

1 **Ecometrics: A Trait-based Approach to Paleoclimate and Paleoenvironmental**
2 **Reconstruction**

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22 **ABSTRACT**

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24 Ecometrics is a trait-based approach to study ecosystem variability through time.
25 An ecometric value is derived from describing the distribution of functional traits at the
26 community level, which may arise by environmental filtering, extinction, or convergence.
27 An ecometric relationship describes the correspondence between spatially explicit
28 ecometric values and corresponding environmental variation. Transfer functions and
29 maximum likelihood approaches have been developed with modern trait-environment
30 relationships to reconstruct paleotemperature, paleoprecipitation, and paleovegetation
31 cover given the distribution of functional traits within a community. Because the focus
32 for this approach is on the traits and not on species, it is transferable through space and
33 time and can be used to compare no-analog communities. In this paper we review the
34 concepts and history of ecometric analysis and then describe practical methods for
35 implementing an ecometric study.

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I. SUMMARY

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One of the factors that sort species geographically into communities is the filtering of species by their functional morphologies along climate and environmental gradients (e.g., mammalian herbivores with higher molars eat more gritty and abrasive vegetation and therefore more species with higher molars live in places with more gritty and abrasive vegetation), thus, the morphology has a direct relationship with its environmental condition. In this sorting process, the distribution of functional traits within a community moves toward an optimal environmental condition. These functional traits may be described in terms of their distributions within a community and descriptors of the distribution of community level functional traits have been defined as ecometrics (Eronen *et al.* 2010a; Polly *et al.* 2011). Thus, ecometrics are traits described at the community level that have a relationship with environmental condition. Ecometrics are spatially variable, because the composition of species and traits in communities vary through geography. If species are perfectly sorted, the trait distributions in communities will parallel variation in the environmental condition to which the traits are functionally linked (i.e. the ecometric correlation equals one). If the ecometric correlation is strong, one can estimate the most likely environmental condition given a specific ecometric value using a transfer function or likelihood estimation. If the ecometric correlation is not strong, one may still be able to estimate the most likely environmental condition, but the likelihood surface would be more flat, which would produce a more ambiguous reconstruction. The power of this approach is that functional trait measurements are transferable through space and through time, regardless of the specific species that make up the community. For this reason, ecometrics is a useful approach to reconstruct

59 paleoclimate and paleoenvironment (Damuth *et al.* 1992).

60 **II. TERMS**

61 **Functional trait** – a behavioral, biochemical, morphological, phenological,
62 physiological, or structural characteristic that has a physical or chemical interaction with
63 a specific environmental factor. This characteristic is expressed as a phenotype of
64 individual organisms and it is considered relevant to the response of organisms to the
65 surrounding abiotic conditions. A functional trait is something that can be observed and
66 measured.

67 **Geographic sorting** – the process by which trait distributions are arranged in geographic
68 space along gradients of environmental conditions.

69 **Taxon free** – not depending on taxonomic identity (i.e. it is a descriptor based on trait
70 values rather than on presence or absence of particular taxa). For example, using palms as
71 indicators of frost-free conditions is a taxon-based approach, whereas using counts of
72 stomatal density as indicators of carbon dioxide concentration is a taxon-free approach
73 (Beerling *et al.* , 2011).

74 **Ecometric value** – a statistic summarizing the distribution of a functional trait within a
75 community at a single geographic location. Means, variances, proportions, and extremes
76 have been used as descriptors in previous studies; however, any parameter that describes
77 a distribution of functional traits may be used.

78 **Ecometric patterning** – geography, or spatial variation, of ecometric values across
79 communities. Perfect patterning represents optimal distributions of populations and
80 species. The lack of patterning could represent a lack of useable covariation, a mismatch
81 between the trait and the environment, or it could result from the inappropriate choice of

82 environmental correlates.

83 ***Ecometric correlation*** – product-moment correlation between ecometric variation and
84 variation in the environmental condition. High correlations evince a close match between
85 the functional requirements of local communities and their abiotic condition.

86 ***Ecometric likelihood*** – the probability of finding a particular environmental condition
87 given the ecometric value of a community at any single geographic location.

88 ***Ecometric load*** – the amount of mismatch between the distribution of functional traits
89 and the selective optimum for the local environment. High loads may indicate risk to
90 changing environmental conditions. Note that high ecometric loads can be present even
91 with high ecometric correlations if traits are weakly but consistently sorted.

92 ***Ecometric optimum*** – the optimal distribution of an ecometric trait in a particular
93 environment. The optimum is more likely to be a distribution rather than a single trait
94 value, especially in locally heterogeneous environments (e.g., a savannah habitat favors
95 both large and small body sizes).

96 ***Transfer function*** – a function that represents the relationship between the ecometric trait
97 values and a relevant environmental variable.

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99 **III. THEORETICAL AND HISTORICAL BACKGROUND**

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101 Functional traits are features that organisms use to interact with their environment
102 and with other organisms (Diaz and Cabido 2001; Violle *et al.* 2007). Functional traits of
103 species within a community ultimately mediate the relationship between organisms'
104 morphology and their ecology and link organisms to biotic and abiotic conditions present

105 at particular geographic locations at a particular point in time (Ricklefs and Travis 1980;
106 Chapin 1993; Poff 1997). A certain combination of biotic and abiotic conditions will thus
107 favor traits that maximize an organism's performance, either through natural selection or
108 geographic sorting. Natural selection is an evolutionary process that acts on the variation
109 in a population, where individuals that thrive in their environment produce the most
110 offspring and disproportionately share their traits with the next generation (Darwin and
111 Wallace 1858). Species that move geographically in response to environmental change
112 may follow an environment for which they are already adapted and form new
113 assemblages as a result (Jackson and Overpeck 2000). We are not concerned with the
114 trait values of particular species, but with the distribution of traits within communities
115 (e.g., mean, standard deviation, and range; Damuth *et al.* 1992). Even weak sorting
116 processes can produce trait gradients at the community level, as has been demonstrated in
117 climate gradients in plant leaf traits (Wolfe 1979; Reich *et al.* 1997; Wilf 1997; Wright *et*
118 *al.* 2004; Royer *et al.* 2005; Wing *et al.* 2005; Cornwell and Ackerly 2009; Peppe *et al.*
119 2011), large mammalian herbivores dental traits (Janis and Fortelius 1988; Damuth *et al.*
120 1992; Fortelius *et al.* 2002; Mendoza *et al.* 2005; Damuth and Janis 2011; Eronen *et al.*
121 2010b, 2012), carnivoran locomotor traits (Polly 2010), snake locomotor traits (Lawing *et*
122 *al.* 2012), and mammal life history, physiological, and range traits (Lawing *et al.* 2016).
123 The study of functional traits that have a relationship with climate or environmental
124 gradients at the community level has been termed ecometrics to distinguish it from
125 ecomorphology of particular species or clades (Eronen *et al.* 2010a; Polly *et al.* 2011).
126 **Figure 1** shows a few examples of the morphology of ecometric traits.
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[insert **Figure 1** near here]

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130 The relationship between the distribution of functional traits in a community and
131 the corresponding environmental factors in the local environment is likely to be complex.
132 Some trait-environment relationships favor a single ecometric optimum in each local
133 environment such that all species tend to have the same trait value. Stomatal density on
134 plant leaves might be expected to have a single optimal value across all members of a
135 community because carbon dioxide concentrations and evapotranspiration conditions are
136 the same for all. However, locally heterogeneous environments are likely to favor a
137 heterogeneous ecometric optimum. For example, savannah environments tend to favor a
138 combination of large body masses (for animals that can travel long distances to procure
139 food in a comparatively resource poor habitat and defend themselves in the open) and
140 small body masses (for species that can subsist on the resources found in a limited area
141 and can find cover in grasses or tree tops). The nature of the ecometric optimum will
142 dictate how it should be measured. An optimum that favors a single trait value can always
143 be adequately represented with the community mean, but an optimum that favors a
144 complex distribution may be better characterized by variance, skewness, or other
145 measure. Temporal variation in environmental conditions may also shape the distribution
146 of the ecometric optimum. For example, Žliobaitė *et al.* (2016) recently showed that
147 recurring extreme conditions (like drought) were better predictors of dental traits than
148 average conditions, indicating that recurring limiting conditions may be important drivers
149 of community functional trait distributions.

150

Historical Background

151 Bailey and Sinnott (1915) conducted the first study of community-level functional
152 traits. They showed plant communities that have more leaves with ridges, or non-entire
153 margins, occur in moist temperate climates that experience warm summers and cold
154 winters. Conversely, plant communities that have leaves with no ridges, or entire leaf
155 margins, occur in dry climates including tropic, alpine and arctic regions, moors, steppes,
156 deserts, saline situations, and other physiologically dry climates. They used the
157 proportion of species within a community with a specified phenotype as their metric to
158 describe the community, what we refer to as an ecometric trait value.

159 Since Bailey and Sinnott (1915) demonstrated the variation in community leaf
160 shape across a temperature gradient, researchers have used leaf shape and other traits to
161 reconstruct paleotemperature. Most notably, Wolfe (1979, 1993) quantified the
162 relationship between leaf margins and temperature, which led to many quantitative
163 paleoclimate reconstructions from leaf assemblages, called leaf-margin analysis.
164 Contemporary to and since Wolfe's work, researchers have been interested in identifying
165 the function of leaf teeth (see Royer and Wilf (2006) for a history and discussion).

166 The ecometric approach has grown out of the formalization by Damuth *et al.*
167 (1992) of “taxon-free” characterizations of animal communities. These authors were
168 interested in understanding long-term evolutionary and ecological processes. They argued
169 that distributions of traits such as body size, dietary type, locomotor specialization, and
170 predator-to-prey ratios serve as descriptive indices that can be used to compare important
171 aspects of community function in the Paleozoic, Mesozoic, and Cenozoic or between
172 faunal and floral realms in a single time period, because they capture information about
173 productivity, resource availability, community physiognomy, and resource partitioning,

197 precipitation, between diet and precipitation (66.5%), and when diet and tooth crown
198 height are combined (74.2%). Community hypsodonty levels, therefore, have a strong
199 correlation with annual precipitation, which affects both plant tissue properties and the
200 amount of local grit (Fortelius *et al.* 2014) and may be used as a paleoprecipitation proxy
201 that constrain regional details about vegetation patterns and climate models (Fortelius *et*
202 *al.* 2002).

203 Together with other dental traits, hypsodonty can additionally be used to
204 estimate more indirect properties like net primary productivity (Liu *et al.* , 2012) or more
205 proximate ones like production of volcanic ash (Strömberg *et al.* , 2013). Such complex
206 combinations of proximal and distal environmental factors are likely to be associated
207 with all ecometric traits (Polly and Head 2015). Žliobaitė *et al.* (2016) showed that dental
208 traits are closely linked to vegetation greenness (NDVI) in addition to precipitation and
209 temperature. This is reassuring as NPP estimates used in Liu *et al.* (2012) are computed
210 using precipitation as an input and highly dependent on NPP. NDVI is a direct
211 observation of vegetation greenness and is independent of precipitation and temperature
212 measurements. The NDVI depends on climatic conditions and reflects NPP and thus the
213 availability and quality of herbivores' food. Using data from present-day seasonal
214 environments in Africa, Žliobaitė *et al.* (2016) demonstrate that the dental traits show
215 strong correlations to non-availability of preferred plant foods (e.g., during dry seasons or
216 longer dry periods), rather than the properties of average foods consumed. This is the
217 main functional link between climate and herbivore teeth and closely follows the
218 suggestion by Owen-Smith (2002) (see also discussion in Liu *et al.* 2012 and Fortelius *et*
219 *al.* 2014).

220 Other dental characteristics (such as dental wear patterns, dental structure, and
221 tooth crown complexity) have also been used as estimates of diet in mammals (Fortelius
222 and Solounias 2000; Evans *et al.* 2007; Eronen *et al.* 2010a; Wilson *et al.* 2012; Evans
223 2013; Saarinen 2014; Saarinen and Karme 2017). Wilson *et al.* (2012) used the dental
224 shape descriptor of orientation patch count (OPC), which is a measure of dental
225 complexity that correlates well with feeding ecology in extant mammals, to determine the
226 paleodiet of the extinct mammalian clade Multituberculata. They were able to identify a
227 shift from a more carnivorous or omnivorous diet among early multituberculates into a
228 more herbivorous diet around 85 million years ago. This shift coincided with the rise of
229 angiosperms. Since vegetation patterns are driven by climatic conditions, these other
230 dental characteristics could potentially be used as climatic proxies. Evans (2013)
231 reviewed dental shape descriptors, which can be used in ecometric studies and will be
232 useful for describing environmental conditions in the past.

