



Article

# Design, Modelling and Simulation of a Wing Sail Land Yacht

Vítor Tinoco<sup>1</sup> , Benedita Malheiro<sup>1,2\*</sup>  and Manuel F. Silva<sup>1,2</sup> 

<sup>1</sup> ISEP/IPP – School of Engineering, Polytechnic of Porto, Porto, Portugal; {1141231,mbm,mss}@isep.ipp.pt

<sup>2</sup> INESC TEC, Porto, Portugal;

\* Correspondence: [mbm@isep.ipp.pt](mailto:mbm@isep.ipp.pt)

Version March 17, 2021 submitted to Appl. Sci.

**Featured Application:** This work describes the design, modelling and simulation of a free-rotating wing sail solution for an autonomous environmental land yacht probe. The adopted method involves the application of land sailing principles for the design, the usage of Fusion 360 tool for 3D modelling and the integration of Gazebo with the Robotic Operating System (ROS) framework for the simulation of the land yacht.

**Abstract:** Autonomous land yachts can play a major role in the context of environmental monitoring, namely, in open, flat, windy regions such as iced planes or sandy shorelines. This work addresses the design, modelling and simulation of a land yacht probe equipped with a rigid free-rotating wing sail and tail flap. The wing was designed with a symmetrical airfoil and dimensions to provide the necessary thrust to displace the vehicle. Specifically, it proposes a novel design and simulation method for free rotating wing sail autonomous land yachts. The simulation relies on the Gazebo simulator together with the ROS middleware. It uses a modified Gazebo aerodynamics plugin to generate the lift and drag forces and the yawing moment, two newly created plugins, one to act as a wind sensor and the other to set the wing flap angular position, and the 3D model of the land yacht created with Fusion 360. The wing sail aligns automatically to the wind direction and can be set to any given angle of attack, stabilising after a few seconds. Finally, the obtained polar diagram characterises the expected sailing performance of the land yacht. The described method can be adopted to evaluate different wing sail configurations as well as control techniques for autonomous land yachts.

**Keywords:** Robotic sailing; design; modelling; simulation; wing sail; flap tail; land yacht

## 1. Introduction

In the last decades a broad range of research has been conducted in autonomous systems, ranging from land to marine or aerial robots, since these vehicles are useful in a very broad spectrum of tasks, due to their ability to remove humans from dangerous environments, relieve them of tedious tasks, or simply go to locations otherwise inaccessible or inhospitable [1]. Diverse applications have been envisaged for these platforms, from exploration of remote places [2] to warfare [3].

In order to have truly autonomous systems, they must present not only control autonomy, but also energy autonomy. A possibility for granting energy autonomy to land and marine vehicles is to make use of wind to propel the vehicle [4] and, eventually, to power its on-board systems [5–7]. To propel these vehicles, can be adopted "traditional" cloth sails (the most common approach), rigid wing sails and mechanical devices, such as Flettner rotors and vertical and horizontal axis turbines or, even, more uncommon options, such as different sail concepts or towing kites [8].

Sailing with conventional cloth sails has been practised all around the world for thousands of years and virtually all boats, apart from those in recent sailing history, used conventional fabric sails [4].

34 Although flexible fabric sails have a number of useful properties, especially when controlled by a  
35 human sailor, they also present a number of limitations and / or drawbacks which can be overcome by  
36 alternative sail types, in particular rigid wing sails [8]. Among the advantages of using rigid wing  
37 sails for autonomous systems are the fact that its control is easier to automate and their increased  
38 reliability [8]. Given these advantages, the use of rigid wing sails has been proposed, for example, for  
39 powering commercial ships [9].

40 The vast majority of robotic sailing research is focused on wind propelled water platforms –  
41 sailboats; however, there is a lesser common type of sailing vehicles – land yachts. As autonomous  
42 robotic platforms, land yachts can play an important role in the context of environmental monitoring,  
43 namely, in the case of open flat windy regions, such as iced planes or sandy shorelines. As a result,  
44 autonomous land yachts can be used to monitor river, lake or ocean shoreline environments, or even  
45 for planetary exploration [10]. Like a sailboat, a land yacht does not require motors for propulsion, as  
46 it uses the wind, resulting in a considerable increase in power autonomy [11–13].

47 Although the majority of the autonomous sailing research addresses sailboats, there are also  
48 works on land yachts. The latter include the contributions of:

- 49 1. Landis *et al.* [10,14] propose the NASA Zephyr land sailing rover. It is intended to be used in  
50 Venus, a harsh, windy planet. The conceptual design uses a NACA0015 airfoil with a wingspan  
51 of 5.44 m, a lateral area of 12 m<sup>2</sup> and weighs 49 kg. The chassis has a triangular shape with three  
52 wheels and weighs 35 kg.
- 53 2. Xie *et al.* [11] present the Autonomous Controlled Four Wheeled Land Yacht concept. This land  
54 vehicle is propelled by a single wing sail with a symmetrical profile, 1 m wingspan, a lateral area  
55 of 0.25 m<sup>2</sup>, a mass of 2.15 kg and a rotation range of 0° to 360°. The chassis is composed by an  
56 aluminium hull and two front and two rear wheels with a total mass of 19 kg.
- 57 3. Chen *et al.* [15] propose the Multiple Wing Sail Land Yacht. It adopts a triple wing sail design to  
58 reduce the wind velocity required to start the vehicle motion. The remaining features are equal  
59 to those of the previous example.
- 60 4. Zhu *et al.* [13] adopt a free-rotating NACA0015 wing sail with a wingspan of 2.5 m and a lateral  
61 area of 1.25 m<sup>2</sup> design to rig a land yacht. The steel chassis has one front wheel and two rear  
62 wheels. Although not fully autonomous, the angle of attack of the free-rotating wing sail is set  
63 by controlling the tail flap, which induces torque on the wing sail.
- 64 5. Mirzaei *et al.* [16] describe a land yacht developed with a NACA0012 airfoil. The airfoil has a  
65 wingspan of 1 m and a lateral area of 0.5 m<sup>2</sup>. The chassis has a triangular shape with a front  
66 wheel and two rear wheels and has a mass of 8 kg.
- 67 6. Dong *et al.* [17] describe a land yacht with a wing sail and a chassis. The NACA0015 airfoil has a  
68 wingspan of 0.8 m, a lateral area of 0.24 m<sup>2</sup> and a rotation range of 0° to 270°. The chassis has  
69 four steel wheels and plastic frame.
- 70 7. Reina *et al.* [18] detail a land yacht model which has a NACA0012 airfoil with a wingspan of 3 m  
71 and a lateral area of 2 m<sup>2</sup>. The triangular chassis has three wheels and weighs 100 kg.

72 The main characteristics of the above reviewed land yachts are compared in Table 1. All these  
73 prototypes share the type of sail – symmetrical wing sails – and perception sensors – Global Navigation  
74 Satellite Systems (GNSS) receivers, inertial and wind direction and velocity units. Apart from the  
75 proposals of [13,17,18], the remaining platforms adopt a four wheeled chassis with a higher rear wheel  
76 baseline. This design option provides, according to [11,15,16], greater stability and maneuverability.

77 Land yachts are not only governed by the principles of sailing [4], but sail design is an essential  
78 part of their development [19]. The research and development performed on rigid-wing sails has a  
79 much bigger scope than just land yachts. This type of sails is, as previously stated, commonly used in  
80 marine vessels such as sailboats. Like the autonomous land yachts, several autonomous rigid-wing  
81 sailboats have been developed by the scientific community. Some examples of these vessels are: (i) the  
82 Atlantis autonomous catamaran [20] which uses a NACA0015 airfoil as the wing sail with a wingspan  
83 of 5.37 m and a lateral area of 7.8 m<sup>2</sup>. Furthermore, the wing sail is free rotating, meaning it is not

**Table 1.** Reviewed Autonomous Land Yachts

Source	Wing Sail						Chassis		
	Airfoil	Free Rot.	Angle Range (°)	Wingspan (m)	Lat. Area (m <sup>2</sup> )	Mass (kg)	Material	Wheels	Mass (kg)
Xie <i>et al.</i> [11]	NACA0018	No	0 to 360	1	0.25	2.15	Aluminum	4	19
Chen <i>et al.</i> [15]	3 x NACA0018	No	0 to 360	3 x 1	3 x 0.25	3 x 2.15	Aluminum	4	19
Zhu <i>et al.</i> [13]	NACA0015	Yes	0 to 360	2.5	1.25	-	Steel	4	-
Mirzaei <i>et al.</i> [16]	NACA0012	No	-	1	0.5	-	-	3	8
Dong <i>et al.</i> [17]	NACA0015	No	0 to 270	0.8	0.24	-	Steel & Plastic	4	-
Reina <i>et al.</i> [18]	NACA0012	No	-	3	0.66	-	-	3	100
Geoffrey <i>et al.</i> [10]	NACA0015	No	-	5.44	12	49	-	3	35

84 controlled directly and aligns with the wind direction (as it is a symmetrical airfoil). Instead, the wing  
 85 sail is controlled by a wing flap that induces torque on the wing sail, making it shift slightly to an  
 86 angle of attack; (ii) the AROO sailboat [21] which uses a rigid-wing sail with a wingspan of 1.30 m and  
 87 a lateral area of 0.23 m<sup>2</sup>; (iii) the ASPire [22], which uses a free-rotating wing sail with a NACA632-618  
 88 profile. The wing sail wingspan is of 2.8 m and the lateral area is of 2.1 m<sup>2</sup>. The focus of this work is on  
 89 a land vehicle; however, as mentioned before, the research performed on marine vessels can be used  
 90 on a land yacht, namely the wing sail.

