



Full Length Article

Stokes and anti-Stokes luminescence from cubic elpasolite Cs₂NaYF₆ crystals doped with Er³⁺ and Yb³⁺ ionsP.A. Loiko^{a,*}, N.M. Khaidukov^b, J. Méndez-Ramos^c, E.V. Vilejshikova^a, N.A. Skoptsov^a, K.V. Yumashev^a^a Center for Optical Materials and Technologies (COMT), Belarusian National Technical University, 65/17 Nezavisimosti Ave., Minsk 220013, Belarus^b N.S. Kurnakov Institute of General and Inorganic Chemistry, 31 Leninskii Prospekt, Moscow 119991, Russia^c Departamento de Física, Universidad de La Laguna, Tenerife, 38206 La Laguna, Spain

ARTICLE INFO

Article history:

Received 29 October 2015

Received in revised form

31 January 2016

Accepted 22 February 2016

Available online 15 March 2016

Keywords:

Elpasolite crystals

Erbium

Ytterbium

Luminescence

Up-conversion

ABSTRACT

Er³⁺ and Yb³⁺ doped cubic elpasolite Cs₂NaYF₆ crystals including stoichiometric compositions Cs₂NaErF₆ and Cs₂NaYbF₆ have been synthesized under hydrothermal conditions. Absorption, stimulated-emission and gain cross-sections spectra have been determined for the ²F_{5/2}→²F_{7/2} (Yb³⁺) and ⁴I_{13/2}→⁴I_{15/2} (Er³⁺) transitions at room-temperature. The maximum σ_{SE} values are 1.8 × 10⁻²¹ cm² at 993 nm (Yb³⁺) and 3.8 × 10⁻²¹ cm² at 1535 nm (Er³⁺). Elpasolite crystals provide exceptionally long radiative lifetimes of the excited-states for both ions, namely τ(²F_{5/2})=6.3 ms and τ(⁴I_{13/2}) ~ 32 ms for 10 at% Yb³⁺:Cs₂NaYF₆ and 10 at% Er³⁺:Cs₂NaYF₆ which can be used in high pulse energy Q-switched lasers. Up-conversion luminescence has been studied for Er³⁺ doped and Er³⁺, Yb³⁺ codoped Cs₂NaYF₆ crystals.

© 2016 Elsevier B.V. All rights reserved.

1. Introduction

Halide compounds having the elpasolite structure can be described by a general formula A₂BMX₆ where A and B are monovalent alkali ions provided that the ionic radius of A is greater than that of B, M stands for trivalent metal ions, which can be Al, Sc, transition elements and rare earth elements, and X is a halogen [1]. The elpasolite compounds crystallize in the face-centered cubic space group Fm3m [2] and can be described as double perovskites. In the structure the A alkali cations are located in the cuboctahedral sites whereas the B alkali cations and the M trivalent metal ions regularly alternate along the unit cell axes in octahedral sites. Accordingly, the MX₆ octahedra are perfectly cubic with O_h site symmetry for trivalent metal ions, while the MX₆ octahedra do not share halide ions with each other, i.e. the elpasolite structure is characterized by the isolated MX₆ octahedra. In addition, as all the halide compounds, elpasolites are materials with low-phonon energy.

The above mentioned peculiarities of elpasolite hosts lead to a significant reduction of the multiphonon relaxation rates for optically active rare earth (RE) ion dopants, which allows for an increased lifetime of some excited levels that can relax radiatively

or can store energy for further up-conversion and cross-relaxation as well as provide relatively low concentration quenching of luminescence, which allows obtaining efficient luminescence in A₂BMX₆ containing high trivalent RE ion concentrations up to 100 at%.

To date, some spectroscopy data for several RE ions (Er³⁺, Yb³⁺, Tm³⁺, Eu³⁺) doped into the Cs₂NaYF₆ compound have been published; however, characterization of these materials is far from completeness mainly due to the difficulty of synthesizing optical quality crystals of elpasolites in general and Cs₂NaYF₆ in particular. For example, VUV 5d–4f luminescence of Er³⁺ ions, including a stoichiometric Cs₂NaErF₆ compound, has been studied followed by crystal field calculations for Er³⁺ ions [3,4]. Near-IR (~2.7 μm) emission of Er³⁺ ions in Cs₂NaYF₆ has been also investigated and the lifetime of the ⁴I_{11/2} excited-state has been detected to be as long as ~1 ms at room-temperature for highly-doped (> 10 at%) samples [5]. Absorption and emission as well as crystal field analysis for Yb³⁺ ions in Cs₂NaYbF₆ has been reported [6–8]. In particular, very long lifetime of the Yb³⁺ excited-state, τ(²F_{5/2})=5.63 ms, at room-temperature is observed for Cs₂NaYbF₆. Some spectroscopic peculiarities of Tm³⁺ ions in Cs₂NaYF₆ have been also studied [3,6,9] and crystal field calculations for a Tm:Cs₂NaYF₆ crystal have been performed [10]. The spectroscopic properties of Eu³⁺ and Tb³⁺ ions doped into Cs₂NaYF₆ have been investigated as well [11–13].

* Corresponding author.

E-mail address: kinetic@tut.by (P.A. Loiko).

The fluoride cubic elpasolite Cs_2NaYF_6 is isostructural with the chloride elpasolite $\text{Cs}_2\text{NaYCl}_6$, that has been extensively studied as an low phonon energy host for optically active ions of 3d, 4f and 5f elements, for example Er^{3+} [14,15]. In particular, $\text{Cs}_2\text{NaYCl}_6$ crystals doubly doped with Er^{3+} and Yb^{3+} have been studied as the near-IR-to-visible frequency converters [16,17] based on photon up-conversion processes [18]. As a result of upconversion mechanisms, Er^{3+} - Yb^{3+} ion pairs can convert near-IR ($\sim 1 \mu\text{m}$) emission of InGaAs laser diodes to green and red light. On the other hand, Cs_2NaYF_6 is harder and less moisture-sensitive than $\text{Cs}_2\text{NaYCl}_6$. Thus, the study of visible emissions in Er^{3+} and Yb^{3+} ions doped Cs_2NaYF_6 crystals is of practical interest for developing photon upconverters. High efficiency of up-conversion in the cubic elpasolite Cs_2NaYF_6 can be achieved due to the low value of the maximum phonon frequency which is 468 cm^{-1} [11]. This value is higher than that for $\text{Cs}_2\text{NaYCl}_6$ (285 cm^{-1}) [19] but it is acceptable for energy storage on excited levels. In addition, long lifetimes of the first excited-states of Er^{3+} and Yb^{3+} ions observed for highly-doped Cs_2NaYF_6 crystals indicate their potential for generation of high pulse energies in passively Q-switched near-IR lasers.

