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Microscale Processes and Dynamics during CH₄–CO₂ Guest-Molecule Exchange in Gas Hydrates

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Abstract: The exchange of CH₄ by CO₂ in gas hydrates is of interest for the production of natural gas from methane hydrate with net zero climate gas balance, and for managing risks that are related to sediment destabilization and mobilization after gas-hydrate dissociation. Several experimental studies on the dynamics and efficiency of the process exist, but the results seem to be partly inconsistent. We used confocal Raman spectroscopy to map an area of several tens to hundreds μm of a CH₄ hydrate sample during its exposure to liquid and gaseous CO₂. On this scale, we could identify and follow different processes in the sample that occur in parallel. Next to guest-molecule exchange, gas-hydrate dissociation also contributes to the release of CH₄. During our examination period, about 50% of the CO₂ was bound by exchange for CH₄ molecules, while the other half was bound by new formation of CO₂ hydrates. We evaluated single gas-hydrate grains with confirmed gas exchange and applied a diffusion equation to quantify the process. Obtained diffusion coefficients are in the range of 10^{−13}–10^{−18} m²/s. We propose to use this analytical diffusion equation for a simple and robust modeling of CH₄ production by guest-molecule exchange and to combine it with an additional term for gas-hydrate dissociation.

Keywords: gas hydrate; CH₄ hydrate; CO₂ hydrate; mixed-gas hydrates; guest-molecule exchange; solid-state diffusion; conversion mechanism; Raman spectroscopy; laboratory experiments

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1. Introduction

Gas hydrates are crystalline compounds in which a basic structure composed of water molecules forms different types of cages that contain small gas molecules. Those enclathrated molecules are termed guest molecules. Natural gas-hydrates host predominantly biogenic methane as a guest molecule and occur at high pressures as well as low to moderate temperatures either in continental margin sediments overlain by at least several hundred meters of water or in permafrost soil [1]. During the past three decades, marine natural gas hydrates have increasingly gained attention. Depending on the focus of consideration, they are either regarded as a potential unconventional resource of natural gas [2–4], a potential hazard due to their global warming-induced dissociation whereby the potent greenhouse gas CH₄ is released and the geomechanical stability of the seafloor is weakened [5], or as a means to store CO₂ as an immobile mineral [6]. A much-discussed strategy for tackling the aforementioned three aspects of natural-gas production, carbon-dioxide sequestration, and geohazard mitigation, is the in situ exchange of the guest molecule CH₄ with the guest molecule CO₂ [7], hereafter termed gas exchange. The swapping of the two molecules is thermodynamically favored [8,9], takes place spontaneously, and has several benefits:

- The use of fossil natural gas as an energy resource produces CO₂. Hence, it is not the ideal choice for a society that is under pressure to mitigate global warming. By

sequestering CO₂ in gas hydrates during the methane-production process, the carbon footprint of the natural gas can be significantly decreased or even become negative (i.e., more CO₂ is stored than is being produced from burning the methane).

- Pressure reduction in the hydrate reservoir is presently considered to be the most economically feasible and least technologically complex strategy for gas production from gas hydrates [10]. When the pressure falls below the stability pressure, the gas hydrates dissociate and the released gas can be produced. A drawback of this production strategy is the endothermic nature of gas-hydrate dissociation [11]. The reservoir cools down and the effect of the pressure decrease is counteracted by a temperature reduction that drives the system back into the thermodynamic gas-hydrate stability field. CH₄–CO₂ exchange, on the other hand, is a slightly exothermic process [8] and therefore avoids the problem of reservoir cooling. Therefore, combining pressure reduction with gas exchange is considered to be a promising production strategy: while gas hydrate dissociation ensures a rapid mobilization of the CH₄ as a gas phase, guest-molecule exchange or rapid reformation of CO₂-rich gas hydrates can balance the energy consumption of the dissociation process. This approach has already been tested on a larger scale during the 2012 Ignik Sikumi field test [12,13] by injecting a mixture of N₂ and CO₂ gas into the reservoir.
- Gas hydrates increase the geomechanical stability of their host sediment [14,15]. When load-bearing gas hydrate is removed during gas production, the sediment can be mobilized and an uncontrollable sand production can occur, as observed in 2013 during a field test in the Nankai Trough, Japan [16]. In the worst case, collapsing or slumping of the continental margin sediments can result in a general geomechanical hazard. Gas exchange, on the other hand, preserves the crystal structure of gas hydrate, thereby preventing the loss of sediment stability.
- Gas-hydrate dissociation occurs when the thermodynamic parameters of the environment change to values outside of the gas-hydrate stability region. This could be triggered during gas production from gas hydrates, but also by warming bottom water temperatures [5]; by pressure reduction due to, for example, isostatic rebound after postglacial melting of ice sheets [17]; or rapid sedimentation events, such as those encountered in active channel–levee systems [18]. Since CO₂ hydrates are thermodynamically more stable than CH₄ hydrates at a range of relevant temperature and pressure conditions [1], it has been discussed whether a proactive change of the gas hydrate composition by gas production in combination with hydrate conversion could mitigate potential risks from dissociation of gas hydrates occurring near equilibrium conditions.

Despite the apparent benefits of CH₄–CO₂ hydrate conversion, laboratory-scale experiments revealed several problems: While some hydrate-conversion experiments seemed to confirm the feasibility of the concept [19,20], other researchers observed an unfeasibly slow exchange process (e.g., [21,22]). Moreover, the published results for exchange efficiencies and exchange kinetics vary widely (e.g., see listed comparisons in [21,23]). This is partly due to the fact that most experiments were not conducted at comparable conditions, which highlights a strong effect of initial conditions (e.g., gas-hydrate grain sizes) and process parameters. It is obvious that the interpretation of the experiments and understanding of the overall process is less straight forward than initially thought. For example, the existing state of knowledge at the time of the Ignik Sikumi gas-hydrate production test, in which depressurization of the reservoir was combined with hydrate conversion, was not sufficient to model the production results [13].

The molecular mechanism of the guest-molecule exchange is subject to discussions. The driving force for the exchange is the difference in the chemical potential of molecules in the gas hydrate and in the surrounding fluid phase [24]. This chemical potential difference initiates a fast exchange of molecules at the gas-hydrate surface, which is in direct contact with the fluid. Results from molecular dynamics simulations indicate that

the direct contact layer could be exchanged within 20 nanoseconds [25]. Following the fast exchange converting the surface of the hydrate grain, the CO₂ molecules need to migrate into the cages of the solid crystalline structure inside of the gas-hydrate grain, and an outbound migration through the crystal lattice is required for the CH₄ molecules. This solid-state diffusion (also termed “solid-state percolation” because of the relatively high mobility of the enclathrated molecules compared to conventional solid materials) depends mainly on the deviation of the system from the thermodynamic equilibrium, the thermal energy of the molecules, and the activation energies of the respective steps of the migration process. These steps can include, for example, lattice reorientations, lattice destruction, and reformation or defect hopping. Proposed mechanisms include a complete dissociation and reformation of the crystal lattice [26], the formation of a secondary CO₂ hydrate layer on top of the primary CH₄ hydrate grain with subsequent breaking and reformation of the underlying lattice structure [27], the dissolution and replacement of the outermost gas-hydrate shell of the primary grain with subsequent diffusion into a mostly intact crystal lattice [28], or the migration of guest molecules through holes in the cage walls after the outermost shell of the gas-hydrate grain had been dissolved and replaced by an amorphous CO₂ hydrate [29]. These mechanisms have mostly been derived from computer simulations. Although they are partly consistent with experimental observations, there is no direct experimental proof for any of the proposed concepts.

A full quantitative evaluation of laboratory experiments, which would facilitate a detailed understanding of the dynamic conversion process, is difficult due to the high complexity of the ongoing processes. The sample itself contains a multiple and sometimes even a changing number of phases. Besides the solid gas-hydrate phase, there needs to be a fluid CO₂-rich phase that can be either gaseous or, at high pressures, liquid. Depending on the experimental concept, an initial aqueous phase with or without additives like salt ions, and a solid matrix, e.g., sediment, could also be present. The CO₂ and the released CH₄ mix with a gas phase and can be dissolved in liquid phases. When solubilities are exceeded, additional gaseous or liquid phases occur. An initially pure CO₂ phase would not only trigger a gas-exchange process, but would dissolve a fraction of the other molecular components of the sample, namely CH₄ and water, in order to reach its equilibrium composition. H₂O can dissolve to a few mol % in CO₂ liq [30], and gas-hydrate decomposition is highly likely to occur until the solubility equilibrium is reached. The situation at the gas-hydrate grain surface can be even more complex. Released CH₄ from dissolving or exchanging gas hydrates is postulated to form microbubbles [31] at the gas-hydrate surface, which would further complicate the description of concentration gradients, component availabilities, and phase distributions. If sufficient amounts of all necessary gas-hydrate-forming molecules are present, either from primary phases or from gas-hydrate dissolution, secondary gas hydrates can form. All of these processes may occur locally and can, therefore, cause significant heterogeneities inside of the sample volume. Dissociation and formation of gas hydrates may result in a local depletion or oversaturation of the involved molecular components. The exothermic (formation and gas exchange) or endothermic (dissociation) nature of the processes changes the local temperature while gas released from gas-hydrate dissociation or gas consumption from gas-hydrate formation influences the pore pressure. In summary, the processes that take place following CO₂ injection into CH₄ hydrates are highly complex, coupled and depend on a multitude of parameters that might vary on the micro or even the submicro scale. A thorough description of the sample evolution would require the knowledge of at least the following properties and parameters: the shape and radius of the gas-hydrate grains; the distribution of all phases and their constituents in space and time; the solubilities of minor constituents in the fluid phases; the thermal properties and diffusive, convective, and advective transport properties for all components; porosities; surface potentials; gas-hydrate phase boundaries; occupancies of the gas-hydrate cages; local (partial) pressure and temperature; and the energy budget of the involved processes. Obviously, not all of the above-listed parameters are accessible during laboratory experiments. Basic thermodynamic and

kinetic parameters are compiled in books as well as review articles and can, for example, be found in [1,14,23,32].

Although there has been a substantial effort by some researchers to precisely control and standardize as many sample properties as possible (e.g., [33]), there is still no experimental setup that allows for a complete characterization of the sample on all relevant scales before, during, and after the exchange. Depending on the experimental setup and the chosen observation techniques, different aspects of the sample and the exchange kinetics can be measured. Phase distributions in gas-hydrate-bearing samples have been measured with magnetic resonance imaging (MRI) (e.g., [34–36]), X-ray computed tomography (X-ray CT) (e.g., [37,38]), and electrical resistivity tomography (ERT) [39], in which MRI images molecules in mobile phases, CT discriminates between sample components with sufficiently different atomic numbers, and ERT allows differentiation between more or less conductive materials. None of these techniques can determine the relative amount of CO₂ or CH₄ in a phase. These properties can only be indirectly deduced from phase transitions that can be attributed to specific component compositions. For the measurement of phase compositions, gas chromatography (GC) (e.g., [21,40–42]), solid-state nuclear magnetic resonance (NMR) spectroscopy (e.g., [43–45]), neutron diffraction (e.g., [33,46]), and Raman spectroscopy (e.g., [20,22,26,45,47]) have been employed. GC measures the abundance of the different molecules in a produced gas phase, while NMR spectroscopy and neutron scattering aim to assess the solid gas-hydrate phase. Raman spectroscopy, on the other hand, is able to obtain spectra from all of the involved phases. With the exception of confocal Raman spectroscopy, all of these techniques measure bulk properties of the sample. But from the above discussion it is likely that the conversion process is heterogeneous and might involve several simultaneously occurring processes like gas-hydrate dissociation and reformation [26], and the existence of different types of gas hydrate in parallel [48,49]. In this case, the measurement of bulk parameters would average over these processes and the results cannot be attributed exclusively to gas exchange. Pointwise measurements can be obtained with focal-point spectroscopy techniques like confocal Raman spectroscopy [50]. Their results are more meaningful for a singled-out process, but they might not be representative for the overall sample behavior. With bulk measurements, general CO₂ retention and CH₄ production rates, as well as the overall efficiency of the hydrate conversion, can be measured, while the kinetics and efficiency of a specific process could only be achieved from a local measurement.

Our goal was to investigate which processes take place and to what extent during CH₄–CO₂ exchange in gas hydrates, and to single out the direct gas exchange for a quantification of the guest-molecule replacement dynamics. To achieve this goal, spectral mapping was performed on grids that extended several 100 μm in the *x* and *y* directions. This way, we could follow changes in gas-hydrate composition on a sample region that exceeded several grain sizes. We performed four hydrate-conversion experiments: one with and three without constant flow of the liquid phase. Raman spectroscopic mapping revealed a highly heterogeneous sample evolution, including gas-hydrate dissolution, formation of different types of secondary gas hydrates, and gas exchange. This result could explain some of the disputed findings from other published experiments. Gas exchange on single gas-hydrate grains could be fitted with a regular diffusion equation, and trends in the diffusion coefficients could be restrained.

2. Materials and Methods

The methodologies of the four hydrate-conversion experiments cover different experimental protocols and procedures. During one of the experiments, hereafter termed “*Flow*”, a steady flow of liquid CO₂ was pumped through a sediment/CH₄ hydrate matrix. The initial CH₄ hydrate was formed from gas-saturated water inside of the sample cell. Three other experiments were conducted with a static gaseous CO₂ phase. In one of the experiments, hereafter termed “*NoFlow*”, the initial CH₄ hydrates were also formed from CH₄-saturated water. Pressure and temperature conditions were close to the gas/liquid

phase boundary, but no condensation was observed, and Raman spectroscopy confirmed the presence of a gaseous CO_2 phase. In the other two experiments, CH_4 hydrates were formed from exposure of ice grains to a CH_4 gas atmosphere. These experiments were termed “NoFlowI1” and “NoFlowI2”. The necessity to perform the experiments within the stability range of all involved gas hydrates demands that the samples are cooled and pressurized. Figure 1 shows a phase diagram for CH_4 hydrate, CO_2 hydrate, and CO_2 [32,51,52]. Phase boundaries for CH_4 - CO_2 mixed-gas hydrates are located between the respective phase boundaries for the pure gas hydrates [7,53,54]. The experimental conditions of the four experiments are marked inside the phase diagram. Experiment *NoFlow* was performed at 271.85 K and 3.47 MPa. The *NoFlowI1* experiments were measured at 272.05 K and 2.94 MPa (*NoFlowI1*) and 272.15 K and 2.96 MPa (*NoFlowI2*), respectively. The realization of experiment *Flow* required different parameters: a complete freezing of the sample or fast formation of secondary gas hydrates needed to be prevented in order to avoid a blockage of the flow-through cell. Hence, this experiment was performed at a higher temperature and consequently required a higher sample pressure for gas-hydrate stabilization. Temperature and pressure of this experiment were 281.15 K and 13 MPa, respectively.

