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3 Adaptive reconstruction of radar reflectivity in clutter-contaminated areas by
4 accounting for the space-time variability

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Abstract

Identification and elimination of clutter is necessary for ensuring data quality in radar Quantitative Precipitation Estimates (QPE). For uncorrected scanning reflectivity after signal processing, the removed areas have been often reconstructed by horizontal interpolation, extrapolation of non-contaminated PPIs aloft, or combining both based on a classification of the precipitation type. We present a general reconstruction method based on the interpolation of clutter-free observations. The method adapts to the type of precipitation by considering the spatial and temporal variability of the field provided by the multi-dimensional semivariogram. Six different formulations have been tested to analyze the gain introduced by each source of information: (1) horizontal interpolation, (2) vertical extrapolation, (3) extrapolation of past observations, (4) volumetric reconstruction, (5) horizontal and temporal reconstruction, and (6) volumetric and temporal reconstruction. The evaluation of the reconstructed fields obtained with the 6 formulations has been done (i) over clutter-free areas by comparison with the originally observed values, and (ii) over the real clutter-contaminated areas by comparison with the rainfall accumulations from a raingauge network. The results for 24 analyzed events (with a variety of convective and widespread cases) suggest that the contribution of extrapolation of past observations is not fundamental, and that the volumetric reconstruction is the one that overall adapted the best to the different situations.

1 Introduction

The production of radar Quantitative Precipitation Estimates (QPE) requires processing the observations to ensure their quality and its conversion into the variable of interest (e.g., precipitation rates near the surface). This processing is done through a chain of algorithms applied to mitigate the sources of uncertainty that affect radar observations: radar miscalibration, beam blockage, ground and sea clutter associated with anomalous propagation, path and radome attenuation, the vertical variability of precipitation combined with the loss of representativeness of radar observations with range, or the variability of the drop size distribution that controls the conversion of the measured variables into precipitation rate [e.g., Corral et al. (2009); Villarini and Krajewski (2009)].

Some of these algorithms involve the reconstruction of the meteorological signal in areas where the signal is lost (e.g., due to total beam blockage, severe path attenuation by heavy rain) or strongly contaminated, for instance, in the areas affected by ground or sea clutter.

Identification and reconstruction of clutter-affected areas is often part of the signal processing through the analysis of the Doppler spectrum [e.g., Doviak and Zrnic (1993)]. However, this approach is known to have some limitations (i) to distinguish precipitation from clutter in the areas with Doppler velocities near zero, and (ii) to reconstruct the precipitation signal. As a result this processing causes, in many cases systematic underestimation of precipitation [e.g., Hubbert et al. (2009); Moiseev and Chandrasekar (2009)].

Alternatively, other clutter elimination approaches are applied to the uncorrected moment data (typically, reflectivity). This requires first identifying clutter areas, through the analysis of statistical properties of radar measurements based on decision trees or fuzzy logic concepts [e.g., Steiner and Smith (2002); Berenguer et al. (2006); Gourley et al. (2007) and references therein]. Secondly, the reconstruction of the meteorological signal is done by either horizontal

interpolation or extrapolation from the non-contaminated PPIs aloft [e.g., Bellon et al. (2007) and Germann et al. (2006)]. A combination of the two was also proposed by Sánchez-Diezma et al. (2001) by adapting the reconstruction to the type of precipitation affecting clutter-contaminated areas: horizontal interpolation is used in widespread precipitation areas, and vertical extrapolation is preferred for convective cells with some vertical development. In this way, this method reduces the negative effects of strong gradients of the reflectivity field; i.e., widespread precipitation shows more variability in the vertical (specially related to the presence of the bright band and the weaker reflectivity of solid precipitation), while convective situations are typically characterized by high variability in the horizontal. Hereafter, we will refer to this method as SSDZ2001.

In this paper, we propose a new reconstruction method that avoids the pre-classification used by SSDZ2001 to choose between horizontal interpolation and vertical extrapolation. Instead, the proposed method uses the available observations (in the horizontal, in the vertical and from previous time steps) that are weighted based on the analysis of the spatial and temporal structure of the rainfall field. Section 2 presents the different formulations of the method, which has been used to reconstruct reflectivity fields in clutter-contaminated areas under different rainfall situations (see Section 3). Evaluation of the results is presented in Section 4.

2 Reconstruction method

Once clutter echoes are removed from radar reflectivity measurements, it is necessary to fill the resulting gaps with an estimate of the weather-related reflectivity. The reconstruction method proposed here capitalizes on the spatial and temporal structure of the reflectivity field [e.g., Zawadzki (1973)]. This section introduces first the general formulation of the proposed method and, secondly, the specific formulations adapted to the use of different observations in space and time.

82 **2.1 General formulation**

83 The reconstructed radar field at a location and time $\mathbf{x}=[x_o, y_o, z_o, t_o]$ is estimated as a linear
 84 combination of n clutter-free observations $Z(\mathbf{x}_i)$:

$$\hat{Z}(\mathbf{x}) = \sum_{i=1}^n \lambda_i Z(\mathbf{x}_i) \quad (1)$$

85 where λ_i is the weight given to the observation $Z(\mathbf{x}_i)$.

86 According to the Ordinary Kriging approach [e.g., Goovaerts (1997)], the optimal and
 87 unbiased estimate $\hat{Z}(\mathbf{x})$ can be obtained with the weights that are the solution of the following
 88 linear system:

$$\begin{bmatrix} \gamma_{11} & \cdots & \gamma_{1n} & 1 \\ \vdots & \ddots & \vdots & \vdots \\ \gamma_{n1} & \cdots & \gamma_{nn} & 1 \\ 1 & \cdots & 1 & 0 \end{bmatrix} \begin{bmatrix} \lambda_1 \\ \vdots \\ \lambda_n \\ \xi \end{bmatrix} = \begin{bmatrix} \gamma_1 \\ \vdots \\ \gamma_n \\ 1 \end{bmatrix}, \quad (2)$$

89 where γ_{ij} is the semivariogram for a separation vector $\Delta_{ij}=\mathbf{x}_i-\mathbf{x}_j$, and γ_i is the one for a
 90 separation vector $\Delta_i=\mathbf{x}_i-\mathbf{x}$. A Lagrange multiplier (ξ) is introduced to guarantee that the
 91 estimate $\hat{Z}(\mathbf{x})$ is unbiased. The semivariogram is a measure of the field variability and is
 92 generally defined as:

$$\gamma(\Delta) = \frac{1}{2} \text{var}[Z(\mathbf{x}) - Z(\mathbf{x} + \Delta)] \approx \frac{1}{2} \frac{1}{N(\Delta)} \sum_{k=1}^{N(\Delta)} [Z(\mathbf{x}_k) - Z(\mathbf{x}_k + \Delta)]^2 \quad (3)$$

where $\text{Var}[\]$ denotes the variance operator, Δ is the lag in space and time, and $N(\Delta)$ is the number of points used to estimate the semivariogram for a separation Δ . Based on (3), further details on how the semivariograms have been estimated are presented in Appendix A.

2.2 Implemented reconstruction method

The general method presented above has been implemented to reconstruct the reflectivity gaps using 4-Dimensional neighboring clutter-free observations ($Z(\mathbf{x}_i)$ in (1)): (i) within the PPI, (ii) in the closest non-contaminated PPI above, and (iii) the most recent radar volume scan (after compensating the effect of the motion). To illustrate the contribution of each of these components, the method has been configured as 3 formulations that use them separately (single-source formulations), and 3 other formulations that combine them.

2.2.1 Single-source formulations

2.2.1.1 HOR: Horizontal interpolation

The reflectivity estimate $\hat{Z}(\mathbf{x})$ at a given location and time $\mathbf{x}=[x_o, y_o, z_o, t_o]$ is reconstructed by interpolating the N_H neighboring non-contaminated observations on the same PPI and at the same time. That is, in (1), $Z(\mathbf{x}_i)=Z(x_i, y_i, z_o, t_o)$. In our case, we use the N_H neighboring non-contaminated observations within the band of pixels surrounding the areas to be reconstructed [as is usually done by the methods based on horizontal interpolation, e.g., Bellon et al. (2007)]. Consequently, the number of points used in this reconstruction method, N_H , depends on the size and shape of the clutter area to be reconstructed.

2.2.1.2 VERT: Vertical extrapolation

The reflectivity estimate $\hat{Z}(\mathbf{x})$ at a given location and time $\mathbf{x}=[x_o, y_o, z_o, t_o]$ is obtained by extrapolating the closest non-contaminated reflectivity observation in the vertical. Note that

the reconstruction performed in this way does not apply the Ordinary Kriging approach, because the estimate is obtained by direct vertical extrapolation of a single observation; i.e., $\hat{Z}(x_o, y_o, z_o, t_o) = Z(x_o, y_o, z_i, t_o)$, where z_i represents the height of the closest clutter-free PPI.

2.2.1.3 NOW: Extrapolation of past observations with the motion field

The reconstructed value is taken as the observation in the previous Quality-Controlled volume scan taking into account the effect of the motion of precipitation. The estimate at a given location and time $\mathbf{x}=[x_o, y_o, z_o, t_o]$ is obtained by following its trajectory backwards in time with a semi-Lagrangian scheme: $\hat{Z}(x_o, y_o, z_o, t_o) = Z(x_o - u \cdot \Delta t, y_o - v \cdot \Delta t, z_o, t_o - \Delta t)$, where (u, v) stands for the motion field of Z , and Δt is the time between two consecutive scans. Similarly as for the VERT method, this approach does not apply the Ordinary Kriging approach because the reconstruction is done by direct extrapolation in time.

This procedure is very similar to what is done in nowcasting algorithms to extrapolate reflectivity observations to the future. The tracking algorithm to estimate the motion field and the extrapolation technique used here are the same as those presented by Berenguer et al. (2011).

2.2.2 Multiple-source formulations

The combination of the observations used in the three methods of section 2.2.1 is explored here. The novelty of the formulations presented below is that they allow an adaptive combination of the different sources of information in the Ordinary Kriging framework. The structure of the field as depicted by the semivariogram determines the weight given to each observation in (1) through the linear system of (2).

2.2.2.1 HV: Volumetric reconstruction

This formulation combines the observations used in methods HOR and VERT. Consequently, $n=N_H+1$ observations are used in equations (1) and (2) for the reconstruction of $\hat{Z}(x_o, y_o, z_o, t_o)$: (i) N_H neighboring observations on the same PPI, $Z(\mathbf{x}_i)=Z(x_i, y_i, z_o, t_o)$, and (ii) one observation in the vertical extrapolated from the closest non-contaminated PPI above, $Z(\mathbf{x}_i)=Z(x_o, y_o, z_i, t_o)$

2.2.2.2 HN: Horizontal-temporal reconstruction

This formulation combines the observations used in methods HOR and NOW.