In the present paper, the data on optical absorption, near-IR and visible f-f emissions of Cs_2NaYF_6 crystals doped with Er^{3+} and Yb^{3+} ions as well as $\text{Cs}_2\text{NaErF}_6$ and $\text{Cs}_2\text{NaYbF}_6$ are reported.

2. Experimental

Crystals of cubic elpasolite Cs_2NaYF_6 doped with Er^{3+} and Yb^{3+} ions as well as $\text{Cs}_2\text{NaErF}_6$ and $\text{Cs}_2\text{NaYbF}_6$ were grown under hydrothermal conditions. For hydrothermal experiments, copper-insert lined autoclaves with a volume of $\sim 40 \text{ cm}^3$ were utilized, and the inserts were separated by perforated diaphragms into synthesis and crystallization zones. The fluoride crystals were synthesized by a direct temperature-gradient method as a result of the reaction of the aqueous solutions containing 35–40 mol% CsF and 8–10 mol% NaF with oxide mixtures $(1-x)\text{Y}_2\text{O}_3 - x\text{Ln}_2\text{O}_3$ ($\text{Ln}=\text{Er}$ and Yb) at a temperature of $\sim 750 \text{ K}$ in the synthesis zone, a temperature gradient along the reactor body of up to 3 K/cm, and a pressure of $\sim 100 \text{ MPa}$. Under these conditions, spontaneously nucleated crystals of up to 0.5 cm^3 were grown in the upper crystallization zone of the autoclave for 200 h. The purities of the utilized rare earth oxides were 99.99%.

The structure type and phase purity of synthesized samples were characterized with conventional powder X-ray diffraction (XRD) technique and powder XRD patterns were obtained by using a Bruker D8 Advance X-Ray powder diffractometer with Cu K α radiation.

Absorption spectrum was measured for 10 at% Er^{3+} and 10 at% Yb^{3+} doped Cs_2NaYF_6 crystals with a Varian CARY 5000 spectrophotometer (the spectral bandwidth, SBW, was 0.1 nm). Thin polished platelets ($\sim 1 \text{ mm}$) of crystals were used.

Luminescence spectra were measured with a lock-in amplifier, a monochromator MDR-23 (SBW $\sim 0.1 \text{ nm}$) and Hamamatsu G5851 and C5460-01 photodetectors. The spectral sensitivity of the set-up was accurately determined with a halogen lamp with calibrated spectral power density. Near-IR luminescence and up-conversion luminescence (UCL) of Er^{3+} and Yb^{3+} ions was excited by InGaAs laser diode emitting at $\sim 960 \text{ nm}$ (excitation to the $\text{Er}^{3+}4\text{I}_{15/2}$ state or $\text{Yb}^{3+}2\text{F}_{5/2}$ state). Excitation light was focused on a sample in a $\sim 100 \mu\text{m}$ spot; the maximum power density was $\sim 40 \text{ kW/cm}^2$. Luminescence was also excited at ~ 355 and $\sim 520 \text{ nm}$ (excitation to the $2\text{G}_{9/2}$ and $2\text{H}_{11/2}$ states of Er^{3+} , respectively) and a ns optical parametric oscillator (OPO) Lotis TII LT-2214 was used. CIE chromaticity coordinates of phosphors were calculated by using the photoluminescence data.

For the studies of luminescence decay of Yb^{3+} ions, OPO with the pulse duration of $\sim 20 \text{ ns}$ was tuned to 960 nm. Luminescence was collected by a wide-aperture lens and re-imaged to the input slit of a monochromator MDR-12 (tuned to 1020 nm, SBW $\sim 1 \text{ nm}$); then it was detected with a fast Hamamatsu G5851 photodetector (response time, $< 100 \text{ ns}$) and a 500 MHz Textronix TDS-3052B digital oscilloscope. To avoid the reabsorption loss, studied crystals were finely powdered and immersed in glycerin ($\sim 5 \text{ wt}\%$ powder content).

All spectroscopic studies were performed at room temperature.

3. Results and discussion

The X-ray phase analysis has confirmed that all the synthesized compounds are single-phase samples containing only the cubic elpasolite phases, space group Fm3m, $Z=4$ (ICDD PDF Cards: 00-020-1214; 00-021-0221; 00-021-0224) [1]. X-ray diffraction patterns of Cs_2NaYF_6 , $\text{Cs}_2\text{NaErF}_6$ and $\text{Cs}_2\text{NaYbF}_6$ are showed in Fig. 1 and they can be indexed with a cubic cell with the lattice parameter, $a=9.057 \text{ \AA}$, 9.045 \AA and 9.016 \AA , respectively. Lattice parameter (a), volume of the unit cell (V), density (ρ) and concentration (N) of the Y^{3+} , Er^{3+} and Yb^{3+} ions which have been obtained from the X-ray diffraction studies for these compounds are summarized in Table 1. One can see that there is a marginal change in cell parameters due to differences in rare earth ionic radii and it should be also noted that the unit cell parameters determined in this study are notably less than those tabulated in [1].

An absorption spectrum measured for a 10 at% $\text{Er}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal is shown in Fig. 2. For the $4\text{I}_{15/2} \rightarrow 4\text{I}_{11/2}$ transition, the peak absorption cross-section is $\sigma_{\text{abs}}=0.07 \times 10^{-21} \text{ cm}^2$ at 963 nm. The full width at half maximum (FWHM) for this band is $\sim 24 \text{ nm}$. Such low absorption determines low efficiency for the excitation of Er^{3+} ions by using InGaAs diodes. Indeed, for the stoichiometric $\text{Cs}_2\text{NaErF}_6$ crystal, the corresponding peak absorption coefficient is $\alpha \sim 0.37 \text{ cm}^{-1}$, which means that the absorption of diode emission is not complete even for a few mm-thick crystal. For the $4\text{I}_{15/2} \rightarrow 4\text{I}_{13/2}$ transition that is typically used for the in-band excitation of

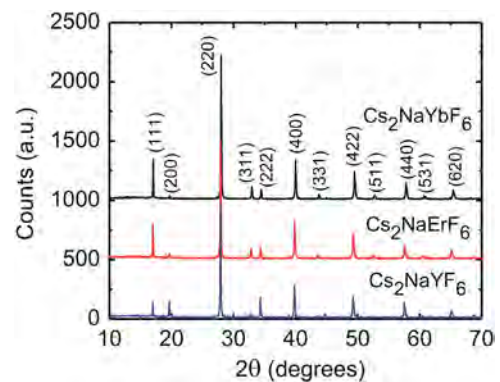


Fig. 1. X-ray diffraction patterns for Cs_2NaYF_6 , $\text{Cs}_2\text{NaErF}_6$ and $\text{Cs}_2\text{NaYbF}_6$ crystals; numbers on the graph represent the Miller indices, (hkl).