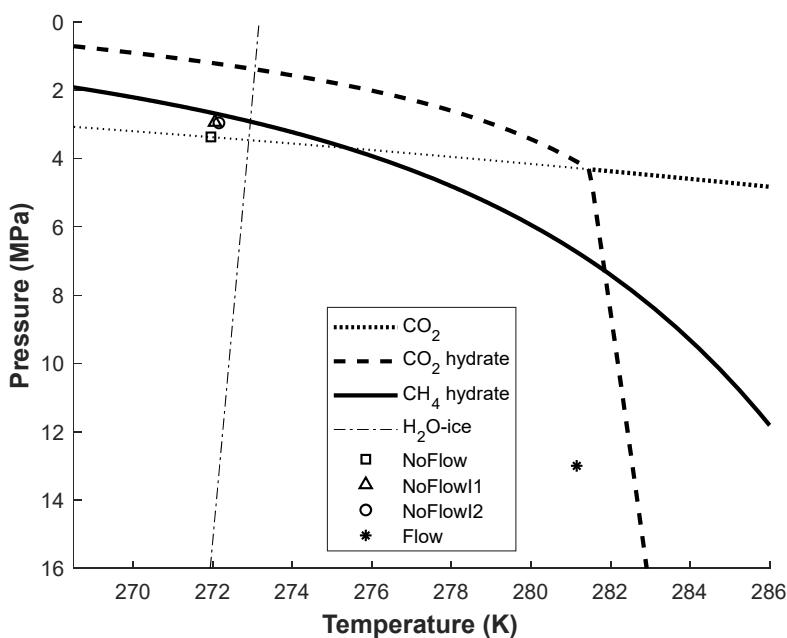


Figure 1. The CO_2 gas/liquid phase boundary, the water/ice Ih phase boundary [55], and phase boundaries for CH_4 hydrate and CO_2 hydrate in the pressure and temperature range relevant to the presented experiments. The liquid CO_2 phase and gas hydrates exist below the respective curves at higher pressures. Experimental conditions are marked with symbols.

2.1. Pressure Cells

Two different pressure cells were used in the experiments (Figure 2). Both cells were specifically designed for Raman spectroscopy experiments at pressure and temperature conditions that correspond to conditions in natural gas-hydrate reservoirs. The more basic cell, termed the “standard cell”, was used for the experiments without flow and is a stainless-steel cell with a sample chamber volume of 1 mL. It is fitted with ports for gas inlet, gas outlet, and a temperature sensor. A 6 mm-thick quartz glass window is inserted in the cell cap to allow visual inspection of the sample and nondestructive analysis by Raman spectroscopy. The cell incorporates a heat exchanger circulating cooling liquid and can be operated at temperatures between 273 and 293 K and pressures up to 10 MPa.

The second cell, termed the “flow-through cell”, was designed for flow-through experiments. It consists of a PEEK pressure housing with a long tubular cell of 6 mL volume,

hosting 5 sapphire windows arranged along the cell. It is fitted with ports for fluid inlet and fluid outlet. This cell can sustain pressures of up to 15 MPa and temperatures can be controlled in the range from 273 to 303 K. It is thermally coupled to a copper heat exchanger circulating a cooling liquid.

When cooled, a jet of N₂ gas is blown over the pressure cell window in order to avoid condensation of moisture from the ambient air.

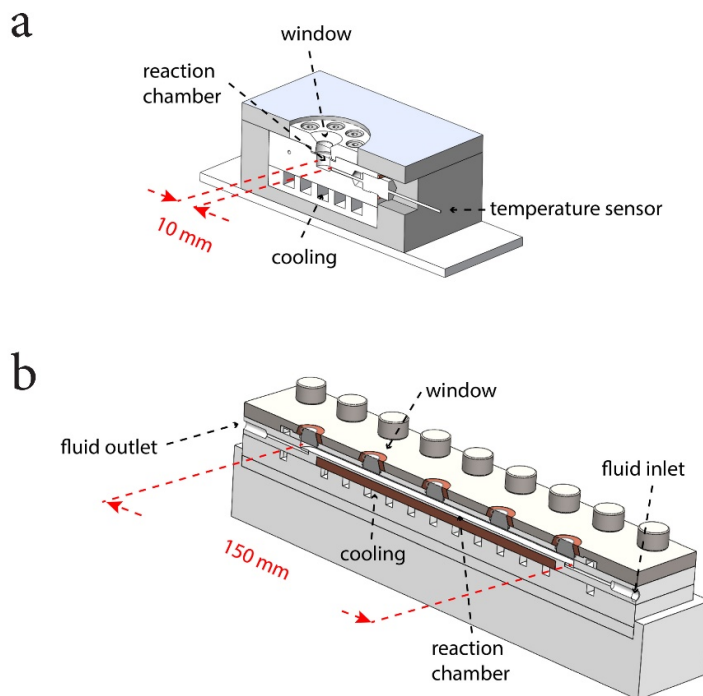


Figure 2. Cross sections of pressure cells for gas-hydrate-exchange experiments. (a) Standard cell for static operation. Fluid inlet and outlet are located in the left half of the cell (not shown). (b) Flow-through cell.

2.2. CH₄ Hydrate Formation

For the experiments *NoFlow11* and *NoFlow12*, CH₄ hydrate was derived from ice grains that were exposed to a CH₄ gas atmosphere (CH₄ 4.5, Air Liquide Deutschland GmbH, Düsseldorf, Germany). Deionized water was filled in a spray bottle and sprayed into liquid nitrogen. The derived ice grains were sieved to obtain different size fractions. Ice grains with diameters ranging from 100 to 200 µm were filled directly into the standard pressure cell (experiment *NoFlow11*) or into a capillary that was placed in upright position in the cooled standard pressure cell (experiment *NoFlow12*). Some quartz grains were added to the surface of the sample. The Raman spectra of quartz were used for calibration of the spectrometer and for monitoring and correction of spectral shifts during the measurement period. The pressure cell was flushed four times with CH₄ and then pressurized to 10 MPa at 255 K in a freezer. After two days, the cell was transferred to the Raman spectrometer and connected to a Julabo F30C chiller (Julabo, Seelbach, Germany) for temperature control and to a CH₄ gas supply for pressure control. The sample was repeatedly cycled through the freezing point of water at temperatures between 274 K and 275 K for an additional 1–2 days. Then, pressure and temperature were lowered to the experiment settings and the sample was allowed to equilibrate for one day. The distribution of CH₄ hydrate at the sample surface was mapped with Raman spectroscopy in selected field of views (FOVs) and one or two FOVs were chosen for repeated measurements during the exchange experiment.

In the experiment *NoFlow*, CH₄ hydrate was formed from CH₄-saturated water. First, 500 mL deionized water was filled into a stirred reactor (Parr Instrument Company, Moline, IL, USA) and pressurized with CH₄ to 9.5 MPa at room temperature (297 K). The standard pressure cell was connected to the reactor and filled with gas-saturated water. Over a period of 5 days, the sample temperature was cycled twice between 275 K and 270 K. Subsequently, the sample was left at 270 K for an additional 22 days. Gas-hydrate formation was confirmed by mapping of selected sample areas with Raman spectroscopy. From these maps, suitable FOVs for hydrate conversion monitoring were chosen.

CH₄ hydrates in the experiment *Flow* were also derived from CH₄-saturated deionized water. The flow-through pressure cell was packed with quartz sand with a mean grain size of 0.29 mm and a modal grain size distribution (G20TEAS, Schlingmeier, Schwülper, Germany) and cooled to 268 K. Then, 500 mL of deionized water was pressurized in the stirred reactor with CH₄ gas at room temperature (291 K) to 15 MPa and the gas-saturated water was circulated through the cell with a flow rate of 1 mL/min. After three days, gas-hydrate formation caused the sample to clog, stopping the flow. The temperature was raised stepwise to 274 K over three days to resume the flow. CH₄ hydrate formation was confirmed by Raman spectroscopy mapping at cell windows 2, 3, and 4. Suitable FOVs for monitoring of the exchange experiment were identified in window 4, downstream of the cell center. The circulation of CH₄-saturated fluid was stopped after an additional 60 days.

2.3. CH₄-CO₂ Exchange Experiments

We used a LabRAM HR 800 confocal Raman microscope (Horiba Jobin Yvon, Bensheim, Germany) to map the gas-hydrate conversion. Exchange experiments with the standard cell were started by reducing the CH₄ gas pressure to the specified experiment pressure and by adjusting the temperature to about 272 K. CO₂ gas (CO₂ 4.5, Air Liquide Deutschland GmbH, Düsseldorf, Germany) was then pumped through the sample with a Teledyne ISCO syringe pump (Teledyne ISCO, Lincoln, NE, USA) for a few minutes and the exchange of the gas phase was monitored with Raman spectroscopy. When the signal of the gaseous CH₄ had disappeared, all valves were closed. Before the inflow of CO₂, a Raman map of the initial CH₄ hydrate distribution was taken. After the gas phase exchange finished, Raman spectral maps were measured either continuously or during selected time periods. The spectral range of the maps was alternated among 139 cm⁻¹ to 2270 cm⁻¹ for the CH₄ signal and 2211 cm⁻¹ to 3953 cm⁻¹ for the CO₂ and OH bands. The Raman parameters for the experiments are listed in Table S1. The *NoFlowI* experiments were measured with a fast imaging mode (DuoScan and SWIFT mode of the spectrometer) in which the size of the Raman laser beam was expanded by a vibrating mirror to several tens of μm in the *x* and *y* planes (DuoScan), and measurements were taken not pointwise, but during constant movement of the sample through the laser beam (SWIFT). In contrast to the strictly confocal pointwise measurements, in which a pixel of the spectral map represents only a few μm of the sample and there is no information from areas in-between two grid points, the pixel in spectral maps from those fast imaging techniques include signal from the full area between grid points.

The flow-through experiment was performed at a higher sample temperature of 281.15 K to avoid a clogging of the cell by the potential formation of ice or a fast secondary gas-hydrate formation near the fluid inlet of the cell. CO₂ was injected by a Teledyne ISCO syringe pump with an inlet pressure of 13 MPa and a flow rate of 0.02 mL/min. After 7 h of injection, the sample clogged due to CO₂ hydrate formation and the pump switched off. The flow could be resumed after a holding period of 13 h, but the cell clogged again after 2 h of operation and the flow could not be reinstalled during a second holding period of 3 h. Then, 25 h after the start of CO₂ injection, the temperature was increased to 283 K and the operation could be continued.

2.4. Evaluation of Raman Data

The peaks of the measured Raman spectra were fitted with linearly weighted Gaussian–Lorentzian line shapes (pseudo-Voigt) using the spectrometer software (Labspec 6, Horiba Jobin Yvon, Bensheim Germany). Peaks of CH₄ and CO₂ in the gas, liquid, and gas-hydrate phases differ in position and in peak width and can therefore be distinguished [56,57]. The peak areas were exported from the Labspec software, and data from different time points were merged with a Matlab script (The Mathworks, Nattick, MA, USA). Gas-filled areas of the sample were identified, and from these areas, a noise threshold for the gas-hydrate signals was generated. Signal values smaller than the threshold were set to zero. Obvious outliers of the data were removed after visual inspection. All maps were inspected for potential shifts in *x* or *y* due to inaccuracies of the *xy*-table movement, and recognized shifts were corrected. Afterward, the maps were cut to the area that was covered in all shifted maps of the series. Then, the final maps for CH₄ and CO₂ hydrates were subtracted from the first maps. All pixels with gas hydrates in the first and/or the final map were attributed a process according to the following criteria:

- CH₄ hydrate dissociation: no CO₂ hydrate signal and decreasing CH₄ hydrate signal
- Secondary (sec.) CH₄ hydrate formation: no CO₂ hydrate signal and increasing CH₄ hydrate signal
- Secondary (sec.) CO₂ hydrate formation: no CH₄ hydrate signal and increasing CO₂ hydrate signal
- Secondary (sec.) mixed-hydrate formation: increasing CH₄ hydrate signal and increasing CO₂ hydrate signal
- Gas exchange Type 1 (CH₄ exchanged with CO₂): decreasing CH₄ hydrate signal and increasing CO₂ hydrate signal

For the evaluation of the second period of the *Flow* experiment (CO₂ flow halted after clogging of the pressure cell), additional processes had to be defined. The initial signals of this time series correspond to the signals at the beginning of the hold period and include CO₂ hydrates and mixed hydrates that formed during the first flow period. Hence, the transformation of these additional phases needs to be considered:

- CO₂ hydrate dissociation: no CH₄ hydrate signal and decreasing CO₂ hydrate signal
- Mixed-hydrate dissociation: both gas hydrate signals initially present; decreasing CH₄ hydrate signal and decreasing CO₂ hydrate signal
- Gas exchange Type 2 (CO₂ exchanged with CH₄): CO₂ hydrate signal initially present; increasing CH₄ hydrate signal and decreasing CO₂ hydrate signal

The signal of all pixels of a map with the same attribute was summed up in order to follow the time evolution of the respective processes. In the case of CH₄ hydrate, the signal was normalized to the total initial CH₄ gas-hydrate signal. For the CO₂ hydrate signal, the normalization was not that straightforward: The experiment was not run long enough to reach the equilibrium concentration of CO₂. Hence, the signal could not be normalized to the signal of the final steady state, but was normalized to the total signal of the last map of the experiment. Unfortunately, this did not allow us to relate the inventory changes to the initial gas-hydrate content, but the observed trends were clear and continuous, and we expect that the derived conclusions are still relevant.

Cage occupancy ratios of CH₄ molecules in large cages and small cages in the CH₄ hydrate lattice were calculated from the equation:

$$cr = \theta_L/\theta_S = (A_L \times F_{MS})/(3A_S \times F_{ML}), \quad (1)$$

where A_L and A_S are the fitted peak areas for large cage signals and small cage signals, respectively; θ are cage occupancies for large (*L*) and small (*S*) cages; and the *F* factors are the quantification factors $F_{ML} = 1.01$ and $F_{MS} = 1.12$ [58]. The cage occupancies are related to the overall numbers of large cages and small cages, respectively. Both CH₄ and CO₂ gas hydrates, as well as mixed hydrates of these gases, are structure 1 (S1) gas hydrates. Hence, there is no structural change and only a minor change in the lattice constant from 11.83 to 11.82 during the transition [46]. The factor 1/3 in the equation accounts for the fact

that the number of large cages in the SI structure is three times the number of small cages [1].

