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Chapter 2.1

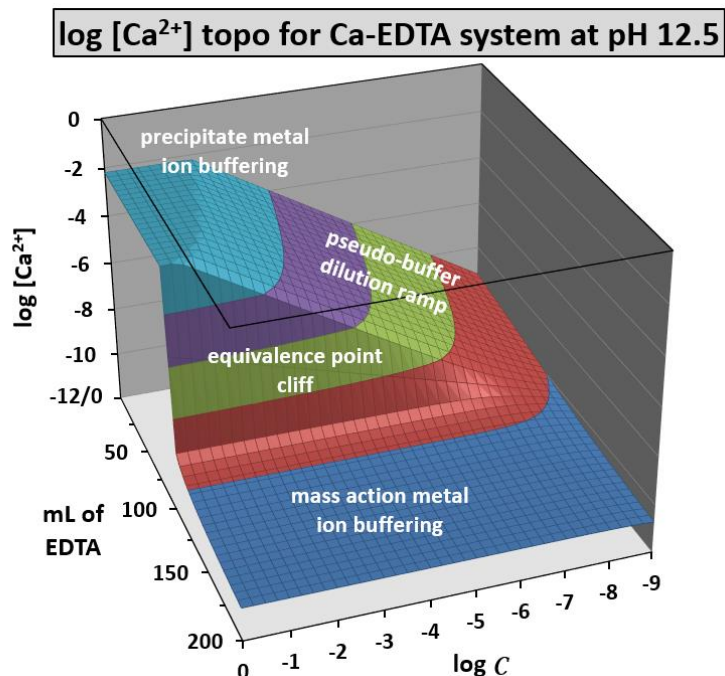
Visualization of Metal Ion Buffering Via 3-D Topo Surfaces of Complexometric Titrations

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Abstract

This chapter examines 1:1 metal-ligand complexometric titrations in aqueous media. It presents surfaces that plot computed equilibrium parameters above a composition grid with titration progress (mL of ligand) as the x -axis and overall system dilution ($\log C$) as the y -axis. The sample systems in this chapter are restricted to EDTA as a ligand. Other chelating ligands that form exclusively 1:1 complexes could also be modeled with this software. The surfaces show the quality of the equivalence point break under various conditions. More importantly, they develop the phenomenon of metal ion buffering. They clearly distinguish the difference between “pseudo-buffering” and “true buffering”. They introduce terminology for two different forms of metal ion buffering: 1) mass action metal ion buffering under excess ligand conditions; and 2) precipitate metal ion buffering when hydroxide precipitates are present under excess metal ion conditions. Systems modeled are EDTA titrations of Cu^{2+} , Ca^{2+} and Mg^{2+} . A final section demonstrates a second type of topo that helps evaluate the optimal pH for an EDTA titration. Supplemental files include the Complexation TOPOS software, an Excel workbook that generates topo surfaces in under 20 seconds, and teaching suggestions. Required inputs are: 1) stability constants for the metal-ligand complex; 2) acid dissociation constants for the ligand, 3) stability constants for hydroxy complexes from of the metal cation; and 4) a K_{sp} value and stoichiometry for hydroxide precipitates. Many of these constants are contained in a workbook tab. Also included are a PowerPoint lecture and teaching materials (for lecture, homework, and pre-laboratory activities) that are suitable in general chemistry courses or third-year and graduate courses in analytical chemistry, biochemistry and geochemistry.



2.1.1 Introduction

Chapters 1.1 – 1.3 dealt with topos for acid-base titrations. This chapter is the first that focuses instead on metal-ligand complexation. It simply moves from Brønsted-Lowry acid-base reactions (exchange of protons in water) to Lewis acid-base reactions (exchange of electron pairs in water, e^- pair donor-acceptor reactions). The phenomenon of metal ion buffering figures prominently in the discussions. We clearly distinguish the difference between “pseudo-buffering” and “true buffering” as well as introduce terminology for two different forms of metal ion buffering: 1) mass action metal ion buffering under excess ligand conditions; and 2) precipitate metal ion buffering when hydroxide precipitates are present under excess metal ion conditions.

Why is it important to understand Lewis acid-base reactions? For chemistry students, metal complexation reactions comprise a large arena of research for catalysts¹, ion-exchange resins², pharmaceuticals³ and analytical methods.⁴ For example, the determination of water hardness with ethylenediaminetetraacetic acid (EDTA) is a standard water quality test.⁵ In biochemistry, these metal-ligand reactions help explain how essential metal ions bind to proteins.⁶ With geochemistry, metal complexation is central to describing the fate and transport of toxic heavy metals and radionuclides in the environment.⁷

Complexation TOPOS, a new computer program available as a supplemental file in this chapter, examines metal-ligand systems where only 1:1 complexes form. The most familiar systems of this type are metals interacting with hexadentate EDTA. The program creates 3-D trend surfaces above a composition grid that encompasses a wide range of solution conditions. The primary composition grid used has a titration curve x -axis (mL of EDTA) and a dilution y -axis ($\log C$). Other composition grids are possible, for example, mL of EDTA vs. pH which appear later in this chapter. Variables that can be plotted as z -coordinates to form trend surfaces include free metal ($[M^{n+}]$), free ligand ($[L]$), metal-ligand complex ($[ML]$), protonated ligand forms ($[H_xL]$) and hydroxy-metal complexes ($[M(OH)_x]$). By including dilution as a composition grid dimension, the concept of metal ion buffering can be nicely visualized.

This chapter focuses on EDTA titrations. Treatment of simple EDTA complexometric titrations is appropriate for inclusion in introductory chemistry courses. Complexation TOPOS includes competing side-reactions from protons and hydroxide ions. Discussions of these complications and metal ion buffering are more appropriate topics for upper division and graduate level chemistry courses.

2.1.2 The Chemical Model for 1:1 Complexation Systems

The aqueous equilibrium chemistry that occurs in a metal-ligand complexation titration is more complicated than that for a simple Brønsted-Lowry acid-base system. As these procedures are being conducted in aqueous solution, there are competing reactions for both the metal ion and ligand components. Competition for the metal ion occurs between the ligand of interest and the ever-present OH^- of the water itself. In a similar fashion, there is competition for the ligand's binding sites between metal ions and the ever-present H_3O^+ of the water. Finally, if the concentration of metal and hydroxide ions gets sufficiently high, there is also the possibility of metal hydroxide precipitation. Because of these competing processes, metal complexation titrations are often done at constant pH to reduce the variables in the system. That practice is employed here.

A sample metal-ligand system will be useful for describing the competitive reactions as well as introducing the symbol conventions adopted for the

equilibrium constants of each reaction. A computer simulation is only as good as the completeness of the chemical model from which it has been constructed. Thus, it pays to describe as much of the chemistry as is possible.