Table 1

Lattice parameter (a), unit cell volume (V), calculated density (ρ) and absolute concentration of rare earth ions (N) for cubic elpasolites (space group: Fm3m, $Z=4$).

Composition	a , \AA	V , \AA^3	ρ , g/cm^3	N , at/cm^3
Cs_2NaYF_6	9.057	742.9	4.42	5.38×10^{21}
$\text{Cs}_2\text{NaErF}_6$	9.045	740.0	5.15	5.41×10^{21}
$\text{Cs}_2\text{NaYbF}_6$	9.016	732.9	5.24	5.46×10^{21}

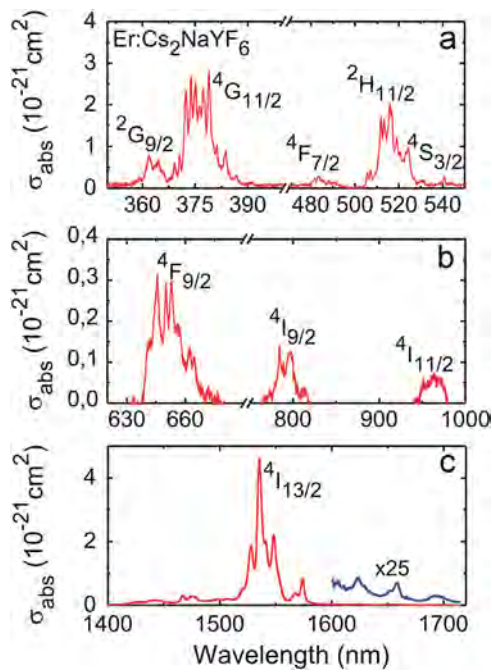


Fig. 2. Absorption cross-section spectra for a 10 at% Er³⁺:Cs₂NaYF₆ crystal.

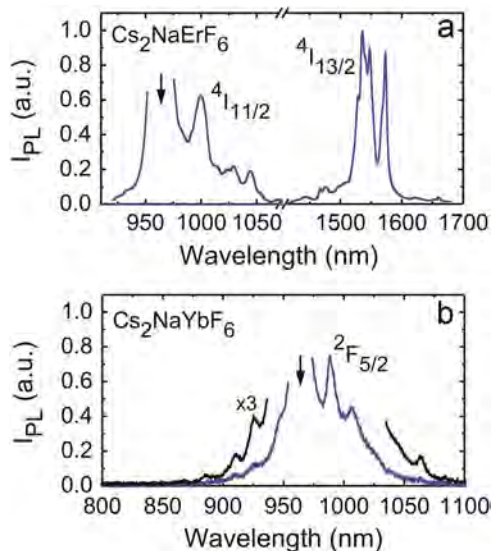


Fig. 3. Near-IR emission spectra of Cs₂NaErF₆ (a) and Cs₂NaYbF₆ (b) crystals; excitation wavelength is denoted by arrow (960 nm).

Er³⁺ ions, the absorption is much stronger, $\sigma_{\text{abs}} = 4.6 \times 10^{-21} \text{ cm}^2$ at 1532.2 nm. The FWHM of this band is 5.4 nm.

Near-IR emissions of Er³⁺ ions have been studied under 960 nm excitation by using a stoichiometric Cs₂NaErF₆ crystal. The luminescence band related to the Er³⁺ $^4I_{13/2} \rightarrow ^4I_{15/2}$ transition spans from ~ 1.4 to $1.68 \mu\text{m}$, see Fig. 3(a). The band in the 920–1060 nm spectral range is attributed to the $^4I_{11/2} \rightarrow ^4I_{15/2}$ transition of Er³⁺ ions.

Emission of Er³⁺ ions at $\sim 1.5 \mu\text{m}$ is eye-safe and interesting for laser operation. To calculate the corresponding stimulated-emission cross-sections σ_{SE} spectra, two methods can be used. The first one is the reciprocity method [20]:

$$\sigma_{\text{SE}}(\lambda) = \sigma_{\text{abs}}(\lambda) \frac{Z_1}{Z_2} \exp\left(-\frac{hc/\lambda - E_{\text{ZL}}}{kT}\right), \quad (1)$$

where Z_1 and Z_2 are the lower and upper manifold partition functions, respectively, E_{ZL} is the energy corresponding to the zero phonon line, h is the Planck constant, c is the speed of light, λ is the light wavelength, k is the Boltzmann constant and T is the crystal temperature (room-temperature). Partition functions are determined as:

$$Z_m = \sum_k g_k^m \exp(-E_k^m/kT), \quad (2)$$

where $m = 1, 2$; g_k^m is the degeneration of the sublevel having the number k and the energy E_k^m measured from the lower sublevel of the corresponding multiplet. The set of E_k^m values for the $^4I_{15/2}$ and $^4I_{13/2}$ states of Er³⁺ ions in the Cs₂NaYF₆ crystal [4] is listed in Table 2.

Calculation of σ_{SE} with the reciprocity method is beneficial as it does not require the information about the radiative lifetime τ_{rad} of the emitting state as well as direct measurement of the emission spectrum which can be changed as a result of the reabsorption loss. The obtained results are shown in Fig. 4(a). The maximum σ_{SE} value is $3.8 \times 10^{-21} \text{ cm}^2$ at 1532.2 nm. This value is lower than the typical peak σ_{SE} values for the Er³⁺ $^4I_{13/2} \rightarrow ^4I_{15/2}$ transition in widespread oxide and fluoride laser hosts, $0.5\text{--}1 \times 10^{-20} \text{ cm}^2$ [21]. In the spectral range where laser operation is expected, the maximum σ_{SE} value is $1.5 \times 10^{-21} \text{ cm}^2$ at 1574.1 nm. Radiative lifetime of the Er³⁺ emitting state ($^4I_{13/2}$) can be

Table 2

Energies of Stark sub-levels for the ground-states and the first excited-states of Er³⁺ and Yb³⁺ in Cs₂NaYF₆ crystals [4,8].

