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POWER STUDIES OF THE LIKELIHOOD RATIO TEST
AND OTHER ALLIED TESTS FOR A RESTRICTIVE FORM
OF THE BEHRENS-FISHER PROBLEM

par

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SUR PLACE

POWER STUDIES OF THE LIKELIHOOD RATIO TEST AND OTHER ALLIED TESTS

FOR A RESTRICTIVE FORM OF THE BEHRENS-FISHER PROBLEM

by

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SUMMARY

This technical report (together with technical reports EP75-R-40 and EP75-R-41) constitutes our final analysis of the Behrens-Fisher problem under the assumption of equal coefficients of variation. In this report we compare, by simulation technique, the power of five statistical tests, two of which were derived in the first report: the likelihood ratio (L-R) test and an asymptotically (in some sense) invariant test.

It is seen that the L-R test is highly satisfactory for all values of the coefficient of variation and that the invariant test, which is computationally much simpler than the L-R test, is a good competitor for coefficient of variation greater then or equal to 3. Moreover the L-R test remains robust even for an appreciable deviation from unity of the ratio of two coefficients of variation.

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## THEORY

Let $\{X_{ij}, j = 1,2,\ldots,n_i\}$ be a random sample of size $n_i$ from a univariate population $N(\mu_i, \beta^2 \mu_i^2 = \sigma_i^2)$ $i = 1,2$. The coefficient of variation $\beta$ is unknown and we assume the means $\mu_1, \mu_2$, both positive.

Several parametric statistical tests can be used to test $H_0: \mu_1 = \mu_2 = \mu\ (>0)$ against $H_1: \mu_1 = \mu_2$. In this report, we study the power of five statistical tests: t-test, F-test, t'-test, likelihood ratio test (LR) and the U-test. The last two tests are new and were derived by Clement and Sinha (1975). Here is a brief description of each test.

t-test: reject $H_0$ at $\alpha$-level if

$$\frac{|\bar{X}_1 - \bar{X}_2|}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} > t_{n_1 + n_2 - 2, \frac{\alpha}{2}} \tag{1}$$

where

$$\bar{X}_i = \frac{1}{n_i} \sum_{j=1}^{n_i} X_{ij}, \quad i = 1,2 \tag{2}$$

$$S_p^2 = \frac{1}{n_1 + n_2 - 2} [n_1 S_1^2 + n_2 S_2^2] \tag{3}$$

$$S_i^2 = \frac{1}{n_i} \sum_{j=1}^{n_i} (X_{ij} - \bar{X}_i^2), \quad i = 1,2 \tag{4}$$

$t_{n_1 + n_2 - 2, \frac{\alpha}{2}}$ is the $1 - \frac{\alpha}{2}$ percentage point of a Student-t distribution with $n_1 + n_2 - 2$ d.f.

F-test: reject $H_0$ at $\alpha$-level if

$$\frac{n_1 S_1^2 / n_1 - 1}{n_2 S_2^2 / n_2 - 1} > F_{n_2 - 1}^{n_1 - 1}(\frac{\alpha}{2}) \quad \text{or} \quad < F_{n_2 - 1}^{n_1 - 1}(1 - \frac{\alpha}{2})$$

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where $S_i^2$ is defined by (4) and $F_{n_2-1}^{n_1-1}(\frac{\alpha}{2})$ is the $1-\frac{\alpha}{2}$ percentage point of a Fisher-Snedecor F-distribution with $n_1-1$ d.f. in the numerator and $n_2-1$ d.f. in the dominator.

$t'$-test (Fryer): reject $H_0$ at $\alpha$-level if

$$t' = \frac{|\bar{X}_1 - \bar{X}_2|}{\sqrt{\dfrac{S_1^2}{n_1-1} + \dfrac{S_2^2}{n_2-1}}} > t'_{\frac{\alpha}{2}}$$

where

$$t'_{\frac{\alpha}{2}} = \omega_1 \, t_{n_1-1,\frac{\alpha}{2}} + \omega_2 \, t_{n_2-1,\frac{\alpha}{2}}$$

$$\omega_1 = \frac{S_1^2/n_1-1}{S_1^2/n_1-1 + S_2^2/n_2-1} \quad , \quad \omega_2 = 1-\omega_1$$

L-R test (Clement and Sinha): reject $H_0$ at $\alpha$-level if

$$-2 \log \lambda > \lambda_\alpha$$

where

$$\lambda = [S_1^2 + A_1]^{n_1/2} [S_2^2 + A_2]^{n_2/2} [S^2]^{-(n_1+n_2)/2}$$

$$A_1 = n_2[(n_1+n_2)\bar{X}_1^2(\bar{X}_2^2 + 2S_2^2) - \sqrt{n_1+n_2}\,\bar{X}_1\bar{X}_2 B]/2(n_1+n_2)\{n_1\bar{X}_1^2 + (n_1+n_2)S_2^2\}$$

$$A_2 = n_1[(n_1+n_2)\bar{X}_2^2(\bar{X}_1^2 + 2S_1^2) - \sqrt{n_1+n_2}\,\bar{X}_1\bar{X}_2 B]/2(n_1+n_2)\{n_2\bar{X}_1^2 + (n_1+n_2)S_1^2\}$$

$$B = \{(n_1+n_2)\bar{X}_1^2\bar{X}_2^2 + 4n_2\bar{X}_1^2S_2^2 + 4n_1\bar{X}_2^2S_1^2 + 4(n_1+n_2)S_1^2S_2^2\}^{\frac{1}{2}}$$

and $\lambda_\alpha$ is the $1-\alpha$ percentage point that can be found in tables prepared by Clement and Sinha. The test is refered to as LAMDA in the tables.

.4

U-test (Clement and Sinha):  Under the assumption of <u>large</u> common homogeneous coefficient of variation, the <u>approximate most powerful unbiased invariant test</u> is:  reject $H_0$ at $\alpha$-level if

$$\left\{ \sum_{j=1}^{n_1} X^2_{ij}/n_1 \right\} \Big/ \left\{ \sum_{j=1}^{n_2} X^2_{ij}/n_2 \right\} > F^{n_1}_{n_2}\left(\frac{\alpha}{2}\right) \quad \text{or} < F^{n_1}_{n_2}\left(1-\frac{\alpha}{2}\right)$$

## TABLES FOR POWER STUDIES

The tables have a standard format which is self explanatory. We find the:

Sample sizes: N1, N2

Means: MU1, MU2

Standard deviations: SIGMA1, SIGMA2

Coefficients of variation: BETA1, BETA2

Two other parameters are noted

THETA = MU1/MU2

PSI = BETA1/BETA2

The parameter PSI is designed to study the robustness of the L-R test when relaxing the assumption of homogeneous coefficients of variation and has proved extremely helpful.

The number of rejections, out of 100 samples, simulated with the given populations parameters, is given for each test. 90 such tables are presented. Several tables have been repeated with 1000 samples. These tables are: 5A, 14A, 15A, 24A, 25A, 27A, 35A, 36A, 37A and they can be distinguished by smaller printing caracters.

Sample sizes used are:

$$N1 = 10 \quad , \quad N2 = 10 \quad , \quad \text{table} \quad 1 \text{ to table } 38$$

$$N1 = 2 \quad , \quad N2 = 4 \quad , \quad \text{table } 39 \text{ to table } 51$$

$$N1 = 6 \quad , \quad N2 = 10 \quad , \quad \text{table } 52 \text{ to table } 64$$

$$N1 = 6 \quad , \quad N2 = 20 \quad , \quad \text{table } 65 \text{ to table } 77$$

$$N1 = 10 \quad , \quad N2 = 20 \quad , \quad \text{table } 78 \text{ to table } 90$$

For sample sizes $(N_1, N_2)$ = (2,4), (6,10), (6,20), (10,20) the same set of population parameters are used and they correspond to a subset of population parameters of the first 38 tables.

Many cross-references can be made between the tables and in order to facilitate this process, we give here the description of each table.

| Table no | N1 | N2 | $\mu_1$ | $\mu_2$ | $\sigma_1$ | $\sigma_2$ | $\beta_1$ | $\beta_2$ | $\theta$ | PSI |
|---|---|---|---|---|---|---|---|---|---|---|
| 1 | 10 | 10 | 8 | 10 | 2 | 2.5 | 0.25 | 0.25 | 0.8 | 1 |
| 2 | | | 2 | 6 | 1 | 3 | 0.5 | 0.5 | 0.33 | 1 |
| 3 | | | 2.67 | 4.67 | 2 | 3.5 | 0.75 | 0.75 | 0.57 | 1 |
| 4 | | | 2 | 4 | 2 | 4 | 1 | 1 | 0.5 | 1 |
| 5 | | | 1 | 3 | 2 | 6 | 2 | 2 | 0.33 | 1 |
| 5A | | | same as table 5 but with 1000 samples | | | | | | | |
| 6 | | | 1 | 1 | 2 | 4 | 2 | 4 | 1 | 0.5 |
| 7 | | | 8 | 10 | 2 | 2 | 0.25 | 0.20 | 0.8 | 1.25 |
| 8 | same | | 1 | 2 | 2 | 1 | 2 | 0.5 | 0.5 | 4 |
| 9 | as | | 1 | 3 | 2 | 2.5 | 2 | 0.83 | 0.33 | 2.40 |
| 10 | above | | 4 | 6 | 2 | 2.5 | 0.5 | 0.42 | 0.67 | 1.20 |
| 11 | | | 1 | 3 | 2 | 4 | 2 | 1.33 | 0.33 | 1.50 |
| 12 | | | 1 | 1 | 2 | 2 | 2 | 2 | 1 | 1 |
| 13 | | | 1 | 1 | 0.5 | 0.5 | 0.5 | 0.5 | 1 | 1 |
| 14 | | | 1 | 2 | 3 | 6 | 3 | 3 | 2 | 1 |
| 14A | | | same as table 14 but with 1000 samples | | | | | | | |