233 Another well-studied trait in both endothermic and ectothermic vertebrates is
234 body size, initiated by the work of Bergmann (1947). Mean body size in non-flying
235 mammals has been shown to increase as temperature decreases, and therefore mean body
236 size increases geographically toward the poles (Rodriquez *et al.* 2008; Eronen *et al.*
237 2010a). It has also been documented in ectothermic animals that body size is positively
238 correlated with mean ambient temperature (Makarieva *et al.* 2005). This has allowed for
239 the use of ectothermic animals, to be used to estimate paleotemperatures (Head *et al.*
240 2009; Polly *et al.* 2011; Head *et al.* 2013). Examples of ecometrics in plants, birds,
241 mammals, and snakes are detailed in Table 1, showing the functional trait and the
242 environmental condition for which it is related.

243

244 **Table 1. Examples of ecometrics in plants, birds, mammals, and snakes.**

245 **Environmental conditions are mean annual temperature (MAT), annual**

246 **precipitation (AP), atmospheric carbon dioxide (pCO₂), net primary productivity**

247 **(NPP), trophic position (TP), dietary classification (DC), and vegetation cover (VC).**

Group	Functional Trait	Environmental Condition	Citation
Plants	Leaf margin	MAT	Wolf 1979
Plants	Leaf shape	MAT	Wolf 1990; Royer <i>et al.</i> 2005; Peppe <i>et al.</i> 2011
Plants	Stomata counts	pCO ₂	Beerling <i>et al.</i> 2002
Birds	Body mass	MAT	Meiri and Dayan 2003
Mammals	Body mass	MAT	Damuth <i>et al.</i> 1992
Mammals	Tooth morphology	AP; TP; DC; NPP	Evans 2013
Ungulates	Hypsodonty	AP	Fortelius <i>et al.</i> 2002
Carnivorans	Limb proportion	VC; MAT; AP	Polly 2010
Snakes	Body length	MAT	Head <i>et al.</i> 2009
Snakes	Tail proportion	VC	Lawing <i>et al.</i> 2012

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Ecometric patterning

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Geographic sorting of traits along environmental gradients is one of three

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processes by which ecometric patterning can emerge, along with evolutionary adaptation

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and extinction (Polly *et al.* 2015). Environmental gradients are shown to filter species

253 geographically (Belmaker and Jetz 2012). The filtering effects of environmental gradients
254 may sort species geographically by their traits, resulting in local communities with
255 similar trait values that are correlated with local environmental conditions. The ecometric
256 approach was formalized as a way of synthesizing data from the ecological present and
257 geological past to measure responses of ecosystems to climate change in order to better
258 predict the risks posed by global change over the next millennia (Eronen *et al.* 2010a;
259 Polly *et al.* 2011). It has been used to investigate the impacts and risk of extinction
260 (Wilson *et al.* 2012; Polly and Sarwar 2014; Polly and Head 2015) and to understand
261 non-ecological processes (Lawing *et al.* 2016). The relative roles of geographic sorting,
262 local adaptation, and extinction have been investigated by process-based simulation
263 (Polly *et al.* 2015). Ecometrics and its paleontological precursors have been used to
264 estimate paleobiotic conditions using traits (Damuth *et al.* 1992). For example, ecotherm
265 body size (Head *et al.* 2009; Head *et al.* 2013) and leaf shape (Wolfe 1993; Little *et al.*
266 2010) have been used as paleothermometers and tooth crown height, hyposodonty, has
267 been used to estimate paleoaridity (Fortelius *et al.* 2002).

268 The ecometric approach may be used to forecast community responses to
269 anthropogenic climate change (Barnosky *et al.* , 2017). The concept of ecometric load,
270 which is the mismatch between community-level functional trait values and optimal
271 performance, potentially allows us to estimate the vulnerability of a community to
272 climate or environmental change when the optimal performance of the traits along an
273 environmental gradient is known (Polly *et al.* 2015). If changing conditions increase the
274 ecometric load, communities are more likely to become vulnerable.

275 Methods for using ecometrics to characterize paleoclimate and paleoenvironments
276 have been expanded extensively. For example, Head *et al.* (2009) made a significant push
277 forward on the construction of ecometric models and the application of the transfer
278 function. Instead of solely using correlative models for inference, they used a mechanistic
279 model from the physiology of poikilothermic metabolism along with modern
280 observations of boid snakes and the temperatures they live in to predict paleotemperature
281 at 58-60 Ma (Paleocene) in the neotropics. They found a minimum mean annual
282 temperature of 30-34°C was needed in the Cerrejon Formation in Colombia during this
283 time in order for the large boid, *Titanoboa*, to survive. This is several degrees warmer
284 than the mean annual temperature of 26-27°C found in that area of the world.

285 The effects of faunal sampling, extinction, and extirpation on ecometric patterns
286 was investigated by Polly and Sarwar (2014) using resampling and rarefaction methods
287 with calcaneum gear ratios. Gear ratios are related to the locomotor style of an animal
288 and, in turn, related to the animal's habitat. Polly and Sarwar (2014) showed that
289 extinction, extirpation, and range change have minimal effects on ecometric correlations
290 when they affect less than a quarter of the species in North American carnivoran
291 communities. If the correlation between gear ratio and an environmental variable, such as
292 vegetation cover, is either high or low, then extinction of more than 25% of species will
293 alter the correlations, but the strongly and weakly correlated environmental variables will
294 still be distinguished. Local extinctions, extirpation, caused a decline in ecometric
295 correlations; however, up to 75% of species could be lost this way before ecometric
296 patterns were completely lost. This result suggested that even in fossil faunal
297 assemblages with a small proportion of the total fauna, the ecometric patterns may still be

298 recoverable if enough independent assemblages are considered. These authors also
299 showed that global extinction and large-scale extirpation have a less predictable effect on
300 ecometric correlations than do local extinctions. How the ecometric pattern is affected
301 by global extinction depends on which organisms go extinct and what their ecometric
302 correlation was. So, if a species, such as a polar bear, is a large contributor to local
303 ecometric means, and if its range is correlated to an extreme of the environmental
304 variable, such as zero vegetation cover, then its extinction could drive correlation up or
305 down dependent on the circumstance.

306 *Ecometric Modeling*

307 Polly *et al.* (2016a) used stochastic modeling to assess the role of population level
308 processes in the formation of ecometric patterns. They systematically varied parameters
309 like local selection intensity, probability of dispersal, probability of extirpation, gene
310 flow, and ancestral trait value to understand the interaction between geographic sorting
311 processes, trait selection, and clade dynamics in producing ecometric patterns. These
312 authors introduced the concept of ecometric load, an analogy with genetic or mutational
313 load, as the mismatch between the distribution of functional traits in a community (or a
314 group of communities) and the selective optimum for those traits in the local environment
315 (Polly *et al.* 2016a). In cases where ecometric load can be measured, it may help predict
316 whether environmental change is likely to make a community more vulnerable to
317 reorganization or extinction. Interestingly, their models frequently produced parallel trait
318 evolution in different clades, rather than the kinds of phylogenetically correlated trait
319 distributions that are observed in many clades. For example, calcaneum gear ratio, which
320 has strong ecometric sorting in the real world, also has a strong phylogenetic correlation

321 with about 60% of its variance being explained by phylogeny (Polly *et al.* , 2017). The
322 lack of phylogenetic correlation in the models suggested that empirically observed
323 examples of trait-based phylogenetic sorting of species into communities in the modern
324 world results from large-scale turnover in environments.

325 *Ecometrics and ecogeographical rules*

326 Ecogeographical rules often describe patterns that we would classify as ecometric.
327 Ecogeographic rules are hypotheses about how morphological variation changes along
328 environmental or geographic gradients. They may be rules regarding within-species
329 variation or between-species variation. Across species variation has been the most
330 important component of variation to consider for the ecometric approach.

331 The most notable ecogeographic rule is Bergmann's Rule (Bergmann 1847;
332 Blackburn *et al.* 1999). It states that body mass correlates with temperature and this has
333 been demonstrated both intraspecifically (Ashton 2002; Freckleton *et al.* 2003) and
334 interspecifically (Blackburn and Hawkins 2004; Diniz-Filho *et al.* 2007). Other
335 ecogeographical rules include Allen's rule (length of appendages in endotherms
336 positively correlate with temperature; Allen 1877), Gloger's rule (pigmentation is
337 correlated with humidity within endothermic species; Gloger 1833), Fox's rule (among
338 small Australian mammals during community assembly, it is more likely that species
339 entering a community will represent different functional groups; Fox 1987) and Jordan's
340 rule (there is an inverse relationship between meristic characters and water temperature;
341 Lincoln *et al.* 1982). See Gaston *et al.* (2008) for a review of ecogeographic rules.

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343 **IV. IMPLEMENTING AND ECOMETRIC ANALYSIS**

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345 In order to document the existence of an ecometric pattern, three types of data are
346 required: geographic ranges of species, abiotic conditions, and functional trait
347 measurement of species. The spatial resolution of the data and the density of sampling of
348 traits and environmental variables within local communities will depend on the scale of
349 the functional relationship and on the question being addressed. Here we focus on
350 ecometric patterns that emerge at regional, continental, or global scales, but the same
351 principles could be applied to patterns that emerge on landscape scales. To simplify
352 large-scale analysis, we recommend measuring trait distributions by sampling the trait
353 once for each species making up the local community and making the assumption that
354 each species has the same trait value everywhere it occurs. Finer scale analyses might
355 benefit from sampling the frequencies of traits among the individuals in a local
356 community to account for variation in abundance of the species making up the
357 community, or from measuring the local values of traits within each community. Because
358 of our choice of scale, our analysis requires information about the geographic range
359 where species are known to live or where they have the potential to live. For our
360 purposes, local community composition includes all the species whose ranges overlap at
361 a sampling point, an assumption that is reasonable for coarse scale analysis, but which
362 might be unreasonable for a finer-scale landscape analysis.

363

Geographic Range

364 Geographic range data are often available from field guides and are becoming
365 more readily available online as spatial shapefiles. For example, NatureServe
366 (www.natureserve.org) and International Union for Conservation of Nature host a

367 website that has an option to download spatial data that depict the ranges of species as
368 polygons (www.iucnredlist.org). The ranges are typically drawn by experts and represent
369 the general areas of occupation of a species. Species occurrences may be used to draw
370 range maps, if no range maps are available, so long as the occurrence data are relatively
371 randomly distributed across the entire environmental range of the species. Once the
372 geographic ranges are obtained, a sampling scheme for measuring the trait-environment
373 relationship needs to be determined. Sampling sites may be systematically or randomly
374 scattered across the extent of the study area. A list of species that occur at each sample
375 site should then be compiled. Some sources of data for geographic ranges include the
376 NatureServe and IUCN for mammals, birds, amphibians, coral and some fishes
377 (www.iucnredlist.org). Plant distribution data for North America and Europe are
378 available from USDA PLANTS database (plants.usda.gov) and from the European
379 Environmental Agency (eea.europa.eu). The Global Biodiversity Information Facility
380 contains species occurrences (longitude and latitude) of both plants and animals
381 (www.gbif.org). A geographic information system (GIS) is useful to work with
382 geographic ranges and other geographic information. Open source systems are available,
383 such as QGIS, DIVA, or even R. Proprietary software is also available; the most popular
384 products are developed through ESRI. Researchers should check with their institutions
385 for GIS services and licensing.

