

1 **An investigation of particle breakage in loess**

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31 **Abstract**

32 The paper presents a detailed experimental investigation of particle breakage in three
33 kinds of loess, i.e., sandy loess, silty loess and clayey loess. It is firstly found that
34 particle breakage can occur within loess in oedometer test, which results in a better-
35 graded soil at the end of the test. Initial breakage stresses for both the silty and clayey
36 loess are less than 0.5 MPa, and about 2 MPa for the sandy loess. The relative breakage
37 (B_r) is used to evaluate the particle breakage degree, and it is found that for all the three
38 kinds of loess tested, B_r increases with the increasing loading stress until it reaches a
39 threshold, after which B_r tends to keep a constant value. Particles within the loose
40 specimens break more easily than those within the dense ones, especially for the sandy
41 and silty loess. It is also observed that for the specimens reconstituted with previously
42 tested soils, particle breakage degree decreases significantly, which means little particle
43 breakage occurs in the pre-crushed specimens.

44 **Keywords**

45 Loess, Particle breakage, Compression, Soil grading

46

47 **1. Introduction**

48 Loess is a typical silt-sized soil (Liu, 1985). But it is a special soil with a bonded
49 structure that is sensitive to rainfall, erosion, cyclic loading, and human activities (Peng
50 et al., 2019). The mechanical behavior of loess has been extensively studied through
51 laboratory tests, whereas there has been no investigation of its particle breakage.
52 Virtually all investigations involving soil testing above normal geotechnical pressures
53 have resulted in considerable particle breakage (Hardin,1985; Bishop,1966; Terzaghi
54 and Peck,1948). For example, the particles at the bottom of a high dam or the tip of pile,
55 especially during driving, or in the sliding zone of a landslide (Indraratna et al., 1998).
56 In recent years, some geotechnical mega-projects have been carried out in the loess area
57 of China such as the removal of the tops of mountains and infilling of valleys by
58 compaction (Li et al., 2014). Particle breakage might occur in these cases. Hence an
59 investigation of loess particle breakage is necessary to identify the engineering
60 properties of such granular materials.

61

62 Particle morphology (shape, size, angularity, roundness, and the surface roughness etc.),
63 particle composition (initial void ratio and gradation), loading conditions (state of
64 effective stress, effective stress path) and the constituent minerals are the main
65 influencing factors that affect the amount of particle breakage. The relationship between
66 these factors and the soil crushing strength as well as the empirical correlations has
67 been studied by many researchers (Zhang et al., 2019; Mehta and Patel, 2017; Xiao et
68 al., 2017; Shahnazari and Rezvani, 2013; Altuhafi and Coop, 2011b; Erzin et al., 2012;
69 Arasan et al., 2011; Feda, 2002; Lade et al., 1996). It was reported that the larger and
70 angular particles in soil with less quartz percentage break more easily (Erzin and Yilmaz,
71 2008). And the stress state of sufficient magnitude is the key factor that determines the

72 quantity of particle breakage (Altuhafi and Coop, 2011b). The relative density of soil
73 affects the inter-particle contacts and average contact stress, which in turn determines
74 the crushing characteristics (Erzin and Yilmaz, 2008; Lade, et al. 1996).

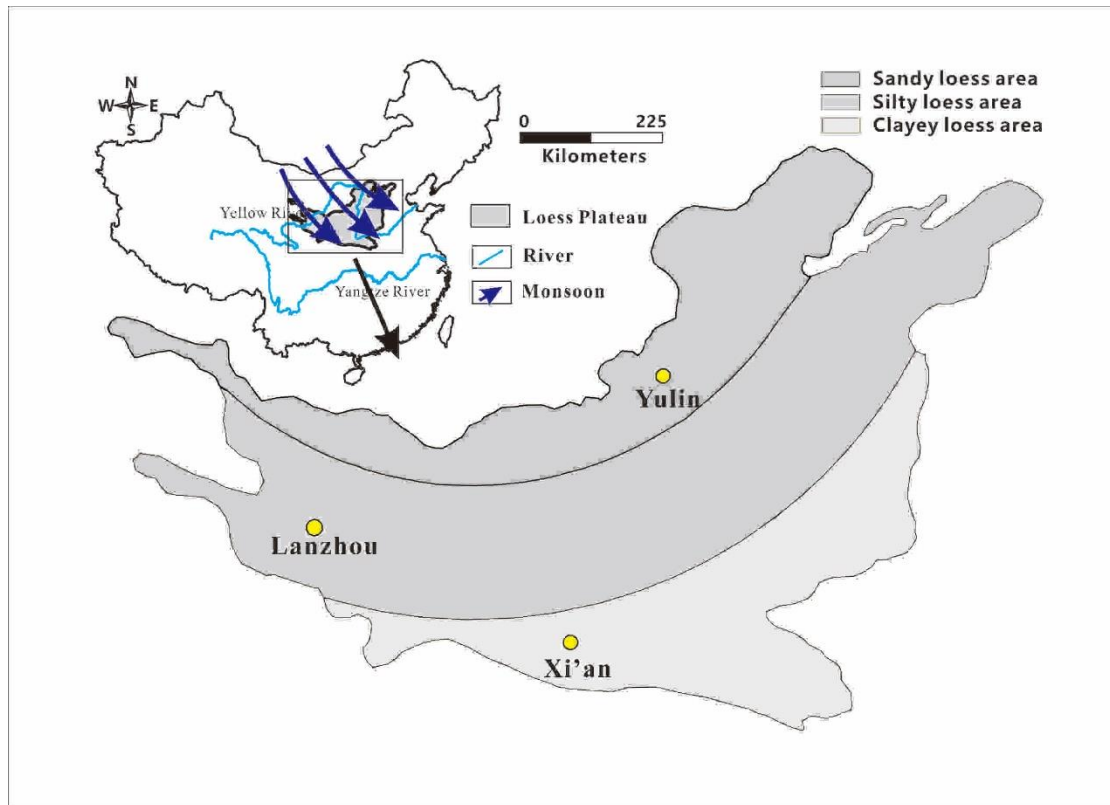
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76 Particle breakage alters the matrix of particle size distribution (PSD) and the pore size
77 distribution (Mehta and Patel, 2018), which is directly linked to the engineering
78 behavior of soils, such as the hydraulic conductivity (Valdes and Caban, 2006), stiffness
79 (Fu et al., 2014), strength (Indraratna et al., 1998), dilatancy (Liu and Gao, 2016; Wang
80 et al., 2019), and critical states (Bandini and Coop, 2011; Ghafghazi et al., 2014; Wood
81 and Maeda, 2008; Coop et al., 2004). The above studies mainly focused on the particle
82 breakage of sands, ballast, coal, rockfill and cemented soils. The loess soils are mainly
83 composed of more silt-sized particles (0.005~0.075 mm) than the sands and other
84 granular soils reported. The silt grains can be about 50-100% of the total weight,
85 varying with locations in China (Liu, 1985). Recently, there are evidences showing that
86 particle breakage occurs in silty-sized iron tailings (Li and Coop, 2019). It therefore
87 raises questions whether the silts of loess will break down during loading and whether
88 the crushed particles will affect the compression behavior of loess.

89

90 A series of oedometer tests were therefore conducted to explore loess particle breakage.
91 Three loess zones have been identified in China, namely the sandy, silty and clayey
92 loess zones according to the PSD. The loess specimens used in this study were retrieved
93 from Yulin city (the sandy loess zone), Lanzhou city (the silty loess zone) and Xi'an
94 city (the clayey loess zone), respectively. The sampling locations are shown in Fig. 1.
95 Note that the clayey loess is actually finer silty loess though it was retrieved from the
96 clayey loess zone. Although it does have more clay-sized particles than the silty and

97 sandy loess, it is still composed predominantly of silts (Fig. 2). A laser particle size
98 analyzer was used in the study to identify the particle breakage through capturing the
99 variations of PSD. This method avoids human interference to the greatest extent
100 possible. In addition, the required quantity of soil is small.
101



102
103 Fig. 1 Sampling sites on the loess plateau of China
104

105 2. Materials and Methods

106 Fig. 2 presents the PSD curves of the loess before testing. The results were obtained
107 with a Mastersizer 2000 laser diffractometer. For each soil, an average value of three
108 parallel measurement results was used to capture the soil particle size accurately. The
109 percentages of fine particles (less than 0.005 mm) are about 2.2%, 3.7% and 20.1% for
110 sandy loess of Yulin, silty loess of Lanzhou and clayey loess of Xi'an, respectively.

111

112 The index properties for the three materials are presented in Table 1. The specific
113 gravity of the loess is about 2.68 ~ 2.73. The coefficient of uniformity C_u and the
114 coefficient of curvature C_c that characterize the shape of the PSD curve are expressed
115 in Eq. (1) and Eq. (2). Fig. 3 shows the plasticity chart for the soils. The clayey loess
116 has a medium plasticity while the sandy and silty loess have a low plasticity. Fig. 4
117 shows the mineral compositions of the samples. The main mineral components are
118 quartz, albite, calcite and clay minerals for all tested materials. From the sandy loess to
119 the clayey loess, the contents of quartz and albite decrease while the calcite and clay
120 minerals increase with the increasing proportion of fine particles.

121

$$122 \quad C_u = \frac{D_{60}}{D_{10}} \quad (1)$$

$$123 \quad C_c = \frac{D_{30}^2}{D_{60}D_{10}} \quad (2)$$

124 where the C_u is coefficient of uniformity, C_c is the coefficient of curvature, D_{10} , D_{30}
125 and D_{60} are the particle diameters at 10%,30%, and 60% of passing mass of soil.

126

127 Oedometer tests were carried out to investigate the particle breakage under loading. The
128 maximum vertical stress applied ranges from 0.1 to 35 MPa. The height and diameter
129 of the oedometer ring were 20 mm and 50 mm, respectively, except in the 35 MPa tests,
130 for which the height and diameter were both 20 mm. It was demonstrated that the
131 sample size has negligible effect on particle breakage by analyzing the PSDs of samples
132 with 20 mm and 50 mm diameter cells before and after tests. All the reconstituted
133 specimens were prepared using the wet compaction method at a water content of about
134 10% by weight. The wet soil was mixed evenly and then compacted by 3 layers in a

135 split mold. The compaction hammer weighs 570 g and falls from 20 cm height above
136 the top of the ring. After the specimens were prepared, vacuum saturation method was
137 adopted to saturate the specimens. Then the specimens were loaded in stages to reach
138 the chosen maximum vertical stress. The specimen deformation is related to the content
139 of clay particles as well as the applied stress level. The end standard of the consolidation
140 test in this study is that the deformation within 1 hour is less than 0.01 mm to avoid
141 creep (Leung et al., 1996; Takei et al., 2001). For the loess specimens with a vertical
142 loading stress of less than 1 Mpa, 4 hours are enough to reach the end standard. For the
143 tests that the maximum vertical loading of 35 MPa is applied, 16 hours of loading are
144 needed. The oedometer cells were filled with water to make certain that all suctions
145 were dissipated. At the end of each test, unload to the final stage of 12.5 kPa and
146 maintain no less than 12 hours. After fully unloaded, the final water content of
147 specimens was measured. The initial specific volume v_i equals to $1+e$ was calculated
148 by two independent ways, as shown in Eq. (3) and Eq. (4), from the initial specimen
149 volume and final water content measurements. An average results of these two methods
150 was taken. The tests with the two specific volume values with difference greater than
151 0.04 were discarded.