| Table no | N1 | N2 | $\mu_1$ | $\mu_2$ | $\sigma_1$ | $\sigma_2$ | $\beta_1$ | $\beta_2$ | $\theta$ | PSI |
|---|---|---|---|---|---|---|---|---|---|---|
| 15 | 10 | 10 | 1 | 2 | 4 | 8 | 4 | 4 | 0.5 | 1 |
| 15A | | | same as table 15 but with 1000 samples | | | | | | | |
| 16 | | | 1 | 0.5 | 4 | 2 | 4 | 4 | 2 | 1 |
| 17 | | | 1 | 5 | 5 | 25 | 5 | 5 | 0.2 | 1 |
| 18 | | | 1 | 1.2 | 10 | 12 | 10 | 10 | 0.8 | 1 |
| 19 | | | 0.95 | 1 | 0.475 | 0.5 | 0.5 | 0.5 | 0.95 | 1 |
| 20 | | | 0.8 | 0.6 | 4 | 3 | 5 | 5 | 1.33 | 1 |
| 21 | | | 0.6 | 0.2 | 3.6 | 1.2 | 6 | 6 | 3 | 1 |
| 22 | | | 1 | 1.5 | 2 | 3 | 2 | 2 | 0.67 | 1 |
| 23 | | | 2 | 1.5 | 1 | 3 | 0.5 | 2 | 1.33 | 0.25 |
| 24 | | | 1 | 0.5 | 3 | 1.5 | 3 | 3 | 2 | 1 |
| 24A | | | same as table 24 but with 1000 samples | | | | | | | |
| 25 | | | 0.75 | 0.5 | 2.25 | 1.5 | 3 | 3 | 1.5 | 1 |
| 25A | | | same as table 25 but with 1000 samples | | | | | | | |
| 26 | same | | 1 | 0.5 | 4 | 2 | 4 | 4 | 2 | 1 |
| 27 | as | | 0.75 | 0.5 | 3 | 2 | 4 | 4 | 1.5 | 1 |
| 27A | above | | same as table 27 but with 1000 samples | | | | | | | |
| 28 | | | 0.75 | 0.5 | 3.75 | 2.5 | 5 | 5 | 1.5 | 1 |
| 29 | | | 0.5 | 1.5 | 1 | 3 | 2 | 2 | 0.33 | 1 |
| 30 | | | 1 | 2 | 0.05 | 0.10 | 0.05 | 0.05 | 0.5 | 1 |
| 31 | | | 1 | 2 | 0.10 | 0.20 | 0.10 | 0.10 | 0.5 | 1 |
| 32 | | | 1 | 2 | 0.15 | 0.30 | 0.15 | 0.15 | 0.5 | 1 |
| 33 | | | 1 | 1.5 | 0.2 | 0.3 | 0.20 | 0.20 | 0.33 | 1 |
| 34 | | | 1 | 2 | 0.5 | 1.2 | 0.5 | 0.6 | 0.5 | 0.83 |
| 35 | | | 1 | 2 | 1 | 4 | 1 | 2 | 0.5 | 0.5 |
| 35A | | | same as table 35 but with 1000 samples | | | | | | | |
| 36 | | | 1 | 2 | 1.5 | 2 | 1.5 | 1 | 0.5 | 1.5 |
| 36A | | | same as table 36 but with 1000 samples | | | | | | | |
| 37 | | | 1 | 2 | 1 | 3 | 1 | 1.5 | 0.5 | 0.67 |
| 37A | | | same as table 37 but with 1000 samples | | | | | | | |
| 38 | | | 1 | 2 | 2 | 2 | 2 | 1 | 0.5 | 2 |

| Table no | N1 | N2 | $\mu_1$ | $\mu_2$ | $\sigma_1$ | $\sigma_2$ | $\beta_1$ | $\beta_2$ | $\theta$ | PSI |
|---|---|---|---|---|---|---|---|---|---|---|
| 39 | 2 | 4 | same | as | in | table 1 | | | | |
| 40 | | | " | " | " | " | 4 | | | |
| 41 | | | " | " | " | " | 6 | | | |
| 42 | | | " | " | " | " | 7 | | | |
| 43 | | | " | " | " | " | 10 | | | |
| 44 | same | | " | " | " | " | 11 | | | |
| 45 | as | | " | " | " | " | 14 | | | |
| 46 | above | | " | " | " | " | 20 | | | |
| 47 | | | " | " | " | " | 31 | | | |
| 48 | | | " | " | " | " | 34 | | | |
| 49 | | | " | " | " | " | 35 | | | |
| 50 | | | " | " | " | " | 36 | | | |
| 51 | | | " | " | " | " | 38 | | | |
| | | | | | | | | | | |
| 52 | 6 | 10 | " | " | " | " | 1 | | | |
| 53 | | | " | " | " | " | 4 | | | |
| 54 | | | " | " | " | " | 6 | | | |
| 55 | | | " | " | " | " | 7 | | | |
| 56 | | | " | " | " | " | 10 | | | |
| 57 | same | | " | " | " | " | 11 | | | |
| 58 | as | | " | " | " | " | 14 | | | |
| 59 | above | | " | " | " | " | 20 | | | |
| 60 | | | " | " | " | " | 31 | | | |
| 61 | | | " | " | " | " | 34 | | | |
| 62 | | | " | " | " | " | 35 | | | |
| 63 | | | " | " | " | " | 36 | | | |
| 64 | | | " | " | " | " | 38 | | | |
| | | | | | | | | | | |
| 65 | 6 | 20 | " | " | " | " | 1 | | | |
| 66 | | | " | " | " | " | 4 | | | |
| 67 | same | | " | " | " | " | 6 | | | |
| 68 | as | | " | " | " | " | 7 | | | |
| 69 | above | | " | " | " | " | 10 | | | |

| Table no | N1 | N2 | $\mu_1$ | $\mu_2$ | $\sigma_1$ | $\sigma_2$ | $\beta_1$ | $\beta_2$ | $\theta$ | PSI |
|---|---|---|---|---|---|---|---|---|---|---|
| 70 | 6 | 20 | same | as | in | table | 11 | | | |
| 71 | | | " | " | " | " | 14 | | | |
| 72 | same | | " | " | " | " | 20 | | | |
| 73 | as | | " | " | " | " | 31 | | | |
| 74 | above | | " | " | " | " | 34 | | | |
| 75 | | | " | " | " | " | 35 | | | |
| 76 | | | " | " | " | " | 36 | | | |
| 77 | | | " | " | " | " | 38 | | | |
| 78 | 10 | 20 | " | " | " | " | 1 | | | |
| 79 | | | " | " | " | " | 4 | | | |
| 80 | | | " | " | " | " | 6 | | | |
| 81 | | | " | " | " | " | 7 | | | |
| 82 | | | " | " | " | " | 10 | | | |
| 83 | same | | " | " | " | " | 11 | | | |
| 84 | as | | " | " | " | " | 14 | | | |
| 85 | above | | " | " | " | " | 20 | | | |
| 86 | | | " | " | " | " | 31 | | | |
| 87 | | | " | " | " | " | 34 | | | |
| 88 | | | " | " | " | " | 35 | | | |
| 89 | | | " | " | " | " | 36 | | | |
| 90 | | | " | " | " | " | 38 | | | |

## SOME CONCLUSIONS

Extensive study of the tables indicates that the L-R test has the following remarkable properties.

1)  Lohrding stated, for the equal sample size case $(n_1 = n_2)$, that the L-R test was good only for the coefficient of variation between 0.25 to 1.0. Contrary to Lohrding's conclusion the L-R test indicates maximum power for all values of the common coefficient of variation. Moreover the same conclusion holds true for equal and unequal sample sizes alike. This is confirmed by table 1, 2, 3, 4, 5, 14, 15, 16, 17, 18, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 39, 40, 45, 47, 52, 53, 58, 60, 65, 66, 71, 72, 78, 79, 84, 86.

2)  This is not to say that other tests do not achieve the same power as the L-R test but they do so only under some restrictive conditions.

    Such is the case when the standard deviations are nearly equal for the t-test: table 1, 7, 10, 19, 30, 31, 32, 33, 36, 38, 39, 42, 43, 47, 50, 51, 52, 55, 56, 60, 63, 64, 65, 68, 69, 73, 76, 77, 78, 81, 82, 86, 89, 90.

    Such is the case when the standard deviations are widely different for the F-test: table 5, 6, 14, 15, 16, 17, 21, 22, 24, 26, 27, 28, 29, 37, 41, 45, 54, 58, 67, 71, 80, 84.

3)  Another very important finding is that the L-R ratio test remains robust when relaxing the assumption of equal coefficient of variation. As a practical rule the L-R test remains robust in the range $0.67 \leqslant PSI \leqslant 1.50$ where $PSI = \beta_1/\beta_2$. This is supported by table 7, 10, 11, 34, 36, 37, 42, 43, 44, 48, 50, 55, 57, 61, 63, 68, 69, 70, 74, 76, 81, 82, 83, 89.

4) However, if the common coefficient of variation is greater than or equal to 3, the approximately optimum most powerful invariant test (U-test) has nearly the same power as the L-R test. This is evident from table 12, 14, 15, 16, 17, 18, 24, 25, 26, 27, 28, 29, 45, 58, 71, 84. But since the former is computationally much simpler that the latter, we advocate its use whenever the common coefficient is greater than 3.

## ACKNOWLEDGEMENT

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    Statist. 40, 1374-1385.

```
*****************
*   TABLE  NO  1  *
*****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 8.000 | MU2=10.000 |
| SIGMA1= 2.000 | SIGMA2= 2.500 |
| BETA1=SIGMA1/MU1= 0.250 | BETA2=SIGMA2/MU2= 0.250 |
| THETA=MU1/MU2= 0.800 | PSI=BETA1/BETA2= 1.000 |

```
***********************************************
*               *           ALPHA-LEVEL          *
* TEST STATISTIC **********************************
*               *   0.01   *   0.05   *   0.10   *
***********************************************
*    LAMBDA     *    28    *    51    *    66    *
***********************************************
*      U        *    0     *    0     *    0     *
***********************************************
*      F        *    0     *    3     *    10    *
***********************************************
*      T        *    23    *    49    *    65    *
***********************************************
*    TPRIME     *    11    *    +5    *    62    *
***********************************************
```

```
******************
*  TABLE  NO  2  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 2.000 | MU2= 6.000 |
| SIGMA1= 1.000 | SIGMA2= 3.000 |
| BETA1=SIGMA1/MU1= 0.500 | BETA2=SIGMA2/MU2= 0.500 |
| THETA=MU1/MU2= 0.333 | PSI=BETA1/BETA2= 1.000 |

```
***********************************************************
*                *             ALPHA-LEVEL              *
* TEST STATISTIC ******************************************
*                *   0.01   *   0.05   *   0.10   *
***********************************************************
*    LAMBDA      *   100    *   100    *   100    *
***********************************************************
*      U         *    87    *   100    *   100    *
***********************************************************
*      F         *    65    *    88    *    94    *
***********************************************************
*      T         *    86    *    96    *    99    *
***********************************************************
*    TPRIME      *    72    *    94    *    98    *
***********************************************************
```

```
*******************
*  TABLE  NO  3  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 2.670 | MU2= 4.670 |
| SIGMA1= 2.000 | SIGMA2= 3.500 |
| BETA1=SIGMA1/MU1= 0.750 | BETA2=SIGMA2/MU2= 0.750 |
| THETA=MU1/MU2= 0.570 | PSI=BETA1/BETA2= 1.000 |