386 *Environmental Data*

387 Environmental factors can be measured directly in the field at sample sites or
388 collected from maps representing the geographic variability of the environmental
389 condition. For every sample site, the environmental variables that are functionally linked

390 to the trait of interest should be sampled. PRISM Climate Group and WorldClim
391 databases provide relatively high-resolution datasets of climate for the globe
392 (www.prism.oregonstate.edu and www.worldclim.org, respectively). Global potential
393 vegetation is available from UW SAGE (www.washington.edu/research/tools/sage/);
394 global historical vegetation coverage is available from Oak Ridge National Laboratories
395 (dx.doi.org/10.3334/ORNLDAAC/419); global digital elevation models and annual
396 productivity are available from NASA (earthobservatory.nasa.gov/) and USGS
397 (nationalmap.gov/elevation.html); global soil distributions are available from
398 International Institute for Applied Systems Analysis (www.iiasa.ac.at/); global land cover
399 is available from the European Space Agency (www.esa.int/); global nitrogen deposition
400 is available from Oak Ridge National Laboratory (www.ornl.gov/); global freeze and thaw
401 status is available from the National Snow and Ice Data Center (nsidc.org/); global
402 terrestrial ecosystems are available from World Wildlife Fund (www.worldwildlife.org).
403 In addition to all of these data sources, there are numerous others to find online and in the
404 published literature. One may use any reliable map as a reference for the environmental
405 condition at sample localities.

406 *Functional Traits*

407 Functional traits should be measured or categorized for each species that has the
408 functional trait of interest within each community. Ideally, one would measure the traits
409 from all the species that occur at each sampling location; however, a species value may
410 be used for all of the locations in which that species occurs. Species values for traits may
411 be collected from measuring specimens directly or from obtaining measures from the
412 published literature. Typically only one value for each species is necessary; however, if

436 sampling sites into a table with the mean trait values and the associated environmental
437 values in columns and sites in the rows. If there is more than one environmental variable
438 associated with the trait of interest, then in this table each variable requires its own
439 column. Ecometric correlation can easily be calculated from this table as the Pearson's
440 correlation coefficient (r), or a nonparametric equivalent, of the two columns as a
441 measure of correspondence between the environmental parameter and the ecometric trait.
442 If the performance relationship between trait and environment is known, the ecometric
443 load can be calculated as the mean absolute difference between the observed trait means
444 and the expected values for all rows in the table (i.e. the residual between the observed
445 and expected values). Note that ecometric load is largely independent of the ecometric
446 correlation, except insofar that a weak correlation requires at least some mismatch
447 between performance optimum and realized trait mean and thus cannot have a load of
448 zero (Polly *et al.* 2016a). Ecometric patterns with strong correlations can also have strong
449 loads. Establish a transfer function to determine the specific relationship between the two
450 variables (i.e. it estimates function coefficients). If there are fossil localities to estimate
451 past abiotic conditions, then apply the transfer function to the mean of the functional
452 traits measured from the fossils at a single fossil site. Calculate confidence limits for the
453 estimated abiotic condition.

454 Ecometric estimates of paleoenvironment can be made from a regression-based
455 transfer function or from a likelihood distribution of environmental values given an
456 observed ecometric value. If regression-based methods are used, reduced major axis
457 (RMA) regression may be the most appropriate if there is uncertainty in the independent
458 variable. Transfer functions are prediction equations derived from regressing the

459 environmental variable of interest onto the predictive trait value. Different transfer
460 functions are used depending on the type of trait variable and the type of environmental
461 variable. Other considerations include the type of predicted relationship between the trait
462 and environment and the statistical fitting procedures.

463 Transfer functions have been typically calibrated with modern distributions of
464 species and their functional traits. For optimal use of the transfer function, for both
465 reconstructing abiotic condition and tracking trait distributions through time, the
466 functional trait should be either directly fossilizable or able to be estimated from fossil
467 specimens. For example, hypsodonty may be estimated directly from fossil specimens
468 (Fortelius *et al.* 2002) and body size may be accurately estimated from fragmentary
469 skeletal and dental remains (Alexander 1989; MacFadden 1990).

470

471 **V. STRENGTHS OF APPROACH**

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473 Ecometrics allows us to quantify the dynamic relationships between organisms
474 and their environment. Arguably, the primary strength is that ecometric traits are
475 predictable and transferable through space and time. Since ecometrics uses taxon-free
476 descriptors of community characteristics, it allows for the comparison of community
477 changes in the modern world to those in deep time (Eronen *et al.* 2010a; Polly *et al.*
478 2011). The species that make up the community in the modern world do not need to be
479 the same as those that make up the paleocommunity; the only thing the two communities
480 need to share is the functional trait under study. Because ecometrics focuses on traits that
481 are directly related to environmental conditions, it can be applied to questions on many

482 geographic and temporal scales (Wolfe 1994; Wether *et al.* 1999; Thompson *et al.* 2001;
483 Fortelius *et al.* 2002). This quality allows ecometrics to be applied at local community
484 levels up to global community levels. It also allows for the comparison of ecometric
485 patterning across these scales. In addition, many ecometric traits are easily measured on
486 both animal and plant fossils (Alexander 1989; MacFadden 1990; Fortelius *et al.* 2002;
487 Royer *et al.* 2005; Head *et al.* 2009).

488

489 **VI. BIASES AND SHORTCOMINGS**

490

491 The incomplete nature of the fossil record may influence the quality of data in
492 ecometric studies. However, Polly and Sarwar (2014) showed that even if only 25% of
493 the species of a community are found in a fossil locality, the ecometric patterns still
494 appear. Taphonomic issues with the fossil preservation should also be taken into account,
495 because the functional traits used in ecometric studies need to be measurable or inferred
496 from the fossil remains. It has often not been the case where this is an issue (Alexander
497 1989; MacFadden 1990; Fortelius *et al.* 2002; Royer *et al.* 2005; Head *et al.* 2009; Peppe
498 *et al.* 2011; Wilson *et al.* 2012) and there are various ways to remove the taphonomic
499 influence from the fossil, thus returning it, or a model of it, to its original state (i.e.,
500 retrodeformation methods; Webster and Hughes 1999; Angielczyk and Sheets 2007).

501 Several important assumptions are made with the ecometric approach, including,
502 that the ecometric relationship doesn't change through time and that the full range of
503 morphologies and environmental conditions are represented (i.e. they are not truncated –
504 there are no biased extinctions and only analogous climate conditions). If these are

505 reasonable assumptions for the ecometric trait in question, one may use an ecometric
506 relationship to reconstruct paleoclimate and paleoenvironment, given a couple more
507 assumptions about the fossil localities. The community of fossils within the fossil
508 localities being studied should represent the actual community of species that co-occurred
509 with the depositional environment. In addition, the functional traits should be measurable
510 in the preserved fossils. More work is needed to quantify coefficients describing the
511 relationship between functional traits and environmental conditions to understand if and
512 how they change through time and space.

513 More research needs to be done concerning intraspecific variation. Intraspecific
514 variation, at least in regards to carnivoran calcaneum gear ratios, is high, and it does not
515 follow community level ecometric patterning. Models seem to support the idea that this is
516 possible due to the high level of gene flow within populations, but the overall signal at
517 the community level overshadows the intraspecific variation of the populations.

518

519

VII. ECOMETRICS EXAMPLE

520

521 In this section we provide a worked example of how mean annual temperature can
522 be estimated from the distribution of body masses in North American mammals using a
523 likelihood approach. In addition to presenting the method, we also discuss the theory for
524 why ecometric distributions are related to local environment and how our methodology is
525 related to that theory.

526

527 When the relationship between trait performance and environment is known, the
likelihood function can, in theory, be determined *a priori* (Arnold 1983). Performance-

528 environment relationships can sometimes be estimated for traits recovered in fossils using
529 tools such as finite element analysis, hydrodynamic or mechanical principles, or
530 functional morphological experimentation (e.g., Baumiller *et al.* 1991; Rayfield 2007;
531 Wroe 2008; Shino and Suzuki 2011; Stayton 2011; Polly *et al.* 2016b). However, in
532 many cases the performance-environment relationship is unknown, even when the trait-
533 function relationship is well understood. For example, the functional role of hind-limb
534 gear ratio of mammals is understood (it is related through physical lever principles to the
535 efficiency of hind limb extension, and thus to the mechanics of walking, springing,
536 climbing, and running), but its distribution in a particular environment is difficult to
537 predict *a priori* because it is likely to be influenced by a combination of factors such as
538 vegetation physiognomy, terrain ruggedness, substrate, snow cover, and predator-prey
539 interactions (Klein *et al.* 1987; Polly 2008, 2010; Crête and Larivière 2003). In such
540 cases, likelihoods can be estimated directly from empirical data by making the
541 assumption that the distribution of traits in modern communities is close enough to
542 equilibrium to be representative. Polly and Sarwar (2014) found this to be a reasonable
543 assumption for carnivore limb ratios, but care should be taken before generalizing that
544 result to other traits.

545

546 [insert **Figure 2** near here]

547

548 Likelihoods for paleoenvironmental parameters can be estimated empirically by
549 projecting environmental variables into an ecometric space, which is a mathematical
550 space whose axes are statistical descriptors of the distribution of traits in local

551 communities (**Figure 2A**). Ecometric space is in some ways the conceptual opposite of
552 Hutchinson's (1957) niche space, in which a species' niche is the volume it occupies in a
553 multidimensional space whose axes are environmental variables. Translated into
554 ecometric terms, the niche of a species is circumscribed by the performance of the
555 functional traits that relate it to the environmental factors. An ecometric space inverts that
556 relationship by mapping the distribution of environmental parameters on trait-based axes,
557 except that those axes describe the distribution of traits in community assemblages rather
558 than the traits of a single species. **Figure 2A** shows mean annual temperature mapped
559 into an ecometric space whose axes are defined by the distribution of log body mass (kg)
560 of mammals.

561 To create this ecometric space we sampled mammal faunas at 50 km intervals
562 across the entirety of North America. At each sampling point we calculated the mean and
563 standard deviation of the body masses (kg) of the local mammals from the data compiled
564 by Smith *et al.* (2003) and we recorded the local mean annual temperature (MAT) from
565 Hijmans *et al.* (2005).

566 Estimating the likelihood of MAT from community trait characteristics is then a
567 three-step process. First, the trait data should be binned so that a frequency distribution of
568 the environmental variable can be calculated. The number of bins is arbitrary, but it
569 should be coarse enough to encompass a reasonable number of communities in the
570 densest areas of the trait space, yet fine enough to be biologically meaningful. The ideal
571 bin size would be about as wide as the standard errors of the means and standard
572 deviations in the bin. We divided our ecometric space into 625 bins (25 X 25).

573 Second, the MAT observations in each trait bin were themselves binned to
574 tabulate their frequency distribution. The number of temperature bins is also arbitrary (we
575 used a bin size of 1°C). Once binned, a discrete probability density function (PDF) can be
576 estimated by dividing the bin counts by the total number of observations. A continuous
577 PDF can also be fit to the frequency data. **Figure 2B** shows a continuous PDF for
578 temperature in communities with a mean ln body mass between 3.05 (21.11 kg) and 3.13
579 (22.87 kg) and a standard deviation between 1.05 and 1.10 (black box in **Figure 2A**)
580 based on a Gaussian kernel density estimate with bandwidth of 1°C.

581 With these pieces in place, a maximum likelihood estimate of the environmental variable
582 (MAT) can be made by measuring the trait (body mass) mean and standard deviation at a
583 site of interest and then finding the environmental value that maximizes the PDF. The
584 maximum likelihood estimates of MAT for all the sampling locations in North America
585 are shown in **Figure 2C**, compared with the real MAT values in **Figure 2D**. This
586 estimate (MAT at sampling locations) is reasonable, but tends to be too low in high
587 elevation areas and too warm at lower elevations (see anomaly map in **Figure 2E**). On
588 average, the discrepancy between the real MAT and the estimate based on mammal body
589 masses was 3.9°C, which serves as an approximate standard error (but one that is
590 probably underestimated because the likelihood functions were estimated from the same
591 data on which they were tested).