Multiplet (Yb ³⁺)	Sub-levels, cm ⁻¹	Multiplet (Er ³⁺)	Sub-levels, cm ⁻¹
$^2F_{7/2}$	3	$^4I_{15/2}$	0
	324		25
	656		57
			259
$^2F_{5/2}$	10,389	$^4I_{13/2}$	287
			6492
	11,109		6517
			6532
			6682
			6686

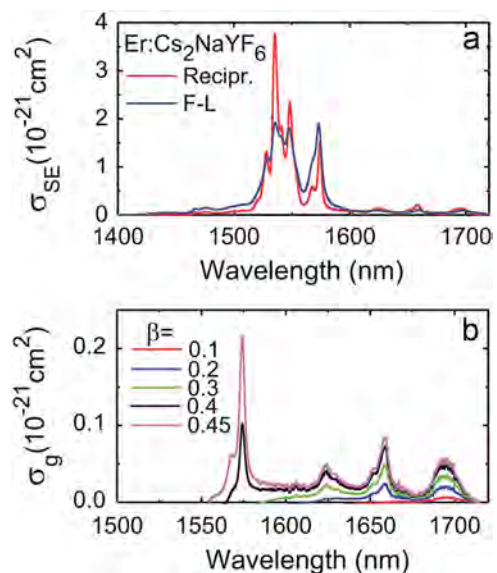


Fig. 4. (a) Stimulated-emission cross-sections spectra calculated with the reciprocity and F-L methods for a 10 at% Er³⁺:Cs₂NaYF₆ crystal, (b) gain cross-sections [$\sigma_{\text{g}} = \beta \sigma_{\text{SE}} - (1 - \beta) \sigma_{\text{abs}}$] spectra, $\beta = N_2/N$ is the inversion ratio.

estimated from the so-called modified reciprocity method (n is the crystal refractive index) [22]:

$$\tau_{\text{rad}} = \frac{1}{8\pi n^2 c Z_1} \frac{Z_2 \exp(-E_{\text{ZL}}/kT)}{\int \lambda^{-4} \sigma_{\text{abs}}(\lambda) \exp(-hc/(kT\lambda)) d\lambda} \quad (3)$$

For $\text{Er}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal, $\tau_{\text{rad}}(^4I_{13/2})$ has been determined to be $\sim 32 \pm 2$ ms. Previously, lifetime of this state was measured for 1 at% $\text{Er}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal only at cryogenic temperature (4 K), $\tau(^4I_{13/2}) \sim 100$ ms [5] and this value can be considered as a radiative one at low temperatures, as the reabsorption for such crystal doping is nearly vanishing. Such long values are inherent for all the elpasolite crystals [14]. In particular, $\tau(^4I_{13/2}) = 22$ ms for a cubic $\text{Cs}_2\text{NaErCl}_6$ crystal [23]. Independent estimation of the τ_{rad} for $\text{Er}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal can be done with the Judd–Ofelt modeling that will be performed in a separate study.

Using the measured emission spectrum $W(\lambda)$, Fig. 3(a), and the determined radiative lifetime $\tau_{\text{rad}}(^4I_{13/2})$, it is possible to calculate a stimulated-emission cross-sections spectrum for the $^4I_{11/2} \rightarrow ^4I_{15/2}$ transition with the Füchtbauer–Ladenburg (F–L) equation [24]:

$$\sigma_{\text{SE}}(\lambda) = \frac{\lambda^5}{8\pi n^2 \tau_{\text{rad}} c} \frac{W(\lambda)}{\int \lambda W(\lambda) d\lambda} \quad (4)$$

The obtained results are shown in Fig. 4(a) and they are in good agreement with the ones from the reciprocity method, considering strong reabsorption at short wavelengths.

For assessing the prospects of elpasolite crystals to lasers, a useful parameter is the gain cross-section, σ_g :

$$\sigma_g(\lambda) = \beta \sigma_{\text{SE}}(\lambda) - (1 - \beta) \sigma_{\text{abs}}(\lambda), \quad (5)$$

where β is the inversion ratio, $\beta = N_2/N_0$ where N_2 and N_0 are the numbers of ions in the upper laser level and the overall number of ions, respectively. Gain spectra for a 10 at% $\text{Er}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal are shown in Fig. 4(b). For these calculations, we used stimulated-emission cross-sections spectra obtained with the reciprocity method. For low inversion ratios ($\beta < 0.4$), laser operation is expected at several wavelength, $\sim 1624, 1658$ or 1694 nm. For high inversion ratios, the peak centered at 1574 nm dominates in the spectrum.

An absorption spectrum measured for a 10 at% $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal is shown in Fig. 5(a) representing the $^2F_{5/2} \rightarrow ^2F_{7/2}$ transition of Yb^{3+} ions. The peak absorption cross-section is $\sigma_{\text{abs}} = 1.3 \times 10^{-21} \text{ cm}^2$

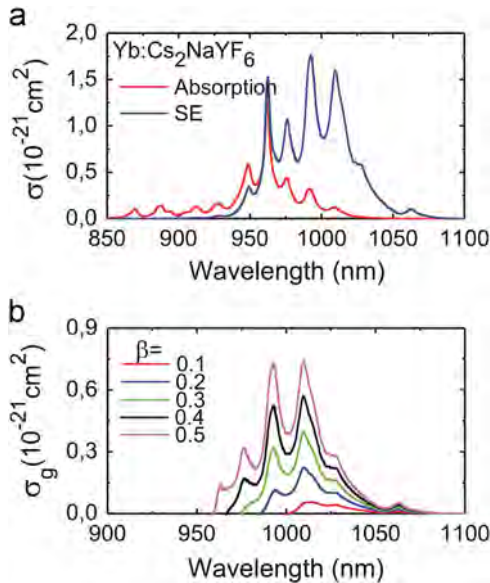


Fig. 5. (a) Absorption and stimulated-emission cross-sections spectra for a 10 at% $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal, (b) gain cross-sections [$\sigma_g = \beta \sigma_{\text{SE}} - (1 - \beta) \sigma_{\text{abs}}$] spectra, $\beta = N_2/N_0$ is the inversion ratio.

at 962.0 nm. Thus, Cs_2NaYF_6 crystals containing both Er^{3+} and Yb^{3+} ions provide significant improvement of the excitation efficiency under using InGaAs laser diodes. In particular, the peak absorption coefficient for the stoichiometric $\text{Cs}_2\text{NaYbF}_6$ crystal, $\alpha = 6.9 \text{ cm}^{-1}$ and FWHM for this band is 5.2 nm.

The stimulated-emission cross-sections spectrum for a 10 at% $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal has been calculated with the reciprocity method, Eq. (1). The spectrum is shown in Fig. 5(a) and the energies of Stark sub-levels for the $^2F_{5/2}$ and $^2F_{7/2}$ states of Yb^{3+} ions used for calculations are listed in Table 2 [8]. The maximum σ_{SE} value is $\sim 1.8 \times 10^{-21} \text{ cm}^2$ at 992.4 nm. Emission of Yb^{3+} ions spans from ~ 920 to 1080 nm. Thus, the tuning range wider than 100 nm is expected under using this crystal as a laser gain medium. This is in agreement with the near-IR emission spectrum of the $\text{Cs}_2\text{NaYbF}_6$ crystal measured directly under 960 nm excitation and shown in Fig. 3(b).