For the evaluation of the gas-exchange process, single gas-hydrate grains with confirmed gas exchange were selected, and the signal evolution on these grains was evaluated separately.

2.5. Evaluation of Gas-Exchange Dynamics

Confocal Raman measurements collect the signal from restricted volumes within the gas-hydrate grain. Since the movement of the guest molecules through the gas hydrate grain is considered to be a solid-state diffusion process, we used the analytical solution of the diffusion equation [59] in spherical coordinates to derive the concentration of the compound $C(r,t)$ as function of time t and radius r [60,61]. For the outward-migrating CH_4 , we get:

$$C(r,t) = C_0 \left[1 - 2 \sum_{j=1}^{\infty} (-1)^{j-1} \frac{\sin\left(j\pi \frac{r}{R_0}\right)}{j\pi \frac{r}{R_0}} e^{-\frac{j^2\pi^2 D}{R_0^2} t} \right], \quad (2)$$

and for the inward-migrating CO_2 , we derive:

$$C(r,t) = C_0 \left[1 - 2 \sum_{j=1}^{\infty} (-1)^{j-1} \frac{\sin\left(j\pi \frac{r}{R_0}\right)}{j\pi \frac{r}{R_0}} e^{-\frac{j^2\pi^2 D}{R_0^2} t} \right], \quad (3)$$

where j is an index, C_0 is the initial concentration, D is the diffusion coefficient, R_0 is the grain radius, and r is the radial position of the focus point in the grain. Regression parameters for this equation are C_0 , r/R_0 , and D/R_0^2 . The measured signal was normalized to the initial signal and C_0 was allowed to vary between 0.9 and 1.1 to account for noise.

The CO_2 signal turned out to be too noisy for a reliable regression of the data and the final concentration of C_0 was unknown since the experiments were aborted before the equilibrated CO_2 concentration was reached. Errors of the regression parameters tended to be larger than the parameters itself. Therefore, a proper quantification of the CO_2 diffusion into the gas-hydrate grains was difficult. Data regression was feasible when the parameter r/R_0 was adapted from the regression results of the CH_4 data, but the resulting diffusion coefficients are less certain than the CH_4 diffusion coefficients.

3. Results

In the following subsections, we describe the results from the four different experiments.

3.1. Experiment NoFlow

Twenty-four sets of spectral maps (CH_4 and CO_2 maps) were measured during the experiment *NoFlow*. The first map was started directly after the pressurization with CO_2 . Eight more map sets were measured during the time period of 22.7 to 28.9 h after the start of the CO_2 exchange, and a set of two spectral maps was derived every 54.5 min. Fifteen maps were measured during the time period of 34–95.2 h after the start of the CO_2 exchange. Here, a set of maps was derived every 74 min due to an additional waiting time between map acquisitions. The map size was $130 \mu\text{m} \times 130 \mu\text{m}$ and Δx and Δy between

two points of the map were both $4.06 \mu\text{m}$. The number of grid points was 32 in each direction, resulting in a total of 1024 spectra per map. After correction for spatial shifts, the map size had to be reduced to 23×29 pixels and a FOV of $93.4 \mu\text{m} \times 117.7 \mu\text{m}$.

Figure 3 shows the initial CH_4 hydrate map and CH_4 and CO_2 hydrate maps after 29, 60, and 91 h. A number of CH_4 hydrate grains, which, due to the restricted resolution, are not clearly outlined, can be seen in the upper 2/3 of the map. The increase in CO_2 hydrate signal in this region did not affect all grains, but occurred mainly between 20 and $50 \mu\text{m}$ in x and 0 and $40 \mu\text{m}$ in y . Other areas show different processes. An increase of CH_4 hydrate can be observed in the upper-left corner, and an increase in both CH_4 hydrate and CO_2 hydrate took place in the lower-right corner, indicating the formation of secondary mixed-gas hydrate. Dissociation of CH_4 hydrate was, for example, taking place in a region close to the coordinate $x = 70 \mu\text{m}$ and $y = 30 \mu\text{m}$. Secondary CO_2 hydrate formation can be observed rapidly after CO_2 injection in the lower third of the map, but did not increase much over time.

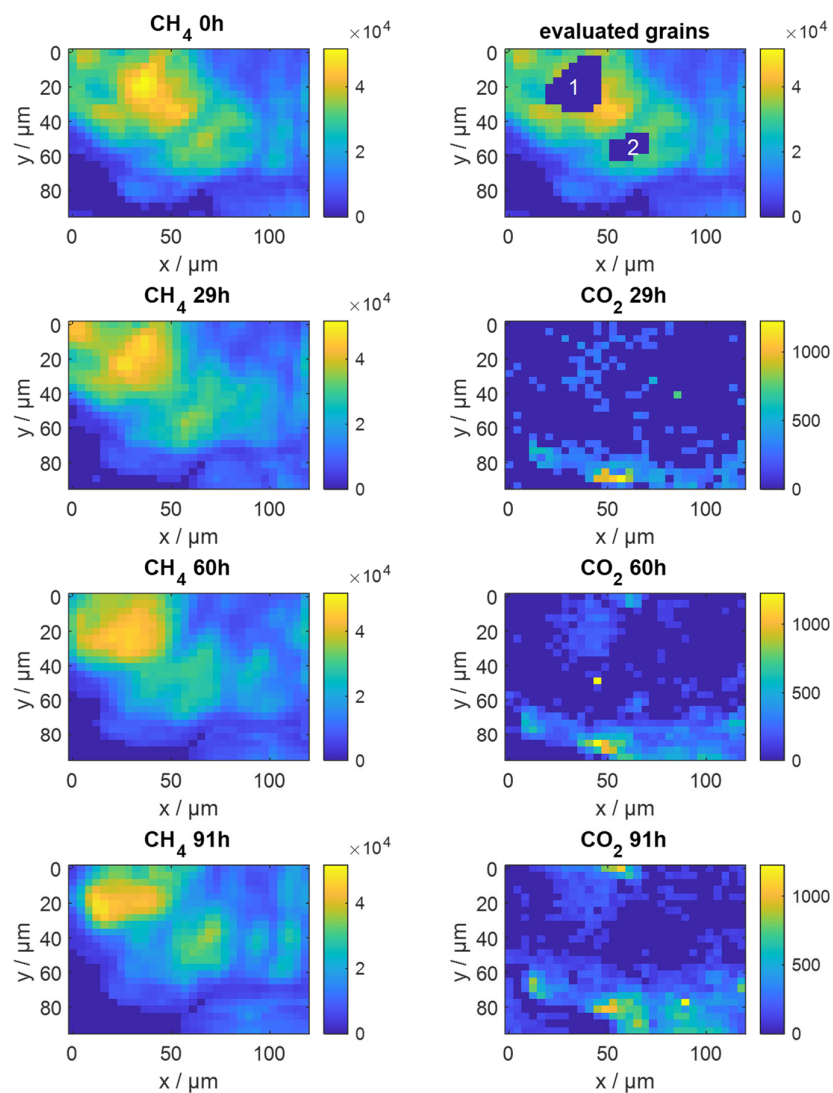


Figure 3. CH_4 and CO_2 hydrate maps of experiment *NoFlow* at times 0 h (only CH_4 hydrate), 29 h, 60 h, and 91 h. Signal intensities are shown in arbitrary units. The location of the two selected gas-hydrate grain areas for gas-exchange evaluation are marked as blue areas in the upper-right map.

Figure 4 shows the time development of the ongoing processes in the FOV. At $t = 0$, only CH_4 hydrate signal was present. The total CH_4 hydrate signal decreased to 79% of its

initial strength in 95 h. As outlined in Section 2.4, all pixels of the gas-hydrate maps were evaluated with respect to signal changes and attributed to a matching formation, dissociation, or exchange process. The time evolution of signals from sample areas with the same specific process is also shown in Figure 4. The first values of these curves represent the fraction of the initial CH_4 hydrate signal that will be changed by the specific process in the course of the experiment. Consequently, the starting values of all CH_4 hydrate processes add up to 1 (or 100%, with rounding errors only 99% in this specific case). In theory, the starting values for the secondary gas-hydrate-formation processes should be zero. In reality, they can be nonzero due to noise or because the secondary gas hydrates overgrow existing CH_4 hydrate structures, which still contribute to the signal as long as the covering layer is thin enough for the laser beam to pass through. In this case, the first value of the curve represents the signal from CH_4 hydrates, which will be overgrown by secondary gas hydrates. The difference between the first and the last value of the curves for the different processes depicts the fraction of the overall signal change that is caused by the respective process.

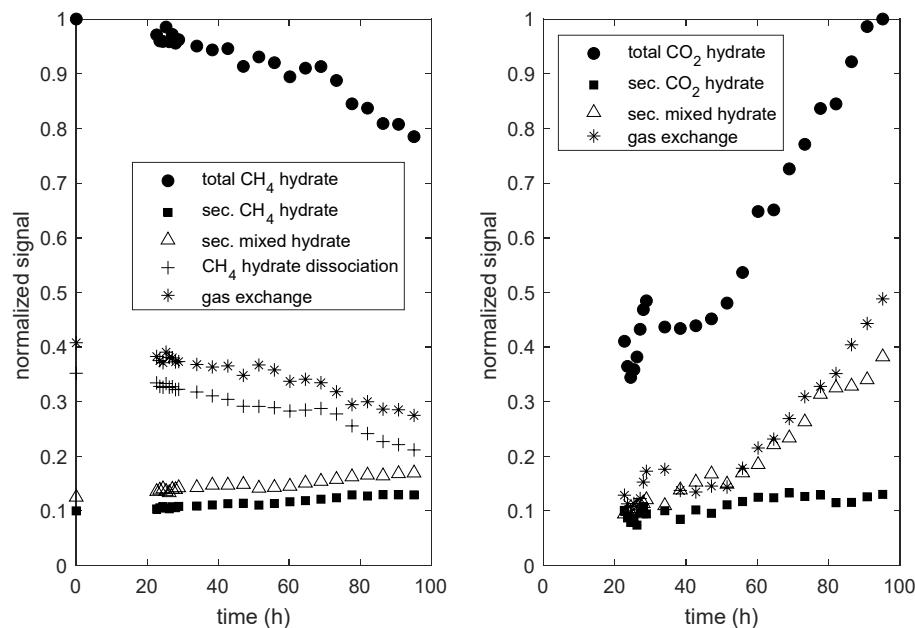


Figure 4. Evolution of the total gas-hydrate signal of experiment *NoFlow* and evolution of the specific processes (see text for explanation). Left: CH_4 hydrate; right: CO_2 hydrate.

It can be observed that only 41% of the initial signal belonged to pixels that would undergo gas exchange in gas-hydrate grains during the observed experimental period, and 35% of the initial signal originated from areas where CH_4 hydrate dissociated during the experiment. Secondary gas-hydrate formation affected 23% of the initial signal: 13% was subject to mixed-hydrate formation, and 10% was subject to CH_4 hydrate formation. The total signal change of -21% to 79% was caused by -14% signal change due to gas exchange, -14% signal change due to gas-hydrate dissociation, $+4\%$ signal change due to secondary mixed-hydrate formation, and $+3\%$ signal change due to secondary CH_4 hydrate formation. Results are also listed in Table 1. The dominant processes were gas exchange and gas-hydrate dissociation, which contributed equally to the decrease in the CH_4 hydrate signal. A total of 25% of the released CH_4 was bound again in secondary gas hydrates within this FOV.

Table 1. The percentage of the initial CH₄ hydrate signal (%S) that was attributed to the respective individual processes and the contribution of these processes to the change of the total CH₄ hydrate signal (ΔS). %S and ΔS for total CH₄ hydrate are consequently (within the range of rounding errors) the sum of the values for all subprocesses. See text for further explanations. Flow 1 is the flow period of experiment *Flow* and Flow 2 is the no-flow period of experiment *Flow*. The duration of the experimental period is given in the last row.

	No Flow		NoFlowI1		NoFlowI2		Flow 1		Flow 2	
	%S	ΔS	%S	ΔS	%S	ΔS	%S	ΔS	%S	ΔS
sec. CH ₄ hydrate	10%	+3%	3%	+1%	10%	+2%			18%	+7%
sec. mix hydrate	13%	+4%	18%	+3%	5%	+2%	2%	+2%	32%	+18%
CH ₄ -CO ₂ ex-change	41%	-14%	53%	-23%	22%	-9%	93%	-56%	23%	-6%
CO ₂ -CH ₄ ex-change									4%	+3%
CH ₄ hydrate diss.	35%	-14%	20%	-10%	62%	-18%	5%	-3%	16%	-4%
mix hydrate diss.									8%	-2%
total CH ₄ hyd	100%	-21%	100%	-29%	100%	-24%	100%	-57%	100%	+17%
experimental pe-riod/h		95		47		41		5.5		10.5

The CO₂ content in gas hydrates was assumed to be zero at the start of the experiment and indeed, no signal above the noise threshold could be derived from the first map ($t = 0$). As for the CH₄ hydrate signal, curves for attributed processes are included in the graph. The results are listed in Table 2: Of the 100% signal increase during the experiment, 49% was caused by gas exchange, 38% by secondary mixed-hydrate formation, and 13% by secondary CO₂ hydrate formation. The noise in the spectral CO₂ hydrate maps 2–9 was significantly higher than in the last 15 maps. As a consequence, the signals from the first 9 maps were omitted for all data fits.