592 One of the primary advantages of using likelihood and ecometric spaces is that the
593 likelihoods of alternative reconstructions can be compared. For example, the maximum
594 likelihood estimate of MAT for the Central American location highlighted by the black
595 circles in **Figure 2C-E** is 24.95°C with $L(24.95)=0.274$ derived from the PDF for that

596 location (**Figure 2B**). The real MAT is 25.3°C, which has $L(25.3)=0.265$, which is
597 clearly much more plausible with a likelihood ratio of 0.967 than an MAT of 20°C,
598 where $L(20.0)=0.024$ produces a likelihood ratio of only 0.088. This approach can be
599 developed into a formal likelihood ratio test of alternative hypotheses about
600 paleoenvironment, and it can be combined with prior probabilities from independent
601 paleoenvironmental proxies into a Bayesian framework (Polly and Head 2015).
602 The second advantage of the likelihood approach is that incommensurable traits can be
603 combined. Mammalian body mass distributions were fairly good predictors of MAT, as
604 might be expected by extrapolating Bergmann's rule, which postulates that subspecies in
605 colder climates will have larger body mass than their conspecifics elsewhere (Bergmann
606 1947; Scholander 1955; Mayr 1963), to the level of species and communities. However,
607 homeothermic mammals are well-insulated from climate and their body size may not be
608 as good predictors of MAT as that of ectotherms (Head *et al.* 2009). Because large
609 ectothermic animals require warm ambient temperatures to sustain their growth rate, the
610 size range of species in hot climates is expected to be greater than in cold climates
611 (Makarieva *et al.* 2005). Using a dataset of ventral scale count as a proxy for size
612 assembled by Lawing *et al.* (2012), we repeated the likelihood estimation for MAT in
613 North America using the range of log scale count and its standard deviation as the
614 dimensions of the ecometric space (**Figure 2F**). These two parameters are both measures
615 of dispersion and are therefore correlated, yet pick out different aspects of the distribution
616 of body size in local communities. These data yield a similar likelihood function for the
617 site in Central America, but with a narrower peak of predicted MAT (**Figure 2G**).
618 Because the likelihood functions are probabilities, they can be combined by multiplying

619 them and renormalizing so that the area under them is 1.0. The resulting function gives
620 the likelihood of MAT given the distribution of body masses in mammals and the
621 distribution of ventral scale counts in snakes. This combined likelihood function provides
622 a better estimate of temperature than either trait does alone (**Figure 2H-J**). The mean
623 anomaly between estimated and real temperature based on the combined estimate is only
624 2.4°C, much better than with mammals alone. Sacrificed is the ability to estimate MAT in
625 the northern part of the continent where the climate is too cold for snakes to live.
626 A fully worked ecometrics example and R code is documented in Appendix I.

627

628

VIII. FUTURE PROSPECTS

629

630 Several aspects of ecometrics need to be addressed with future research. These
631 areas include—intraspecific variation, abundance, phylogenetics, combining multiple
632 ecometrics, conservation, and ecosystem services. Polly *et al.* (2016a) took first steps to
633 identify and define a theory of ecogeography- moving from pattern to process with
634 ecometric modeling. They used modeling to simulate the affects of changing
635 microevolutionary processes on the ecometric patterning seen at the community level. As
636 this area of interest progresses, eventually we hope to be able to observe ecometric
637 patterns and determine which microevolutionary and macroevolutionary processes caused
638 the patterns we see. One area of ecometric study that deserves further study is the affects
639 of intraspecific variation in ecometric patterns. Polly *et al.* (per comm) show that while
640 intraspecific variation, at least in regards to carnivoran calcaneum gear ratios, is high, it
641 does not follow community level ecometric patterning. Models seem to support the idea

642 that this is possible due to the high level of gene flow within populations, but the overall
643 signal at the community level overshadows the intraspecific variation of the populations.

644 Another future development in the field of ecometrics is the prospect of marine
645 ecometrics (Wallin 1991; Yasuhara *et al.* 2015). Due to the depositional environments
646 found in marine systems, marine fossils are the majority of fossils found (Sepkoski
647 1978). Marine fossils are often used in isotopic studies to reconstruct paleoecology
648 (Bowen 1964; Anderson and Arthur 1983; Krantz *et al.* 1987; Wefer and Berger 1991;
649 Rodrigues *et al.* 2014; Huyghe *et al.* 2015; Reich *et al.* 2015). The changes in isotopic
650 fractionation may follow geographical gradients similar to an ecometric (Marchais *et al.*
651 2013; Lynch-Stieglitz *et al.* 2015; Mackenzie *et al.* 2014; Beard *et al.* 2015). However,
652 the isotopic fractionation process is not a morphological trait, it is a metabolic functional
653 trait, and as such, follows different biological, physical, and chemical rules.

654 New advances in remote sensing capabilities could alter the accuracy of our
655 estimates of both species geographic ranges and the environmental condition in which
656 they occur. Remote sensing appears like it will be quite useful when studying changes in
657 plant community structures over large geographic regions. It allows for a level of detail in
658 which single plants are recognizable across regional scales (Jones and Vaughan 2010).

659 Geometric morphometrics will also allow for the study of ecometrics when a
660 particular functional trait changes size across age, but doesn't change shape (or vice
661 versa). New advances will also allow for 3D modeling of functional traits. This may
662 allow for the identification of aspects of the morphology that are better ecometrics than
663 those being used. It can also allow for better ecometrics since we will no longer be using
664 linear or volumetric measurements, but instead use the full 3D shape. Recent work by

665 Polly (2010) and Wilson *et al.* (2012) has shown that this is a viable avenue of future
666 inquiry.

667

668

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967 **Figure 1.** A. Example of an entire leaf margin from a live oak leaf modified from an
968 image by Jeremy Stovall. The leaf margin is entire when its margin is not punctuated. An
969 easy way to determine if the margin is entire or to quantify the entirety of the margin is to
970 overlay the image of the leaf with an oval, as is depicted in the figure with the red outline.
971 Entire leaf margins are characteristic of hotter environments. B. Example of a non-entire
972 leaf margin from a dwarf birch modified from an image by Fox Valley. Non-entire leaf
973 margins are characteristic of cooler environments. C. Example of hypsodonty in a rodent
974 modified by Tapaltsyan *et al.* 2015. Hypsodonty is measured by the crown to root ratio.
975 Hypsodonts are grazers and are characteristic of arid environments with more gritty
976 vegetation. D. Example of brachydonty in a rodent modified from Tapaltsyan *et al.* 2015.
977 Brachydonts are browsers and are found in more wet environments with mixed
978 vegetation. E. Example of a calcaneum from a raccoon modified from an image on
979 boneid.net. Gear ratio is measured on the calcaneum and is the ratio of the length of the
980 sustentacular facet to the total length of the calcaneum. The gear ratio for the raccoon is
981 typical of a plantigrade animal and is characteristic for animals living in high vegetation
982 cover (e.g., dense woodlands). F. Example of a calcaneum from a panther modified from
983 an image on boneid.net. The gear ratio in the panther is typical of a digitigrade animal
984 and is characteristic of animals that are adapted to run through open habitats.

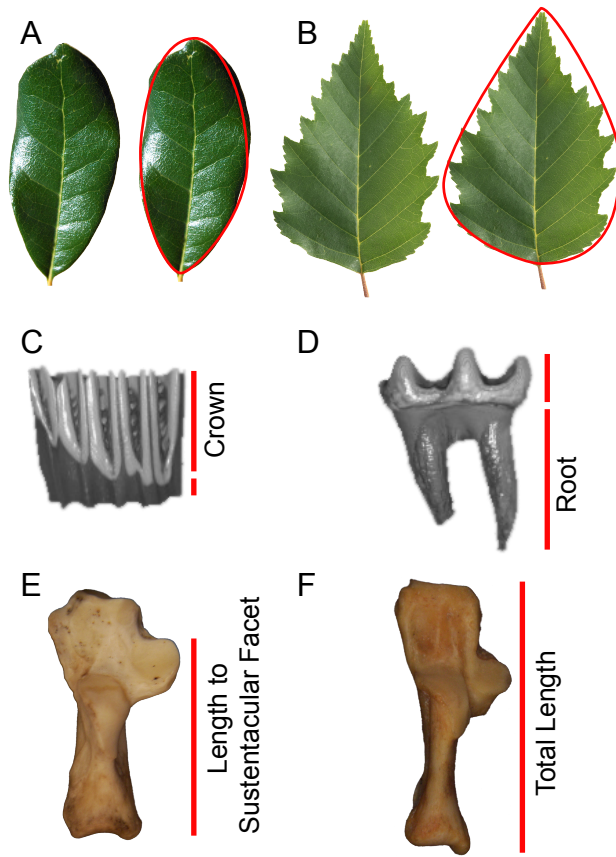
985

986 **Figure 2.** A. Ecometric space for community-level mammalian body mass showing the
987 maximum likelihood estimation of mean annual temperature (MAT) for each bin. B.
988 Likelihood function for MAT based on mammal body mass at the point in Central
989 America highlighted by the black circles in C-E. C. MAT estimated from mammalian

990 body mass. D. Observed MAT. E. anomaly between estimated and observed MAT. F.
991 Ecometric space for snake body size showing the maximum likelihood estimate for MAT
992 in each bin. G. Likelihood function for MAT at the same point in Central America based
993 on snake size. H. MAT estimated from combined mammalian body mass and snake size.
994 I. Observed MAT. E. Anomaly between combined estimate and observed MAT.
995
996

997

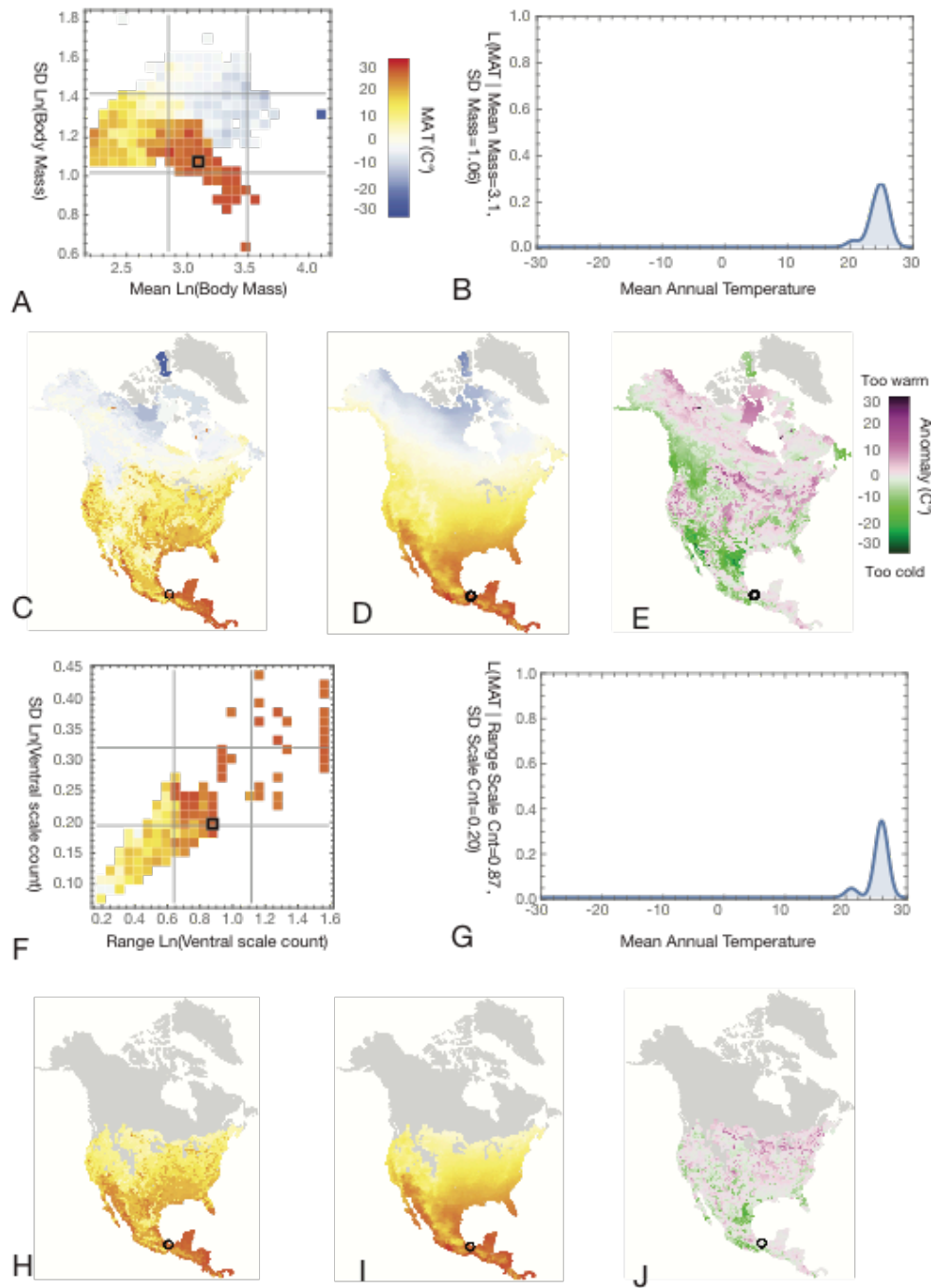
Figure 1



998

999

1000 **Figure 2**



1001
1002

1003

APPENDIX I. ECOMETRICS WORKFLOW AND R CODE

1004

1005

1006 This section demonstrates an econometric modeling workflow using the R Statistical
1007 Programming Language. To demonstrate these models in R, we will work with spatial data.
1008 There are special functions in two packages, *raster* and *sp*, that allow for relatively quick
1009 processing of spatial information (Bivand *et al.* 2015, Hijmans 2015, Pebesma and
1010 Bivand 2005). We will use climate data from the worldclim database (Hijmans *et al.*
1011 2005) and we will use trait data body mass and hypsodonty, from the PanTHERIA
1012 database (Jones *et al.* 2009) and from Eronen *et al.* (2010b). The code below in the gray
1013 boxes can be typed directly into an R console or can be entered into an R script file. The
1014 blue color indicates that the word is a function. The green color indicates that the text is a
1015 character string and the bright blue indicates that the text is recognized as a number. To
1016 start the analysis, load the two required libraries. If they are not installed yet on your
1017 computer, install them with the function `install.packages()`.

```
1018 library(raster)
```

```
1019 ## Loading required package: sp
```

```
1020 library(sp)
```

