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Effects of loading frequency on the functional adaptation of trabeculae predicted by bone remodeling simulation

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Abstract

The process of bone remodeling is regulated by metabolic activities of many bone cells. While osteoclasts and osteoblasts are responsible for bone resorption and formation, respectively, activities of these cells are believed to be controlled by a mechanosensory system of osteocytes embedded in the extracellular bone matrix. Several experimental and theoretical studies have suggested that the strain-derived interstitial fluid flow in lacuno-canalicular porosity serves as the prime mover for bone remodeling. Previously, we constructed a mathematical model for trabecular bone remodeling that interconnects the microscopic cellular activities with the macroscopic morphological changes in trabeculae through the mechanical hierarchy. This model assumes that fluid-induced shear stress acting on osteocyte processes is a driving force for bone remodeling. The validity of this model has been demonstrated with a remodeling simulation using a two-dimensional trabecular model. In this study, to investigate the effects of loading frequency, which is thought to be a significant mechanical factor in bone remodeling, we simulated morphological changes of a three-dimensional single trabecula under cyclic uniaxial loading with various frequencies. The results of the simulation show the trabecula reoriented to the loading direction with the progress of bone remodeling. Furthermore, as the imposed loading frequency increased, the diameter of the trabecula in the equilibrium state was enlarged by remodeling. These results indicate that our simulation model can successfully evaluate the relationship between loading frequency and trabecular bone remodeling.

1. Introduction

Bone is a load-bearing tissue that can adapt its internal structure and outer shape by remodeling to a changing mechanical environment. The morphological changes of the trabecular microstructure are realized by the coupling of osteoclastic bone resorption and osteoblastic bone formation (Parfitt, 1994). It is widely believed that the metabolic activities of these executive cells are coupled with osteocytes, which are interconnected within the extracellular bone matrix, forming a three-dimensional intercellular network through cellular processes (Cowin et al., 1991; Donahue et al., 1995; Kamioka et al., 2001, 2009; Knothe Tate et al., 2004; Sugawara et al., 2005). The osteocyte network is considered to have an important role in mechanosensing and intercellular signal transmission (Mullender and Huiskes, 1997; Burger and Klein-Nulend, 1999; Cowin, 2007; Huo et al, 2008; Adachi et al., 2009a, b, c).

Although the mechanism of cellular mechanosensing is not well understood, attempts have been made to determine the mechanical stimulus that derives the responses of mechanosensor cells. A variety of mechanical stimuli, such as strain energy density (Mullender et al., 1994; Huiskes et al., 2000; Mullender and Huiskes, 1995; Ruimerman at al., 2005), micro-damage (Prendergast and Taylor, 1994; McNamara and Prendergast, 2007; Mulvihill and Prendergast, 2008), stress nonuniformity (Adachi et al., 1997, 2001; Tsubota and Adachi, 2004, 2005, 2006; Tsubota et al., 2002, 2009), and fluid flow (Weinbaum et al., 1994; Burger and Klein-Nulend, 1999; Knothe Tate et al., 1998; Klein-Nulend et al., 2005; Bonewald and Johnson, 2008; Fritton and Weinbaum, 2009), are assumed to be candidates for a remodeling stimulus. Experimental studies indicate that a significant mechanical factor affecting bone remodeling is the strain rate rather than the strain itself (Fritton et al., 2000; Goldstein et al., 1991; Lanyon, 1984). The theoretical study based on poroelasticity (Weinbaum et al., 1994) suggests that the interstitial fluid flow in lacuno-canalicular porosity induced by strain plays an important role in osteocyte mechanosensing. In the microstructure model of Weinbaum et al. (1994), fluid-induced shear stress over the osteocytic process is considered to be a driving force for bone remodeling. This model was later refined, indicating the importance of cellular attachment to canalicular projections (You et al., 2001; Weinbaum et al., 2003; Han et al., 2004) and the fiber connection between the cell membrane and the canalicular wall (Wang et al., 2007) as well as the fluid flow. Thus, the progress in this field of research from the macroscopic to microscopic level has provided important information about the mechanism of cellular mechanosensing.

