1 2	Tidal influence on seismic activity during the 2011-2013 El Hierro
3	volcanic unrest
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Key Points:

- We found significant correlations between tides and volcanic earthquakes during specific phases of the 2011-2013 El Hierro unrest.
- Our results support the hypothesis that tidal stresses may modulate seismicity rates on faults subject to magmatic stressing.
 - Tidal modulation sensitivity depends on depth.

Abstract

The El Hierro volcanic unrest started in July 2011, with an increase in observed seismicity rates in and around the island. After the initial onset, hypocenters migrated southward through September 2011 and culminated in a submarine eruption which began on October 10, 2011 and finished in February 2012. However, the seismic activity continued, with remarkable periods of unrest through 2012 and 2013. The most significant episodes of seismic activity during this crisis are related to magma displacements at depth. In this work, tidal stress was calculated at the hypocenter depth for earthquakes from different stages of this crisis, assigning a tidal stress phase angle to each earthquake. We have found statistically significant correlations between the occurrence of earthquakes and certain ranges of tidal stress phase angles in most of the considered scenarios. The analysis of the time period immediately prior to the submarine eruption suggests that tidal compressive stress favored magma displacements towards a shallow magma reservoir. We also found that tidal modulation changes with depth and that the influence of ocean-loading tides is stronger than the influence of solid Earth tides in the correlations. A

model based on different scenarios of tidal stress compression or extension is introduced to
explain the correlations found in the different stages of seismic unrest. Our results support the
hypothesis that tidal stress may trigger earthquakes during volcanic crisis, favoring magma
migration, particularly at shallow depths.

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Plain Language Summary

The El Hierro volcanic crisis started in July 2011, with an increase in observed seismicity rates in and around the island which culminated in a submarine eruption that started the 10th of October and finished in February 2012. The seismic activity continued, with remarkable periods of unrest through 2012 and 2013. Tidal values and functions corresponding to the times and locations of the earthquakes were calculated. We have found significant correlations between earthquakes and tides in most of the considered scenarios. The analysis of the time period immediately prior to the submarine eruption suggests that compressive tides favored magma rising towards shallow depths. A conceptual model is introduced to explain the correlations found in the different stages of seismic unrest. Our results support the hypothesis that tides may trigger earthquakes during volcanic crisis, favoring magma migration, particularly at shallow depth.

1 Introduction

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Lunar and solar tides rhythmically stress Earth at the tidal periods. These cyclic variations, ranging from 10 to 100 hPa (Tanaka, 2010), appear small compared to earthquake stress drops, which lie between 1000 and 10⁵ hPa (Métivier et al., 2009). Nevertheless, tidal stressing is nonlinear in nature and reaches rates of up to 10 hPa/hour, often higher than tectonic stress rates between earthquakes, which reach approximately 0.2 hPa/hour (Emter, 1997). As rapid tidal stresses are superimposed on the far slower, incremental tectonic stresses, they may provide a potential triggering or modulating effect on seismicity rates. As a result, a good deal of research has been carried out that studies the relationship between tides and earthquakes. A detailed review of this subject can be found in the Supporting Information (Text S1). In this work, we study the correlation between tidal stress and seismicity rates during the volcanic crisis that occurred in El Hierro Island (27.7° N; 18.0° W) between 2011 and 2013. El Hierro is both the youngest and the smallest of the Canary Islands and features the highest concentration of volcanoes in the archipelago (García et al., 2014). The most recent eruption prior to 2011 was in 1793 (Carracedo et al., 2001). The structure of the island is based on three volcanic rifts in directions NE, NW and S (Figure 1a), separated by three important gravitational landslides: El Golfo to the north, Las Playas to the east and El Julan to the south (Masson et al., 2002). Gorbatikov et al. (2013) note the existence of a solidified magma reservoir at the northwest part of the island at a depth between 15 and 25 km. The boundary between the crust and the mantle is set at 12 – 16 km (Watts, 1994; Martí et al., 2017). An intricate array of magma pockets at depths between 12 and 30 km may represent the main magma storage system at El Hierro (Stroncik et al., 2009).

The volcanic crisis started in July 2011, with an important increase in seismic activity and ground deformation in El Hierro Island (López et al., 2012; Ibáñez et al., 2012; González et al., 2013). In the first stage, most of the hypocenters concentrated under Tanganasoga volcano and El Golfo valley in the centre and north of the island (Figure 2a). Starting on mid-September, there was a southwards migration of the hypocenters until a submarine eruption occurred offshore of the southern part of the island on October 10-12, 2011 (Figure 2b). After the eruption onset, seismic activity was located in the north around the El Golfo area (Figure 2c). Correlation between gravity variations and tidal vertical strain was observed (Sainz-Maza et al., 2014), suggesting potential tidal triggering of earthquakes during the first days of the eruption. This eruption ended on March 5, 2012 (González et al., 2013). However, the seismic activity continued, with periods of high seismicity and deformation through 2012 and 2013 (García et al., 2014) related to magma migration at depth (see Figure 2d-e).

Because the rates of diffuse CO_2 emissions may vary before events of volcanic activity (Carapezza et al., 2004), estimating the output of this gas has implications in early warning systems applied to volcanoes. In the case of El Hierro Island, diffuse CO_2 emission have been monitored since 1998 (Melián et al., 2014), and especially during the seismo-volcanic crisis that started in July 2011. Through the analysis of these measurements of CO_2 emission, Melián et al. (2014) found two remarkable periods of efflux increase that may be considered as precursory signals. The first one occurred between 29 September and 12 October, i.e., starting almost two weeks prior the beginning of the submarine eruption and ten days before an event of magnitude M = 4.3. The second significant increase in the rate of diffuse CO_2 emission occurred during the period 24 October to 27 November, preceding both the bubbling observed at the sea between 3 and 7 November and the M = 4.6 event recorded on November 11. However, the time series of diffuse

CO ₂ emission in El Hierro Island does not show any correlation to meteorological parameters such
as rain, soil moisture or barometric pressure (see Figure 7 by Melián et al. (2014)).

2 Seismic and volcanic activity related to El Hierro (2011-2013)

Following the analysis of the seismicity by Ibáñez et al. (2012), we can identify different phases in the seismic activity of El Hierro during the period 2011 to 2013, which are related to different spatial settings of the earthquakes or different stages in the magma migration processes.

In this work, we designate all seismicity prior to the eruption occurred on October 10, 2011, as *Phase 1*. This episode starts with an abnormal increase of earthquakes in July 17, 2011 (Figure 2a). During this period, magma is detected as an intrusion in the base of the oceanic crust (around 9.5 km depth), at the south of the main concentrations of earthquakes (González et al., 2013).

Around mid-September 2011, epicenters start migrating to the south of the El Golfo area

Around mid-September 2011, epicenters start migrating to the south of the El Golfo area (Figure 2b). GPS stations detect north-south deformation, suggesting that magma was migrating away from the magma intrusion site (crust-mantle reservoir, CMR (González et al., 2013). Hypocenters are (on average) deeper than before, and average earthquake magnitudes also are greater (Ibáñez et al., 2012). At the end of September, magma began an upward migration, accumulating at a shallower magma reservoir at around 4.5 km depth. This reservoir likely failed around October 8 with an event of magnitude M = 4.3 that opened a path for magma towards the surface (Figure 1b). Later, between October 10 and 12, the submarine eruption began (González et al., 2013).