The radiative lifetime of the $^2F_{5/2}$ state of Yb^{3+} ions in the Cs_2NaYF_6 crystal determined from the modified reciprocity method, Eq. (3), is $\tau_{\text{rad}}(^4I_{13/2}) = 6.4$ ms. This value is in close agreement with the decay time of Yb^{3+} emission measured directly for a powdered 10 at% $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ composition, $\tau = 6.3$ ms. The corresponding decay curve is shown in Fig. 6 and it is clearly single-exponential. For a stoichiometric $\text{Cs}_2\text{NaYbF}_6$ crystal, similar measurement yields $\tau = 5.7$ ms, which is close to the previously reported value [6], $\tau = 5.63$ ms. Thus, the anomalously weak concentration quenching is observed for $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystals. Determined lifetimes are at least two times longer than those for typical Yb^{3+} -doped fluoride laser hosts with τ ranging typically from 1.5 to 3 ms. This indicates the potential of highly-doped $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystals (up to 100 at%) for generation of high pulse energies in the Q-switched operation mode.

Gain cross-sections spectra for a 10 at% $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal are shown in Fig. 5(b). For low inversion ratios ($\beta < 0.1$), the gain spectrum is flat and it spans from 1000 to 1080 nm, so the multi-peak spectral behavior is expected. For high inversion, two intense local peaks centered at ~ 992 nm and 1009 nm are observed. This indicates the possibility of dual-wavelength laser operation for this crystal.

The lifetimes of the $\text{Yb}^{3+} ^2F_{5/2}$ excited-state and the $^4I_{13/2}$ and $^4I_{11/2}$ excited-states for Er^{3+} ions are presented in Table 3. In this context, it is worth mentioning that even for a stoichiometric $\text{Cs}_2\text{NaErF}_6$ crystal, the value of $\tau(^4I_{11/2})$ is as long as 0.7 ms at room-temperature [5], which indicates that it can be promising medium for $\sim 3 \mu\text{m}$ laser operation on the $^4I_{11/2} \rightarrow ^4I_{13/2}$ transition [25].

UCL spectra of $\text{Er}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystals under the excitation at 960 nm to the $\text{Er}^{3+} ^4I_{11/2}$ state are shown in Fig. 7(a). For a 10 at% Er^{3+} doped crystal, the green emission band spanning from 510 to 580 nm and related to the transitions from the closely located and thermalized state $^2H_{11/2}$ and $^4S_{3/2}$ to the ground state $^4I_{15/2}$

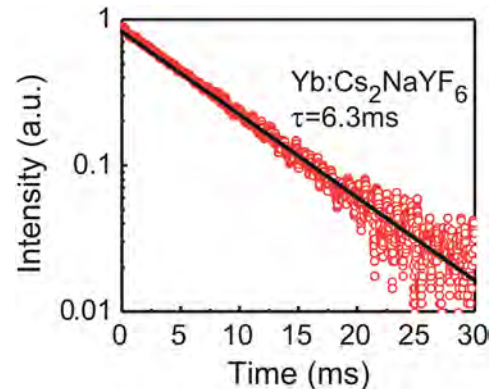


Fig. 6. Luminescence decay curve for a 10 at% $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystal: $\lambda_{\text{exc}} = 960$ nm; luminescence is detected at 1020 nm.

Table 3
Lifetimes of the excited-states of Er³⁺ and Yb³⁺ ions in Cs₂NaYF₆ crystals*.

Ion concentration	Yb ³⁺ ion	Er ³⁺ ion		Er ³⁺ ion	
	$\tau(^2F_{5/2})$, ms	$\tau(^4I_{13/2})$, ms	$\tau(^4I_{11/2})$, ms	$\tau(^4I_{13/2})$, ms	$\tau(^4I_{11/2})$, ms
	This work/ [6]/RT	This work/ [5]/4 K	[5]/RT	[5]/4 K	[5]/4 K
1 at%	–	–	100	12	21
10 at%	6.3; 6.4 _{rec}	–	~32 _{rec}	–	1.1
100 at%	5.7	5.63	–	0.7	1.1

* RT - room temperature, REC - estimated with the reciprocity method.

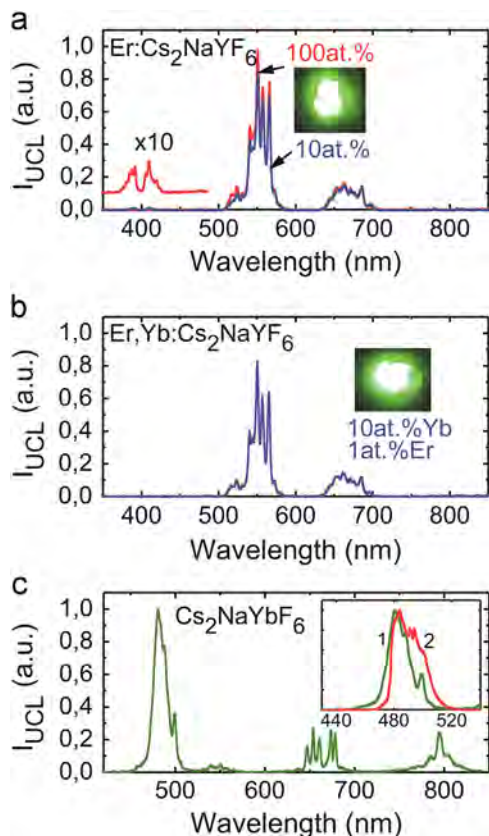


Fig. 7. Up-conversion luminescence (UCL) spectra for (a) 10 at% Er³⁺:Cs₂NaYF₆ and Cs₂NaErF₆, (b) 1 at% Er³⁺, 10 at% Yb³⁺:Cs₂NaYF₆ and (c) Cs₂NaYbF₆ crystals; $\lambda_{exc}=960$ nm; insets show images of the excited samples (a), (b) and details of blue emission from the Cs₂NaYbF₆ crystal (c): 1-measured UCL spectrum, 2-calculated spectrum of cooperative emission, Eq. (6).

dominates in the spectrum. Four intense peaks at 540, 551, 557 and 566 nm are observed within this emission band. The red emission in the range 630–700 nm related to the transition $^4F_{9/2} \rightarrow ^4I_{15/2}$ is much weaker than the green one. The ratio for integrated intensities of these bands (R/G ratio) is 0.27 which is referred to the domination of the excited-state absorption (ESA) over the cross-relaxation (CR) mechanism in generation of UCL, however, further time-resolved studies of UCL are required to support this [26]. In the blue region there is a weak emission band which is due to the transition from the higher-lying excited state $^2H_{9/2}$ to the $^4I_{15/2}$ ground-state.