91 Considering the modelling and/or simulation of platforms propelled by wing sails, there is scant  
 92 research on land yachts:

- 93 1. Chen *et al.* [23] derive a mathematical model for a four-wheel land yacht powered by a wing sail.  
 94 They model the structure, steering gear, servomotors and force of wing sail and, then, simulate  
 95 the motion of land yacht according to the mathematical model. The mathematical model analyzes  
 96 both the linear and steering motions. The simulation and actual experimental results confirm the  
 97 feasibility and reliability of the proposed land-yacht modeling.
- 98 2. Dong *et al.* [17] present the design, simulation and development of a wind-driven land yacht  
 99 propelled by a wing sail. The authors conduct a theoretical analysis and use the ANSYS Fluent  
 100 simulation software to determine the lift and drag coefficients corresponding to each combination  
 101 of attack and heading angles, and the best attack angle corresponding to each different heading  
 102 angle. The simulation and experimental upwind results were concordant.

103 The modelling and/or simulation of sailboat platforms equipped with wing sails is more abundant.  
 104 The following list holds a set of representative works:

- 105 1. Rynne and von Ellenrieder [24] design, simulate and develop a wind (rigid wing sail) and  
 106 solar-powered autonomous surface vehicle (ASV). Before building the ASV, the control simulation  
 107 was performed with a velocity prediction program (VPP). Initial field trials showed that the  
 108 experimental and simulated boat speeds and wind speed/directions were consistent.
- 109 2. Enqvist *et al.* [25] design and simulate a simple, reliable and highly autonomous sailboat. They  
 110 choose a symmetrical, free-rotating wing sail with an additional tail for actuating the wing and  
 111 controlling its angle of attack. The design was further investigated with a computation flow  
 112 dynamics simulation software.
- 113 3. Augenstein *et al.* [26] design and simulate small (1 m) semi-autonomous robotic sailboat platform  
 114 variants equipped with a symmetric airfoil sail, a thin, bulbed keel, and a tail-vane rudder,  
 115 replacing the traditional water rudder. They adopt MATLAB to perform 2D and 3D dynamic  
 116 simulations of the tail-vane rudder design.
- 117 4. Setiawan *et al.* [27] design and simulate an autonomous sailboat dynamic model with four  
 118 degrees of freedom. The simulations were carried out with MATLAB/Simulink to determine the  
 119 effect of flap and rudder deflection angles on boat dynamics.

120 This survey on the simulation of platforms propelled by wing sails shows that none utilizes  
 121 the ROS middleware and the Gazebo simulator. The work presented in this article offers a novel

122 simulated environment for autonomous land yachts using the ROS middleware and the Gazebo  
123 simulator. Furthermore, two Gazebo plugins are developed to (i) act as a wind sensor and (ii) to set the  
124 flap angular position.

125 This article is a condensed version of the thesis presented in [28] and contributes to robotic sailing  
126 through the design, modelling and simulation of an autonomous rigid wing sail land yacht, which  
127 can be used to survey and monitor the shoreline (more specifically sandy areas), with the help of the  
128 Gazebo<sup>1</sup> simulator and the Robot Operating System (ROS)<sup>2</sup> middleware. Moreover, the proposed  
129 method can be followed to perform *a priori* evaluation of alternative wing configurations and control  
130 algorithms, *i.e.*, without the need to build the actual land yachts. The proposed method constitutes a  
131 novel approach to the design and simulation of free rotating wing sail autonomous land yachts. This  
132 kind of sail, which is controlled through the tail flap, minimises the energy consumed by the sail  
133 control system. Once actuated, the flap generates a linear force that induces torque on the wing sail.  
134 This shifts slightly the wing sail from the wind direction, defining the sail's angle of attack.

## 135 2. Materials and Methods

136 This work applies the principles of land sailing physics to the design, modelling and simulation of  
137 a shore monitoring land yacht. The next subsections cover these different stages, detailing the relevant  
138 steps required to reproduce the results.

139 A rigid-wing sail land yacht uses an airfoil as a sail instead of a conventional cloth sail [12]. The  
140 wing sail generates aerodynamic forces, such as lift and drag, and is more efficient, robust and easier  
141 to control than conventional cloth sails as, generally, these cloth sails require more than one actuator  
142 to be controlled and a wing sail only requires one [12]. Even though wind propelled vehicles, when  
143 compared with their fuel or electricity based counterparts, display greater power autonomy, it can be  
144 further increased with the adoption of a free rotating wing sail equipped with a wing flap. By default,  
145 a free rotating wing sail automatically aligns to the wind direction, defining an angle between the cord  
146 of the wing and the oncoming wind flow, called angle of attack. This angle of attack can be controlled  
147 by changing the direction of the wing flap. Specifically, when the angle between the wing flap and the  
148 apparent wind changes, it generates a linear force that induces torque on the wing sail, defining a new  
149 angle of attack.

### 150 2.1. Platform Design

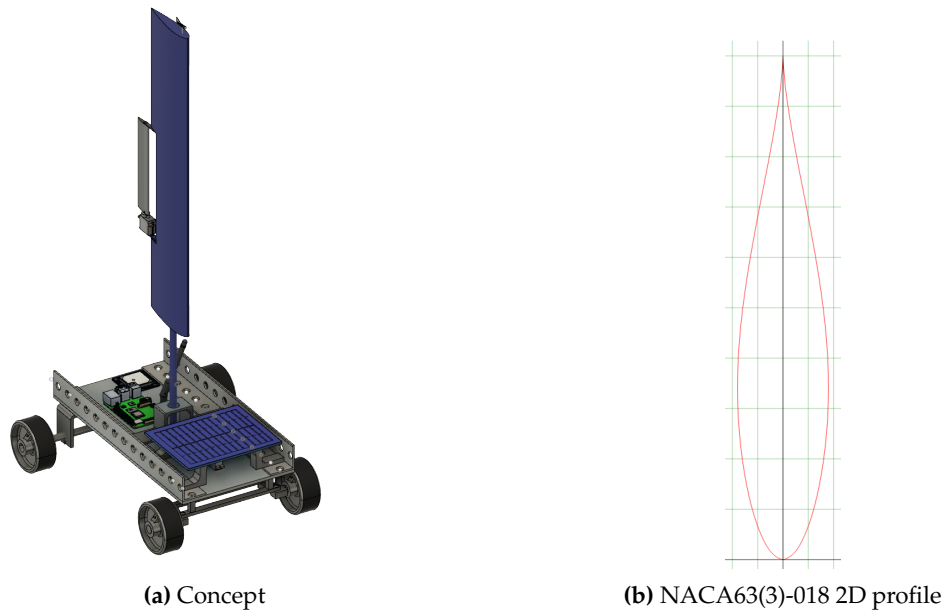
151 The proposed land yacht has a four wheeled chassis, similar to the prototypes presented in [11,15,  
152 17]. The chassis, made of stainless steel grade 316L with a density of 7990 kg/m<sup>3</sup>, has a parallelepipedic  
153 shape with a width of 360 mm, a length of 700 mm and a thickness of 5 mm, totalling 10 kg. Together,  
154 the wing, flap and mast weigh 6 kg. The wing and flap airfoils share the same symmetrical National  
155 Advisory Committee for Aeronautics (NACA) profile. The expected maximum payload of the land  
156 yacht is 4 kg.

157 The land yacht determines its current state with the help of a set of sensors: (i) a GNSS receiver for  
158 the position, an inertial sensor for the attitude, an absolute rotary encoder for the wing sail direction;  
159 (ii) a wind sensor for the apparent wind direction; and (iii) from the previous sensor information, the  
160 angle of attack of the wing sail. Given a mission, the land yacht calculates the desired heading angle  
161 (yacht) and angle of attack (wing sail) to go to the next way point and actuates two servo motors to  
162 control the wing flap and the steering mechanism accordingly. The concept of the designed land yacht  
163 is shown in Figure 1a.