Two gas-hydrate grain regions with confirmed gas exchange were chosen for evaluation of the diffusion constant (marked in Figure 3). The signal of all pixels of the selected grain areas was summed up and fitted with Equation (2). Results are summarized in Table 3. The parameter D_{CH_4}/R_0^2 was $(0.69 \pm 0.25) \times 10^{-7}$ 1/s for grain 1 and $(0.55 \pm 0.11) \times 10^{-7}$ 1/s for grain 2. It was not possible to precisely determine the grain radius R_0 for an accurate calculation of the diffusion coefficient D , since the resolution of the maps was not fine enough. The radius of the evaluated areas, as derived from the maps, was 15 μm for grain 1 and 10 μm for grain 2, but out-of-focus contributions might be missing here. From the maps, the maximum grain diameter could be estimated to be 30 μm , but the resolution was not good enough to ensure that the structure belonged to a single grain and not multiple grains that touched each other. Taking the grain area radius as the lowest possible radius and the map-derived radius as highest possible radius, the corresponding diffusion coefficients for CH₄ ranged from 15.6×10^{-18} to 62.2×10^{-18} m²/s for grain 1 and from 5.5×10^{-18} to 49.8×10^{-18} m²/s for grain 2. The integrated CO₂ signal of the grain areas was fitted with Equation (3) and the parameter r/R_0 was set to the value that was obtained from the CH₄ hydrate regression. Again, D/R_0^2 was in the order of 10^{-7} : $(2.4 \pm 0.58) \times 10^{-7}$ 1/s for grain 1 and $(0.33 \pm 0.11) \times 10^{-7}$ 1/s for grain 2. Considering the possible range for R_0 , the diffusion constant D_{CO_2} was 54.7×10^{-18} to 218.7×10^{-18} m²/s for grain 1 and 3.4×10^{-18} to 30.2×10^{-18} m²/s for grain 2. The signal curves of the grains and the regressed curves are shown in Figure 5.

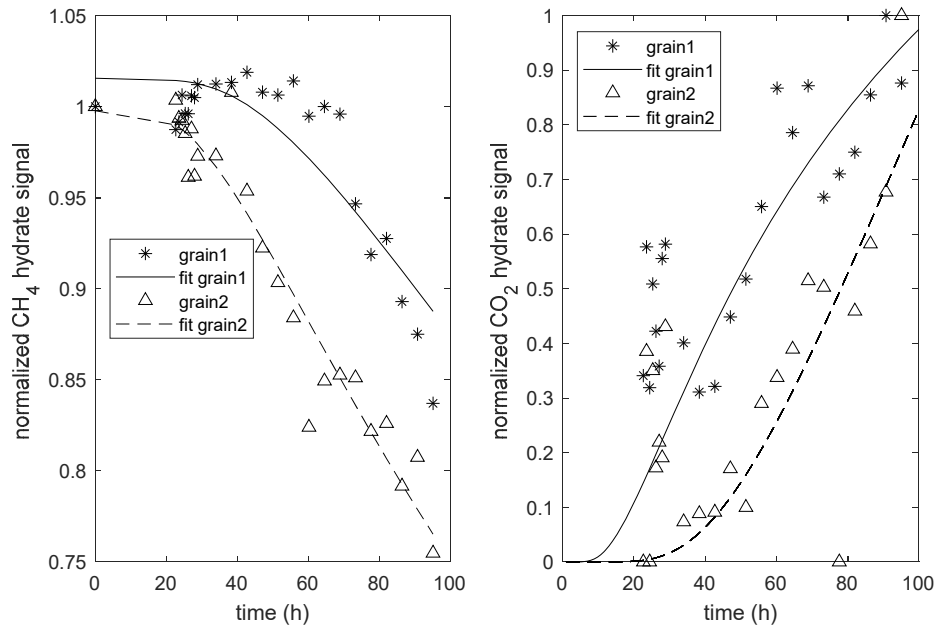


Figure 5. Time evolution of the CH₄ hydrate signal (left) and CO₂ hydrate signal (right) on grains 1 and 2 with regressed curves from the diffusion equation.

Table 2. The percentage of the CO₂ hydrate signal (%S) that was attributed to the respective individual processes and the contribution of these processes to the change of the total CO₂ hydrate signal (ΔS). Flow 1 is the flow period of experiment *Flow* and Flow 2 is the no-flow period of experiment *Flow*. For both flow periods, 100% depicts the CO₂ signal at the end of the Flow 1 period: In the first case, it is the final signal, and in the second case, it is the initial signal. Hence, %S and ΔS for the Flow 2 period refers to the initial signal and not to the final signal. The duration of the experimental period is given in the last row.

	NoFlow	NoFlowI1	NoFlowI2	Flow 1	Flow 2	
	%S	%S	%S	%S	%S	ΔS
sec. CO ₂ hydrate	13%	23%	26%	6%	6%	+10%
sec. mix hydrate	38%	28%	33%	38%	47%	+33%
CH ₄ -CO ₂ exchange	49%	49%	44%	56%	9%	+11%
CO ₂ -CH ₄ exchange					25%	-3%
CO ₂ hydrate diss.					4%	-2%
mix hydrate diss.					7%	-3%
total CO ₂ hyd	100%	100%	100%	100%	100%	+46%
time period/h	95	47	41	5.5	10.5	

Table 3. Regression parameters D/R_0^2 for diffusion on single gas-hydrate grains. For *NoFlowI2*, no gas hydrate grains with gas exchange could be identified. Estimates for grain size ranges are listed with corresponding ranges for diffusion coefficients.

	$D_{CH_4}/R_0^2/10^{-7} s$	$D_{CO_2}/R_0^2/10^{-7} s$	$R_0/\mu m$	$D_{CH_4}/(10^{-18} m^2/s)$	$D_{CO_2}/(10^{-18} m^2/s)$
grain 1 (<i>NoFlow</i>)	0.69 ± 0.25	2.4 ± 0.58	15–30	15.5–62.2	54.7–218.7
grain 2 (<i>NoFlow</i>)	0.55 ± 0.11	0.33 ± 0.11	10–30	5.5–49.8	3.4–30.2
grain 3 (<i>NoFlowI1</i>)	0.09 ± 0.18	1.19 ± 0.172	35–50	11.0–22.4	145.8–297.5
grain 4 (<i>NoFlowI1</i>)	2.08 ± 0.55	17.2 ± 2.44	25–50	130.0–520.0	1075.0–4300.0
grain 5 (<i>NoFlowI1</i>)	2.52 ± 0.47	too noisy	20–50	100.8–630.0	
				$D_{CH_4}/(10^{-14} m^2/s)$	$D_{CO_2}/(10^{-14} m^2/s)$
grain 6 (<i>Flow</i>)	70.5 ± 10.7	91 ± 61.8	100–250	7.1–44.1	9.1–56.9
grain 7 (<i>Flow</i>)	39.5 ± 18.6	108 ± 34.9	100–250	2.9–17.9	4.6–28.9
grain 8 (<i>Flow</i>)	73.6 ± 5.9	236 ± 88.2	100–250	6.7–42.4	21.1–131.9

grain 9 (Flow)	48.8 ± 18.9	88.7 ± 34.8	100–250	4.0–24.7	10.8–67.5
grain 10 (Flow)	55.3 ± 15	132 ± 43.5	100–250	7.4–46.0	23.6–147.5
grain 11 (Flow)	74.1 ± 10.4	156 ± 19.9	100–250	4.9–30.5	8.9–55.4
grain 12 (Flow)	74.1 ± 11.1	116 ± 60.6	100–250	5.5–34.6	13.2–82.5
grain 13 (Flow)	60.5 ± 24.2	63.6 ± 48	100–250	7.4–46.3	15.6–97.5
grain 14 (Flow)	32.7 ± 13.6	30.8 ± 21.9	100–250	3.8–23.6	4.3–26.9
grain 15 (Flow)	44.8 ± 14.5	50.3 ± 30	100–250	9.7–60.5	14.7–91.9
grain 16 (Flow)	79.2 ± 21.3	91.5 ± 41.1	100–250	7.4–46.3	11.6–72.5
grain 17 (Flow)	68.1 ± 6.6	96.5 ± 54.7	100–250	6.1–37.8	6.4–39.8

3.2. Experiment NoFlowI1

A total of 46 spectral maps for CH₄ and the same number of maps for CO₂ were measured during this experiment. The first map was started directly after the pressurization with CO₂. The first five maps for each component were measured with an acquisition time of 0.5 s per data point, and a pixel corresponds to the integral signal of an area of 20 μm × 20 μm. The field of view was 500 μm × 360 μm and the total acquisition time was 12 min per set of maps with fast imaging techniques. The subsequent 15 pairs of spectral maps were measured with an acquisition time of 0.5 s, a total acquisition time of 40 min per set of maps, and a pixel size of 10 μm × 10 μm. Then, 26 more pairs of spectral maps were collected with an acquisition time of 1 s, a total acquisition time of 77 min per set of maps, and a pixel size of 10 μm × 10 μm. The field of view remained constant among all maps, and the last data set corresponds to the time 46.7 h after the start of the hydrate conversion. The first five maps were regridded to match the resolution of the other maps, but the CH₄ data did not match the signal evolution of the subsequent data. Hence, the first five data points were omitted in all fits of CH₄ hydrate data.

Figure 6 shows the initial CH₄ hydrate map and CH₄ and CO₂ hydrate maps after 15, 30, and 45 h. Two larger gas hydrate grains can be seen in the upper-left quadrant, and a number of smaller grains are located in the lower-right quadrant of the field of view. CH₄ hydrate dissociation clearly took place in the upper-right quadrant. A simultaneous increase in CH₄ hydrate signal and CO₂ hydrate signal occurred at the right side around $y = 250 \mu\text{m}$, indicating the formation of secondary mixed gas-hydrates. Secondary CO₂ hydrates were formed rapidly in the pore space between the original grains at $x \sim 50 \mu\text{m}$ and $x \sim 250 \mu\text{m}$. The two larger gas-hydrate grains could not be used for an evaluation of the exchange kinetics since the left grain was partly overgrown by secondary CO₂ hydrate and the right grain exhibited, in parts, an increase in CH₄ signal, indicating a growth of secondary mixed or CH₄ hydrate. Therefore, three areas in the lower-left quadrant of the FOV were chosen for evaluation. These areas are indicated as grains 3, 4, and 5 in Figure 6. Again, the resolution of the image was not good enough to reliably determine the outlines and sizes of present gas-hydrate grains.

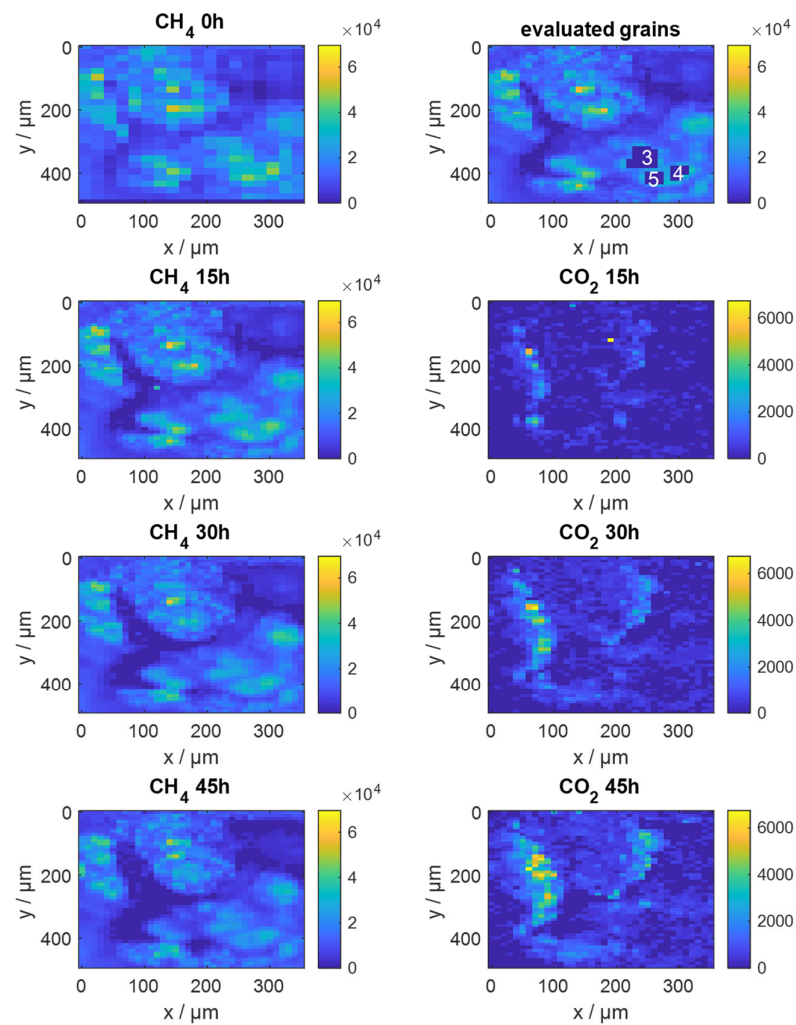


Figure 6. CH₄ and CO₂ hydrate maps of experiment *NoFlow11* at times 0 h (only CH₄ hydrate), 15 h, 30 h, and 45 h. The location of the three selected gas-hydrate grain areas for gas-exchange evaluation are marked as blue areas in the upper-right map.

Figure 7 shows the time development of the ongoing processes. Signals were normalized to the CH₄ hydrate signal of the 6th map (first map with 10 μm resolution) and to the final CO₂ hydrate signal. Table 1 lists the changes in inventory for CH₄, and Table 2 for CO₂. The total CH₄ hydrate signal decreased to 71% during 44 h. This total signal was again divided into fractions that were exposed to the same type of process during the course of the experiment. The dominant fraction, with a contribution of 59% to the total signal, was affected by gas exchange. This signal fraction was responsible for a signal loss of 23% of the total signal. A fraction of 20% of the initial signal was affected by CH₄ hydrate dissociation, which was responsible for 10% of the total signal loss; 18% of the signal belonged to pixels with formation of secondary mixed hydrates; and 3% belonged to pixels with formation of secondary CH₄ hydrates. The signal increase caused by these processes was 3% and 1%, respectively. Unlike experiment *NoFlow*, only 4% of the released CH₄ was bound again in gas hydrates in the observed area. The CO₂ content in gas hydrates started at zero, and the experiment was not run long enough to reach the equilibrium concentration of CO₂. Hence, the signal could not be normalized to the final equilibrium signal, but needed to again be normalized to the final total signal in the experiment. Similar to the CH₄ hydrate, the dominant process was the gas exchange in existing CH₄

hydrate. This process contributed 49% to the rise in CO₂ hydrate signal, while the formation of secondary mixed hydrates contributed 28%, and the formation of secondary CO₂ hydrates contributed 23%. In conclusion, ~50% of the CO₂ bound in gas hydrates was involved in gas exchange, and ~50% was bound in newly formed secondary gas hydrates.