```
***********************************************************
*                  *              ALPHA-LEVEL           *
* TEST STATISTIC   ****************************************
*                  *  0.01  *  0.05  *  0.10  *
***********************************************************
*    LAMBDA        *   24   *   53   *   64   *
***********************************************************
*      U           *    4   *   22   *   40   *
***********************************************************
*      F           *   13   *   30   *   45   *
***********************************************************
*      T           *   13   *   29   *   36   *
***********************************************************
*    TPRIME        *    4   *   25   *   33   *
***********************************************************
```

```
*******************
*   TABLE  NO  4  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                               N2= 10

MU1= 2.000                           MU2= 4.000

SIGMA1= 2.000                        SIGMA2= 4.000

BETA1=SIGMA1/MU1= 1.000         BETA2=SIGMA2/MU2= 1.000

THETA=MU1/MU2= 0.500            PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 38 | 69 | 84 |
| U | 25 | 53 | 68 |
| F | 21 | 49 | 67 |
| T | 10 | 25 | 47 |
| TPRIME | 4 | 19 | 38 |

```
*******************
*   TABLE  NO  5  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 3.000 |
| SIGMA1= 2.000 | SIGMA2= 6.000 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.333 | PSI=BETA1/BETA2= 1.000 |

```
***************************************************
*                  *            ALPHA-LEVEL           *
* TEST STATISTIC   *************************************
*                  *   0.01   *   0.05   *   0.10    *
***************************************************
*    LAMBDA        *    76    *    97    *    97     *
***************************************************
*      U           *    74    *    95    *    98     *
***************************************************
*      F           *    69    *    86    *    94     *
***************************************************
*      T           *    0     *    19    *    28     *
***************************************************
*    TPRIME        *    2     *    14    *    23     *
***************************************************
```

```
******************
*  TABLE NO  5A  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1 = 10 | N2 = 10 |
| MU1 = 1.000 | MU2 = 3.000 |
| SIGMA1 = 2.000 | SIGMA2 = 6.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.333 | PSI=BETA1/BETA2= 1.000 |

```
*****************************************************
*                  *          ALPHA-LEVEL          *
* TEST STATISTIC   *******************************************
*                  *   0.01   *   0.05   *   0.10   *
*****************************************************
*     LAMBDA       *   753    *   926    *   961    *
*****************************************************
*       U          *   729    *   919    *   953    *
*****************************************************
*       F          *   662    *   870    *   928    *
*****************************************************
*       T          *    54    *   153    *   254    *
*****************************************************
*     TPRIME       *    20    *   118    *   208    *
*****************************************************
```

```
*********************
*   TABLE  NO  6   *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 1.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 4.000 |
| THETA=MU1/MU2= 1.000 | PSI=BETA1/BETA2= 0.500 |

```
*********************************************************
*                    *           ALPHA-LEVEL           *
* TEST STATISTIC *****************************************
*                    *  0.01  *  0.05  *  0.10  *
*********************************************************
*     LAMBDA    *   19   *   47   *   63   *
*********************************************************
*      U        *   13   *   44   *   65   *
*********************************************************
*      F        *   22   *   47   *   62   *
*********************************************************
*      T        *    1   *    3   *   12   *
*********************************************************
*    TPRIME     *    0   *    2   *    6   *
*********************************************************
```

```
*********************
*   TABLE  NO 7     *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 8.000 | MU2=10.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 0.250 | BETA2=SIGMA2/MU2= 0.200 |
| THETA=MU1/MU2= 0.800 | PSI=BETA1/BETA2= 1.250 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 26 | 55 | 69 |
| U | 0 | 0 | 0 |
| F | 1 | 5 | 10 |
| T | 34 | 62 | 71 |
| TPRIME | 18 | 50 | 64 |

```
*******************
*  TABLE  NO  8  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 2.000 | SIGMA2= 1.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 0.500 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 4.000 |

```
***************************************************
*                  *          ALPHA-LEVEL        *
* TEST STATISTIC   ********************************
*                  *  0.01  *  0.05  *   0.10  *
***************************************************
*     LAMBDA       *   1    *   5    *    10   *
***************************************************
*       U          *   0    *   0    *    1    *
***************************************************
*       F          *   30   *   55   *    68   *
***************************************************
*       T          *   10   *   29   *    48   *
***************************************************
*     TPRIME       *   2    *   24   *    42   *
***************************************************
```

```
*******************
*  TABLE  NO 10  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                                  N2= 10

MU1= 4.000                              MU2= 6.000

SIGMA1= 2.000                           SIGMA2= 2.500

BETA1=SIGMA1/MU1= 0.500          BETA2=SIGMA2/MU2= 0.416

THETA=MU1/MU2= 0.670             PSI=BETA1/BETA2= 1.200

```
***********************************************************
*                 *            ALPHA-LEVEL              *
* TEST STATISTIC  ****************************************
*                 *   0.01   *   0.05   *   0.10   *
***********************************************************
*    LAMBDA       *    23    *    52    *    66    *
***********************************************************
*      U          *    1     *    8     *    18    *
***********************************************************
*      F          *    4     *    11    *    17    *
***********************************************************
*      T          *    21    *    53    *    64    *
***********************************************************
*    TPRIME       *    13    *    43    *    60    *
***********************************************************
```

```
*******************
*   TABLE  NO 11   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 3.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 1.333 |
| THETA=MU1/MU2= 0.333 | PSI=BETA1/BETA2= 1.500 |

```
*******************************************************
*                  *          ALPHA-LEVEL            *
* TEST STATISTIC   *************************************
*                  *   0.01  *   0.05  *   0.10  *
*******************************************************
*     LAMBDA       *    41   *    69   *    78   *
*******************************************************
*       U          *    45   *    71   *    82   *
*******************************************************
*       F          *    27   *    53   *    67   *
*******************************************************
*       T          *    14   *    27   *    43   *
*******************************************************
*     TPRIME       *     5   *    21   *    34   *
*******************************************************
```

```
*******************
*  TABLE   NO 12   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 1.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 1.000 | PSI=BETA1/BETA2= 1.000 |

```
*********************************************************
*                  *           ALPHA-LEVEL             *
* TEST STATISTIC   **********************************
*                  *  0.01   *   0.05   *   0.10   *
*********************************************************
*    LAMBDA        *    0    *    1     *    8     *
*********************************************************
*      U           *    0    *    1     *    8     *
*********************************************************
*      F           *    1    *    2     *    4     *
*********************************************************
*      T           *    1    *    4     *   10     *
*********************************************************
*    TPRIME        *    0    *    1     *    7     *
*********************************************************
```

```
******************
*  TABLE  NO 13  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                          N2= 10

MU1= 1.000                      MU2= 1.000

SIGMA1= 0.500                   SIGMA2= 0.500

BETA1=SIGMA1/MU1= 0.500     BETA2=SIGMA2/MU2= 0.500

THETA=MU1/MU2= 1.000        PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 2 | 5 | 7 |
| U | 0 | 0 | 1 |
| F | 1 | 6 | 7 |
| T | 1 | 6 | 12 |
| TPRIME | 0 | 4 | 12 |

```
*******************
*  TABLE  NO 14  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 10 | N2= 10 |
|---|---|
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 3.000 | SIGMA2= 6.000 |

| BETA1=SIGMA1/MU1= 3.000 | BETA2=SIGMA2/MU2= 3.000 |
|---|---|
| THETA=MU1/MU2= 2.000 | PSI=BETA1/BETA2= 1.000 |

```
*****************************************************
*                 *            ALPHA-LEVEL         *
* TEST STATISTIC  ***********************************
*                 *  0.01  *  0.05  *   0.10   *
*****************************************************
*    LAMBDA       *   28   *   52   *   69     *
*****************************************************
*      U          *   27   *   58   *   67     *
*****************************************************
*      F          *   27   *   48   *   58     *
*****************************************************
*      T          *    2   *    6   *   17     *
*****************************************************
*    TPRIME       *    1   *    5   *    8     *
*****************************************************
```

```
*******************
*   TABLE NO 14A   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                                   N2= 10

MU1= 1.000                               MU2= 2.000

SIGMA1= 3.000                            SIGMA2= 6.000

BETA1=SIGMA1/MU1= 3.000          BETA2=SIGMA2/MU2= 3.000

THETA=MU1/MU2= 2.000             PSI=BETA1/BETA2= 1.000

```
***********************************************************
*                    *          ALPHA-LEVEL              *
* TEST STATISTIC  *****************************************
*                    *  0.01   *   0.05   *   0.10   *
***********************************************************
*     LAMBDA         *  238    *   509    *   657    *
***********************************************************
*       U            *  257    *   537    *   661    *
***********************************************************
*       F            *  217    *   484    *   618    *
***********************************************************
*       T            *   9     *    63    *   125    *
***********************************************************
*     TPRIME         *   1     *    39    *    95    *
***********************************************************
```

```
*******************
*   TABLE   NO 15   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 4.000 | SIGMA2= 8.000 |

BETA1=SIGMA1/MU1= 4.000      BETA2=SIGMA2/MU2= 4.000

THETA=MU1/MU2= 0.500      PSI=BETA1/BETA2= 1.000

```
**********************************************************
*                    *           ALPHA-LEVEL              *
* TEST STATISTIC   ***************************************
*                    *  0.01  *  0.05  *   0.10   *
**********************************************************
*    LAMBDA         *   26   *   60   *   70     *
**********************************************************
*      U            *   33   *   58   *   75     *
**********************************************************
*      F            *   27   *   54   *   70     *
**********************************************************
*      T            *    1   *    5   *   14     *
**********************************************************
*    TPRIME         *    0   *    3   *    9     *
**********************************************************
```

```
*********************
*   TABLE NO 15A   *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 4.000 | SIGMA2= 8.000 |

BETA1=SIGMA1/MU1= 4.000      BETA2=SIGMA2/MU2= 4.000

THETA=MU1/MU2= 0.500      PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL 0.01 | 0.05 | 0.10 |
|---|---|---|---|
| LAMBDA | 266 | 551 | 683 |
| U | 296 | 570 | 695 |
| F | 255 | 506 | 646 |
| T | 16 | 70 | 138 |
| TPRIME | 6 | 47 | 104 |