The initial system explored here consists of copper(II), Cu^{2+} , as the metal ion and ethylenediaminetetraacetic acid, EDTA, a classic hexadentate ligand. EDTA forms a very stable 1:1 complex with cupric ion. The complex formed between Cu^{2+} and EDTA really represents a displacement of the six H_2O molecules that are in the coordination sphere of the aqueous Cu^{2+} ion. For simplicity we will ignore the water molecules in most of our formulas. Copper(II) can react in water to form $\text{Cu}(\text{OH})^+$, $\text{Cu}(\text{OH})_2^0$, $\text{Cu}(\text{OH})_3^-$ and $\text{Cu}(\text{OH})_4^{2-}$. If the pH is above 4.3 and there is little or no EDTA present, Cu^{2+} can precipitate as $\text{Cu}(\text{OH})_2(\text{s})$. Below are the reactions and constants used in generating the accompanying figures for the Cu-EDTA system. All constants used in this paper are from Martel et al.'s *NIST Critical Stability Constants of Metal Complexes Database 46*.⁸

Complexation reactions: These are written as overall reactions as opposed to step-wise reactions. Since there is just one stoichiometry here, only a β_1 is required.



As we discuss the shifts from one copper species to another, we will use γ coefficients to quantify how much is present in each form. These are analogous to the α coefficients used in acid-base species distribution diagrams.

γ_0 represents the fraction present as free copper ion, *i.e.*, Cu^{2+}

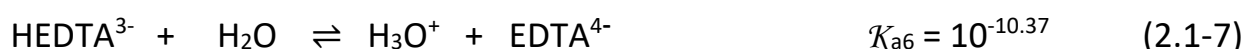
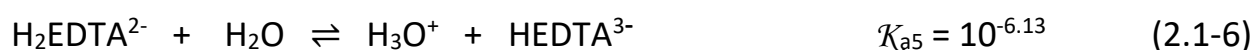
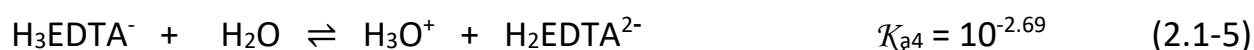
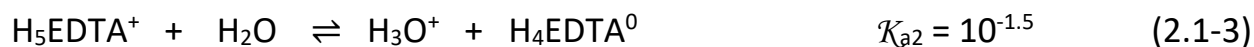
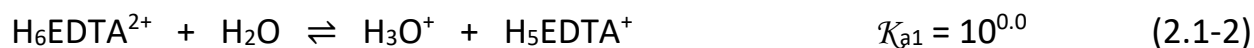
γ_1 represents the fraction present as CuEDTA^{2-}

For simplicity, we are ignoring the hydroxide species in our γ values.

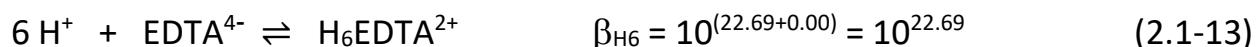
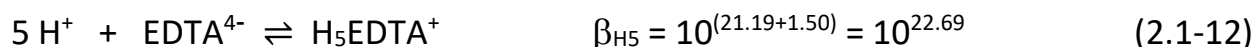
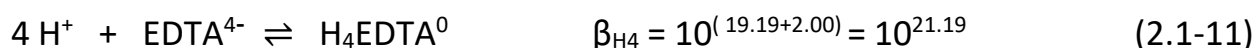
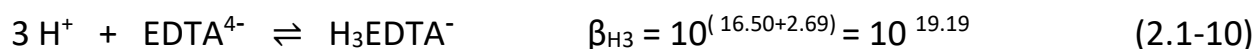
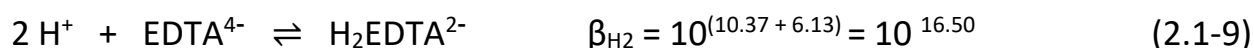
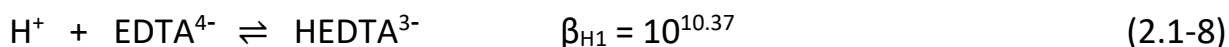
Protonation of ligand reactions: Acid-base chemistry is traditionally treated as loss of protons. Given the structure of our computer program, it is more convenient here to write these in the reverse direction. This is equivalent to forming “hydrogen complexes” of the ligands. All that needs to be done is switch the order of constants and change the sign on their $\text{p}K_a$ values. The last proton lost is the same as the first proton “complexed”. These, too, are done as overall,

not step-wise, constants. Below is a comparison of the standard K_a notation and the β_H notation used in our model equations. The Complexation TOPOS model asks the user to list pK_a values and then automatically converts them into the log β_H values that it employs.

Step-wise dissociation of EDTA:



Overall constants for protonation of EDTA:



Metal Hydrolysis Reactions: Whenever metal ions are dissolved in water, there is a possible interaction with OH^- as a ligand. We will ignore writing formulas with coordinated H_2O because it is easier to follow the complexation chemistry. Stability constants for four hydroxy complexes of copper are included.

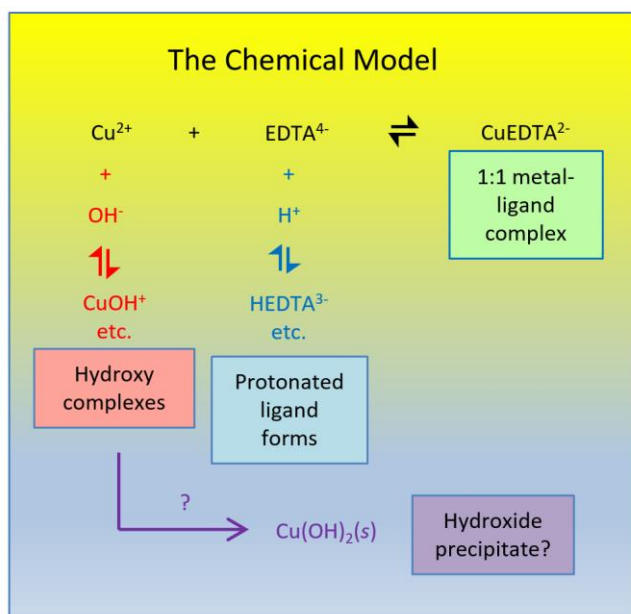


Hydroxide Precipitation: For the Cu^{2+} system, we also need to be alert for the possibility of a 1:2 cupric hydroxide precipitate, $\text{Cu(OH)}_2(\text{s})$. Thus, it is also necessary to have any pertinent K_{sp} s available to check for precipitation conditions.



All aspects of the chemical model are summarized as Figure 2.1-1.

Figure 2.1-1. A simplified diagram for the Cu^{2+} -EDTA sample system.



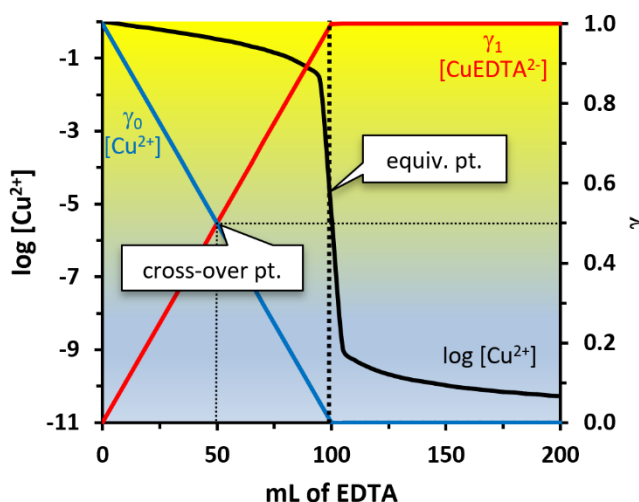
It should be noted that, as presented here, several factors are intentionally omitted for the sake of pedagogic clarity in the chemical model. We are ignoring activity effects which can make a substantial difference in the experimental values observed. Most equilibrium constants are reported for a specific ionic strength.