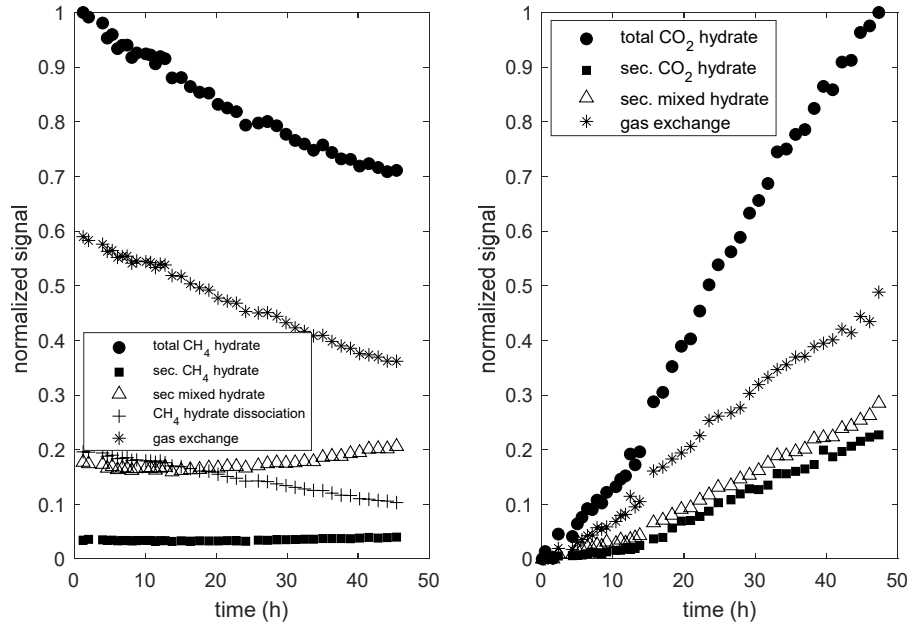


Figure 7. Evolution of the total gas-hydrate signal of experiment *NoFlow11* and evolution of the specific processes. Left: CH₄ hydrate; right: CO₂ hydrate.

Three gas-hydrate grain regions with assigned gas exchange were chosen for evaluation of the diffusion constant. The positions of the grain areas are marked in Figure 6. The signal of all pixels of the selected grain areas was summed up and fitted with the diffusion equation. Results are visualized in Figure 8 and summarized in Table 3. The parameter D_{CH_4}/R_0^2 was $(0.09 \pm 0.18) \times 10^{-7}$ 1/s for grain 3, $(2.08 \pm 0.55) \times 10^{-7}$ 1/s for grain 4, and $(2.52 \pm 0.47) \times 10^{-7}$ 1/s for grain 5. From the evaluation of the CO₂ hydrate signal, we derived $D_{CO_2}/R_0^2 = (1.19 \pm 0.17) \times 10^{-7}$ 1/s for grain 3 and $D_{CO_2}/R_0^2 = (17.2 \pm 2.44) \times 10^{-7}$ 1/s for grain 4. The signal from grain 5 was too noisy for a regression. The higher variability of the results originated from the higher noise in the CO₂ maps, which was a consequence of the generally lower signal in the maps. Again, the grain radii could not be reliably determined. The ice grains were sieved to a fraction of 100 μ m to 200 μ m diameter, but the grains in the maps appeared to be more around 100 μ m diameter or a bit smaller. Grain diameters as derived from the maps were 70, 50, and 40 μ m, respectively, for grains 3, 4, and 5. With these size estimates, the range for the diffusion constant D_{CH_4} resulted in 11.0×10^{-18} – 22.4×10^{-18} m²/s for grain 3, 130.0×10^{-18} – 520.0×10^{-18} m²/s for grain 4, and 100.8×10^{-18} – 630.0×10^{-18} m²/s for grain 5; and the value for the diffusion constant D_{CO_2} ranged from 145.8×10^{-18} – 297.5×10^{-18} m²/s for grain 3 and 1075×10^{-18} – 4300×10^{-18} m²/s for grain 4.

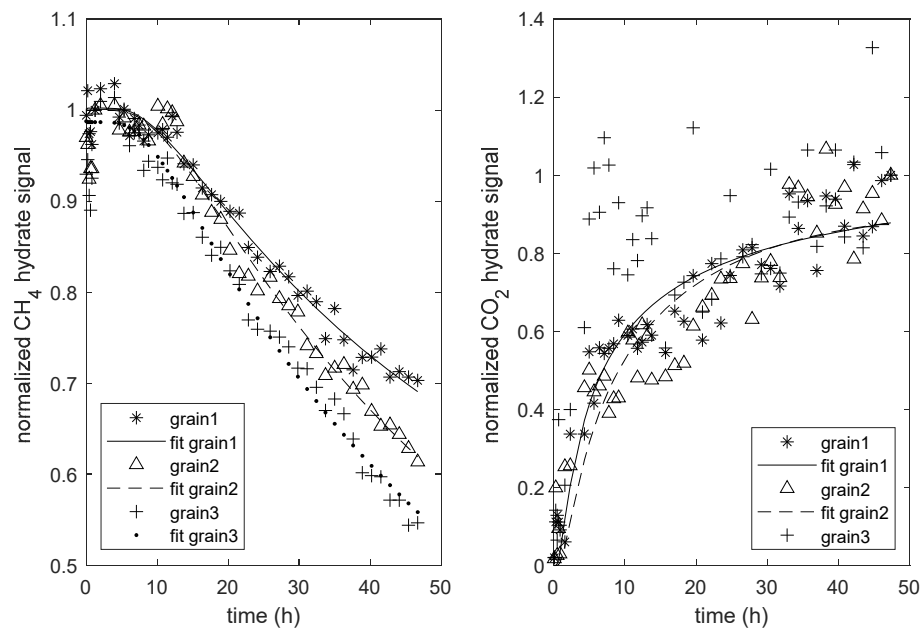


Figure 8. Time evolution of the CH₄ hydrate signal (left) and CO₂ hydrate signal (right) on grains 3, 4, and 5 with regressed curves.

3.3. Experiment NoFlowI2

Spectral mapping during experiment *NoFlowI2* started only 20 min after pressurizing the sample cell with CO₂. Maps with three different accumulation times were measured: The first eight map sets, which were measured in the first 4 h after the start of the hydrate conversion, had an accumulation time of 0.5 s, followed by eight map sets with a 1 s accumulation time during the next 6 h. One 0.5 s map set was measured at 18 h, and eight more 1 s map sets were measured between 18.5 h and 24 h. The final 10 maps had an acquisition time of 2 s and were measured between 26 and 40.5 h after the start of the hydrate conversion. The resolution of the maps was 10 μm in both the x and y directions for all maps, and the total acquisition time for one set of maps was 26 min for 0.5 s acquisition time per pixel, 49 min for 1 s acquisition time per pixel, and 95 min for 2 s acquisition time per pixel. Fast imaging techniques were used for all measurements. Each map set included two spectral maps in the range of the CH₄ signal that covered two different FOVs, and the corresponding two spectral maps in the range of the CO₂ signal. Both FOVs included a part of a quartz grain, and the quartz signal was used for spectral calibration. Unfortunately, the quartz grains moved significantly during the experiment, while the gas-hydrate grains remained fixed. As a consequence, one FOV needed to be excluded from data evaluation because the quartz grain occasionally covered too large a fraction of the gas-hydrate grains. The second FOV was reduced from 210 μm \times 270 μm to 210 μm \times 210 μm in order to cut out the region where the moving quartz grain was located.

Figure 9 shows the first CH₄ hydrate map and CH₄ and CO₂ hydrate maps after 10, 26, and 40 h. It is striking that the CO₂ hydrate signal appeared very locally, while almost all CH₄ hydrates were affected by dissociation. At first sight, secondary CO₂ hydrate formation seemed to take place at the lower edge of the FOV. However, the CH₄ signal in this region also rose, although to a much lesser extent. Hence, there was an ongoing formation of secondary CO₂-rich mixed hydrates, probably with local formation of pure CO₂ hydrate. Only two CH₄ hydrate grains seemed to be subject to gas exchange. Both were located between $x = 100 \mu\text{m}$ – $150 \mu\text{m}$, with $y \sim 50 \mu\text{m}$ for the first grain and $y \sim 125 \mu\text{m}$ for the second grain. On a closer look, the grains showed patches with increasing, as well as patches with decreasing CH₄ concentrations, indicating that several processes seemed to

take place on the same grains in parallel. Consequently, it was not possible to evaluate guest-molecule diffusion on single grains.

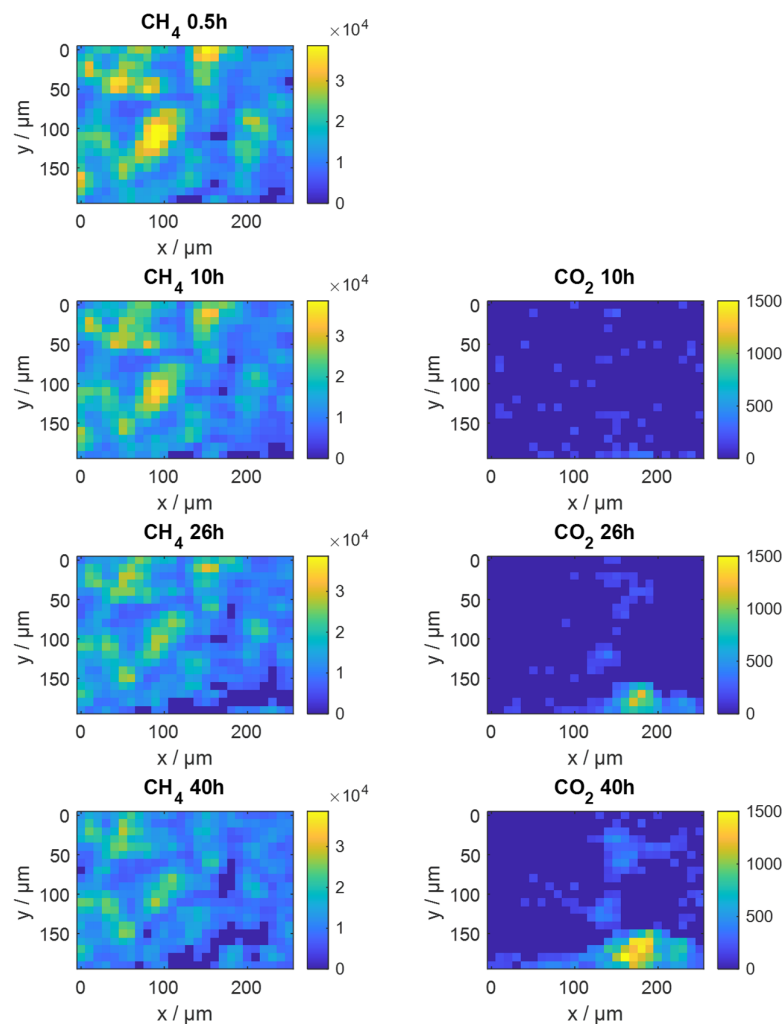


Figure 9. CH₄ and CO₂ hydrate maps of experiment *NoFlowI2* at times 0.5 h (only CH₄ hydrate), 10 h, 26 h, and 40 h.

The time development and the impact of the ongoing processes is shown in Figure 10. Signals were normalized to the CH₄ hydrate signal of the first map and to the final CO₂ hydrate signal. Table 1 and Table 2 list the changes in inventory. The total CH₄ hydrate signal decreased to 76% of the initial signal during 40 h. The dominant process was gas-hydrate dissociation, as expected from the trend in the maps in Figure 9. CH₄ hydrate dissociation accounted for 18% signal loss. A fraction of 62% of the initial signal was affected by this kind of process. The signal loss due to gas exchange was 9%, and contributed, to a much lesser extent than dissociation, to the changes of the CH₄ hydrate signal. 22% of the total signal experienced signal reduction from gas exchange by the end of the experiment. The overall signal loss was partly counteracted by the formation of mixed secondary gas hydrate (+2%, affecting 5% of the initial signal) and the formation of secondary pure CH₄ hydrates (+2%, affecting 10% of the initial signal). The deviation of the sum of the contributions from the 100% total signal loss was a rounding error. The contributions to the rise of the CO₂ hydrate signal were quite similar for all three processes: a 26% rise from secondary CO₂ hydrate formation, a 33% rise from secondary mixed-hydrate formation, and a 41% rise from gas exchange were observed. After a relatively slow

start, gas exchange and secondary CO₂ hydrate formation showed an above-average growth rate during the final hours of the experiment. Upon a closer look, it was noticeable that, for extended periods, the three process signals did not sum up to the total CO₂ hydrate signal. The reason for this behavior was a feature of the evaluation procedure: Only pixels with a CO₂ hydrate signal in the final map were assigned one of the three processes. The temporary surplus in the total signal stems from pixels that had a CO₂ hydrate signal during intermediate times, but not in the final map. This especially occurred between 4 h and 28 h. The additional CO₂ hydrate signal was discontinuous, similar to the signal in the 10 h map in Figure 9. Either the data contained enhanced noise signals during this time, or some of the CO₂ hydrate dissociated again during the course of the experiment.

This experiment was the most difficult to interpret among the presented experiments. The ongoing processes were not well separated, and the assignment of processes to pixels was uncertain. No CH₄ hydrate grains with pure or at least highly dominant gas exchange could be identified, and no diffusion coefficients were obtained.

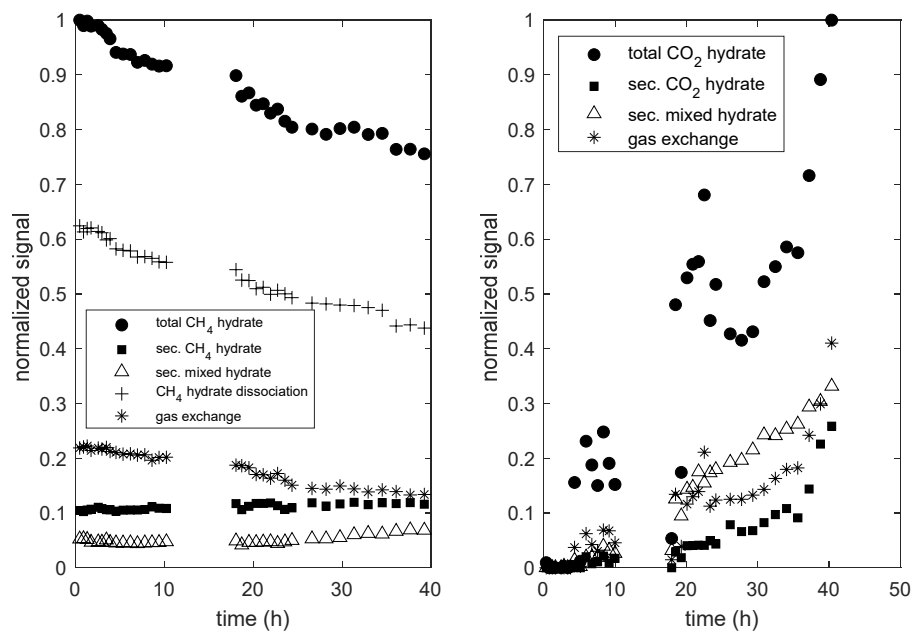


Figure 10. Evolution of the total gas-hydrate signal of experiment *NoFlowI2* and evolution of the specific processes. Left: CH₄ hydrate; right: CO₂ hydrate.

