are compatible with advanced control techniques thus transferring them of enhanced controllability when compared to rectangular-fed brushless dc permanent magnet motors (BLDC) [5]. Due to the abovementioned appealing features, sinusoidally fed PMSMs are being applied as traction motors in EVs.

AFPM synchronous motors are disc-shaped and very compact, therefore being a valid solution for direct drive inwheel applications [6]. The direct drive motor allows simplifying the mechanical structure of the vehicle, thus increasing overall efficiency and minimizing vehicle weight. AFPMs also show an inherent anti-lock braking system (ABS) capability since they can generate a negative torque [7]. In addition, kinetic energy can be recovered during braking stages by applying a regenerative braking strategy. Due to their disclike shape, AFPMs allow different designs including multiple or single air gaps, with slots or slot less configurations or ironless designs [8]. These types of machines are often classified into internal stator (torus) and internal rotor topologies, depending on the function of the central disk. The torus topology includes both NN and NS configurations, where NS refers to a north pole N facing a south pole S placed at the other side of the stator [7].

This paper deals with the internal stator or torus topology, which has two outer rotor discs in a NN configuration. The axially magnetized permanent magnets are glued to both inner faces of the rotor discs. The stator is made of strip wound steel and contains concentrated back-to-back connected windings wounded inside the slots [8]. These radial windings, which are wounded in the radial direction, are required to produce the electromagnetic torque. Due to the multiple air gaps configuration, the use of back-to-back windings allow minimizing copper losses due to the reduced end windings length when compared with other configurations, thus enhancing overall efficiency [3].

Fig. 1 shows a dual outer rotor AFPM topology with NN configuration.

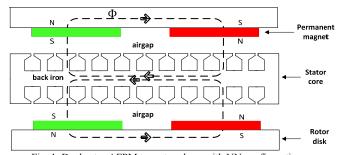


Fig. 1. Dual rotor AFPM torus topology with NN configuration.

Electric machines have a large number of design parameters. Therefore obtaining an optimized design is a challenging task because of the high number of sets of possible solutions involved. The joint use of accurate analytical sizing equations combined with the application of optimization algorithms based on artificial intelligence can help researchers

and engineers to obtain an improved and faster solution of this complex problem.

Therefore, design optimization of electric machines is nowadays receiving much attention as deduced from the number of recently published papers in this topic [9, 10]. This paper is focused to obtain an optimal solution among the huge set of possible solutions by using computationally efficient optimization algorithms leading to a global optimum solution while minimizing the computational burden.

Fault tolerance is a must in safety-critical applications such as in automotive applications. In this paper a set of analytical equations are applied to obtain the geometrical, electric and mechanical parameters of the optimized AFPM and several design restrictions are applied to ensure fault tolerance capability. Some requirements must be accomplished to design fault tolerant machines, including in electric, magnetic, physical, and thermal isolation among phases [11], so phase-to-phase faults probability is minimized [12]. To this end, single-layer fractional slot concentrated windings are particularly appropriate.

In this paper a dual outer rotor AFPM with NN configuration for automotive applications is optimized by applying accurate analytical sizing equations and taking into account fault tolerant constraints assuring a design suited for high requirements applications. To this end three constrained nonlinear optimization algorithms, which include a genetic algorithm (GA) have been applied to optimize the motor when the objective function to be optimized (maximized) is the power density.

### II. THE ANALYZED AFPM MACHINE

The AFPM optimized in this paper is an in-wheel motor for an urban scooter. Fig. 2 shows the main machine dimensions whereas Table I shows the main motor parameters [13] as well as some of the restrictions considered in the design and optimization processes.

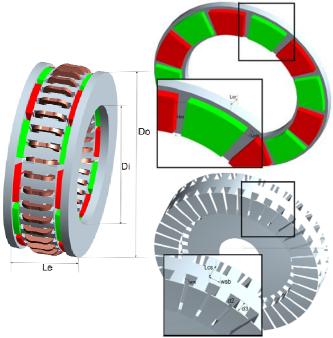


Fig. 2. Motor main dimensions.

As shown in Fig. 2, trapezoidal magnets are used since this geometry allows minimizing the torque ripple in this kind of machines [3].