---

<sup>1</sup> Gazebo simulator website: <http://gazebosim.org>

<sup>2</sup> ROS website: <https://www.ros.org>



**Figure 1.** Land Yacht Design

## 164 2.2. Wing Sail Design

165 The method adopted to define the physical characteristics of the wing sail was suggested by [29].  
 166 The angle of attack  $\alpha$  of a wing sail corresponds to the angle between the wing chord and the apparent  
 167 wind direction. Non-null  $\alpha$  values generate perpendicular and parallel forces relative to the apparent  
 168 wind, known as lift ( $L$ ) and drag ( $D$ ), and their magnitude depends on the corresponding lift ( $C_L$ ) and  
 169 drag ( $C_D$ ) coefficients [30].

170 The selected wing profile was a NACA63(3)-018 symmetrical airfoil as it provides a high lift to  
 171 drag ratio (73) for an  $\alpha = 6.75^\circ$  as well as keeps a low drag coefficient (0.02) at  $\alpha = 10^\circ$ , with a Reynolds  
 172 number of 500 000 [31,32]. The 2D profile of the NACA63(3)-018 airfoil is presented in Figure 1b.

The lift and drag forces produced in a sail depend on its shape and dimensions. In this case, the area of the wing sail surface needs to generate sufficient lifting force to move the land yacht. The lift force is presented in Equation (1), where  $\rho$  is the air density,  $V$  is the apparent wind velocity,  $A$  is the airfoil lateral area (chord  $\times$  wingspan) and  $C_L$  is the airfoil lift coefficient.

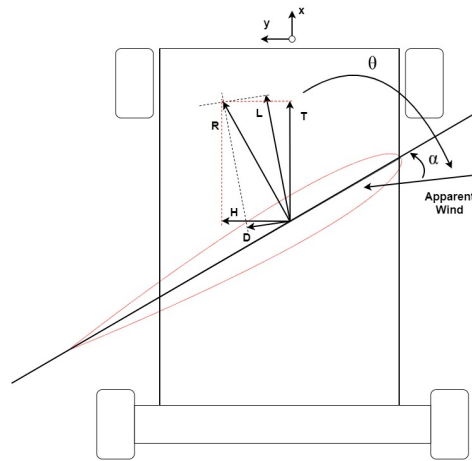
$$L = \frac{1}{2}\rho V^2 A C_L \quad (1)$$

The drag force is given by Equation (2), where  $\rho$  is the air density,  $V$  is the apparent wind velocity,  $A$  is the airfoil lateral area (chord  $\times$  wingspan) and  $C_D$  is the airfoil drag coefficient.

$$D = \frac{1}{2}\rho V^2 A C_D \quad (2)$$

Figure 2 displays the lift  $L$  and drag  $D$  components of the generated aerodynamic force  $R$ , the angle between the vehicle's heading and the apparent wind  $\theta$ , the wing sail angle of attack  $\alpha$ , and the driving or thrust  $T$  force and lateral or heel  $H$  force applied to the vehicle. The force required to put the land yacht in motion is given by Newton's second law presented in Equation (3), where  $m$  and  $a$  are the land yacht mass and acceleration, respectively. In this case, the mass of the vehicle, comprising the chassis, wing set and maximum payload, is assumed to be 20.0 kg.

$$F = ma \quad (3)$$



**Figure 2.** Land Yacht Forces

Replacing the force with the lift expression presented in Equation (1) and adding the friction force, results Equation (4), where  $\mu$  is the friction coefficient and  $g$  is the gravitation acceleration.

$$\frac{1}{2}\rho V^2 AC_L = ma + \mu mg \quad (4)$$

Given that the lift force is perpendicular to the apparent wind direction and the drag force is parallel to the apparent wind direction, the thrust force required to move the land yacht forward  $T$ , which is parallel to the vehicle's  $x$  axis, is related to the lift and drag through  $\theta$ , the angle of the apparent wind. This thrust force can, then, be expressed by Equation (5).

$$T = L\sin\theta - D\cos\theta \quad (5)$$

From the combination of Equations (4) and (5) results Equation (6), which represents the equilibrium of forces involved in the forward motion of the land yacht.

$$\frac{1}{2}\rho V^2 AC_L(L\sin\theta - D\cos\theta) = ma + \mu mg \quad (6)$$

Identically, the lateral or heel force applied to the vehicle's  $y$  axis is expressed by Equation (7), where  $\theta$  represents the apparent wind angle.

$$H = L\cos\theta + D\sin\theta \quad (7)$$

173 Assuming that: (i) the land yacht has a mass of 20.0 kg, an initial acceleration of 0.15 m/s<sup>2</sup> (to start  
 174 moving), and a rolling friction coefficient of 0.002 (bicycle tires on dry concrete<sup>3</sup>); (ii) the apparent wind  
 175 has a velocity of 5 m/s, an angle  $\theta \leq 45^\circ$  and the air density is 1.225 kg/m<sup>3</sup>; and (iii) the NACA63(3)-018  
 176 symmetrical airfoil profile has a lift coefficient of 0.75 with  $\alpha = 10^\circ$  [31], the wing area given by Equation  
 177 (6) is approximately 0.4 m<sup>2</sup>. Based on this set of assumptions, the NACA63(3)-01 wing sail has a chord  
 178 of 400 mm and a wingspan of 1000 mm, whereas the NACA63(3)-01 flap presents a chord of 130 mm  
 179 and a wingspan of 330 mm.

To determine if the stability of the vehicle, it is necessary to consider the existing rolling and anti-rolling moments. According to [12], the rolling moment  $M_r$  generated by the lateral wind on the wing sail is given by Equation (8), where  $L_e$  is the wing sail wingspan,  $\Delta h$  is the wing sail mounting

<sup>3</sup> <http://physicalcycling.com/tire-traction>

distance,  $P_r$  is the true atmospheric pressure,  $P_s$  is the mass-specific gas constant and  $T_r$  is the air temperature.

$$M_r = \frac{88.296P_r V^2 A (C_L \cos(\theta) + C_D \sin(\theta)) [L_e^2 - 100^2 + 2\Delta h(L_e - 100)]}{(273.15 + T_r) P_s L_e} \quad (8)$$

The anti-rolling moment moment  $M_a$ , generated by the vehicle as a whole, is given by Equation (9) [12], where  $B_1$  and  $B_2$  are the front and rear wheel base lines, respectively.

$$M_a = mg(B_1 + B_2)/4 \quad (9)$$

180 The critical vehicle tipping wind velocity occurs with lateral apparent wind, *i.e.*,  $\theta = 90^\circ$  and  
 181  $\alpha = 90^\circ$ . From Equation (8),  $\theta = 90^\circ$ ,  $C_L = 0$  (value of  $C_L$  for  $\alpha = 90^\circ$  [31]) and  $C_D = 2$  (value of  $C_D$  for  
 182  $\alpha = 90^\circ$  [31]), results Equation (10).

$$V \leq \sqrt{\frac{(273.15 + T_r)(B_1 + B_2)mgL_e P_s}{724.33A(L_e^2 + 2\Delta hL_e - 100^2 - 200\Delta h)P_r}} \quad (10)$$

183 Finally, assuming that  $T_r = 20^\circ\text{C}$ ,  $B_1 = 0.5\text{ m}$ ,  $B_2 = 0.38\text{ m}$ ,  $m = 20\text{ kg}$ ,  $g = 9.81\text{ m/s}^2$ ,  $L_e = 1\text{ m}$ ,  $P_s =$   
 184  $8.31432 \times 10^3\text{ N m kmol}^{-1}\text{ K}^{-1}$ ,  $\Delta h = 0.1\text{ m}$  and  $P_r = 101\,325\text{ Pa}$ , the maximum wind velocity that the  
 185 vehicle can withstand is  $12\text{ m/s}$ .

### 186 2.3. Platform Simulation

187 The simulation was performed with the Gazebo simulator and the ROS middleware. The Gazebo  
 188 simulator, which is a three-dimensional open-source dynamics simulator for robotic platforms, was  
 189 chosen as it allows the definition of new models in Simulation Description Format (SDF), provides a  
 190 plugin that simulates aerodynamic forces and is ROS compatible. SDF models comprise collections of:  
 191 (i) links, corresponding to body parts and including collision (geometry), visual (visualization) and  
 192 inertia (dynamics) elements; (ii) joints between links, specifying the parent and child relationship, the  
 193 axis of rotation and limits of the joint; (iii) sensors that collect world data for plugins; and (iv) plugins  
 194 which control the behaviour of the model [33].

#### 195 2.3.1. 3D Model

196 The vehicle and wing sail model were created using the Fusion 360 Computer-Aided Design  
 197 software from AutoDesk. The resulting 3D mesh files were imported to Gazebo through the SDF  
 198 model file, which describes the links and joints of the different parts of the land yacht and loads model  
 199 related plugins, such as the aerodynamics or the sensor plugins. Listing 1 defines a link and imports  
 200 the corresponding 3D mesh file into Gazebo. The link element contains the link name, the link pose  
 201 relative to the base link (in this case the base link is the chassis), the inertial properties (such as mass  
 202 and the inertial matrix), the link collision properties (in this case the collision zone is the same as the  
 203 model format) and the link visual format.