152

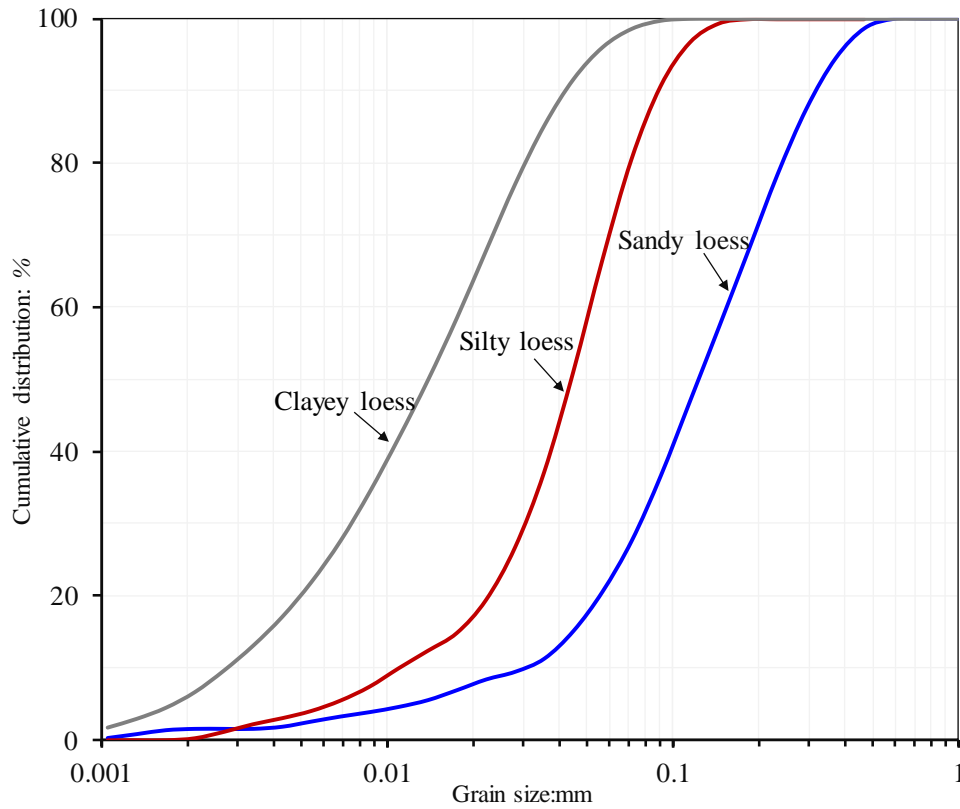
$$153 \quad v_i = \frac{G_s \gamma_w (1 + w_i)}{\gamma_i} \quad (3)$$

$$154 \quad v_i = \frac{G_s w_f + 1}{1 - \varepsilon_v} \quad (4)$$

155 where the G_s is the specific gravity, γ_w is the unit weight of water, γ_i is initial bulk
156 unit weight, w_i and w_f are the initial and final water contents, and ε_v is the volumetric
157 strain.

158

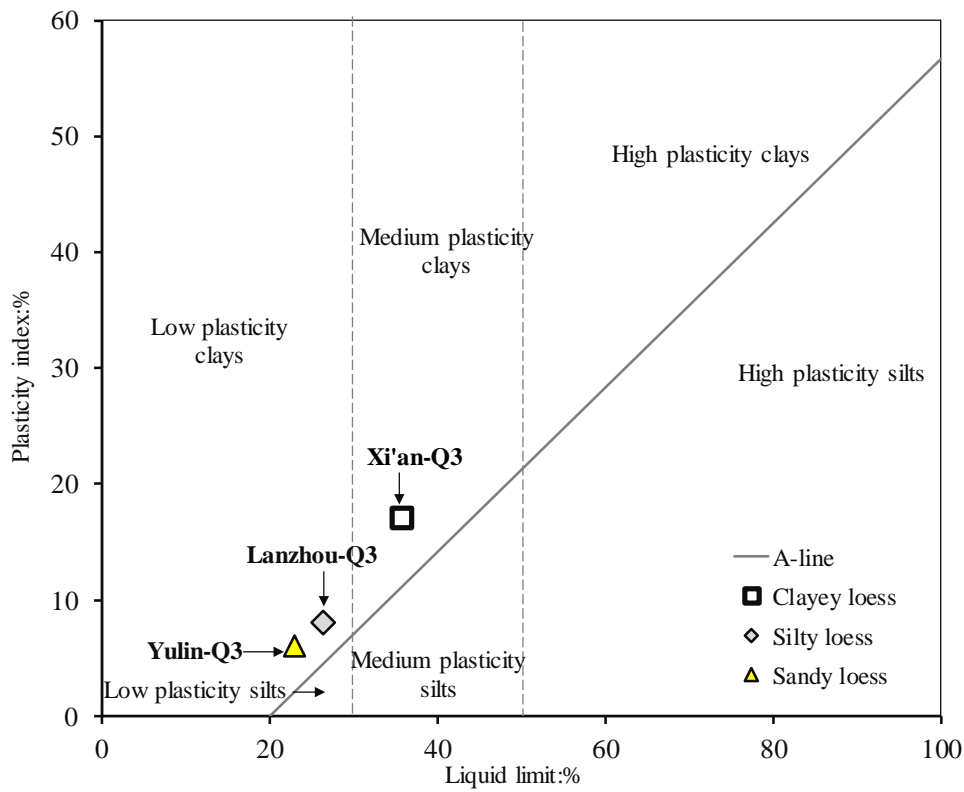
159 Particle breakage during oedometer compression is characterized by capturing the
160 PSDs before and after tests, respectively. In this study, three aspects of particle breakage
161 have been investigated. Firstly, the relationship between particle breakage and the
162 maximum applied vertical stress was studied. In order to eliminate the influence of soil
163 density, efforts were made to create specimens with a given initial void ratio. Secondly,
164 influence of soil initial density on the particle breakage has been identified. To avoid
165 particle breakage in the process of specimen preparation, as pointed out by Sun et al.
166 (2019), the specimens were not compacted to extreme densities. The PSDs of the soils
167 before and after specimen preparation were examined. The results indicated that there
168 was no particle breakage in the specimen preparation. Lastly, to explore the influence
169 of repeated loading on the soil particle breakage, some pre-crushed specimens were
170 remolded and tested again. To provide enough soil materials for the pre-crushed
171 specimen preparation, at least three parallel oedometer tests were carried out under the
172 same conditions. The pre-crushed specimens were then prepared by reconstituting the
173 specimens that had been tested. The first-level pre-crushed specimens were prepared
174 using the tested specimens of uncrushed loess (natural loess). Second-level pre-crushed
175 specimens were prepared using the first-level pre-crushed specimens after testing.



176

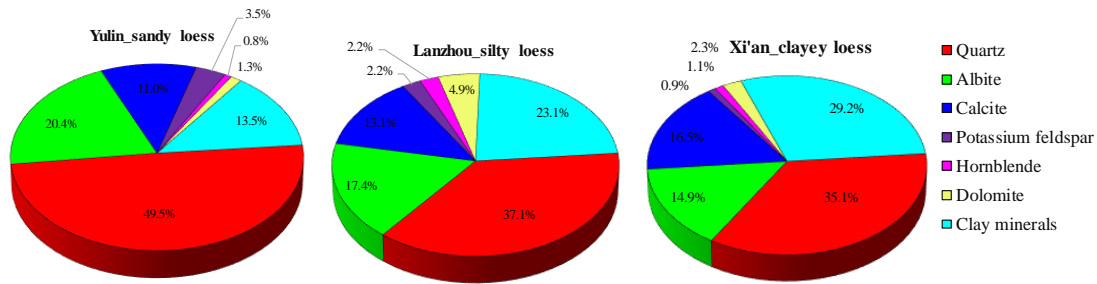
177 Fig. 2 Initial PSD of the loess soils

178



179

180 Fig. 3 Casagrande classification chart for the specimens



181
182 Fig. 4 Mineralogical compositions of the loess
183

184 Table-1 The index properties of the loess

Type of soil	Sampling location	G_s	Liquid Limit (LL)	Plasticity Index (PI)	Percentage finer (<5 μ m)	C_u	C_c
Sandy loess	Yulin	2.68	22.9	6.0	2.2%	4.95	1.22
Silty loess	Lanzhou	2.73	32.0	19.8	3.7%	3.71	1.21
Clayey loess	Xi'an	2.72	25.3	4.9	20.1%	6.64	1.12

185

186 Table-2 Details of the oedometer tests

Loess type	Test number	Sampling location	Preparation method	Initial specific volume: v_0	$\sigma_{v' \max}$ (MPa)	Final specific volume: v_f
Sandy loess	01	YL	WC	1.719	5.6	1.415
	02	YL	WC	1.753	15	1.311
	03	YL	WC	1.742	0.5	1.581
	04	YL	WC	1.736	2	1.519
	05	YL	WC	1.598	2	1.497
	06	YL	WC	1.803	3	1.472
	07	YL	WC	1.499	5.6	1.403
	08	YL	WC	1.543	15	1.365
	09	YL	WC	1.405	18	1.330
	10	YL	WC	1.469	25	1.348
	11	YL	WC	1.504	35	1.328
	12	YL	WC	1.718	35	1.324
	13	YL	WC	1.780	4	1.456
	14	YL	WC*	1.783	4	1.457
	15	YL	WC**	1.772	4	1.448
Silty loess	16	LZ	WC	2.116	4	1.709
	17	LZ	WC	2.053	15	1.517
	18	LZ	WC	1.937	0.5	1.772
	19	LZ	WC	2.022	1	1.752
	20	LZ	WC	1.714	1	1.654
	21	LZ	WC	1.966	2	1.696
	22	LZ	WC	2.054	4	1.637
	23	LZ	WC	1.799	4	1.620
	24	LZ	WC	1.823	10	1.543