We have chosen the reported values from the NIST⁸ tables which often were measured at an ionic strength of 0.10 M. In practice, when we have conducted experimental verifications, we have employed a total ionic strength adjustor (ISA) to eliminate variations caused by activity changes. This has necessitated confining our experimental solutions to less than 0.100 M ionic strength. We are also ignoring ion pair formation which brings together oppositely charged species as outer sphere complexes or fully solvated ions.

2.1-3 Traditional 2-D Ligand into Metal Titrations

Before presenting a full 3-D topo surface for a metal-ligand complexation system, it is beneficial to look at one of the 2-D slices from which it is assembled. Figure 2.1-2 shows a simulation for 100 mL of 1.0 M Cu^{2+} being titrated with 1.0 M EDTA at pH 4.0. Both the complexometric titration curve ($\log [\text{Cu}^{2+}]$) and the metal speciation traces (γ_x) have been plotted against the mL of EDTA. While most treatments of complexometric titrations use pCu^{2+} as the y-axis, we prefer $\log [\text{Cu}^{2+}]$. With this choice, movement on the y-axis relates directly to what is happening with concentration. A rise on the y-axis corresponds to an increase in concentration; a decrease in y is a drop in concentration.

Figure 2.1-2. Titration curve and metal speciation (γ_x) when 100 mL of 1.0 M Cu^{2+} is titrated with 1.0 M EDTA at pH 4.0.



The $\log [\text{Cu}^{2+}]$ trace shows a typical EDTA complexometric titration curve with a sharp equivalence point break from an upper slope to a lower slope. The

titration curve shows a fairly shallow slope both before and after the equivalence point is reached.

Species distribution diagrams for the fraction of free metal ion (γ_0) and the fraction of CuEDTA^{2-} complex (γ_1) also appear. These traces reveal the chemical situation during the titration. As EDTA is added linearly, the two γ -curves track the steady conversion of Cu^{2+} to CuEDTA^{2-} . Half way to the equivalence point, the speciation curves reach a cross-over; both γ_0 and γ_1 are 0.50. At 100 mL the conversion is essentially complete with γ_1 near 1 and γ_0 close to 0.

The complexometric titration curve illustrates that the value of $\log [\text{Cu}^{2+}]$ is somewhat stable before and after the equivalence point break. This is a situation akin to pH buffering in acid-base systems. Metal ion buffering occurs when changing solution composition does not cause large shifts in the $\log [\text{Cu}^{2+}]$ value. Some authors⁹⁻¹¹ have labeled both the before and after sections of the complexometric curve in Figure 2.1-2 as “buffer zones”. Creation of a $\log [\text{Cu}^{2+}]$ topo surface over a titration-dilution composition grid, however, will demonstrate that the pre-equivalence point section is a “pseudo-buffer” region while the post-equivalence point section is a “true metal ion buffering” situation. Similar pseudo-buffering behavior for acid-base systems is discussed in Chapter 1.1.4.

2.1.4 The $\log [\text{Cu}^{2+}]$ 3-D Topo Surface: Buffering vs. Pseudo-Buffering

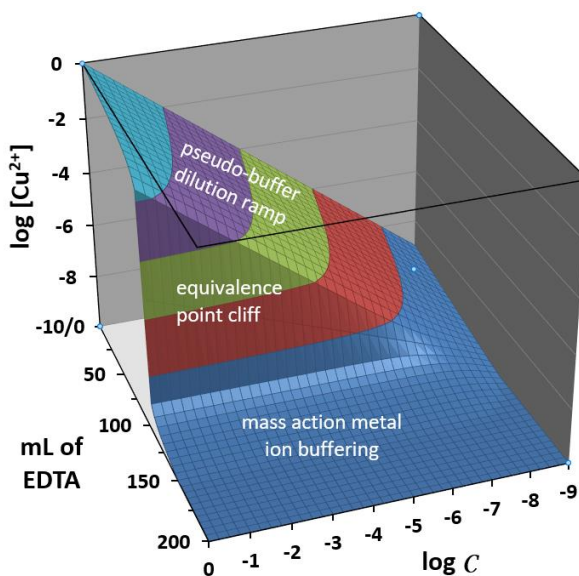
While a 2-D plot of a ligand-into-metal titration captures much about complexation equilibria, adding a dilution axis to create trend surfaces above a composition grid will reveal even more insights into possible system behaviors. Examination of the trend surfaces will quickly reveal the difference between metal ion pseudo-buffering and true metal ion buffering.

Our composition grid here consists of an x -axis that follows titration progress (mL of EDTA). The y -axis is the dilution parameter ($\log C$). Each grid slice in the titration direction represents a system for which both the titrant and the analyte concentrations are at a specific pre-experiment value. Complexation TOPOS assumes both are equimolar. Thus, the $\log C = 0$ front slice of the surface is associated with titrating a 1.0 M Cu^{2+} sample with a 1.0 M EDTA solution. The $\log C = -1$ slice represents titrating a 0.10 M Cu^{2+} sample with 0.10 M EDTA.

The Complexation TOPOS program will allow the user to easily generate a variety of helpful topo surfaces. All that is required is the set of equilibrium constants for the desired system. Many of these are compiled within the Complexation TOPOS workbook itself under the “Selected constants” tab.

The most fundamental topo surface for a ligand-into-metal titration is that for the free metal concentration. Figure 2.1-3 shows the log free metal ion surface for our sample Cu^{2+} -EDTA system at pH 4.0. This surface could easily be obtained experimentally by using a cupric ion-selective electrode. The viewing angle has been selected to make all portions of the surface visible. Text has been superimposed to show three general features of the surface: 1) a pre-equivalence point pseudo-buffer ramp; 2) the equivalence point cliff; and 3) the mass action metal ion buffer plateau. Each of these will be discussed in more detail.

Figure 2.1-3. The $\log [\text{Cu}^{2+}]$ topo surface for the Cu^{2+} -EDTA system at pH 4.0.



Pre-equivalence point portions of the grid form a metal ion “pseudo-buffering ramp”. The term pseudo-buffering is used for a situation in which the parameter of interest is controlled by an excess of a reactant. Before the 100-mL point, there is an excess of free Cu^{2+} . Excess Cu^{2+} decreases linearly with the addition of EDTA titrant, but given the log scale of the z -axis, the slope does not change dramatically over this region. If the system is diluted, however, the concentration of excess Cu^{2+} diminishes at the same rate as the overall system concentration. With each one unit change on the $\log C$ axis, the $\log [\text{Cu}^{2+}]$ value also changes by one unit. The combination of a slow decrease in the x -direction

and the steady decrease in the y-direction creates a ramp feature that descends at an angle of 45°. If the dilution were continued to even lower system concentrations, this ramp trend would continue.

As one approaches the equivalence point volume at 100 mL, the change in $\log [\text{Cu}^{2+}]$ becomes precipitous. Over the course of three grid points at 95, 100, and 105 mL, a 10 mL span, the curve drops to a low plateau. For the 1.0 M grid line this equivalence point cliff falls more than seven log units and shows a decrease in $[\text{Cu}^{2+}]$ of about 24,200,000 times. The height of the cliff decreases in the dilution direction because the starting value for $[\text{Cu}^{2+}]$ is successively lower. Note, though, that the plateau to which it drops, stays at essentially the same level. By a $\log C$ value of -7.75, the cliff has largely disappeared.