3.4. Experiment Flow

The experiment *Flow* was the most complex among the presented experiments: It was operated in flow-through mode in a pressure cell filled with quartz sand. During the experiment, secondary gas hydrate formation changed the permeability of the sample and caused a change of the sample pressure. The pressure log close to the entrance of the sample cell is presented in Figure S5. The pressure was relatively constant around 13 MPa during the first 2 h, then it rose to 15 MPa over the next 4 h. When the pressure peaked above this value, the pump was automatically shut off to protect the pressure cell. This shut-off happened at late evening and was not noticed by an operator until 13 h later. During this period, the pressure dropped again to 14 MPa and the sample was at no-flow conditions. By coincidence, the FOV and the map resolution were changed shortly before the pump went idle, and the data set divided into two subsets: 6 sets of maps were taken at flow conditions and had a pixel distance of 100 μm in the x and y directions, a FOV size of 4200 μm \times 2900 μm , and a total acquisition time of 60 min per set of maps. This series was succeeded by 10 sets of maps that were measured without flow, with a pixel distance of 20 μm in the x and y directions, a FOV size of 1200 μm \times 1200 μm , and an acquisition

time of 80 min per set of maps. It was possible to restart the flow again, and two more maps with $100\ \mu\text{m} \times 100\ \mu\text{m}$ resolution could be sampled, but 2 h later, a more severe blockage occurred. This time, the flow could only be resumed after raising the sample temperature to $10\ ^\circ\text{C}$. At this temperature, the pressure remained relatively stable for the next 15 h. However, since temperature changes have a strong effect on dynamics, we refrained from including data from this period into our evaluation.

Figure 11 shows the CO_2 hydrate maps from times 0, 3, and 17 h. The first three maps cover the flow period before the first blockage, and the 17 h map was taken following the restart of the flow. A white rectangle marks the position of the smaller FOV from the high-resolution measurements during the no-flow period. The 0 h CO_2 hydrate map illustrates the slow progression of the liquid CO_2 into the sample: at this time, the CO_2 front had reached the FOV, but had not proceeded into the upper $600\ \mu\text{m}$. Actually, the map was taken 2 h after start of the CO_2 flow, but there was no CO_2 present in two earlier measurements, and the time scale was shifted by 2 h in order to assign the time zero to the first contact with CO_2 . Unfortunately, the earlier CH_4 gas-hydrate maps could not be used as initial gas-hydrate-concentration maps, because the exchange of the pore fluid changed the refractive index, which resulted in a changed focus depth. It is noticeable that rapid secondary gas hydrate formation took place in the pore space in-between the CH_4 hydrate grains. This secondary gas hydrate was partly a pure CO_2 hydrate and partly a mixed-gas hydrate with a high fraction of CO_2 . As shown in the following maps, the CO_2 hydrate signal also expanded into the region of the CH_4 hydrate grains, indicating gas exchange. The CH_4 hydrate maps revealed several clusters of CH_4 hydrate grains. Due to the low resolution of the maps, the outline of the grains was badly resolved. But from high-resolution maps, it can be seen that the grain diameters could be up to several $100\ \mu\text{m}$, which was much larger than the grains in the other experiments. The time evolution of the gas-hydrate maps revealed a quite uniform behavior: After rapid formation of CO_2 or CO_2 -rich secondary gas hydrates, mainly gas exchange took place.

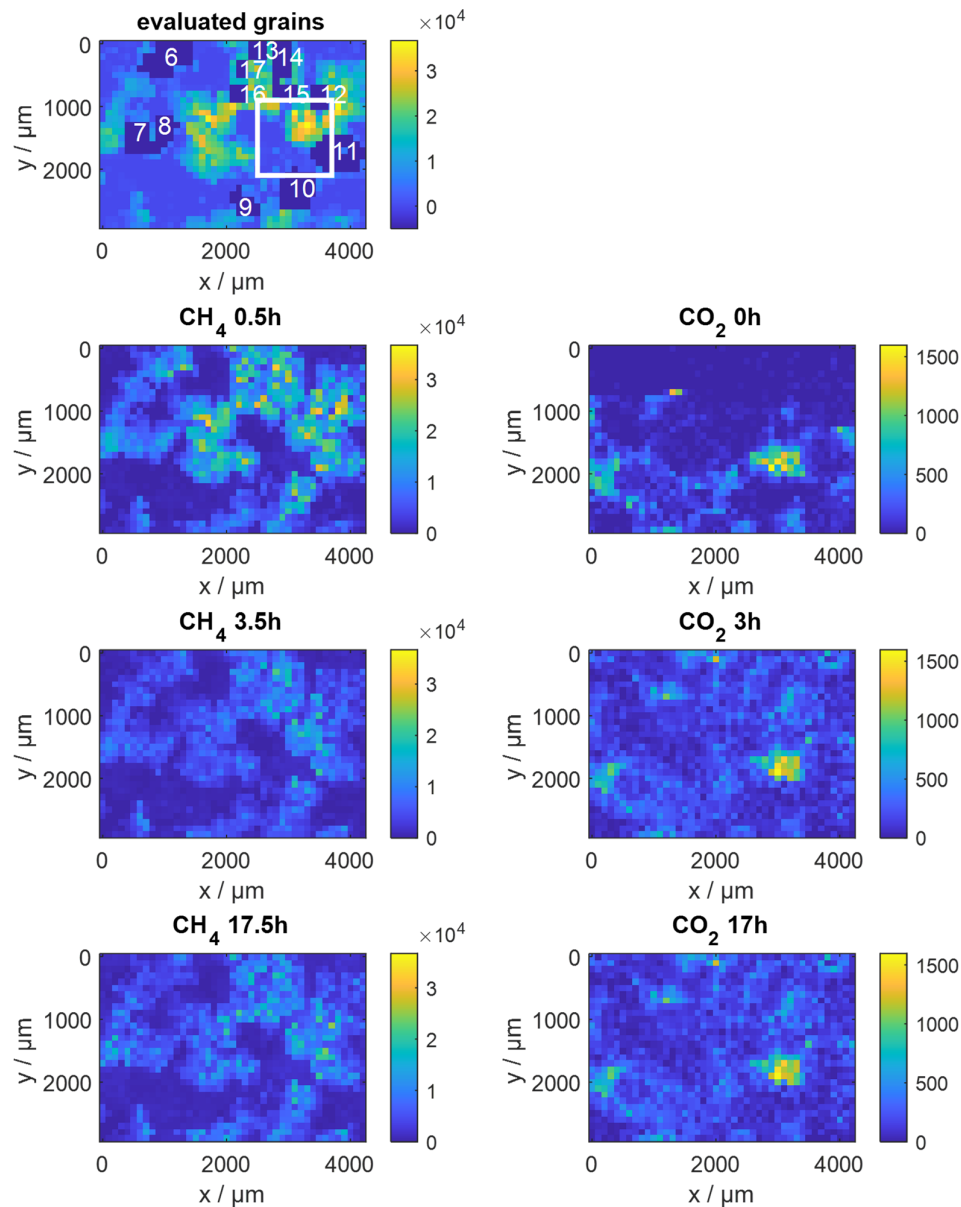


Figure 11. CH₄ and CO₂ hydrate maps of experiment *Flow* during the flow period at 0 h, 3 h (before stop of flow), and 17 h (after reinstatement of flow conditions). The white rectangle marks the location of the smaller FOV, and the positions of the evaluated gas-hydrate grains are marked as dark blue areas.

A closer look into the different possible processes and their time evolution confirmed that the dominant contribution to the CH₄ hydrate signal change came from gas exchange. Figure 12 shows the time development of the ongoing processes. As for the other experiments, total signals were normalized to the initial CH₄ hydrate signal and to the final CO₂ hydrate signal. The total CH₄ hydrate signal decreased to 43% of its initial strength in 5 h, which was much more rapid than in the experiments without flow. Of this signal, 93% belonged to pixels that would undergo gas exchange in gas-hydrate grains during the observed experimental period, and 56% of the total signal was lost due to this process. An additional 3% of the total signal was lost because of CH₄ hydrate dissociation, which was almost balanced by a 2% signal increase due to the formation of secondary mixed hydrates. The affected fraction of the total signal was 5% for secondary gas-hydrate for-

mation and 2% for gas-hydrate dissociation. There was no significant indication for secondary CH₄ hydrate formation. The mixing of released CH₄ with the flowing liquid CO₂ seemed to be sufficiently effective in avoiding high local CH₄ concentrations that could reprecipitate as secondary CH₄ hydrate.

The increase in CO₂ content in the gas-hydrate phase was also highly affected by gas exchange (+56%), but also to a large extent by the formation of secondary mixed hydrates (+38%). Pure CO₂ hydrates accounted for only 6% of the signal increase. This apparent contradiction to the CH₄ hydrate evolution, in which almost all of the signal change was attributed to gas exchange, originated in the fact that the secondary mixed hydrates were CO₂-rich and contributed more to CO₂ signal rise than to CH₄ signal rise. The observed rapid formation of secondary gas hydrates required free water, but almost no gas-hydrate dissociation could be observed. This means that either the water from the gas-hydrate-formation step was not removed efficiently before the exchange experiment was started, or gas-hydrate dissociation did occur in sample volumes that were not included in the FOV and were therefore not monitored.

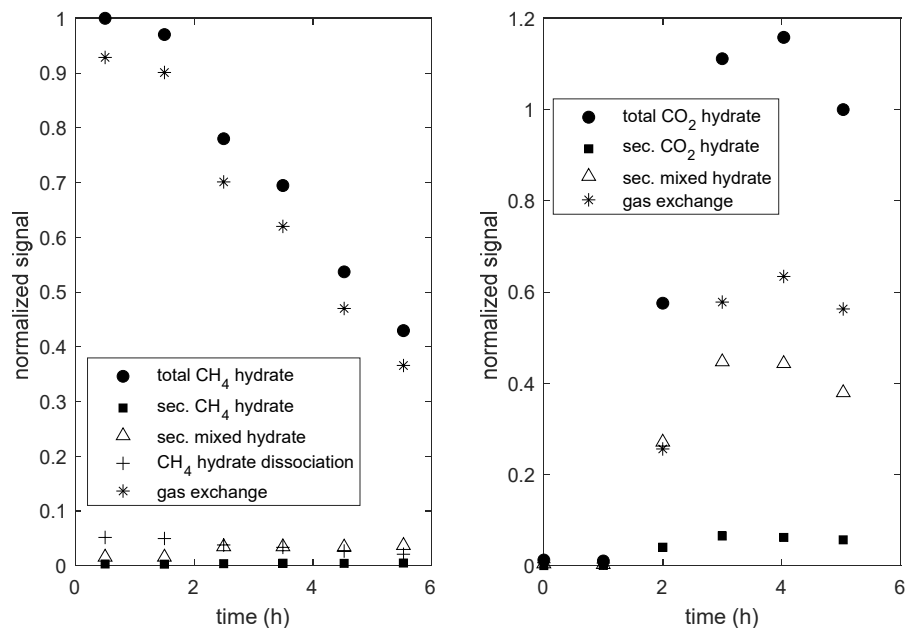


Figure 12. Evolution of the total gas hydrate signal during the flow period of experiment *Flow* and evolution of the specific processes. Left: CH₄ hydrate; right: CO₂ hydrate.

Solid-state diffusion coefficients for CH₄ and CO₂ were evaluated at 12 different grain positions. Grain locations are marked in Figure 11. The evolution on the single-grain signals are presented in Figure 13 and the results of the regressions are listed in Table 3. Values for D_{CH_4}/R_0^2 ranged from 33×10^{-7} to 79×10^{-7} 1/s, and values for D_{CO_2}/R_0^2 ranged from 31×10^{-7} to 236×10^{-7} 1/s. The average values were 60×10^{-7} 1/s for CH₄ and 109×10^{-7} 1/s for CO₂. As in the other experiments, the evaluation of the CO₂ hydrate data was more prone to noise, which was reflected in the broader range of diffusion constants and the relatively high errors of the regression parameters. Due to the coarse resolution, it was more difficult to estimate the gas-hydrate grain radii. The more finely resolved maps in Figure 13 contain gas-hydrate grains with radii of about 100 to 250 μm . With this range of R_0 , we calculated solid-state diffusion coefficients in the range of 10^{-13} to 10^{-14} m²/s for both CH₄ and CO₂, with D_{CO_2} being roughly twice as large as D_{CH_4} .

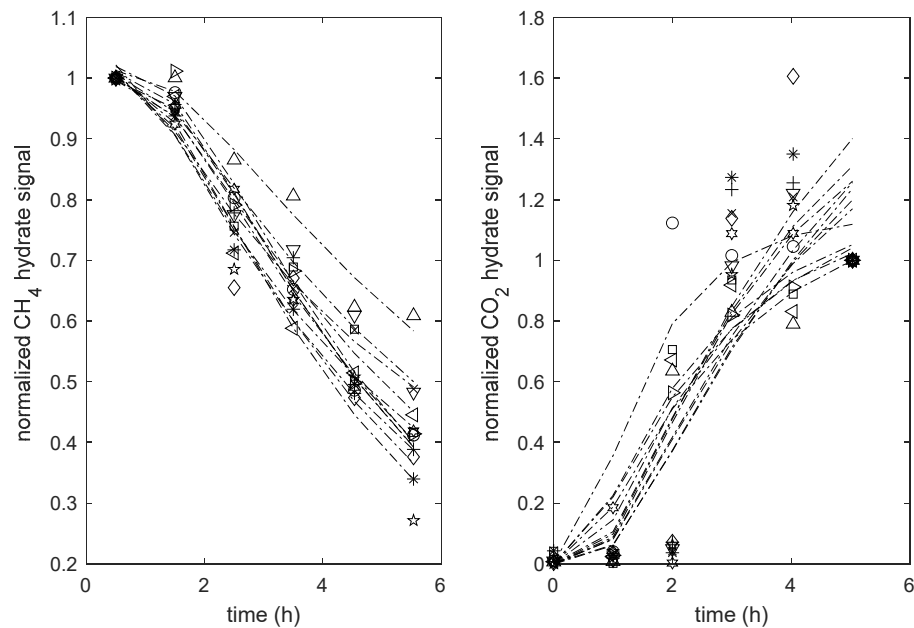


Figure 13. Time evolution of the CH_4 hydrate signal (left) and the CO_2 hydrate signal (right) on grains 6–17 with re-gressed curves. Different symbols denote different grains.