```
******************
*  TABLE  Nu 16  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 0.500 |
| SIGMA1= 4.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 4.000 | BETA2=SIGMA2/MU2= 4.000 |
| THETA=MU1/MU2= 2.000 | PSI=BETA1/BETA2= 1.000 |

```
****************************************************
*                  *           ALPHA-LEVEL        *
* TEST STATISTIC   ********************************
*                  *   0.01   *  0.05   *  0.10    *
****************************************************
*     LAMBDA       *    22    *   53    *   62     *
****************************************************
*       U          *    24    *   55    *   65     *
****************************************************
*       F          *    20    *   49    *   59     *
****************************************************
*       T          *     0    *    6    *   12     *
****************************************************
*     TPRIME       *     0    *    1    *   11     *
****************************************************
```

```
******************
*  TABLE  NO 17  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 10 | N2= 10 |
|---|---|
| MU1= 1.000 | MU2= 5.000 |
| SIGMA1= 5.000 | SIGMA2=25.000 |
| BETA1=SIGMA1/MU1= 5.000 | BETA2=SIGMA2/MU2= 5.000 |
| THETA=MU1/MU2= 0.200 | PSI=BETA1/BETA2= 1.000 |

```
*****************************************************
*               *           ALPHA-LEVEL            *
* TEST STATISTIC *************************************
*               *  0.01   *  0.05   *  0.10   *
*****************************************************
*    LAMBDA     *   99    *   99    *   99    *
*****************************************************
*     U         *   98    *   99    *   99    *
*****************************************************
*     F         *   98    *   99    *   99    *
*****************************************************
*     T         *    2    *   14    *   18    *
*****************************************************
*    TPRIME     *    0    *    9    *   17    *
*****************************************************
```

```
*********************
*   TABLE   NO 18   *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 10 | | N2= 10 |
|---|---|---|
| MU1= 1.000 | | MU2= 1.200 |
| SIGMA1=10.000 | | SIGMA2=12.000 |

BETA1=SIGMA1/MU1=10.000      BETA2=SIGMA2/MU2=10.000

THETA=MU1/MU2= 0.800      PSI=BETA1/BETA2= 1.000

```
***************************************************
*                    *        ALPHA-LEVEL         *
* TEST STATISTIC *************************************
*                    *  0.01  *  0.05  *  0.10  *
***************************************************
*   LAMBDA    *    2   *    5   *   11   *
***************************************************
*     U       *    2   *    7   *   15   *
***************************************************
*     F       *    1   *    8   *   11   *
***************************************************
*     T       *    0   *    6   *   10   *
***************************************************
*   TPRIME    *    0   *    4   *    9   *
***************************************************
```

```
*******************
*   TABLE   NO 19   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 0.950 | MU2= 1.000 |
| SIGMA1= 0.475 | SIGMA2= 0.500 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 0.500 | BETA2=SIGMA2/MU2= 0.500 |
| THETA=MU1/MU2= 0.950 | PSI=BETA1/BETA2= 1.000 |

```
******************************************************
*                    *         ALPHA-LEVEL            *
* TEST STATISTIC ***********************************
*                    *  0.01  *  0.05  *   0.10   *
******************************************************
*    LAMBDA      *    1   *    7   *   13    *
******************************************************
*      U         *    0   *    0   *    0    *
******************************************************
*      F         *    0   *    1   *    7    *
******************************************************
*      T         *    2   *    7   *   13    *
******************************************************
*    TPRIME      *    0   *    4   *   10    *
******************************************************
```

```
*******************
*  TABLE  NO 20  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 10 | N2= 10 |
|---|---|
| MU1= 0.800 | MU2= 0.800 |
| SIGMA1= 4.000 | SIGMA2= 3.000 |
| BETA1=SIGMA1/MU1= 5.000 | BETA2=SIGMA2/MU2= 5.000 |
| THETA=MU1/MU2= 1.333 | PSI=BETA1/BETA2= 1.000 |

```
***********************************************************
*                    *          ALPHA-LEVEL          *
*  TEST STATISTIC  ***************************************
*                    *  0.01  *  0.05  *  0.10  *
***********************************************************
*     LAMBDA      *    0    *   16   *   25   *
***********************************************************
*       U         *    1    *   19   *   27   *
***********************************************************
*       F         *    2    *   13   *   22   *
***********************************************************
*       T         *    1    *    6   *   10   *
***********************************************************
*     TPRIME      *    1    *    5   *    8   *
***********************************************************
```

.36

```
*******************
*   TABLE   NO 21   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 0.600 | MU2= 0.200 |
| SIGMA1= 3.600 | SIGMA2= 1.200 |
| BETA1=SIGMA1/MU1= 6.000 | BETA2=SIGMA2/MU2= 6.000 |
| THETA=MU1/MU2= 3.000 | PSI=BETA1/BETA2= 1.000 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 68 | 88 | 93 |
| U | 69 | 88 | 94 |
| F | 64 | 89 | 93 |
| T | 2 | 4 | 7 |
| TPRIME | 0 | 3 | 5 |

```
*******************
*   TABLE  NO 22  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 1.500 |
| SIGMA1= 2.000 | SIGMA2= 3.000 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.670 | PSI=BETA1/BETA2= 1.000 |

```
*****************************************************
*                    *            ALPHA-LEVEL              *
* TEST STATISTIC *************************************
*                    *   0.01   *   0.05   *   0.10   *
*****************************************************
*     LAMBDA     *     4    *    17    *    28    *
*****************************************************
*       U        *     4    *    15    *    24    *
*****************************************************
*       F        *     5    *    19    *    27    *
*****************************************************
*       T        *     0    *     3    *    10    *
*****************************************************
*     TPRIME     *     0    *     1    *     7    *
*****************************************************
```

```
*****************
*  TABLE  NO 23  *
*****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 2.000 | MU2= 1.500 |
| SIGMA1= 1.000 | SIGMA2= 3.000 |
| BETA1=SIGMA1/MU1= 0.50 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 1.333 | PSI=BETA1/BETA2= 0.125 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 20 | 53 | 66 |
| U | 3 | 16 | 23 |
| F | 71 | 89 | 94 |
| T | + | 8 | 10 |
| TPRIME | 0 | 8 | 9 |

```
*****************
*  TABLE  NO 24  *
*****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 0.500 |
| SIGMA1= 3.000 | SIGMA2= 1.500 |
| BETA1=SIGMA1/MU1= 3.000 | BETA2=SIGMA2/MU2= 3.000 |
| THETA=MU1/MU2= 2.000 | PSI=BETA1/BETA2= 1.000 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 26 | 59 | 68 |
| U | 28 | 60 | 70 |
| F | 23 | 53 | 67 |
| T | 1 | 6 | 15 |
| TPRIME | 0 | 2 | 8 |

```
*******************
*   TABLE NO 24A   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                            N2= 10

MU1= 1.000                        MU2= 0.500

SIGMA1= 3.000                     SIGMA2= 1.500

BETA1=SIGMA1/MU1= 3.000     BETA2=SIGMA2/MU2= 3.000

THETA=MU1/MU2= 2.000        PSI=BETA1/BETA2= 1.000

```
*********************************************************
*                    *          ALPHA-LEVEL            *
* TEST STATISTIC *****************************************
*                    *   0.01  *   0.05  *   0.10  *
*********************************************************
*    LAMBDA          *   282   *   551   *   691   *
*********************************************************
*      U             *   300   *   571   *   695   *
*********************************************************
*      F             *   248   *   511   *   647   *
*********************************************************
*      T             *   20    *   74    *   135   *
*********************************************************
*    TPRIME          *   9     *   51    *   101   *
*********************************************************
```

```
*******************
*   TABLE NO 25   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | | | |
|---|---|---|---|
| N1= 10 | | N2= 10 | |
| MU1= 0.750 | | MU2= 0.500 | |
| SIGMA1= 2.250 | | SIGMA2= 1.500 | |
| BETA1=SIGMA1/MU1= 3.000 | | BETA2=SIGMA2/MU2= 3.000 | |
| THETA=MU1/MU2= 1.500 | | PSI=BETA1/BETA2= 1.000 | |

```
********************************************************
*                *             ALPHA-LEVEL             *
* TEST STATISTIC ***************************************
*                *   0.01   *   0.05   *   0.10   *
********************************************************
*    LAMBDA      *    8     *    25    *    34    *
********************************************************
*    U           *    10    *    24    *    30    *
********************************************************
*    F           *    8     *    25    *    33    *
********************************************************
*    T           *    2     *    5     *    6     *
********************************************************
*    TPRIME      *    0     *    4     *    5     *
********************************************************
```

```
*******************
*   TABLE NO 25A   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 10 | N2= 10 |
|---|---|
| MU1= 0.750 | MU2= 0.500 |
| SIGMA1= 2.250 | SIGMA2= 1.500 |

BETA1=SIGMA1/MU1= 3.000          BETA2=SIGMA2/MU2= 3.000

THETA=MU1/MU2= 1.500          PSI=BETA1/BETA2= 1.000

```
*************************************************************
*                    *            ALPHA-LEVEL              *
* TEST STATISTIC *********************************************
*                    *   0.01   *   0.05   *   0.10   *
*************************************************************
*      LAMBDA     *    49    *    190    *    312    *
*************************************************************
*        U        *    67    *    201    *    314    *
*************************************************************
*        F        *    51    *    179    *    287    *
*************************************************************
*        T        *    10    *    74     *    126    *
*************************************************************
*      TPRIME     *     7    *    46     *    101    *
*************************************************************
```

```
******************
*   TABLE  NO 26  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 0.500 |
| SIGMA1= 4.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 4.000 | BETA2=SIGMA2/MU2= 4.000 |
| THETA=MU1/MU2= 2.000 | PSI=BETA1/BETA2= 1.000 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 24 | 55 | 71 |
| U | 28 | 59 | 76 |
| F | 26 | 53 | 65 |
| T | 0 | 5 | 11 |
| TPRIME | 0 | 2 | 6 |

```
*******************
*   TABLE   NO 27   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 0.750 | MU2= 0.500 |
| SIGMA1= 3.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 4.000 | BETA2=SIGMA2/MU2= 4.000 |
| THETA=MU1/MU2= 1.500 | PSI=BETA1/BETA2= 1.000 |

```
****************************************************
*                     *         ALPHA-LEVEL          *
*  TEST STATISTIC  ********************************
*                     *   0.01   *   0.05   *   0.10   *
****************************************************
*      LAMBDA      *    11    *    24    *    37    *
****************************************************
*        U         *    11    *    24    *    40    *
****************************************************
*        F         *    11    *    25    *    40    *
****************************************************
*        T         *     1    *     4    *     5    *
****************************************************
*      TPRIME      *     0    *     4    *     5    *
****************************************************
```

```
******************
*  TABLE NO 27A   *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                          N2= 10