These features determine the yellow-green color of UCL from 10 at% Er³⁺:Cs₂NaYF₆ with $x=0.385$ and $y=0.603$ in the 1931 CIE chromaticity coordinates as well as high color purity, $p > 98\%$, caused by the dominant wavelength at 562 nm. Color purity p was calculated from the CIE 1931 chromaticity diagram with respect to

the CIE-E illuminant (uniform white, $x=0.333$ and $y=0.333$). It is defined as $p=a/b$ where a is the distance from the white point to the sample color point and b is the distance from the white point to the point on the spectral locus corresponding to the dominant wavelength. The color purity is a quantitative measure of the saturation of a particular color. For a stoichiometric Cs₂NaErF₆ crystal and a 1 at% Er³⁺, 10 at% Yb³⁺:Cs₂NaYF₆ crystals, very similar UCL spectra are observed, see Fig. 7. Color characteristics for UCL from the studied crystals are summarized in Table 4.

In addition, UCL from a stoichiometric Cs₂NaYbF₆ crystal has been studied under the excitation at 960 nm to the Yb³⁺ $^2F_{5/2}$ state. The emission bands observed in Fig. 7(c) are due to ET from Yb³⁺ to impurity Tm³⁺ and Er³⁺ ions and UCL from Tm³⁺ dominates. Both Tm and Er are presented as trace impurities in ytterbium oxide, Yb₂O₃, reagent and thus their amount in stoichiometric crystal is enough to provide detectable UCL. The bands at 450–505, 640–680 and 750–820 nm are related to the transitions $^1G_4 \rightarrow ^3H_6$, $^1G_4 \rightarrow ^3F_4$ and $^3H_4 \rightarrow ^3H_6$ for Tm³⁺, respectively, whereas weak green Er³⁺ emission from the $^2H_{11/2}$ and $^4S_{3/2}$ states to the $^4I_{15/2}$ ground state is detected at ~550 nm. The red Er³⁺ emission from the $^4F_{9/2}$ state at ~650 nm can overlap with the red Tm³⁺ one, so it is not discovered. Accordingly, UCL from the Cs₂NaYbF₆ crystal is blue-violet.

In the previous study of a Cs₂NaYbF₆ crystal [6], the strong emission band at ~480 nm is at least partially attributed to cooperative emission from Yb³⁺–Yb³⁺ ion pairs [27]. This effect is known for materials with the strong clustering of Yb³⁺ ions [28]. In this case, a pair of closely located ions can form a virtual excited state with the energy $2E(^2F_{5/2}) \sim 20,000$ cm⁻¹. The emission from this state can be observed in the region 480–500 nm [29]. The emission spectrum can be calculated as the convolution of the near-IR emission spectrum of Yb³⁺ ions related to the $^2F_{5/2} \rightarrow ^2F_{7/2}$ transition [27]:

$$F_{coop}(E) = \int F_{IR}(E')F_{IR}(E-E')dE'. \quad (6)$$

The result of this calculation is presented in the inset of Fig. 7(c). The cooperative emission should occur in the spectral range 475–510 nm with a maximum at ~484 nm that is very close to the maximum of the $^1G_4 \rightarrow ^3H_6$ Tm³⁺ emission in the Cs₂NaYF₆ crystal [3]. Thus, it is difficult to distinguish these effects spectrally. In [6] it has been found that the decay time of blue emission from a Cs₂NaYbF₆ crystal is 2.73 ms, which is almost exactly half of $\tau(^2F_{5/2})$ measured at ~1 μ m for Yb³⁺ ions. Such a correlation is expected for cooperative emission, $\tau_{coop} = \tau_{IR}/2$. Thus, blue UCL may be attributed to both Tm³⁺ impurity centers and cooperative emission. It should be also noticed that such intense UV up-conversion emissions can contribute to enhance the spectral response of photocatalytic semiconductor electrodes used in water-splitting processes for sustainable production of hydrogen, since they can help in bridging large bands gaps of efficient photocatalysts, like α -Fe₂O₃ (hematite), located at around 560 nm and eventually increase the efficiency of photoelectrochemical devices.

Table 4

CIE 1931 color coordinates x , y , dominant wavelength λ_d and color purity p for luminescence from Er³⁺–doped elpasolite crystals.

Crystal	x	y	λ_d , nm	p	Color
Exc. 960 nm					
10 at% Er ³⁺ :Cs ₂ NaYF ₆	0.385	0.603	562	98%	Yellow–green
Cs ₂ NaErF ₆	0.343	0.656	556	99%	Yellowish–green
1 at% Er ³⁺ , 10 at% Yb ³⁺ :Cs ₂ NaYF ₆	0.340	0.660	555	99%	Yellowish–green
Exc. 355 nm					
10 at% Er ³⁺ :Cs ₂ NaYF ₆	0.333	0.650	555	99%	Yellowish–green
Cs ₂ NaErF ₆	0.325	0.586	553	75%	Yellowish–green

In Fig. 8(a), log–log plots for the UCL intensity (I_{UCL}) versus the excitation power P are shown for a Cs_2NaErF_6 crystal. For the up-conversion process, I_{UCL} is proportional to the n th power of P , i.e. $I_{UCL} \sim P^n$ [30] where n is the number of pump photons absorbed per up-converted photon emitted. A plot of $\log I_{UCL}$ versus $\log P$ yields a straight line with slope n . For green emissions that occur from the ${}^2H_{11/2}$ and ${}^4S_{3/2}$ states, for the slope of this dependence $n=2.1$ (524 nm) and 1.9 (557 nm), which means that two pump photons are required to populate the above mentioned states. There is the same situation for red emission from the ${}^4F_{9/2}$ state at 660 nm where $n=2.1$. Normally, excitation of Er^{3+} ions to the higher lying excited states is achieved in two steps, for example ground-state absorption (GSA) ${}^4I_{15/2} \rightarrow {}^4I_{11/2}$ followed by excited-state absorption (ESA) from the ${}^4I_{11/2}$ or the ${}^4I_{13/2}$ states. For Cs_2NaErF_6 , cross-relaxation (CR) between the adjacent Er^{3+} ions, which can participate as an additional mechanism for the population of the ${}^4F_{9/2}$ state, seems to be very weak. Indeed, the R/G ratio for UCL is not enhanced when the Er^{3+} concentration in Cs_2NaYF_6 increases from 10 to 100 at%, Fig. 7(a). This well correlates with the large distance between the isolated Y^{3+} sites in the $Er^{3+}:Cs_2NaYF_6$ crystal, so the probability of CR is not varied with the increase of the Er^{3+} concentration in the elpasolite hosts. No significant dependence of R/G ratio on the excitation power was detected.