	25	LZ	WC	1.987	15	1.483
	26	LZ	WC	1.694	15	1.485
	27	LZ	WC	1.762	25	1.466
	28	LZ	WC	1.787	35	1.439
	29	LZ	WC	1.943	35	1.366
	30	LZ	WC	2.066	4	1.639
	31	LZ	WC*	1.968	4	1.616
	32	LZ	WC**	1.946	4	1.600
	33	XA	WC	2.042	1.6	1.480
	34	XA	WC	2.096	5	1.411
	35	XA	WC	2.083	15	1.325
	36	XA	WC	1.986	0.1	1.820
	37	XA	WC	2.073	0.5	1.632
	38	XA	WC	2.086	1	1.559
	39	XA	WC	1.650	1	1.558
	40	XA	WC	1.986	1.6	1.484
Clayey loess	41	XA	WC	0.931	2	0.493
	42	XA	WC	2.577	4	2.131
	43	XA	WC	1.570	5	1.385
	44	XA	WC	1.660	15	1.315
	45	XA	WC	1.920	30	1.309
	46	XA	WC	1.910	4	1.419
	47	XA	WC*	1.953	4	1.432
	48	XA	WC**	1.849	4	1.400

187 Notations: YL, Yulin; XA, Xi'an; LZ, Lanzhou; WC, wet compaction; WC*, the first
188 level pre-crushed specimen by compaction method; WC**, the second level pre-
189 crushed specimen by compaction method.
190

191 3. Test results and analysis

192 3.1. Influence of stress level on particle breakage

193 Fig. 5 presents the results of tests in which the maximum vertical stresses applied were
194 different. It shows that the three types of loess have different shapes in their
195 compression paths and one-dimensional normal compression lines (1D-NCLs).
196 Although the clayey loess has low clay content, its compression path is more like that
197 of a clay soil. The compression path reaches its 1D-NCL at only a few tens of kPa, and
198 the 1D-NCL is concave upwards. With the increase of coarser particles, the slopes of
199 1D-NCL (compression index) of clayey loess, silty loess and sandy loess reach 0.09,

200 0.13 and 0.09, respectively. The compression paths of silty loess at the end of the tests
201 are even above the clayey loess though the latter had the loosest initial density. The silty
202 and sandy loess show a typical sandy or silty mode of behavior as expected, where the
203 compression curves are convex upwards and then reach a unique 1D-NCL only at high
204 stresses. In these cases, the loess tends to a higher compressibility at higher stresses
205 after experiencing an initially low compressibility. The yield of the sandy and silty loess
206 is very gradual, in contrast to poorly graded sands, but which is typical for better graded
207 silty soils (Vilhar et al., 2013).

208

209 Fig. 6 presents the PSDs of the soils before and after testing, respectively. The applied
210 maximum vertical stresses for the oedometer tests are labelled. The PSDs of the soils
211 after testing are clearly different from those before the test. For the clayey loess, the
212 significant particle breakage seems to commence at about 0.1 MPa ~ 0.5 MPa, while
213 for the sandy loess it starts at about 2 MPa ~ 3 MPa. For the silty loess, the lowest
214 maximum vertical stress applied was 0.5 MPa, for which the particle breakage was
215 already significant. With further increases of the maximum vertical stress, there is more
216 particle breakage.

217

218 From Fig. 6, at higher stresses the particle breakage of the clayey loess is clearly less
219 than that of silty loess. The latter is then less than that for the sandy loess. This is
220 consistent with the dependence of breakage on particle size identified by McDowell et
221 al. (1996), even if the stress at which that breakage starts is not the same. Detailed
222 comparisons cannot be made as there are differences of grading uniformity and of
223 mineralogy among the various soils. For example, the sandy loess has a similar grading
224 to an alluvial silty sand tested by Vilhar et al. (2013). But the breakage of sandy loess

225 is very much greater.

226

227 More details about the size of the particles broken in the test can be found in Fig. 7,
228 which presents the density distributions of different sized particles in the specimens
229 before and after testing. It is observed that the tested silty loess has a distribution that
230 keeps the peak at about the same point, while for the sandy loess the peak migrates to
231 the left and for the clayey loess the peak migrates slightly to the right although the
232 clayey loess cannot cross the initial grading, of course, so it is constrained. The main
233 particle sizes that are broken in the sandy, silty, and clayey loess are about 0.1~0.6 mm,
234 0.03~0.1 mm and 0.007~0.025 mm, respectively. These particle size ranges do not
235 overlap with each other, reflecting the particle breakage dose not significantly change
236 the PSDs of tested loess. The new finer particles generated due to breakage mainly
237 accumulate in the sizes of 0.001~0.15 mm, 0.001~0.03 mm and 0.001~0.007 mm for
238 the sandy, silty, and clayey loess respectively. It seems that the coarser particles break
239 into a wider range of finer particles.

240

241 It is interesting to observe where the breakage occurs in each soil. In the clayey loess,
242 the coarser particles of 0.025-0.08 mm the percentage of which is 21%, did not break
243 much. However, this size range is mostly prone to break in the silty loess. In contrast
244 with the sandy loess, the particle sizes of this range probably did not break much as
245 there is an accumulation in this size range. However, this does not mean that there is no
246 breakage in the size range although the accumulation is greater than any breakage. The
247 large-scale breakage of sandy loess was predominantly in the coarser particle fraction.
248 Herein, as the grading of samples gradually change from sandy loess, silty loess to
249 clayey loess, the breakage within each soil moves towards the finer fraction of each soil.

250 These observations for the sandy loess contrast what has been observed in poorly-
251 graded sands, where the breakage occurs preferentially in the finer gradings, leading to
252 a tendency towards fractal gradings (McDowell and Bolton, 1998). Although in gap
253 graded soils, similar breakage in both the coarse and fine fractions has been observed
254 in sandy loess (Zhang et al., 2017).

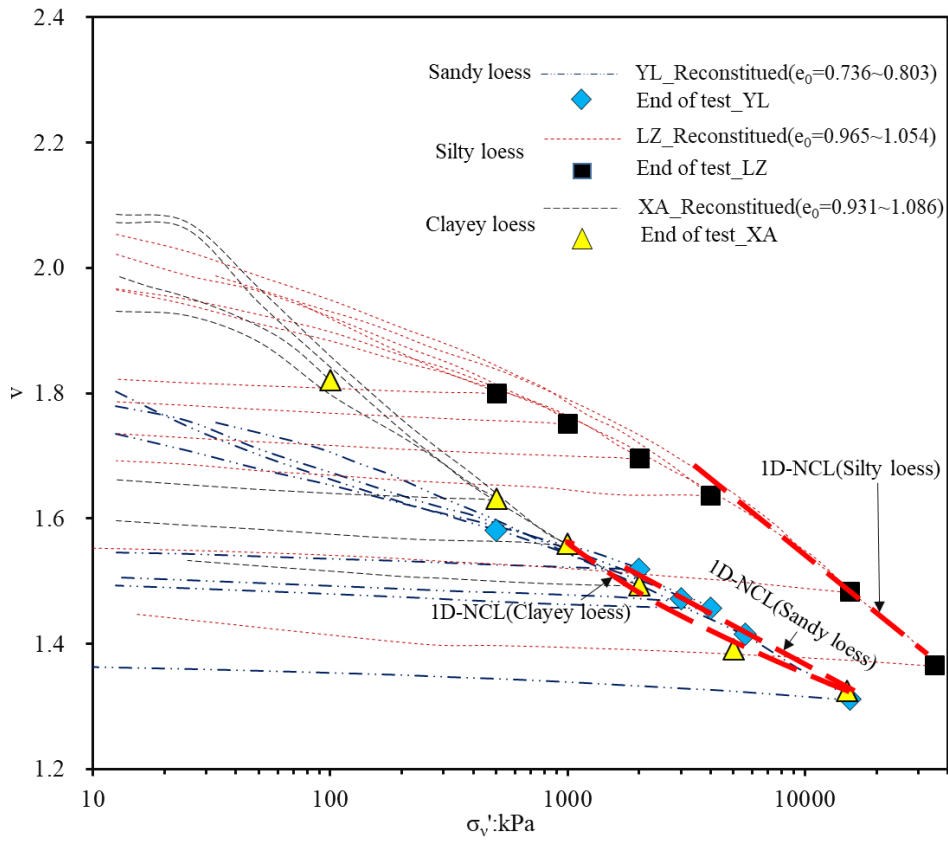
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256 Fig. 8 shows the SEM images before and after tests, respectively, illustrating the
257 particles and their arrangement in the specimens. Generally, the mean particle size of
258 the specimens after test are smaller than those prior to loading though the soil density
259 after test is much larger than that before test. For the sandy loess, it is clear that the
260 particles with dimensions larger than 100 μm decrease due to particle breakage. In these
261 cases, the particle fractures can be clearly seen but the pieces still remained in close
262 proximity to each other. The coarse particles were originally irregular in shape with
263 some angular corners which may have generated their breakage (Erzin and Yilmaz,
264 2008). For the silty loess, the particles with dimensions larger than 50 μm decrease due
265 to particle breakage. For the clayey loess, the change is not obvious. This is mainly
266 because that particle breakage is very small and the soil experienced a more
267 significantly compression. In this case, it is much difficult to identify particle size
268 variations from SEM image observations. Some large particles can also be seen in the
269 clayey loess, immersed in a matrix of greatly increased fines. It is evident from the SEM
270 images that some of the particles are aggregated fines, which is easy to break once the
271 vertical loading was applied. However, the grading changes would not reflect the
272 aggregate breakages because the laser diffractometry method requires the specimen to
273 be stirred in a water bath which would break them up.