2.2.2.3 HVN: Volumetric-temporal reconstruction

This formulation combines the observations used in methods HOR, VERT and NOW.

3 Data and study domain

The analysis domain is the area covered by the Corbera de Llobregat single-polarization C-band Doppler radar, located near Barcelona, northeast of Spain (white diamond in Fig. 1). The region has torrential characteristics, and a good part of the yearly rainfall totals (ranging from 400 to 1000 mm) are frequently accumulated during a few events along the year.

The evaluation of the proposed method has been done over 24 rainfall events occurred between 2001 and 2005 (see details in Table 1). The radar data were collected at a frequency of 5620 MHz and with a beam width of 0.90° and up to 240 km in range. Every 10 minutes the radar scans 20 PPIs for elevations between 0.5° and 25° , with a resolution of 2 km in range and 0.86° in azimuth. As part of the processing of radar reflectivity data, we have applied the algorithm of Delrieu et al. (1995) to mitigate the effect of beam blockage by the terrain. Non-

meteorological echoes have been identified with the technique of Berenguer et al. (2006). It is based on a fuzzy-logic classifier that discriminates non-meteorological echoes from weather echoes using a number of statistical features that characterize the properties of ground and sea clutter. Finally, the reflectivity in clutter-contaminated areas has been reconstructed with the method presented in Section 2.

Also, the rainfall records obtained with the raingauges available over the area (see Fig. 1) have been used as reference in the evaluation.

4 Evaluation

We have applied the six formulations presented in section 2.2 to reconstruct clutter-contaminated reflectivity over the volume scans collected for the 24 rainfall events of Table 1.

The evaluation of their performance requires a reference. However, a direct reference is not available in the areas where the reflectivity field is contaminated by clutter. Here, we have assessed the quality of the reconstructed estimates: (i) by implementing the techniques over a clutter-free area where the originally observed values can be used as reference, and (ii) by comparing radar rainfall estimates with the observations of a raingauge network over the real clutter-contaminated areas.

Also, the performance of the proposed method has been compared with that of the technique by SSDZ2001 (see section 1), which is currently implemented in the operational radar QPE chain EHIMI (Corral et al., 2009).

4.1 Reconstruction over clutter-free areas

We have evaluated the reconstructed values by comparison with real radar observations over clutter-free areas [similarly as done by Sánchez-Diezma et al. (2001)]. Figure 1 shows the

observed clutter map in mean propagation conditions and the clutter-free areas where this analysis has been performed (violet shading). The latter has been chosen to have the same structure as the observed clutter map, but has been rotated to guarantee that the reference value is available (i.e., the original data in these locations are not contaminated by clutter). The evaluation has been done in terms of event rainfall accumulations. These have been obtained using a Marshall and Palmer (1948) Z-R relationship. Note that using this Z-R is a simplification aiming at analyzing the results of the clutter reconstruction in rainfall units [i.e., the impact of the Z-R variability and its relationship with the type of precipitation are neglected (e.g., Sempere-Torres et al., 1998)].

The results are first illustrated for two characteristic events (a typical widespread situation and a strong convective case, respectively events #20 and #21 in Table 1), and then summarized for the rest of the cases.

4.1.1 Widespread case: 11 May 2004

On 11 May 2004, a widespread rainfall system affected the radar domain for about 24 hours and produced a rather uniform accumulation field (indicated by the low coefficient of variation) with a maximum raingauge value of 21.6 mm (see Table 1 and Fig. 2 left).

Table 2 shows the scores computed for the accumulations estimated from the reflectivity fields reconstructed with the different formulations of the proposed method. For this event, the best scores are obtained with the formulations that include horizontal interpolation (similar score values are obtained with SSDZ2001, HOR, HV and HN). This could be expected, given the widespread nature of this event (with smooth gradients of the reflectivity field in the horizontal –this can also be seen in the cross section of Fig. 3). Consequently, the scatter plots between rainfall accumulations produced from the reference and the reconstructed reflectivity with these methods show a very good agreement (as can be seen in

Fig. 4 for HOR). On the other hand, the performance of VERT is affected by the strong variability of reflectivity in the vertical (see Fig 3 top). As a result, the accumulated rain is systematically overestimated where the reconstruction uses PPIs affected by the bright band, and underestimated where the reconstruction uses observations extrapolated from the snow levels (see Fig. 4, middle panel). The use of previous quality-controlled volume scans (included in NOW, HN and HVN) results in relatively good reconstructions of the accumulated values (with correlation values above 0.96, Table 2). However, the information from previous time steps does not contribute to improve the reconstruction: the scores obtained with HOR and HV are, respectively, as good or better than those obtained with HN and HVN.

4.1.2 Convective case: 02 September 2004

This event was a convective situation that lasted for around 18 hours with several convective cells affecting mostly the coastal area and over the sea. Some of these cells had an important vertical development (up to 14 km, see the bottom cross section of Fig. 3) and lasted for a few hours.

In this case, reconstruction by horizontal interpolation (HOR) produced rather poor results (the correlation value is 0.75, bottom part of Table 2). Instead, reconstruction by vertical extrapolation (VERT) produces better results. In particular, Fig. 5 shows that VERT is able to better reproduce the high accumulation values than HOR. The combination of these two formulations (HV) benefits from the adaptive use of vertical and horizontal interpolation at each location and time, resulting in better scores (Table 2). Interestingly, the best reconstructions of the total accumulation for this event were obtained with the formulations using the previous quality-controlled volume scans (specially NOW and HVN). As shown in Fig. 5, NOW shows smaller biases and better reproduction of large rainfall accumulations.

The nature of this situation (the largest convective cell in front of the coast in the southern part of the domain was rather stationary and lasted for about 4 hours) particularly favored the use of time information. Contrarily, for other kinds of convective events (e.g., situations with small fast-evolving convective cells with short life times), one would not expect such a good performance with NOW.

4.1.3 Evaluation over 24 events

To provide a more robust evaluation of the proposed reconstruction method, 24 events (between 2001 and 2005) were chosen. The analyzed cases (summarized in Table 1) include a wide variety of rainfall situations. Figure 6 shows the bias, mean absolute relative error (MARE), the Pearson correlation coefficient and the root mean square error (RMSE) obtained for the total rainfall accumulations estimated using the different formulations to reconstruct reflectivity in the violet areas of Fig. 1. In general, the formulations that use multiple sources of information (SSDZ2001, HV, HN, and HVN) outperform those using a single source of information (HOR, VER, and NOW). Similarly as shown before, VERT has difficulties in reconstructing the accumulations for the widespread cases (as it is clear, for example, in the correlation panel of Fig. 6). The use of previous volume scans alone (NOW) is systematically not as good as the use of horizontal information alone (HOR) except for event #21 (the one presented in section 4.1.2). The adaptive combined use of horizontal and vertical interpolation (HV and HVN) results in consistently better reconstructions than SSDZ2001, which is based on either using horizontal interpolation or vertical extrapolation based on the identified precipitation type. Between HV and HVN, the latter seems to be less robust in a few cases (e.g., events #3, #5, #19, and #20), which shows that the contribution of time information can be sometimes counterproductive in combination with horizontal and vertical information.

4.2 Radar-raingauge comparison

The comparison between raingauge records and radar rainfall estimates is done in terms of event-accumulated rainfall (G and R , respectively). Radar rainfall accumulations are obtained from the first PPI (0.5°) of the reconstructed volume scans using a uniform Marshall and Palmer (1948) Z - R relation and accounting for the motion of the precipitation field and for the evolution of rainfall intensities within consecutive reflectivity scans [as discussed by Fabry et al. (1994)]. Radar estimates in areas where reflectivity measurements are affected by ground clutter in mean propagation conditions have been obtained with the different reconstruction methods (the location of raingauges in clutter-contaminated areas can be seen in Fig. 1). We have identified these R - G pairs as light grey squares in the R - G scatterplots (see e.g., Fig. 7). Consequently, a good reconstruction of the reflectivity values in these areas would make the squares fall within the cloud of R - G pairs shown as black dots (for raingauge locations where radar measurements are not affected by ground clutter). This would indicate that the reconstructed R values behave similarly as those in clutter-free areas. Other than this, we cannot expect the reconstruction methods to improve the R - G scatterplots, because the differences between raingauge observations and radar estimates are explained by a number of other factors (out of the scope of this paper) such as radar calibration errors, radome and path attenuation, the effect of not considering the vertical profile of reflectivity, the variability of the Z - R relationship, representativeness differences between radar and raingauges, or gauge problems.

On the other hand, we have analyzed the impact of the reconstruction techniques on (a) the conditional probability of 10-minute radar accumulations to exceed 0.1 mm given that the collocated raingauge measures rainfall ($P(Z \geq 0.1 \text{ mm} \mid R \geq 0.1 \text{ mm})$, i.e., the probability of rainfall detection, POD), and (b) the conditional probability of the radar estimating some

rainfall when raingauges measure no rainfall ($P(Z > 0.1 \text{ mm} \mid R = 0 \text{ mm})$, i.e., the probability of false detection, POFD). Similarly to Berenguer et al. (2006), we have plotted the dependence of these scores as a function of range. In general, the POD tends to decrease with range due to the effect of beam overshooting in shallow precipitation, path attenuation, and the fact that the radar sampling volume becomes bigger with range.

4.2.1 Widespread case: 11 May 2004

Figure 7 shows the scatter plots between collocated radar and raingauge accumulations corresponding to this widespread case. The large scatter between radar and raingauge accumulations at those locations where radar observations are not affected by ground clutter (black dots in Fig. 7) can be in part explained by the effect of the vertical profile of reflectivity (the bright band peak was around 1.9 km and affecting the first PPI between 60 and 90 km, Figs. 2 and 3).

Similarly as shown in Section 4.1.1, the use of the reflectivity measurements from PPIs aloft to reconstruct clutter-contaminated reflectivity measurements in the first PPI (VERT) results in increased scatter compared to HOR and NOW (for the latter two, the grey squares fall within the cloud of black dots). Similar behavior is obtained with the formulations that include horizontal interpolation (SSDZ2001, HV, HN, and HVN), which results in the scores summarized in Table 3 (top).

The values of POD for HOR, NOW, and VERT (Fig. 8 left) are very close to 1.0 at near range while those of POFD (Fig. 8 right) are around 0.2. However, VERT systematically underdetects the occurrence of precipitation observed at ranges beyond 70 km (at these ranges both the POD and the POFD for the grey squares are systematically lower than for the black dots), due to the fact that the reconstruction uses observations extrapolated from the snow region and even above precipitation. It is also worth highlighting the poor POD values at two

raingauge locations by NOW. These two raingauges are located in the middle of a large ground clutter area on the north part of the domain, where the radar is scanning in the snow layers (more prone to underdetection), and where the apparent motion is slow. These factors result in that the reconstructed values are obtained by extrapolation from points where NOW was already applied in the previous quality-controlled scan. Because of this, NOW uses data extrapolated from around the clutter area that were actually recorded several time steps before. As expected for a widespread case, the POD and POFD graphs for HV, HN, HVN and SSDZ2001 (not shown) are very similar to those shown for HOR (Fig. 8 top).

