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# CONSTITUTIVE RELATIONSHIP OF 7075 ALUMINUM ALLOY BASED ON MODIFIED ZERILLI-ARMSTRONG (M - ZA) MODEL

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The Gleeble – 3500 thermal simulation testing machine was used to perform isothermal tensile test on 7075 aluminum alloy at a deformation temperature of 300 - 450 °C and a strain rate of 0,01 - 1 s<sup>-1</sup>, and the true stress-strain curve of the alloy was obtained. Based on the true stress-strain data, the modified Zerilli-Armstrong (M-ZA) model was used to construct the constitutive model of the alloy, and the fitting accuracy of the model was analyzed.

Keyword: 7075 aluminum alloy, isothermal tensile, flow stress, temperature, modified Zerilli-Armstrong model

# INTRODUCTION

7075 aluminum alloy has the characteristics of low density, high strength and hardness and good processing performance. It is an important lightweight and highstrength structural material. 7075 aluminum alloy is an Al-Zn-Mg-Cu series heat-treatable high-strength deformed aluminum alloy. In practical engineering applications, the Finite element method (FEM) is a powerful tool to simulate the thermoplastic forming process of materials and determine the optimal forming process conditions for metals and the accuracy of the finite element simulation results is closely related to the accuracy of the constitutive model [1, 2]. Therefore, in order to obtain high-quality 7075 aluminum alloy components during the thermoplastic forming process, it is necessary to construct a more accurate constitutive model based on the thermal deformation behavior of 7075 aluminum alloy.

Currently, researchers have conducted many studies on high-temperature intrinsic constitutive models of alloys. He [3] used the modified Zerilli-Armstrong model to predict the high temperature deformation behavior of 20CrMo alloy steel. Cai [4] used the strain-compensated Arrhenius constitutive equation to predict the high temperature deformation behavior of 3Cr23Ni8Mn3N alloy steel. Ji[5] used the modified Johnson – Cook constitutive equation to predict the high temperature deformation behavior of TA15 alloy.

In this study, The Gleeble – 3500 thermal simulation testing machine was used to perform isothermal tensile test on 7075 aluminum alloy at a deformation temperature of 300 - 450 °C and a strain rate of 0,01 - 1 s<sup>-1</sup>, and the true stress-strain curve of the alloy was obtained. Based on the true stress-strain data, the modified Zerilli-Armstrong (M-ZA) model [6] is used to construct the

constitutive model of the alloy and analyze the fitting accuracy of the model.

# EXPERIMENTAL MATERIALS AND PROCESSES

The material used in the test is a rolled 2 mm thick 7075 aluminum alloy sheet, and its chemical composition is shown in Table 1.

Table 1 Chemical composition of 7075 aluminum alloy sheet/wt.%

Si	Fe	Cu	Mn	Mg
0,07	0,22	1,4	0,04	2,2
Cr	Zn	Ti	AI	
0,19	5,4	0,02	Bal,	

In order to study the thermal deformation behavior of 7075 aluminum alloy, a Gleeble - 3500 thermal simulation testing machine was used to perform uniaxial hot tensile test on 7075 aluminum alloy. The geometry and dimensions of the uniaxial hot tensile specimen are shown in Figure 1 (unit: mm). First, the specimen was heated to 450 °C at a rate of 20 °C/s, and then heated to a solid solution temperature of 480 °C at a rate of 5 °C/s, and kept for 10 minutes. The specimen is lowered to the deformation temperature at a rate of 50 °C/s, and the temperature of the specimen is kept uniform for 10 seconds. Stretching is carried out at a constant temperature and strain rate, and the specimen is rapidly cooled after being stretched to preserve its microstructure at high temperature. The deformation temperature is 300 °C, 350 °C, 400 °C, and 450 °C, and the strain rate is 0,01 s<sup>-1</sup>,0,1 s<sup>-1</sup>,1 s<sup>-1</sup>. The stress-strain curve of 7075 aluminum alloy is shown in Figure 2.

### MODIFIED ZERILLI-ARMSTRONG MODEL

The modified ZA model (M-ZA) is expressed as follows:

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Figure 1 Shape and size of high temperature tensile specimen



**Figure 2** Stress-strain curve of 707 5 aluminum alloy. (a) T = 300 °C; (b) T = 350 °C; (c) T = 400 °C; (d) T = 450 °C

$$\sigma = (C_1 + C_2 \varepsilon^m) \exp[-(C_3 + C_4 \varepsilon)T + (C_5 + C_6 T^*) \ln \dot{\varepsilon}^*]$$
(1)

Where:  $C_1$ ,  $C_2$ ,  $C_3$ ,  $C_4$ ,  $C_5$ ,  $C_6$  and *m* are the material constants;  $\dot{\varepsilon}$  is the strain rate (s<sup>-1</sup>);  $\dot{\varepsilon}^* = \dot{\varepsilon} / \dot{\varepsilon}_{ref}$ ,  $T^* = T - T_{ref}$ ,  $\dot{\varepsilon}_{ref}$  and  $T_{ref}$  are the reference strain rate and reference temperature, respectively.