Similar slopes ($n \sim 2$) for the log–og plots of the UCL intensity vs. the excitation power are observed also for a 1 at% Er^{3+} , 10 at% $Yb^{3+}:Cs_2NaYF_6$ crystal, Fig. 8(b). In this case, the first step of the UCL mechanism is the excitation of Er^{3+} ions through the GSA ${}^2F_{7/2} \rightarrow {}^2F_{5/2}$ of Yb^{3+} ions and the energy-transfer from Yb^{3+} to Er^{3+} , ${}^2F_{5/2}(Yb^{3+}) \rightarrow {}^4I_{11/2}(Er^{3+})$. On the other hand, in any case, 2 pump infrared photons are required for the generation of one visible photon. More detailed discussion about the mechanisms of UCL in hosts containing Er^{3+} and Yb^{3+} can be found elsewhere [31].

In Fig. 8(a), the I_{UCL} vs P plot for the blue UCL from a Cs_2NaYbF_6 crystal is also presented and the slope of this straight line is 2.4. This value is intermediate between the theoretical value of 2 for pure cooperative emission and 3 for pure $Tm^{3+}G_4 \rightarrow {}^3H_6$ emission. This supports our idea that the blue emission from the Cs_2NaYbF_6 crystal is due to the both processes.

Under excitation into the ${}^2G_{9/2}$ or the ${}^2H_{11/2}$ states of Er^{3+} in Cs_2NaYF_6 at 355 nm or 520 nm, respectively, all the crystals singly doped with Er^{3+} ions demonstrate emission spectra similar to those obtained under near-IR excitation, Figs. 9(a), 3(a) and 7(a). The corresponding color coordinates can be found in Table 4. However, for a 1 at% Er^{3+} , 10 at% $Yb^{3+}:Cs_2NaYF_6$ crystal the spectra are different from those of Er^{3+} doped Cs_2NaYF_6 crystals. In particular, a broad emission band spanning from 940 to 1050 nm is detected. This band is clearly different from the

luminescent band related to the ${}^4I_{11/2} \rightarrow {}^4I_{15/2}$ transition of Er^{3+} ions and has the spectral features of emission on the $Yb^{3+}{}^2F_{5/2} \rightarrow {}^2F_{7/2}$ transition. Excitation of Yb^{3+} ions is due to the so-called down-conversion (“quantum cutting”) process for the $Er^{3+}-Yb^{3+}$ ion pairs [32,33].

It should be also noted that enhancement of the efficiency of the up- and down- conversion processes in cubic elpasolites is possible with the ytterbium compositions $Cs_2NaEr_xYb_{1-x}F_6$ containing relatively high Er^{3+} concentrations.

4. Conclusions

To conclude, we have studied absorption and luminescence of Er^{3+} and Yb^{3+} ions in cubic elpasolite Cs_2NaYF_6 crystals as well as in crystals of Cs_2NaErF_6 and Cs_2NaYbF_6 synthesized under hydrothermal conditions. Stimulated-emission and gain cross-sections have been determined for the $Yb^{3+}{}^2F_{5/2} \rightarrow {}^2F_{7/2}$ and the $Er^{3+}{}^4I_{13/2} \rightarrow {}^4I_{15/2}$ transitions in 10 at% $Yb^{3+}:Cs_2NaYF_6$ and 10 at% $Er^{3+}:Cs_2NaYF_6$ at room temperature. The maximum σ_{SE} values are $1.8 \times 10^{-21} \text{ cm}^2$ at 993 nm (Yb^{3+}) and $3.8 \times 10^{-21} \text{ cm}^2$ at 1535 nm (Er^{3+}). The possibility of dual-wavelength laser operation and wide tuning range exceeding 100 nm for laser emission are

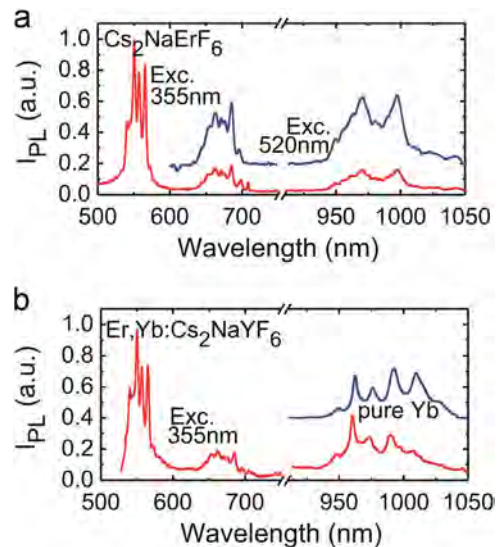


Fig. 9. Luminescence of Cs_2NaErF_6 (a) and 1 at% Er^{3+} , 10 at% $Yb^{3+}:Cs_2NaYF_6$ (b) crystals after excitation into the ${}^2G_{9/2}$ state at 355 nm and into the ${}^2H_{11/2}$ state at 520 nm; the spectrum of Yb^{3+} emission from the Cs_2NaYbF_6 crystal is added in (b) for comparison.

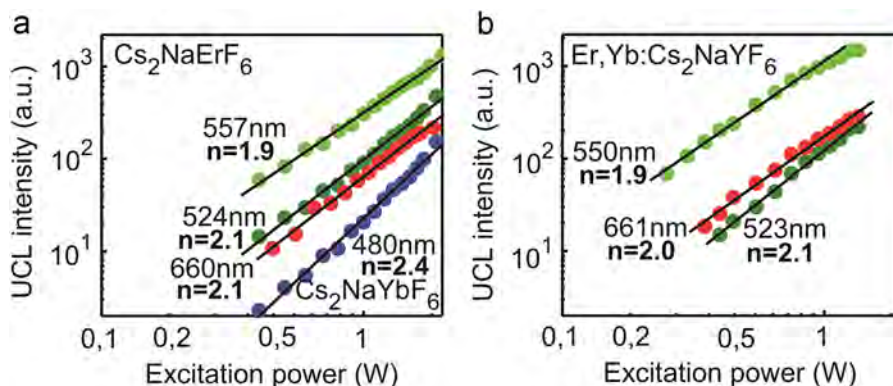


Fig. 8. Dependences of the UCL intensity on the excitation power in a log–log scale for (a) Cs_2NaErF_6 , Cs_2NaYbF_6 and (b) 1 at% Er^{3+} , 10 at% $Yb^{3+}:Cs_2NaYF_6$ (b) crystals; $\lambda_{exc}=960 \text{ nm}$; n is the number of pump photons absorbed per up-converted photon emitted.

expected for $\text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystals. Due to their structure peculiarities, elpasolite crystals provide exceptionally long radiative lifetimes of the excited-states for both Yb^{3+} and Er^{3+} ions, $\tau(^2\text{F}_{5/2})=6.3$ ms and $\tau(^4\text{I}_{13/2}) \sim 32$ ms, respectively, together with relatively weak UCL, which makes them attractive for high pulse energy Q-switched lasers. Under excitation at 960 nm, $\text{Cs}_2\text{NaErF}_6$ crystals provide yellowish-green UCL with CIE coordinates $x=0.353$, $y=0.656$. Down-conversion is detected for $\text{Er}^{3+}, \text{Yb}^{3+}:\text{Cs}_2\text{NaYF}_6$ crystals.