204 Listing 2 specifies a joint between two links, including the joint type (since it is connecting a wheel,  
 205 then the joint type is revolute), the joint name, the pose relatively to the child link, the child and parent  
 206 links (in this case it is the wheel and the chassis, respectively), the rotation axis (in this case the joint  
 207 rotates in the  $y$  axis), and the joint friction and damping. Finally, the SDF world file loads the land  
 208 yacht model file as well as the environmental characteristics, such as the ambient light and ground  
 209 plane, and the world related plugins. The land yacht model presented in Figure 3 is composed of a  
 210 chassis, four wheels, a steering mechanism composed of 4 links, a wing sail and a flap (11 links and 12  
 211 joints).

Listing 1: SDF Link Example

```

1 <link name='steering_middle'>
2   <pose>3.373 -0.12 0.6 0 0 0</pose>
3   <inertial>
4     <mass>0.195315</mass>
5     <inertia>
6       <ixx>1.614e-3</ixx>
7       <ixy>4.98132e-7</ixy>
8       <ixz>1.72258e-7</ixz>
9       <iyy>7.383226e-6</iyy>
10      <iyz>2.843631e-6</iyz>
11      <izz>1.612e-3</izz>
12    </inertia>
13  </inertial>
14  <collision name='collision'>
15    <geometry>
16      <mesh>
17        <uri>model://my_robot/Cad_Files/SteeringMiddleGazebo.stl</uri>
18        <scale>0.01 0.01 0.01</scale>
19      </mesh>
20    </geometry>
21  </collision>
22  <visual name='visual'>
23    <geometry>
24      <mesh>
25        <uri>model://my_robot/Cad_Files/SteeringMiddleGazebo.stl</uri>
26        <scale>0.01 0.01 0.01</scale>
27      </mesh>
28    </geometry>
29  </visual>
30 </link>

```

Listing 2: SDF Joint Example

```

1 <joint type="revolute" name="left_back_wheel_hinge">
2   <pose>0 0 0 0 0 0</pose>
3   <child>left_back_wheel</child>
4   <parent>chassis</parent>
5   <axis>
6     <xyz>0 1 0</xyz>
7   <dynamics>
8     <friction>0.0625</friction>
9     <damping>0.4</damping>
10  </dynamics>
11 </axis>
12 </joint>

```

### 2.3.2. ROS Integration

To launch Gazebo using ROS, the package `gazebo_ros_pkgs`<sup>4</sup> was reused. This package enables the interface between ROS and Gazebo, allowing also the creation of ROS nodes inside Gazebo plugins. A ROS package, named `land_yacht`, was created specifically for the development of the simulation. This package uses a launch file to load an empty world from `gazebo_ros_pkgs` together with the

<sup>4</sup> `gazebo_ros_pkgs` website: [http://wiki.ros.org/gazebo\\_ros\\_pkgs](http://wiki.ros.org/gazebo_ros_pkgs)



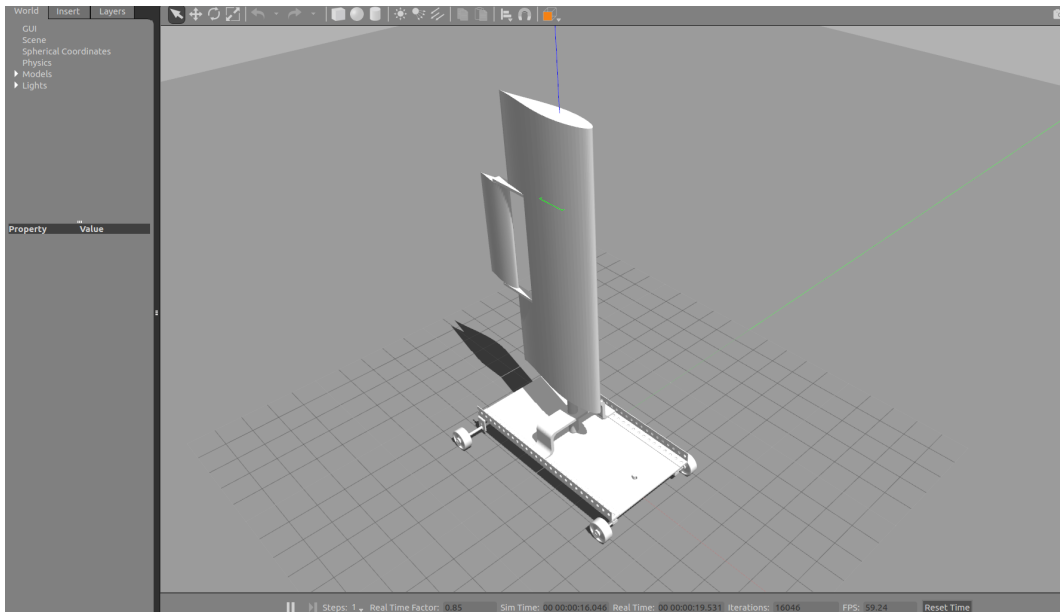


Figure 3. Land Yacht 3D Model in Gazebo

217 model of the land yacht, and a node responsible for the control of the wing flap and the steering. This  
 218 empty world serves merely as an interface between `gazebo_ros_pkgs` and `land_yacht`. For this to  
 219 be possible, the world file, which loads the vehicle model, must be stored in a subfolder of the ROS  
 package named `worlds`. A block diagram of this setup is presented in Figure 4.

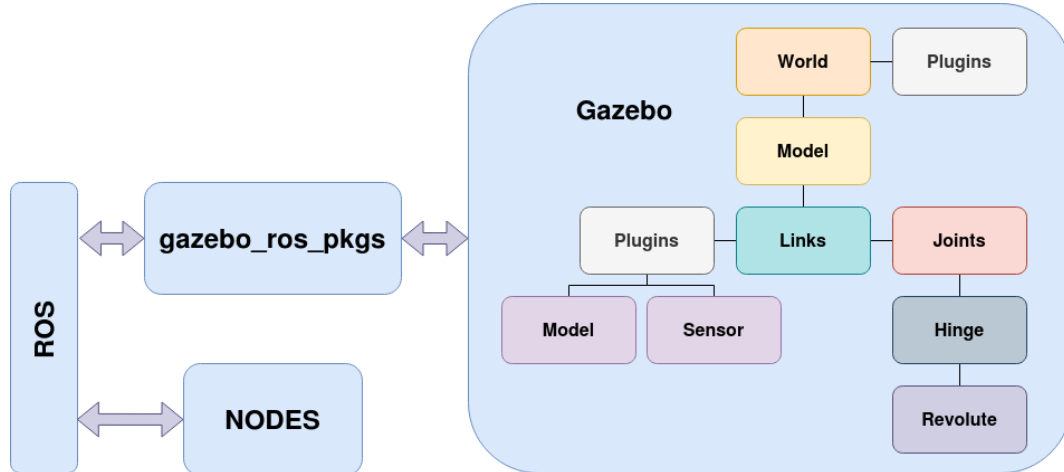


Figure 4. Gazebo-ROS Interface Block Diagram [28]

220

### 221 2.3.3. Gazebo Plugins

222 The simulation of the land yacht uses three plugins: a modified `liftdragplugin`<sup>5</sup> and two  
 223 new plugins named `land_yacht_plugin` and `land_yacht_appar_wind`. The `land_yacht_plugin`  
 224 enables the control from ROS of the wing sail flap and of the land yacht steering; and the  
 225 `land_yacht_appar_wind` plugin simulates an apparent wind sensor (velocity and direction of the  
 226 wind relative to the land yacht).