4.2.2 Convective case: 02 September 2004

The scatter plots between radar estimates and raingauges observations are presented in Fig. 9. In general, the radar-raingauge comparisons at the clutter-free locations (black dots) agree well. For the reconstructed locations (light grey squares), HOR systematically underestimates raingauge accumulations and performs worse than VERT and NOW (consistently with the results seen in Section 4.1.2). The dependence of POD with range (Fig. 10) shows more variability than that for the widespread event and is not clearly affected by the poor performance of HOR. Instead, it produces a larger number of false detections (higher POFD).

On the other hand, the radar-raingauge plots for VERT and NOW are very similar and show less biased accumulations than HOR (Fig. 9). However, in terms of the POD and POFD (Fig. 10), the reconstruction obtained with NOW is clearly worse than VERT within the first 50 km: The bottom panels of Fig. 10 show that in these ranges, NOW underdetected rain and produced too many false detections (for some raingauges, POFD is over 0.4). We attribute this result to the fast evolution of the rainfall systems near the radar (including initiation and dissipation of small convective cells), which is not accounted for by the extrapolation of the rainfall from the previous time step. This factor affects the POD and POFD, where the

analysis is done in terms of 10-minutes accumulations, while it has a less important effect in terms of total event accumulations (as shown in Figs. 5 and 9) because misses and false detections seem to compensate.

The bottom part of Table 3 shows similar scores among the formulations that combine horizontal interpolation and vertical extrapolation (SSDZ2001, HV, and HVN), as a result of the flexibility of these formulations to weigh the most representative observations in each location and at each time step and confirming the results presented in section 4.1.2. The results in terms of POD for these formulations (not shown) are slightly better than VERT in terms, but this compensates with slightly worse performance in terms of POFD (in any case, still clearly better than the results obtained with HOR or NOW).

4.2.3 Evaluation over 24 events

Figure 11 summarizes the comparison between radar estimates and raingauges accumulations in terms of bias, MARE, correlation and RMSE for the 24 analyzed events and for all the formulations (similar as Fig. 6 for the analysis of the reconstruction over clutter-free areas).

The graphs show that for some events VERT and NOW clearly perform worse than the rest, and, to a lesser extent, the same happens with HOR (for instance in event #5). Besides this, very similar scores are obtained for most of the methods that combine different sources of information. However, this does not necessarily imply that the different methods perform similarly. As we have pointed out at the beginning of section 4.2, the interpretation of R-G scores is not straightforward and needs to be done considering (i) that the scores have been computed using all raingauges (in both clutter-free and clutter-affected areas) which in general reduces the differences between methods, and (ii) the effect of the error sources in radar QPE that have not been accounted in this study, which requires analyzing the results event by event (similarly as done in Sections 4.2.1 and 4.2.2). These analyses (not shown

here) confirm the results presented for the two cases above and in Section 4.1.3: the combined use of horizontal and vertical information results in improved reconstructed accumulations, while the contribution of the information from the previous volume scan is not found significant.

5 Conclusion

In this study we have proposed and tested 6 different formulations of a method to reconstruct radar reflectivity in the areas affected by ground clutter. The proposed formulations interpolate clutter-free observations within the first PPI (horizontal interpolation), from the PPIs above (extrapolation in the vertical), and/or from the previous volume scan (extrapolation in time using a nowcasting technique). The interpolation is done in the Ordinary Kriging framework, which is based on the structural analysis of the field (in space and time) to determine the weights to be given to the available clutter-free observations. The structure of the field is characterized through the multi-dimensional sample semivariogram, which is estimated within the vicinity of each area to be reconstructed.

The evaluation of the proposed techniques has been done over 24 rainfall events in the area of Barcelona (NE of Spain). The reconstruction methods have been first applied over a clutter-free area (mostly over the sea). This allowed us to use the original observations as reference. However, it is worth pointing out that systematic differences in the space-time structure of precipitation over the sea and land could slightly bias the validity of the results. The second part of the evaluation has been performed over the actually clutter-contaminated areas using raingauge observations as reference.

Our results show the strengths and weaknesses of horizontal and vertical information for the reconstruction of the reflectivity fields:

- Horizontal interpolation shows its best performance in widespread precipitation, while it fails at handling the high horizontal variability of convective situations;
- Vertical extrapolation is useful in situations with deep convection, but is not a good solution in widespread rain, due to the larger variability of the radar fields in the vertical: it results in overestimation when the first clutter-free PPI is affected by the bright band, or underestimation when it is in the snow level or above. It is worth pointing out that these systematic errors in stratiform rain could be partially mitigated by implementing a VPR correction when extrapolating observations in the vertical [see Wesson and Pegram (2004); Bellon et al. (2007) and references therein].

These results coincide with what has been reported by other authors [e.g., Sánchez-Diezma et al. (2001)].

We have also implemented a nowcasting technique (NOW) to reconstruct reflectivity fields by extrapolation of the previous quality-controlled volume scan. On average, this approach has been found to be systematically not as good as horizontal interpolation alone. This is in part due to the fact that sometimes NOW uses reflectivity estimates that were already reconstructed in the previous time step (because the original observations were affected by clutter contamination). This significantly affects the quality of the reconstruction over large clutter areas. Also, time extrapolation might result in misses and false detections in cases with fast-evolving small-scale convection.

The adaptive interpolation of horizontal and vertical observations (HV) consistently improves the reconstruction of the reflectivity field thanks to the weight assigned to the available observations through the structural analysis of the field. Overall, the benefit of including information from the previous volume scan (extrapolation in time) in the interpolation is not

systematically evident: HN is in general outperformed by HV, while the results obtained with HVN are usually very similar to those of HV.

In conclusion, among the analyzed formulations, our recommendation for the reconstruction of reflectivity volume scans is to use HV because it produced the most robust results (with no outliers) and is computationally cheaper than HVN. Wesson and Pegram (2006) proposed a method similar to HV, also based on a kriging approach. The main difference from HV is in the representation of the field variability. They first apply a pre-classification of the type of precipitation, and then they use average parametric and isotropic semi-variograms adapted to each precipitation type.

Finally, the proposed framework is not only useful for the reconstruction of reflectivity fields, but it might also be interesting for other radar variables. In particular, the reconstruction of polarimetric variables will be explored in a forthcoming paper.

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Appendix A Estimation of the semivariogram

One of the key points of the proposed method is the estimation of the semivariogram. We have chosen to estimate the sample semivariogram using equation (3) [similarly as Velasco-Forero et al. (2009); Sempere-Torres et al. (2012)]. The main difference with respect to these authors is that we have estimated the semivariogram locally within a neighborhood of each clutter area to better depict the local variability of the field.

This means that the most complete formulation (HVN) needs an estimate of the 4-dimensional semivariogram $\gamma(\Delta x, \Delta y, \Delta z, \Delta t)$ around each ground echo area, with the maximum lag in height, Δz_{\max} , being the distance between the first PPI and the closest clutter-free PPI, and $\Delta t=10$ minutes (the temporal resolution of radar data).

Figures A1 and A2 show an example for the first PPI measured on 06 July 20:03 at 16:20 UTC. The top panels show the reflectivity measurements within a subdomain of the radar coverage from which the sample multi-dimensional semivariograms were estimated (bottom panels of Figs. A1 and A2). The obvious differences between the estimated semivariograms are due to the local differences in the spatial variability of the reflectivity field, which justifies the need of estimating the semivariogram locally to guarantee the optimal reconstruction of the field.

Similarly, the other configurations based on the Ordinary Kriging approach (namely, HOR, HV and HN) make use of the 2-D and 3-D semi-variogram.

432 **References**

- 433 Bellon, A., Lee, G., Kilambi, A., Zawadzki, I., 2007. Real-time comparisons of VPR-
434 corrected daily rainfall estimates with a gauge mesonet. *Journal of Applied*
435 *Meteorology and Climatology*, 46(6): 726-741.
- 436 Berenguer, M., Sempere-Torres, D., Corral, C., Sanchez-Diezma, R., 2006. A fuzzy logic
437 technique for identifying nonprecipitating echoes in radar scans. *Journal of*
438 *Atmospheric and Oceanic Technology*, 23(9): 1157-1180.
- 439 Berenguer, M., Sempere-Torres, D., Pegram, G.G.S., 2011. SBMcast - An ensemble
440 nowcasting technique to assess the uncertainty in rainfall forecasts by Lagrangian
441 extrapolation. *Journal of Hydrology*, 404: 226-240.
- 442 Corral, C., Velasco, D., Forcadell, D., Sempere-Torres, D., 2009. Advances in radar-based
443 flood warning systems. The EHIMI system and the experience in the Besòs flash-
444 flood pilot basin. In: Samuels, P., Huntington, S., Allsop, W., Harrop, J. (Eds.), *Flood*
445 *Risk Management: Research and Practice*. Taylor & Francis, London, UK, pp. 1295-
446 1303.
- 447 Delrieu, G., Creutin, J.D., Andrieu, H., 1995. Simulation of Radar Mountain Returns Using a
448 Digitized Terrain Model. *Journal of Atmospheric and Oceanic Technology*, 12(5):
449 1038-1049.
- 450 Doviak, R.J., Zrnich, D.S., 1993. *Doppler radar and weather observations*, 562 pp.
- 451 Fabry, F., Bellon, A., Duncan, M.R., Austin, G.L., 1994. High-Resolution Rainfall
452 Measurements by Radar for Very Small Basins - the Sampling Problem Reexamined.
453 *Journal of Hydrology*, 161(1-4): 415-428.

454 Germann, U., Galli, G., Boscacci, M., Bolliger, M., 2006. Radar precipitation measurement in
455 a mountainous region. *Quarterly Journal of the Royal Meteorological Society*,
456 132(618): 1669-1692.

457 Goovaerts, P., 1997. *Geostatistics for natural resources evaluation. Applied Geostatistics*
458 *Series*. Oxford University Press, 483 pp.

459 Gourley, J.J., Tabary, P., Parent du Chatelet, J., 2007. A Fuzzy Logic Algorithm for the
460 Separation of Precipitating from Nonprecipitating Echoes Using Polarimetric Radar
461 Observations. *Journal of Atmospheric and Oceanic Technology*, 24(8): 1439-1451.

462 Hubbert, J.C., Dixon, M., Ellis, S.M., 2009. Weather Radar Ground Clutter. Part II: Real-
463 Time Identification and Filtering. *Journal of Atmospheric and Oceanic Technology*,
464 26(7): 1181.