TABLE I. Main Parameters Of The Analyzed AFPM

Dimensional constraints			
Machine outer diameter	$D_o$	< 300 mm	
Inner to outer diameter ratio	$\lambda = D_i/D_o$	0.40 - 0.75	
Stator slots	Q	18	
Motor effective axial length	$L_e$	< 200 mm	
Air gap length	g	0.5 - 2.5 mm	
Air gap flux density	$B_{g}$	0.35 – 0.95 T	
Material	limitation		
Max. stator and rotor core flux densities	$B_{cs}$ , $B_{cr}$	< 1.5 T	
PM remanence	$B_r$	1.3 T	
PM relative permeability	$\mu_r$	1.05	
	ements		
Rated line-to-line voltage	$V_{L-L}$	< 100 V	
Input phase current (peak value)	$I_{s,peak}$	< 20 A	
Number of phases	m	3	
Number of stators	$m_1$	1	
Output power	$P_{out}$	1 kW	
Base electrical frequency	$f_b$	50 Hz	
Pole pairs	p	8	
Motor efficiency	$\eta$	> 80%	
Electric loading	$A_s$	10 - 30 kA/m	
Air gap flux density	$B_{g}$	0.35 - 0.95T	
Current density	$J_{s}$	$3.5 \text{ A/mm}^2$	
Ratio of the average to the peak air gap flux density	$lpha_l$	0.48	
Aspect ratio coefficient	$K_l$	0.7	
Electrical power waveform factor	$K_p$	0.5	
Current wave form factor	$K_i$	$\sqrt{2}$	
EMF factor	$K_{\mathrm{e}}$	$0.692/\eta$	
Copper fill factor	$K_{cu}$	0.228	
Carter coefficient	$K_c$	0.8	
Peak corrected factor of the air gap flux density	$K_f$	0.8	
Leakage flux factor	$K_d$	2/π	

## ANALYTICAL SIZING EQUATIONS OF THE AFPM

In this section the equations to size the AFPM are described. An analytical expression of the sizing equation for axial flux permanent magnet synchronous machines is given in [13],

$$P_{R} = \frac{m}{m_{1}} \frac{\pi}{2} K_{e} K_{i} K_{p} K_{l} \eta B_{g} A_{s} \frac{f}{p} (1 - \lambda^{2}) \frac{1 + \lambda}{2} D_{o}^{2} L_{e}$$
 (1)

where the physical variables and parameters in (1) are defined in the nomenclature section.

The selection of the ratio  $\lambda = D_i/D_o$  between the inner and outer diameters is critical in order to optimize machine performance, since it greatly influences the magnetic and electrical loadings. Although according to [14] the maximum value of  $\lambda$  is  $\frac{1}{\sqrt{3}}$ , in practice  $\lambda$  usually lies between 0.6 – 0.8 to maximize the maximum torque to weight ratio.

The machine total outer diameter  $D_t$  is related to the protrusion  $W_{cuo}$  of the end windings in the radial direction from the iron core [9] as,

$$D_t = D_O + 2W_{cuo} \tag{2}$$

Protuberances exist in both the axial and radial directions of the AFPM. The amplitude of the protrusions is related to the stator electrical loading  $A_s$ , current density  $J_s$ , and copper fill factor  $K_{cu}$  as,

$$W_{cuo} = \frac{\sqrt{D_o^2 + \frac{4A_s D_g}{K_{cuJ_s}}} - D_o}{2}, \quad W_{cui} = \frac{\sqrt{D_i^2 + \frac{4A_s D_g}{K_{cuJ_s}}} - D_i}{2}$$
 (3)

The effective stack or axial length of the AFPM depends on the of rotor and stator axial lengths as,

$$L_e = L_s + 2L_r + 2g \tag{4}$$

The axial length of the stator is related to the stator core axial length and the amplitude of the protrusions by,

$$L_s = L_{cs} + 1.6W_{cui} \tag{5}$$

where the axial length of the stator core may be calculated from the magnetic flux density in the air gap  $B_g$ , the stator core flux density  $B_{cs}$  and the ratio  $\lambda = D_i/D_o$  as,  $L_{cs} = \frac{B_g \pi D_o (1+\lambda)}{B_{cs} 4p}$ 

$$L_{cs} = \frac{B_g \pi D_o(1+\lambda)}{B_{cs} 4p} \tag{6}$$

Similarly, the axial length of the rotor  $L_r$  may be obtained from the axial length of rotor core  $L_{cr}$  and the length of the permanent magnets  $L_{PM}$  as,

$$L_r = L_{cr} + L_{PM} \tag{7}$$

$$L_{PM} = \frac{\mu_{r,PM} + B_g}{0.95B_r - \frac{1}{K_d} B_u} (g + W_{cui})$$
 (8)