<sup>5</sup> Gazebo aerodynamics plugin: <http://gazebosim.org/tutorials?tut=aerodynamics&cat=physics>

227 The `liftdragplugin` simulates the aerodynamic forces and the pitching moment on an airfoil  
 228 (the torque generated by the wind on the airfoil), since it was developed for airplanes. Given that  
 229 an airfoil on a land yacht is positioned vertically, the plugin will calculate the yawing moment. In  
 230 short, the `liftdragplugin`, apart from generating lift and drag forces, also aligns the wing sail to  
 231 the direction of the wind. However, this plugin was created to simulate these forces on aeroplanes  
 232 or fixed wing drones in windless conditions. In other words, this plugin assumes the world's wind  
 233 velocity corresponds to the world's linear velocity of the vehicle, which, in this case, is only partially  
 234 correct. The plugin was modified to add the world's wind velocity to the world's linear velocity of the  
 235 vehicle. For example, if the vehicle is moving westward with a linear velocity of 1 m/s and there is  
 236 a westerly wind of 2 m/s, then the two linear velocities are added, generating a total apparent wind  
 237 velocity of 3 m/s. Without this change, the apparent wind velocity would remain 1 m/s. Finally, the  
 238 plugin was also adapted to subscribe a ROS topic that broadcasts the world's wind velocity in the  $x$   
 239 and  $y$  axis. Figure 5 displays a diagram that details the processing pipeline of the modified plugin.  
 240 Before calculating the lift and drag forces, the plugin subtracts the vehicle linear velocity and the  
 241 true wind velocity in the world frame and, subsequently, uses the vehicle orientation to establish the  
 242 apparent wind, which corresponds to the relative wind to the vehicle. With the apparent wind and  
 243 the wing sail angular position, the plugin calculates the wing sail angle of attack (AoA) and, using  
 244 the linearised airfoil parameters, determines the lift and drag coefficients. With these coefficients, the  
 245 plugin calculates the lift and drag forces to get the resulting force. This resulting force is applied to  
 246 the wing sail pressure point, in this case it is situated in the middle of the wing, and is also used to  
 247 calculate its yawing moment. This yawing moment is translated into torque and, finally, applied to the  
 wing sail.

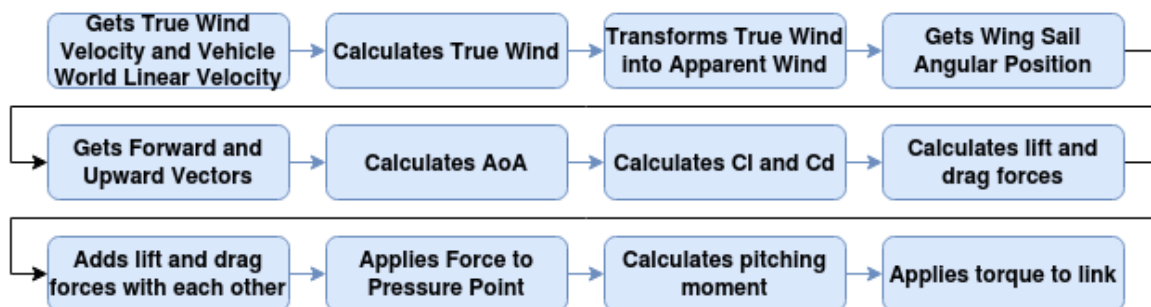


Figure 5. Liftdragplugin Diagram

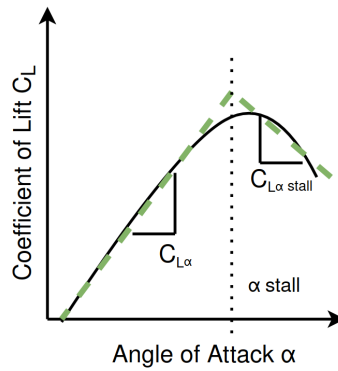
248 The `land_yacht_plugin` is composed of a ROS node that subscribes two topics – the flap angle  
 249 and steering angle – and publishes the vehicle ground truth for control and debugging. When the  
 250 plugin receives new messages from the subscribed topics it sets the corresponding joint angle to the  
 251 broadcasted value.  
 252

253 The `land_yacht_appar_wind` plugin converts the true wind (velocity and direction in the world  
 254 reference frame) into the vehicle's apparent wind (velocity and direction in the vehicle reference frame).  
 255 It subscribes the true wind topic, transforms the true into the apparent the wind, using the vehicle's  
 256 heading and velocity in the world reference frame, and, finally, publishes the result in a new topic.

257 Plugins can be loaded in the model or the world SDF file. Listing 3 illustrates the loading of the  
 258 `liftdragplugin`. The NACA63(3)-018 airfoil characteristics correspond to the stall and the slopes of  
 259 the lines obtained from linearising the characteristic lift and drag coefficient curves [31], shown in the  
 260 example presented in Figure 6. Each curve is approximated by two lines which intersect at the stall of  
 261 the curve and these line slopes are used to describe the airfoil.

#### 262 2.3.4. Wing Sail Control

263 The control of the angle of attack of the wing sail is indirect, *i.e.*, it is set through the flap. The  
 264 flap has a Proportional-Differential (PD) controller which uses as inputs the apparent wind direction



**Figure 6.** LiftDragplugin Curve Linearization Example

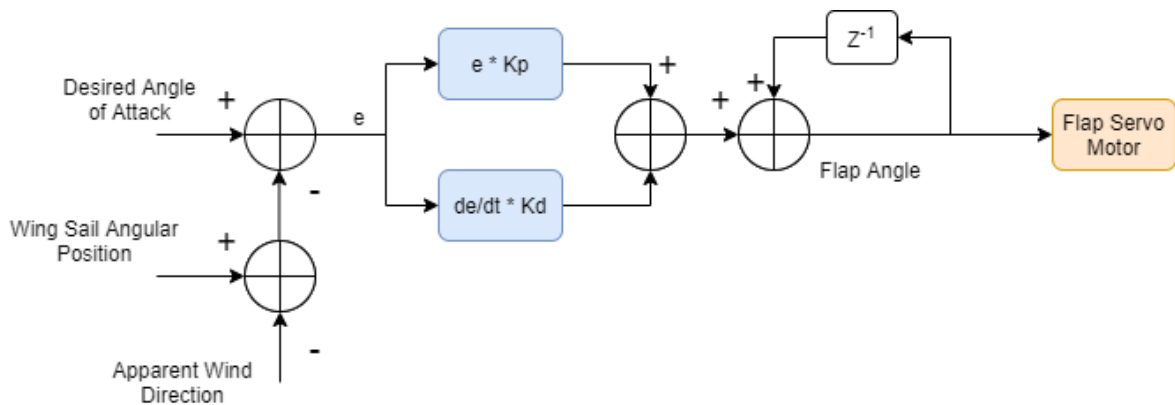
**Listing 3:** SDF Plugin Example

```

1 <plugin name="sail_plugin" filename="libTese_LiftDragPlugin.so">
2   <a0>0.0</a0>
3   <cla>5.72957795131</cla>
4   <cda>-0.57295779513</cda>
5   <cma>-0.05</cma>
6   <alpha_stall>0.17453292519</alpha_stall>
7   <cla_stall>-2.86478897565</cla_stall>
8   <cda_stall>2.29183118052</cda_stall>
9   <cma_stall>0.2</cma_stall>
10  <cp>0.05 0 1.5</cp>
11  <area>0.4</area>
12  <fluid_density>1.2041</fluid_density>
13  <forward>-1 0 0</forward>
14  <upward>0 1 0</upward>
15  <link_name>wing_sail</link_name>
16  <radial_symmetry>>true</radial_symmetry>
17 </plugin>

```

265 (published in the apparent wind topic) and the wing sail angular position (published in the sail rotation  
 266 topic), and outputs the desired flap angle. A block diagram of the wing flap control is presented in  
 267 Figure 7, where  $e$  is the error and  $de/dt$  the differential error between the desired and the current angle of  
 attack, and  $K_p$  and  $K_d$  are the proportional and differential gains, respectively.



**Figure 7.** Flap Control Block Diagram

### 269 3. Results & Discussion

#### 270 3.1. Experimental Setup

271 Figure 8 presents the set of nodes and topics involved in this experimental setup. The Gazebo  
 272 environment (gazebo node) subscribes the wind, steering and flap topics and publishes the ground  
 273 truth as well as the sail rotation and apparent wind topics. The control node (land\_yacht\_control)  
 274 subscribes the ground truth, the sail rotation and the apparent wind from Gazebo, and publishes  
 275 the flap control topics. The true\_wind\_generator node generates and publishes the real time true  
 276 wind conditions (in the world reference frame). The teleop\_key\_pub manual control node reuses the  
 teleop\_twist\_keyboard<sup>6</sup> package and was added to the setup for debugging purposes.