On 15 October 2011, new seismic activity was located in the north around the El Golfo area. We will consider this a separate stage (*Phase 2*; Figure 2c) in the seismic activity, as these

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earthquakes happen far from the eruption site, in the opposite side of the island. Hypocenters in Phase 2 are deeper than in Phase 1, with a depth range between 15 and 25 km (Ibáñez et al., 2012). Four of the earthquakes that occurred during *Phase 2* show magnitudes M > 4, including an M = 4.6 event recorded on November 11, 2011. The seismic activity decreases progressively through December 2011, although there are some earthquakes during January and February 2012, as well as some visible effects of the submarine eruption on the sea surface. The end of the eruption was officially decreed in March 5, 2012. See González et al. (2013) for a detailed description on the seismic and volcanic activity during *Phases 1* and 2. After the ending of the submarine eruption, new episodes of seismic activity occurred, the most relevant (in terms of number of earthquakes) being those recorded primarily in June-July 2012 and March-April 2013. For the purposes of this research, we will refer to these two crises as *Phase 3* (2012-06-14 to 2012-08-21; Figure 2d) and *Phase 4* (2013-03-17 to 2013-04-30; Figure 2e). Some authors think that there is oceanographic and geochemical evidence that the seismic activity in *Phase 3* is coincident in time with submarine volcanic activity offshore the western coast of El Hierro (Pérez et al., 2014; García-Yeguas et al., 2014), but this volcanic activity must be interpreted in terms of magma injection processes that do not necessarily culminate in an eruptive process (Blanco et al., 2015; Pérez et al., 2015). There is no evidence of new eruptions near El Hierro island after the one that occurred between October, 2011 and March, 2012, although several authors do suggest that the magmatic processes around El Hierro island continued after the conclusion of that eruption (García et al., 2014). Hypocenters in *Phase* 3 are located under the west wing of the island, whereas events in *Phase 4* are, on average, the most distant from the island. It is during *Phase 4* that the strongest seismic activity took place, in

addition to the largest magnitude earthquake (M = 4.9) and the greatest number of landslides (García et al., 2014).

3 Study of the seismicity and Earth tides correlation

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3.1 Earthquake data

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Seismicity data related to the El Hierro volcanic crisis were obtained from the Spanish Geographical Survey, IGN [www.ign.es]. Our main data source is a catalog featuring all earthquakes within the period 17/07/2011 - 31/12/2013, and including event number, date, time, latitude, longitude, depth, intensity, magnitude, magnitude type and location area. Very low magnitudes are excluded because the location of small earthquakes may be affected by significant errors, especially in a small island like El Hierro (García et al., 2014). Therefore, we used only earthquakes with magnitude $M_c > 1.5$, where M_c is the minimum magnitude of completeness based on a frequency-magnitude distribution analysis using the Maximum Curvature (MAXC) technique (Mignan and Woessner, 2012). In addition, in the case of the earthquakes that occurred during *Phase 1*, we used the catalog of Domínguez Cerdeña et al. (2014), where all events previous to the submarine eruption with magnitude $M \ge 1.5$ were relocated using program hypoDD (Waldhauser and Ellsworth, 2000), which improved the precision in the location of earthquakes by as much as 10 times. This relocated catalog also is accessible from the IGN website. The best-fitting double-couple fault plane solution for a set of observed first motion polarities is provided only for one event, so fault mechanisms will not be considered in this study.

Application of the declustering algorithm of Reasenberg (1985) to the catalog shows that for each one of the four phases there exists one big cluster which includes 90 - 95 % of the

events that occurred during that phase. The list of parameters used in the declustering process (van Stiphout et al., 2012) can be found in the Supporting Information (Table S1). Figure 3 shows the location of the earthquakes in each *cluster C1 – C4*. A visual comparison between Figure 2 and Figure 3 suggests that, in every *Phase i* (i = 2,3,4), most of the events not belonging to the corresponding *cluster Ci* may be a remnant or continuation of previous phases, implying that they are not necessarily related to the magma movements or physical processes which originated each phase. As a result, only the events in the *clusters C1 – C4* have been considered here, as we are going to study the possible modulation effects of tides on seismicity in each one of the four phases independently.

Tidal stress and strain were calculated for the locations of all events in each cluster, in order to estimate statistical correlations for tidal modulation of the occurrence of earthquakes in the different phases of the seismic crisis.

3.2 Calculation of tides

In order to obtain the tidal stress at the earthquake locations, it is necessary to consider both the solid tide and the ocean tide. In addition, the calculation must include the depth of the events. Strains derived from the solid tides at depths less than 25 km are not significantly different from surface strains but strains due to the ocean loading component may change significantly between the surface and a depth of 25 km (Thomas et al., 2012).

Our method uses the software package SPOTL (Agnew, 2012) for the calculation of tidal strains. Body tides are calculated on an elastic Earth following Munk and Cartwright (1966). The ocean tidal model we have used is osu.tpxo72atlas (Agnew, 2012), which is a hydrodynamic

model assimilating altimetry data from TOPEX/Poseidon and Jason. It combines three basin-wide solutions (Atlantic Ocean 2011-atlas, Pacific Ocean 2011-atlas and Indian Ocean 2011-atlas), each one of which also incorporates a set of high-resolution local models. Tidal waves considered in the study are M_m , M_f , Q_1 , Q_1 , Q_1 , Q_1 , Q_1 , Q_2 , Q_2 , Q_2 , Q_2 , Q_3 , Q_4 . The original SPOTL codes where modified to use depth-dependent Green functions in the calculations, following the methodology described in Royer et al. (2015) for the modeling of tidal strains at depth. Then tidal stresses are derived from tidal strains following Hooke's law for a tridimensional isotropic body (Fischer et al., 2006), with Poisson's ratio $\nu = 0.25$ and rigidity $\mu = 30$ GPa. We consider positive stress as extension.

To study the correlations between tides and earthquakes, we assign a phase angle, ϕ , to each event, which can be evaluated later in statistical terms. For this purpose, a golden section search routine (Press et al., 1992) is used to estimate the extreme tidal values closest to the time of occurrence of the event. Finally, we assign the phase angle ϕ to the earthquake by linear interpolation, assuming the time distance between two tidal peaks defines a complete cycle of 360° (see Figure 4).

3.3 Statistical methods

The Schuster test was used in order to determine whether there is a non-random distribution of the calculated tidal phases (Emter, 1997). In this test, each *i*-th earthquake is assigned a unit length vector in the direction of the phase angle ϕ_i . The modulus R of the vector sum \mathbf{R} over the total number of earthquakes N_{tot} is given by

$$R^{2} = \left(\sum_{i=1}^{N_{tot}} \cos \phi_{i}\right)^{2} + \left(\sum_{i=1}^{N_{tot}} C \sin \phi_{i}\right)^{2}$$

$$\tag{1}$$

where C is a factor correcting local asymmetries in tides (Wilcock, 2009). It must be noted that no significant tidal asymmetries where found in El Hierro in the time periods considered in this study, as all C values observed for tidal strain or tidal stress are in the range 1 ± 0.0020 .

Then, the probability P_s that the phase distribution to be non-random is estimated by

$$P_s = \exp\left(\frac{-R^2}{N_{tot}}\right). \tag{2}$$

 P_s represents the significance level with which to reject the null hypothesis that the earthquake phase angles represent a completely random distribution. Small values of P_s (< 0.05) indicate the existence of a high correlation between tidal stress and the occurrence of earthquakes.

As we are treating highly clustered seismicity, we are not dealing with independent earthquakes. Given the high sensitivity of the Schuster test (Emter, 1977), that means the catalog may be biased in a way that favors the rejection of the null hypothesis. One way to assess the significance of the observed P_s values is the use of a Monte Carlo permutation test (Noreen, 1989; Fortin and Jacquez, 2000). For each of the four *clusters C1 – C4* we order the earthquakes according to their phase angle ϕ , and we divide them into segments (phase angle ranges) of equal length (different segment lengths are tested, see next section). Then, a number *NSIM* of simulations (e.g., 10000 simulations) are performed for each cluster with the segments in random

order, obtaining a probability value P_s * according to the Schuster test for each simulation.

