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## LAMAX-S

# A Language for Matrix Calculation on Super Computers

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#### Introduction 1

In supercomputing, matrix calculation and vector calculation are used frequently. But because of the lack of matrix calculation function in FORTRAN, it is very difficult to write an efficient program for various super computers. In most cases, we have to tune up a program so as to fit the program coding to a peculiarity of each super computer.

We have been designed and implemented a new programming language, LAMAX-S (a LAnguage for MAtriX calculation on super computer) and its processor. LAMAX-S is an enhanced FORTRAN:

LAMAX-S = FORTRAN + Matrix class and its calculation

The purpose of LAMAX-S is as follows.

- writability & readability To introduce matrix class to FORTRAN, we can write a program easily which uses a matrix calculation. Matrix calculation can be programmed as an expression directly. And there are many operations for matrix data.
- efficiency LAMAX-S is designed so as to run as fast as possible on various super computers. LAMAX-S generates a well-tuned FORTRAN source program for various super computers.

LAMAX-S is realized as a preprocessor to FORTRAN. That is, LAMAX-S source program is translated to the equivalent FORTRAN source program by the LAMAX-S preprocessor. Then, the FORTRAN program is compiled by FORTRAN compiler, and linked with Matrix calculation library. This process is shown in Fig. 1.

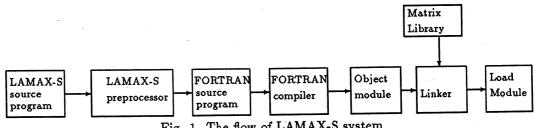


Fig. 1. The flow of LAMAX-S system

In this paper, we will introduce the outline of LAMAX-S informally.

### 2 A brief introduction using sample programs

#### 2.1 Regression

1 1

In order to show the image of LAMAX-S, we show a brief sample program list in program 1. This program is for calculating regression model. In the following regression model,

 $Y = X\beta + \varepsilon$ 

where, Y is a vector which has n elements, X is  $n \times k$  matrix,  $\beta$  is a vector which has k elements,  $\varepsilon$  is a vector which has n elements.  $\hat{\beta}$  is definded as follows:

$$\widehat{\beta} = (X'X)^{-1}X'Y$$

1	С	
2	C	Regression
3	с	
4		<pre>parameter(n=10,k=5)</pre>
5		real*8 X:rectangluar[n,k]
6		real*8 Y:vector[n]
7		real*8 B:vector[k]
8		real*8 E:vector[n]
9		
10		call minput(X)
11		call minput(Y)
12		
13		B = 1 / (X'*X) * X' * Y
14		$\mathbf{E} = \mathbf{Y} - \mathbf{X} \mathbf{*} \mathbf{B}$
15		
16		call mprint(B)
17		call mprint(E)
18		
19		stop
20		end

As LAMAX-S is an enhanced FORTRAN, most of FORTRAN statements can be included in a LAMAX-S source program. Line 1-3 are comment line. Line 4,19 and 20 are all FORTRAN statements. Line 5-8 declare matrix and vector variables. In Line 5, X is declared as an  $n \times k$  rectangular matrix variable which element type is real\*8 (double precision). Y and E are both vector variables which have n elements, and which element type is also real \*8. B is also a vector variable which has k elements. Line 10-11, 16 and 17 are LAMAX-S built-in subroutine call. A built-in subroutine named "minput" inputs matrix or vector data in a special format. Also "mprint" subroutine prints out matrix or vector data in a special format. Line 13,14 are expression which calculate the regression. In LAMAX-S, a representation of an inverse matrix uses a division expression: for example, an inverse matrix A or  $A^{-1}$  is represented as 1/A. An operator '(single quotation) represents a transposed matrix. Therefore, an expression,

$$\widehat{\beta} = (X'X)^{-1}X'Y$$

program 1. The regression program

B = 1 / (X'X) \* X' \* Y

is represented in LAMAX-S as follows:

#### 2.2 simultaneous linear equation using Jacobi-method

Program 2. shows a program of simultaneous linear equation using Jacobi-method. We solve the following simultaneous linear equation:

AX = b

In the first step of the method, matrix A is split as follows:

$$A = L + D + U$$

where L is a lower triangular matrix, D is a diagonal matrix, U is an upper triangular matrix. Using the following expression, an approximate value is renewal.

$$X_{(new)} = D^{-1}(b - (L+U)X_{(old)})$$

In line 18, matrix A is split to L (lower triangular part of A), D (diagonal part of A), and U (lower triangular part of A). In line 20, 0::vector [n] means a constant vector which has n elements and all the values are zero. In line 24, "absmax" function is a build-in function of LAMAX-S. The function returns a maximum absolute value which absolute value is a maximum in the argument.