Note that (8) depends on the PM relative permeability and remanent flux density,  $\mu_{r,PM}$  and  $B_r$  respectively, the flux density  $B_u$  at the surface of the PMs, and a flux leakage factor

The axial length of the rotor core  $L_{cr}$  may be expressed as:

$$L_{cr} = \frac{B_u \pi D_o(1+\lambda)}{8B_{cr} p} \tag{9}$$

 $B_{cr}$  being the flux density in the rotor core.

Since the PMs are placed in the rotor discs, whereas an AC magnetic flux flows through the stator core, the flux flowing through the rotor core is almost constant.

According to [13] there is a link between the electric frequency and the stator core flux density, which may be expressed as,

$$B_{cs} = \begin{cases} 5.47 f^{-0.32} \text{ T } f > 40 Hz\\ 1.7 - 1.8 \text{ T } f \le 40 Hz \end{cases}$$
 (10)

In addition, the rotor core flux density should be within the interval,

$$B_{cr} = 1.6 - 1.8 \text{ T}$$
 (11)

 $B_{cr} = 1.6 - 1.8 \text{ T}$  (11) The air gap flux density in an AFPM may be expressed as:

$$B_a = K_d B_u \tag{12}$$

The electrical loading  $A_s$  in AFPMs is a function of the machine average diameter  $D_g$ :

$$A_s = 2mN_{ph} \frac{I_{s,N}}{\pi D_a} \tag{13}$$

where  $D_g$  is calculated as,  $D_g = \frac{(D_0 + D_i)}{2}$ 

$$D_g = \frac{(D_0 + D_i)}{2} \tag{14}$$

The number of slots per phase and per phase and pole pair and per pole are calculated respectively as,

$$q_{mp} = Q/m \tag{15}$$

$$q_{mp} = Q/pm \tag{16}$$

The number of turns per phase is calculated as,

$$n_s = N_{ph}/q \tag{17}$$

The air gap inductance is defined by, 
$$L_g = \frac{n_s^2 \mu_{r,PM} \mu_0 \theta_c (D_0^2 + D_i^2) k_d}{8(L_{PM} + 2\mu_{r,PM} k_c g)} \tag{18}$$

where  $\theta_c = 2\pi/2p$  is the angular coil pitch.

The slot inductance is obtained as,

$$L_{s} = n_{s}^{2} \left[ \frac{\mu_{0} d_{3}}{3w_{ch}} + \frac{\mu_{0} d_{2}}{0.5(w_{s} + w_{ch})} \right] \left( \frac{D_{0} - D_{i}}{2} \right)$$
(19)

 $\omega_{sb}$  being is the slot width;  $\omega_s$  the slot opening,  $d_2$  the stator slot tip length and  $d_3$  the conductor slot depth as shown in Fig.

Therefore the phase inductance is calculated as,

$$L_{ph} = 2q_{mp}(L_q + L_s) \tag{20}$$

The slot resistance is calculated from the conductor resistivity  $\rho$  and the cross-section  $S_q$  as,

$$R_{s} = \frac{\rho n_{s}^{2} (D_{o} + D_{i})}{2k_{c} S_{q}}$$
 (21)

The phase resistance is calculated from the slot resistance as,

$$R_{ph} = 2q_{mp}R_s \tag{22}$$

The magnitude of the phase impedance results in,

$$Z_{nh} = |R_{nh} + j\omega L_{nh}| \tag{23}$$

The peak value of the electromotive force is obtained as,

$$EMF_{max} = K_e N_{ph} B_g \frac{f}{p} (1 - \lambda^2) D_o^2$$
 (24)