The evolution of the gas-hydrate phase during no-flow conditions was monitored on a smaller FOV with higher resolution. This provided a better insight into the ongoing processes, but did not enable us to directly link signal amplitudes from the flow period to signal amplitudes from the no-flow period. Figure 14 shows CH_4 hydrate and CO_2 hydrate maps that were taken 5, 10, and 15 h after the first contact with the liquid CO_2 phase, with the 5 h maps being taken around the time when the flow stopped. A striking feature of the CO_2 hydrate map is a patch of pure CO_2 hydrate in the lower half of the FOV. This patch did expand over time, and it also showed increasing CH_4 hydrate signal in the CH_4 hydrate maps. The patch grew toward the initial CH_4 hydrate grains and began to cover them. A map of the relative CH_4 hydrate cage-occupancy ratio change during this time period is also included in Figure 14. The color scale of the map was cut at -1 and 1 to ensure a sufficient contrast of the image. While the cage-occupancy ratio of the initial gas-hydrate grains decreased over time due to further exchange of CH_4 with CO_2 or a resetting of CH_4 molecules to small cages, the cage-occupancy ratio increased on the secondary CO_2 hydrate patch. This means that we need to consider an additional process: gas exchange of CO_2 with CH_4 in CO_2 hydrate grains or mixed-hydrate grains with high CO_2 content. An increase of the cage-occupancy ratio can also be observed at the edge of the initial CH_4 hydrate grains, where the CO_2 -rich secondary gas hydrate patch touched the CH_4 -rich primary gas hydrates. What we observed here was an overgrowth of the initial grains with CO_2 -rich mixed-gas hydrate. The integral evolution of the mean cage-occupancy ratio is presented in Figure S4. A fast decay from 1 to 0.65 caused by rapid gas exchange during the flow period was followed by a slower exchange from 0.65 to 0.6 during the no-flow period. Here, a slowed-down exchange during no-flow conditions was additionally counteracted by an increase of the cage-occupancy ratio in regions that were subject to the reverse exchange process.

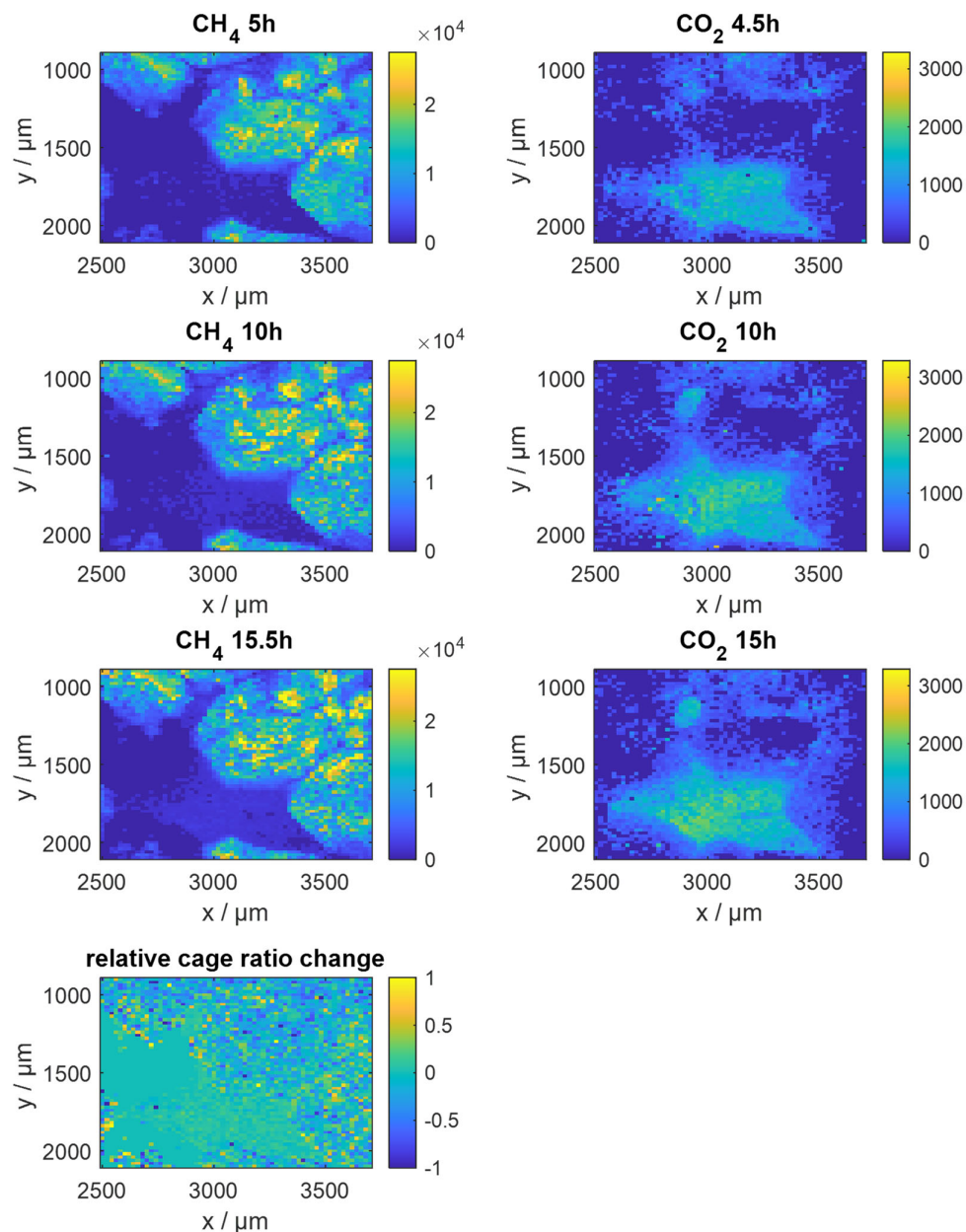


Figure 14. CH₄ and CO₂ hydrate maps of experiment *Flow* during the no-flow period at 5 h, 10 h, and 15 h, and the relative change in the cage-occupancy ratio during the period 5h to 15h.

Three additional possible processes were added to the process attribution for the no-flow period: the exchange of CO₂ with CH₄ in gas hydrates, the dissociation of mixed-gas hydrate, and the dissociation of pure CO₂ hydrate. In order to distinguish the two types of gas exchange, we used the term “exchange 1” for exchange of CH₄ with CO₂ and the term “exchange 2” for the exchange of CO₂ with CH₄. Actually, it was not clear if a rise of CH₄ concentration in CO₂-rich gas hydrates was an exchange process or an overgrowth of existing gas hydrate with a secondary mixed hydrate that was more enriched in CH₄, but we considered the definition of the process as gas exchange as a valid and likely choice as long as no further information was available. Figure 15 shows the time evolution of the different processes. This is the only case in which CO₂ was already present in gas hydrates at the beginning of the evaluation period. Deviating from the quantification of the other experiments, CO₂ data were normalized to the first total signal value and not to the last.

It was noticeable that the overall signals for both guest molecules increased. The total CH₄ hydrate signal increased by 17% during the 13 h time period. The total rise of the CH₄ hydrate signal required a source of methane, which was most likely gas-hydrate dissociation outside of the measured sample area, but also could have been a reabsorption of freed CH₄ from gas exchange that could not be transported away when the flow stopped. Only a small amount of gas-hydrate dissociation was observed. The signal from the fraction of pixels that underwent mixed-gas-hydrate dissociation (8% of the total signal) contributed with -2% to the overall signal change during the experimental period, and the signal from pixels with detected CH₄ hydrate dissociation (16% of the total signal) contributes to a -4% signal change. The pure CH₄ hydrate contributed 18% to the signal, and its growth increased the total signal by 7%. Most of the signal (59%) was associated with mixed-gas hydrates: the growth of secondary mixed hydrates (CO₂ and CH₄ hydrate signal increased simultaneously) was attributed to pixels that contributed 32% of the initial total signal and caused 18% of the total increase. A further 3% signal increase originated from the exchange of CO₂ with CH₄ (4% of the initial total signal affected), while 6% of the signal was lost due to exchange of CH₄ with CO₂ (23% of the initial total signal affected).

The total CO₂ hydrate signal growth was 46% over the time span of 13 h. With 47% of the initial signal and a rise of 33%, the formation of new secondary mixed hydrates was the major process for binding of CO₂ in gas hydrates. Gas exchange of CH₄ with CO₂ (+11%) and the formation of secondary CO₂ hydrate (+10%) also contributed substantially to the signal change. These two processes affected pixels with 9% and 6% of the initial signal, respectively. Loss of CO₂ from gas hydrates was relatively small and was caused by three different processes: CO₂ hydrate dissociation (-2%, 4% of the initial signal), mixed-hydrate dissociation (-3%, 7% of the initial signal), and exchange of CO₂ with CH₄ (-3%, 25% of the initial signal).

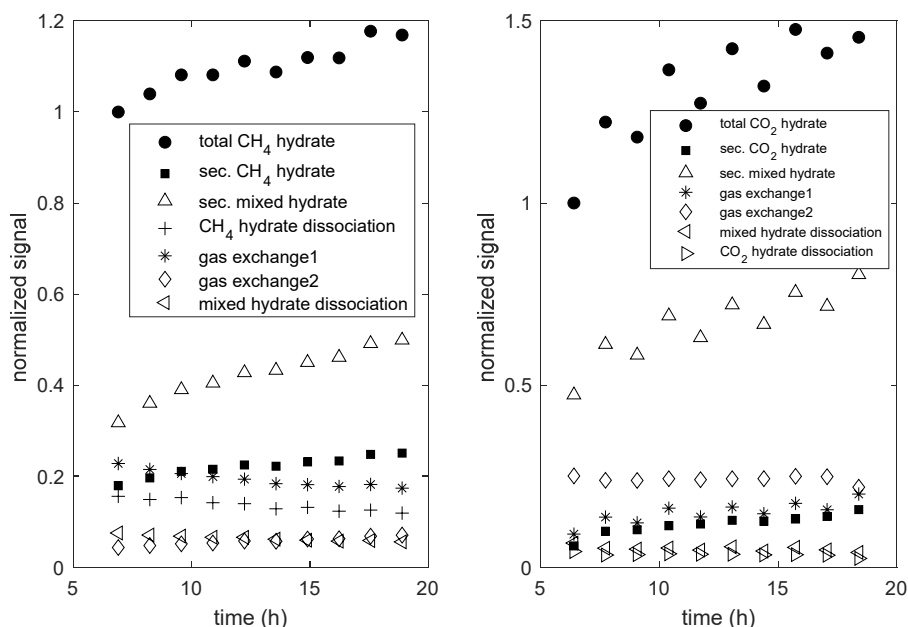


Figure 15. Evolution of the total gas hydrate signal during the flow period of experiment *Flow* and evolution of the specific processes. Left: CH₄ hydrate, right: CO₂ hydrate.

4. Discussion

4.1. Comparability of the Experiments and Limitations of this Study

In this study, we present and evaluate data from four experiments with different experimental conditions. Three experiments (*NoFlow*, *NoFlowI1*, and *NoFlowI2*) were per-

formed at similar pressure and temperature conditions, while experiment *Flow* was performed at higher pressures and temperatures. Kinetic processes depend considerably on the temperature. Therefore, obtained kinetic parameters like diffusion coefficients were expected to differ among the *NoFlow* and *Flow* experiments. The larger diffusion coefficients, which were derived from experiment *Flow*, reflect the higher mobility of molecules at higher temperatures and support the plausibility of our results. However, they cannot be used to prove the repeatability of the results. The same is true for the presence of the liquid CO₂ phase in experiment *Flow*. The higher concentration of CO₂ molecules in the fluid phase was expected to enhance the exchange process.

Another difference among the experiments was the presence of a porous matrix. In experiment *Flow*, the gas hydrate was formed in a sand matrix, while experiment *NoFlow* was set up completely without sand, and only a few sand grains were put loosely on top of the gas-hydrate grains in the *NoFlow* experiments. The sand matrix affected the experiment in two ways: transport of the constituents was hindered by the tortuous pathways in the sample and the chemical potential of the gas-hydrates changes in the vicinity of the quartz surface [36]: Chaouachi et al. [37] observed that gas-hydrate grains do not grow directly in contact with quartz-grain surfaces. We postulate that the presence of sand was not relevant to the results of our study, since we could only observe gas-hydrate grains that were located directly at the surface of the sample and were not covered by quartz grains.

The difference among the diffusive transport in the gas phase of the *NoFlow* experiments and the advective transport in the liquid phase of the *Flow* experiment did not seem to have much influence on the results either. Both set-ups allowed for a sufficiently fast transport of the molecules in the fluid phase.

A larger concern was the different gas-hydrate-formation protocols. For two experiments, gas hydrates were formed from ice grains, and for another two experiments, gas hydrates were formed from a gas-saturated aqueous solution. Since the temperature was cycled several times above the freezing point of water during the ice/gas hydrate conversion, we expected that only gas-hydrate structures were left, and that the crystal lattice did not differ among grains from different formation protocols. But the ripening time of the crystals was drastically different and varied from 1–2 days in experiments *NoFlow* to 60 days in experiment *Flow*. During the ripening period, empty cages, which are expected to occur, especially in ice-derived gas hydrates, are filled by diffusion of guest molecules from the surrounding liquid into the crystal lattice, and the average grain size increases due to Ostwald ripening [62]. The cage-occupancy ratios of the initial CH₄ hydrates (Figures S1–S4) indicated that only experiment *Flow* was performed with fully evolved gas-hydrate crystals. CH₄ hydrates from the other experiments incorporated a significantly higher number of empty cages, which might have facilitated the diffusion of molecules through the lattice.

The analysis of the microscale processes was not affected much by the listed experimental differences. Here, the main source of error was the noise in the spectral maps. We observed the same processes during all of the experiments, but with a rather large spatial inhomogeneity. Hence, intersample differences were comparable with intrasample differences. As long as we cannot map areas with hundreds of gas-hydrate grains with a spatial resolution of less than 100 μm, we can measure only trends and general characteristics, and these were consistent for all of the experiments.