465 Marshall, J.S., Palmer, W.M., 1948. The Distribution of Raindrops with Size. *Journal of*
466 *Meteorology*, 5(4): 165-166.

467 Moisseev, D.N., Chandrasekar, V., 2009. Polarimetric Spectral Filter for Adaptive Clutter and
468 Noise Suppression. *Journal of Atmospheric and Oceanic Technology*, 26(2): 215.

469 Sanchez-Diezma, R., Sempere-Torres, D., Creutin, J.-D., Zawadzki, I., Delrieu, G., 2001. An
470 improved methodology for ground clutter substitution based on a pre-classification of
471 precipitation types, 30th International Conference on Radar Meteorology. *Amer.*
472 *Meteor. Soc.*, Munich, Germany, pp. 271-273.

473 Sempere-Torres, D., Berenguer, M., Velasco-Forero, C.A., 2012. Blending of radar and gauge
474 rainfall measurements. A preliminary analysis of the impact of measurement errors,

475 Weather Radar and Hydrology (Proceedings of a symposium held in Exeter, UK,
476 April 2011). IAHS, pp. 365.

477 Sempere-Torres, D., Porra, J.M., Creutin, J.D., 1998. Experimental evidence of a general
478 description for raindrop size distribution properties. *Journal of Geophysical Research-*
479 *Atmospheres*, 103(D2): 1785-1797.

480 Steiner, M., Smith, J.A., 2002. Use of Three-Dimensional Reflectivity Structure for
481 Automated Detection and Removal of Nonprecipitating Echoes in Radar Data. *Journal*
482 *of Atmospheric and Oceanic Technology*, 19(5): 673-686.

483 Velasco-Forero, C.A., Sempere-Torres, D., Cassiraga, E.F., Gómez-Hernández, J.J., 2009. A
484 non-parametric automatic blending methodology to estimate rainfall fields from rain
485 gauge and radar data. *Advances in Water Resources*, 32(7): 986-1002.

486 Villarini, G., Krajewski, W.F., 2009. Review of the Different Sources of Uncertainty in
487 Single Polarization Radar-Based Estimates of Rainfall. *Surveys in Geophysics*, 31(1):
488 107-129.

489 Wesson, S.M., Pegram, G.G.S., 2004. Radar rainfall image repair techniques. *Hydrol. Earth*
490 *Syst. Sci.*, 8(2): 220-234.

491 Wesson, S.M., Pegram, G.G.S., 2006. Improved radar rainfall estimation at ground level.
492 *Natural Hazards and Earth System Sciences*, 6: 323-342.

493 Zawadzki, I.I., 1973. Statistical Properties of Precipitation Patterns. *Journal of Applied*
494 *Meteorology*, 12(3): 459-472.

495

Table 1. Summary of the 24 events analyzed in this study. Types “C” and “S” stand for “convective” and “stratiform”, respectively. #gauges indicates the number of rain gauges that measured significant rain during the event. Mean and Max stand for the average and maximum rainfall observed or estimated at rain gauge locations. CV is the coefficient of variation of rainfall accumulations at raingauge locations (defined as the ratio between the standard deviation and the mean value; i.e., high CV values indicate significant spatial variability of the accumulated field).

	Event start	Duration [h]	Type	Rain gauges				Radar		
				# gauges	Mean [mm]	Max [mm]	CV	Mean [mm]	Max [mm]	CV
#1	14/07/2001 01:00	23.0	C	49	12.5	71.3	1.27	7.8	44.1	1.30
#2	15/07/2001 00:00	13.0	C	76	21.3	65.0	0.63	18.8	59.9	0.61
#3	15/07/2001 17:00	28.0	C/S	57	12.6	43.4	0.86	11.6	39.5	0.73
#4	19/07/2001 00:00	20.0	S	101	23.1	38.6	0.35	22.5	40.4	0.37
#5	14/11/2001 00:00	96.0	S/C	105	65.9	167.1	0.38	55.3	209.0	0.52
#6	08/08/2002 00:00	20.0	C/S	88	7.0	36.8	0.91	6.2	27.6	0.78
#7	09/08/2002 12:00	12.0	S	80	6.2	34.6	1.01	3.8	15.5	0.75
#8	10/08/2002 05:00	16.0	C	62	10.6	47.3	0.82	9.1	37.7	0.96
#9	22/08/2002 00:00	21.0	S/C	86	16.5	60.1	0.82	12.8	38.1	0.54
#10	26/08/2002 00:00	24.0	C	66	14.6	71.9	1.08	9.5	51.1	1.03
#11	08/10/2002 18:00	54.0	C/S	107	73.4	193.3	0.46	61.3	152.1	0.31
#12	24/11/2002 00:00	24.0	S	106	24.1	47.8	0.34	23.4	60.2	0.42
#13	10/12/2002 00:00	24.0	S/C	101	43.7	96.5	0.52	28.4	90.5	0.66
#14	06/07/2003 01:00	20.0	C	36	8.4	34.4	1.01	8.4	35.1	0.91
#15	17/08/2003 03:00	21.0	C/S	100	22.3	64.2	0.56	15.3	50.1	0.49
#16	04/09/2003 05:00	40.0	S/C	65	8.7	38.4	1.04	9.4	60.4	1.32
#17	07/09/2003 01:00	18.0	S/C	96	18.0	56.3	0.65	9.8	27.4	0.43
#18	22/09/2003 00:00	24.0	C	77	12.2	68.4	1.03	10.6	72.1	0.96
#19	16/04/2004 00:00	24.0	S	100	43.3	142.8	0.78	25.5	60.6	0.47
#20	11/05/2004 00:00	24.0	S	104	12.8	21.6	0.28	9.9	19.2	0.41
#21	02/09/2004 00:00	18.0	C	76	10.1	73.3	1.25	9.8	43.7	0.90
#22	03/09/2004 00:00	12.0	C/S	95	15.0	37.7	0.60	11.3	21.9	0.31

#23	12/10/2005 00:00	51.0	S/C	104	61.8	259.4	0.62	51.5	242.7	0.59
#24	14/10/2005 07:00	41.0	S/C	102	31.4	78.0	0.43	26.6	49.7	0.36

503

504

505 Table 2. Scores obtained for the reconstruction of event accumulations in clutter-free areas
 506 (analysis of section 4.1) with the different reconstruction methods for the examples of 11 May
 507 2004 (Event #20 of Table 1) and 02 September 2004 (Event #21 of Table 1). The light gray
 508 shaded cells indicate the method for which the best score is obtained.

Widespread case: 11 May 2004 00:00 – 24:00							
	SSDZ2001	HOR	VERT	NOW	HV	HN	HVN
Bias [mm]	0.07	0.12	-5.17	-0.37	0.08	-0.12	1.2
RMSE [mm]	0.49	0.54	7.86	0.91	0.53	0.57	1.71
MARE [%]	4.3	4.7	68.9	8.2	4.5	4.8	15.2
Correlation	0.99	0.99	0.20	0.97	0.99	0.99	0.96

Convective case: 02 Sep 2004 00:00 – 24:00							
	SSDZ2001	HOR	VERT	NOW	HV	HN	HVN
Bias [mm]	-1.44	-0.51	-0.48	0.33	-0.42	-0.58	-0.26
RMSE [mm]	2.78	3.27	2.52	2.28	2.37	2.57	1.85
MARE [%]	57.0	96.3	89.0	45.5	73.5	78.7	59.6
Correlation	0.77	0.75	0.83	0.90	0.87	0.87	0.92

509

510 Table 3. Same as Table 2, but for the comparison of radar and raingauge totals (section 4.2).

Widespread case: 11 May 2004 00:00 – 24:00							
	SSDZ2001	HOR	VERT	NOW	HV	HN	HVN
Bias [mm]	-2.89	-2.89	-2.88	-3.08	-2.89	-2.99	-2.45
RMSE [mm]	4.35	4.35	4.70	4.58	4.36	4.45	4.24
MARE [%]	35.9	35.9	38.8	37.9	36.0	36.6	35.3
Correlation	0.36	0.36	0.27	0.35	0.36	0.34	0.35
Convective case: 02 Sep 2004 00:00 – 24:00							
	SSDZ2001	HOR	VERT	NOW	HV	HN	HVN
Bias [mm]	-0.60	-1.56	-0.99	-0.61	-1.03	-1.03	-0.80
RMSE [mm]	4.16	4.46	4.10	4.20	4.08	4.39	4.08
MARE [%]	66.1	65.8	61.1	68.4	62.2	69.1	63.0
Correlation	0.84	0.83	0.83	0.83	0.85	0.83	0.84

511

512 **List of Figure captions**

513 Figure 1. Area where the experiment has been carried out and mean ground clutter map in
514 clear-air conditions for the domain covered by the Barcelona radar (the location of the radar is
515 indicated by the white diamond). The violet shaded areas show where the signal has been
516 reconstructed for the evaluation of the different formulations (analysis presented in section
517 4.1). The orange diamonds show the location of the raingauges used for the evaluation of the
518 performance of the formulations (section 4.2).

519 Figure 2. Top: Reflectivity measurements on the first PPI observed on 11 May 2004 at 13:10
520 UCT (left) and on 02 September 2004 at 07:30 UTC (right). Bottom: Estimated rainfall
521 accumulation during the two example cases of 11 May 2004 (left) and 02 September 2004
522 (right).

523 Figure 3. Vertical cross sections of the reflectivity volume scans shown in Fig 2 on 11 May
524 2014 at 13:10 UTC along the segment A-B (top) and 02 September 2004 at 07:30 UTC along
525 the segment C-D (bottom). Radar beam paths for different elevations (thin green lines) have
526 been calculated supposing normal propagation conditions. The black shades are the terrain
527 profile along the cross sections.

528 Figure 4. Scatterplots between reference and reconstructed rainfall accumulations over the
529 violet clutter-free areas shown in Fig. 1 for the event of 11 May 2004. The reconstruction has
530 been performed over reflectivity volume scans with the HOR, VERT and NOW methods (left,
531 middle, and right panels, respectively).

532 Figure 5. Same as Fig. 4, but for the event of 02 September 2004.

533 Figure 6. From top to bottom, accumulation bias, MARE, correlation, and RMSE over the
534 clutter-free areas (shown in Fig. 1) where the 6 tested formulations and SSDZ2001 have been

535 used to reconstruct the reflectivity (section 4.1). The results are presented for the 24 analyzed
536 events (note that, despite of the use of lines, the events are in no way connected).