MU1= 0.750                      MU2= 0.500

SIGMA1= 3.000                   SIGMA2= 2.000

BETA1=SIGMA1/MU1= 4.000         BETA2=SIGMA2/MU2= 4.000

THETA=MU1/MU2= 1.500            PSI=BETA1/BETA2= 1.000

```
*********************************************************
*                 *           ALPHA-LEVEL              *
* TEST STATISTIC  **************************************
*                 *   0.01   *   0.05   *   0.10   *
*********************************************************
*    LAMBDA       *    46    *   188    *   307    *
*********************************************************
*      U          *    62    *   200    *   317    *
*********************************************************
*      F          *    51    *   179    *   287    *
*********************************************************
*      T          *    10    *    66    *   116    *
*********************************************************
*    TPRIME       *     5    *    39    *    97    *
*********************************************************
```

```
*******************
*   TABLE   NO 28   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 0.750 | MU2= 0.500 |
| SIGMA1= 3.750 | SIGMA2= 2.500 |
| BETA1=SIGMA1/MU1= 5.000 | BETA2=SIGMA2/MU2= 5.000 |
| THETA=MU1/MU2= 1.500 | PSI=BETA1/BETA2= 1.000 |

```
***************************************************
*                  *           ALPHA-LEVEL         *
* TEST STATISTIC   ********************************
*                  *   0.01  *   0.05  *   0.10   *
***************************************************
*    LAMBDA        *    5    *   17    *   30     *
***************************************************
*      U           *    4    *   18    *   29     *
***************************************************
*      F           *    4    *   20    *   27     *
***************************************************
*      T           *    1    *    6    *    8     *
***************************************************
*    TPRIME        *    0    *    4    *    8     *
***************************************************
```

```
*****************
*  TABLE  NO 29  *
*****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 10 | N2= 10 |
|---|---|
| MU1= 0.500 | MU2= 1.500 |
| SIGMA1= 1.000 | SIGMA2= 3.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.333 | PSI=BETA1/BETA2= 1.000 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 68 | 91 | 97 |
| U | 70 | 90 | 95 |
| F | 62 | 87 | 94 |
| T | 3 | 13 | 24 |
| TPRIME | 1 | 8 | 20 |

```
******************
*  TABLE  NO 30  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.050 | SIGMA2= 0.100 |
| BETA1=SIGMA1/MU1= 0.050 | BETA2=SIGMA2/MU2= 0.050 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 1.000 |

```
*******************************************************
*               *            ALPHA-LEVEL            *
* TEST STATISTIC ************************************
*               *   0.01   *   0.05   *   0.10   *
*******************************************************
*     LAMBDA    *   100    *   100    *   100    *
*******************************************************
*       U       *    0     *    98    *   100    *
*******************************************************
*       F       *   30     *    52    *    62    *
*******************************************************
*       T       *   100    *   100    *   100    *
*******************************************************
*     TPRIME    *   100    *   100    *   100    *
*******************************************************
```

```
*******************
*  TABLE  NO 33  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 1.500 |
| SIGMA1= 0.200 | SIGMA2= 0.300 |
| BETA1=SIGMA1/MU1= 0.200 | BETA2=SIGMA2/MU2= 0.200 |
| THETA=MU1/MU2= 0.333 | PSI=BETA1/BETA2= 1.000 |

```
*****************************************************
*                  *          ALPHA-LEVEL         *
*  TEST STATISTIC  ********************************
*                  *  0.01  *  0.05  *  0.10  *
*****************************************************
*     LAMBDA       *   98   *  100   *  100   *
*****************************************************
*       U          *    0   *    0   *    6   *
*****************************************************
*       F          *    7   *   16   *   29   *
*****************************************************
*       T          *   93   *   98   *   99   *
*****************************************************
*     TPRIME       *   85   *   98   *   99   *
*****************************************************
```

```
******************
*   TABLE  NO 34  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.500 | SIGMA2= 1.200 |
| BETA1=SIGMA1/MU1= 0.500 | BETA2=SIGMA2/MU2= 0.600 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.833 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 79 | 98 | 100 |
| U | 20 | 66 | 80 |
| F | 40 | 67 | 75 |
| T | 34 | 62 | 79 |
| TPRIME | 20 | 53 | 78 |

```
******************
*   TABLE  NO 35   *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| NI= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 1.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.500 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 89 | 98 | 99 |
| U | 80 | 95 | 97 |
| F | 91 | 96 | 98 |
| T | 5 | 14 | 19 |
| TPRIME | 4 | 10 | 17 |

```
*******************
*  TABLE NO 35A   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.000 | SIGMA2= 4.000 |

BETA1=SIGMA1/MU1= 1.000      BETA2=SIGMA2/MU2= 2.000

THETA=MU1/MU2= 0.500      PSI=BETA1/BETA2= 0.500

| TEST STATISTIC | ALPHA-LEVEL 0.01 | 0.05 | 0.10 |
|---|---|---|---|
| LAMBDA | 904 | 976 | 992 |
| U | 791 | 942 | 968 |
| F | 900 | 965 | 980 |
| T | 34 | 118 | 195 |
| TPRIME | 15 | 85 | 149 |

```
*********************
*   TABLE  NO 36   *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.500 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 1.500 | BETA2=SIGMA2/MU2= 1.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 1.500 |

```
*********************************************************
*                 *           ALPHA-LEVEL              *
* TEST STATISTIC  ***************************************
*                 *  0.01  *  0.05  *  0.10  *
*********************************************************
*    LAMBDA       *   8    *   24   *   33   *
*********************************************************
*      U          *   6    *   24   *   34   *
*********************************************************
*      F          *   3    *   11   *   10   *
*********************************************************
*      T          *   5    *   24   *   40   *
*********************************************************
*    TPRIME       *   2    *   20   *   33   *
*********************************************************
```

```
*******************
*   TABLE NO 36A   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.500 | SIGMA2= 2.000 |

BETA1=SIGMA1/MU1= 1.500        BETA2=SIGMA2/MU2= 1.000

THETA=MU1/MU2= 0.500        PSI=BETA1/BETA2= 1.500

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 74 | 257 | 398 |
| U | 72 | 241 | 398 |
| F | 32 | 117 | 215 |
| T | 78 | 236 | 347 |
| TPRIME | 39 | 181 | 296 |

```
*********************
*   TABLE   NO 37   *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.000 | SIGMA2= 3.000 |
| BETA1=SIGMA1/MU1= 1.000 | BETA2=SIGMA2/MU2= 1.500 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.667 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 77 | 94 | 97 |
| U | 58 | 82 | 94 |
| F | 70 | 90 | 96 |
| T | 8 | 21 | 26 |
| TPRIME | 1 | 16 | 23 |

```
*******************
*   TABLE NO 37A   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 1000 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                          N2= 10

MU1= 1.000                      MU2= 2.000

SIGMA1= 1.000                   SIGMA2= 3.000

BETA1=SIGMA1/MU1= 1.000         BETA2=SIGMA2/MU2= 1.500

THETA=MU1/MU2= 0.500            PSI=BETA1/BETA2= 0.667

```
***********************************************************
*                  *           ALPHA-LEVEL              *
* TEST STATISTIC ******************************************
*                  *   0.01   *   0.05   *   0.10   *
***********************************************************
*     LAMBDA       *   749    *   902    *   949    *
***********************************************************
*       U          *   566    *   816    *   896    *
***********************************************************
*       F          *   671    *   860    *   907    *
***********************************************************
*       T          *   79     *   201    *   294    *
***********************************************************
*     TPRIME       *   38     *   159    *   251    *
***********************************************************
```

```
*******************
*   TABLE  NO 38   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 1.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 2.000 |

```
***********************************************************
*                    *         ALPHA-LEVEL              *
* TEST STATISTIC  *************************************
*                 *   0.01   *   0.05   *   0.10   *
***********************************************************
*    LAMBDA       *     3    *     8    *    12    *
***********************************************************
*      U          *     2    *     8    *    11    *
***********************************************************
*      F          *     1    *     7    *    11    *
***********************************************************
*      T          *     5    *    19    *    27    *
***********************************************************
*    TPRIME       *     2    *    15    *    23    *
***********************************************************
```

```
********************
*   TABLE   NO 39   *
********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1 = 2 | N2 = 4 |
| MU1 = 8.000 | MU2 = 10.000 |
| SIGMA1 = 2.000 | SIGMA2 = 2.500 |
| BETA1=SIGMA1/MU1= 0.250 | BETA2=SIGMA2/MU2= 0.250 |
| THETA=MU1/MU2= 0.800 | PSI=BETA1/BETA2= 1.000 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 5 | 22 | 33 |
| U | 0 | 0 | 0 |
| F | 1 | 4 | 8 |
| T | 4 | 18 | 28 |
| TPRIME | 0 | 3 | 18 |

```
*******************
*   TABLE  NO 40  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1=  2 | N2=  4 |
|---|---|
| MU1= 2.000 | MU2= 4.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 1.000 | BETA2=SIGMA2/MU2= 1.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 1.000 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 2 | 13 | 18 |
| U | 1 | 7 | 16 |
| F | 1 | 1 | 8 |
| T | 2 | 7 | 15 |
| TPRIME | 0 | 3 | 9 |

```
***************
*  TABLE  NO 41  *
***************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 2 | N2= 4 |
| MU1= 1.000 | MU2= 1.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 4.000 |
| THETA=MU1/MU2= 1.000 | PSI=BETA1/BETA2= 0.500 |

```
*****************************************
*                    *        ALPHA-LEVEL              *
* TEST STATISTIC *****************************************
*                    *  0.01   *   0.05   *   0.10   *
*****************************************
*    LAMBDA      *    0    *    3    *    10    *
*****************************************
*      U         *    0    *    7    *    13    *
*****************************************
*      F         *    1    *    1    *    6     *
*****************************************
*      T         *    0    *    6    *    7     *
*****************************************
*    TPRIME      *    0    *    4    *    4     *
*****************************************
```

```
********************
*   TABLE   NO  42  *
********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  2 | N2=  4 |
| MU1= 3.000 | MU2=10.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 0.250 | BETA2=SIGMA2/MU2= 0.200 |
| THETA=MU1/MU2= 0.800 | PSI=BETA1/BETA2= 1.250 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 3 | 14 | 29 |
| U | 0 | 0 | 0 |
| F | 2 | 6 | 9 |
| T | 3 | 18 | 28 |
| TPRIME | 0 | 2 | 6 |

```
**********************
*   TABLE   NO 43   *
**********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1= 2 | N2= 4 |
| MU1= 4.000 | MU2= 6.000 |
| SIGMA1= 2.000 | SIGMA2= 2.500 |

BETA1=SIGMA1/MU1= 0.500      BETA2=SIGMA2/MU2= 0.416

THETA=MU1/MU2= 0.670      PSI=BETA1/BETA2= 1.200