274

275 Based on the PSDs (Figs. 6 and 7) and the SEM images (Fig. 8), three micro-fabric
276 models for the clayey loess, silty loess and sandy loess are proposed as illustrated in
277 Fig. 9. For the clayey loess, the percentage of fine particles (<0.025 mm) are 70%. The
278 coarse particles (>0.025 mm) are largely isolated by the matrix of fine particles (Fig.
279 9a) and may not form a percolating system. Herein, the force transmission is through
280 the contacts between the fine particles and contacts between the fine particles and the
281 coarse particles or fines aggregates. Consistently with McDowell and Bolton (1998),
282 for a given vertical stress, the higher coordination number of the large particles allows
283 them to survive. As the stress increases, the content of large-sized particles in the clay
284 loess does not change significantly referring to the particle size between 0.025 and 0.08
285 mm, rather than continuous to decrease. For the particles in these size ranges, with the
286 increase of loading stress, the variations of particle breakage can be neglected. For the
287 silty loess, the percentage of fine particles (<0.03 mm) are less than 25%, while the
288 coarse particles of silts (0.03-0.075 mm) and sands (0.075-0.08 mm) make up about 58%
289 and 17%, respectively. For the sandy loess, the percentage of sand particles (0.075-0.6
290 mm) is 72%. As the coarse particle content increases from the clayey, silty to sandy
291 loess, it forms a percolating system with the fines increasingly in the between voids so
292 that the breakage shifts towards the coarser fraction.

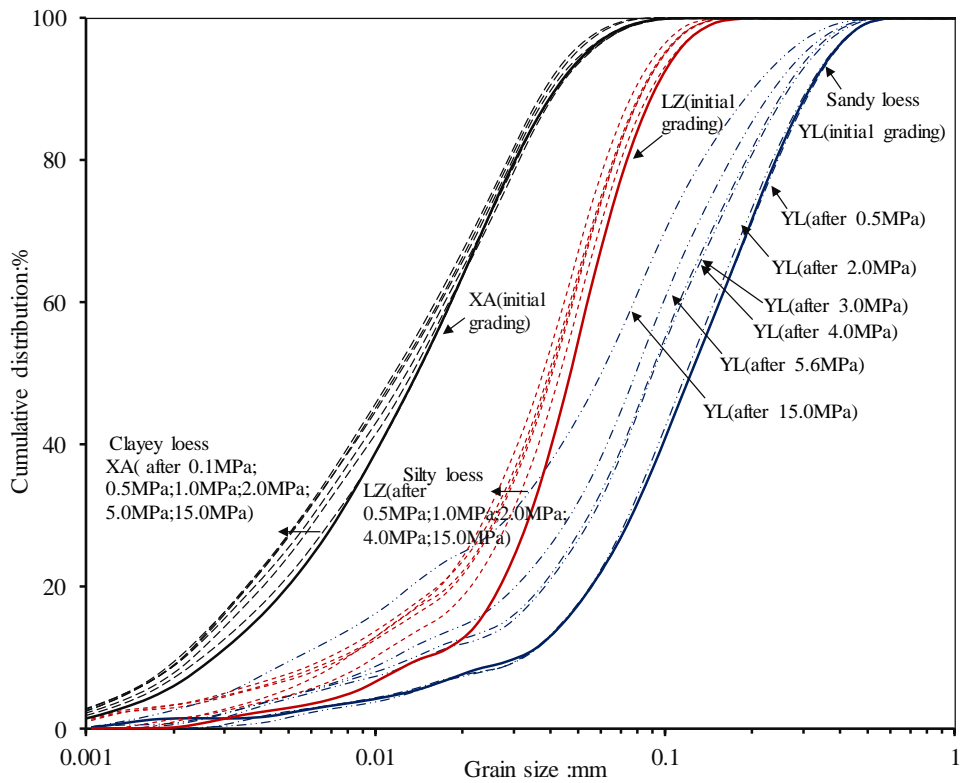
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295 Fig. 5 The compression curves obtained from the oedometer tests

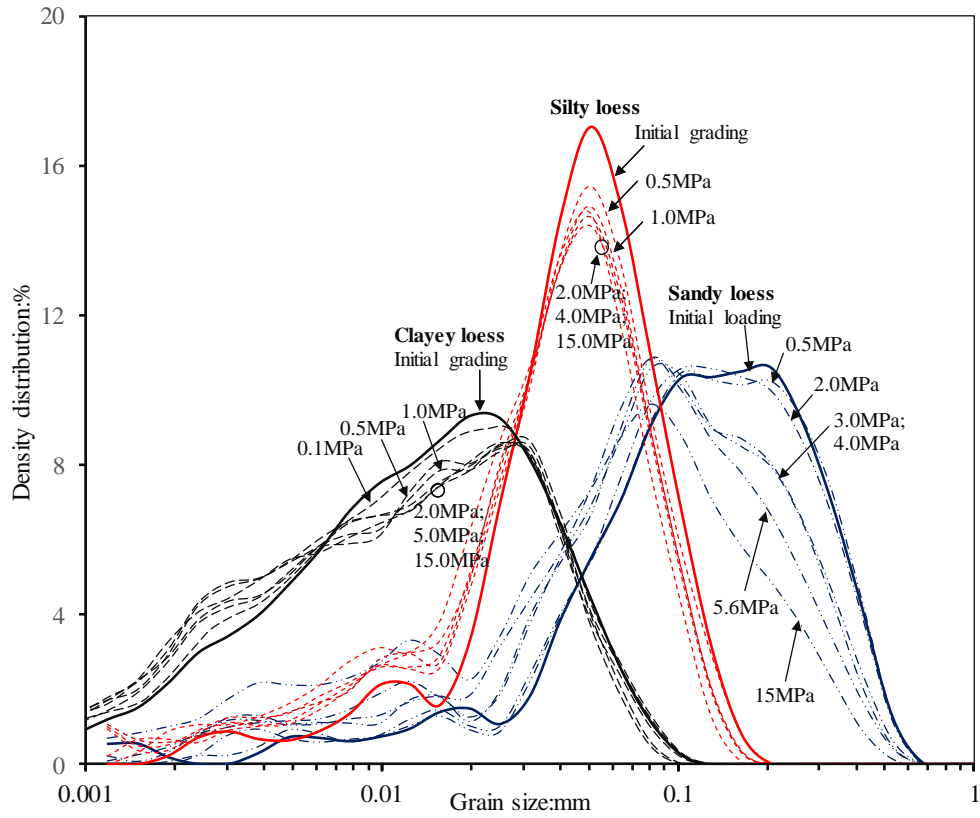
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298 Fig. 6 PSD curves of the loess in initial condition and after testing

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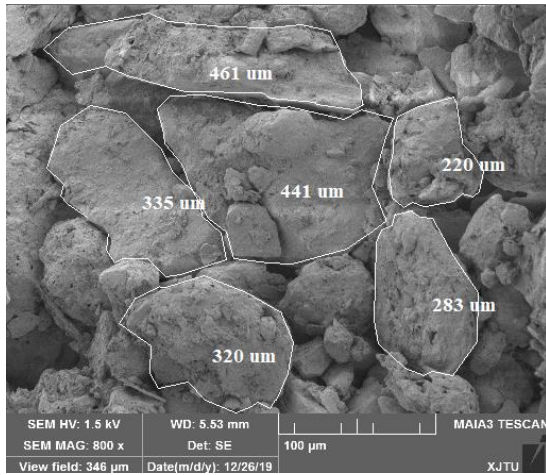


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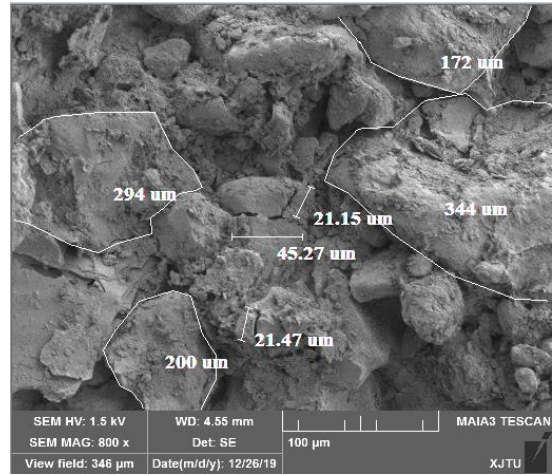
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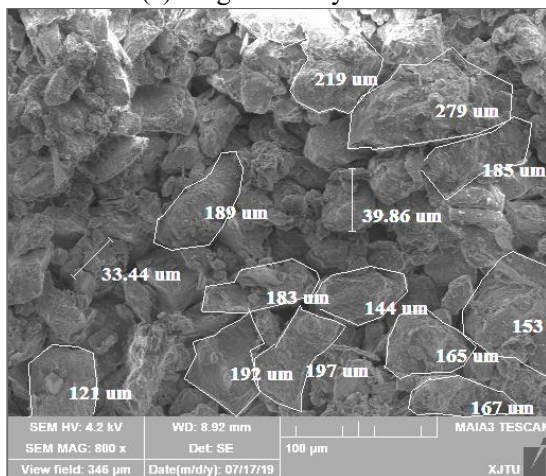
Fig. 7 Density distributions of particle sizes before and after testing



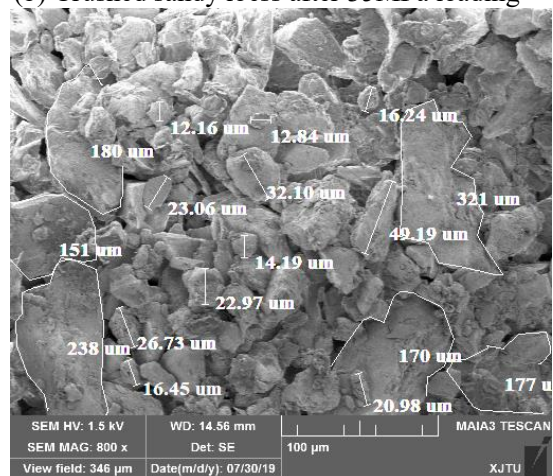
(a) Original sandy loess



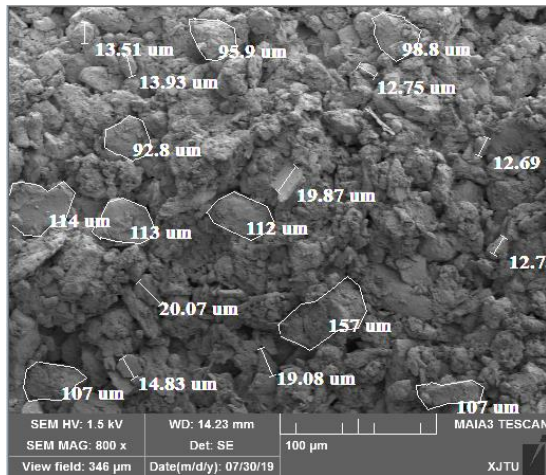
(b) Crushed sandy loess after 35MPa loading