537 Figure 7. Scatterplots of accumulated raingauge rainfall and radar estimates for a widespread
538 rain event (11 May 2004, #20 of Table 1). Reconstruction of radar reflectivity in clutter-
539 contaminated areas has been done with HOR (left), VERT (middle), and NOW (right). Light
540 gray squares correspond to rain gauges collocated with radar bins affected by clutter in mean
541 propagation conditions. Black dots correspond to rain gauges in areas not affected by clutter.

542 Figure 8. POD (left) and POFD (right) as a function of range corresponding to a widespread
543 case (11 May 2004, #20 of Table 1). The reconstruction of radar reflectivity in clutter-
544 contaminated areas has been done (from top to bottom) with HOR, VERT and NOW. Light
545 gray squares correspond to rain gauges collocated with radar bins affected by clutter in mean
546 propagation conditions. Black dots correspond to rain gauges in areas not affected by clutter.

547 Figure 9. Same as Fig. 7, but for a convective case (02 September 2004, #21 of Table 1).

548 Figure 10. Same as Fig. 8, but for a convective case (02 September 2004, #21 of Table 1)

549 Figure 11. Similar as Fig. 6, but for the radar-raingauge comparison (section 4.2)

550 Figure A1. Top: Subdomain (northeast of the radar) of the reflectivity field observed on 06
551 July 2003 at 16:20 UTC on the first PPI (left), on the second PPI (middle) and, on the first
552 PPI observed from 16:10 UTC extrapolated to compensate the effect of motion (right). The
553 areas in white are affected by ground clutter, and thus have not been used to estimate the
554 semivariogram. Bottom: 2D semivariogram estimated within the subdomain (expressed in
555 units of % of the field variance) for lags, $\Delta z=0$ and $\Delta t=0$ (left), $\Delta z=1$ PPI and $\Delta t=0$ (middle),
556 and $\Delta z=0$ and $\Delta t=10$ minutes (right).

557 Figure A2. Same as Fig. A1, but for another subdomain (northwest of the radar).

Figure 1

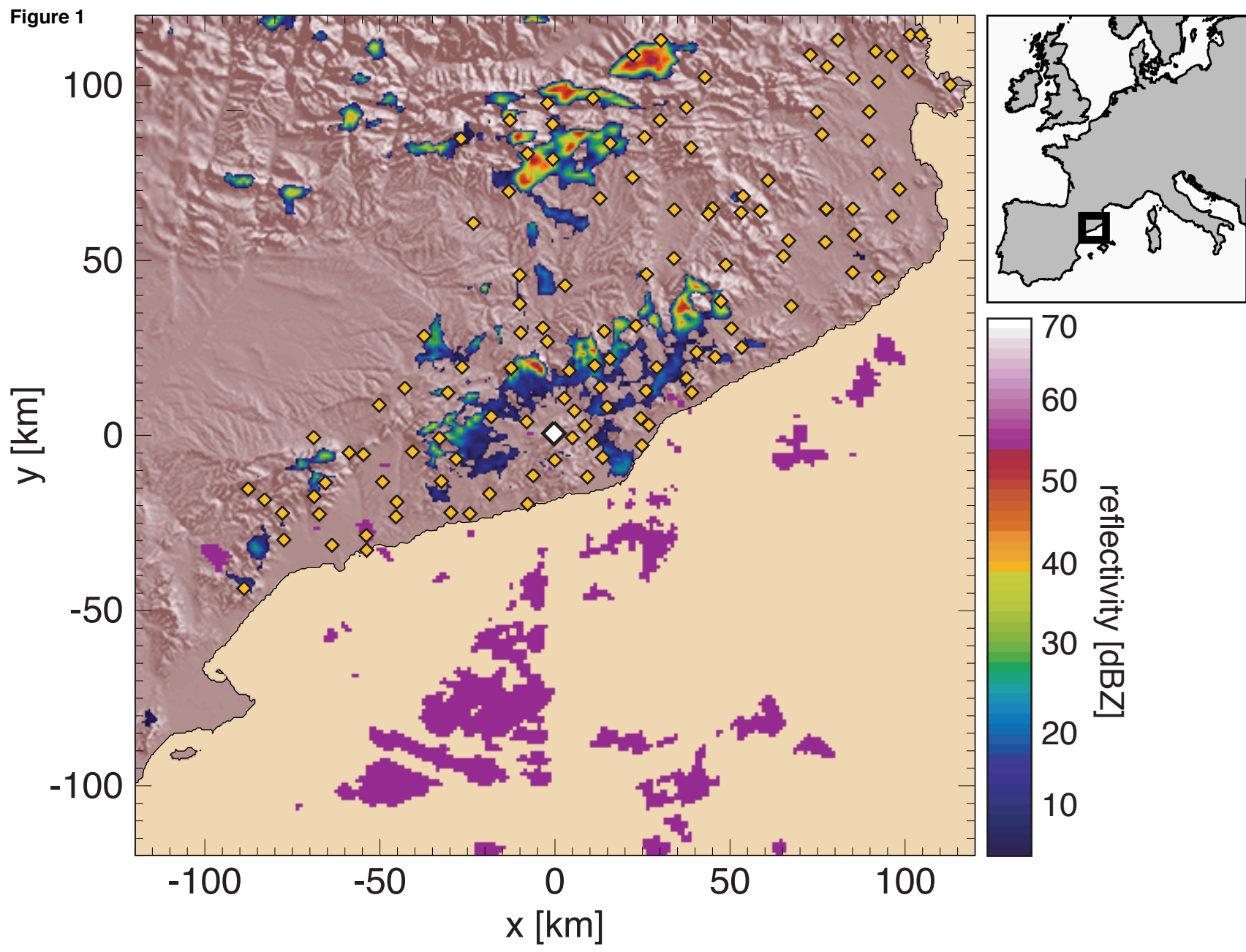
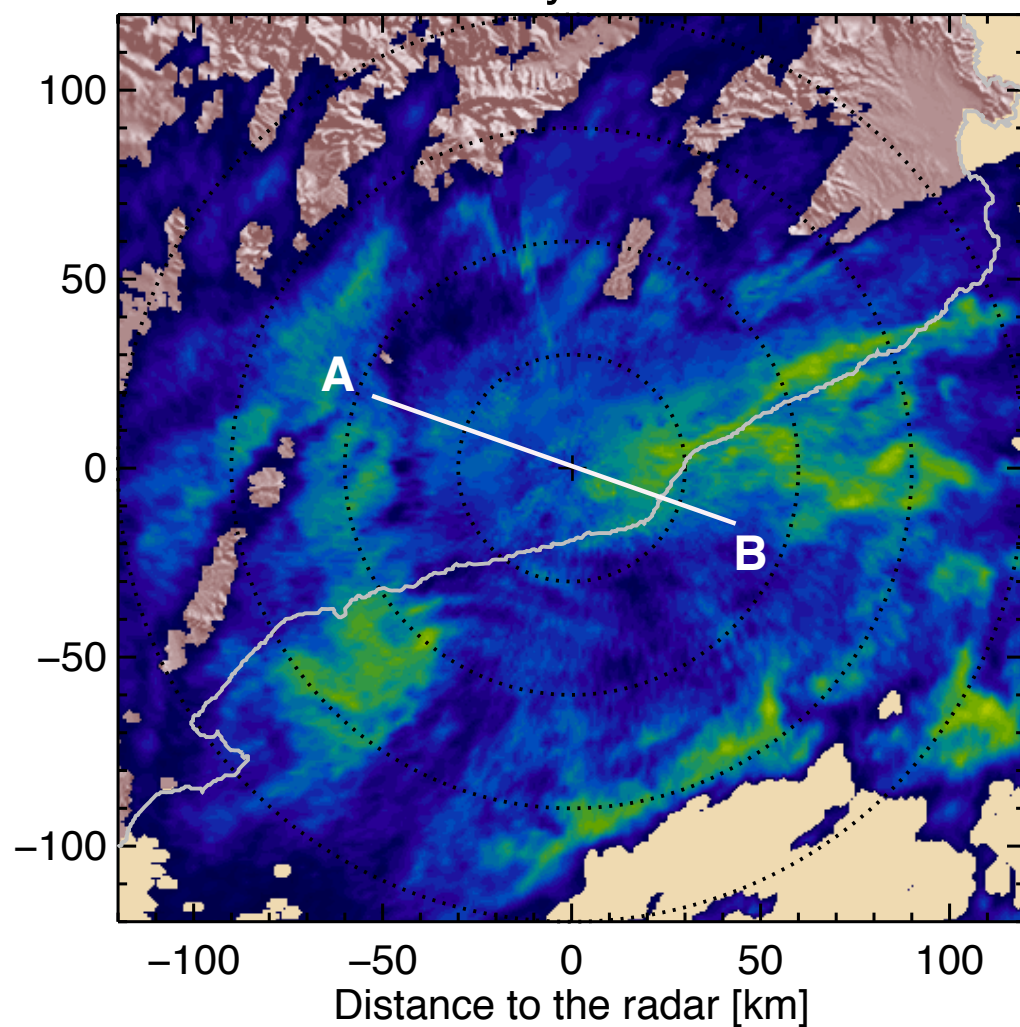
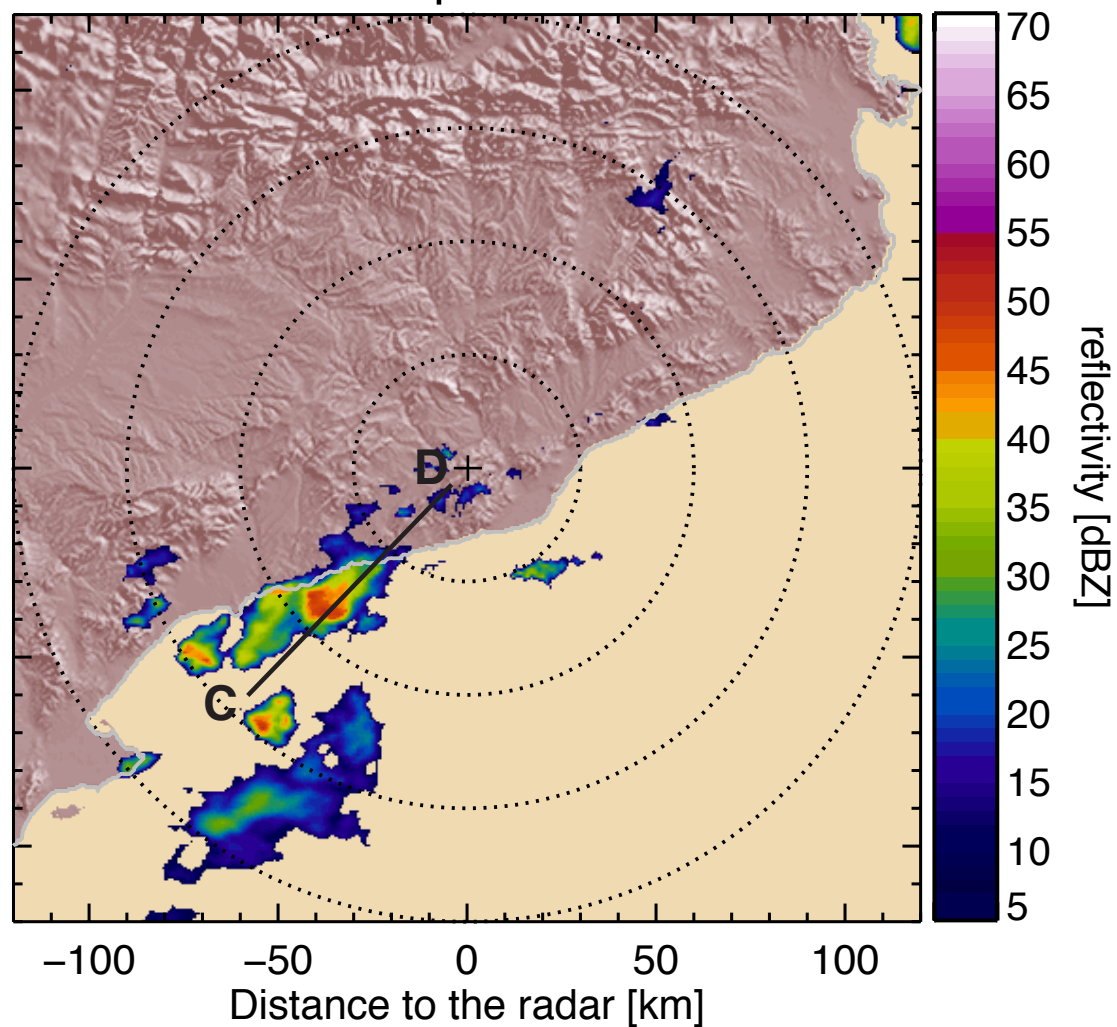