Acknowledgments

This research was partially supported by the Russian Foundation for Basic Research (Research Project no. 15-03-02507a); Fundación CajaCanarias (AYE06) within the Project MAGEC (Materials for Advanced Generation of Energy at Canary Islands) and the Spanish Ministry of Economy and Competitiveness (Project ENE2013-47826-C4-4-R).

References

- [1] G. Meyer, *Prog. Sol. St. Chem.* 14 (1982) 141.
- [2] L.R. Moras, *J. Inorg. Nucl. Chem.* 36 (1974) 3876.
- [3] V.N. Makhov, N.M. Khaidukov, D. Lo, J.C. Krupa, M. Kirm, E. Negodin, *Opt. Mater.* 27 (2005) 1131.
- [4] X. Zhou, P.A. Tanner, M.D. Faucher, *J. Phys. Chem. C* 111 (2007) 683.
- [5] H. Vrielinck, I. Izeddin, V.Y. Ivanov, T. Gregorkiewicz, F. Callens, D.S. Lee, A.J. Steckl, N.M. Khaidukov, *Mater. Res. Soc. Symp.* 866 (2005) V381.
- [6] D.S. Pytalev, A. Jaffres, P. Aschehoug, P.A. Ryabochkina, A.V. Malov, N.M. Khaidukov, M.N. Popova, *J. Lumin.* 153 (2014) 125.
- [7] M.L. Falina, K.I. Gerasimova, A.M. Leushin, N.M. Khaidukov, *J. Lumin.* 128 (2008) 1103.
- [8] X. Zhou, M.F. Reid, M.D. Faucher, P.A. Tanner, *J. Phys. Chem. B* 110 (2006) 14939.
- [9] B.Z. Malkin, D.S. Pytalev, M.N. Popova, E.I. Baibekov, M.L. Falin, K.I. Gerasimov, N.M. Khaidukov, *Phys. Rev. B* 86 (2012) 134110.
- [10] P.A. Tanner, M.D. Faucher, *Chem. Phys. Lett.* 445 (2007) 183.
- [11] P.A. Tanner, Y.L. Liu, N. Edelstein, K. Murdoch, N.M. Khaidukov, *J. Phys. : Condens. Matter* 9 (1997) 7817.
- [12] J.R.G. Thorne, M. Jones, C.S. McCaw, K.M. Murdoch, R.G. Denning, N.M. Khaidukov, *J. Phys. : Condens. Matter* 11 (1999) 7851.
- [13] A.J. Berry, I.D. Morrison, R.G. Denning, *Mol. Phys.* 93 (1998) 1.
- [14] W. Ryba-Romanowski, Z. Mazurak, B. Jezowska-Trzebiatowska, *J. Lumin.* 27 (1982) 177.
- [15] P.A. Tanner, C.S.K. Mak, W.-M. Kwok, D.L. Phillips, M.D. Faucher, *Phys. Rev. B* 66 (2002) 165203.
- [16] Z. Mazurak, E. Lujowiak, B. Jezowska-Trzebiatowska, W. Ryba-Romanowski, *J. Lumin.* 29 (1984) 47.
- [17] Z. Mazurak, E. Lujowiak, B. Jezowska-Trzebiatowska, *J. Lumin.* 33 (1985) 159.
- [18] F. Auzel, *Chem. Rev.* 104 (2004) 139.
- [19] G.N. Papatheodorou, *J. Chem. Phys.* 66 (1977) 2893.
- [20] S.A. Payne, L.L. Chase, L.K. Smith, W.L. Kway, W.F. Krupke, *IEEE J. Quant. Electron.* 28 (1992) 2619.
- [21] P.A. Loiko, E.A. Arbabzadah, M.J. Damzen, X. Mateos, E.B. Dunina, A.A. Kornienko, A.S. Yasukevich, N.A. Skoptsov, K.V. Yumashev, *J. Lumin.* 171 (2016) 226.
- [22] A.S. Yasyukevich, V.G. Shcherbitskii, V.E. Kisel, A.V. Mandrik, N.V. Kuleshov, *J. Appl. Spectr.* 71 (2004) 202.
- [23] P.A. Tanner, *Mol. Phys.* 63 (1988) 365.
- [24] B.F. Aull, H.P. Jenssen, *IEEE J. Quantum Electron.* 18 (1982) 925.
- [25] B.J. Dinerman, P.F. Moulton, *Opt. Lett.* 19 (1994) 1143.
- [26] J. Mendez-Ramos, V. Lavin, I.R. Martin, U.R. Rodriguez-Mendoza, J.A. Gonzalez-Almeida, V.D. Rodriguez, A.D. Lozano-Gorrin, P. Nunez, *J. Alloy. Compd.* 323–324 (2001) 753.
- [27] Ph Goldner, F. Pelle, D. Meichenin, F. Auzel, *J. Lumin.* 71 (1997) 137.
- [28] F. Auzel, D. Meichenin, F. Pellé, P. Goldner, *Opt. Mater.* 4 (1994) 35.
- [29] P.A. Loiko, G.E. Rachkovskaya, G.B. Zakharevich, A.A. Kornienko, E.B. Dunina, A.S. Yasukevich, K.V. Yumashev, *J. Non-Cryst. Solids* 392–393 (2014) 39.
- [30] M. Pollnau, D.R. Gamelin, S.R. Luthi, H.U. Gudel, *Phys. Rev. B* 61 (2000) 3337.
- [31] P.A. Loiko, N.M. Khaidukov, J. Méndez-Ramos, E.V. Vilejshikova, N.A. Skoptsov, K.V. Yumashev, *J. Lumin.* 170 (2015) 1.
- [32] L. Aarts, B.M. van der Ende, A. Meijerink, *J. Appl. Phys.* 106 (2009) 023522.
- [33] J.J. Eilers, D. Biner, J.T. van Wijngaarden, K. Krämer, H.-U. Güdel, A. Meijerink, *Appl. Phys. Lett.* 96 (2010) 151106.