Finally, for each cluster we count the number NSIG of random simulations in which the P_s *

value obtained is lower than the P_s value of the original distribution of events. The ratio

$$MC_{sl} = \frac{(NSIG+1)}{(NSIM+1)} \tag{3}$$

provides the significance level of our test (Noreen, 1989).

In addition, the American Statistical Association (ASA) expresses concern regarding the hypothesis testing based on *p*-values, stating that these practices are prone to generate false positives (Wasserstein and Lazar, 2016). Bayarri et al. (2016) propose a simple alternative to the use of *p*-values in testing null hypothesis, based on the Bayes factor *B*, which is defined as

$$B = \frac{average\ likelihoo\ of\ the\ observed\ data\ under\ the\ alternative\ hypothesis}{likelihoo\ of\ the\ observed\ data\ under\ the\ null\ hypothesis} \tag{4}$$

Although B may be difficult to compute, it can be approximated by an upper bound \overline{B} which is a

function of the p-values obtained with the usual statistical tests used in testing hypothesis.

According to Bayarri et al. (2016), and considering the Schuster test as the appropriate one for

our null hypothesis testing:

$$B \le \overline{B} = \frac{1}{-eP_S \log P_S} \tag{5}$$

Here we use the p-values P_s calculated by means of the Schuster test to derive this upper bound \overline{B} of the Bayes factor B. According to Bayarri et al. (2016), the standard significant threshold for rejecting the null hypothesis when using this Bayesian alternative is $\overline{B} > 16$. The use of this Bayesian method is a new application to the assessment of correlations between tides and earthquakes, and it has implications for earlier studies of tidal triggering of

seismicity where the statistical significance was primarily based on *p*-values.

4 Results

Results for the application of the Schuster test to the earthquake clusters defined in section 3.1 are shown in Table 1. The upper bound \overline{B} of the Bayes factor B is also shown in Table 1 in order to compare results. According to the Schuster test, very high correlation ($P_s < 0.05$) appears in three of the four *clusters* (C1, C3 and C4) between tidal confining stress (i.e., the trace of the tidal stress tensor) and the occurrence time of earthquakes. However, when we consider the value of the upper bound of the Bayes factor, only the correlations for *clusters* C1 and C4 are statistically significant.

Table 2 shows the results of a Monte Carlo permutation test (10000 simulations) applied to the earthquake *clusters* C1-C4, following the methodology explained in section 3.3. For each

the earthquake *clusters C1-C4*, following the methodology explained in section 3.3. For each *cluster*, the corresponding catalog has been divided into 72 segments of 5° width. Different segment sizes may produce different results, because the greater the segment length is, more patterns from the original distributions are repeated in the simulations and the number of possible permutations diminishes (Bhatnagar et al., 2016). As a result, a catalog divided into 144 segments of 2.5° width was also tested (see Table 2). According to this permutation test, the

correlation is statistically significant for *clusters C1*, C3 and C4, although the value of the significance level, MC_{sl} , provided for cluster C3, is clearly higher (implying a weaker statistical significance) than those obtained for *clusters C1* and C4. On the other hand, the random shuffling of segments in *cluster C2* distribution produces a great number of P_s * values lower than the original P_s value for both segment lengths considered here, meaning that the correlation is not statistically significant.

Figure 5 shows the histograms of the frequency distributions of tidal confining stress phase angles for *clusters C1*, *C2*, *C3* and *C4*, respectively. In these histograms, earthquakes are collected in phase angle ranges of 30° width. The sinusoidal curve applied to the frequency distributions is obtained by least squares fitting of the expression

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$$P(\phi) = P_0 + P_1 \cos(\phi - \alpha),$$
 (6)

where ϕ is the phase angle, P_0 is the mean frequency, P_1 is the amplitude of the curve and α is the phase of the curve (Tanaka et al., 2002). A triangle marks the peak of the fitted curve associated to the histogram, which occurs on the phase angle maximizing eq. (6).

Figure 5a shows that the histogram corresponding to cluster C1 (coincident with Phase 1 in the seismic crisis, i.e., all the seismicity prior to the starting of seismic tremor signal) is clearly biased towards the right side of the phase angle axis, the phase range where tidal stress is increasing ($180^{\circ} < \phi \le 360^{\circ}$). The fitted curve peaks around phase angle $\phi = 251^{\circ}$. As seen in Tables 1 and 2, the correlation between confining tidal stress and the occurrence of earthquakes in cluster C1 is remarkably high for every statistical test. The histogram corresponding to cluster C2 (Figure 5b) does not show a statistically significant correlation with any of the applied

methods, although the most populated phase angle range is $270^{\circ} < \phi \le 300^{\circ}$. Cluster C3		
corresponds to <i>Phase 3</i> , the seismic activity recorded during June-August 2012 under the		
northwest rift. According to the Schuster test and the Monte Carlo permutation test, there also is		
high correlation between tidal stress and the occurrence of earthquakes, although both the P_s		
statistical and the ratio MC_{sl} are not as conclusive as those obtained for <i>cluster C1</i> . Besides, the		
correlation is not significant if we consider the application of the upper bound \overline{B} of the Bayes		
factor B (Table 1). The fitted curve for cluster C3 distribution has a peak around $\phi = 209^{\circ}$ (Figure		
5c). Finally, the histogram obtained from <i>cluster C4</i> data (Phase 4, which includes the seismicity		
observed during 2013 March-April and expanding offshore eastwards) is similar to the <i>cluster</i>		
C1 histogram, with a distribution biased towards the phase angle range where confining tidal		
stress is increasing (180° < $\phi \le 360$ °), and a fitted curve whose peak lays around $\phi = 288$ ° (Figure		
5d). All the statistical tests considered for <i>cluster C4</i> data suggest very high correlation (Tables 1		
and 2).		
As some of the distributions (namely the histograms corresponding to <i>clusters C1</i> and <i>C4</i>)		
show an apparent bias towards phase range $180^{\circ} < \phi \le 360^{\circ}$, a simple binomial test (see e.g.,		
Wonnacot and Wonnacot, 1977) was performed in order to evaluate if the events are more prone		
to happen in the increasing-tide half cycle (180° < $\phi \le 360$ °) rather than in the decreasing-tide		
half cycle (0° < $\phi \le 180$ °). The results of applying that test to the four clusters appear in Table 3,		
showing very high correlation in the cases of <i>clusters C1</i> and <i>C4</i> , and a poor correlation (not		
statistically significant) for <i>clusters C2</i> and <i>C3</i> . The upper bound \overline{B} of the Bayes factor B has		
also been calculated for the probability value P_i derived from the binomial test (Table 3).		

5 Discussion

The initial results from the statistical tests (Tables 1, 2, and 3) and the analysis of the phase angle distribution (Figure 5) suggest that the earthquakes belonging to *clusters C1* and *C4* are highly correlated with tidal confining stress, supporting the hypothesis that tidal stress may trigger earthquakes, especially in the case of events related to volcanic areas (Rydelek et al., 1988; Emter, 1997), and therefore facilitate the magma migration process. The absence of correlation in the case of *cluster C2* may be due to the fact that most of the seismicity belonging to that period of time (2011-10-17 to 2012-01-01) may be related to the collapse of deep sections of the magma plumbing system as magma withdrew (Martí et al., 2013; González et al., 2013), instead of produced by a progressive magma migration process (González et al., 2013) as in *Phase 1 (cluster C1)*, or the post-eruption *Phase 4 (cluster C4)*, which was also associated with migration of magma (García et al., 2014).

Finally, the correlation between earthquakes and tidal confining stress in the events belonging to *cluster C3* is doubtful. The probability values corresponding to the Schuster test and

belonging to cluster C3 is doubtful. The probability values corresponding to the Schuster test and the Monte Carlo permutations test are statistically significant based on the commonly-used 0.05 threshold, even though they are higher (implying a weaker correlation) than the values obtained for clusters C1 or C4. But if we consider the value of the upper bound \overline{B} of the Bayes factor B (Table 1), where the threshold for statistical significance is $\overline{B} > 16$, the result is no longer significant. Nevertheless, the earthquakes in cluster C3 occurred during the post-eruption process we are calling *Phase 3*, where magma migration also occurred (García et al., 2014), so a weak correlation should not be ruled out.