Figure 2

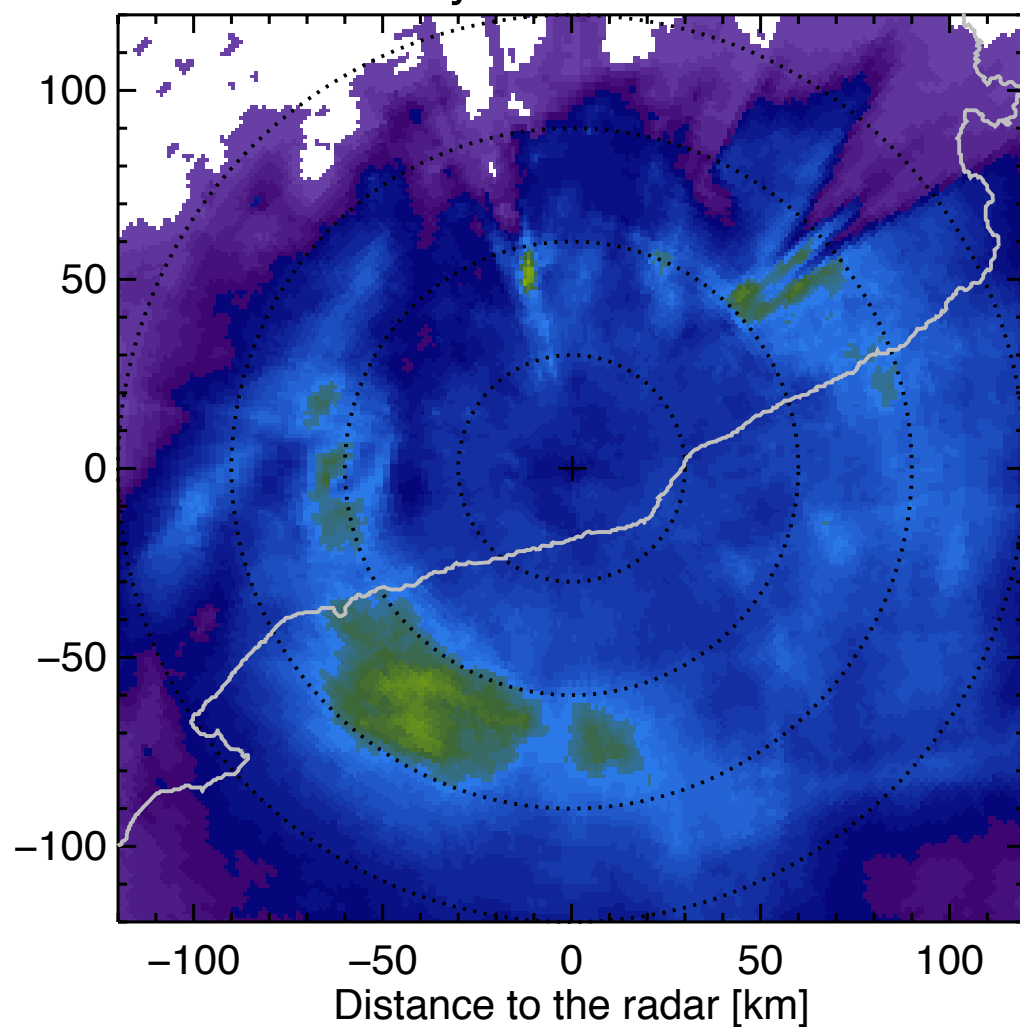
HV: 11 May 2004 13:10



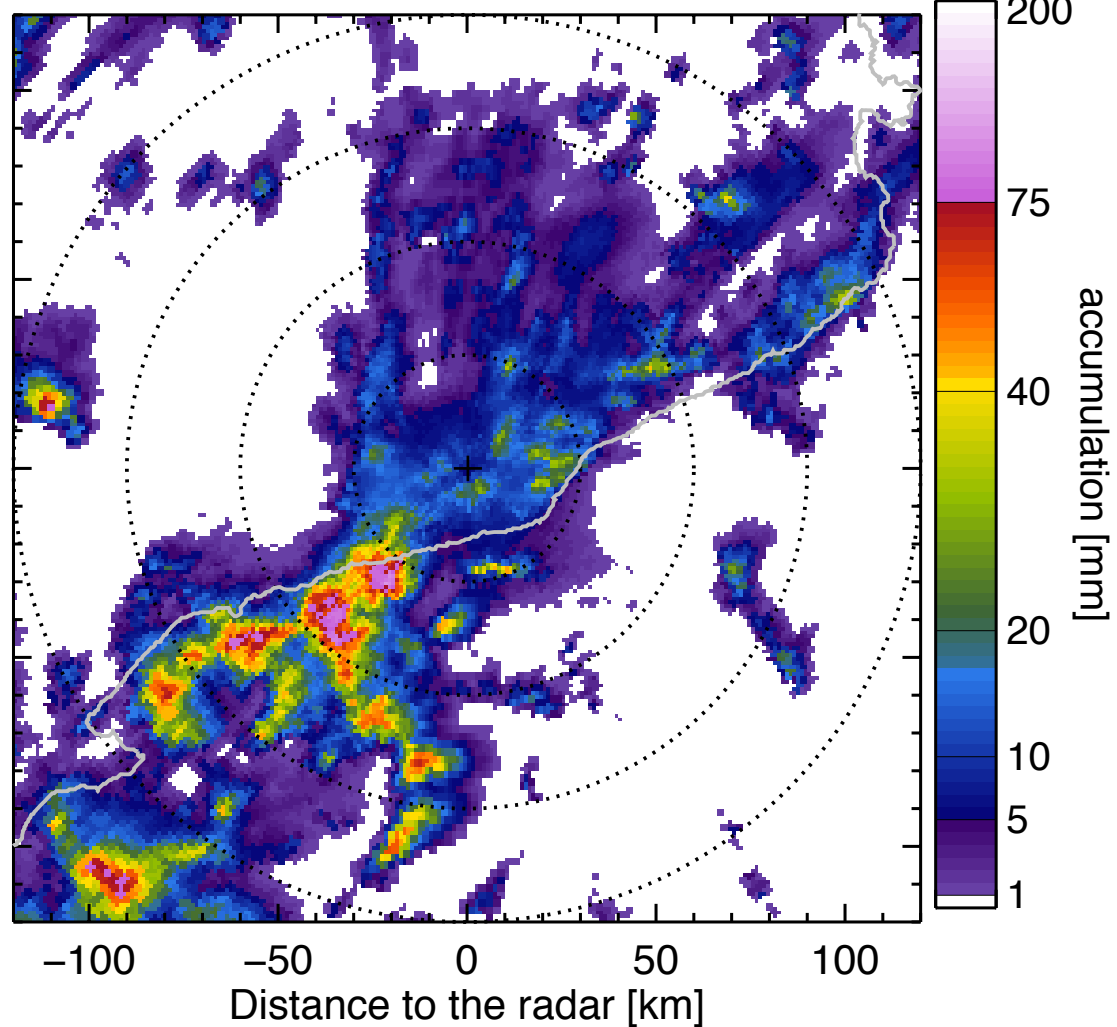
HV: 02 Sep 2004 07:30



HV: 11 May 2004 00:00 – 24:00



HV 02/09/2004 00:00 – 18:00