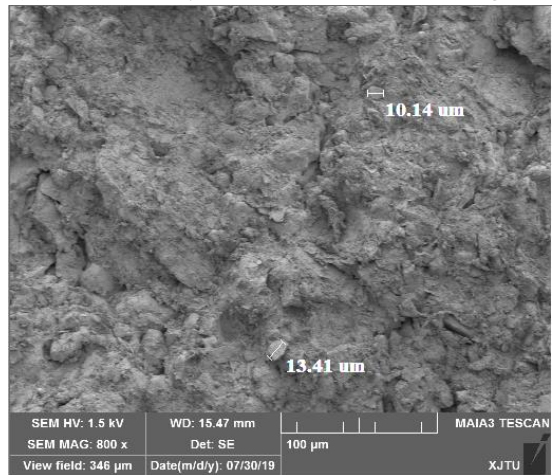
(c) Original silty loess



(d) Crushed silty loess after 35MPa loading



(e) Original clayey loess



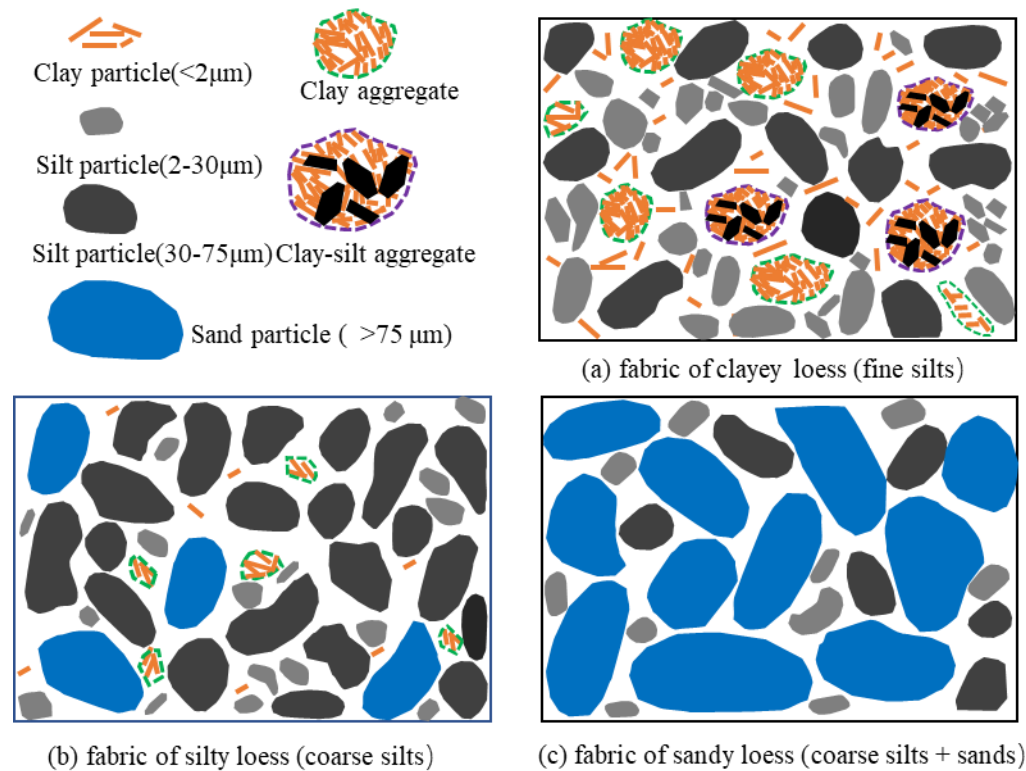
(f) Crushed clayey loess after 35MPa loading

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304

Fig. 8 SEM images of the original soils and crushed soils after 35 MPa vertical loading stress of Yulin sandy loess, Lanzhou silty loess and Xi'an clayey loess

306



307

308 Fig. 9 Fabric models proposed for three loess soils

309

310 The relative breakage (B_r) developed by Hardin (1985) as illustrated in Fig. 10 is a

311 commonly used parameter to quantify the particle breakage, which is adopted in this

312 study. The assumption that the finest particles don't contribute to the breakage has been

313 verified in this particle breakage analysis. However, Hardin had a cut off at 0.074 mm

314 because he used sieving while in this study it is clear that the finer particles break. For

315 rock minerals, the comminution limit is in the order of 1 μm and the particles of less

316 than 1 μm is neglectable (Vilhar et al., 2013). For the tested loess, their particles are

317 even coarser than the rock materials, of which the particles size of less than 2 μm are

318 neglectable. In this study, 2 μm was taken as the crushing limit to define B_r .

319

320 Fig. 11 shows the results of B_r versus the maximum vertical stress applied in the

321 oedometer tests, the compression paths of which were presented in Fig. 5. As discussed

322 above, the initial stress that caused the particle breakage is less than 0.5 MPa for the
323 clayey and silty loess, and less than 3 MPa for the sandy loess. Once breakage
324 commences, B_r increases rapidly with increasing stress initially. However, after about
325 2 MPa, the B_r of the clayey and silty loess tend towards more constant values, or at
326 least the breakage decelerates rapidly, with much less further breakage in the specimen.
327 The B_r value at 30 MPa for the clayey loess decreases due to some small experimental
328 scatter. The slowing down of the breakage occurs because of the increase of
329 coordination numbers due to the large increase of the numbers of finer particles. For
330 the sandy loess, the B_r value continuously increases though it tends to increase more
331 slowly when the maximum vertical stress of 35 MPa was applied. This may be due to
332 that sandy loess has a higher proportion of quartz, which is a mineral with greater
333 strength (Fig. 4), while the silty and clayey loess have higher proportions of feldspars
334 (albite and potassium) along with calcite/dolomite, which are all weaker minerals
335 (Nakata et al., 1999). On the other hand, these differences may also be linked to the
336 predominance of breakage in different parts of the PSD.

337

338 The input specific work, W is introduced here to explore the factors to influence B_r .
339 According to the experimental conclusion of Indraratna and Salim (2002), the total
340 input energy should eventually be converted to particle rearrangement, particle friction
341 and particle breakage energy consumption. The W can be calculated with the
342 integration, as shown in Eq.(5)

$$343 \quad W = \int \sigma'_a d\varepsilon_a \quad (5)$$

344 where σ'_a is the vertical stress and ε_a is the axial strain.

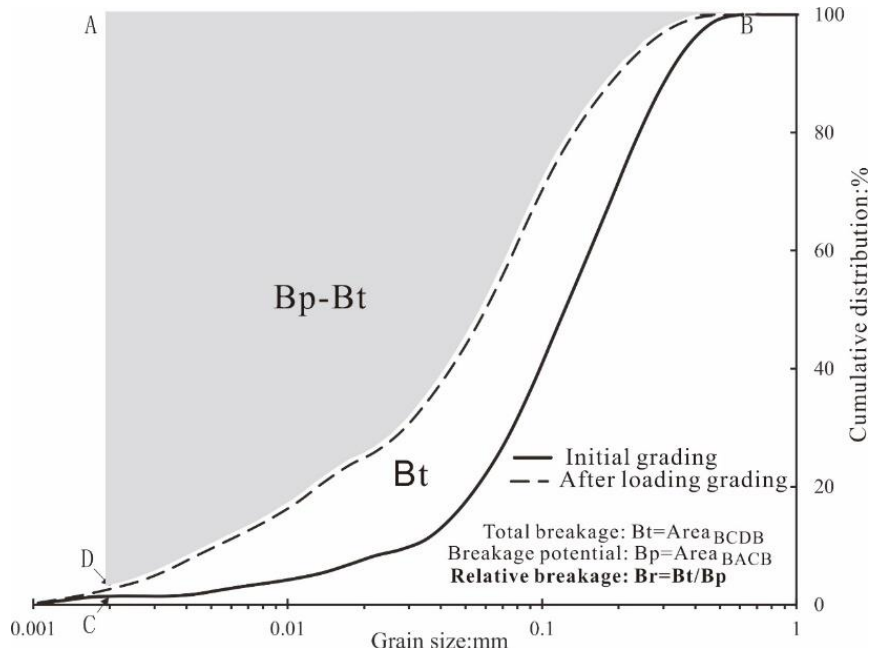
345

346 The input specific work is calculated from the vertical stress at the beginning of test as
347 the starting point, until the end of test. The relationship between B_r and W during
348 the compression process is presented in Fig. 12. With the increase of the W , the B_r
349 increases non-linearly, which has also been validated by many researchers (Xiao et al.,
350 2019;Huang et al., 2014). The law of B_r and W is consistent with that of B_r and
351 the maximum vertical stress, indicating that the input work of the samples with similar
352 initial void ratio is mainly affected by vertical stress during the loading process. At the
353 initial stage, the clayey loess and silty loess have a higher B_r value than that of the
354 sandy loess. It indicates that the clayey loess and silty loess are easier to break than the
355 sandy loess. But with the increasing W , the B_r approximately reaches a constant
356 value.

357

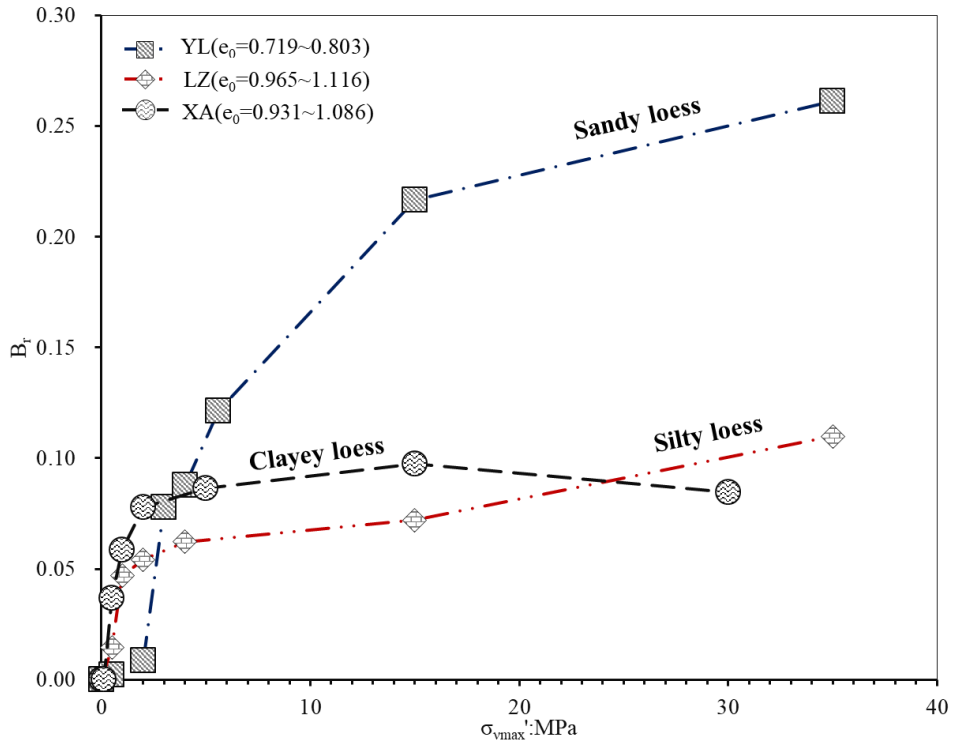
358 Relative breakage B_r has a significant advantage of representing the overall amount
359 of breakage as a single parameter. But it does not consider the differences of soil grading
360 or the characteristics of the grain-size distribution (Yu et al., 2019). In this study, the
361 interacting effects of soil grading on particle breakage and the influence of particle
362 breakage on grading were identified. Two parameters, the mean particle size (D_{50}) and
363 the coefficient of uniformity (C_u), have been used to define the PSD. Fig. 13 presents
364 the relationships among B_r , D_{50} and C_u of the specimens after compression. In Fig.
365 13a, after particle breakage, D_{50} follows a unique relationship with B_r for each soil.
366 Even for the clayey loess, the variation of D_{50} is very small because the breakage in
367 the clayey loess was mainly for the particles with sizes less than D_{50} . The overall effect
368 for D_{50} of the three soils is to converge with each other. Fig. 13b shows the