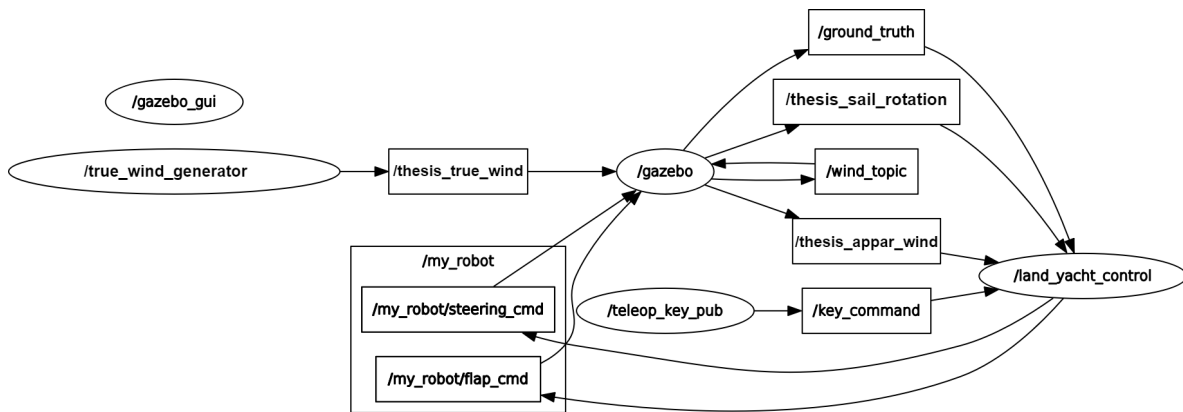


Figure 8. Experimental Setup

277

#### 278 3.2. Wing Sail Alignment to the Wind

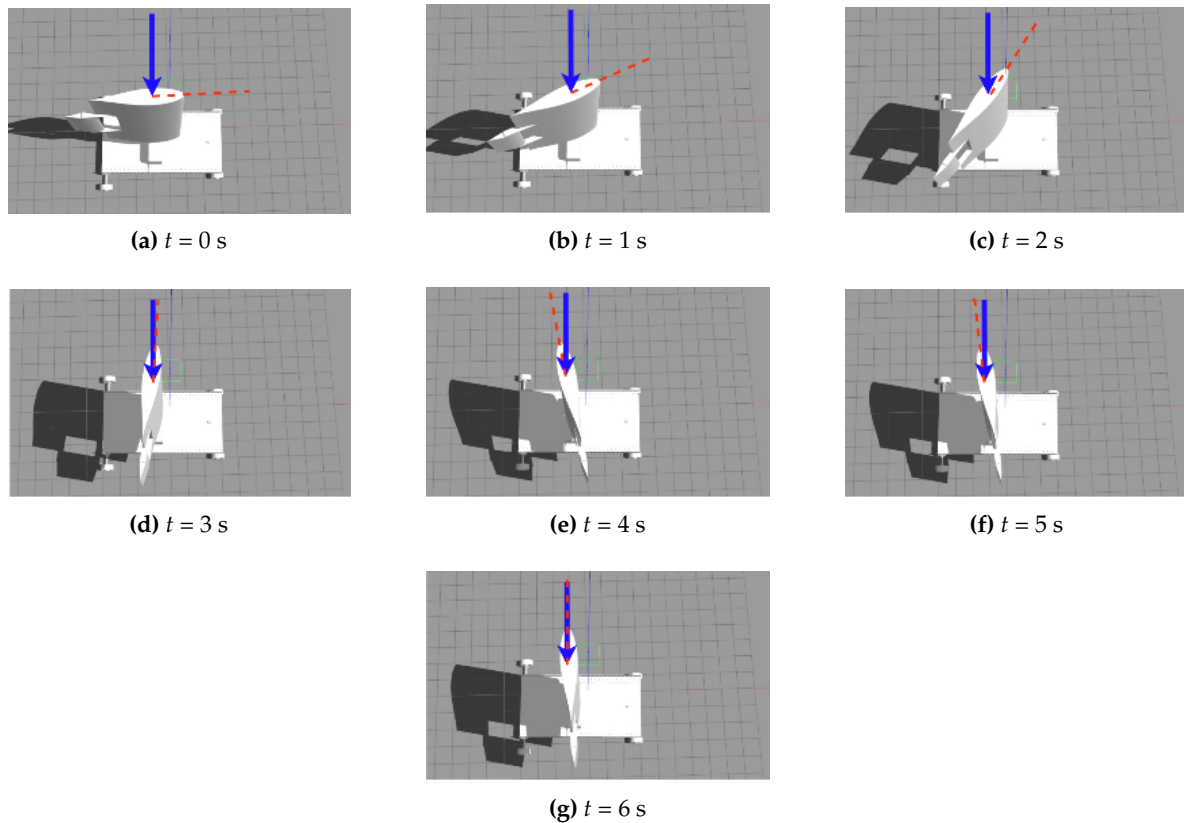
279 This test validates the wing sail alignment to the wind without any control on the flap (the flap  
 280 remains aligned with the wing sail at all times). The behaviour of the wing sail was tested with an  
 281 initial apparent wind direction of  $90^\circ$  ( $\alpha_i = 90^\circ$ ) and apparent wind velocities of 8 kn, 9 kn and 10 kn.  
 282 The final desired angle of attack is  $0^\circ$  ( $\alpha_f = 0^\circ$ ). The wing sail response is presented in Figure 9, where  
 283 the blue arrow is the wind direction and the dashed red line is the wing sail direction.

284 Figure 10 displays the time response of the wing sail angle of attack. These results show that,  
 285 when the wing and tail are aligned, the wing sail aligns automatically to the wind due to the yawing  
 286 moment of the aerodynamics plugin. Although the wing sail takes identical time to stabilise with  
 287 different wind velocities, the higher the wind velocity, the higher the overshoot.

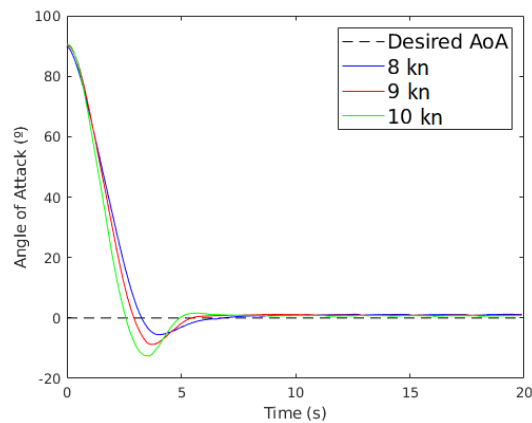
#### 288 3.3. Wing Sail Response to the Flap Angle

289 These tests verify if the wing sail turns correctly given a change in the flap angle. Initially, the  
 290 wing sail was aligned to the apparent wind direction ( $\alpha_i = 0^\circ$ ) and the flap angle was set to  $0^\circ$ . The test  
 291 consisted of turning the flap manually, using the keyboard, to the left and to the right, as is presented  
 292 in Figure 11. The wing sail responded correctly to the flap angle change. It turned to the right when  
 293 the flap angle was set to the left, and to the left when the flap angle was set to the right.

<sup>6</sup> teleop\_key\_pub website: [http://wiki.ros.org/teleop\\_twist\\_keyboard](http://wiki.ros.org/teleop_twist_keyboard)



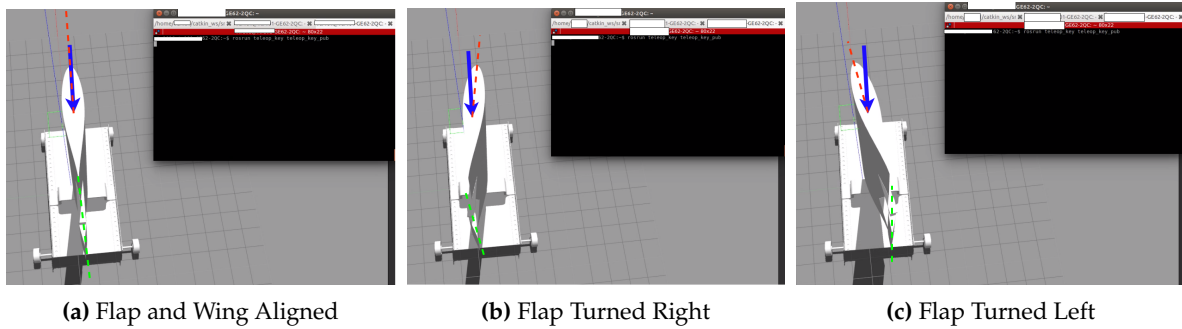
**Figure 9.** Wing Sail Alignment to the Wind Over Time (10 kn)



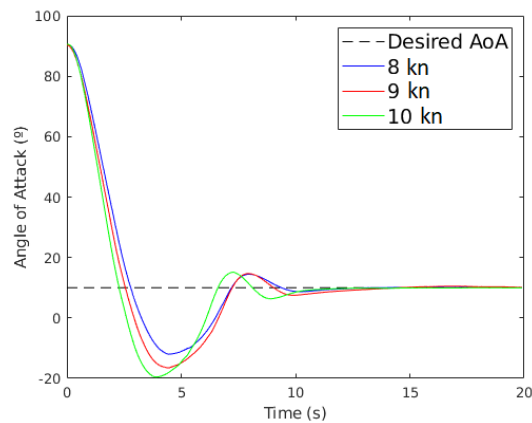
**Figure 10.** Time Response of the Wing Sail AoA ( $\alpha_i = 90^\circ$ ,  $\alpha_f = 0^\circ$ )

#### 294 3.4. Setting the Wing Sail to an Angle of Attack

295 These tests check if the wing sail direction is controllable through the flap angle. Specifically, it  
 296 verifies if the wing sail stabilizes at a defined angle of attack. The apparent wind direction was set  
 297 to  $90^\circ$  ( $\alpha_i = 90^\circ$ ), the apparent wind velocity to 8 kn, 9 kn and 10 kn, and the final desired angle of  
 298 attack ( $\alpha_f$ ) to  $10^\circ$ . Figure 12 plots the obtained time responses. The wing sail direction overshoots the  
 299 desired angle of attack but stabilizes after a few seconds. These results validate the wing sail control as  
 300 it successfully stabilized the wing sail to the defined angle of attack.