1021

1022 Load the sampling locations and look at the first six rows of data with the functions
1023 `read.csv()` and `head()`. The first function `read.csv()` is a wrapper for another function
1024 called `read.table()`, which can be used in place of `read.csv()`, if the data are in tab
1025 delimited format. Use the `help()` function to see the documentation associated with each
1026 function.

```
1027 points <- read.csv("data/SamplingPoints.csv")
```

```
1028 head(points)
```

```
1029 ## GLOBALID Longitude Latitude
```

```
1030 ## 1 103148 -42.1727 83.26264
```

```
1031 ## 2 103149 -38.3442 83.26264
```

```
1032 ## 3 103150 -34.5156 83.26264
```

```
1033 ## 4 103151 -30.6871 83.26264
```

```
1034 ## 5 103152 -26.8586 83.26264
```

```
1035 ## 6 103235 -79.4690 82.81348
```

```
1036
```

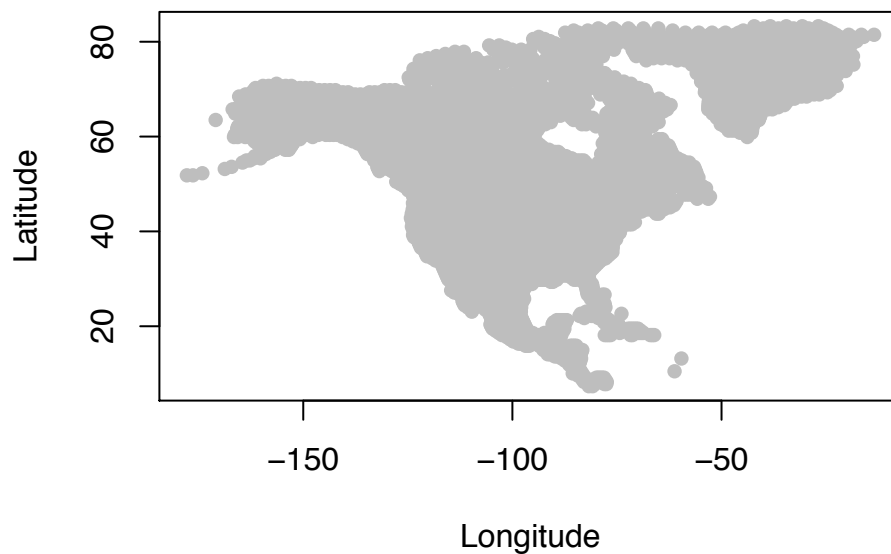
1037 Plot the sampling locations with the function plot() to visualize the geographic

1038 distribution of the sampling locations. In this example, we use 50 km equidistant points

1039 sampled across North America. These are the same points used in Polly (2010).

```
1040 plot(points[,2:3], col = "gray", pch = 16)
```

```
1041
```



```
1042
```

1043 Download raster climate data from the worldclim database using the `getData()` function
1044 from the package `raster` that we loaded with the `library()` function (Hijmans *et al.* 2005,
1045 Hijmans 2015). In this example, we download the 10 minute resolution, but if you would
1046 like to try a higher resolution data set, then change the argument named `res` to 2.5 or 0.5.
1047 Extract the temperature and precipitation for each sampling location using the `extract()`
1048 function.

```
1049 bioclim <- getData("worldclim", download = T, path = "data", var = "bio", res = 10)
```

1050

1051 Extract the temperature for each sampling location.

```
1052 temperature <- extract(bioclim[[1]], points[,2:3])
```

1053

1054 Calculate the temperature range for all the sampling localities to make a plot of the
1055 temperature. We add one to the range to make the range equal to index values that we can
1056 use to subset the color function. The R language starts the subset of data at an index value
1057 of 1. Calculate the color value associated with each temperature value and the
1058 temperature values associated with even breaks to assign legend values.

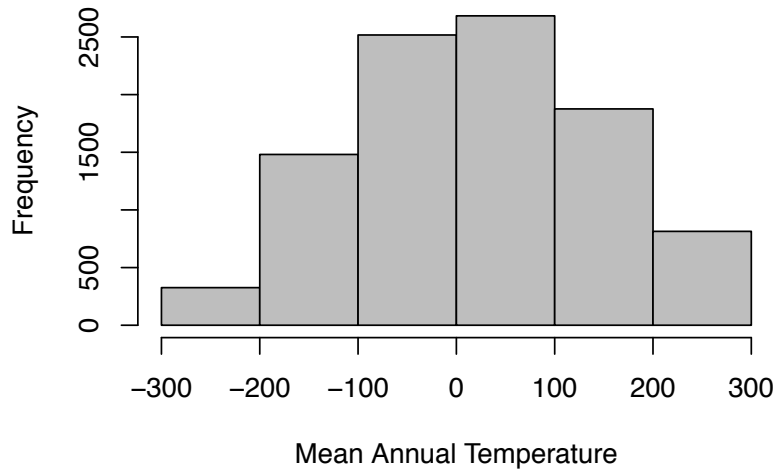
```
1059 temp_range <- 1 + max(temperature, na.rm = T) - min(temperature, na.rm = T)
```

```
1060 colfunc_temp <- colorRampPalette(c("darkblue", "blue", "gray", "yellow",
```

```
1061 "red"))(temp_range)[1 + temperature - min(temperature, na.rm = T)]
```

```
1062 h <- hist(temperature, main = "", xlab = "Mean Annual Temperature", col = "gray",
```

```
1063 breaks = 5)
```



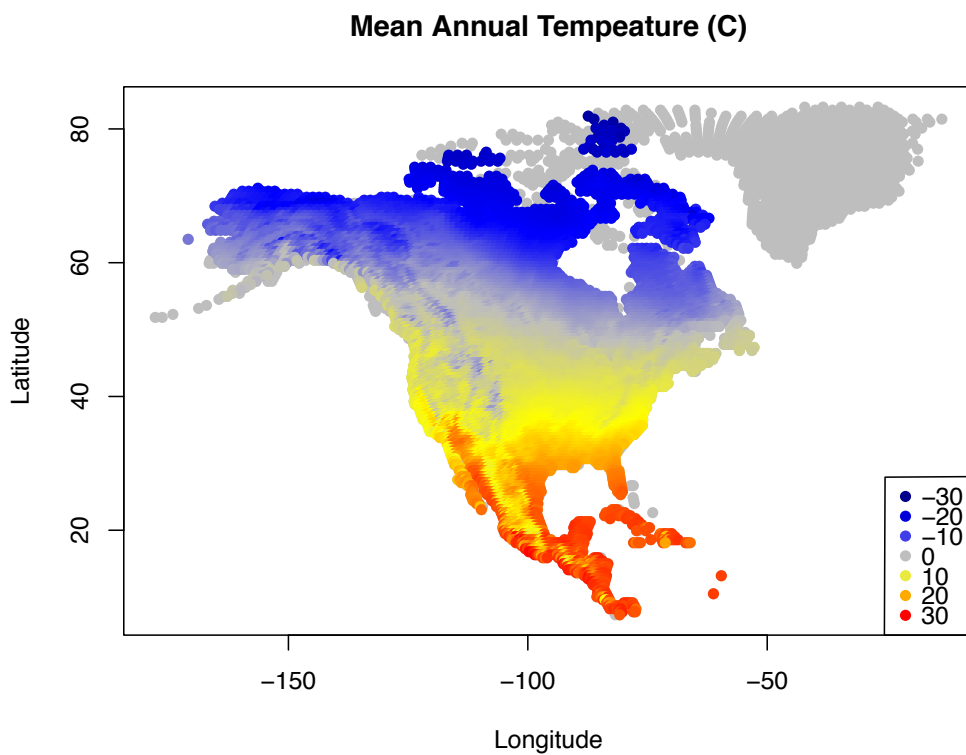
1064

1065 `plot(points[,2:3], col = colfunc_temp, pch = 16, main = "Mean Annual Temperature (C)")`

1066 `legend("bottomright", legend = h$breaks/10, pch = 16, col =`

1067 `colorRampPalette(c("darkblue", "blue", "gray", "yellow", "red"))(length(h$breaks)))`

1068



1069

1070 Extract the precipitation for each sampling locality.

```
1071 precipitation <- extract(bioclim[[12]], points[,2:3])
```

1072

1073 Calculate the precipitation range for all the sampling localities to make a plot of the

1074 precipitation. Also, calculate color value associated with each precipitation value and the

1075 precipitation values associated with even breaks to assign legend values.

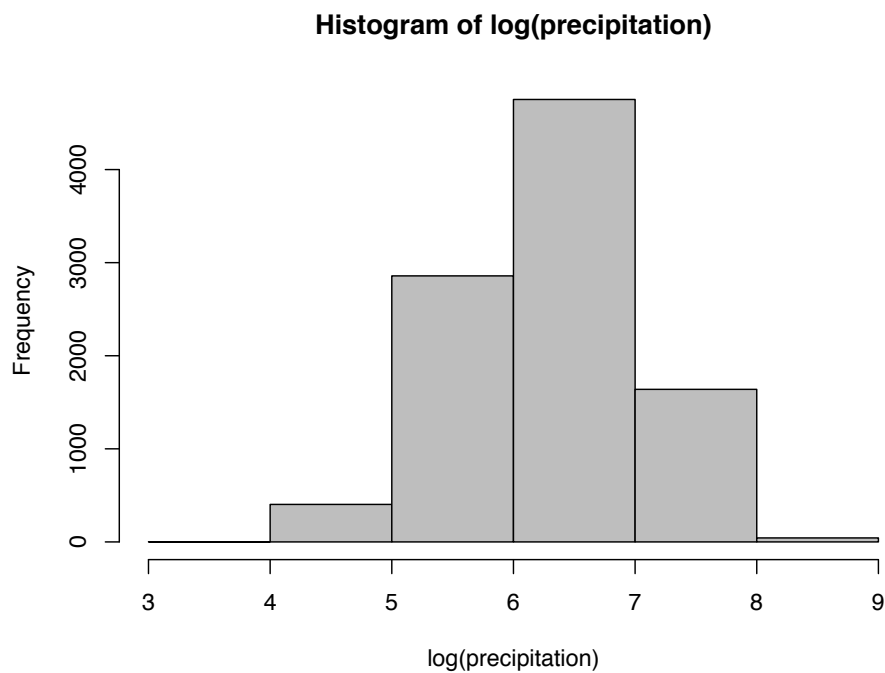
```
1076 precip_range <- 1 + max(log(precipitation), na.rm = T) - min(log(precipitation), na.rm =  
1077 T)
```

```
1078 colfunc_pr <- colorRampPalette(c("brown", "green"))(precip_range)[1 +
```

```
1079 log(precipitation) - min(log(precipitation), na.rm = T)]
```

```
1080 h <- hist(log(precipitation), breaks = 5, col = "gray")
```

