## THE ROLE OF THE TEACHER IN OBJECT-LEVEL AND META-LEVEL LEARNING

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#### DECLARATION

I declare that this research report is my own, unaided work. It is being submitted for the Degree of Master of Science in the University of the Witwatersrand, Johannesburg. It has not been submitted before for any degree or examination in any other University.

(Signature of candidate)

27<sup>th</sup> of July 2012

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#### ABSTRACT

The National Curriculum statement, or NCS for short, proposes significant shifts in the way that teachers carry out their work. Strategies, such as investigation and collaborative work were promoted as a reform model for effective teaching and learning. Thus, the intention of this research project is to determine how mathematics teachers are implementing the new reform in South Africa.

Based on Sfard's theory of commognitive development, a theoretical framework has been established and the focus specified in the following research questions:

1. How does a teacher mediate instruction during object-level & meta-level learning?

2. What enables and constrains her/his facilitative mediation in the case of Congruency in Grade 9?

3. What can we learn about the practical efficacy of Sfard's discourse theory?

In order to explore the actual teaching process the research project presents a case study constituted from two teaching practices on one topic, Congruency, at a College in Johannesburg. The purpose of observing and interviewing two teachers on the same lessons is to get a greater variety of conversation on object-level and meta-level learning. At the same time analysing their teaching process in-depth creates an opportunity to have different possibilities of mediating collaborative learning. The study addresses the three research questions through two related activities – non-participant observation and semi-structural interviews with teachers (in order to provide an opportunity for teachers to express their opinion).

Two main findings can be summarized: Firstly, the way the teacher manages instruction originates from her/his teaching style. The data analysis clearly confirms that mediation of the two teachers on the topic Congruency does not differ according object-level and meta-level learning, but according to the teachers. The second finding is related with Sfard's theoretical perspective: on the one hand the Department recommends investigative activities, whilst, on the other hand, Sfards' theory states that reinvention by the learner is highly unlikely. Therefore the practical efficacy of Sfard's theory is that in meta-level learning investigative activities are not appropriate and the role of the teacher should be dominant, not necessarily as facilitator.

This research study is an empirical proof of the validity of Sfard's theory and unspecified requirements of the Department of Education.

KEYWORDS: object-level learning, meta-level learning, Congruency, Commognitive theory.

# Table of contents

Contents	Page
Declaration	ii
Acknowledgement	iii
Abstract and Keywords	iv
List of Tables	viii
List of Figures	viii

# Chapter 1

Introduction		1
1.1	A motivation for undertaking this study	1
1.2	The research topic and research questions	3
1.3	Congruency discursive shift	4

# Chapter 2

Literature review		7
2.1	Research view against the transmission model of teaching	7
2.2	New view of the role of the teacher and the learners in the	
	learning-teaching process	8
2.3	Listening as a new actions in collaborative learning	10
2.4	Never telling is a misconception. Reformulating telling	
	as <i>initiating</i> and <i>eliciting</i>	11
2.5	Sfards' view of teaching	12
2.6	The van Hiele Levels of Geometric Understanding	13
2.7	A model of geometric discourse development	14

## Chapter 3

Theoretical framework		16
3.1	Review of the Cognitive, Socio-cultural, Situated and	
	Commognitive theories.	16
	3.1.1 The Constructivist/ Cognitive Theory	16
	3.1.2 Socio-cultural Theory	17
	3.1.3 Situated Theory	18

3.2	2 Commognitive Theory		20
	3.2.1	Early publication of Sfard	20
	3.2.2	Basic Commognitive Tenets.What is thinking?	22
	3.2.3	What is Mathematics?	23
	3.2.4	What is learning?	25
	3.2.5	What is commognitive conflict?	26

## Chapter 4

Methodology and design		28
4.1	Methodology	28
4.2	Generalizability and Trustworthiness	31
4.3	Collaborating with teachers	31
4.4	Description of the designed lessons	32
	4.4.1 First lesson. First activity	33
	4.4.2 First lesson Second activity	34
	4.4.3 Fourth Lesson. First activity	36
	4.4.4 Fourth Lesson. Second activity	38
4.5	Data collection	39
4.6	Analytical Framework	40

### Chapter 5

Data of Analysis	
5.1.1 Unit of analysis	44
5.2.1 First teacher (T1). First Lesson. First Activity.	44
5.2.2 Second Activity	47
5.3.1 Second teacher (T2). First Lesson. First Activi	ty. 51
5.3.2 Second Activity	53
5.4.1 First teacher. Fourth Lesson. First Activity.	56
5.4.2 Second Activity	58
5.5.1 Second teacher. Fourth Lesson. First Activity	. 59
5.5.2 Second Activity	61
5.6.1 Findings	62

Chapter 6	
Answer of second research question	63
Analysis of data from the interview	
Chapter 7	
Interpretation of the lessons according	
to Sfard's theory	67
7.1 Interpretation of the lessons according to Sfard's theory	67
7.2 Final Thoughts	72
REFERENCES	75

# List of diagrams

Diagram 1: Four key concepts of mathematical discourse	24
Diagram 2: Geometric schema	24

Diagram 3: Mathematical teaching cycle	30
Diagram 4: Initiating and eliciting	40
Diagram 5: Deed, ritual and exploration	70

#### List of tables

Table	1: Comparison of two types of learning	5
Table	2: Summary table from analytical framework	43
Table	3: T1: Short description of first lesson, first activity	44
Table	4: T1: Summary table for first lesson, first activity	45
Table	5: T1: Short description of first lesson, second activity	47
Table	6: T1: Summary table for first lesson, second activity	48
Table	7: T2: Short description of fist lesson, first activity	51
Table	8: T2: Summary table for first lesson, first activity	51
Table	9: T2: Short description of first lesson, second activity	53
Table <sup>·</sup>	10: T2: Summary table for first lesson, second activity	54
Table <sup>·</sup>	11: T1: Short description of fourth lesson, first activity	56
Table <sup>·</sup>	12: T1: Summary table for fourth lesson, first activity	56
Table <sup>·</sup>	13: T1: Short description for fourth lesson, second activity	58
Table <sup>·</sup>	14: T1: Summary table for fourth lesson, second activity	58
Table	15: T2: Short description of fourth lesson, first activity	59
Table <sup>·</sup>	16: T2: Summary table of fourth lesson, first activity	59
Table <sup>·</sup>	17: T2: Short description of fourth lesson, second activity	61
Table	18: T2: Summary table of fourth lesson, second activity	61
Table	19: Deeds, explorations and rituals – comparison	68

### List of appendices

APPENDIX A – Transcript of the lessons and descriptions for the first teacher APPENDIX B – Transcript of the lessons and descriptions for the second teacher **APPENDIX C** – The interviews' questions

- **APPENDIX D** The interview transcript of the first teacher
- **APPENDIX E** The interview transcript of the second teacher