Below the equivalence point cliff there is a broad plateau that comprises the “mass action metal ion buffer” zone. No matter which direction one moves in this region, the value of $\log [\text{Cu}^{2+}]$ remains remarkably stable. The appearance of a plateau on a log free metal ion topo is the hallmark of a true metal buffering situation. Metal ion buffering is a concept infrequently encountered in analytical courses. With true metal ion buffering there is more chemistry occurring than simply a slow change caused by dilution of an excess species. The main difference between pseudo-buffering and mass action buffering for a metal ion is that, with the latter, dilution does not affect the free metal ion concentration substantially.

Consider the equilibrium constant expression for the 1:1 CuEDTA^{2-} complex:

$$\beta_1 = \frac{[\text{CuEDTA}^{2-}]}{[\text{Cu}^{2+}][\text{EDTA}^{4-}]} = 10^{18.80} \quad (2.1-19)$$

This is based on eq 2.1-1 in the chemical model. Because this system is restricted to 1:1 complexes, there is only a single overall stability constant, β_1 . (When higher stoichiometries are present there would be a β_2 for the 1:2 complex, a β_3 for the 1:3 complex, and so forth.) Eq 2.1-19 can be rearranged to solve for $[\text{Cu}^{2+}]$:

$$[\text{Cu}^{2+}] = \frac{1}{\beta_1} \times \frac{[\text{CuEDTA}^{2-}]}{[\text{EDTA}^{4-}]} \quad (2.1-20)$$

When the logarithm of both sides is taken, a metal ion analog to the logarithmic form of the Guldberg and Waage Mass Action Law¹² (see eq 1.1-2) for traditional acid-base buffers appears.

$$\log[\text{Cu}^{2+}] = -\log \beta_1 + \log \frac{[\text{CuEDTA}^{2-}]}{[\text{EDTA}^{4-}]} \quad (2.1-21)$$

Since $\log \beta_1$ is a constant, eq 2.1-21 indicates that $\log [\text{Cu}^{2+}]$ is controlled by the ratio of $[\text{CuEDTA}^{2-}]$ to $[\text{EDTA}^{4-}]$. But once the equivalence point has been passed, these two species track together. While the value for $[\text{EDTA}^{4-}]$ is quite small (due to the 94.6% predominant $\text{H}_2\text{EDTA}^{2-}$ form at pH 4), it slowly creeps toward its fractional concentration in the titrant solution as more is added. Only tiny amounts of free Cu^{2+} remain. Adding titrant dilutes the $[\text{CuEDTA}^{2-}]$ that has formed PLUS dissociates a small amount of it. As the system is diluted with water under these conditions, $[\text{CuEDTA}^{2-}]$ and $[\text{EDTA}^{4-}]$ decrease proportionally at the same rate. Thus, the ratio of the two important controlling species in eq 2.1-21 stays nearly constant.

How can the value of $\log [\text{Cu}^{2+}]$ remain almost unchanged by dilution? The answer is because dilution, through the mass action effect, causes a tiny bit of the complex to dissociate. The dilution water molecules more effectively solvate and separate the Cu^{2+} and EDTA^{4-} ions such that they cannot as easily re-encounter each other and re-complex. Consider the dissociation equation (2.1-22), the same formation equation (eq 2.1-1) with waters in the coordination sphere included:



Dilution is essentially perturbing the equilibrium by adding product. According to Le Chatelier's principle, the system will regain equilibrium by shifting to the left. The amount of Cu^{2+} released by the tiny amount of dissociation, is exactly what is needed to keep the $\log [\text{Cu}^{2+}]$ essentially constant. Table 2.1-1 follows this process for a 10-fold dilution that represents two points from the 150-mL dilution

slice of the Cu^{2+} -EDTA topo with $\text{pH} = 4$. The “Before Dilution” row lists the values of the system at 0.1 M. The “After Dilution” row simply drops each value by an order of magnitude for the 10-fold dilution. The “ Δ to Equilib” row shows the changes in the three relevant species as the perturbed equilibrium adjusts to new values. Finally, the “New Equilib” row holds the concentrations at 0.01M that once again satisfy the equilibrium constant expression of 2.1-19.

Table 2.1-1. Mass action metal ion buffering for a 10-fold dilution in the 150-mL slice of the $\log \text{Cu}^{2+}$ topo at $\text{pH} 4$. Before dilution = 0.10 M; after dilution = 0.010 M

	$[\text{Cu}^{2+}]$	$[\text{EDTA}^{4-}]$	$[\text{CuEDTA}^{2-}]$	$\frac{[\text{CuEDTA}^{2-}]}{[\text{EDTA}^{4-}]}$	$\log [\text{Cu}^{2+}]$
Before dilution	$1.05939184 \times 10^{-10}$	$5.98416234 \times 10^{-11}$	$3.9999999894 \times 10^{-2}$	6.684310617×10^8	-9.97494337
After dilution	$1.05939184 \times 10^{-11}$	$5.98416234 \times 10^{-12}$	$3.9999999894 \times 10^{-3}$	6.684310617×10^8	-10.97494337
Δ to Equilib	$+9.53452580 \times 10^{-11}$	$+2.85372013 \times 10^{-19}$	$-9.537571080 \times 10^{-11}$	----	----
New Equilib	$1.05939176 \times 10^{-10}$	$5.98416263 \times 10^{-12}$	$3.9999998940 \times 10^{-3}$	6.684310139×10^8	-9.97494340

Table 2.1-1 illustrates just how effective the mass action metal ion buffering is. Despite the fact that a 10-fold dilution has occurred, the value for $[\text{Cu}^{2+}]$ only changes in the eighth significant figure once the system has re-equilibrated. The shift to that new equilibrium has contributions from the small amount of dissociation that are almost nine times larger (actually, 8.99999928 times larger) than the diluted pre-existing $[\text{Cu}^{2+}]$. When added to the prior amount of Cu^{2+} , it is just what is needed to keep the equilibrium value of $[\text{Cu}^{2+}]$ essentially constant. Note, too, that the ratio of CuEDTA^{2-} to EDTA^{4-} has also remained effectively constant because the two species tracked proportionately together. The difference in their ratios only occurs in the eighth significant figure. The mass action metal ion buffering will continue until the amount of CuEDTA^{2-} complex that can still dissociate is too small to counterbalance the dilution of Cu^{2+} .