A number of computational models for bone remodeling using finite element analysis have been proposed to investigate the mechanism of bone self-regulation (Cowin, 1993; Huiskes et al., 1987, 2000; Jang and Kim, 2008; Coelho et al., 2009; Dunlop et al., 2009; Martinez-Reina et al., 2009; Gerhard et al., 2009). We have developed a mathematical model for trabecular surface remodeling by assuming the nonuniformity of local stress on the trabecular surface as a driving force for remodeling (Adachi et al., 1997, 2001; Tsubota and Adachi, 2004, 2005, 2006; Tsubota et al., 2002). Applying this phenomenological model to the trabecular remodeling simulation for an entire human proximal femur, we were able to successfully describe a three-dimensional trabecular pattern similar to that in the actual femur (Tsubota et al., 2009). However, this model does not explicitly consider the possible mechanisms at the cellular level, even though bone remodeling is accomplished by the coupling of the cellular activities of osteoclasts, osteoblasts, and osteocytes.

In order to explain the macroscopic tissue level changes in trabecular morphology in terms of the microscopic cellular level activities, we recently proposed a mathematical model for bone remodeling, taking cellular mechanosensing and intercellular communication into consideration (Adachi et al., 2010). This model is based on the hypothesis that osteocytes respond to fluid-induced shear stress (Weinbaum et al., 1994; Klein-Nulend et al., 1995a, b) and deliver their mechanical signals to the surface cells by intercellular communication (Adachi et al., 2009c). As a result, bone formation and resorption are regulated. The validity of our model was demonstrated by a remodeling simulation for a two-dimensional trabecular model (Adachi et al., 2010). The purpose of this study is to investigate the effects of loading frequency, which is thought to be a significant mechanical factor for bone remodeling. By applying the mathematical model for bone remodeling (Adachi et al., 2010) to the three-dimensional voxel finite element model of a trabecula, we performed bone remodeling simulation for a single trabecula subjected to cyclic uniaxial loading with various frequencies.

2. Methods

2.1. Mathematical model of trabecular bone remodeling

Theoretical framework

The proposed theoretical framework for trabecular bone remodeling is illustrated in Fig. 1. Mechanical loading applied to bone tissue induces bone matrix deformation and interstitial fluid flow. The mechanical behavior of the interstitial fluid can be quantified by the fluid pressure p and its gradient Δp . The osteocytes buried in the bone matrix or the cells on the trabecular surface, such as osteoblasts and bone lining cells, respond to the fluid flow and transduce the mechanical stimulus into the biochemical signal S_{oc} . Then, the produced signal is transmitted to the trabecular surface through an intercellular network system and is integrated as the total stimulus S_{sf} . Finally, the rate of trabecular surface remodeling \dot{M} , which expresses formation and resorption of the trabecular surface, is regulated by the stimulus S_{sf} .

While the process of generating interstitial fluid flow by applied loading is purely mechanical, the other three processes, i.e., cellular mechanosensing, intercellular communication, and trabecular surface remodeling, are achieved by the intricate mechanical-biochemical coupling phenomena, and their detailed mechanisms remain unproven. In the following subsections, the mathematical models of each process are constructed based on rational assumptions.

Cellular mechanosensing

It is believed by many researchers that osteocytes in the bone matrix have a role as mechanosensory cells, and shear stress caused by interstitial fluid flow over the osteocytes processes can be considered to be a mechanical stimulus. The evaluation of the shear stress was based on the microstructure model of Weinbaum et al. (1994) shown in Fig. 2. This model accounts for the interstitial fluid flow through a fiber matrix, such as proteoglycan, in an annular canaliculus. Assuming the fluid flow is governed by the Brinkman equation, the shear stress $\tau_p(n)$, acting on the osteocyte processes that align in direction *n*, can be derived using the fluid pressure gradient at bone tissue level ∇p as:

$$\tau_{\rm p}(\boldsymbol{n}) = \frac{qr_{\rm p}}{\gamma} \left[A_{\rm I} I_{\rm I} \left(\frac{\gamma}{q} \right) - B_{\rm I} K_{\rm I} \left(\frac{\gamma}{q} \right) \right] \nabla p(\boldsymbol{x}) \cdot \boldsymbol{n} , \qquad (1)$$

where constants A_1 and B_1 are given by

$$A_{1} = \frac{K_{0}(\gamma) - K_{0}(\gamma/q)}{I_{0}(\gamma/q)K_{0}(\gamma) - I_{0}(\gamma)K_{0}(\gamma/q)},$$

$$B_{1} = \frac{I_{0}(\gamma/q) - I_{0}(\gamma)}{I_{0}(\gamma/q)K_{0}(\gamma) - I_{0}(\gamma)K_{0}(\gamma/q)}.$$
(2)