1081

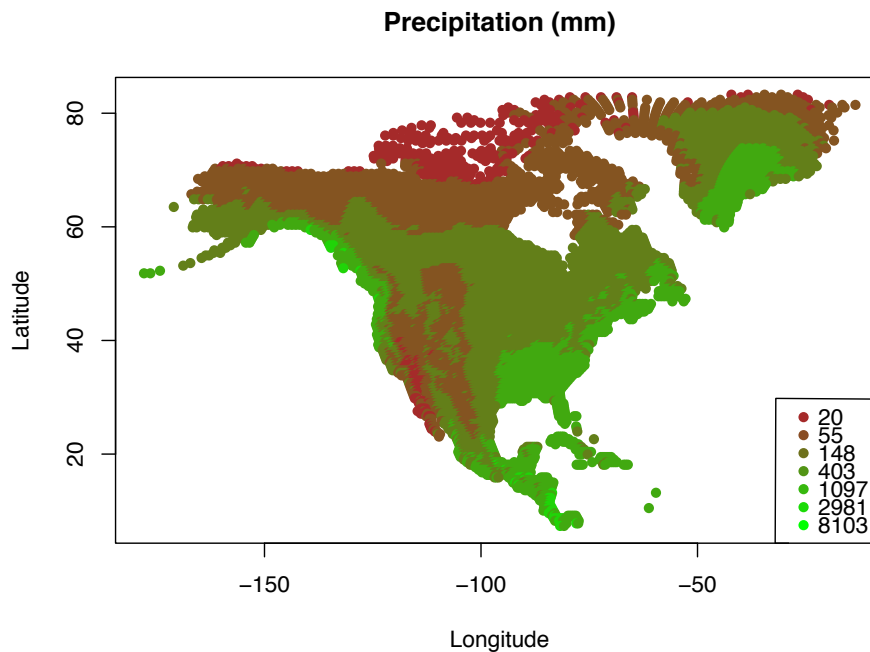


1082

```

1083 plot(points[,2:3], col = colfunc_pr, pch = 16, main = "Precipitation (mm)")
1084 legend(-36.25, 60.5, legend = round(exp(h$breaks)), pch = 16, col =
1085 colorRampPalette(c("brown", "green"))(length(h$breaks)))
1086

```



```

1087
1088 Compile the climate variables into a new data.frame called climate. Remove the variables
1089 that are taking up memory with the rm() function if your memory is getting sluggish.

```

```

1090 climate <- cbind(points, temperature, precipitation)
1091 #rm(bioclim, temperature, precipitation, points)

```

```

1092
1093 Visually check the climate variables for normality and if they are not mostly normally
1094 distributed, transform them for normality.

```

```

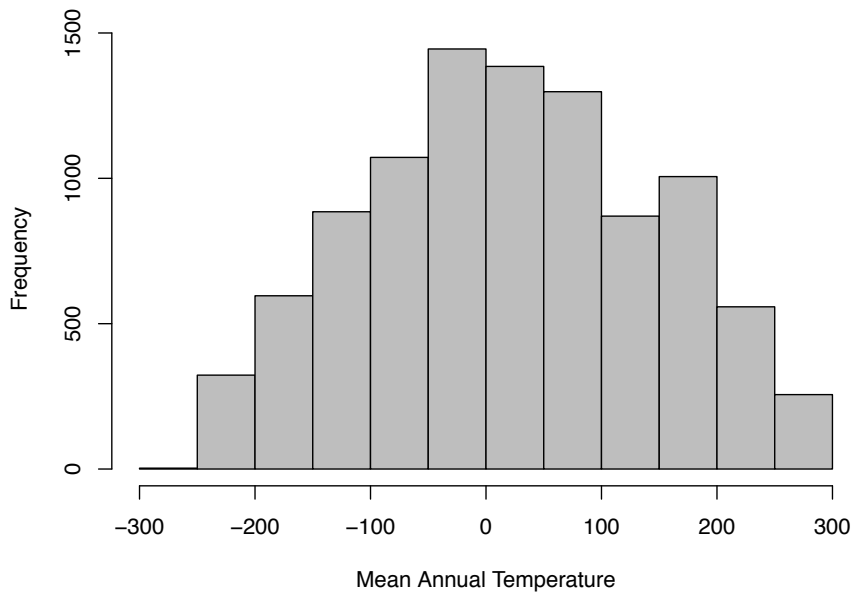
1095 head(climate)

```

```

1096 ## GLOBALID Longitude Latitude temperature precipitation
1097 ## 1 103148 -42.1727 83.26264 -169 139
1098 ## 2 103149 -38.3442 83.26264 -170 141
1099 ## 3 103150 -34.5156 83.26264 -175 149
1100 ## 4 103151 -30.6871 83.26264 -185 166
1101 ## 5 103152 -26.8586 83.26264 -180 139
1102 ## 6 103235 -79.4690 82.81348 -207 90
1103
1104 hist(climate[,4], main = "", xlab = "Mean Annual Temperature", col = "gray")
1105

```

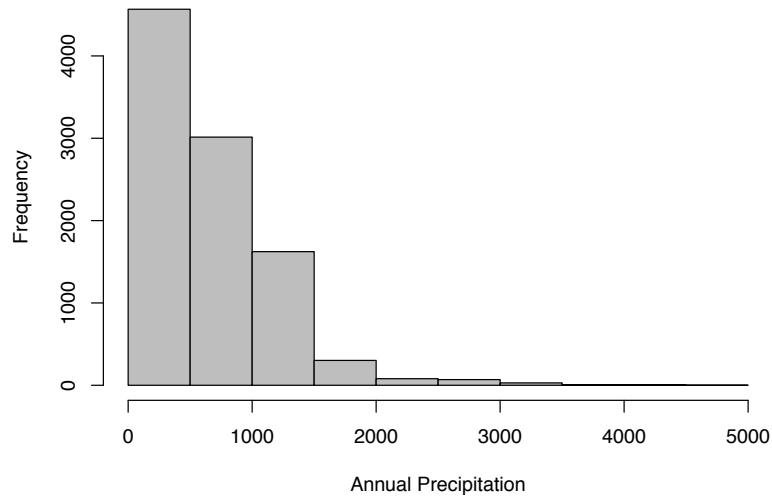


```

1106
1107
1108 Temperature appears to be mostly normally distributed, so now we check precipitation.
1109

```

```
1110 hist(climate[,5], main = "", xlab = "Annual Precipitation", col = "gray")
```



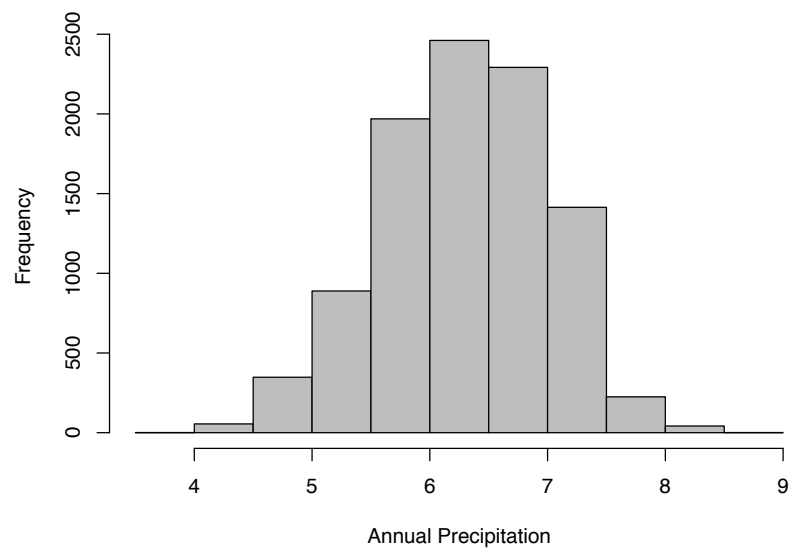
```
1111
```

```
1112 Precipitation appears to be log distributed. We log transform this variable to get it closer
```

```
1113 to normality.
```

```
1114 climate[,5] <- log(climate[,5])
```

```
1115 hist(climate[,5], main = "", xlab = "Annual Precipitation", col = "gray")
```



```
1116
```


1117 Next, we read in the trait data from a folder called data. We assign the row names of the
1118 new data frame to the names of the taxon within the dataset. We look at the first six rows
1119 of the trait data frame with the head() function. The two traits that we use in this example
1120 are body mass and hypsodonty index. Body mass is reported in grams and is the mass of
1121 any adult reported in the PanTHERIA database (Jones *et al.* 2009) from live or freshly-
1122 killed specimens. These include captive, wild, provisioned, or unspecified populations
1123 and include male, female, and sex unspecified individuals. The mean for each species is
1124 reported for each species. The second trait that we use is an index for hypsodonty from
1125 Eronen *et al.* (2010b).

```
1126 traits <- read.csv("data/NAmammalTraits.csv")
1127 rownames(traits) <- traits$TaxonName
1128 head(traits)
1129 ##           TaxonName BodyMass hypsodonty_index
1130 ## Didelphis virginiana Didelphis virginiana 3.387760      1
1131 ## Aplodontia rufa      Aplodontia rufa 2.906448      3
1132 ## Sciurus carolinensis Sciurus carolinensis 2.736715      1
1133 ## Sciurus griseus     Sciurus griseus 2.847480      1
1134 ## Sciurus niger       Sciurus niger   NA      1
1135 ## Tamiasciurus douglasii Tamiasciurus douglasii 2.352183      1
```

1136

1137 Now we read in shapefiles containing polygons that represent the geographic ranges for
1138 all of the species of interest. These specific shape files were obtained from IUCN Redlist

1139 using their spatial data download option (www.iucnredlist.org). If you are dealing with
1140 large shapefiles, then this step will take a reasonable amount of processing time.

```
1141 geography <-  
1142 shapefile("data/TERRESTRIAL_MAMMALS/TERRESTRIAL_MAMMALS.shp")  
1143
```

1144 Next we create a list of species at each sampling locality by first turning the sampling
1145 points into spatial points with the function `SpatialPoints()`. We assign the coordinate
1146 reference system of our spatial points to a `proj4string` to match the coordinate reference
1147 system of the spatial polygons representing the geographic ranges. We then create a list
1148 with the function `over()`. If you are dealing with large shapefiles, keep in mind that the
1149 `over()` function will take a reasonable amount of time to process.

```
1150 sp <- SpatialPoints(climate[,2:3], proj4string = CRS(proj4string(geography)))  
1151 o <- over(sp, geography, returnList = T)  
1152
```

1153 The sample size at each site is calculated by determining the length of the vector returned
1154 for each site. The ecometric for body mass and hypsodonty index are summarized for the
1155 community level distribution. Here, we summarize with the mean.

```
1156 richness <- unlist(lapply(o, function(x) length(traits[x$binomial,"hypsodonty_index"])))  
1157 ecometric_bodymass <- unlist(lapply(o, function(x)  
1158 mean(traits[x$binomial,"BodyMass"], na.rm = T)))  
1159 ecometric_hypsodonty <- unlist(lapply(o, function(x)  
1160 mean(traits[x$binomial,"hypsodonty_index"], na.rm = T)))  
1161
```