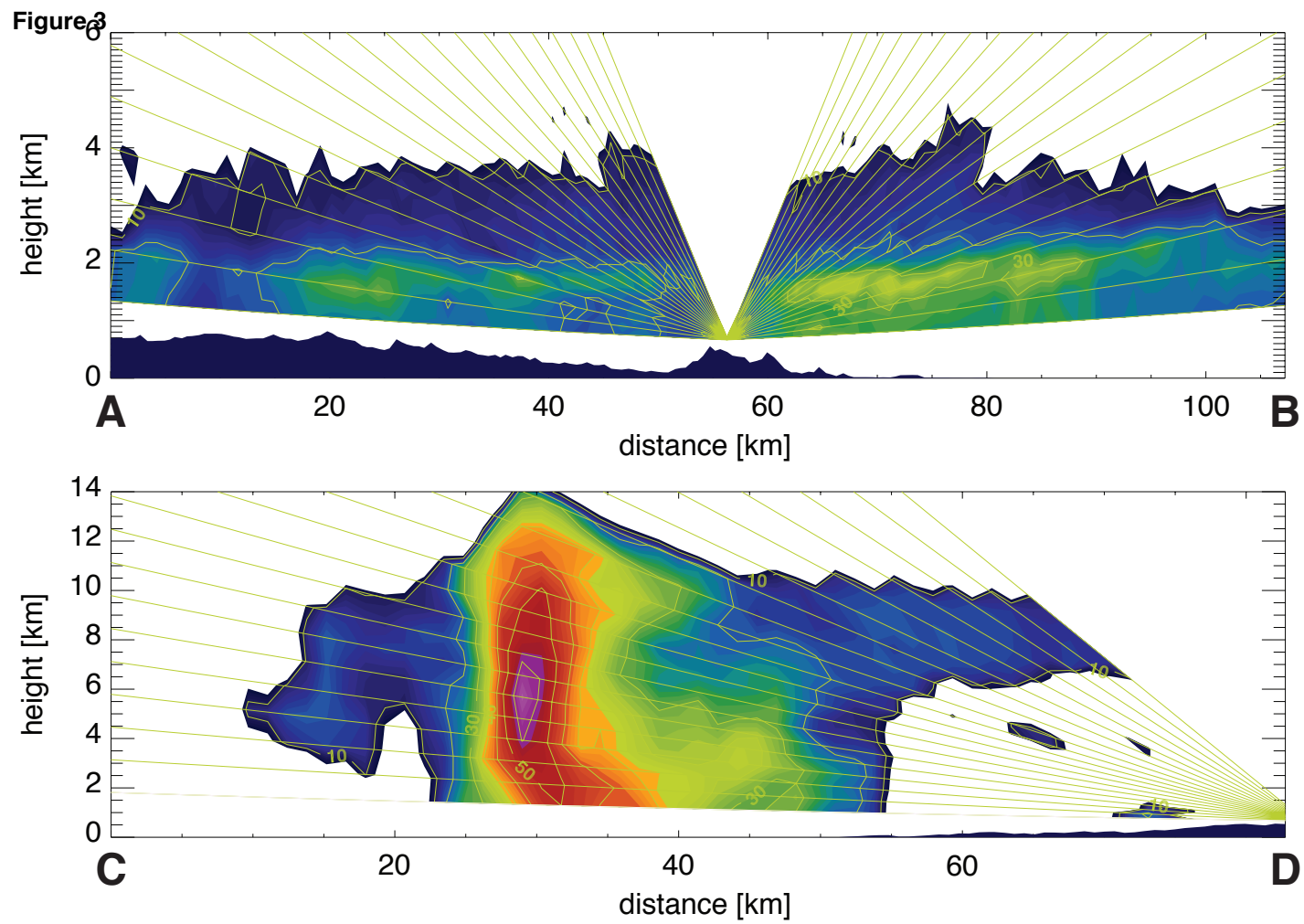


Figure 4

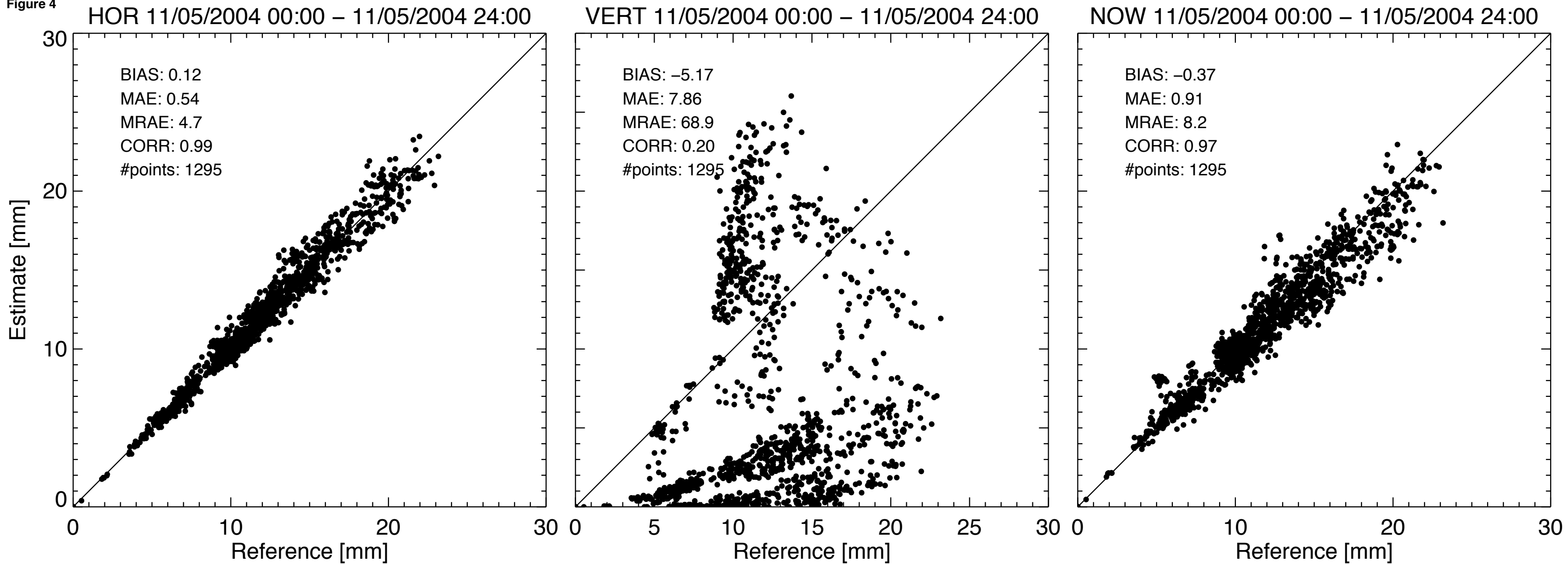


Figure 5

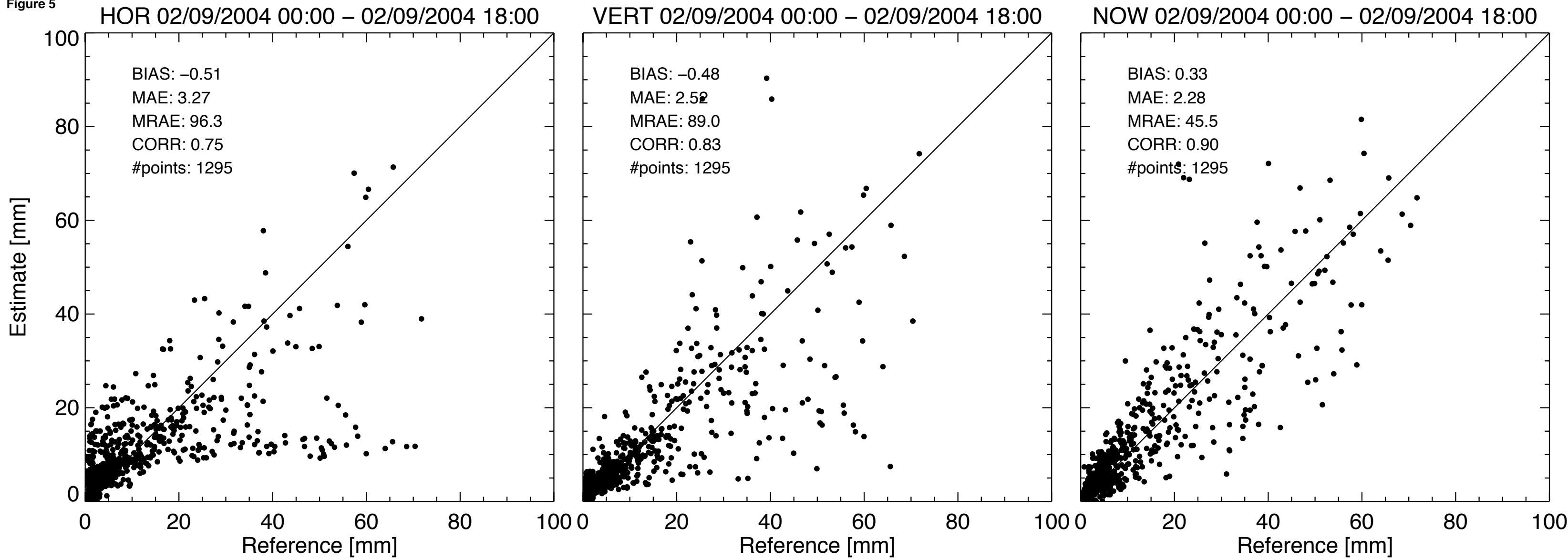


Figure 6

SSDZ2001 HOR VERT NOW

HV HN HVN