Just how good is the mass action metal ion buffering against dilution? If the solution is diluted by a factor of 10, 100, or 1000 under mass action metal ion buffering conditions, there is little change in the $\log [\text{Cu}^{2+}]$ value. As shown in Table 2.1-2, again at the 150-mL dilution grid line, $\log [\text{Cu}^{2+}]$ stays at a value of -9.97494 from $\log C = 0$ through $\log C = -4$. Thus, the system has been diluted by a factor of 10,000 and $\log [\text{Cu}^{2+}]$ has not wavered in its fifth decimal place. Eventually, sufficient dilution will begin to erode the metal ion buffer capacity as

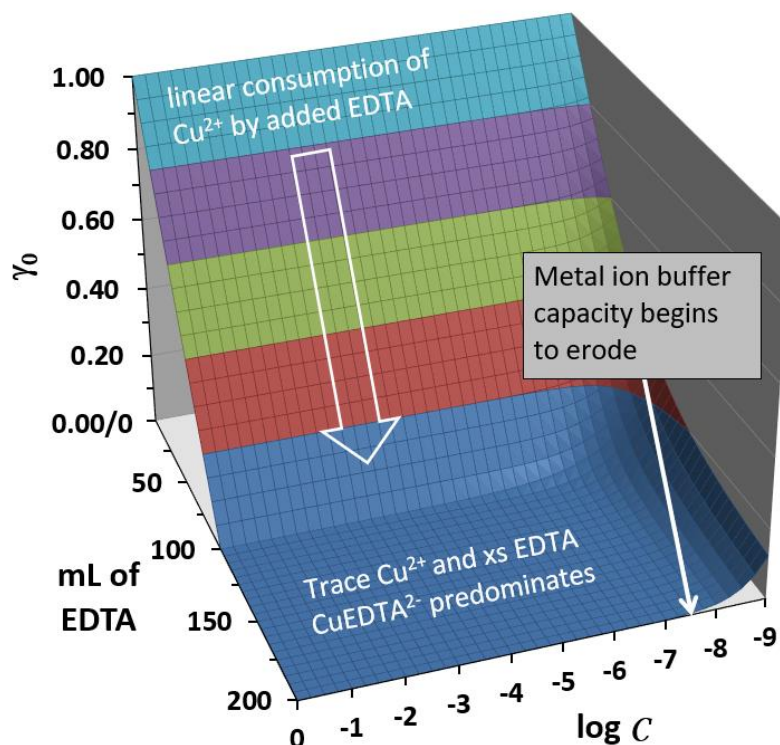
the quantity of CuEDTA^{2-} available to dissociate becomes smaller and smaller. Given the strength of the CuEDTA^{2-} complex, however, this will not occur for a lot more dilution cycles. The value of $\log [\text{Cu}^{2+}]$ has only diminished by 2% at the back edge of the composition grid after undergoing a billion-fold dilution. This is evidence that the buffer capacity is starting to erode. Were dilutions continued to further levels, a pseudo-buffer ramp would now develop and merge into the pre-equivalence point ramp.

Table 2.1-2. % Change in $\log [\text{Cu}^{2+}]$ for the 150-mL dilution slice of the Cu^{2+} -EDTA system at pH 4.0

mL of EDTA	$\log C$	$\log [\text{Cu}^{2+}]$	% change in $\log [\text{Cu}^{2+}]$	Extent of dilution
150	0	-9.97494	---	x1
150	-1	-9.97494	3.114×10^{-8}	x10
150	-2	-9.97494	3.426×10^{-7}	x100
150	-3	-9.97494	3.456×10^{-6}	x1000
150	-4	-9.97495	-0.00010	x10,000
150	-5	-9.97498	-0.00040	x100,000
150	-6	-9.97529	-0.00351	x1,000,000
150	-7	-9.97836	-0.03428	x10,000,000
150	-8	-10.00665	-0.31789	x100,000,000
150	-9	-10.17819	-2.03760	x1,000,000,000

3-D species distribution surfaces add further insights into the behavior of metal ion across the composition grid. We consider here only the free Cu^{2+} and the CuEDTA^{2-} complex. We ignore Cu^{2+} -hydroxy species. Figure 2.1-4 illustrates the fraction of metal in the free ion form, γ_0 , at each composition grid location. At higher $\log C$ values, there is a broad ramp descending at a 45° -angle indicating the steady consumption of Cu^{2+} with the addition of EDTA^{4-} as the CuEDTA^{2-} complex forms. The ramp bottoms out near $\gamma_0 = 0$ as soon as the equivalence point is reached at 100 mL.

Figure 2.1-4. The γ_0 trend surface (fraction of free Cu^{2+}) for the Cu^{2+} -EDTA system at pH 4.00.

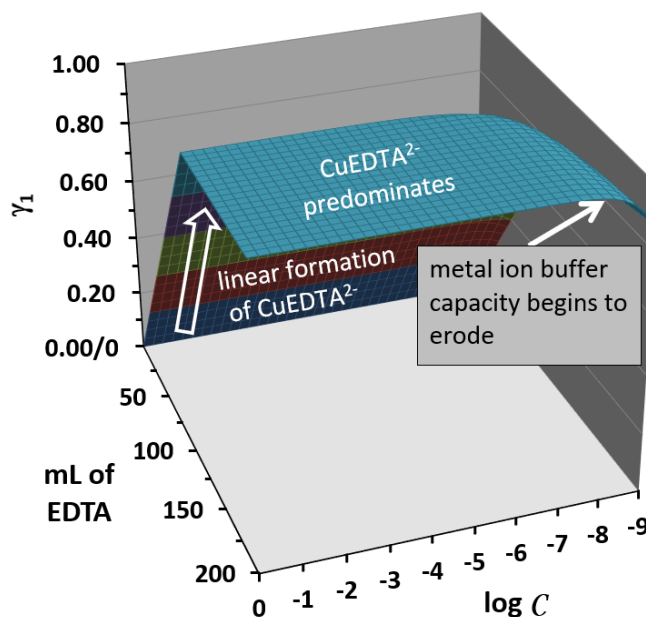


The extent of dilution-driven dissociation of the complex is also shown on this surface in the upward sweep of γ_0 as one gets to the lowest $\log C$ values of the front edge of the figure. The dilution at which the upward sweep begins is dependent on the value of β_1 for a complex and the pH at which the system is being modeled. Its appearance indicates that the metal ion buffer capacity of the system is becoming depleted. For the 200-mL slice, 12.4 % of the complex has dissociated by the $\log C = -9$ grid point.

The same effect can be seen in the γ_0 values on the pre-equivalence point consumption ramp. There is a slight upward curl at the point where dissociation of whatever complex is present begins to become significant. The CuEDTA^{2-} complex has such a large β_1 that not much dissociation has occurred even at the lowest $\log C$ point of -9. The strength of H_3O^+ for a ligand cannot compete until it hugely overwhelms the Cu^{2+} through mass action effects. At $\log C = -9$, H_3O^+ is present at about a 100,000-fold excess.

The companion γ_1 species surface, showing CuEDTA^{2-} complex behavior, is seen in Figure 2.1-5. For most $\log C$ values, a broad 45°-ramp slopes upward instead of downward because, in this instance, it represents formation of the complex. Once the equivalence point at 100 mL has been reached, there is an expansive plateau with γ_1 essentially equal to 1. At the right edge, the surface begins to curve downwards, an indication that dilution-driven dissociation of the complex is beginning to be more significant, namely, the metal ion buffering capacity of the system is almost depleted. Were the surface continued to lower $\log C$ values, a descending logarithmic ramp would develop that ultimately levels asymptotically to $\gamma_1 = 0$.

Figure 2.1-5. The γ_1 trend surface (fraction of CuEDTA^{2-}) for the Cu^{2+} -EDTA system at pH 4.00.