1162 **FIRST APPROXIMATION WITH TRANSFER FUNCTION**

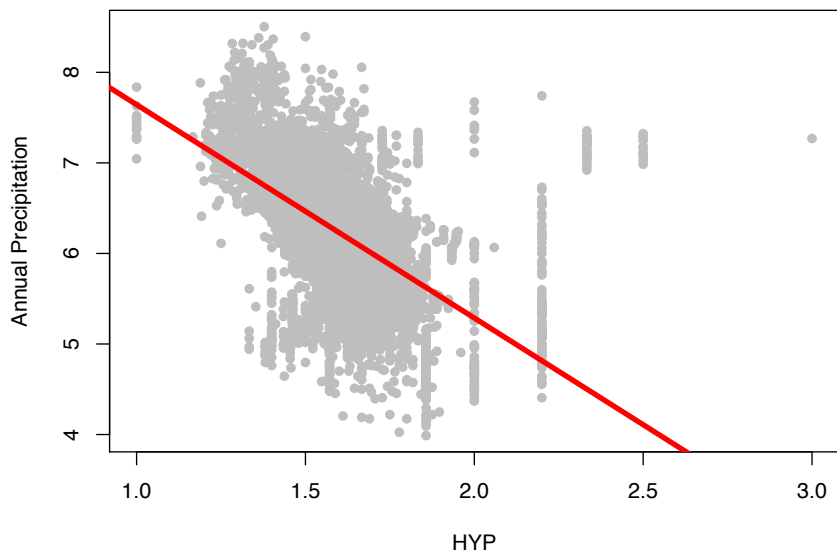
1163 Now we create a model describing the relationship between traits and climate. First we
1164 consider the relationship between hypsodonty and precipitation. We build a simple linear
1165 model to describe the variation in precipitation due to the variation in hypsodonty using
1166 the function `lm()`. We only use sites that we have data for more than five species. We
1167 look at a summary of the model using the function `summary()`. Both the intercept and the
1168 coefficient (here the coefficient represents the slope of the linear relationship) are not
1169 zero ($p < 0.001$). The amount of explained variation (R^2) is 30%. We then make a
1170 scatterplot of those variables to look at the general spread of data and add the linear
1171 model with the function `abline()`.

```
1172 model_hyp <- lm(climate[richness > 5,5] ~ ecometric_hypsodonty[richness > 5])
1173 summary(model_hyp)
1174 ## Call:
1175 ## lm(formula = climate[richness > 5, 5] ~ ecometric_hypsodonty[richness > 5])
1176 ## Residuals:
1177 ##   Min    1Q  Median    3Q   Max
1178 ## -1.9984 -0.3348 -0.0163  0.3821  4.3388
1179 ## Coefficients:
1180 ##
1181 ## (Intercept)          9.99886  0.06160 162.3 <2e-16
1182 ## ecometric_hypsodonty[richness > 5] -2.35602  0.03869 -60.9 <2e-16
1183 ## (Intercept)          ***
1184 ## ecometric_hypsodonty[richness > 5] ***
```

```

1185 ## ---
1186 ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
1187 ## Residual standard error: 0.5834 on 8651 degrees of freedom
1188 ## (15 observations deleted due to missingness)
1189 ## Multiple R-squared: 0.3001, Adjusted R-squared: 0.3
1190 ## F-statistic: 3709 on 1 and 8651 DF, p-value: < 2.2e-16
1191 plot(ecometric_hypsodonty[richness > 5], climate[richness > 5,5], xlab = "HYP", ylab =
1192 "Annual Precipitation", pch = 16, col = "gray")
1193 abline(model_hyp, col = "red", lwd = 4)
1194

```



1195

1196 From this model, we can see there is some predictive power in this transfer function, but

1197 the linear model does not capture the relationship well. In the next section we will show

1198 how to estimate annual precipitation from hypsodonty with a maximum likelihood

1199 approach that better captures the relationship between annual precipitation and

1200 hypsodonty.

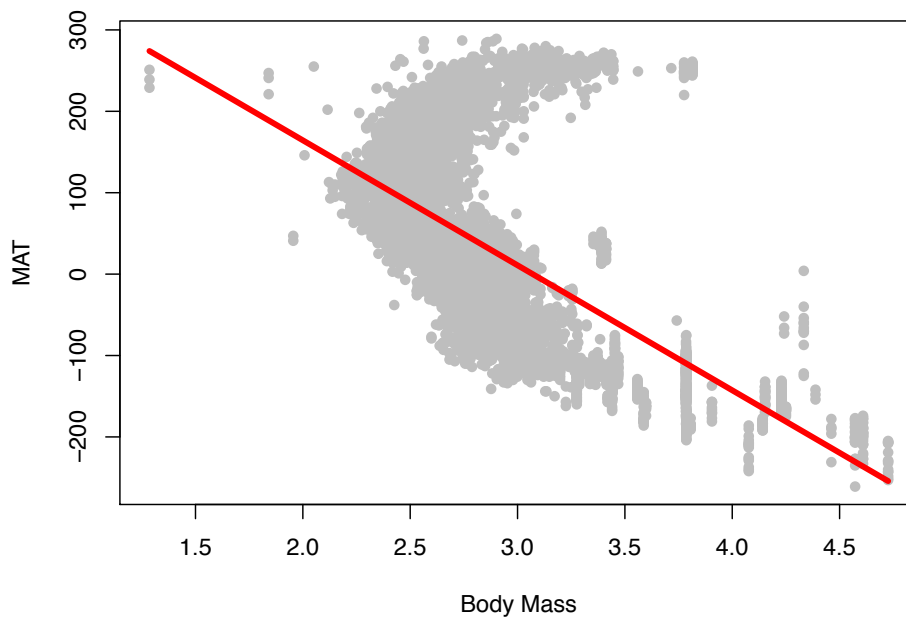
1201 Now we create a model describing the relationship between the body mass and
1202 temperature. We build a linear model to describe the variation in body mass due to the
1203 variation in temperature using the function `lm()`. We look at a summary of the model
1204 using the function `summary()`. Both the intercept and all the coefficients are significantly
1205 different from zero ($p < 0.001$). The amount of explained variation (R^2) is approximately
1206 34%. We then make a scatterplot of those variables to look at the general spread of data
1207 and add the model with the function curve().

```
1208 model_mass <- lm(climate[richness > 5,4] ~ ecometric_bodymass[richness > 5])
1209 summary(model_mass)
1210 ## Call:
1211 ## lm(formula = climate[richness > 5, 4] ~ ecometric_bodymass[richness > 5])
1212 ## Residuals:
1213 ##   Min     1Q   Median     3Q    Max
1214 ## -170.72  -65.22  -24.73   43.71  375.19
1215 ## Coefficients:
1216 ##              Estimate Std. Error t value Pr(>|t|)
1217 ## (Intercept)          471.512     6.571   71.76 <2e-16 ***
1218 ## ecometric_bodymass[richness > 5] -153.559     2.304  -66.64 <2e-16 ***
1219 ## ---
1220 ## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
1221 ## Residual standard error: 92.6 on 8651 degrees of freedom
1222 ## (15 observations deleted due to missingness)
```

```

1223 ## Multiple R-squared: 0.3392, Adjusted R-squared: 0.3391
1224 ## F-statistic: 4440 on 1 and 8651 DF, p-value: < 2.2e-16
1225 plot(ecometric_bodymass[richness > 5], climate[richness > 5,4], ylab = "MAT", xlab =
1226 "Body Mass", pch = 16, col = "gray")
1227 curve(model_mass$coefficients[1] + model_mass$coefficients[2] * x, col = "red", lwd =
1228 4, add = T)
1229

```



1230

1231 From this model, we can see that, again, there is some predictive power in this transfer

1232 function, but the linear model does not capture the relationship well. In the next section

1233 we will show how to estimate mean annual temperature from body mass with a maximum

1234 likelihood approach that better captures the relationship between the two.

1235 The coefficients that were estimated in both of these models can be used to estimate

1236 paleotemperature and precipitation. Confidence limits can also be calculated given the

1237 input dataset. It is important to note that the size of the confidence limits will vary with

1238 climate. For example, between 5 C and 28 C, there is a stronger relationship with body
1239 size than below or above those temperatures. Hypsodonty has high variability throughout
1240 the precipitation range present in North America; however, there is a central tendency
1241 about the average relationship between precipitation and hypsodonty index that is useful
1242 in reconstructing paleoprecipitation with confidence limits.

1243

1244 **MAXIMUM LIKELIHOOD ESTIMATION**

1245 Although transfer functions, while easy to apply and adequate for first approximations,
1246 assume a fairly simple relationship one-to-one relationship between environment and trait
1247 means. Combining different traits that have functional relationships with the same
1248 environmental factor is also awkward with conventional regression-based transfer
1249 functions, especially if the traits are fundamentally different in kind or scale (e.g., body
1250 mass measured in kg and humerus shape measured in Procrustes units).

1251 An alternative strategy is to estimate the likelihood of environmental parameters given
1252 the distribution of traits in a community (Lawing *et al.* 2012; Polly and Head 2015). This
1253 approach, like many likelihood or Bayesian methods, requires far fewer assumptions
1254 about the statistical distributions of variables and it allows otherwise incommensurable
1255 data to be combined into the same estimate.

1256 To begin, we need to create another variable at the community level, namely the standard
1257 deviation, to use in the maximum likelihood estimate of temperature.

```
1258 sd_ecometric_bodymass <- unlist(lapply(o, function(x)
```

```
1259 sd(traits[x$binomial,"BodyMass"], na.rm = T)))
```

1260

1261 We create bins using the body mass variable and extract the break points for each bin.

```
1262 #bin the community level trait distribution into 25X25
1263 #first take the range of each
1264 mtemp <- range(ecometric_bodymass, na.rm = T)
1265 sdtemp <- range(sd_ecometric_bodymass, na.rm = T)
1266 #get the break points for the mean and sd
1267 mbrks <- seq(mtemp[1], mtemp[2], diff(mtemp)/25)
1268 sdbrcs <- seq(sdtemp[1], sdtemp[2], diff(sdtemp)/25)
1269 #assign bin codes for each
1270 mbc <- .bincode(ecometric_bodymass, breaks = mbrks)
1271 sdbc <- .bincode(sd_ecometric_bodymass, breaks = sdbrcs)
```

1272

1273 We calculate the temperature for each bin.

```
1274 #calculate the data for the raster
1275 obj <- array(NA,dim = c(25,25))
1276 for(i in 1:25){
1277   for(j in 1:25){
1278     dat <- round(temperature[which(mbc==i & sdbc==j)]/10)
1279     obj[26 - j,i] <- mean(dat, na.rm = T)
1280   }
1281 }
```

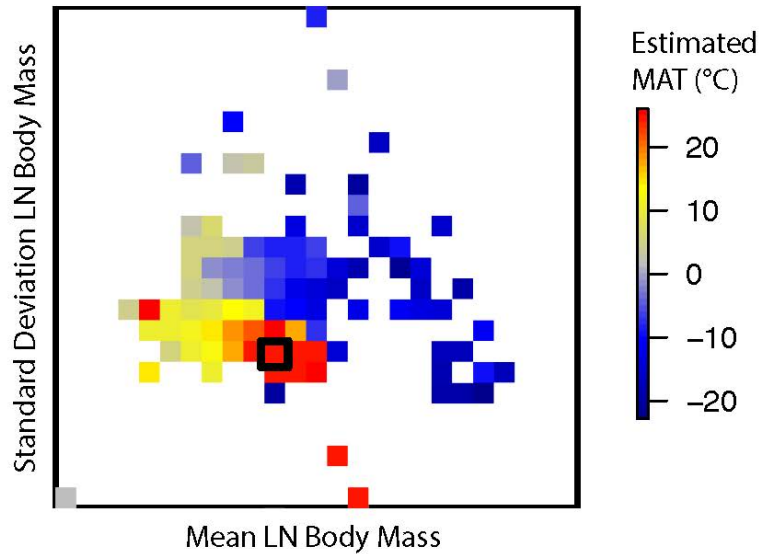
1282

1283 Next, we create a raster to store the body mass and temperature data for bins.


```

1284 #make a raster
1285 r <- raster(extent(0,25,0,25), resolution = 1)
1286 #set the values to the obj
1287 r <- setValues(r,obj)
1288
1289 Plot the raster and highlight the bin that we will use to extract data to show an example of
1290 that maximum likelihood estimate.
1291 #make an empty plot
1292 plot(1:25, 1:25, type = "n", xlim = c(1,25), ylim = c(1,25),
1293      xaxs = "i", yaxs = "i", asp = 1, axes = F, xlab = "", ylab = "")
1294 #add the rectangle/box
1295 rect(0, 1, 25, 25, lwd = 3)
1296 #add the raster data
1297 plot(r, col = colorRampPalette(c("darkblue", "blue",
1298   "grey", "yellow", "red"))(round(maxValue(r) -
1299   minValue(r))), add = T)
1300 #this is mean = 3.1, 12, and sd = 1.08, 10
1301 rect(11, 9, 12, 10, lwd = 4)

```



1302

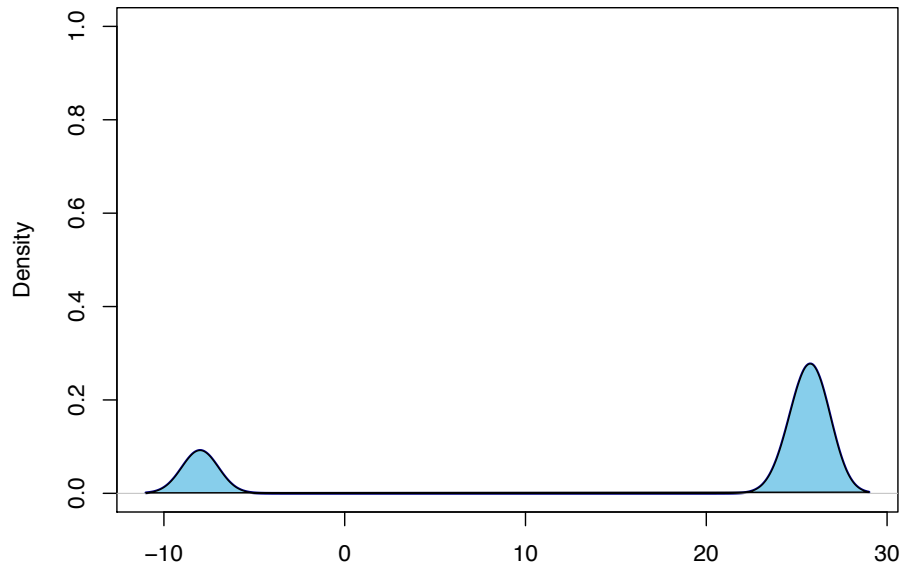
1303 The colors in this raster plot show the Mean Annual Temperature maximum likelihood
 1304 estimate given the associated mean and standard deviation of each bin.