The peak value of the stator current is calculated as,

$$I_{s,max} = A_s \pi K_i \frac{(1+\lambda)}{2} \frac{D_o}{2mN_{ph}}$$
 (25)

Finally, the power density is calculated as:  $P_{den} = \frac{P}{\frac{\pi}{4} D_o^2 L_e}$ 

$$P_{den} = \frac{P}{\frac{\pi}{4}D_o^2 L_e} \tag{26}$$

#### RESTRICTIONS FOR MAXIMIZING FAULT TOLERANCE IV.

To ensure a high level of fault tolerance in electric machines, the phase windings should be arranged in independent modules, i.e. they should avoid as much as possible electric, magnetic, physical and thermal coupling [15, 16]. Magnetic isolation allows minimizing voltages induced in adjacent phases due to a fault current in the damaged phase. In addition, both physical and thermal isolation reduce the risk of faults between phases. Non-overlapping windings provide

minimum mutual inductance between phases, thus minimizing interactions between the faulty phase and the others, so they are highly recommended in fault tolerant machines.

Restrictions imposed in this paper to ensure a high level of fault tolerance capability in the analyzed three-phase AFPM are summarized below [16],

- 1. Non-overlapping single-layer fractional-slot concentrated windings are used. However, because of the low winding factor of single-layer windings, p should be similar but not equal to Q. Therefore, the following relationship between the number of stator slots Q and the number of pole pairs pshould be accomplished:  $2p = Q \pm 2$ .
- When dealing with single-layer windings, the harmonic content of both the MMF and EMF is higher than in double-layer windings, thus increasing acoustic noise and torque pulsation levels [16]. This problem may be minimized by selecting a suitable slot/pole ratio. The number of stator teeth must be an even multiple of the number of phases to reduce acoustic noise and vibrations, thus extending the service life of the shaft bearings. This results in Q = 6n, where n is an integer number [16]. This condition can be expressed as,

$$Q \pm 2 = 2p \tag{27}$$

3. To increase the phase inductances and reduce the short circuit currents, the slots in the stator should be deep enough [12]. The phase inductance calculated as  $Z_L$  =  $EMF/I_s$  must be close to 1 p.u., i.e.

$$Z_{ph} = \pi L_b \tag{28}$$

where the base value of the phase inductance  $L_b$  is calculated

$$L_b = \frac{\psi_b}{I_{aN}} \tag{29}$$

And the base value of the flux linkage is defined as,

$$\psi_b = \frac{V_{ph,N}}{\omega_b} \tag{30}$$

 $\omega_b = 2\pi f_b$  being the base electrical angular frequency.

Both the air gap and slot impedances  $L_g$  and  $L_s$  in (18) and (19), respectively, are adjusted during the optimization process to obtain unity phase impedance according to (28).

# THE OPTIMIZATION FUNCTIONS DEALT WITH

In this paper three optimization methods have been applied, namely genetic algorithm (GA), fmincon and fminimax solvers already implemented in the Matlab® environment.

Genetic algorithms (GAs) are a family of mathematical methods widely applied to solve optimization problems both constrained and unconstrained. GAs are search methods based on genetics and natural selection [10] and are being applied in the field of design optimization of electric machines [9,14]. In the case of electrical machines design optimization, GA searches the space of the motor parameters emulating genetic reproduction mechanisms, crossover, and mutation with the objective of obtaining an optimal design. GA recurrently modifies the population of individual solutions by randomly selecting at each step individuals from the current population. Therefore, GA generates in at each iteration a population of individuals, the best one approaching a local optimal solution. These selected specimens are the parents which generate the children individuals for the subsequent generation. This process is repeated over successive generations with the finality of obtaining population individuals evolving toward an optimal solution. GA may be applied to solve different optimization problems which cannot be solved by traditional methods that use the gradient information of optimization since GA doesn't use the gradient information. Therefore, GA may be applied even in problems with highly nonlinear, non-differentiable or stochastic objective functions [17].

In order to generate the next generation of individuals from the current population, GA uses the following rules at each step,

- 4. Individual's selection (parents) for the next generation.
- 5. Crossover operators which usually combine two parents' solutions to generate offspring or children solutions for the next generation.
- Mutation operators which allow maintaining genetic diversity from one generation to the next. They apply random changes to individual parents and to children solutions

Fig. 3 summarizes the steps involved in the GA method.