It should be noted that there are differences in the frequency distributions obtained for the different *clusters* (Figure 5). The peak of the sinusoidal curve lies around tidal stress phase angle

$\phi = 288^{\circ}$ (i.e., close to the maximum tidal stress) in the histogram related to <i>cluster C4</i> (Figure
5d). For the <i>cluster C1</i> histogram it is centered at $\phi = 251^{\circ}$ (i.e., halfway between minimum tidal
stress and maximum tidal stress; Figure 5a), while the histogram for cluster C3 is around $\phi =$
209°, close to the minimum tidal stress, although still in the increasing leg of the tidal stress
frequency distribution (Figure 5c). These differences may be due to the different types of focal
mechanisms controlling the seismicity in the clusters and/or also related to the depth of the
earthquakes, as controlled by magma location.

As suggested elsewhere (Tanaka, 2002; Xu et al., 2011), the trend of the correlation between tidal stress and the occurrence time of earthquakes may vary according to the type of fault. Due to the lack of information about focal mechanisms in the earthquake catalog used, an analysis of tidal stress triggering according to faulting type in the El Hierro volcanic crisis is beyond the scope of this work, but it should be considered in the future, if additional information becomes available.

Figure 6 provides additional information about tides and seismicity in the context of the submarine eruption occurred at the end of *Phase 1*. We have calculated tidal volume strain in the setting of the shallow reservoir (latitude 27.6653°, longitude -18.0370°, depth 4.5 km; see González et al., 2013) at two-hour intervals during the time period covered by *Phase 1*, and we have compared it to the number of earthquakes in *cluster C1* recorded every two hours during the same time period.

The plot is divided in two parts, with the beginning of the southward migration of earthquakes on September 15, 2011, marking the separation between the two. During the first period (Figure 6a; 2011-07-15 to 2011-09-14) no clear correlation appears between the biggest earthquake swarms recorded and the highest (or lowest) tidal amplitudes in the fortnightly

period. In fact, most of the swarms seem to occur when the upper envelope of the tidal strain		
amplitudes graph is low (or the lower envelope is high), which seems counter-intuitive. On the		
other hand, in the second period (Figure 6b; 2011-09-15 to 2011-10-15) it is obvious that the		
most significant episodes of seismic activity prior to the submarine eruption of October 10, 2011		
began around September 26, 2011, when the tidal volume strain graph is close to its extreme		
values. This also is the time when magma begins the upward migration towards the shallower		
magma reservoir, as shown by González et al., (2013), which suggests that tidal strain can trigger		
earthquakes favoring magma migration at shallow depths. Similar figures covering Phase 2,		
Phase 3 and Phase 4 are provided as Supporting Information (Figures S1 – S3).		
In order to investigate tidal triggering in the period immediately prior to the submarine		
eruption, we divided the <i>cluster C1</i> in two <i>sub-clusters</i> : <i>C1A</i> (2011-07-21 to 2011-09-25) and		
C1B (2011-09-26 to 2011-10-10, starting with the upward movements of magma to the shallower		
reservoir). The results of the application of the statistical tests to <i>sub-clusters C1A</i> and <i>C1B</i> are		
summarized in Table 4, whereas the histograms of the frequency distributions of confining tidal		
stress phase angles are shown in Figure 7.		
As in cluster C1, both sub-clusters C1A and C1B show high correlation between confining		
tidal stress and the occurrence time of earthquakes (Table 4), but there is a significant difference		
between both distributions. The peak of the fitted curve lies around tidal stress phase angle ϕ =		
279° (which is halfway between minimum tidal stress and maximum tidal stress, although closer		
to the maximum) in the histogram related to sub-cluster C1A (Figure 7a). For the sub-cluster		
C1B histogram, it lies around $\phi = 216^{\circ}$ (i.e., close to the minimum tidal stress), with a large		
number of events concentrating on the tidal phase range $150^{\circ} < \phi \le 210^{\circ}$, central to the		
distribution (Figure 7b). As we consider tidal stress positive in extension, minimum tidal stress is		

indeed maximum tidal stress in compression. This suggests that, during the period of upward migration of magma towards the shallower magma reservoir, tidal compressive stress favors these magma displacements and the subsequent seismic activity. Figure S4 in Supporting Information features a study of tidal confining stress amplitudes corresponding to the earthquakes in *sub-clusters C1A* and *C1B* which supports this interpretation.

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These results suggest that there are different tidal modulations of the seismic events related to magma ascent, depending on the depth. In order to continue testing the sensitivity of the correlation to depth, we have focused on tidal confining stress, and we have considered 15 km depth as a threshold, as the boundary between the crust and the mantle lies at 15-16 km in the vicinity of the Canary Islands (Watts, 1994). In sub-clusters C1A and C1B, where most of the events belong to the depth range 10 – 15 km, high correlation is found between confining tidal stress and the occurrence time of earthquakes (see Table 4). In cluster C2, where the vast majority of events are > 15 km depth, there is no statistically significant correlation with tides, as seen in Tables 1 and 2. In *cluster C3*, where, again, the great majority of hypocenters are in depth values > 15 km, the correlation is clearly lower than in *sub-cluster C1A* or *sub-cluster C1B* (see Tables 1 and 2). Finally, in *cluster C4* we have considered two *sub-cluster*: *C4A* (earthquakes with hypocenters in the depth range between 0 and 15 km, 526 events), and C4B (earthquakes with depth > 15 km, 1556 events). Table 5 shows the results of the application of the statistical tests defined in section 3.3 to both sub-clusters C4A and C4B. In all cases, sub-cluster C4A gives a high correlation with tidal confining stress that is better than the one obtained for the whole cluster C4 (as seen in Tables 1 and 2). Figure 7c shows the histogram of the frequency distribution of tidal confining stress phase angles for sub-cluster C4A. The most populated tidal phase range is $240^{\circ} < \phi < 270^{\circ}$, and the peak of the fitted curve lies around tidal stress phase

angle $\phi = 300^{\circ}$, a value quite close to the maximum of the fitted curve corresponding to the entire cluster C4 (Figure 5d). On the other hand, there is no statistically significant correlation with tidal confining stress for *sub-cluster C4B* (Table 5). These results suggest that tidal stress correlation with the origin times of the earthquakes is better for events whose hypocenters are at crustal levels.

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So far, our results suggest that there is a correlation between tidal stress values and the occurrence of earthquakes during the 2011 – 2013 volcanic crisis in El Hierro island. But stressing-rate could be the controlling factor, rather than maximum/minimum values. That being the case, the strongest gradients of tidal variations might be more important for triggering of earthquakes than the absolute value of the tidal stress, as it was noted by McNutt and Beavan (1981) and McNutt and Beavan (1984). With that in mind, we calculate tidal confining stress rates corresponding to all earthquake clusters or sub-clusters C1A, C1B, C2, C3, C4A and C4B, and attempt to determine if the events occur more frequently when tidal stress rate is higher. The corresponding histograms appear in Figure 8, and the results for the statistical tests are shown in Table 6. There are three *clusters* with statistically significant values for all the tests defined in Section 3.3, namely C1A (Figure 8a), C1B (Figure 8b) and C4A (Figure 8e). There are no significant correlations between earthquakes and tidal stress rates in the events belonging to clusters C2 (Figure 8c) and C4B (Figure 8f). Finally, the correlation for cluster C3 appears to be statistically significant when using the Schuster test or the Monte Carlo permutations test, but it is not significant when considering the upper bound \overline{B} of the Bayes factor B (Table 6), so this correlation must be considered with caution. In addition, in most of these *clusters* (Figures 8a, 8c, 8d, 8e, 8f), the most frequently occurring phase angle range is the high-tide half cycle ($0^{\circ} < \phi$ $< 90^{\circ}$ or $270^{\circ} < \phi < 360^{\circ}$), where tidal confining stress rates are higher. The exception here is