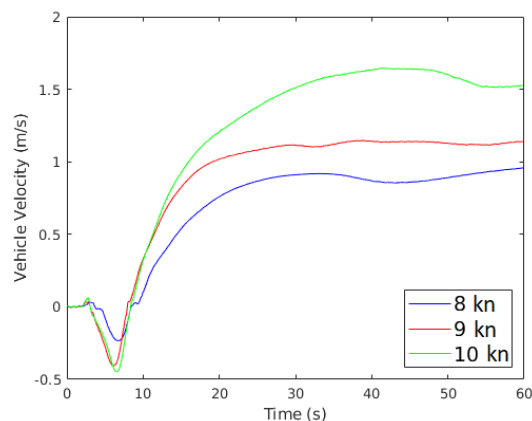
**Figure 11.** Wing Sail Response to Flap Angle Changes (8 kn)



**Figure 12.** Time Response of the Wing Sail AoA ( $K_p = 0.05$ ,  $K_d = 0.07$ ,  $\alpha_i = 90^\circ$ ,  $\alpha_f = 10^\circ$ )

### 301 3.5. Vehicle Motion

302 The final experiment tests if the wing sail provides enough lift to displace the vehicle. The initial  
 303 apparent wind direction was set to  $90^\circ$  ( $\alpha_i = 90^\circ$ ), the apparent wind velocity to 8 kn, 9 kn and 10 kn,  
 and the final desired angle of attack ( $\alpha_f$ ) to  $10^\circ$ . Figure 13 shows the vehicle velocity over time. Initially,



**Figure 13.** Vehicle Velocity Over Time ( $K_p = 0.05$ ,  $K_d = 0.07$ ,  $\alpha_i = 90^\circ$ ,  $\alpha_f = 10^\circ$ )

304 the vehicle displays negative velocities because the wing sail overshoots the desired angle of attack  
 305 for a short period of time. With negative angle of attack values, negative lift coefficients are obtained  
 306 and, consequently, negative accelerations, making the vehicle move slightly backwards. After this  
 307 period, the vehicle starts moving forward with positive acceleration. The velocity increases until the  
 308 acceleration of the vehicle becomes null or the terminal maximum velocity is achieved. The velocity  
 309

310 can be reduced by changing the angle of attack of the wing sail until, ultimately, it becomes zero,  
 311 eventually stopping the vehicle. This experiment shows that the wing sail was able to provide enough  
 312 lift to move the vehicle.

### 313 3.6. Polar Diagram

314 The polar diagram characterises the optimal performance of a wind propelled platform as a  
 315 function of the wind velocity and apparent wind angle. In this test, the autonomous flap control was  
 316 responsible for the optimisation of the lift force applied to the wing sail. Three different wind velocities  
 317 were simulated (8 kn, 9 kn and 10 kn) together with apparent wind direction increments of 5° from 0°  
 318 to  $\pm 180^\circ$ .

319 The velocity started increasing at approximately  $\pm 45^\circ$  until peaked at  $\pm 90^\circ$ . After peaking, the  
 320 maximum velocity started decreasing until it reached null values near  $\pm 180^\circ$ , as shown in the polar  
 321 diagram presented in Figure 14. The no go zone is visible between  $-45^\circ$  and  $45^\circ$ , and between  $-135^\circ$   
 and  $135^\circ$ .

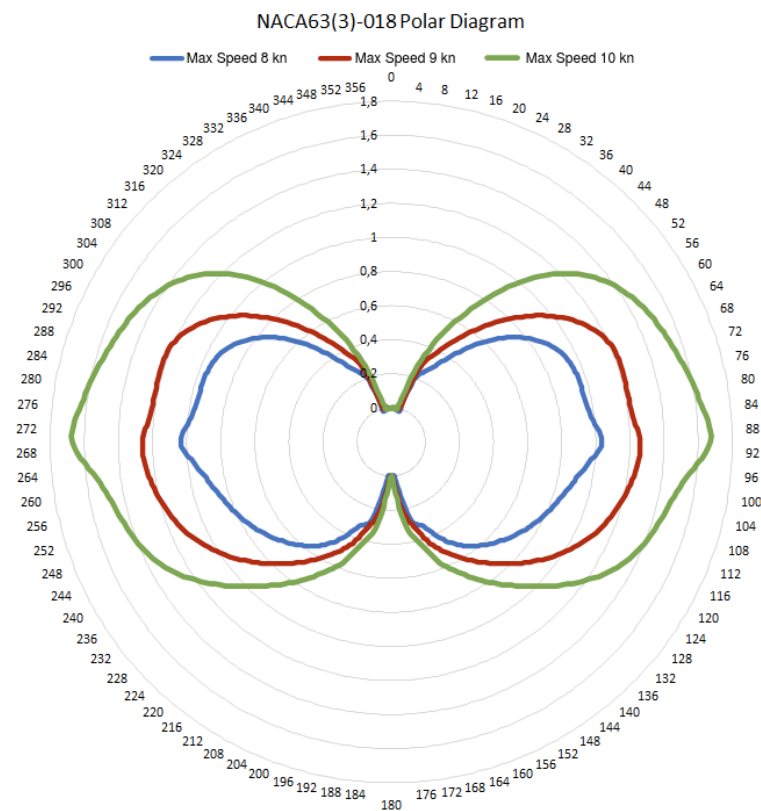


Figure 14. Land Yacht Polar Diagram

322

## 323 4. Conclusions

324 The design, modelling and simulation of an autonomous wing sail land yacht was successful as  
 325 the wing sail responded correctly to the wind direction and to changes in the flap angle. Furthermore,  
 326 the sailing behaviour of the designed land yacht is characterised by its polar diagram. Some of the  
 327 values used in the modelling and simulation were arbitrated since there was no possibility of obtaining  
 328 them through experimentation. This simulated environment can be further enhanced to provide  
 329 several different scenarios, such as sandy coastal regions, and can be utilised by a different modelled  
 330 land yacht with a different type of airfoil, provided the airfoil characteristics. Although the control  
 331 was not the main focus of this work, it can also be refined to solve the identified frailties. Future work  
 332 will focus on experimenting with different types of airfoils and control techniques.

333 **Author Contributions:** Vítor Tinoco was responsible for the investigation, implementation of the methodology  
 334 and software as well as the preparation of the original draft. Benedita Malheiro and Manuel F. Silva contributed  
 335 with the conceptualization, review and editing, supervision and funding acquisition.

336 **Funding:** This work was partially financed by National Funds through the FCT – Fundação para a Ciência e a  
 337 Tecnologia (Portuguese Foundation for Science and Technology) as part of project UIDB/50014/2020.

338 **Conflicts of Interest:** The authors declare no conflict of interest.

### 339 Abbreviations

340 The following abbreviations are used in this manuscript:

341	$\alpha$	Angle of Attack
	$\alpha_i$	Initial Angle of Attack
	$\alpha_f$	Final Angle of Attack
	$\theta$	Angle of the Apparent Wind
342	AoA	Angle of Attack
	GNSS	Global Navigation Satellite System
	NACA	National Advisory Committee for Aeronautics
	PD	Proportional-Differential
	ROS	Robot Operating System
	SDF	Simulation Description Format