1	~	
		-ilease lines anotic write least
2		simultaneous linear equation using Jacobi-method
3		
4		parameter(n=100, eps=1D-12)
5		n an
6	:	real*8 A:square[n]
7		
8		real*8 D:diagonal[n]
9		real*8 L:lower_tr[n,1]
10		real*8 U:upper_tr[n,1]
11	,	real*8 X:vector[n]
12	:	real*8 NewX:vector[n]
13	:	real*8 B:vector[n]
14		
15		call minput(A)
16		call minput(B)
17		
18		L ^ D ^ U  {-1,1} << A
19		
20		X = 0::vector[n]
21		
22		do 10 i=1,100
23		NewX = 1/D * ( B - ( L + U ) * X )
24		if(absmax(NewX-X).le.eps) goto 20
25		X = NewX
26	10	continue
27		
28		write(*,*) 'could not solve after 100 iterations'
29		goto 30
30		
31	20	continue
32		write(*,*) 'could solve'
33		call mprint(NewX)
34		· · · · · · · · · · · · · · · · · · ·
35	30	continue
36	50	stop
37		end
0.		

Program 2. simultaneous linear equation using Jacobi-method

### 3 LAMAX-S grammar

### 3.1 Matrix declaration

Table 1. shows the matrix form in LAMAX-S. As shown in Table 1., each matrix/vector variable has three attributes: form, density and symmetry. The underlined attribute is default.

Table 1. The Form in LAMAX-S					
Form	Density of element	Symmetry			
$rectangular(m \times n)$ matrix					
square matrix					
vector	dense	symmetric			
row vector					
band matrix	sparse	asymmetric			
diagonal matrix					
tridiagonal matrix					
upper triangular matrix					
lower triangular matrix					

These attributes are declared in declaration statements. In LAMAX-S, the form of declaration statement is as follows.

Tal	ble	2.	De	clar	ation	of	Form

explanation of matrix form	syntax of declaration
rectangular(m×n) matrix	rectangular[m,n]
$(m \times m)$ square matrix	square[m]
vector which has m elements	vector[m]
row vector which has m elements	rvector[m]
$(m \times m, s upper band wide, t lower band wide) band matrix$	band[m,s,t]
(m×m) diagonal matrix	diagonal[m]
(m×m) tridiagonal matrix	diag_3[m]
(m×m) upper triangle matrix	upper_tr[m]
$(m \times m)$ lower triangle matrix	lower_tr[m]

Density of element and symmetricity are specified after size parameter followed by colon (:) in a type declaration statement. For example, the following statement declares A as a rectangular matrix which size is  $100 \times 10$ , and its elements are all integer.

integer A:rectangular[100,10]

The following statement declares A as a square matrix which size is  $100 \times 100$ , and also which is symmetric.

integer A:square[100:symmetric]

And the following statement declares A as a sparse matrix.

integer A:rectangular[100,10:sparse[150]]

"sparse[150]" indicates that the matrix A has 1,000 elements, but as the matrix is sparse, the actual non zero elements are at most 150.

Of course, the following statement declares a symmetric sparse matrix.

#### integer A:square[100:symmetric,sparse[150]]

Now several examples are shown below:

declaration in a program	meaning	element type
<pre>integer A:rectangular[m,n]</pre>	m×n rectangular matrix	integer
real*8 A:band[m,nu,nl]	m×m band matrix	real*8
<pre>complex A:band[1000,nu,ul:sparse[200]]</pre>	$1000 \times 1000$ band matrix	complex

### 3.2 Matrix operator

For the writability, LAMAX-S has an enough operator to write a complex matrix calculation. Table 3. shows the matrix calculation operators.

priority	operator	meaning	syntax	result form
1	3	transposed	M,	M
2	!	LU decomposition	! M	M
3	**	power	S**S,M**S	S,M
4	*	matrix multiplication	S*S,S*M,M*S,M*M	S,M,M,M
4	Ł.	multiplication by element	M&M	М
4	1	division	S/S, M/S	S,M
4	1.	inverse matrix	S/M, M/M	M,M
4	Х	division by element	M%M	M
4	?	solution	M?M	M
4		concatenation	C//C	С
5	+	positive sign	+S,+M	S,M
5	-	negative sign	—S,—M	S,M
5	+	addition	S+S,M+M	S,M
5	-	subtraction	S-S,M-M	S,M
6	=	assignment	S=S,M=M	S,M
6	:=	enforced assignment	M:=M	
6	<=	insertion	M{S,S}<=M	
6	=>	extraction	M{S,S}=>M	
6	<=>	exchange	M<=>M	
6	<<	partition	M< <m< td=""><td>······································</td></m<>	······································

Table 3. Matrix calculation operators in LAMAX-S<sup>1</sup>

### 4 Actual implementation

The LAMAX-S precompiler processor has been implemented by **ISP**(Research Institute of Systems Planning.) The latest processor is called as version 1.1. Version 1.1 is only for **PIAX** machine, which is a personal super computer developed by **NKK**. Now, we are planning to implement the processor for other super computers.

It is very sorry that version 1.1 lacks the following two functions.

- sparse matrix calculation
- optimization peculiar to matrix calculation.

As a matrix library, version 1.1 uses LINPACK. Namely, LAMAX-S processor generates FORTRAN program which include LINPACK subroutine call. But in other super computer, we are going to use a built-in libraries of the super computer. For example, in NEC SX, ASL will be used as a library. In Hitachi S-820, Matrix/HAP will be used.

<sup>&</sup>lt;sup>1</sup>S:scalar, M:matrix or vector, C:character

The first step of our project, that is, to implement usable processor of LAMAX-S will be accomplished. Our Next step consists of the following three:

- to introduce sparse matrix calculation
- to introduce optimization peculiar to matrix calculation.
- to support other super computer