369 relationships between B_r and C_u of the specimens after testing. The particle
 370 breakage generally leads to the C_u increasing in an approximately linearly
 371 relationship, indicating that the soils become better graded. Within some scatter, this
 372 relationship is unique for the three soils.



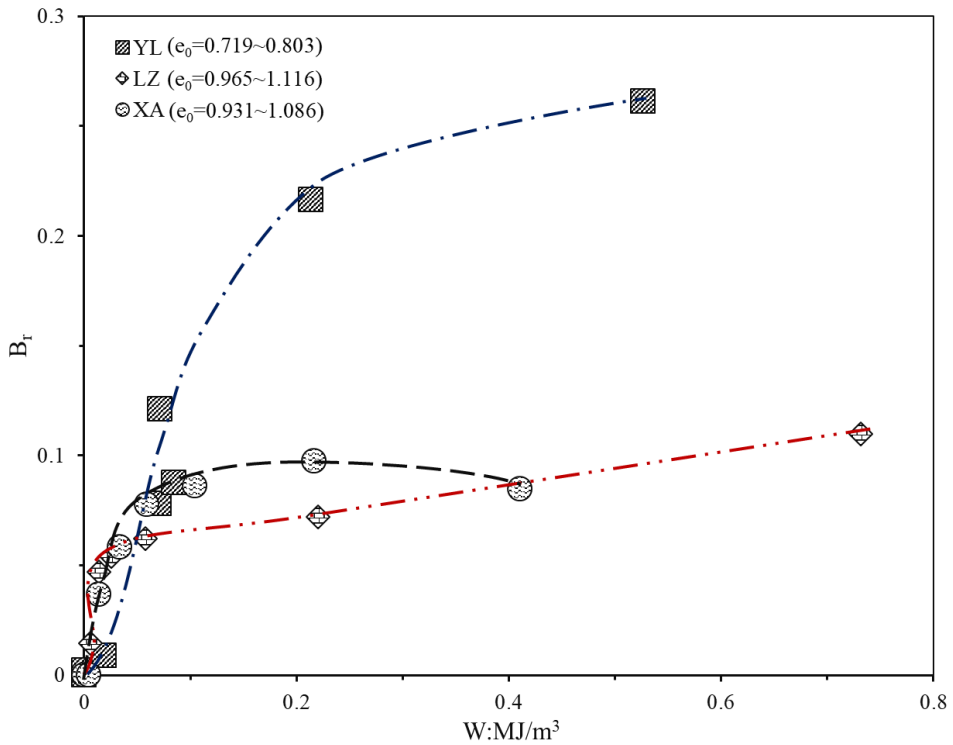
374 Fig. 10 Definition of the relative breakage B_r , modified from Hardin (1985)

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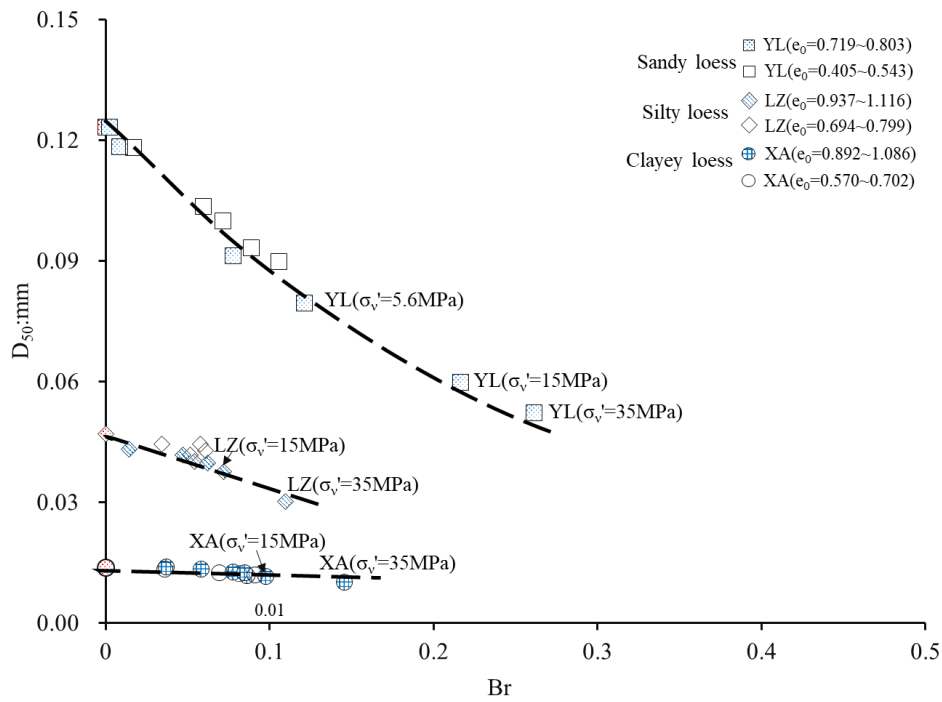
377 Fig. 11 Relative breakage B_r of the specimens compressed to different stress levels



378

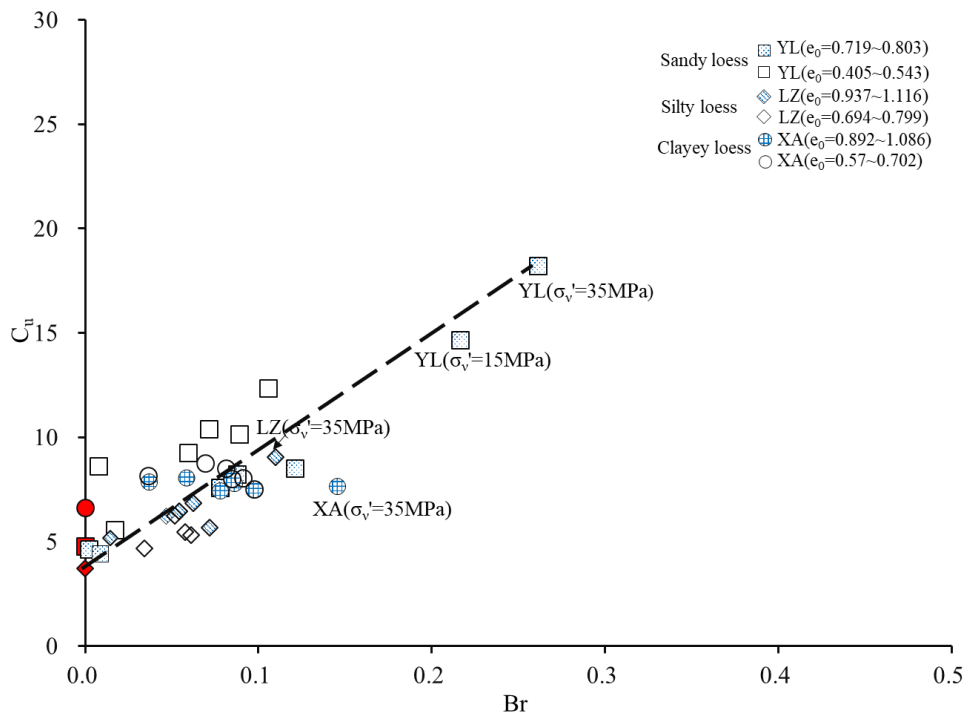
379 Fig. 12 The relationship between B_r and W during the compression process

380



381

382 (a) B_r against D_{50} after compression



383

384 (b) B_r against C_u after compression

385 Fig. 13 The effect of particle breakage on the soil grading after compression

386

387 3.2. Influences of specimen density on particle breakage

388 Fig. 14 shows the compression curves of specimens with different initial void ratio. In

389 order to identify the influence of initial density on particle breakage, the PSDs of
390 specimens were compared before and after testing. The results are presented in Fig. 15.
391 For the specimens of dense sandy loess, e.g. YL ($\sigma'_v = 5.6$ MPa, $e_0 = 0.499$), the PSDs
392 after tests are very close to the initial one. While for the loose specimens, e.g. YL ($\sigma'_v =$
393 5.6 MPa, $e_0 = 0.719$), coarser particles broke and a significant difference of the PSDs
394 of the dense specimens was found. At larger stresses, the particle breakage in the loose
395 specimen, e.g. YL ($\sigma'_v = 35$ MPa, $e_0 = 0.718$), is much more significant than in the dense
396 one, e.g. YL ($\sigma'_v = 35$ MPa, $e_0 = 0.504$). In fact, the particle breakage in the loose
397 specimen at a low vertical stress, YL ($\sigma'_v = 5.6$ MPa, $e_0 = 0.719$), is much more than that
398 of the dense specimen at a higher stress, YL ($\sigma'_v = 35$ MPa, $e_0 = 0.504$). These
399 differences reflect the key importance of coordination number on breakage (McDowell
400 and Bolton, 1998). Similar conclusions were found in the silty and clayey loess, as can
401 be seen in Fig. 16.