2.1.5 Metal Hydroxide Precipitates: Another Kind of Metal Ion Buffering

The Complexation TOPOS program will automatically check for the complication of metal hydroxide precipitate formation. The user is asked to supply the stoichiometry and the K_{sp} value for the solid metal hydroxide that could form if the pH is too high. After a grid point has been solved for $[\text{M}^{n+}]$, this value is used with the $[\text{OH}^-]$ associated with the specified pH to compute a trial ion product, TIP, that has the same form as the K_{sp} expression (eq 2.1-18). If the TIP is larger than the K_{sp} , precipitate will be present and the grid cell in the TIP

data array will be colored yellow. Once metal hydroxide precipitates have been confirmed, it is easy to compute a corrected $[M^{n+}]$ value from the K_{sp} expression. This corrected value can subsequently be used with the β_1 equation to obtain corrected free ligand and complex concentrations.

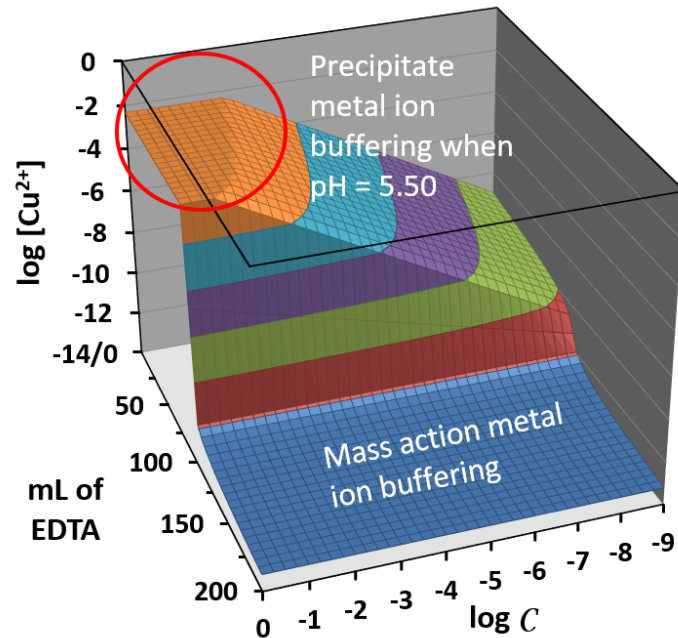
An example of a system with hydroxide precipitate conditions is shown for the Cu^{2+} -EDTA system in Figure 2.1-6 where the pH has been raised to 5.50. The figure is a portion of the TIP data array, indicating with yellow-shaded cells, the grid points for which precipitates occur. Note that the cell holds a log TIP value that is exactly equal to the $\log K_{sp}$ as indicated in cell B271 of the spreadsheet. The precipitate region does not usually extend beyond the equivalence point because the excess complexing ligand will out-compete OH^- for the remaining free metal ion. Log TIP cells with a white background have a value less than $\log K_{sp}$, indicating that the solution is unsaturated with respect to the hydroxide precipitate.

Figure 2.1-6. A portion of the log TIP data array from Complexation TOPOS showing $Cu(OH)_2(s)$ is present at pH 5.50 for yellow grid points.

	A	B	C	D	E	F	G	H	I
270	Log trial ion product precipitate check (log TIP)								
271	vs log Ksp =	-19.32	mL of ligand						
272			0.0	5.0	10.0	15.0	20.0	25.0	30.0
273	log total metal	0	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
274		-0.25	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
275		-0.5	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
276		-0.75	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
277		-1	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
278		-1.25	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
279		-1.5	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
280		-1.75	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
281		-2	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32	-19.32
282		-2.25	-19.32	-19.32	-19.33	-19.38	-19.42	-19.47	-19.51
283		-2.5	-19.50	-19.54	-19.58	-19.63	-19.67	-19.72	-19.76
284		-2.75	-19.75	-19.79	-19.83	-19.88	-19.92	-19.97	-20.01
285		-3	-20.00	-20.04	-20.08	-20.13	-20.17	-20.22	-20.26
286		-3.25	-20.25	-20.29	-20.33	-20.38	-20.42	-20.47	-20.51

Portions of the $\log [Cu^{2+}]$ surface where hydroxide precipitation has occurred will exhibit a flat plateau at the upper left-hand corner of the surface in the viewing angle employed (Figure 2.1-7). The fact that it is a plateau indicates that metal ion buffering is taking place. This is a different style of achieving a constant metal ion concentration in that it is a saturated solution of a hydroxide salt. Mass action metal ion buffering is also seen on this topo as the broad, lower plain that extends towards the front edge of the surface.

Figure 2.1- 7. The $\log [\text{Cu}^{2+}]$ surface for pH 5.50 with the precipitate metal ion buffer plateau region circled.



Systems that encounter hydroxide precipitate conditions exhibit perfect “precipitate metal ion buffering”. As long as there is some precipitate present, the K_{sp} equation (eq 2.1-18) is in effect. Rearranging that equation to solve for metal ion yields:

$$[\text{Cu}^{2+}] = \frac{K_{sp}}{[\text{OH}^-]^n} \quad (2.1-23)$$

Because the systems modeled in this chapter are at fixed pH, they are also at fixed $[\text{OH}^-]$. Both parts of the right-hand side of eq 2.1-23 are constants and, thus, $[\text{Cu}^{2+}]$ (and $\log [\text{Cu}^{2+}]$) will not vary. This can be verified by checking the $\log [\text{Cu}^{2+}]$ data array for grid locations that are colored yellow in the TIP array. For the example system of Figure 2.1-7, the $\log [\text{Cu}^{2+}]$ is fixed at -2.329.

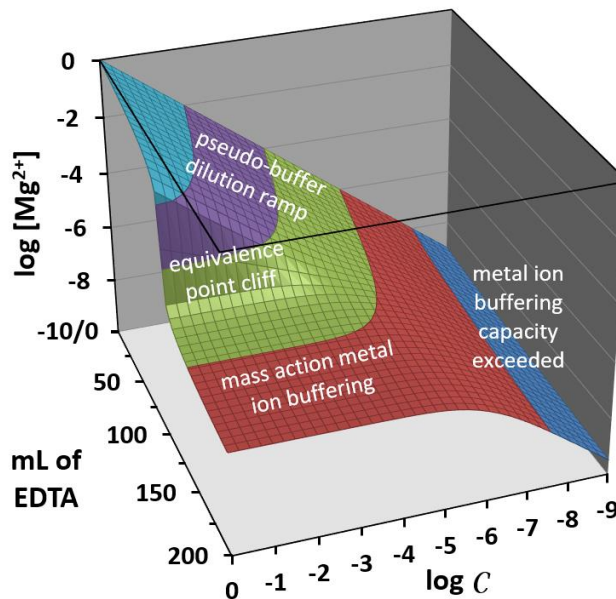
2.1.6 Another Sample System: Mg^{2+} -EDTA

Another set of topo surfaces for a system with EDTA complexes that are weaker than those of Cu^{2+} is useful for illustrating the role that β_1 plays in controlling surface features. The Mg^{2+} -EDTA system works well in this regard. The MgEDTA^{2-} complex has a log stability constant of 8.79, ten orders of

magnitude smaller than CuEDTA^{2-} 's value of 18.80. On the other hand, the $\log K_{sp}$ of -9.2 for $\text{Mg}(\text{OH})_2(\text{s})$ is ten orders of magnitude higher than $\text{Cu}(\text{OH})_2(\text{s})$'s value of -19.32. Hydroxide precipitates will not be as problematic at higher pHs. The pH used for the surfaces modeled here is 8.0.