In these equations, q is the ratio of the radius of the canaliculus r_c to that of the process r_p $(q = r_c/r_p)$, γ is the dimensionless parameter defined by $\gamma = r_c/\sqrt{k_p}$, and I_0 , I_1 , K_0 , and K_1 are modified Bessel functions (Weinbaum et al., 1994). The constant k_p is the permeability of the fiber matrix in the fluid annulus and can be approximated by the equation $0.0572a_0^2 (\Delta/a_0)^{2.377}$ using the fiber radius a_0 and the spacing of the fiber matrix Δ (Tsay and Weinbaum, 1991). The fluid pressure gradient ∇p is calculated using poroelastic finite element analysis (Detournay and Cheng, 1993; Manfredini et al., 1999).

In this study, it was assumed that osteocytes are susceptible to the average value of fluid-induced shear stress in a day, and the quantity of biochemical signals that osteocytes produce is equivalent to the value of the integral of the average shear stress on the cell processes. Introducing the volume fraction of canaliculi oriented to n, $\rho_c(n)$, at a particular position x (Kameo et al., 2010), the signal $S_{oc}(x)$ produced by the osteocytes per unit bone volume can be defined as:

$$S_{\rm oc}(\mathbf{x}) = \int_0^{2\pi} d\varphi \int_0^{\pi/2} \frac{2r_{\rm p}}{r_{\rm c}^2} \rho_{\rm c}(\mathbf{n}) \overline{|\tau_{\rm p}(\mathbf{n})|} \sin\theta d\theta , \qquad (3)$$

where, θ is the angle between the x_3 -axis in the arbitrarily given Cartesian coordinate system (x_1, x_2, x_3) and the vector \mathbf{n} , φ is the angle between the x_1 -axis and the projection of \mathbf{n} onto the x_1x_2 -plane measured counterclockwise, and $\overline{|\tau_p(\mathbf{n})|}$ is the time-averaged shear stress in a day. Though the volume fraction of canaliculi $\rho_c(\mathbf{n})$ depends on their orientation, in this modeling, the cell processes were assumed to extend isotropically, i.e., $\rho_c(\mathbf{n}) = \rho_c = 1/2\pi$, for simplicity.

Intercellular communication

The biochemical signals produced by osteocytes are delivered to the osteoblasts and osteoclasts on the trabecular surface. The intercellular communication of biochemical signals through the network system is illustrated in Fig. 3. Assuming that the cell on a particular trabecular surface location receives the signals only from the osteocytes within a limited region Ω and the cellular communication depends on the distance between cells, the total stimulus S_{sf} at position \mathbf{x}_{sf} on the trabecular surface is defined as

$$S_{\rm sf}(\boldsymbol{x}_{\rm sf}) = \int_{\Omega} w(l) S_{\rm oc}(\boldsymbol{x}) d\Omega \quad \text{with } w(l) = 1 - l/l_{\rm L} (l \le l_{\rm L}), \tag{4}$$

where w(l) is a weight function that describes the decay in signal intensity relative to the distance *l* and *l*_L is the maximum distance for intercellular communication. The total stimulus S_{sf} is a positive scalar function, indicating cellular activity on the trabecular surface.

Trabecular surface remodeling

The self-regulation of bone mass is achieved by osteoclastic bone resorption and osteoblastic bone formation. In this study, it was assumed that activities of osteoclasts and osteoblasts are regulated by the decrease and increase in the mechanical stimulus from the physiological equilibrium condition, respectively. Regarding the total stimulus $S_{sf}(\mathbf{x}_{sf})$ as the driving force for bone remodeling, the relationship between the rate of trabecular surface remodeling \dot{M} and $S_{sf}(\mathbf{x}_{sf})$ can be qualitatively described by the function:

$$\dot{M}_{max} = \begin{cases} \dot{M}_{max} & \left(S_{sf}^{U} < S_{sf}\right) \\ \frac{\dot{M}_{max}}{2} \left[\sin \pi \left\{ \frac{S_{sf} - \left(S_{sf}^{O} + S_{sf}^{Z}/2\right)}{S_{sf}^{U} - \left(S_{sf}^{O} + S_{sf}^{Z}/2\right)} - \frac{1}{2} \right\} + 1 \right] & \left(S_{sf}^{O} + \frac{S_{sf}^{Z}}{2} < S_{sf} \le S_{sf}^{U}\right) \\ \dot{M}(S_{sf}) = \begin{cases} 0 & \left(S_{sf}^{O} - \frac{S_{sf}^{Z}}{2} < S_{sf} < S_{sf}^{O} + \frac{S_{sf}^{Z}}{2} \right) \\ -\frac{\dot{M}_{max}}{2} \left[\sin \pi \left\{ \frac{S_{sf} - \left(S_{sf}^{O} - S_{sf}^{Z}/2\right)}{S_{sf}^{L} - \left(S_{sf}^{O} - S_{sf}^{Z}/2\right)} - \frac{1}{2} \right\} + 1 \right] & \left(S_{sf}^{L} \le S_{sf} < S_{sf}^{O} - \frac{S_{sf}^{Z}}{2} \right) \\ \left[-\dot{M}_{max} & \left(S_{sf} < S_{sf}^{L}\right) \end{cases} \right)$$
(5)

where the mechanical stimulus at the remodeling equilibrium $S_{sf} = S_{sf}^{O}$, the lazy zone S_{sf}^{Z} , and the maximum formation/resorption rate \dot{M}_{max} and $-\dot{M}_{max}$ are considered in the rate equation as shown in Fig. 4. To express trabecular surface movement in the simulation, the level set method (Osher and Sethian, 1988), which is a numerical technique for tracking interfaces and shapes of materials, was employed.

2.2. Procedures of trabecular bone remodeling simulation

By applying the mathematical model for trabecular bone remodeling to a voxel finite element model of a trabecula, trabecular surface remodeling was simulated by the following procedures.

- (1) The initial shape of a trabecula is discretized using cubic voxel finite elements.
- (2) The fluid pressure p and its gradient Δp inside the trabecula are calculated based on poroelastic finite element analysis.
- (3) The biochemical signal S_{oc} is calculated by Eq. (3) using the value of fluid-induced shear stress τ_p derived by Eq. (1).
- (4) The total stimulus on the trabecular surface S_{sf} is calculated by Eq. (4).
- (5) The rate of trabecular surface remodeling \dot{M} is determined by Eq. (5).
- (6) Based on the value of \dot{M} , the shape of the trabecular surface is updated using the level set method, and then the voxel finite element model of the trabecula is recreated.
- (7) Unless a remodeling equilibrium is attained, return to procedure (2), where the remodeling equilibrium is accomplished when the changes in the bone volume are sufficiently small.

2.3. Voxel modeling of a single trabecula

As a simple trabecular model, a three-dimensional single trabecular model under cyclic uniaxial loading was constructed as shown in Fig. 5. The region for analysis was $a_1 \times a_2 \times a_3 =$ 0.8 mm × 1.6 mm × 1.2 mm, discretized by cubic voxel finite elements with an edge size of 40 µm. A single trabecula, the diameter was 240 µm, was set at the center of the region with a skew angle of 30°. The trabecula was modeled as a homogeneous and isotropic poroelastic material (Cowin, 1999; Kameo et al., 2008, 2009) with the material properties listed in Table 1 (Smit et al., 2002; Beno et al., 2006; Adachi et al., 2010). To impose external loadings, two parallel, 40-μm-thick plates were added to the upper and lower edges. While the plates have the same material properties as the trabecula, they do not change in the shape during remodeling.

A shear-free condition was applied to the lower plane, and a free leakage of interstitial fluid on the trabecular surfaces was assumed. On the upper plane, cyclic loading $F(t) = \sigma_3(a_1a_2)\sin 2\pi ft$ ($\sigma_3 = 0.07$ MPa) was applied along the direction of the x_3 -axis, keeping the x_3 -displacement u_3 uniform. To investigate the effect of frequency of the applied loading on morphological changes in the trabecula, the loading frequency f was determined as f = 1, 5, and 10 Hz.

The settings of the physiological parameters explained in the previous section were specified as follows. The radius of the osteocytic process r_p and the radius of the canaliculus r_c were determined based on the average values measured by You et al. (2004): $r_p = 52$ nm, r_c = 129.5 nm. The fiber radius a_0 and the fiber spacing Δ were taken as $a_0 = 0.6$ nm and $\Delta = 7$ nm (Weinbaum et al., 1994). The maximum remodeling rate $\dot{M}_{max} = 40 \,\mu$ m/day (Jaworski and Lok, 1972) was based on the resorption rate of osteoclasts. The maximum distance for intercellular communication l_L was set to $l_L = 200 \,\mu$ m, referring to the *in vitro* experiment involving the observation of the propagation of calcium signaling between bone cells (Huo et al., 2008; Adachi et al., 2009c). The parameters associated with the mechanical signal, S_{sf}^U , S_{sf}^O , and S_{sf}^Z , were arbitrarily set to 1.5 μ N, 0.5 μ N, 1.0 μ N, and 0.2 μ N, respectively.