1305 We extract the data for the highlighted bin and plot the kernel density with a Gaussian
 1306 kernel. This shows the distribution of the likelihood surface.

```

1307 #grab all the data for that box
1308 dat <- round(temperature[which(mbc==12 & sdbc==10)]/10)
1309 #plot the kernel density with gaussian kernel, bandwidth = 1
1310 mod <- density(dat, bw = 1)
1311 plot(mod, ylim = c(0,1), col = "darkblue", lwd = 2)
1312 polygon(mod$x, mod$y, col = "skyblue")

```



N = 13 Bandwidth = 1

1313

1314 This likelihood surface shows a bimodal distribution of the most likely temperature.

1315 Although it is bimodal, it is much more likely that the temperature falls on the warm end
 1316 of the spectrum, as opposed to the cold end.

1317 Next, we calculate the maximum likelihood for all bins.

```

1318 modmax <- array(NA, dim = length(points[,1]))
1319 mod <- list()
1320 for(i in 1:length(points[,1])){
1321   if(!(is.na(mbc[i]) | is.na(sdbc[i]))){
1322     dat <- round(temperature[which(mbc==mbc[i] & sdbc==sdbc[i])]/10)
1323     mod[[i]] <- density(dat, bw = 1)
1324     modmax[i] <- mod[[i]]$x[which.max(mod[[i]]$y)]
1325   }}
1326 modmax <- round(modmax*10)

```

1327 We only use bins with more than the number of species specified as the cutoff. Here we
1328 use seven. This means that there needs to be at least seven species recorded at each
1329 location to be included in the estimate.

```
1330 cutoff <- 7
```

1331

1332 To plot the maximum likelihood temperature estimate from the econometric values, we
1333 create a color palette for the temperature estimates. In addition, we save the histogram
1334 with five break points to a variable to use in plotting.

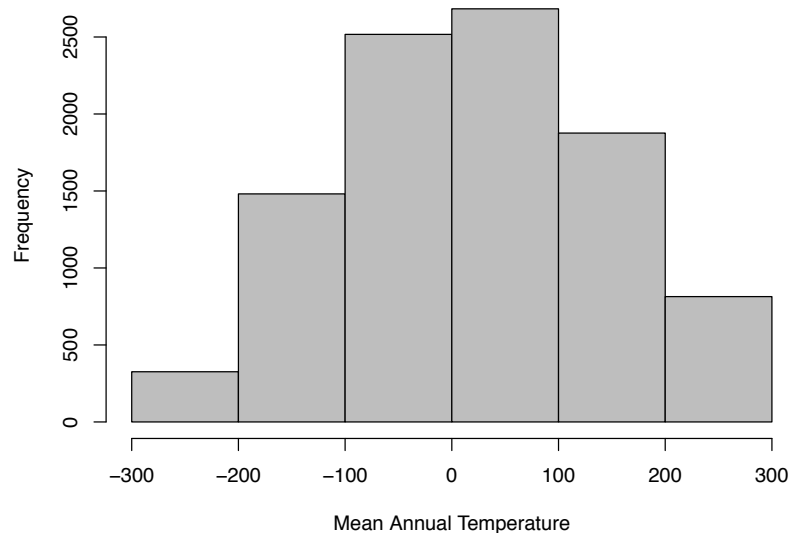
```
1335 colfunc_eco <- colorRampPalette(c("darkblue", "blue", "gray", "yellow",
```

```
1336 "red"))(temp_range)[1 + modmax - min(modmax, na.rm = T)]
```

```
1337 h <- hist(temperature, main = "", xlab = "Mean Annual Temperature", col = "gray",
```

```
1338 breaks = 5)
```

1339



1340

1341

1342 We plot the maximum likelihood temperature estimate from body mass.

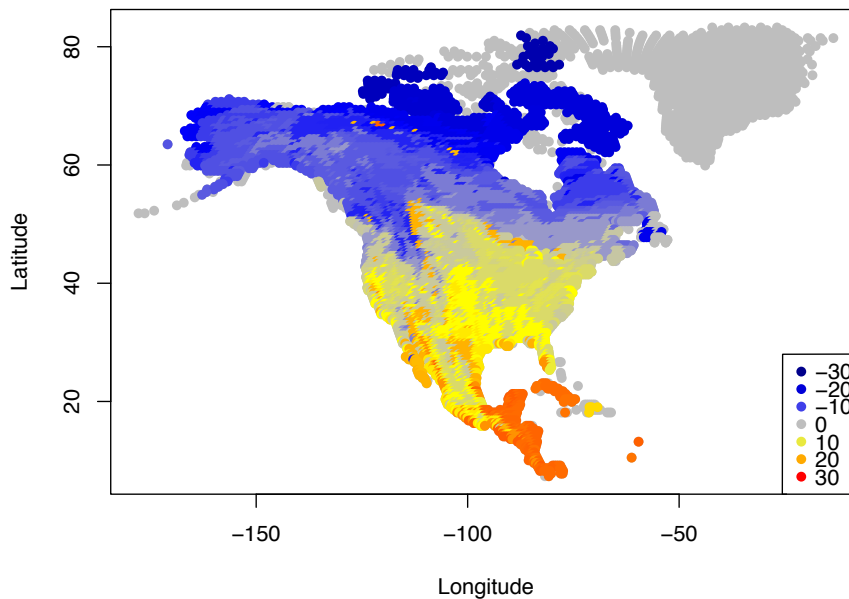
```
1343 plot(points[,2:3], col = "gray", pch = 16)
```

```
1344 points(points[richness > cutoff, 2:3], col = colfunc_eco[richness > cutoff], pch = 16)
```

```
1345 legend(-31.5, 61, legend = h$breaks/10, pch = 16, col = colorRampPalette(c("darkblue",
```

```
1346 "blue", "gray", "yellow", "red"))(length(h$breaks)))
```

1347



1348

1349 Next we plot the actual temperature to compare with the estimated temperature.

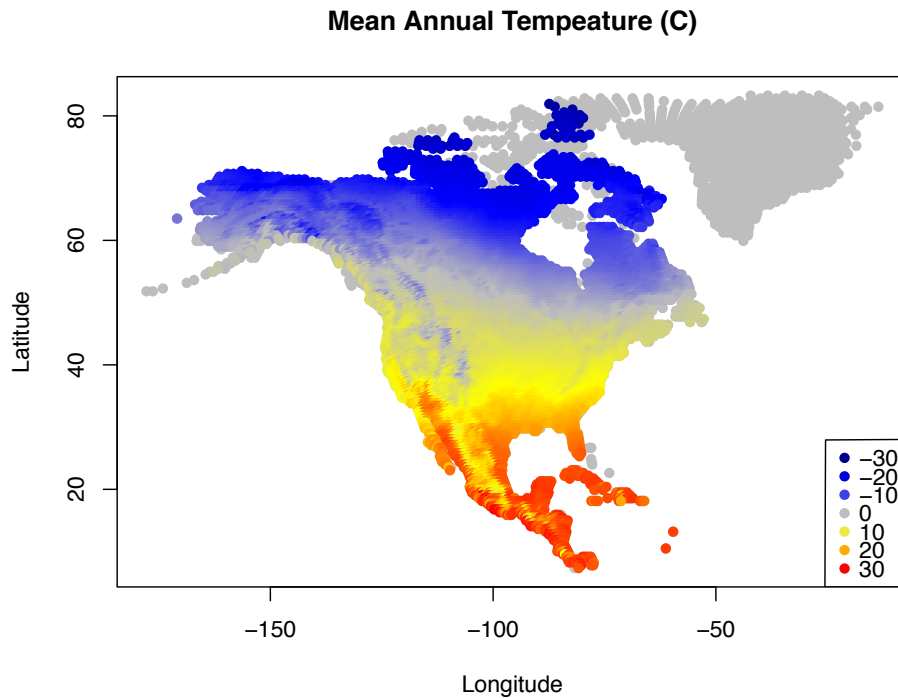
```
1350 plot(points[,2:3], col = "gray", pch = 16, main = "Mean Annual Temperature (C)")
```

```
1351 points(points[richness > cutoff,2:3], col = colfunc_temp[richness > cutoff], pch = 16)
```

```
1352 legend(-31.5, 61, legend = h$breaks/10, pch = 16, col = colorRampPalette(c("darkblue",
```

```
1353 "blue", "gray", "yellow", "red"))(length(h$breaks)))
```

1354



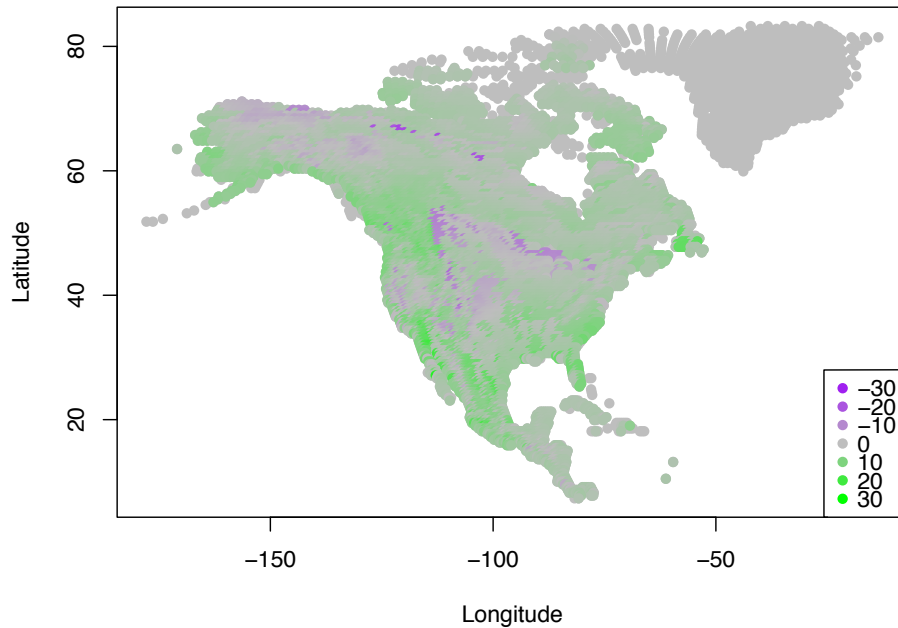
1355

1356 We plot the anomaly to visualize the difference between the estimated and actual Mean
 1357 annual Temperature.

```

1358 plot(points[,2:3], col = "gray", pch = 16)
1359 anom <- temperature - modmax
1360 colfunc_anom <- colorRampPalette(c("purple", "grey", "green"))(max(anom, na.rm =
1361 T) - min(anom, na.rm = T))[1 + anom - min(anom, na.rm = T)]
1362 points(points[richness > cutoff, 2:3], col = colfunc_anom[richness > cutoff], pch = 16)
1363 legend(-31.5, 61, legend = h$breaks/10, pch = 16, col = colorRampPalette(c("purple",
1364 "grey", "green"))(length(h$breaks)))
1365

```



1366

1367 The anomaly between the estimated Mean Annual Temperature and the actual Mean
 1368 Annual Temperature shows that most of the temperature estimates are less than one
 1369 degree C.

1370

1371

APPENDIX I. REFERENCES

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