The $\log \text{Mg}^{2+}$ topo for this system is contained in Figure 2.1-8. Note that it has the same features as that for Cu^{2+} (Figure 2.1-3) with the following differences: 1) The equivalence point cliff is shorter because the MgEDTA^{2-} complex is weaker and leaves more metal ion in solution under excess EDTA conditions; and 2) there is a more pronounced drop-off at the back of the mass action metal ion buffer plateau because its dilution buffer capacity is less than that for the Cu^{2+} surface. The weaker MgEDTA^{2-} complex dissociates more readily with addition of water. H_2O as a ligand is more competitive with EDTA in this system. The difference between the $\log \beta_1$ and $\log \beta_{\text{OH}1}$ values for the Cu^{2+} system is $18.80 - 6.50 = 12.30$ while that for the Mg^{2+} system is only $8.79 - 2.60 = 6.19$.

Figure 2.1-8. The $\log [\text{Mg}^{2+}]$ surface for the Mg^{2+} -EDTA system at pH 8.0.



The two metal species distribution topographs for Mg^{2+} -EDTA are found in Figure 2.1-9. Here, too, the same speciation features are found, but the weaker β_1 stability constant means that a complete transition in species is brought about through dilution. With the Cu^{2+} species surfaces, there were no regions in which free Cu^{2+} ion predominated once the half equivalence point had been reached in each titration. With the Mg^{2+} species surfaces there is a strip starting near $\log C =$

-6.50 where Mg^{2+} predominates all the way across in the titration progress direction. Dilution has dissociated CuEDTA^{2-} ; H_2O now surrounds the metal ion.

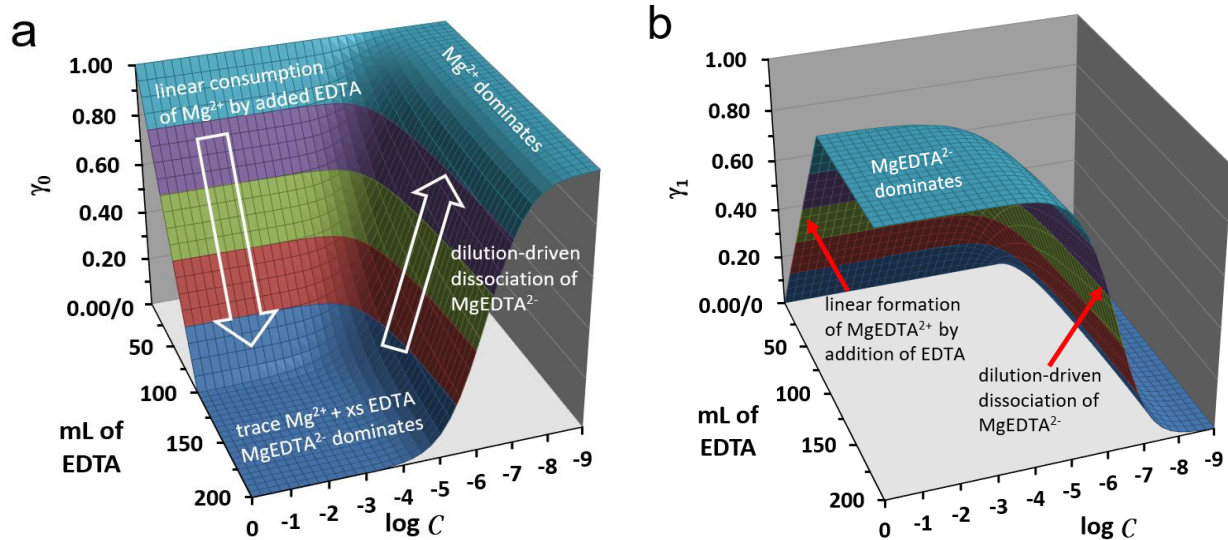


Figure 2.1-9. The species trend surfaces for the Mg^{2+} -EDTA system at pH 8.0.
a) γ_0 (fraction of Mg^{2+}); b) γ_1 (fraction of MgEDTA^{2-})

2.1.7 Titration Feasibility Surfaces

For some EDTA complexes, the pH can get too low for a good equivalence point break. The pH can also get too high for a good equivalence point break. Additionally, the quality of the break depends on the concentration of the metal ion of interest. Complexation TOPOS creates a second type of trend surface to help visualize the optimal pH for conducting an EDTA titration. Called Titration Feasibility Surfaces, they are constructed over a different grid-point system – mL of EDTA vs. pH.

Complications at low pH occur when H_3O^+ competes for binding sites on the EDTA molecule. The competition is more significant when the stability constant for a metal ion's EDTA complex is on the small side. Consider Ca^{2+} and Mg^{2+} , the ions most responsible for hard water. Both exhibit low pH complications in that Ca^{2+} has a somewhat low $\log \beta_1$ of only 10.65 and Mg^{2+} is even lower with a $\log \beta_1$ of 8.79. These are much smaller when compared to that of Cu^{2+} which has a substantially higher $\log \beta_1$ value of 18.80.

Traditionally, the inclusion of low pH complications has been handled with a conditional stability (or formation) constant, β_1' .¹³ A conditional constant is computed using the species distribution coefficient for the completely unprotonated form of the ligand. For EDTA, this corresponds to α_6 (or sometimes noted as Y^4). An example conditional constant for Ca^{2+} would be written as:

$$\beta_1' = \frac{\beta_1}{\alpha_6} = \frac{[\text{CaEDTA}^{2-}]}{[\text{Ca}^{2+}]\alpha_6[\text{uncomplexed ligand}]} \quad (2.1-24)$$

Accounting for low pH complications is often handled by providing a table or a plot listing the pH at which the β_1' for individual metal ion species is equal to 10^8 , a value large enough to provide a good equivalence point break.

Conditional constants as in eq 2.1-24 account for low pH complications, but not the high pH complications from OH^- ions competing against EDTA for the metal cation of interest. Formation of hydroxy complexes and hydroxide precipitates also interfere with the equivalence point break by lowering the free metal ion concentration prior to its occurrence. Eq 2.1-24 could be further modified to include a metal speciation coefficient, γ_0 .

$$\beta_1'' = \frac{\beta_1}{\gamma_0\alpha_6} = \left(\frac{[\text{CaEDTA}^{2-}]}{\gamma_0[\text{uncomplexed Ca}]\alpha_6[\text{uncomplexed ligand}]} \right) \quad (2.1-25)$$

Here, the γ_0 includes not only γ_1 as above (the fraction of CuEDTA^{2-}), but also $\gamma_{\text{OH}1}$ (the fraction of CuOH^+), $\gamma_{\text{OH}2}$ (the fraction of $\text{Cu}(\text{OH})_2^0$), $\gamma_{\text{OH}3}$ (the fraction of $\text{Cu}(\text{OH})_3^-$), $\gamma_{\text{OH}4}$ (the fraction of $\text{Cu}(\text{OH})_4^{2-}$), and $\gamma_{\text{Cu}(\text{OH})_2(s)}$ (the fraction of $\text{Cu}(\text{OH})_2(s)$).