The quantification of diffusion coefficients requires the precise control and the exact knowledge of all relevant parameters. This type of experiment is especially prone to errors and uncertainties. As discussed above, some of the experimental parameters affected the diffusion coefficients, but were not exactly known or not exactly reproduced among experiments. In addition, the rather high noise in the comparably low CO₂ hydrate signals caused uncertainties in the regression of the data. Also, the deviation of the size of the Raman laser focus from the ideal point source and the deviation of the grain shape from

an ideal sphere contributed unknown errors to the results. All these errors can be considered small compared to the error that originated from the uncertainty in grain radius. Hence, we only quantified and listed this major error, and neglected all other errors. Consequently, we could only provide a rather large range for the diffusion coefficients and were not able to derive exact values. However, there are only few reported results for diffusion coefficients of guest molecules in gas-hydrate grains, and we believe that a constraint of the order of magnitude is indeed valuable information.

4.2. Microscale Processes

The gas-hydrate maps presented in this manuscript are unique with respect to the possibility of following the response of CH₄ hydrate to exposure with CO₂ on a scale of several tens to several hundred μm, which covers the size of several gas-hydrate grains. On this scale, neither the molecular-scale mechanisms of the CO₂ invasion into the gas-hydrate crystal structure can be resolved, nor is it certain that the processes in the chosen FOV are representative of the whole sample. However, the size range is ideal to identify, separate, and follow different parallel processes in the sample, and to facilitate bridging microscale and multiscale modeling approaches.

The identification of processes occurring in response to CO₂ injection is mandatory in order to fully understand hydrate conversion. We could confirm that, besides gas exchange, gas-hydrate dissociation and the formation of secondary gas hydrates also took place. Initial dissolution of part of the gas hydrate was expected to occur due to the nonequilibrium of the gas-hydrate components (water and guest molecules) in the gas-hydrate phase and in the liquid phase. While the gas distribution could be equilibrated by gas exchange, water was released only by dissociation.

It is noticeable that a process, once it had begun, did not change as long as there was no change in experimental conditions (e.g., a change from flow conditions to no-flow conditions in experiment *Flow*). A gas-hydrate grain that started to dissolve seemed to dissolve completely, and if the solubilities or the equilibrium concentrations in the fluid phase were exceeded, secondary gas hydrates were formed from the freed molecules. This secondary gas-hydrate formation can be rather fast: in the presented CO₂ hydrate maps, secondary CO₂ hydrates started to occur already in early maps. They precipitated very locally in the pore space and usually kept growing from these early nucleations. If there was abundant CH₄ in the fluid phase, it could exchange with or enter into CO₂ hydrates, and a reverse exchange occurs. A recent publication by Pan et al. [63], in which the fate of gas-hydrate grains during gas-hydrate conversion was observed with confocal Raman spectroscopy in combination with optical microscopy, also reported the existence of different microscale processes during gas-hydrate conversion. They could also show that the surface morphology of gas-hydrate grains that were subject to gas-exchange changed, and that a rearrangement of the crystal structure at the grain surface seemed to occur. However, our experimental setup did not allow for the identification of this surface process.

The dominant processes for the redistribution of CH₄ in the system were gas exchange and gas-hydrate dissociation. Their relative contributions appeared to differ among experiments, but most likely, relative contributions were not homogeneous across the sample. During experiment *Flow*, for example, very little dissociation was observed, but the precipitation of secondary gas hydrates hinted at the presence of dissociation outside of the FOV. Our results indicated that, at least at the beginning of the exchange, gas-hydrate dissociation and gas exchange contributed approximately the same amount to CH₄ release. This was likely to change at later times, when released molecules approached equilibrium concentrations in the fluid phase and the driving force for dissolution became smaller. However, due to the restricted experimental time, this behavior could not be observed in our experiments.

Our experiments confirmed that guest molecules can be exchanged in intact gas hydrate grains and do not require a complete dissolution and reformation of gas hydrates,

as postulated in [26], although this process was present in the sample as well, and occurred in parallel. A partial dissolution of the lattice structure at the outer surface of the grains cannot be excluded, but would concern only small volumes of the grains, and the occurrence of free water or ice in the sample was mainly related to gas-hydrate dissolution. The observed existence of different types of gas hydrate in parallel [48,49] also was confirmed by our observations. Gas exchange and secondary gas-hydrate formation occurred in parallel, and could also differ locally due to a variable local availability of the compounds.

The observations for CO₂, which is absent from the initial samples, indicated consistently that about 50% of the reacting CO₂ was involved in gas exchange, and the other ~50% was bound in secondary pure or CO₂-rich gas hydrates. If a local enrichment of CH₄ in the fluid phase was prevented by advective flow or fast diffusion in a gas phase, the secondary gas hydrates were CO₂-rich, while the enhanced and nonuniform local availability of CH₄ in samples with insufficient transport of the released components led to more inhomogeneous secondary gas hydrates.

A very obvious change in sample behavior was observed after the transition from flow conditions to no-flow conditions in experiment *Flow*. An initially quite effective gas exchange came almost to a halt when the flow stopped, and the CH₄ hydrate signal increased even during the no-flow period. This was probably caused by the accumulation of released CH₄ close to the gas-hydrate grains: Diffusive transport is very ineffective in a liquid phase, and when the local CH₄ solubility in CO₂ liq is exceeded, microbubbles could form that are at a higher concentration and are a better-accessible reservoir for CH₄-consuming processes than the dissolved gas in the liquid phase.

4.3. Exchange Dynamics

The quantification of exchange dynamics from the presented gas-hydrate maps has to be carefully considered. Most published hydrate-conversion experiments have been interpreted from the evaluation of bulk sample parameters. One model that describes the bulk evolution of a sample during progression of a reaction front into a solid spherical specimen is the shrinking core model [64]. This model has, with individual modifications, repeatedly been used for the description of the gas-exchange process in solid gas-hydrate grains (e.g., [33,65]). The overall shrinking core conversion ratio α is given by:

$$\alpha = 1 - (2t \times D_{sc}/R_0^2)^{1.5}, \quad (4)$$

where R_0 is the sphere radius, t is the time, and D_{sc} is the shrinking core diffusion constant. While this model seems to be a good approach for an integrated bulk signal, the Raman laser focus was a few μm inside of the grains for most parts of the grain areas in the maps. The expected fast gas exchange at the grain surface was not captured, and the dynamics were dominated by the much slower dynamics inside of the grains. Therefore, it is important to evaluate these kind of point measurements with a position-dependent equation and not with an equation that has been derived for bulk processes. On the other hand, the laser focus is not really a point probe. The focus of the Raman laser nominally collects a signal from a volume with a cross section of only a few μm , which is small compared to the size of the gas-hydrate grains [50,66]. In practice, the sampling volume is further enlarged by scattering and optical effects at transitions between materials with different refractive indices, and there are estimates that only ~50% of a typical confocal Raman signal originates from the focal volume [66]. Nevertheless, the sampled volume is still restricted to less than the volume of one gas-hydrate grain, and can represent a local instead of a global evolution. The unknown focus depth and focus size might be considered to be a relevant source of errors for the evaluation of the data in this manuscript. It is certain that the signals from single pixels in the selected areas did not originate from the same depth, and that the focus itself did collect signal from a finite but diffuse volume, and not from a point as required by the used form of the diffusion equation [50,66]. It turned out that the main uncertainty for the quantification of our data was the radius of the gas-hydrate grain,

which cannot be determined with sufficient accuracy. Therefore, we can neglect the smaller errors arising from the inability to precisely focus the excitation point. One other concern is the lack of knowledge of the exact fluid composition at the gas-hydrate grain boundaries. The exchange depends on the concentration gradient, but the resolution of the maps was not fine enough to resolve this property, and a map from a constant depth could not provide the concentration gradient at the position above the inner grain volume. However, an accumulation of CH₄ in the integral gas phase could not be observed from Raman data. The diffusive and possibly convective transport into the relatively large gas space above the sample seemed to be fast enough to prevent an accumulation at these early stages of the experiment. During flow conditions in experiment *Flow*, the fluid exchange was definitely very effective, as can be seen from the change in process behavior after the stop of the flow. Hence, the assumption of a CH₄-depleted fluid phase and a constant concentration gradient as driving force seems to be a valid assumption for this setup.

The obtained solid-state diffusion coefficients represent an important outcome of the experiments: they were derived from a fraction of the data that could be attributed directly to the gas-exchange process. Unfortunately, because of the discussed uncertainties, we could only determine a range for the diffusion coefficient instead of a reliable number. At ~272 K and 3–3.5 MPa, the derived values for D_{CH_4} were in the order of magnitude 10^{-16} – 10^{-18} m²/s, and the values for D_{CO_2} were in the order of magnitude 10^{-15} – 10^{-17} m²/s. The CO₂ diffusion coefficients tended to be higher than the CH₄ diffusion coefficients. The slower CH₄ diffusion might be intrinsic, but it is also possible that a part of the CH₄ relocated to empty small cages and did not leave the gas-hydrate grain. The initial cage-occupancy ratio of >1 in the experiments *NoFlow*, *NoFlow1*, and *NoFlow2* revealed the presence of empty cages, and shows that the CH₄ hydrates had not reached their steady-state composition (see Figures S1–S4). For the flow-through experiment with liquid CO₂, the derived values for D_{CH_4} and D_{CO_2} were more similar, although the CO₂ diffusion still tended to be about twice as fast. Here, the initial cage occupancy ratio was 1, therefore a high cage occupancy with fewer empty cages was likely. Diffusion coefficients were in the order of magnitude 10^{-13} – 10^{-14} m²/s for both molecules at 281 K and 13–15 MPa. This was several orders of magnitude faster than for the experiments without flow, but the temperature of this experiment was significantly higher and above the freezing point of water. Therefore, it can be excluded that an ice layer formed at the grain surface that hindered guest-molecule migration in and out of the grain. Generally, the exchange kinetics are known to increase with higher temperature [21,65,67,68], and the process is more effective with liquid CO₂ [67], while a pressure dependence has only been observed for gaseous CO₂ and not for liquid CO₂ [21,67]. Published diffusion coefficients for guest molecules in gas hydrates vary by several orders of magnitude. Results from molecular dynamics simulations indicate a higher mobility of the guest molecules. Geng et al. [68] reported diffusion coefficients in the range of 10^{-10} to 10^{-13} m²/s at 270 K and 10^{-9} m²/s at 280 K, and Kondori et al. [69] derived diffusion coefficients in the range of 10^{-10} to 10^{-12} m²/s at temperatures from 270 to 280 K. Graue et al. [36] fitted isothermal phase-field simulations to guest-exchange data from magnetic resonance imaging experiments, and reported a diffusivity coefficient of 1.7×10^{-9} m²/s. The most sophisticated experimental data so far has been published by Salamantin et al. [29]. The authors extrapolated guest-molecule diffusion coefficients from ice/gas-hydrate conversion experiments to their experimental conditions of $T = 277$ K and $p = 3.8$ MPa, and derived at $D_{\text{CH}_4} = 2.8 \times 10^{-14}$ m²/s and $D_{\text{CO}_2} = 8.1 \times 10^{-14}$ m²/s. These values compare well with the ranges that we obtained from our data, but were derived from a more complex model. It can be concluded that the rather simplistic approach of applying a Fickian diffusion equation to the solid-state exchange process did provide diffusion constants in the expected orders of magnitude. The advantage of the model is that a fully analytical solution is available for a constant concentration gradient, i.e., at least for the initial phase of the exchange experiment or for an experiment with an effective fluid exchange. For a bulk phase evaluation of the exchange process, the diffusion equation needs to be rewritten in a form that calculates the amount of CH₄ molecules $n_{\text{CH}_4}(t)$ in a gas-

hydrate grain of radius r as a function of time by integrating the radius-dependent Equation (2) over the grain volume:

$$n_{CH_4}(t) = \frac{8C_0R_0^3}{\pi} \sum_{j=1}^{\infty} \frac{1}{j^2} e^{-\frac{j^2\pi^2D}{R_0^2}t}. \quad (5)$$

One other important observation from our data was that, at least at early stages, CH₄ hydrate dissolution and secondary CO₂ hydrate formation occurred in parallel to gas exchange, and those contributions cannot be neglected. Therefore, any type of equation for the modeling of bulk CH₄ release through gas exchange should be supplemented with an equation for the release of CH₄ from gas-hydrate dissociation:

$$n_{CH_4}(t) = n_{\text{exchange}}(t) + n_{\text{dissociation}}(t) \quad (6)$$

A formalism for the description of the dissociation of gas hydrate can, for example be found in the works of Kim et al. and Clarke and Bishnoi [70,71], and further dissociation kinetic models are listed in the review article by Kondori et al. [25]. It is possible that the dissociation process comes to a stop when the initially dissociating grains are completely decomposed and a transition to pure gas exchange might need to be implemented in a thorough modeling approach.

The gas-exchange process with diffusion coefficients $D < 10^{-13}$ m²/s is too slow for an economically feasible gas-hydrate exploitation, and it is commonly agreed that a commercial approach that includes gas exchange needs to be combined with a second production method like pressure reduction. The resulting dynamic gas-hydrate system can be even more complex than the ones described here [72], and the development of a relatively simple and robust mathematical formalism for modeling of the system evolution is mandatory. The shrinking core equation is such a simplistic approach, but it is not suitable for a description of the initial fast exchange at the surface of the gas-hydrate grains. One possibility to tackle this shortcoming is the combination of the shrinking core model with a faster decaying equation like the Avrami equation [63,65]. With the use of the common diffusion equation plus a dissociation term, we propose an alternate robust tool for the evaluation of bulk data from gas-exchange experiments.

Supplementary Materials: The following are available online at www.mdpi.com/1996-1073/14/6/1763/s1, Table S1: Raman measurement parameters, Figures S1–S4: CH₄ cage-occupancy ratios, Figure S5: Pressure curve of experiment *Flow*.

Author Contributions: Conceptualization, N.K.B., C.D., and M.H.; methodology, E.K., N.K.B., C.D., and M.H.; software, E.K. and N.K.B.; formal analysis, E.K.; investigation, N.K.B. and E.K.; writing—original draft preparation, E.K.; writing—review and editing, E.K., N.K.B., C.D., and M.H.; visualization, E.K. and C.D.; supervision, M.H.; project administration, M.H.; funding acquisition, M.H. All authors have read and agreed to the published version of the manuscript.

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Data Availability Statement: Data will be made available in the Pangaea data base (www.pangaea.de) and linked to this publication. While the data is not published, please contact the corresponding author for questions and requests.

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Conflicts of Interest: The authors declare no conflict of interest.

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