```
*******************************************************
*                  *          ALPHA-LEVEL              *
* TEST STATISTIC  **************************************
*                  *  0.01   *  0.05   *   0.10   *
*******************************************************
*    LAMBDA        *    4    *   19    *    25    *
*******************************************************
*      U           *    0    *    0    *     3    *
*******************************************************
*      F           *    0    *    4    *    10    *
*******************************************************
*      T           *    1    *   11    *    24    *
*******************************************************
*    TPRIME        *    0    *    5    *    12    *
*******************************************************
```

```
*********************
*   TABLE  NO 44   *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  2                                    N2=  4

MU1= 1.000                              MU2= 3.000

SIGMA1= 2.000                          SIGMA2= 4.000

BETA1=SIGMA1/MU1= 2.000          BETA2=SIGMA2/MU2= 1.333

THETA=MU1/MU2= 0.333          PSI=BETA1/BETA2= 1.500

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 3 | 6 | 17 |
| U | 2 | 10 | 16 |
| F | 0 | 2 | 7 |
| T | 3 | 8 | 13 |
| TPRIME | 3 | 5 | 9 |

```
*******************
*   TABLE   NO 45   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  2 | N2=  4 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 3.000 | SIGMA2= 6.000 |
| BETA1=SIGMA1/MU1= 3.000 | BETA2=SIGMA2/MU2= 3.000 |
| THETA=MU1/MU2= 2.000 | PSI=BETA1/BETA2= 1.000 |

```
****************************************************
*                    *          ALPHA-LEVEL             *
* TEST STATISTIC ***********************************
*                    *   0.01   *   0.05   *   0.10   *
****************************************************
*     LAMBDA     *     1    *     9    *    15    *
****************************************************
*       U        *     3    *     8    *    15    *
****************************************************
*       F        *     0    *     2    *     9    *
****************************************************
*       T        *     0    *     2    *     5    *
****************************************************
*     TPRIME     *     0    *     2    *     5    *
****************************************************
```

.67

```
*********************
*   TABLE   NO 46   *
*********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE


N1= 2                                    N2= 4

MU1= 0.800                               MU2= 0.600

SIGMA1= 4.000                            SIGMA2= 3.000

BETA1=SIGMA1/MU1= 5.000          BETA2=SIGMA2/MU2= 5.000

THETA=MU1/MU2= 1.333             PSI=BETA1/BETA2= 1.000


| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 0 | 6 | 11 |
| U | 1 | 9 | 13 |
| F | 1 | 8 | 9 |
| T | 3 | 9 | 16 |
| TPRIME | 1 | 4 | 8 |

```
******************
*  TABLE  NO 47  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1= 2 | N2= 4 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.100 | SIGMA2= 0.200 |

BETA1=SIGMA1/MU1= 0.100    BETA2=SIGMA2/MU2= 0.100

THETA=MU1/MU2= 0.500    PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
|  | 0.01 | 0.05 | 0.10 |
| LAMBDA | 100 | 100 | 100 |
| U | 0 | 0 | 0 |
| F | 0 | 7 | 12 |
| T | 98 | 100 | 100 |
| TPRIME | 31 | 82 | 99 |

```
****************
*  TABLE  NO 48  *
****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  2 | N2=  4 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.500 | SIGMA2= 1.200 |
| BETA1=SIGMA1/MU1= 0.500 | BETA2=SIGMA2/MU2= 0.600 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.833 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 9 | 32 | 52 |
| U | 0 | 1 | 6 |
| F | 0 | 5 | 14 |
| T | 2 | 21 | 34 |
| TPRIME | 1 | 5 | 21 |

```
******************
*  TABLE  NU 49  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  2 | N2=  4 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 1.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.500 |

| TEST STATISTIC | ALPHA-LEVEL 0.01 | 0.05 | 0.10 |
|---|---|---|---|
| LAMBDA | 5 | 22 | 44 |
| U | 5 | 14 | 34 |
| F | 1 | 11 | 17 |
| T | 0 | 5 | 8 |
| TPRIME | 0 | 3 | 8 |

```
*******************
*   TABLE  NO 50   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  2                          N2=  4

MU1= 1.000                      MU2= 2.000

SIGMA1= 1.500                   SIGMA2= 2.000

BETA1=SIGMA1/MU1= 1.500         BETA2=SIGMA2/MU2= 1.000

THETA=MU1/MU2= 0.500            PSI=BETA1/BETA2= 1.500

```
**************************************************************
*                    *        ALPHA-LEVEL                   *
* TEST STATISTIC     ***************************************
*                    *  0.01   *   0.05   *   0.10   *
**************************************************************
*    LAMBDA          *    0    *    7     *    13    *
**************************************************************
*      U             *    2    *    7     *    12    *
**************************************************************
*      F             *    0    *    2     *    5     *
**************************************************************
*      T             *    1    *    7     *    10    *
**************************************************************
*    TPRIME          *    0    *    4     *    5     *
**************************************************************
```

```
*******************
*   TABLE  NO 51  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 2 | N2= 4 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 1.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 2.000 |

```
**************************************************
*                  *         ALPHA-LEVEL         *
* TEST STATISTIC   ********************************
*                  *  0.01  *  0.05  *  0.10  *
**************************************************
*    LAMBDA        *    1   *    4   *    8   *
**************************************************
*    U             *    0   *    5   *   10   *
**************************************************
*    F             *    0   *    7   *   14   *
**************************************************
*    T             *    2   *   11   *   16   *
**************************************************
*    TPRIME        *    1   *    2   *    9   *
**************************************************
```

.73

```
*******************
*   TABLE  NO 52   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 6 | N2= 10 |
| MU1= 8.000 | MU2=10.000 |
| SIGMA1= 2.000 | SIGMA2= 2.500 |
| BETA1=SIGMA1/MU1= 0.250 | BETA2=SIGMA2/MU2= 0.250 |
| THETA=MU1/MU2= 0.800 | PSI=BETA1/BETA2= 1.000 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 13 | 35 | 55 |
| U | 0 | 0 | 0 |
| F | 0 | 9 | 14 |
| T | 13 | 27 | 46 |
| TPRIME | 7 | 23 | 42 |

```
******************
*  TABLE  NO 53  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 6 | N2= 10 |
| MU1= 2.000 | MU2= 4.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 1.000 | BETA2=SIGMA2/MU2= 1.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 1.000 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 26 | 53 | 72 |
| U | 15 | 35 | 53 |
| F | 6 | 24 | 45 |
| T | 0 | 15 | 37 |
| TPRIME | 1 | 21 | 38 |

```
*******************
*   TABLE   NO 54   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1=  6 | N2= 10 |
| MU1= 1.000 | MU2= 1.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |

BETA1=SIGMA1/MU1= 2.000     BETA2=SIGMA2/MU2= 4.000

THETA=MU1/MU2= 1.000     PSI=BETA1/BETA2= 0.500

```
*****************************************************
*                    *         ALPHA-LEVEL          *
* TEST STATISTIC *************************************
*                    *  0.01  *   0.05   *   0.10   *
*****************************************************
*    LAMBDA     *    9    *    34    *    47    *
*****************************************************
*      U        *   11    *    31    *    45    *
*****************************************************
*      F        *    7    *    31    *    45    *
*****************************************************
*      T        *    0    *     3    *     5    *
*****************************************************
*    TPRIME     *    0    *     2    *     5    *
*****************************************************
```

```
********************
*  TABLE  NO 55  *
********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 6 | N2= 10 |
|---|---|
| MU1= 8.000 | MU2=10.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 0.250 | BETA2=SIGMA2/MU2= 0.200 |
| THETA=MU1/MU2= 0.800 | PSI=BETA1/BETA2= 1.250 |

```
*********************************************************
*                    *          ALPHA-LEVEL            *
* TEST STATISTIC *****************************************
*                    *  0.01   *   0.05   *   0.10   *
*********************************************************
*     LAMBDA      *    14    *    43    *    56    *
*********************************************************
*       U         *     0    *     0    *     0    *
*********************************************************
*       F         *     1    *     6    *     9    *
*********************************************************
*       T         *    19    *    +4    *    56    *
*********************************************************
*     TPRIME      *     3    *    35    *    52    *
*********************************************************
```

```
*******************
*  TABLE  NO 56  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  6                            N2= 10

MU1= 4.000                        MU2= 6.000

SIGMA1= 2.000                     SIGMA2= 2.500

BETA1=SIGMA1/MU1= 0.500        BETA2=SIGMA2/MU2= 0.416

THETA=MU1/MU2= 0.670           PSI=BETA1/BETA2= 1.200

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 14 | 32 | 47 |
| U | 0 | 2 | 8 |
| F | 1 | 5 | 8 |
| T | 10 | 32 | 45 |
| TPRIME | 4 | 27 | 41 |

```
*******************
*   TABLE   NO 57   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 6 | N2= 10 |
| MU1= 1.000 | MU2= 3.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 1.333 |
| THETA=MU1/MU2= 0.333 | PSI=BETA1/BETA2= 1.500 |

```
**********************************************************
*                    *           ALPHA-LEVEL              *
* TEST STATISTIC  ****************************************
*                    *   0.01   *   0.05   *   0.10   *
**********************************************************
*     LAMBDA        *    20    *    52    *    68    *
**********************************************************
*       U           *    15    *    44    *    64    *
**********************************************************
*       F           *     7    *    30    *    50    *
**********************************************************
*       T           *     5    *    16    *    24    *
**********************************************************
*     TPRIME        *     2    *    15    *    22    *
**********************************************************
```

```
*******************
*   TABLE  NO 58   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 6 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 3.000 | SIGMA2= 6.000 |
| BETA1=SIGMA1/MU1= 3.000 | BETA2=SIGMA2/MU2= 3.000 |
| THETA=MU1/MU2= 2.000 | PSI=BETA1/BETA2= 1.000 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 7 | 31 | 55 |
| U | 8 | 30 | 53 |
| F | 7 | 22 | 39 |
| T | 0 | 1 | 3 |
| TPRIME | 0 | 1 | 6 |

```
*******************
*   TABLE   NO 59   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  6                              N2= 10

MU1= 0.800                          MU2= 0.600

SIGMA1= 4.000                       SIGMA2= 3.000

BETA1=SIGMA1/MU1= 5.000        BETA2=SIGMA2/MU2= 5.000

THETA=MU1/MU2= 1.333           PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
| --- | --- | --- | --- |
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 5 | 10 | 17 |
| U | 7 | 13 | 20 |
| F | 5 | 12 | 19 |
| T | 0 | 6 | 12 |
| TPRIME | 0 | 1 | 4 |