3. Results

The progress of morphological changes in a single trabecula and the distribution of the average fluid-induced shear stress acting on the osteocytic processes in a day $\overline{|\tau_p|}$ are shown in Fig. 6a–c for the loading frequency f = 1, 5, and 10 Hz, respectively.

In the case f = 1 Hz, as shown in Fig. 6a, relatively-large shear stress was observed at the inner surfaces with an acute angle in the initial state. This enlarged the stimuli S_{sf} that the trabecular surface cells received from neighboring osteocytes, and bone formation was promoted around both ends, while at the middle of the trabecula, the morphology was almost unchanged. At 3 days, bone resorption dominated on the outer surfaces with an obtuse angle due to small fluid-induced shear stress. After bone remodeling for 6 days, the concentration of fluid-induced shear stress observed in the initial state was relieved. As a result of successive remodeling, the single trabecula aligned along the loading direction.

As shown in Fig. 6b and 6c, the fluid-induced shear stress close to the trabecular surfaces in the initial state became larger with increase in the loading frequency. The stimuli S_{sf} on the surfaces exceeded the physiological equilibrium value, and bone formation occurred on the entire surface in both cases when f = 5 and f = 10 Hz. While this remodeling enlarged the diameter of the trabecula, the original orientation was preserved. The process of bone remodeling after 3 days was similar to that in the case f = 1 Hz, and as a result, the longitudinal direction of the trabecula coincided with the loading direction. As the imposed loading frequency increased, the diameter of the trabecula in the equilibrium state also increased.

To evaluate morphological changes in the trabecula quantitatively, the corresponding changes in bone volume fraction and the apparent stiffness during remodeling are plotted in Fig. 7a and 7b, where the bone volume fraction refers to the ratio of the volume of the trabecula to that of the total analysis region, and apparent stiffness is defined as the ratio of the loading amplitude σ_3 to the apparent strain on the upper edge u_3/a_3 . Regardless of the value of the loading frequency, the bone volume fraction increased slightly at an early stage, and then gradually decreased and converged at the constant value as shown in Fig. 7a. On the other hand, the apparent stiffness of the trabecula increased monotonically and reached a uniform plateau value for all cases as shown in Fig. 7b. As the applied loading frequency increased, the equilibrium values of the bone volume fraction and the apparent stiffness also increased. The relationship between the loading frequency and the bone volume fraction at 30 days is indicated in Fig. 8. This figure also includes the results when f = 3 and f = 20 Hz. As shown in this figure, the bone volume fraction is not proportional to the loading frequency and tends to converge at a certain value under high loading frequency.

4. Discussion

We constructed a mathematical model for trabecular bone remodeling that considers cellular mechanosensing and intercellular signal transmission. To investigate the effect of the applied loading frequency on bone remodeling, we simulated morphological changes of a single trabecula under cyclic uniaxial loading with various frequencies. The results indicated that the diameter of the trabecula in the remodeling equilibrium state increased with the increase in the loading frequency, while all the trabeculae reoriented to the loading direction regardless of the value of frequency.

Several computational models for bone remodeling including cellular mechanosensing have been proposed. They assume that the transduction from the external mechanical load to biochemical signals produced by sensor cells is caused by strain energy density (Mullender et al., 1994; Huiskes et al., 2000; Mullender and Huiskes, 1995; Ruimerman at al., 2005), accumulation of micro-damage (Prendergast and Taylor, 1994; McNamara and Prendergast, 2007; Mulvihill and Prendergast, 2008), or nonuniformity of local stress on trabecular surface (Adachi et al., 1997, 2001; Tsubota and Adachi, 2004, 2005, 2006; Tsubota et al., 2002, 2009). These mathematical models, which are based on the phenomenological hypothesis that cellular activities are affected by the mechanical state at the tissue level, can successfully explain bone mechanical adaptation by remodeling. However, the process of cellular mechanosensing is closely related to the mechanical state at the microscopic level. The novelty of our model is that it is possible to consider the mechanical hierarchy from microscopic cellular activities to the macroscopic changes in trabecular morphology by quantifying the mechanical behavior of interstitial fluid in lacuno-canalicular porosity.