sub-cluster C1B (Figure 8b), where the highest frequency corresponds to phase angle range 240° 450 $<\phi$ < 270°. It should be noted that, in the time period covered by *sub-cluster C1B*, our previous 451 analysis of tidal strain and stress values suggests that tidal compression plays a key role in 452 earthquake triggering, rather than tidal extension, and this could explain the difference in 453 behavior of sub-cluster C1B. 454 Our analysis of tidal triggering of earthquakes in El Hierro based on tidal stress rate 455 agrees with the results from our previous analysis based on tidal stress values (Tables 1, 2, 4 and 456 5), in the sense that the subsets of events where the statistical significance is poorer are *clusters* 457 C2, C3 and sub-cluster C4B, which are mostly composed of earthquakes > 15 km depth, even 458 though in the case of *cluster C3* the results are still statistically significant for both Schuster and 459 Monte Carlo tests. If we discard *clusters C2* and *sub-cluster C4B* (as they obtain the worst results 460 with all the statistical tests considered), there is an interesting similarity between the frequency 461 distributions of clusters C1A and C4A, and between cluster C3 and sub-cluster C1B. Whereas the 462 maximum of the fitted curve in the distributions of sub-clusters C1A (Figure 8a) and C4A 463 (Figure 8e) lies around extreme values of the tidal stress rate cycle ($\phi = 356^{\circ}$ and $\phi = 11^{\circ}$, 464 respectively), it is centered close to $\phi = 290^{\circ}$ in both frequency distributions for sub-cluster C1B 465 (Figure 8b) and *cluster C3* (Figure 8d). Although the correlation found for *cluster C3* is not as 466 consistent as the one obtained for *sub-cluster C1B* (it is not statistically significant when we 467 apply the Bayesian alternative to p-values) these results may reflect that, in the case of cluster C3 468 and sub-cluster C1B, tidal compression plays an influence in promoting magma movements 469 towards shallow depths. Finally, we have seen that both seismic activities belonging to sub-470 471 cluster C1B and cluster C3 can be related to volcanic activity due to magma injection processes, even though these processes only ended with an eruption in the case of the *cluster C1B* activity. 472

In all the time periods considered in this study, ocean-loading tides are stronger than solid
Earth tides. According to Cochran et al. (2004), tidal stresses due to body tides can reach values
up to 5×10^3 Pa, which is one order of magnitude less than the values that can be reached by
tidal stresses induced by ocean loading tides (5 x 10^4 Pa) in ocean basins. For all the events in the
different clusters in the study, we have calculated half cycle amplitudes (see definition in Figure
4) induced by ocean tidal loading confining stress and half cycle amplitudes due to Earth tidal
confining stress. The former is, on average, between five and six times greater than the latter,
depending on the cluster (see data in the repository
https://zenodo.org/record/3714198#.YDX_OXIPGUI). Therefore, the ocean tidal signal appears
to be more important than the body tidal signal in the modulation of the seismic activity during
the El Hierro volcanic crisis. This result could be of general application in many of the volcanic
events in oceanic islands and should be confirmed with additional, complementary studies.
In order to show if the magnitude cutoff chosen for the catalogs is relevant in the results
obtained, we have performed some of the statistical tests over the catalogs removing all
earthquakes with $M \le 2$. As seen in Table S2 in the Supporting Information, the results are quite
similar to the ones obtained in the original analysis, where $M=1.5$ was the lower magnitude
cutoff. We have not performed the statistical tests over declustered catalogs because, as we have
told in Section 3, this seismicity is highly clustered in such a way that replacing each cluster for
the biggest or the first event in the cluster series results in catalogs with very few elements. An
example is shown in Table S3 in the Supporting Information, where a declustering process using
a cutoff of $M=2.5$ is described. Table S4 in the Supporting Information provides a more detailed
description of the declustered catalogs D1-D4 so produced.

We have tested also possible correlations between earthquakes and strong rains in the
island. Meteorological data are provided by the Spanish Meteorological Agency (AEMET)
(<u>http://www.aemet.es/es/datos_abiertos</u>). Figures S5, S6 and S7 in the Supporting Information
show the comparative between earthquakes and pluviometry during the periods covered by
clusters C1, C2 and C4 (there is no graph for cluster C3 because apparently there was no rain
during that time period). Although some correlation seems to exist between rains and some parts
of the earthquakes sequences (mainly for <i>cluster C4</i> , see Figure S7), it must be noted that the
only data source for the rains is Hierro Aeropuerto Station, which is located at the northeast of
the island and whose data may not be usable for all the locations of the earthquakes.

Our interpretation of the volcano dynamics that generate the various tidal correlations found in this work is detailed in Figure 9. During the time period 2011-07-17 to 2011-09-25 (*sub-cluster C1A*), magma begins to accumulate in the deep CMR, and then migrates longitudinally around the center of the CMR (Figure 9a). In this context, at low tide and the lowering of sea level, the weight of the ocean over the seafloor around the island diminishes, resulting in a decrease in compression and an increase in extension. High values of extensional tidal confining stress rates may favor magma displacement and encourage extensional faulting. The seismic activity related to this time period may be biased to higher values of tidal stress rates. On the other hand, during the period defined by *sub-cluster C1B* (2011-09-26 to 2011-10-10), magma ascends towards the shallower reservoir, which is smaller than the CMR, and accumulates there until the eruption started on October 10, 2011 (Figure 9b). As the longitudinal displacement is almost nonexistent, magmatic activity in the shallow reservoir may be more sensitive to small changes in tidal stress compression. At high tide, sea level rises and the compression exerted on the seafloor by the body of water increases, promoting magma ascent

and the build-up of pressure within the magma chamber. Tidal confining stress compression, together with tectonic and volcanic stresses, would encourage magma to migrate into zones of weakness to ascend, favoring seismic activity in the process. Note that Figure 7b suggests that it is tidal compressive stress which promotes the seismic activity related to this period.

There appears to be no correlation between tides and seismicity during the co-eruption phase, to which the earthquakes in *cluster C2* belong (2011-10-17 to 2012-01-01). As suggested before, one possible reason is that seismicity could have originated with the collapse of deep sections of the magma plumbing system as magma withdrew (Martí et al., 2013; González et al., 2013), rather than being produced by a progressive magma migration process (González et al., 2013). For the correlation between tidal confining stress and earthquakes in *cluster C3*, a mechanism based on tidal compression similar to that described in Figure 9b is a possible explanation, as we know that the earthquakes belonging to that period can be related to volcanic activity due to magma injection processes under the west wing of the island (Blanco et al., 2015). Nevertheless, more research is needed in order to confirm that this correlation is a function of the proposed physical mechanism because the hypocenters in *cluster C3* are at deeper depths than those ones of *sub-clusters C1A* or *C1B*. In addition, the correlation found in *cluster C3* is poorer than those obtained for *sub-clusters C1A* or *C1B*, and it is not statistically significant when we estimate the upper bound of the Bayes factor (Tables 1 and 6).

Finally, a look at the dispersion of the hypocenters of the events in *cluster C4* (see Figure 3d) suggests important magma displacements in longitude. In this context, the mechanism described in Figure 9a, based on extensional tidal confining stress rates promoting magma displacements and related seismic activity, may provide an explanation to the correlations found for *cluster C4* and the *sub-cluster C4A*. The lack of correlation in the case of *sub-cluster C4B*

(even though its hypocenter distribution is similar to the original *cluster C4*, as seen in Figure S8 in the Supporting Information) may be due to the greater depth of the events when compared to those in *sub-cluster C4A*.