```
*******************
*   TABLE   NO 60   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  6 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.100 | SIGMA2= 0.200 |
| BETA1=SIGMA1/MU1= 0.100 | BETA2=SIGMA2/MU2= 0.100 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 1.000 |

```
*****************************************************
*                 *           ALPHA-LEVEL           *
* TEST STATISTIC  *********************************
*                 *   0.01  *   0.05  *   0.10  *
*****************************************************
*    LAMBDA       *   100   *   100   *   100   *
*****************************************************
*      U          *    0    *    0    *    53   *
*****************************************************
*      F          *    18   *    35   *    54   *
*****************************************************
*      T          *   100   *   100   *   100   *
*****************************************************
*    TPRIME       *   100   *   100   *   100   *
*****************************************************
```

```
*******************
*   TABLE   NO 61   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1=  6 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.500 | SIGMA2= 1.200 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 0.500 | BETA2=SIGMA2/MU2= 0.600 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.833 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 57 | 88 | 97 |
| U | 4 | 24 | 52 |
| F | 12 | 43 | 61 |
| T | 18 | 43 | 61 |
| TPRIME | 17 | 47 | 67 |

```
******************
*   TABLE  NO 62  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  6 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.000 | SIGMA2= 4.000 |
| BETA1=SIGMA1/MU1= 1.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.500 |

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 67 | 90 | 97 |
| U | 44 | 80 | 90 |
| F | 60 | 89 | 94 |
| T | 1 | 4 | 11 |
| TPRIME | 2 | 7 | 18 |

```
*******************
*   TABLE  NO 63   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  6 | N2= 10 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.500 | SIGMA2= 2.000 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 1.500 | BETA2=SIGMA2/MU2= 1.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 1.500 |

```
*************************************************
*                   *        ALPHA-LEVEL        *
* TEST STATISTIC    ***************************
*                   *  0.01  *  0.05  *  0.10   *
*************************************************
*     LAMBDA        *   8    *   17   *   26    *
*************************************************
*       U           *   3    *   11   *   25    *
*************************************************
*       F           *   2    *    9   *   20    *
*************************************************
*       T           *   4    *   21   *   29    *
*************************************************
*     TPRIME        *   1    *   16   *   23    *
*************************************************
```

```
******************
*  TABLE  NO 65  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  6                           N2= 20

MU1= 8.000                       MU2=10.000

SIGMA1= 2.000                    SIGMA2= 2.500

BETA1=SIGMA1/MU1= 0.250          BETA2=SIGMA2/MU2= 0.250

THETA=MU1/MU2= 0.800             PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 25 | 44 | 59 |
| U | 0 | 0 | 0 |
| F | 1 | 8 | 12 |
| T | 16 | 35 | 54 |
| TPRIME | 11 | 36 | 56 |

```
******************
*   TABLE  NO 66  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1=  6 | N2= 20 |
| MU1= 2.000 | MU2= 4.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |

BETA1=SIGMA1/MU1= 1.000      BETA2=SIGMA2/MU2= 1.000

THETA=MU1/MU2= 0.500      PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 35 | 65 | 80 |
| U | 12 | 43 | 65 |
| F | 8 | 31 | 46 |
| T | 6 | 17 | 27 |
| TPRIME | 8 | 33 | 49 |

```
******************
*   TABLE  NO 67   *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 6 | N2= 20 |
| MU1= 1.000 | MU2= 1.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 2.000 | BETA2=SIGMA2/MU2= 4.000 |
| THETA=MU1/MU2= 1.000 | PSI=BETA1/BETA2= 0.500 |

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 14 | 42 | 60 |
| U | 9 | 32 | 49 |
| F | 9 | 31 | 49 |
| T | 0 | 0 | 0 |
| TPRIME | 0 | 3 | 8 |

```
****************
*  TABLE  NO 68  *
****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=  6 | N2= 20 |
| MU1= 8.000 | MU2=10.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |

BETA1=SIGMA1/MU1= 0.250     BETA2=SIGMA2/MU2= 0.200

THETA=MU1/MU2= 0.800     PSI=BETA1/BETA2= 1.250

| | ALPHA-LEVEL | | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 29 | 57 | 69 |
| U | 0 | 0 | 0 |
| F | 0 | 7 | 13 |
| T | 34 | 58 | 71 |
| TPRIME | 20 | 46 | 62 |

```
******************
*  TABLE  NO 69  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1=  6 | N2= 20 |
| MU1= 4.000 | MU2= 6.000 |
| SIGMA1= 2.000 | SIGMA2= 2.500 |

BETA1=SIGMA1/MU1= 0.500      BETA2=SIGMA2/MU2= 0.416

THETA=MU1/MU2= 0.670      PSI=BETA1/BETA2= 1.200

```
*********************************************************
*                    *          ALPHA-LEVEL            *
* TEST STATISTIC  ***************************************
*                    *  0.01  *  0.05  *  0.10  *
*********************************************************
*    LAMBDA          *   23   *   49   *   61   *
*********************************************************
*      U             *    0   *    4   *    9   *
*********************************************************
*      F             *    0   *    5   *    8   *
*********************************************************
*      T             *   18   *   44   *   56   *
*********************************************************
*    TPRIME          *   11   *   43   *   56   *
*********************************************************
```

```
*******************
*   TABLE  NO 70   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  6                              N2= 20

MU1= 1.000                          MU2= 3.000

SIGMA1= 2.000                       SIGMA2= 4.000

BETA1=SIGMA1/MU1= 2.000        BETA2=SIGMA2/MU2= 1.333

THETA=MU1/MU2= 0.333           PSI=BETA1/BETA2= 1.500

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 40 | 65 | 76 |
| U | 31 | 62 | 76 |
| F | 16 | 42 | 53 |
| T | 1 | 11 | 27 |
| TPRIME | 7 | 33 | 48 |

```
*******************
*  TABLE  NO 71  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  6                              N2= 20

MU1= 1.000                          MU2= 2.000

SIGMA1= 3.000                       SIGMA2= 6.000

BETA1=SIGMA1/MU1= 3.000        BETA2=SIGMA2/MU2= 3.000

THETA=MU1/MU2= 2.000          PSI=BETA1/BETA2= 1.000

```
*************************************************************
*                 *            ALPHA-LEVEL            *
* TEST STATISTIC  ******************************************
*                 *  0.01   *   0.05   *   0.10   *
*************************************************************
*    LAMBDA       *   22    *    47    *    65    *
*************************************************************
*      U          *   13    *    36    *    50    *
*************************************************************
*      F          *    8    *    33    *    53    *
*************************************************************
*      T          *    0    *     0    *     3    *
*************************************************************
*    TPRIME       *    0    *     2    *     9    *
*************************************************************
```

```
*****************
*  TABLE  NO 72  *
*****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=  6                          N2= 20

MU1= 0.800                      MU2= 0.600

SIGMA1= 4.000                   SIGMA2= 3.000

BETA1=SIGMA1/MU1= 5.000         BETA2=SIGMA2/MU2= 5.000

THETA=MU1/MU2= 1.333            PSI=BETA1/BETA2= 1.000

```
***********************************************************
*               *          ALPHA-LEVEL                   *
* TEST STATISTIC ****************************************** 
*               *   0.01  *   0.05  *   0.10  *
***********************************************************
*    LAMBDA     *    1    *   11    *   16    *
***********************************************************
*      U        *    4    *   14    *   21    *
***********************************************************
*      F        *    1    *    9    *   20    *
***********************************************************
*      T        *    1    *    4    *   13    *
***********************************************************
*    TPRIME     *    1    *    3    *    5    *
***********************************************************
```

```
******************
*   TABLE   NO 73   *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1=   6 | N2= 20 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.100 | SIGMA2= 0.200 |

BETA1=SIGMA1/MU1= 0.100          BETA2=SIGMA2/MU2= 0.100

THETA=MU1/MU2= 0.500          PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL 0.01 | 0.05 | 0.10 |
|---|---|---|---|
| LAMBDA | 100 | 100 | 100 |
| U | 0 | 0 | 68 |
| F | 11 | 30 | 49 |
| T | 100 | 100 | 100 |
| TPRIME | 100 | 100 | 100 |

```
*******************
*   TABLE   NO 74   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 6 | N2= 20 |
|---|---|
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.500 | SIGMA2= 1.200 |

| BETA1=SIGMA1/MU1= 0.500 | BETA2=SIGMA2/MU2= 0.600 |
|---|---|
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.833 |

```
***************************************************
*                  *           ALPHA-LEVEL            *
* TEST STATISTIC   ********************************
*                  *   0.01   *   0.05   *   0.10   *
***************************************************
*    LAMBDA        *    74    *    89    *    96    *
***************************************************
*      U           *     3    *    31    *    60    *
***************************************************
*      F           *    18    *    50    *    69    *
***************************************************
*      T           *    16    *    41    *    61    *
***************************************************
*    TPRIME        *    36    *    72    *    84    *
***************************************************
```

```
*******************
*   TABLE  NO 75  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1=   6                        N2= 20

MU1= 1.000                     MU2= 2.000

SIGMA1= 1.000                  SIGMA2= 4.000

BETA1=SIGMA1/MU1= 1.000        BETA2=SIGMA2/MU2= 2.000

THETA=MU1/MU2= 0.500           PSI=BETA1/BETA2= 0.500

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 84 | 98 | 99 |
| U | 59 | 89 | 95 |
| F | 62 | 94 | 99 |
| T | 0 | 0 | 4 |
| TPRIME | 3 | 14 | 28 |

```
*********************
*   TABLE  NC 76   *
*********************
```

.97

TOTAL NUMBER CF REJECTICN CUT CF 1CO SAMPLES
SIMULATED WITH THE GIVEN POPULATICN PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 6                                    N2= 20

MU1= 1.CCC                               MU2= 2.C00

SIGMA1= 1.50C                            SIGMA2= 2.0C0

BETA1=SIGMA1/MU1= 1.500        BETA2=SIGMA2/MU2= 1.0C0

THETA=MU1/MU2= 0.50C           PSI=BETA1/BETA2= 1.5CC

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | C.10 |
| LAMBDA | 8 | 23 | 36 |
| L | 6 | 14 | 34 |
| F | 3 | 10 | 12 |
| T | 4 | 17 | 30 |
| TPRIME | 6 | 24 | 34 |

```
*******************
*   TABLE  NC 77  *
*******************
```