As a result of the remodeling simulation when the loading frequency f = 1 Hz, the trabecula rotated toward the loading direction, preserving the total mass as shown in Fig. 7a and 7b. In general, stiffness as a structure is proportional to the volume of material; nevertheless, the apparent stiffness of the trabecula monotonically increased due to bone remodeling. These results indicate that the trabecula actively adapted to the applied

mechanical load by changing its own morphology. In addition, Fig. 7b indicates that the increase in the loading frequency derives the increase in the apparent stiffness. Considering that a trabecula subjected to a cyclic loading has a higher risk of fracturing due to fatigue with the increase in the loading frequency, this behavior also could be understood as a functional adaptation of the trabecula to the mechanical environment. The results qualitatively coincide with the experimental findings that a significant bone ingrowth was observed under high loading rate condition (Goldstein et al., 1991). As shown in Fig. 8, in the high frequency range, the bone volume fraction in the equilibrium state does not vary greatly because the interstitial fluid inside the trabecula does not flow easily, and only the osteocytes in the neighborhood of the surfaces contribute to mechanosensing (Kameo et al., 2008, 2009). From a physiological point of view, these results are reasonable. Until date, we cannot verify the validity of our results quantitatively by a comparison with the experimental observations because of the difficulty in observing the morphological changes in a single trabecula under a controlled mechanical environment in vivo. However, if we could conduct a remodeling simulation based on the same mathematical model for a cancellous bone including multiple trabeculae, it would be possible to compare the simulation results with the results of quantitative experiments with respect to the cancellous bone adaptation (Goldstein et al., 1991; Guldberg et al., 1997a, b).

The setting of the mechanical signal parameters introduced in Eq. (5), i.e., S_{sf}^{U} , S_{sf}^{L} , S_{sf}^{O} and S_{sf}^{Z} , is an important issue in this simulation because it significantly affects the bone remodeling process. The parameter S_{sf}^{O} is the point of remodeling equilibrium, regulating the balance between bone resorption and formation. With the increase in S_{sf}^{o} , resorption becomes more dominant than formation. The parameter S_{sf}^{Z} is the width of the lazy zone (Carter, 1984; Huiskes et al., 1987), representing a remodeling rate sensitivity to the stimulus near the remodeling equilibrium. As the width of the lazy zone S_{sf}^{Z} increases, the changes in bone volume are more suppressed. The morphological changes in a trabecula are more sensitive to the parameter set of S_{sf}^{O} and S_{sf}^{Z} than that of S_{sf}^{U} and S_{sf}^{L} , which describe the remodeling rate sensitivity to the stimulus around the lazy zone. Though these parameters should have to be determined by comparisons with experimental observations, we set them arbitrarily due to the lack of the quantitative experimental results. The set of mechanical signal parameters used here is a case study aimed at explaining physiological bone remodeling; this simulation will also be able to express pathological bone remodeling, such as osteoporosis and osteopetrosis, by choosing the appropriate values of model parameters.

The limitation of our model is that we assumed that the material properties of trabeculae were isotropic. The bone matrix possesses anisotropic mechanical properties due to its microscopic structures. In addition, the observation of a trabecular cross section indicates that the lacuno-canalicular network system has a strong anisotropy that is perpendicular to the trabecular surfaces (Kameo et al., 2010). To investigate their effects on the process of bone remodeling, it will be necessary to resolve the contribution of this anisotropy to the mathematical model. In spite of the above limitations, our mathematical model for trabecular bone remodeling can predict bone functional adaptation successfully. Bone remodeling is a self-regulatory process realized by metabolic activities of many cells at the osteonal and

trabecular level, but the mechanism is still unclear. By refining our model with the progress of future experimental and theoretical studies, this computational simulation will be an extremely helpful method to clarify the mechanism of bone adaptation by remodeling.