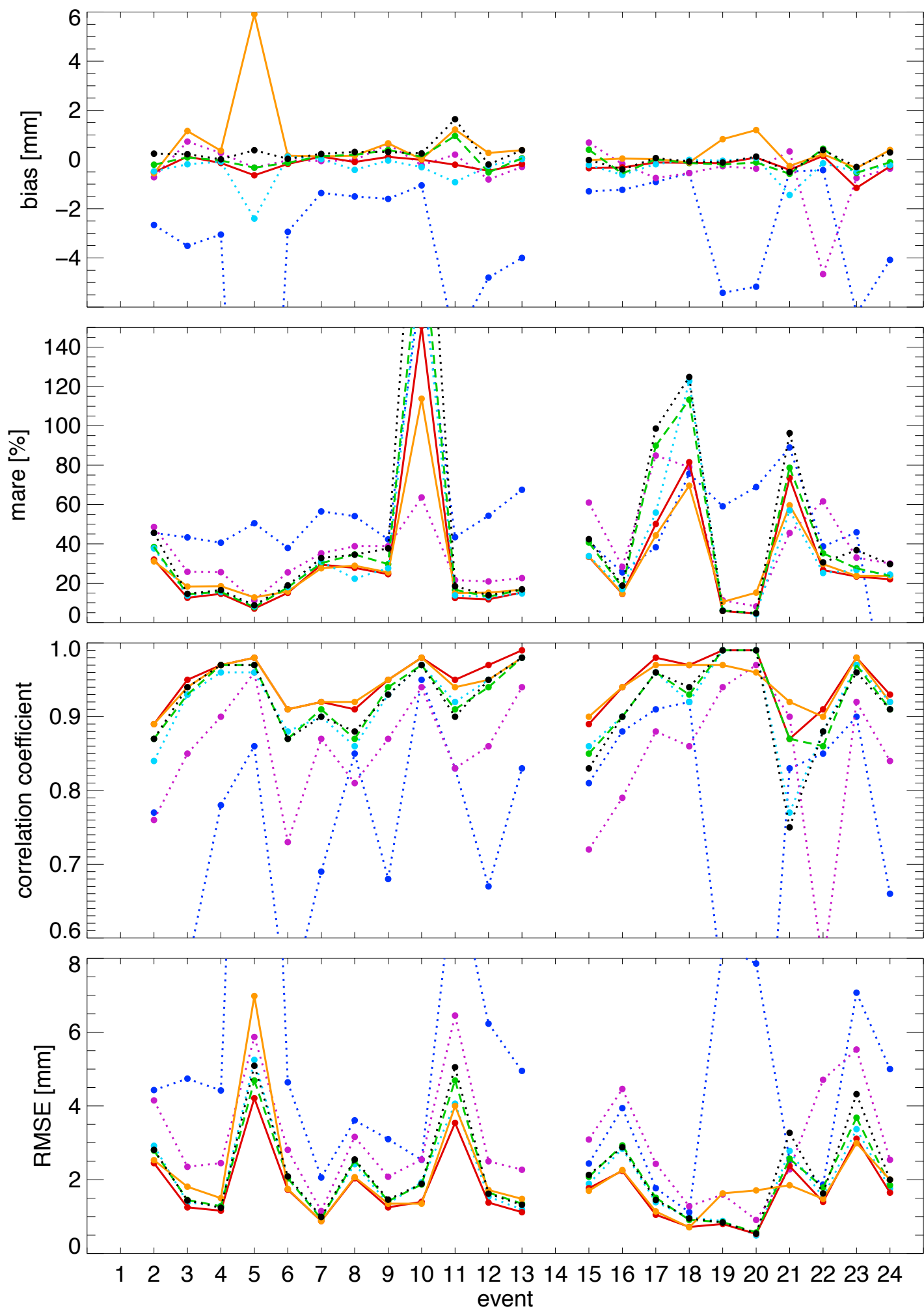


Figure 7

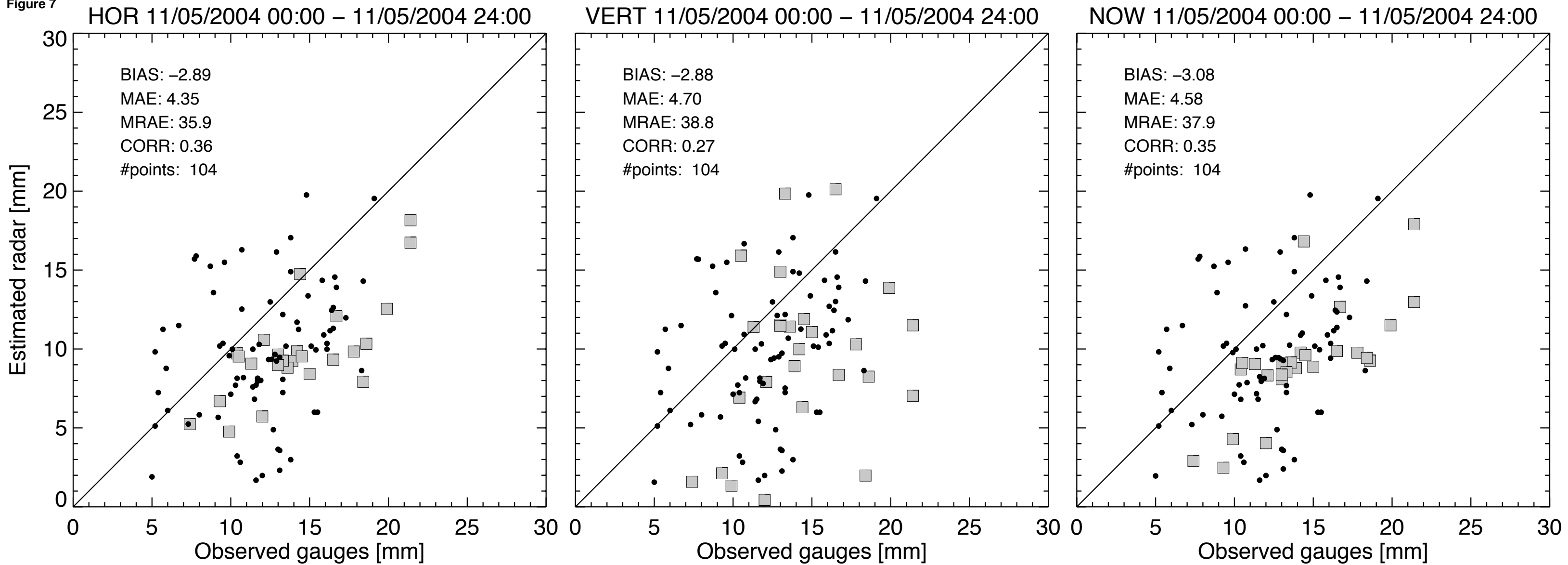


Figure 8

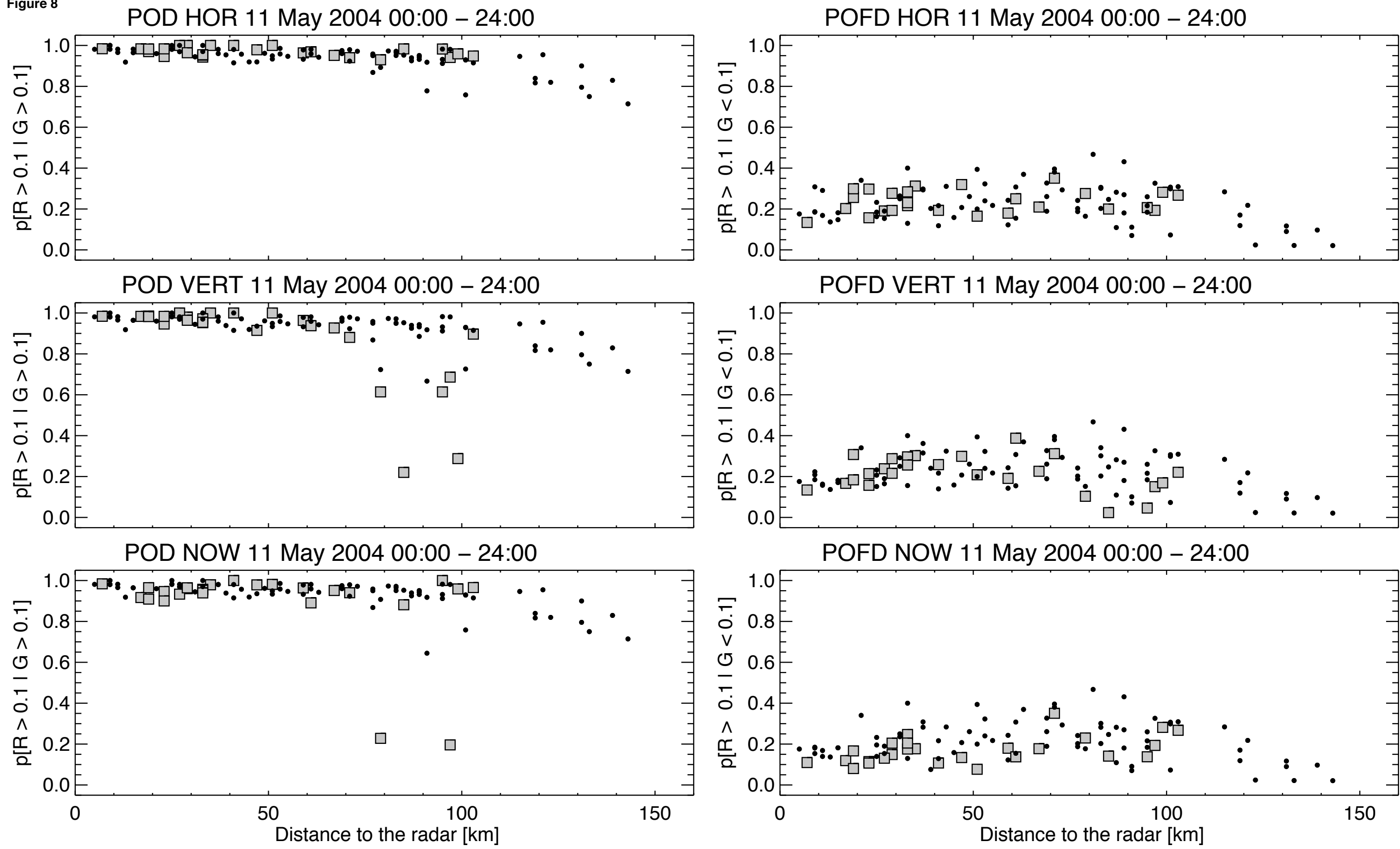


Figure 9

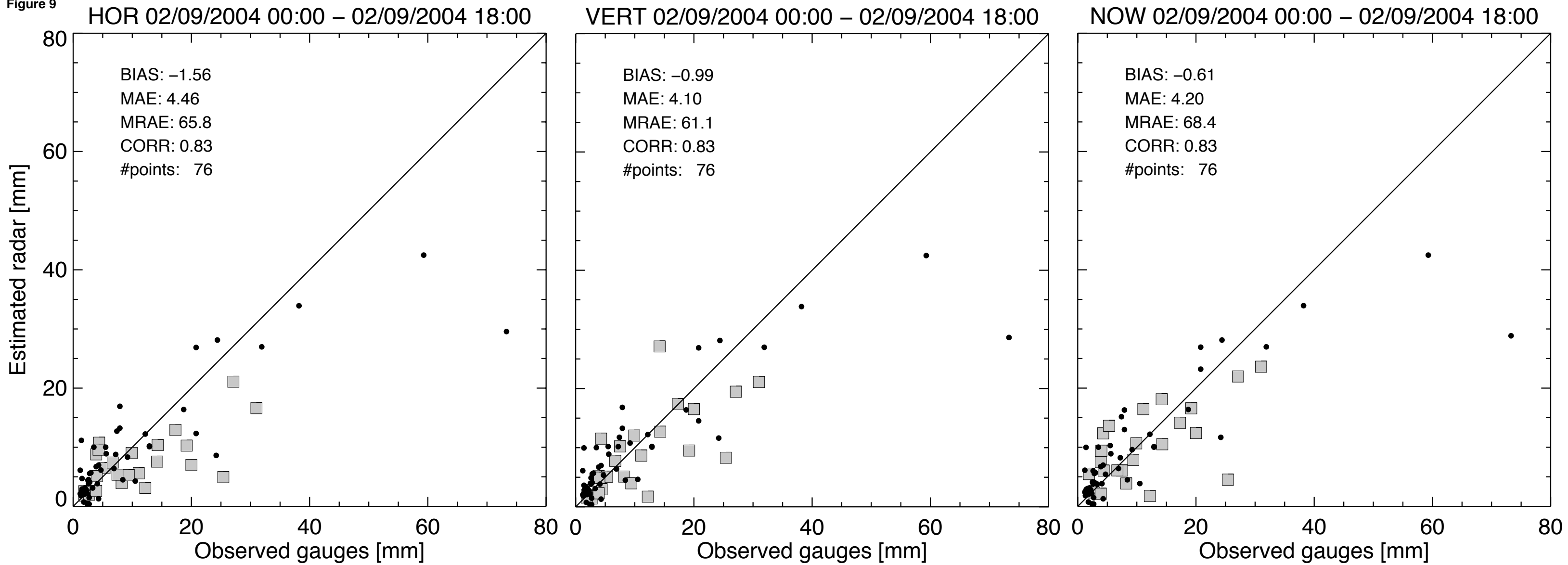


Figure 10