TOTAL NUMBER CF REJECTICN CUT CF 1CO SAMPLES
SIMULATED WITH THE GIVEN PCPULATICN PARAMETERS
FOR 2 SAMPLES CF SIZE


N1=  6                              N2= 20

MU1= 1.CCC                          MU2= 2.0CO

SIGMA1= 2.CCC                       SIGMA2= 2.CCC

BETA1=SIGMA1/MU1= 2.C0O        BETA2=SIGMA2/MU2= 1.C0O

THETA=MU1/MU2= C.5CO           PSI=BETA1/BETA2= 2.0CC


```
***************************************************
*                  *       ALPHA-LEVEL           *
* TEST STATISTIC ***********************************
*                  *  0.01  *  0.05  *  0.10  *
***************************************************
*    LAMBDA        *    3   *   11   *   16   *
***************************************************
*      U           *    5   *    9   *   16   *
***************************************************
*      F           *    1   *    5   *    8   *
***************************************************
*      T           *    4   *   15   *   27   *
***************************************************
*    TPRIME        *    5   *   15   *   25   *
***************************************************
```

```
****************
*  TABLE  NO 78  *
****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                          N2= 20

MU1= 8.000                      MU2=10.000

SIGMA1= 2.000                   SIGMA2= 2.500

BETA1=SIGMA1/MU1= 0.250         BETA2=SIGMA2/MU2= 0.250

THETA=MU1/MU2= 0.800            PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 46 | 72 | 84 |
| U | 0 | 0 | 0 |
| F | 2 | 7 | 20 |
| T | 34 | 65 | 76 |
| TPRIME | 36 | 63 | 78 |

```
********************
*  TABLE  NO 79  *
********************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

|  |  |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 2.000 | MU2= 4.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |

BETA1=SIGMA1/MU1= 1.000        BETA2=SIGMA2/MU2= 1.000

THETA=MU1/MU2= 0.500        PSI=BETA1/BETA2= 1.000

```
***********************************************************
*                 *           ALPHA-LEVEL            *
* TEST STATISTIC  *****************************************
*                 *  0.01   *   0.05   *   0.10   *
***********************************************************
*    LAMBDA       *   63    *   84     *   95     *
***********************************************************
*      U          *   29    *   68     *   80     *
***********************************************************
*      F          *   28    *   61     *   75     *
***********************************************************
*      T          *   10    *   32     *   50     *
***********************************************************
*    TPRIME       *   17    *   43     *   57     *
***********************************************************
```

```
*****************
*  TABLE  NO 80  *
*****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 1.000 | MU2= 1.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |

BETA1=SIGMA1/MU1= 2.000        BETA2=SIGMA2/MU2= 4.000

THETA=MU1/MU2= 1.000        PSI=BETA1/BETA2= 0.500

| | | ALPHA-LEVEL | |
|---|---|---|---|
| TEST STATISTIC | 0.01 | 0.05 | 0.10 |
| LAMBDA | 33 | 62 | 76 |
| U | 21 | 53 | 66 |
| F | 28 | 57 | 76 |
| T | 0 | 1 | 6 |
| TPRIME | 0 | 4 | 11 |

```
*****************
*  TABLE  NO 81  *
*****************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 8.000 | MU2=10.000 |
| SIGMA1= 2.000 | SIGMA2= 2.000 |
| BETA1=SIGMA1/MU1= 0.250 | BETA2=SIGMA2/MU2= 0.200 |
| THETA=MU1/MU2= 0.800 | PSI=BETA1/BETA2= 1.250 |

```
*****************************************************
*                *            ALPHA-LEVEL          *
* TEST STATISTIC *************************************
*                *  0.01  *  0.05  *  0.10  *
*****************************************************
*    LAMBDA      *   36   *   69   *   82   *
*****************************************************
*      U         *    0   *    0   *    0   *
*****************************************************
*      F         *    3   *    8   *    9   *
*****************************************************
*      T         *   41   *   72   *   81   *
*****************************************************
*    TPRIME      *   28   *   66   *   81   *
*****************************************************
```

```
*******************
*   TABLE  NO 82   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                               N2= 20

MU1= 4.000                           MU2= 6.000

SIGMA1= 2.000                        SIGMA2= 2.500

BETA1=SIGMA1/MU1= 0.500        BETA2=SIGMA2/MU2= 0.416

THETA=MU1/MU2= 0.670           PSI=BETA1/BETA2= 1.200

| TEST STATISTIC | ALPHA-LEVEL | | |
| --- | --- | --- | --- |
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 43 | 67 | 80 |
| U | 0 | 12 | 24 |
| F | 4 | 14 | 20 |
| T | 27 | 63 | 74 |
| TPRIME | 27 | 64 | 74 |

```
*******************
*   TABLE  NO 83   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 1.000 | MU2= 3.000 |
| SIGMA1= 2.000 | SIGMA2= 4.000 |

BETA1=SIGMA1/MU1= 2.000          BETA2=SIGMA2/MU2= 1.333

THETA=MU1/MU2= 0.333          PSI=BETA1/BETA2= 1.500

```
*****************************************************
*                 *          ALPHA-LEVEL            *
* TEST STATISTIC  ***********************************
*                 *  0.01  *  0.05  *  0.10  *
*****************************************************
*    LAMBDA       *   47   *   77   *   89   *
*****************************************************
*      U          *   44   *   73   *   89   *
*****************************************************
*      F          *   24   *   48   *   66   *
*****************************************************
*      T          *    6   *   31   *   51   *
*****************************************************
*    TPRIME       *   11   *   44   *   61   *
*****************************************************
```

```
*******************
*   TABLE   NO 84   *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 3.000 | SIGMA2= 6.000 |
| BETA1=SIGMA1/MU1= 3.000 | BETA2=SIGMA2/MU2= 3.000 |
| THETA=MU1/MU2= 2.000 | PSI=BETA1/BETA2= 1.000 |

```
**********************************************************
*                    *         ALPHA-LEVEL             *
* TEST STATISTIC  ****************************************
*                    *  0.01   *  0.05   *   0.10   *
**********************************************************
*     LAMBDA      *   40    *   63    *    82    *
**********************************************************
*       U         *   34    *   63    *    76    *
**********************************************************
*       F         *   29    *   56    *    75    *
**********************************************************
*       T         *    2    *    8    *    10    *
**********************************************************
*     TPRIME      *    5    *    9    *    10    *
**********************************************************
```

```
******************
*   TABLE  NO 85   *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| N1= 10 | N2= 20 |
|--------|--------|
| MU1= 0.800 | MU2= 0.600 |
| SIGMA1= 4.000 | SIGMA2= 3.000 |

| BETA1=SIGMA1/MU1= 5.000 | BETA2=SIGMA2/MU2= 5.000 |
|-------------------------|-------------------------|
| THETA=MU1/MU2= 1.333 | PSI=BETA1/BETA2= 1.000 |

```
**********************************************************
*                    *           ALPHA-LEVEL            *
* TEST STATISTIC   ***************************************
*                    *   0.01   *   0.05   *   0.10   *
**********************************************************
*      LAMBDA        *     7    *    20    *    35    *
**********************************************************
*        U           *     6    *    20    *    34    *
**********************************************************
*        F           *     3    *    20    *    34    *
**********************************************************
*        T           *     2    *     4    *    12    *
**********************************************************
*      TPRIME        *     0    *     2    *     4    *
**********************************************************
```

```
******************
*   TABLE   NO 86   *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.100 | SIGMA2= 0.200 |

BETA1=SIGMA1/MU1= 0.100          BETA2=SIGMA2/MU2= 0.100

THETA=MU1/MU2= 0.500          PSI=BETA1/BETA2= 1.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 100 | 100 | 100 |
| U | 0 | 98 | 100 |
| F | 25 | 67 | 76 |
| T | 100 | 100 | 100 |
| TPRIME | 100 | 100 | 100 |

```
******************
*   TABLE  NO 87  *
******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 0.500 | SIGMA2= 1.200 |
| BETA1=SIGMA1/MU1= 0.500 | BETA2=SIGMA2/MU2= 0.600 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.833 |

```
*********************************************************
*                    *          ALPHA-LEVEL            *
*  TEST STATISTIC  *************************************
*                    *   0.01  *   0.05  *   0.10  *
*********************************************************
*     LAMBDA       *    94   *   100   *   100   *
*********************************************************
*       U          *    30   *    76   *    92   *
*********************************************************
*       F          *    48   *    76   *    86   *
*********************************************************
*       T          *    41   *    77   *    89   *
*********************************************************
*     TPRIME       *    63   *    91   *    93   *
*********************************************************
```

```
*******************
*  TABLE  NO 88  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.000 | SIGMA2= 4.000 |

| | |
|---|---|
| BETA1=SIGMA1/MU1= 1.000 | BETA2=SIGMA2/MU2= 2.000 |
| THETA=MU1/MU2= 0.500 | PSI=BETA1/BETA2= 0.500 |

```
*************************************************
*               *        ALPHA-LEVEL         *
* TEST STATISTIC ********************************
*               *   0.01  *  0.05   *  0.10   *
*************************************************
*     LAMBDA    *   99    *  100    *  100    *
*************************************************
*       U       *   92    *   97    *   99    *
*************************************************
*       F       *   99    *  100    *  100    *
*************************************************
*       T       *    1    *    7    *    8    *
*************************************************
*     TPRIME    *    5    *   13    *   24    *
*************************************************
```

```
*******************
*  TABLE  NO 89  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

| | |
|---|---|
| N1= 10 | N2= 20 |
| MU1= 1.000 | MU2= 2.000 |
| SIGMA1= 1.500 | SIGMA2= 2.000 |

BETA1=SIGMA1/MU1= 1.500      BETA2=SIGMA2/MU2= 1.000

THETA=MU1/MU2= 0.500      PSI=BETA1/BETA2= 1.500

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 6 | 34 | 50 |
| U | 7 | 20 | 34 |
| F | 3 | 10 | 22 |
| T | 7 | 20 | 29 |
| TPRIME | 8 | 21 | 29 |

```
*******************
*  TABLE  NO 90  *
*******************
```

TOTAL NUMBER OF REJECTION OUT OF 100 SAMPLES
SIMULATED WITH THE GIVEN POPULATION PARAMETERS
FOR 2 SAMPLES OF SIZE

N1= 10                          N2= 20

MU1= 1.000                      MU2= 2.000

SIGMA1= 2.000                   SIGMA2= 2.000

BETA1=SIGMA1/MU1= 2.000         BETA2=SIGMA2/MU2= 1.000

THETA=MU1/MU2= 0.500            PSI=BETA1/BETA2= 2.000

| TEST STATISTIC | ALPHA-LEVEL | | |
|---|---|---|---|
| | 0.01 | 0.05 | 0.10 |
| LAMBDA | 1 | 7 | 16 |
| U | 1 | 12 | 17 |
| F | 1 | 5 | 7 |
| T | 7 | 20 | 26 |
| TPRIME | 7 | 14 | 22 |