6 Conclusions

In July 2011 a volcanic crisis started in El Hierro Island with an increase in observed seismicity rates in the island, with remarkable periods of unrest through 2012 and 2013, even after the submarine eruption that occurred between October 2011 and February 2012. During the period studied here, hypocenters were migrating spatially. We have studied the correlation within the seismicity and the tidal stress calculated at hypocenter depth for the earthquakes of different stages of this crisis, assigning a tidal stress phase angle to each earthquake. Our results show correlation between tidal stress and the origin times of the earthquakes in the context of volcanic areas, with tides enhancing magma movements at depth, confirming that tidal stress can play a role in the triggering of an eruption if the magma system is in a critical state at shallow depths (Sottili et al., 2007).

Although correlation between residual gravity and body tide vertical strain was found by Sainz-Maza et al. (2014) during the first three days of the eruption, suggesting concurrent tidal triggering during the beginning of the eruption, the work presented here is the first study of the recent volcanic crisis in El Hierro focused on the influence of tides in the seismic activity and covering the most significant phases of the 2011-2013 El Hierro unrest.

Summarizing, we have found that tidal stress values and tidal stress rates are correlated with the occurrence times of the earthquakes in different phases during the volcanic crisis at El

Hierro. In addition, the analysis of the time period immediately prior to the submarine eruption suggests that tidal compressive stress favored magma displacements towards the shallower magma reservoir. Tidal modulation also seems to be dependent on depth. We also determined that the influence of ocean-loading tides is stronger than the influence of solid Earth tides in the correlations presented here. We present a conceptual model (see Figure 9) to explain the different correlations between tides and earthquakes found in the different phases in terms of the influence of tidal compression or tidal extension in the magma movements at depth.

Our results, using tidal strains and stresses calculated for thousands of earthquakes at hypocenter depth, applying depth-dependent Green functions and the most recent ocean models available, agree with some previous studies (e.g., Dzurisin, 1980; Rydelek et al., 1988; Berrino and Corrado, 1991; Kasahara et al., 2001; or Bhatnagar et al., 2016). Some of them also show a different polarity according to compression or extension stress or strain (McNutt and Beavan 1981; 1984; Scholz et al., 2019). Our conclusions support the hypothesis that tides may produce a modulation of the earthquake activity in volcanic areas, in particular when magma arrives to shallow depths.

These results, obtained for the volcanic crisis where the last eruption in Canary Islands took place, should be considered in the study of future volcanic reactivation in the archipelago and other volcanic islands. Implications for volcano hazard monitoring may be important, as seismic monitoring of active volcanoes is one of the primary methods for characterizing activity levels and is a significant factor in assessing associated hazard probabilities. Insights into the impact of tidal forces on the seismic activity on active volcanoes have the potential to improve our understanding of volcano dynamics and better quantify eruption hazard.

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599	Used seismic catalog can be downloaded from IGN website, <u>www.ign.es.</u> The remainder of the
600	data is available in the repository https://zenodo.org/record/3714198#.YDX_OXIPGUI
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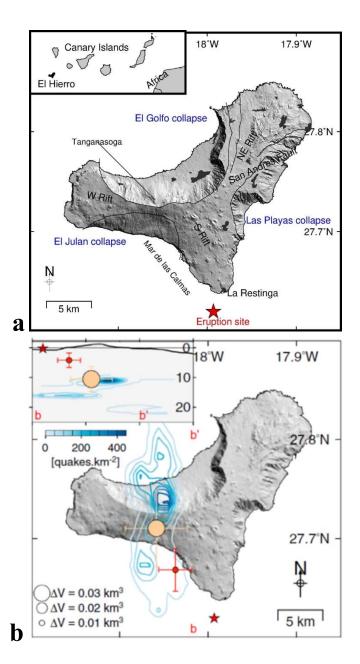


Figure 1. (a) Map of El Hierro Island and the three rift zones (Northeastern, Western-Northwestern, and South-Southeastern) showing topography (shaded topography). Flank collapses and faults are denoted with black lines. Populated areas are shown with gray polygons. Inset: El Hierro (EH) location in the Canary Islands NW of the African continent. Red star indicates the approximate location of the eruption site (same in all map figures). (b) Model of the magma migration process culminating in the submarine eruption in 2011 (October), with the location of the best-fitting spherical point sources: orange, deep crustal source (crust-mantle reservoir, or CMR following the notation by González et al., 2013); and dark red, the shallower crustal reservoir. Seismicity flux (events/km²), which represents the 2-D clustering of background seismicity, is shown the background. Inset shows the vertical cross section b-b' (Modified from González et al., 2013).

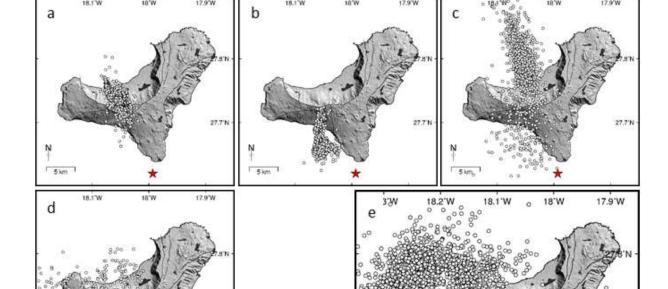


Figure 2. Location of earthquakes that occurred during the different phases detailed in the manuscript: **a)** *Phase 1*, part 1 (2011-07-17 to 2011-09-14); **b)** *Phase 1*, part 2 (2011-09-15 to 2011-10-10); **c)** *Phase 2* (2011-10-15 to 2012-03-05); **d)** Phase 3 (2012-06-14 to 2012-08-21); **e)** Phase 4 (2013-03-17 to 2013-04-30). Only events of $M \ge 1.5$ are shown.

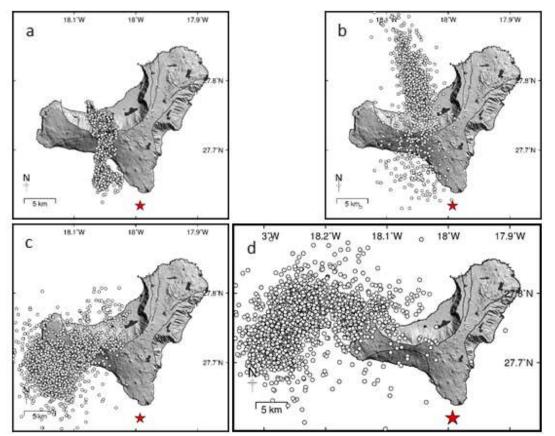


Figure 3. Location of the earthquakes in the four big clusters found in the catalog: **a**) cluster C1, corresponding to Phase 1; **b**) cluster C2, corresponding to Phase 2; **c**) cluster C3, corresponding to Phase 3; **d**) cluster C4, corresponding to Phase 4.