A better solution to including titration complications from both too low and too high pHs is to construct a titration feasibility surface above a grid for which one axis is the titration progress (mL of EDTA) and the other runs the full range of pH values from 0 to 14. Complexation TOPOS includes this feature on a second calculation tab. It uses exactly the same input data as the metal ion topo calculations except that the pH is automatically cycled through all values and the total concentration of metal must be specified. It is fixed over the entire trend surface.

An example titration feasibility surface for the Ca^{2+} -EDTA system appears below as Figure 2.1-10. Two versions are provided – a wire-frame view that gives a visual sense of the topographic nature of the surface (Panel a), and a contour map view that allows for unambiguous determination of the exact grid coordinates for the surface regions (Panel b). A complete titration progresses from an upper plateau on the left to a lower plain on the right. The larger the drop, the better the equivalence point break. Complications from too high a pH are manifest as a shoulder that drops off the left side of the upper plateau. Complications from too low a pH show up as a ramp that slopes up to the right from the lower plain toward the upper level. The dashed yellow line that traverses the topo at pH 11 demonstrates that this is the optimal value for titrating a 0.001 M solution of Ca^{2+} .

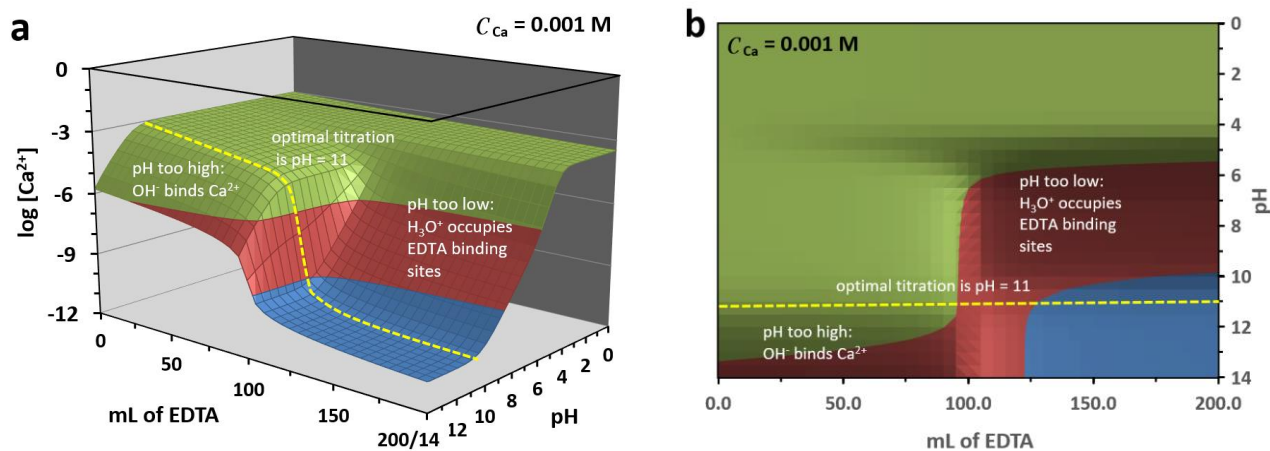


Figure 2.1-10. Titration feasibility surfaces for 0.001 M Ca^{2+} titrated with 0.001 M EDTA that indicate an optimal pH of 11. a) wire-frame; b) contour map.

2.1.8 Conclusions

Complexation TOPOS is new software to help visualize the equilibrium behavior of metal – ligand complexation systems. This chapter organizes the discussion around surfaces constructed above a titration – dilution composition grid where a ligand titrant is added to a metal solution. All examples illustrated here utilize EDTA as the ligand. We have intentionally restricted the system to a ligand that forms only 1:1 complexes. When higher stoichiometries are present, additional complications arise in metal ion buffering.

Viewing the topo surfaces produced by this Microsoft Excel workbook will help students visualize several aqueous equilibrium concepts:

- The surfaces dramatically demonstrate metal ion buffering, a topic not traditionally included in most textbooks;
- The surfaces clearly distinguish the difference between “pseudo-buffering” (that only occurs in the titration direction) and real “metal ion buffering” (that happens in BOTH the titration and dilution directions);
- Two different types of metal ion buffering are introduced – mass action metal ion buffering in post-equivalence point settings, and precipitate metal ion buffering in OH^- saturated pre-equivalence point conditions.
- Species distribution surfaces let students follow the formation of complexes during a titration PLUS discern the dissociation of the complexes as the system is diluted;
- Sloped boundaries on the metal ion buffer plateaus illustrate when buffer capacity has been exceeded; and
- Titration feasibility surfaces provide a means to select the ideal pH for a given analyte concentration.

The Complexation TOPOS software can be used in an introductory collegiate course of general chemistry. An understanding of its fine points, though, will require the chemical sophistication of students in junior- or graduate-level courses in analytical chemistry, biochemistry and aquatic geochemistry. The speed and ease with which new systems can be visualized makes this a powerful tool for simulation studies. Because it is implemented via Microsoft Excel, no new software need be purchased to run it. With run times usually less than 30 seconds, Complexation TOPOS can conveniently be used for “on the fly” calculations by an instructor during a classroom session. A query from a student about “What would happen if...” can easily be addressed with a new run of the program.

2.1.9 Supplementary files

Five downloadable files are included as additional supplements for this chapter:

1. The free, downloadable Complexation TOPOS software implemented as a Microsoft Excel workbook. A table of thermodynamic constants offers a variety of metal ion-EDTA systems to explore. Users, however, are free to supply their own constants as desired. Only systems with exclusively 1:1 complexes will work. Additional input data include protonation constants for the ligand, hydroxy complexation constants for the metal ion, and a K_{sp} for potential hydroxide precipitates.
2. Microsoft PowerPoint slides from which to present a lecture on metal – ligand complexation titrations and metal ion buffering where only 1:1 complexes are formed. This is applicable to EDTA titrations, the most common complexometric procedure in chemistry courses. Teaching points are highlighted and illustrated with extensively annotated surfaces. Separate sections are identified as appropriate for either lower division or upper division students.
3. A “Teaching with Complexation TOPOS” document that lists itemized teaching objectives. Each objective is matched to a range of slides in the PowerPoint lecture, so that an instructor can include whatever points are of interest. Following the discussion of the PowerPoint slides are suggested Complexation TOPOS workbook activities (homework, pre-lab, recitation or peer-led team discussions) and suggestions for coordinated laboratory experiments.
4. A detailed derivation of the mass balance equation that is solved for the equilibrium concentration of free ligand plus a section on the numerical techniques used to solve it.
5. A listing of the Visual Basic code for the Complexation TOPOS macros that compute the concentration of free ligand for each grid point.

As downloaded, Complexation TOPOS worksheets are populated with the Cu^{2+} -EDTA example for the metal ion topo and the 0.001 M Ca^{2+} -EDTA titration feasibility surface presented in this chapter. Constants for other metals are

included in the “Selected Constants” tab of the Complexation TOPOS workbook. Other ligands that will display exclusively 1:1 behavior like EDTA include DCTA (*trans*-1,2-diaminocyclohexanetetraacetic acid) and ATP (adenosine triphosphate).

Ligands that form higher stoichiometries introduce further complications in metal ion buffering. These complications are addressed in Chapter 2.2 Metal Ion Anti-Buffering.

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