402

403 Fig. 17 shows the relationship between B_r and W of samples. It shows the greater
404 the input energy is, the higher the relative breakage will be. For the sample LZ ($\sigma_v = 4.0$
405 MPa) shown in Fig. 17 appears to be contrary to this conclusion, which may be due to
406 the small difference in the initial density as well the uncertain errors. Seen from the Fig.
407 17, the loose samples experienced a bigger input work than the dense samples. The total
408 input energy should eventually be converted to particle rearrangement, particle friction
409 and particle breakage energy consumption (Indraratna and Salim, 2002). Only the
410 particle breakage energy consumption is related to the amount of particle breakage. The
411 higher energy consumption in the loose sample is also composed of the more significant
412 particle rearrangement with comparison of the dense sample. The different particle
413 fabrics in the loose and dense samples, such as there are more point-to-point contacts

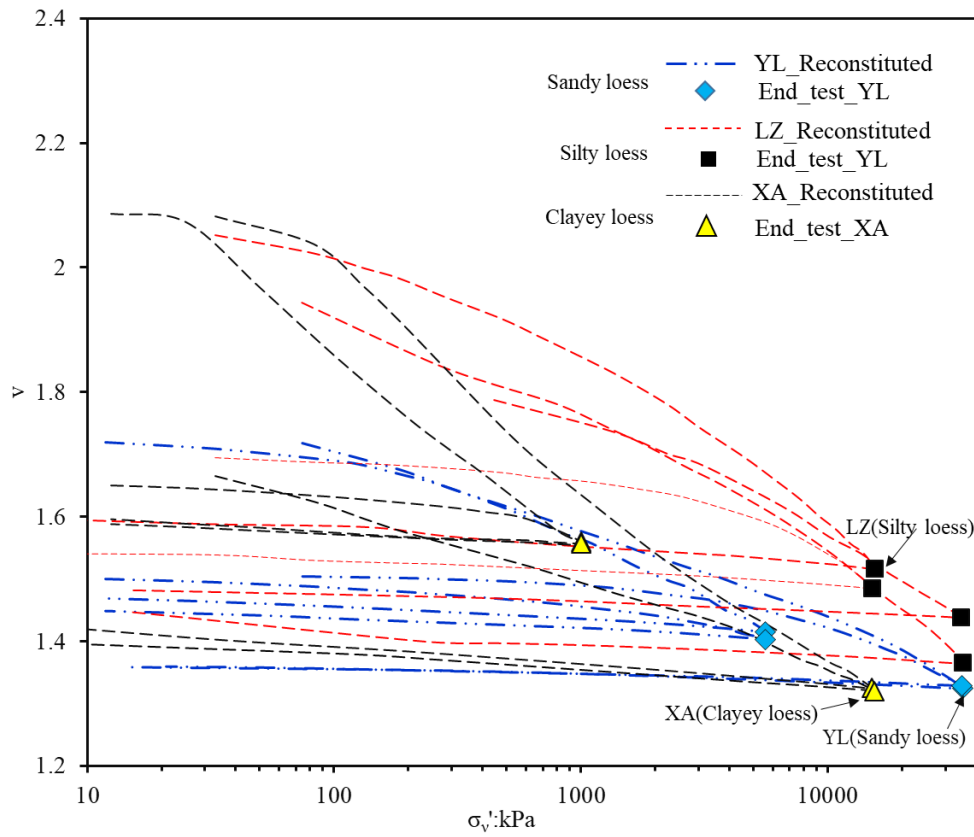
414 in the loose sample, can also cause the difference in particle breakage.

415

416 Fig. 18 shows the detailed results of sizes of broken particles. For the sandy loess (YL),
417 the particle breakage of the loose specimens mainly concentrates in the coarser particles
418 (0.15 ~ 0.55 mm). While under the same stress, the sizes of the broken particles in the
419 dense specimens are slightly different at the range of 0.15~0.25 mm. After breakage,
420 the peak of loose specimens moves more significantly to the left and the distribution
421 becomes more peaked. While for the dense ones, the original flatter shape of density
422 distribution is largely maintained with a smaller leftward translation of the peak. For
423 the silty loess (LZ), the particle breakage of the loose specimens mainly concentrated
424 in the particle sizes of 0.04 ~ 0.18 mm, e.g. LZ ($\sigma'_v = 1$ MPa, $e_0 = 1.022$). But for the
425 dense specimen at the same maximum vertical stress, e.g. LZ ($\sigma'_v = 1$ MPa, $e_0 = 0.714$),
426 the particle breakage concentrates in the sizes of 0.04 ~ 0.07 mm, which is consistent
427 with the sandy loess. However, for the silty loess, the shape of the density distribution
428 changes much less with density than for the sandy loess. For the clayey loess, while
429 density does have a small effect on the quantity of breakage, it does not have a
430 consistent influence on the particle sizes being broken.

431

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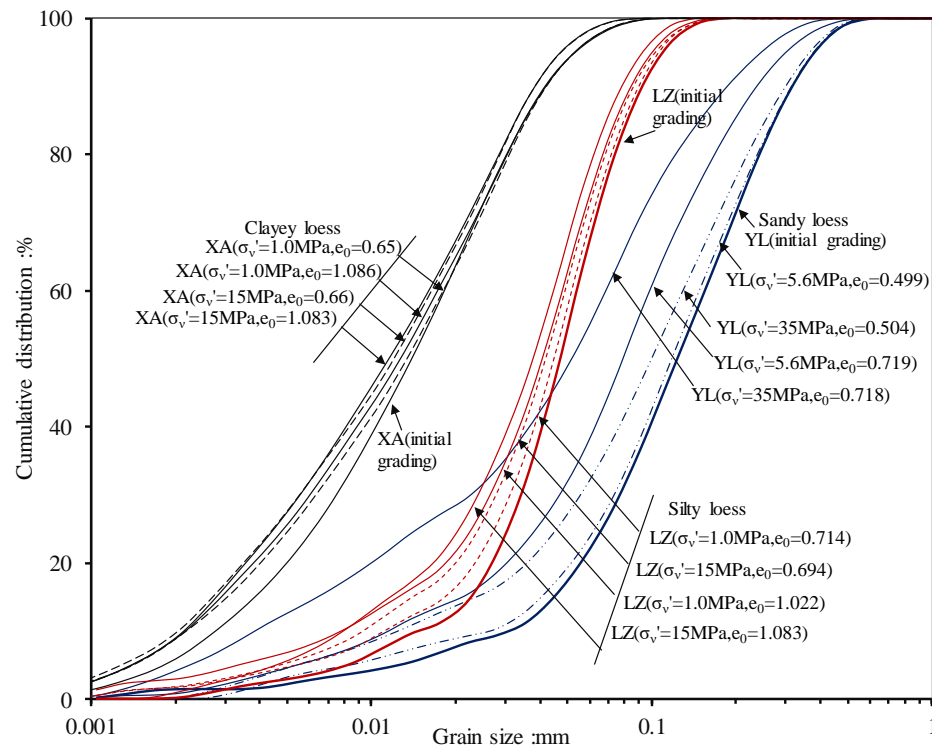


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Fig. 14 The compression curves of specimens of different initial void ratio

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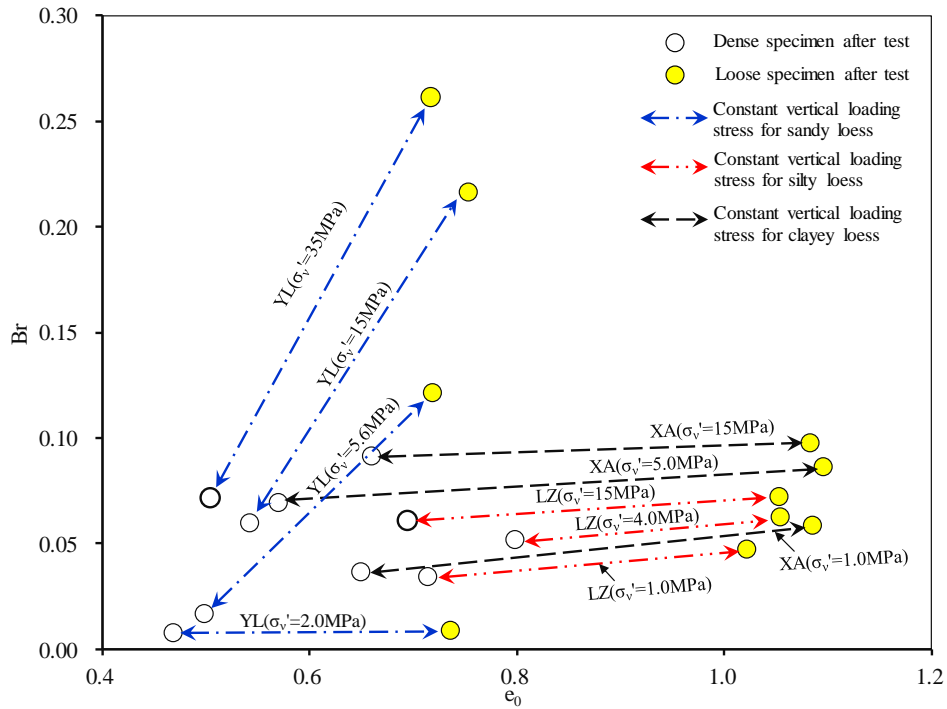


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Fig. 15 PSDs for specimens of different initial densities before and after testing

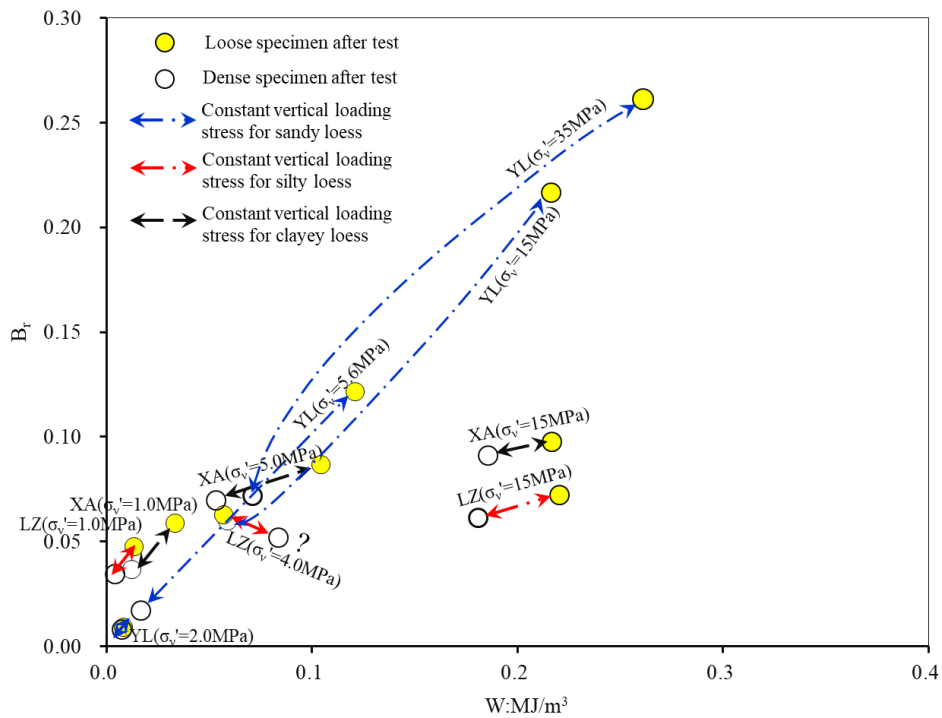
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440 Fig. 16 Relative breakage B_r for specimens of different initial void ratios