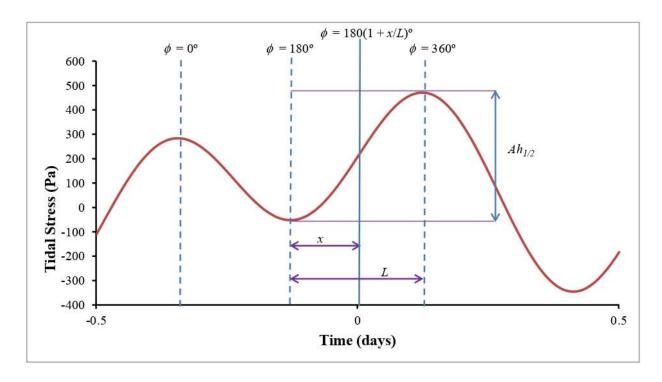
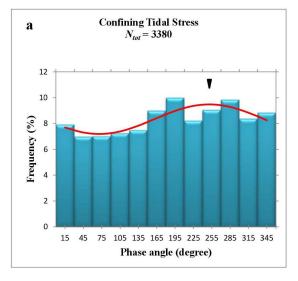
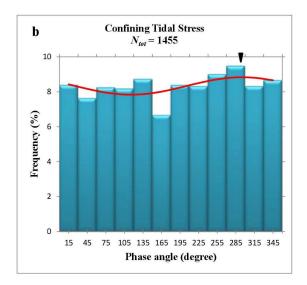
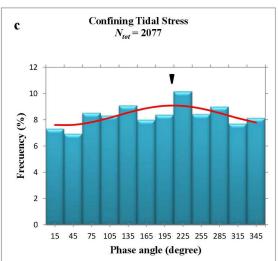


Figure 4. Schematic of the tidal phase method (Wilcock, 2009). The terms $Ah_{1/2}$ and L are the amplitude and time length of the half cycle in which the event occurs, respectively. x is the time difference between the occurrence time of the earthquake and phase $\phi = 180^{\circ}$, positive when the event occurs after phase $\phi = 180^{\circ}$ and negative when it happens prior to phase $\phi = 180^{\circ}$.







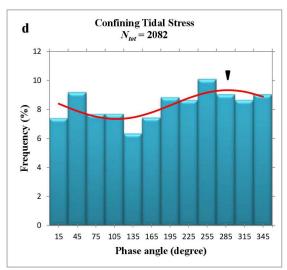
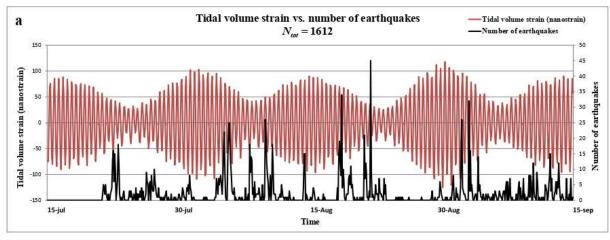


Figure 5. Histograms of the frequency distribution of tidal phase angles for all events in *clusters*: (a) CI (period 2011-07-21 / 2011-10-10); (b) C2 (2011-10-17 to 2012-01-01); (c) C3 (2012-06-25 to 2012-08-13); (d) C4 (2013-03-18 to 2013-04-28). N_{tot} is the number of events of each subset. The curve represents a sinusoidal function fitted to the frequency distribution. The peak of the fitted curve is indicated by a triangle.



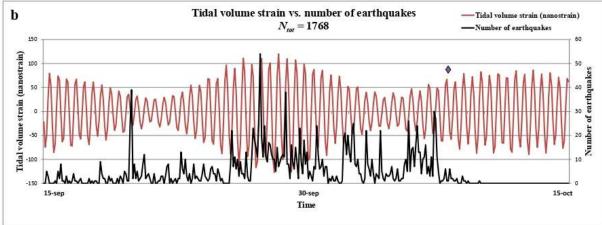
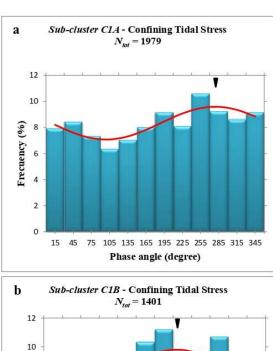
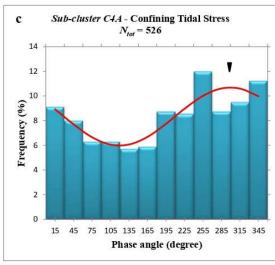
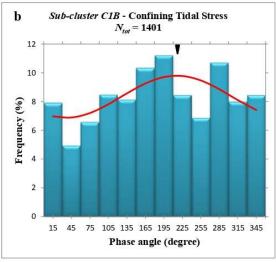


Figure 6. Red line shows tidal volume strain in the setting of the shallow reservoir (see text for details) during a period covering all the seismic activity prior to the submarine eruption (Phase1). Black line represents the number of earthquakes recorded in *cluster C1* every two hours alongside the same time period. The plot has been divided in two parts: (a) 2011-07-15 to 2011-09-14; (b) 2011-09-15 to 2011-10-15. N_{tot} is the number of earthquakes represented in each part. The purple diamond in (b) marks the occurrence of the M = 4.3 earthquake (2011 October 8) which is considered as the event opening a path for the final episode of magma rising towards the surface two days later (González et al., 2013).







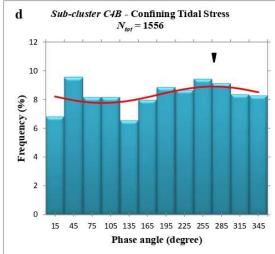


Figure 7. Histograms of the frequency distribution of tidal phase angles for tidal confining stress: (a) for *sub-cluster C1A* (2011-07-17 to 2011-09-25); (b) for *sub-cluster C1B* (2011-09-26 to 2011-10-10). Histograms of the frequency distribution of tidal confining stress phase angles for all events for *cluster C4* according to depth: (c) *sub-cluster C4A*, earthquakes with hypocenters in the depth range between 0 and 15 km; (d) *sub-cluster C4B*, earthquakes with depth greater than 15 km. N_{tot} is the number of events of each subset. The curve represents a sinusoidal function fitted to the frequency distribution. The peak of the fitted curve is indicated by a triangle.

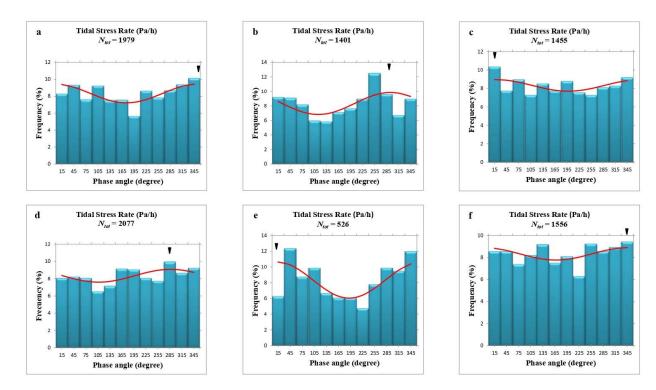
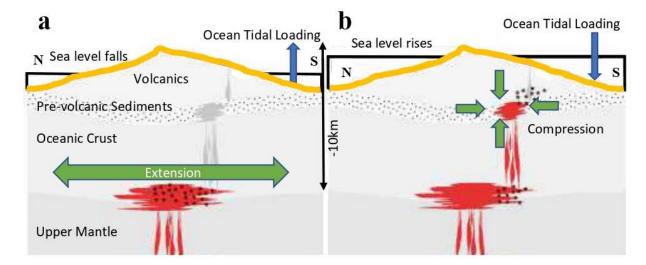


Figure 8. Histograms of the frequency distribution of tidal confining stress rates for all events in *clusters* and *sub-clusters*: (a) C1A (2011-07-17 to 2011-09-25); (b) C1B (2011-09-26 to 2011-10-10); (c) C2 (2011-10-17 to 2012-01-01); (d) C3 (2012-06-25 to 2012-08-13); (e) C4A (2013-03-18 to 2013-04-28, events with depth \leq 15 km only); (f) C4B (2013-03-18 to 2013-04-28, events with depth \geq 15 km only). N_{tot} is the number of events of each subset. The curve represents a sinusoidal function fitted to the frequency distribution. The peak of the fitted curve is indicated by a triangle.