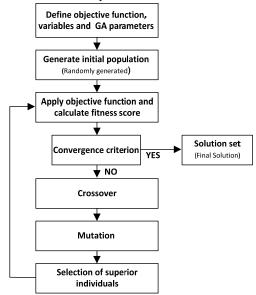


Fig. 3. Steps involved in the GA.

In machine design, there are a considerable number of free parameters. When aiming for an optimal solution, the task becomes extremely complex due to the huge number of possible combinations, unless the number of these free parameters is limited to some extent. In this paper the following eight parameters have been taken as input of the optimization algorithms: inner to outer diameter ratio, air gap flux density, air gap length, electric loading, number of turns per phase, stator slot tip length, slot opening and slot width.

In regards the coding part of the genetic algorithm, these parameters are taken as individuals, and then transformed into a binary string which will form the first chromosome.



Fig 4. Chromosome representation

In this study, the elitist method is used as the selection operator for scattered crossover. This method of reproduction generates a random binary vector, and then chooses the genes from the first parent in which the vector is a 1 and the genes from the second parent containing a 0, the combination of these genes forming the child.

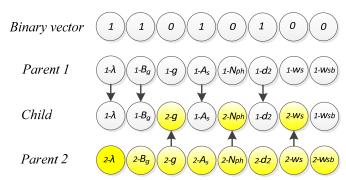


Fig 5. Scattered crossover representation.

The mutation operation randomly generates directions which are adaptive with respect to the last unsuccessful or successful generation. This process is repeated over successive generations with the finality of obtaining population individuals evolving toward an optimal solution.

Two more optimization solvers are used in this paper for comparison purposes, i.e. *fmincon* and *fminimax*. Both functions are included in the Matlab® Optimization Toolbox and can handle linear equalities and inequalities constraints, nonlinear inequality constraint functions and bound constraints.

The *fmincon* solver performs a constrained nonlinear minimization whereas the *fminimax* solver performs a minimax optimization.

Both *fmincon* and *fminimax* solvers are sequential quadratic programming (SQP) methods, i.e. nonlinear programming methods which allow solving constrained minimization problems. These quasi-Newton algorithms try to generalize the Newton's method to constrained optimization problems and are able to find local minima of constrained functions. They don't calculate the Hessian matrix, instead it is approximated by calculating different gradient vectors.

## VI. RESULTS

This section shows the results attained by applying the three aforementioned solvers, i.e. *ga*, *fmincon* and *fminimax*. Eight input variables which are shown in Table II are the input variables of the optimization algorithms in order to optimize the objective or fitness function, i.e. the power density.

TABLE II. INPUT VARIABLES FOR THE OPTIMIZATION ALGORITHM

Input variables to optimize the fitness function			
Input optimization variables	Symbol	Bounds	
Inner to outer diameter ratio	$\lambda = D_i/D_o$	0.40 - 0.75	
Air gap flux density	$B_g$	0.35 - 0.95 T	
Air gap length	g	0.5 - 2.5  mm	

Electric loading	$A_s$	10 - 30  kA/m	
Turns per phase	$N_{ph}$	2 – 100	
Stator slot tip length	$d_2$	1 – 4 mm	
Slot opening	$w_s$	1 – 40 mm	
Slot width	$w_{sb}$	2 – 40 mm	
Variables involved in linear inequalities			
Variables	Symbol	Inequalities	
		inequanties	
Machine outer diameter	$D_o$	< 300 mm	
Machine outer diameter  Motor effective axial length			
	$D_o$	< 300 mm	

Simulation results presented in this section are compared with those provided in [18]. Results provided by this reference work were tested on laboratory. This comprehensive method allows designing an arbitrary-capacity multi-parameter double-sided AFPM motor. Table III shows the results attained the optimization process when designing a standard AFPM, i.e. when no fault tolerant restrictions are applied.