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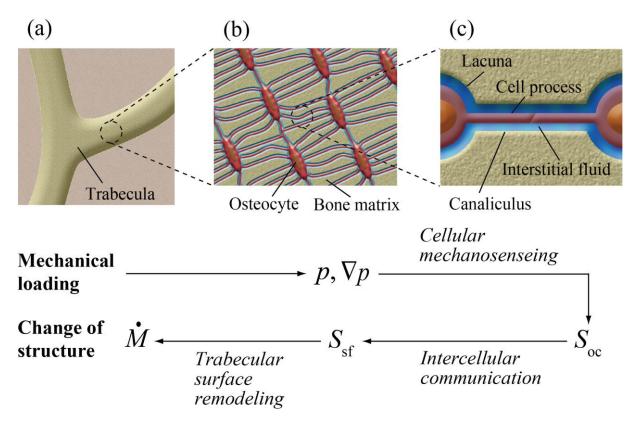


Fig. 1. Modeling framework of trabecular remodeling. This framework considers the mechanical hierarchy from the microscopic to macroscopic level including the (a) trabecular, (b) osteocyte network, and (c) lacuno-canalicular levels.

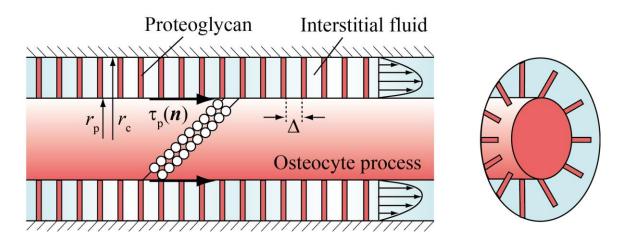


Fig. 2. Modeling of the interstitial fluid flow in an annular canaliculus. (This figure is modified from Weinbaum et al., (1994) with the kind permission of Prof. Sheldon Weinbaum and Elsevier.)

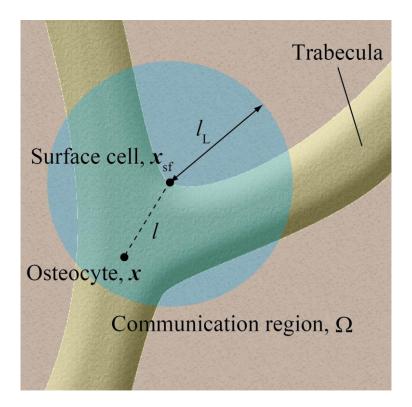


Fig. 3. Modeling of intercellular communication.

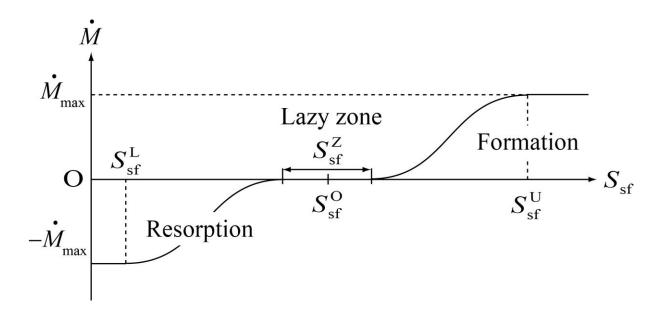


Fig. 4. Relationship between the stimulus S_{sf} that the cell on the trabecular surface can receive and the trabecular surface remodeling rate \dot{M} .

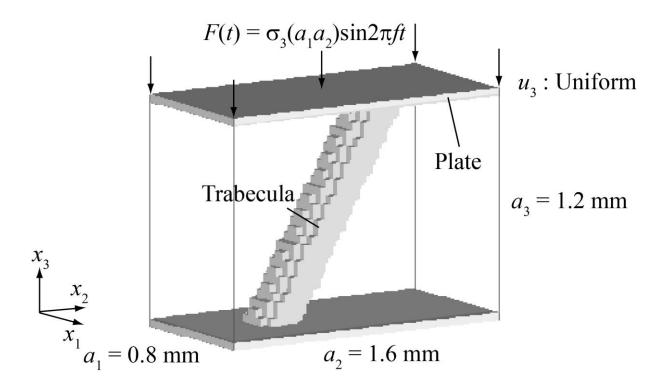


Fig. 5. A model of a single trabecula with a diameter of 240 μ m. On the upper plane, cyclic uniaxial loading is applied along the direction of the x_3 -axis, keeping the x_3 -displacement u_3 uniform.