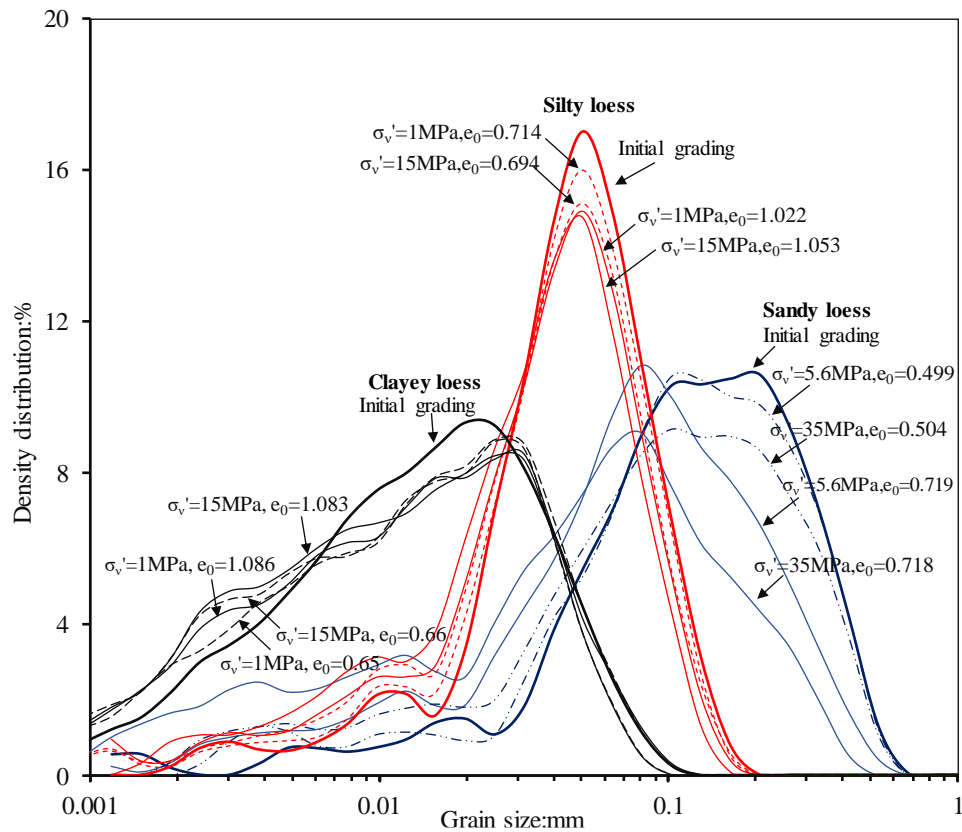
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442

443 Fig. 17 The relationship between B_r and W of samples with different initial void

444 ratios



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Fig. 18 Density distributions of particle sizes for specimens of different initial densities before and after testing

449 3.3. The particle breakage of pre-crushed specimens

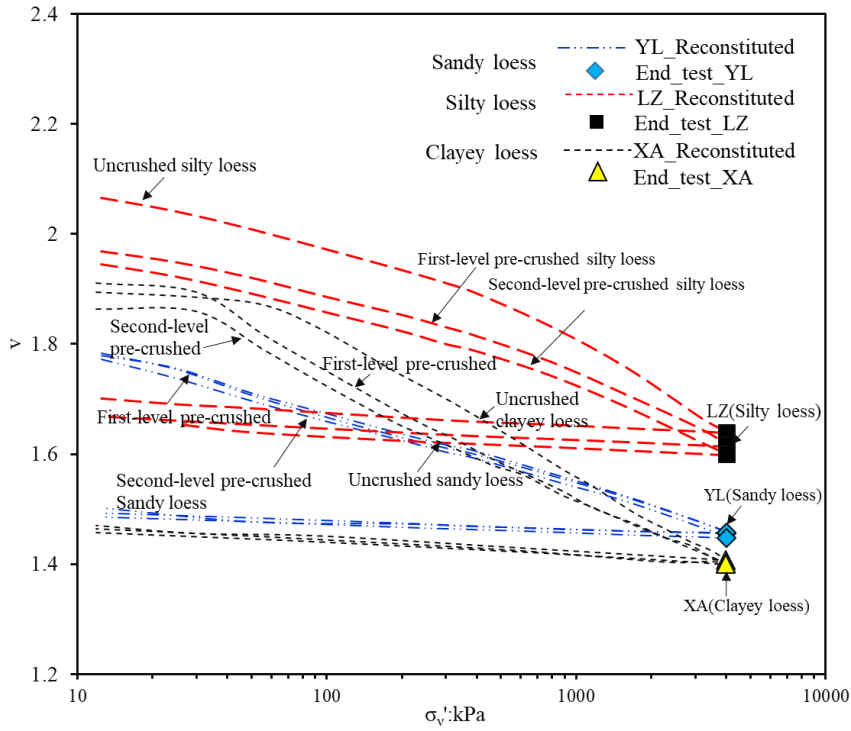
450 Oedometer tests were carried out to study the particle breakage of pre-crushed
451 specimens as shown in Fig. 19. Note that the pre-crushed specimens were made using
452 the already tested samples by wet compaction method. For each soil, the specimens
453 were prepared with the same initial void ratio. For the clayey loess, the compression
454 paths of the various specimens had different yield stresses, then eventually converge.
455 The compression paths for the silty loess do not converge and simply preserve small
456 initial differences of specific volume. Even if there was only a very small measurable
457 particle breakage in the second-level pre-crushed specimen (Fig. 20), the compression
458 curve was still similar to that of the first-level pre-crushed specimen. For the sandy
459 loess, the three specimens follow almost identical compression curves. It seems that the

460 influence of particle breakage on the compressibility of the silty and sandy loess is very
461 small.

462

463 Fig. 20 shows the PSDs of the soils before and after testing, respectively. For the natural
464 uncrushed loess, they broke significantly. But for the first-level pre-crushed loess, only
465 a very small number of particles broke. Compared with the first-level pre-crushed loess,
466 the particle breakage of the second-level pre-crushed sample can be negligible. It can
467 be seen from the compression curves of the clayey loess, silty loess, and sandy loess,
468 the compression curves of the second-level pre-crushed specimens are below the first-
469 level pre-crushed specimens (Fig. 19). The input work is not higher than that in the
470 early loading processes. Herein, no particle breakage occurred in the second-level pre-
471 crushed specimen. The reason why there is little particle breakage in the first-level pre-
472 crushed specimen may be that the reconstituting process changed the soil fabric and
473 created new particle contacts. Clearly, little breakage happens in the second loading.
474 There is no breakage in the third loading. Altuhafi and Coop (2011a) had shown that in
475 one-dimensional compression, the breakage of sands would eventually cease as a fractal
476 grading was approached. But in this study, the changes of grading required to stop
477 breakage are much smaller.

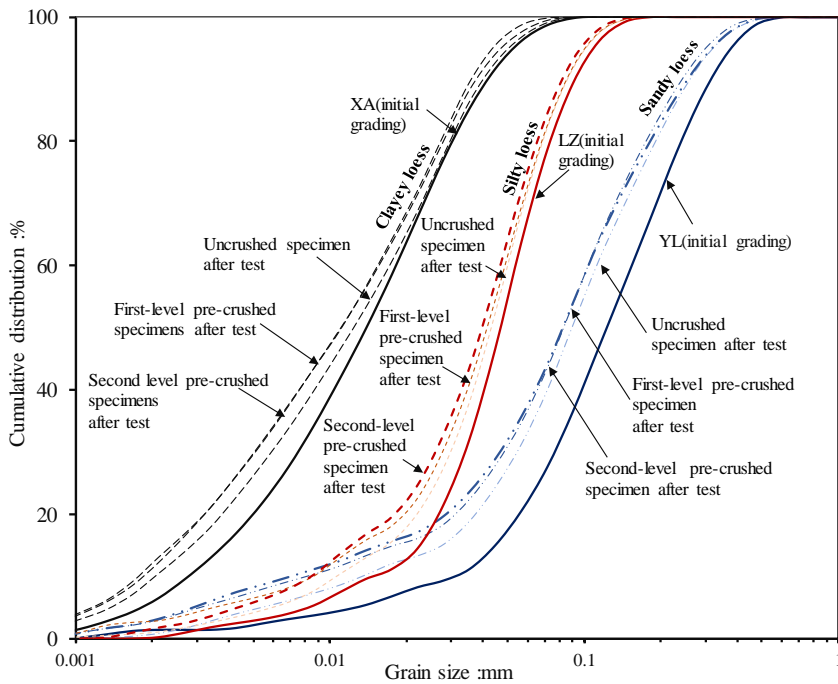
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Fig. 19 Compression curves of the uncrushed and pre-crushed specimens after test



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483

Fig. 20 PSD of uncrushed and pre-crushed specimens after test

484

4. Conclusions

485

An investigation of the one-dimensional compression behavior of sandy, silty, and

486

clayey loess reveals that particle breakage does occur in all the samples, although the

487 particle breakage in sandy loess is much more than that in the silty and clayey loess.
488 The initial stress for breakage is less than 0.5 MPa for the silty loess and clayey loess
489 and around 2 MPa for the sandy loess. The breakage in the silty and clayey loess either
490 ceases or reduces significantly with B_v , reaching an approximately constant value
491 when stress is larger than 2 MPa. The sandy loess did not reach a final degree of
492 breakage even at the maximum vertical stress of 35 MPa. The particles in loose
493 specimens were found to be subject to break easily than dense specimens. This mainly
494 because that the loose specimens experienced a higher input work during one-
495 dimensional loading. Pre-crushing dramatically reduced particle breakage. Only little
496 particles broke in the first-level pre-crushed specimen but no particle breakage occurred
497 in the second-level pre-crushed specimen.

498

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