TABLE III. RESULTS ATTAINEDWHEN NO FAULT TOLERANCE RESTRICTIONS ARE CONSIDERED

•	Ref. [18]	fmincon	fminimax	ga
$P_{den}$ [W/cm <sup>3</sup> ]	0.360	0.382	0.382	0.374
$D_o\left[\mathrm{m}\right]$	0.1640	0.1642	0.1642	0.1628
$N_{ph}$	70	70	73	73
$A_s$ [A/m]	15198	15000	15000	15100
g [mm]	1.1	1.0	1.0	1.0
$L_e$ [mm]	_	82.6	82.6	84.5
$L_{PM}$ [mm]	3.6	2.5	2.5	2.7
$L_{cr}$ [mm]	13.0	13.4	13.4	13.2
$L_{cs}$ [mm]	13.0	13.0	13.0	13.0
$B_g$ [T]	0.48	0.46	0.46	0.47
λ [p.u.]	0.58	0.50	0.50	0.49
η[p.u.]	0.915	0.950	0.940	0.948

Values shown in Table III show that the results attained by applying the three optimization methods are similar to those presented in [18], thus validating the approach applied.

Fig. 6 shows the evolution of the results attained by means of the three studied optimization algorithms.

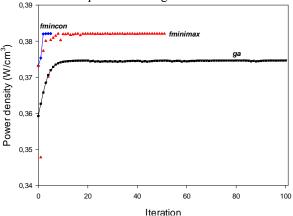


Fig. 6. Fitness function variation when applying the *fmincon*, *fminimax* and *ga* solvers with no fault tolerant restrictions.

According to the results presented in Fig. 6, both *finincon* and *fininimax* algorithms are faster than *ga* in attaining the optimal solution, and in this specific case they also provide a better solution (higher power density).

TABLE IV. RESULTS ATTAINED CONSIDERING FAULT TOLERANCE RESTRICTIONS

	fmincon	fminimax	ga
$P_{den}$ [W/cm <sup>3</sup> ]	0.331	0.322	0.352
$D_o$ [m]	0.1654	0.1672	0.1637
$N_{ph}$	73	73	72
$A_s$ [A/m]	15000	14801	15000
g [mm]	1	1	1
$L_e$ [mm]	87.6	87.7	85.4
$L_{PM}$ [mm]	1.8	1.6	2.3
$L_{cr}$ [mm]	11	11	12.4
$L_{cs}$ [mm]	13	13	13
$B_g[T]$	0.44	0.43	0.45
λ[p.u.]	0.44	0.43	0.46
η[p.u.]	0.84	0.89	0.88

By comparing the results shown in Tables III and IV, it is observed that when applying the fault tolerance restrictions the AFPM's power density unavoidably decreases by a factor less than 8% in the case analyzed. In addition the efficiency also decreases approximately by 7%. In this case the *ga* solver provides the better solution. These results show the effectiveness of the *ga* solver in facing a nonlinear problem such as the fault tolerant design of an AFPM.

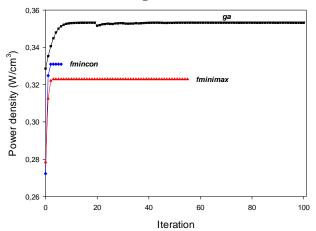


Fig. 7. Fitness function variation when applying the *finincon*, *fininimax* and *ga* solvers with fault tolerant restrictions.

## VII. CONCLUSIONS

In this paper an optimization process to design an in-wheel electric motor for an electric scooter has been analyzed. Concretely, a three-phase axial flux permanent magnet synchronous motor has been optimized based on in its power density by applying a set of sizing analytical equations which deal with the main geometrical, electric and mechanical parameters that define the machine. Comparisons with optimized motors data found in the technical literature show the accuracy of the applied approach since similar power densities are achieved in comparison with previous designs, even when applying fault tolerant constraints. As expected the efficiency is somewhat lowered in a fault tolerant machine mainly due to inductance constraint, because to achieve such high values of inductance an oversized stator is a must, although this could be overcome with an improved refrigeration system. In addition, fault tolerance conditions have been added to the optimization process in order to provide the new motor with fault tolerance capability, since it is required in safety-critical application such as the one analyzed in this paper. Results presented here shown the feasibility of the applied method to design electric motors with enhanced fault tolerance capability. In addition it has been shown that under this approach the power density of the fault tolerant optimized motor is decreased only by about 8% when compared with the reference optimized motor.

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