Choose temperature 350 °C and strain rate 0,01 s<sup>-1</sup> as reference values to calculate the material constants in the model. When the reference strain rate is 0,01 s<sup>-1</sup>, Equation (1) can be transformed into Equation (2):

$$\ln \sigma = \ln \left( C_1 + C_2 \varepsilon^m \right) - \left( C_3 + C_4 \varepsilon \right) T^*$$
(2)

At a reference strain rate of 0,01 s<sup>-1</sup> and 4 deformation temperatures, 7 groups of stress and strain data points with strains ranging from 0,05 to 0,2 with an interval of 0,025 are substituted into Equation (2). The values of  $I_1 = \ln(C_1 + C_2 \varepsilon^m)$  and  $S_1 = -(C_3 + C_4 \varepsilon)$  can be obtained by linear fitting of the relationship of (as shown in Figure 3).  $I_1$  is the intercept of the fitted straight line, and  $S_1$  is the slope of the fitted straight line.

After reconverting  $I_1$ , find the logarithm of both sides of the equation:

$$\ln\left(\exp I_1 - C_1\right) = \ln C_2 + m \ln \varepsilon \tag{3}$$



Figure 3 Fitting relationship between T\* and Ino. (a) fitting; (b) local amplification



**Figure 4** Fitting relationship between deformation parameters. (a)  $\ln \epsilon$  and  $\ln(\exp I, -C_{,})$ ; (b) true strain and  $S_{,}$ 

In the above equation,  $C_1$  is the yield stress value under reference conditions ( $C_1 = 68,55$ ). Substituting  $C_1$ into Equation (3), the value of  $C_2$  and *m* can be obtained by linear fitting of the relationship of (Figure 4(a)). Similarly,  $C_3$  and  $C_4$  can be obtained by linear fitting of the relationship between  $S_1$ - $\varepsilon$  (Figure 4(b)).

Obtain  $C_2 = 18,36$ , m = 0,025,  $C_3 = 0,008$ ,  $C_4 = -1,54 \times 10^{-3}$ .

Let  $S_2 = C_5 + C_6 T^*$ , Equation (1) can be written as Equation (4). Under the specified strain conditions,  $S_2$ can be obtained by linear fitting of relationship (Figure 5(a)), and  $C_5$  and  $C_6$  can be obtained by calculating the linear relationship between  $S_2$  (as shown in Figure 5(b)).

$$\ln \sigma = \ln \left( C_1 + C_2 \varepsilon^m \right) - \left( C_3 + C_4 \varepsilon \right) T^* + S_2 \ln \varepsilon^* \quad (4)$$

Obtain  $C_5 = 0,12, C_6 = 5,93 \times 10^{-4}$ .

The relevant material parameters obtained according to the above steps are summarized in Table 2, and the modified ZA model is as follows

$$\sigma = (68,55 + 18.36\varepsilon^{0.025}) \exp[-(0,008 - 1,54 \times 10^{-3}\varepsilon) + (0,12 + 5,93 \times 10^{-4}T^*)$$
(5)  
$$\ln \dot{\varepsilon}^*]$$

Table 2 Material	parameter	table of	Modified	ZA model
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Constants	C <sub>1</sub>	C2	C <sub>3</sub>	C <sub>4</sub>
Value	68,55	18,36	0,008	-6,32×10 <sup>-4</sup>
Constants	C <sub>5</sub>	C <sub>6</sub>	m	
Value	0,12	5,93×10 <sup>-4</sup>	0,025	



Figure 5 Fitting relationship between deformation parameters. (a)  $\ln \epsilon$  \* and  $\ln \sigma$ ; (b) *T*\*and *S*<sub>2</sub>

# SIMULATION PREDICTION AND VERIFICATION OF CONSTITUTIVE MODEL

According to the M-ZA model, the predicted value of flow stress can be obtained. The comparison result of the predicted value based on the M-ZA model and the experimental value is shown in Figure 6.

In order to more accurately quantify and compare the prediction accuracy of the two constitutive equations established, it is necessary to perform statistical error analysis on the prediction data and experimental data. Introduce two statistical parameters: correlation coefficient (*R*) and average absolute error ( $\delta_{AARE}$ ) to further evaluate the predictive ability of the model:

$$R = \frac{\sum_{i=1}^{N} \left( E_i - \overline{E} \right) \left( P_i - \overline{P} \right)}{\sqrt{\sum_{i=1}^{N} \left( E_i - \overline{E} \right)^2 \times \left( P_i - \overline{P} \right)^2}}$$
(6)

$$\delta_{\text{AARE}} = \frac{1}{N} \sum_{i=1}^{N} \left| \frac{E_i - P_i}{E_i} \right| \times 100\%$$
(7)

Where:  $E_i$  is the experimental value;  $P_i$  is the predicted value;  $\overline{E}$  and  $\overline{P}$  are the average of the experimental value and the predicted value; N is the number of samples.

Figure 7 shows the correlation between the predicted value of flow stress of the M-ZA model and the experimental value. The 45° straight line represents the best regression line between the predicted value and the experimental value. Most of the data points of the M-ZA model are distributed on a straight line. The model's R



Figure 6 Comparison of predicted value and experimental value. (a) T = 300 °C; (b) T = 350 °C; (c) T = 400 °C; (d) T = 450 °C



Figure 7 Correlation test between predicted value and experimental value

= 0,990 and  $\delta_{AARE}$  = 4,44 %. It shows that the predicted value of the model has a very close relationship with the experimental value. The M-ZA model can accurately reflect the high temperature plastic flow behavior of 7075 aluminum alloy.

### CONCLUSION

Deformation temperature and strain rate have a significant effect on the flow stress and strain curve of 7075 aluminum alloy. The value of flow stress increases with the increase of strain rate and decreases with the increase of deformation temperature. The constructed M-ZA constitutive model of 7075 aluminum alloy can highly predict its flow stress. R = 0,990,  $\delta_{AARE} = 4,44$  %.

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