### 343 References

- 344 1. National Academy of Engineering. *Autonomy on Land and Sea and in the Air and Space: Proceedings of a*  
 345 *Forum*; The National Academies Press: Washington, DC, 2018. doi:10.17226/25168.
- 346 2. Zhu, X.; Kim, Y.; Minor, M.A.; Qiu, C. *Autonomous Mobile Robots in Unknown Outdoor Environments*; CRC  
 347 Press: Boca Raton, FL, USA, 2020.
- 348 3. Springer, P.J. *Outsourcing War to Machines – The Military Robotics Revolution*; Praeger Security International:  
 349 Santa Barbara, California, 2018.
- 350 4. Kimball, J. *Physics of Sailing*; CRC Press, 2009.
- 351 5. Miller, P.H.; Hamlet, M.; Rossman, J. Continuous Improvements to USNA SailBots for Inshore Racing and  
 352 Offshore Voyaging. *Robotic Sailing 2012 – Proceedings of the 5th International Robotic Sailing Conference,*  
 353 *2012*, pp. 49–60. doi:10.1007/978-3-642-33084-1\_5.
- 354 6. Anthierens, C.; Pauly, E.; Jeay, F. MARIUS: A Sailbot for Sea-Sailing. *Robotic Sailing 2013 – Proceedings of*  
 355 *the 6th International Robotic Sailing Conference, 2013*, pp. 3–12. doi:10.1007/978-3-319-02276-5\_1.
- 356 7. Miller, P.; Sauzé, C.; Neal, M. Development of ARRTOO: A Long-Endurance, Hybrid-Powered,  
 357 Oceanographic Research Vessel. *Robotic Sailing 2013 – Proceedings of the 6th International Robotic*  
 358 *Sailing Conference, 2013*, pp. 53–65. doi:10.1007/978-3-319-02276-5\_5.
- 359 8. Silva, M.F.; Friebe, A.; Malheiro, B.; Guedes, P.; Ferreira, P.; Waller, M. Rigid wing sailboats: A state of the  
 360 art survey. *Ocean Engineering* **2019**, *187*, 106–150.
- 361 9. Shukla, P.C.; Ghosh, K. Revival of the Modern Wing Sails for the Propulsion of Commercial Ships.  
 362 *International Journal of Physical and Mathematical Sciences* **2009**, *3*, 207 – 212.
- 363 10. Landis, G.; et al.. NIAC Phase 1 Final Report: Venus Landsailer Zephyr. Technical report, NASA, 2014.
- 364 11. Xie, S.; Chen, J.; li, H.; Luo, J.; Pu, H.; Peng, Y. The research on wing sail of a land-yacht robot. *Advances in*  
 365 *Mechanical Engineering* **2015**, *7*, 1–19. doi:10.1177/1687814015623144.
- 366 12. Xie, S.; Feng, K.; Peng, Y.; Luo, J.; Chen, J.; Gu, J. Design and analysis of an autonomous controlled four  
 367 wheeled land yacht. *2014 IEEE International Conference on Information and Automation, ICIA 2014* **2014**, pp.  
 368 773–778. doi:10.1109/ICInfA.2014.6932756.
- 369 13. Zhu, A.; Beer, C.; Juhandi, K.; Orlov, M.; Bacau, N.; Kádár, L.; Duarte, A.J.; Malheiro, B.; Justo, J.; Silva, M.F.;  
 370 Ribeiro, M.C.; Ferreira, P.D.; Guedes, P. Sail Car – An EPS@ISEP 2019 Project. 2020 IEEE Global Engineering  
 371 Education Conference (EDUCON), 2020, pp. 487–492. doi:10.1109/EDUCON45650.2020.9125314.
- 372 14. Landis, G.A.; Oleson, S.R.; Grantier, D. Zephyr: A Landsailing Rover for Venus. 65th International  
 373 Astronautical Congress, 2014, p. 14.



- 374 15. Chen, J.; Ye, Z.; Yang, R.; Cai, G.; Li, J.; Li, H. Design and Control of Multiple Wing-sail Land Yacht  
375 Robot. 2018 IEEE International Conference on Mechatronics and Automation (ICMA), 2018, pp. 1800–1805.  
376 doi:10.1109/ICMA.2018.8484725.
- 377 16. Mirzaei, P.A.; Rad, M. Toward design and fabrication of wind-driven vehicles: Procedure to optimize the  
378 threshold of driving forces. *Applied Mathematical Modelling* **2013**, *37*, 50 – 61. doi:10.1016/j.apm.2011.11.037.
- 379 17. Dong, Y.; Ding, X.; Li, Z.; Zhang, L.; Liu, H.; Ding, N.; Sun, Z.; Qian, H. Wing Sail Land-yacht Modeling  
380 And System Verification. 2019 IEEE International Conference on Robotics and Biomimetics (ROBIO), 2019,  
381 pp. 1350–1355. doi:10.1109/ROBIO49542.2019.8961489.
- 382 18. Reina, G.; Foglia, M. Modelling and handling dynamics of a wind-driven vehicle. *Vehicle System Dynamics*  
383 **2019**, *57*, 697–720. doi:10.1080/00423114.2018.1479529.
- 384 19. Eliasson, R.; Larsson, L.; Orych, M. *Principles of Yacht Design*; Bloomsbury Publishing, 2014.
- 385 20. Elkaim, G. Autonomous Surface Vehicle Free-Rotating Wingsail Section Design and Configuration Analysis.  
386 *Journal of Aircraft - J AIRCRAFT* **2008**, *45*, 1835–1852. doi:10.2514/1.27284.
- 387 21. Neal, M. A Hardware Proof of Concept of a Sailing Robot for Ocean Observation. *IEEE Journal of Oceanic*  
388 *Engineering* **2006**, *31*, 462–469. doi:10.1109/JOE.2006.875101.
- 389 22. Friebe, A.; Olsson, M.; Le Gallic, M.; Springett, J.L.; Dahl, K.; Waller, M. A marine research ASV utilizing  
390 wind and solar power. OCEANS 2017 - Aberdeen, 2017, pp. 1–7. doi:10.1109/OCEANSE.2017.8084648.
- 391 23. Chen, J.; Xie, S.; Luo, J.; Li, H. Wind-driven land-yacht robot mathematical modeling and verification. *Ind.*  
392 *Robot* **2016**, *43*, 77–90.
- 393 24. Rynne, P.F.; von Ellenrieder, K.D. Development and Preliminary Experimental Validation of a Wind-  
394 and Solar-Powered Autonomous Surface Vehicle. *IEEE Journal of Oceanic Engineering* **2010**, *35*, 971–983.  
395 doi:10.1109/JOE.2010.2078311.
- 396 25. Enqvist, T.; Friebe, A.; Haug, F. Free Rotating Wingsail Arrangement for Åland Sailing Robots. *Robotic*  
397 *Sailing 2016*; Alves, J.C.; Cruz, N.A., Eds.; Springer International Publishing: Cham, 2017; pp. 3–18.  
398 doi:10.1007/978-3-319-45453-5\_1.
- 399 26. Augenstein, T.; Singh, A.; Miller, J.; Pomerenk, A.; Dean, A.; Ruina, A. Using a Controlled Sail and Tail to  
400 Steer an Autonomous Sailboat. *Robotic Sailing 2016*; Alves, J.C.; Cruz, N.A., Eds.; Springer International  
401 Publishing: Cham, 2017; pp. 91–103. doi:10.1007/978-3-319-45453-5\_8.
- 402 27. Setiawan, J.D.; Chrismianto, D.; Ariyanto, M.; Sportyawan, C.W.; Widyantara, R.D.; Alimi, S. Development  
403 of Dynamic Model of Autonomous Sailboat for Simulation and Control. 2020 7th International  
404 Conference on Information Technology, Computer, and Electrical Engineering (ICITACEE), 2020, pp.  
405 52–57. doi:10.1109/ICITACEE50144.2020.9239150.
- 406 28. Tinoco, V. Modelling and Simulation of a Wing Sail Land Yacht. Master's thesis, School of Engineering,  
407 Polytechnic of Porto, Porto, Portugal, 2020.
- 408 29. Silva, M.F.; Malheiro, B.; Guedes, P.; Ferreira, P. Airfoil Selection and Wingsail Design for an  
409 Autonomous Sailboat. *Robot 2019: Fourth Iberian Robotics Conference*; Silva, M.F.; Lima, J.L.; Reis,  
410 L.P.; Sanfeliu, A.; Tardioli, D., Eds.; Springer International Publishing: Cham, 2020; pp. 305–316.  
411 doi:10.1007/978-3-030-35990-4\_25.
- 412 30. Getzan, G.D.; Shimada, M.; Shimoyama, I.; Matsumoto, Y.; Miura, H. Aerodynamic behavior of  
413 microstructures. ETFA '94. 1994 IEEE Symposium on Emerging Technologies and Factory Automation.  
414 (SEIKEN) Symposium - Novel Disciplines for the Next Century- Proceedings, 1994, pp. 54–61.  
415 doi:10.1109/ETFA.1994.402023.
- 416 31. Airfoil Tools. NACA 63(3)-018 (naca633018-il). [http://airfoiltools.com/airfoil/details?airfoil=naca633018-  
417 il](http://airfoiltools.com/airfoil/details?airfoil=naca633018-il), 2020. Last accessed 28 November 2020.
- 418 32. Drela, M. XFOIL: An Analysis and Design System for Low Reynolds Number Airfoils. *Low Reynolds*  
419 *Number Aerodynamics*; Mueller, T.J., Ed.; Springer Berlin Heidelberg: Berlin, Heidelberg, 1989; pp. 1–12.
- 420 33. Rivera, Z.B.; Simone, M.C.D.; Guida, D. Unmanned Ground Vehicle Modelling in Gazebo/ROS-Based  
421 Environment. *Machines* **2019**, *7*, 42. doi:10.3390/machines7020042.

422 **Sample Availability:** <https://1drv.ms/u/s!Amsuyvsv73czu1bUoPfhil2n2NZK?e=JYIcfv>