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Figure 9. Schematics of the proposed sequence of volcano activity resulting in the observed correlations between tidal confining stress and earthquakes. (a) Time period 2011-07-17 to 2011-09-25. Magma begins to accumulate in the deep CMR, and then moves longitudinally around the center of the CMR. With low tide, sea level falls and the weight of the ocean over the seafloor of the island diminishes, which means compression decreases and extension increases. High values of extensional tidal confining stress rates may favor the magma displacements and encourage extensional faulting and the seismic activity related to this time period may be related to higher values of tidal stress rates. (b) Time period 2011-09-26 to 2011-10-10. Magma ascends towards a shallow reservoir smaller than the deep CMR and accumulates there until the eruption began on October 10, 2011. With magma concentrated in a reduced volume, magmatic activity in the shallow reservoir may be more sensitive to small changes in tidal stress compression. When the tides are high, sea level rises and the compression exerted on the seafloor by the body of water increases, promoting both magma ascent and the build-up of pressure within the magma chamber. Tidal confining stress compression, together with tectonic and volcanic stresses, would squeeze the magma chamber, escaping through zones of weakness to ascend and favoring seismic activity. (Modified from González et al., 2013)

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Time period	Number of events	P_s value	\overline{B}
2011-07-21 / 2011-10-10	3380	0.3999e-06	62435.7879
2011-10-17 / 2012-01-01	1455	0.1475	1.3033
2012-06-25 / 2012-08-13	2077	0.0112	7.2973
2013-03-18 / 2013-04-28	2082	0.0008	63.1326
	2011-07-21 / 2011-10-10 2011-10-17 / 2012-01-01 2012-06-25 / 2012-08-13	2011-07-21 / 2011-10-10 3380 2011-10-17 / 2012-01-01 1455 2012-06-25 / 2012-08-13 2077	2011-07-21 / 2011-10-10 3380 0.3999e-06 2011-10-17 / 2012-01-01 1455 0.1475 2012-06-25 / 2012-08-13 2077 0.0112

Table 1. Results of the application of Schuster's test and calculation of the upper bound \overline{B} of the Bayes factor B to the earthquake *clusters C1-C4*. P_s is the probability that the phase angle distribution to be random, according to Schuster's test. \overline{B} is derived from P_s according to expression (5). Occurrences where $P_s < 0.05$ or $\overline{B} > 16$ are in bold. Type of tidal stress considered is confining.

			Segment les	ngth: 5°	Segment lengt	th: 2.5°
Cluster	Number of events	P_s value	NSIG $(P^* \le P_s)$ for 10000 permutations	SL MC_{sl}	NSIG $(P^* \le P_s)$ for 10000 permutations	SL MC_{sl}
C1	3380	0.3999e-06	1	0.0002	0	0.0001
<i>C2</i>	1455	0.1475	1767	0.1768	1911	0.1912
<i>C3</i>	2077	0.0112	279	0.0280	140	0.0141
<i>C4</i>	2082	0.0008	22	0.0023	13	0.0014

Table 2. Results of the application of Schuster's test and a Monte Carlo permutation test (10000 simulations) to the earthquake *clusters C1-C4*. Different segment lengths were applied^a. P_s is the probability that the phase angle distribution in the original catalog to be random, according to Schuster's test. For each permutation, a Schuster probability value P^* is obtained. NSIG is the number of permutations where $P^* \le P_s$ for each cluster. SL means "significance level". The significance level MC_{sl} of the permutation test is obtained according to expression (3) in section 3.3. Occurrences where $P_s < 0.05$ or $MC_{sl} < 0.05$ are in bold.

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Cluster	$N_{i,obs}$	$N_{i,obs}/N_{tot}$	P_i	\overline{B}
C1	1835	0.5429	0.33e-06	74696.6798
C2	759	0.5216	0.0520	2.3923
<i>C3</i>	1076	0.5181	0.0522	2.3865
C4	1129	0.5423	0.62e-04	612.4390

Table 3. Results of the binomial test for the confining tidal stress in the seismic crisis of El Hierro. N_{tot} is the number of events of each subset. $N_{i,obs}$ is the number of events observed in the increasing-tide phase angle half cycle (180° < $\phi \le 360^{\circ}$). P_i is the probability of getting a number of increasing-tide phase angle events greater or equal to the observed number $N_{i,obs}$, assuming the null hypothesis that earthquakes are not influenced by tidal stress. \overline{B} is derived from P_i according to expression (5). Occurrences where $P_i < 0.05$ or $\overline{B} > 16$ are in bold.

	Time period	No. of			Segment len		ngth 5° Segment length 2.5°	
Cluster	Time period	events	P_s value	B	NSIG $(P^* \le P_s)$ for 10000 permutations	SL MCsl	NSIG $(P^* \le P_s)$ for 10000 permutations	SL MCsl
CIA	2011-07-17/ 2011-09-25	1979	0.6514e-04	585.9	35	0.0036	4	0.0005
C1B	2011-09-26/ 2011-10-10	1401	0.1633e-04	2043.8	8	0.0009	0	0.0001

Table 4. Results of the application of the statistical tests described in the text to the earthquake *clusters C1A* and *C1B*. P_s is the probability that the phase angle distribution to be random, according to Schuster's test. \overline{B} is derived from P_s according to expression (5). For each permutation, a Schuster probability value P^* is obtained. NSIG is the number of permutations where $P^* \le P_s$ for each cluster. SL means "significance level". The significance level MC_{sl} of the permutation test is obtained according to expression (3) in section 3.3. Occurrences where $P_s < 0.05$, $\overline{B} > 16$ or $MC_{sl} < 0.05$ are in bold. Type of tidal stress considered is confining.

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	er Time period	Number period of events			Segment length 5°		Segment length 2.5°	
Cluster			P_s value	\overline{B}	NSIG $(P^* \leq P_s)$ for	SL	NSIG $(P^* \leq P_s)$ for	SL
					10000 permutations	MC_{sl}	10000 permutations	MC_{sl}
C4A	2013-03-18 /	526	0.6458e-04 5	590.4	7 0.00	0.0008	2	0.0003
C4A	2013-04-28			390.4	/	0.0000	Z	
C4B	2013-03-18 /	1556	0.1578	1.2	2054	0.2055	1629	0.1630
	2013-04-28							

Table 5. Results of the application of the statistical tests described in the text to the earthquake *clusters C4A* and *C4B*. Ps is the probability that the phase angle distribution to be random, according to Schuster's test. \overline{B} is derived from P_s according to expression (5). For each permutation, a Schuster probability value P^* is obtained. NSIG is the number of permutations where $P^* \le P_s$ for each cluster. SL means "significance level". The significance level MC_{sl} of the permutation test is obtained according to expression (3) in section 3.3. Occurrences where $P_s < 0.05$, $\overline{B} > 16$ or $MC_{sl} < 0.05$ are in bold. The type of tidal stress considered is confining.

	No.			Segment length	5°	Segment length 2.5°	
Cluster	events	P_s value	\overline{B}	NSIG $(P^* \leq P_s)$ for	SL	NSIG $(P^* \leq P_s)$ for	SL
	CVOILES			10000 permutations	MC_{sl}	10000 permutations	MC_{sl}
CIA	1979	0.3395e-04	1052.9	15	0.0016	1	0.0002
C1B	1401	0.1394e-04	2360.3	8	0.0009	3	0.0004
<i>C2</i>	1455	0.1226	1.4	2103	0.2104	1714	0.1715
<i>C3</i>	2077	0.0132	6.4	454	0.0455	289	0.0290
C4A	526	0.4524e-04	812.8	12	0.0013	1	0.0002
C4B	1556	0.1220	1.4	1771	0.1772	1319	0.1320

Table 6. Results of the application of the statistical tests described in the text considering tidal stress rates (Pa/h). P_s is the probability that the phase angle distribution to be random, according to Schuster's test. \overline{B} is derived from P_s according to expression (5). For each permutation, a Schuster probability value P^* is obtained. NSIG is the number of permutations where $P^* \le P_s$ for each cluster. SL means "significance level". The significance level MC_{sl} of the permutation test is obtained according to expression (3) in section 3.3. Occurrences where $P_s < 0.05$, $\overline{B} > 16$ or $MC_{sl} < 0.05$ are in bold. The type of tidal stress considered is confining.