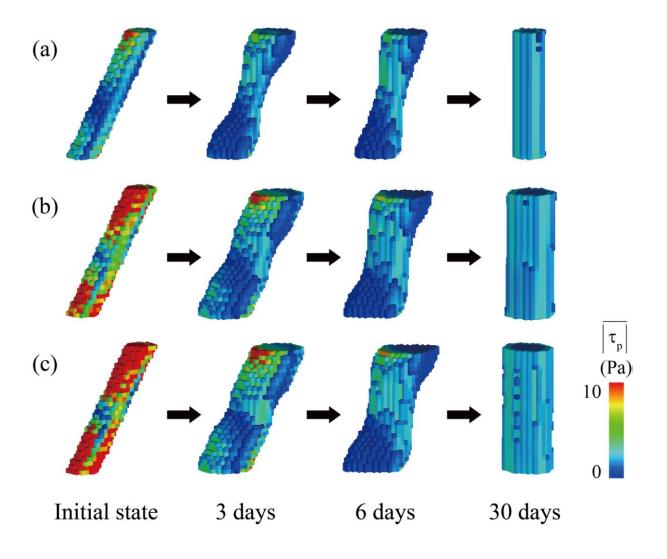


Fig. 6. Change in trabecular morphology and average fluid-induced shear stresses $|\overline{\tau_p}|$ for the applied loading frequencies (a) f = 1 Hz, (b) f = 5 Hz, and (c) f = 10 Hz.

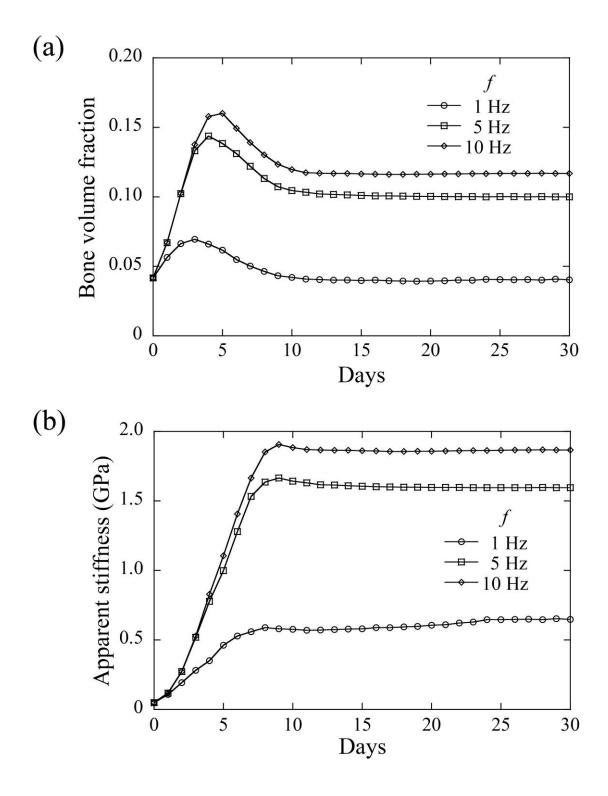


Fig. 7. Quantification of morphological changes in trabecula. (a) Change in bone volume fraction under various loading frequencies, (b) Change in apparent stiffness under various loading frequencies.

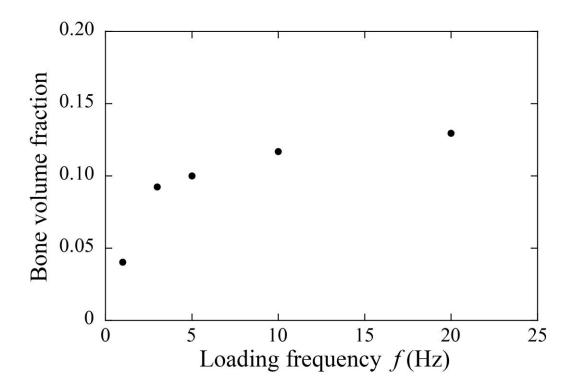


Fig. 8. Relationship between the applied loading frequency f and bone volume fraction.

Properties (units)	Value
k, Permeability (m ²)	1.1×10^{-21}
μ, Viscosity (Pa·s)	1.0×10^{-3}
G, Shear modulus (GPa)	5.94
v, Drained Poisson's ratio	0.325
K_s , Solid bulk modulus (GPa)	17.66
K_{f} , Fluid bulk modulus (GPa)	2.3
φ, Porosity	0.05

Table 1. Material properties of trabecula.

The value of permeability is estimated by Beno *et al.* (2006). The other constants are taken from Smit *et al.* (2002).