

# Distribution of Monthly Rainfall in Northeast Thailand 

Huynh Ngoc Phien,* Anat Arbhabhirama** and Apichai Sunchindah**


#### Abstract

The distribution in space and in time of monthly rainfall in Northeast Thailand is investigated in this paper, using daily data at 56 stations, each having at least 20 years of continuous record. It was found that monthly rainfall sequences at all stations in this region have six significant harmonics corresponding to six periods: 12, 6, 4, 3, 2.4 and 2 months. At a station, the rainfall sequence in a month can be considered to be independent and can be fitted by the leakage law. Moreover, during the months of April through September, monthly rainfall in the region has a general pattern of increasing values towards the eastern and northeastern sections, while during the months of October to January, it has a general pattern of decreasing values towards these sections. Finally, an assessment of water availability for irrigation is made using the distribution of monthly rainfall and the potential evapotranspiration.


## Introduction

Monthly distributions of rainfall in space and time can provide guidelines for crop scheduling, better cropping patterns and the planning and design of water resources development projects. The present study aims at two main objectives: (i) Fitting the distribution in time of the monthly rainfall sequences at various stations in Northeast Thailand, hereafter referred to as the Northeast; (ii) Assessment of water availability for irrigation purposes, based on the most appropriate distribution found in (i) and the evapotranspiration data. In

[^0]addition, several important characteristics of rainfall sequences in the region such as the periodicity and the degree of irregularity are also presented.

## I Study Area and Data Assembly

The Northeast has an area of about $167,300 \mathrm{~km}^{2}$ and a population of approximately 15 million. It consists of 16 provinces listed in alphabetical order as follows: Buriram, Chaiyaphum, Kalasin, Khon Kaen, Loei, Maha Sarakham, Nakhon Phanom, Nakhon Ratchasima, Nong Khai, Roi Et, Sakhon Nakhon, Si Sa Ket, Surin, Ubon Ratchathani, Udon Thani and Yasothon. (Fig. 1)

The daily rainfall data from 56 rainfall stations in the Northeast were employed in the analysis. These stations were selected using the following two criteria:


Fig. 1 Map of the Northeast with the Locations of Selected Rainfall Stations
(i) Continuous daily data for at least 20 years should be available for each station.
(ii) Stations should be evenly distributed over the region.

As a result of these criteria, at least two stations from each province were used in this study, except for the province of Yasothon where only one station satisfies the stated criteria. The stations located at the provincial capitals are designated by their respective names while the remaining ones are denoted by abbreviations as shown in Fig. 1.

The data were processed according to water year, which begins on the 1st of April and ends on the 31st of March of the following year.

The amount of rainfall in a month at a station was obtained by summing up all the daily amounts in that month and the collection of these monthly values over the period of the record formed the monthly rainfall sequence at that station.

## II Distribution of Monthly Rainfall Sequences

## Periodicity

Due to the periodic motion of the earth around the sun and about its own axis, rainfall, like any other hydrologic event, is believed to have periodic components. There have been several methods for determining the periodicity of a hydrologic sequence such as spectral analysis or harmonic analysis (see, for example,

Chow and Karetiotis，1970；Quimpo and Cheng，1974），however，the most widely accepted scheme is that of Yevjevich （1972）．In this context，the monthly rainfall sequence at a station is considered to be a periodic－stochastic process，with periodicities caused by astronomical cycles and stochasticities being the result of the chance processes in the terrestial environment（Yevjevich，1976）．To de－ termine these periodicities，the method of Yevjevich（1972）was used．Details concerning this method can be found in Tao et al．（1976）and in Tao and Delleur （1976）．A brief description is given be－ low．The periodic parts of the monthly means and standard deviations are writ－ ten，using the Fourier series approach，in the following general form：

$$
\begin{equation*}
\nu_{j}=v+\sum_{k=1}^{m}\left(A_{k} \cos \frac{\Pi k j}{6}+B_{k} \sin \frac{\Pi k j}{6}\right) \tag{1}
\end{equation*}
$$

where
$\nu_{j}=$ the periodic part，$j=1, \ldots, 12$ ，
$u=$ the mean of twelve sample statis－ tics $v_{j} ; v_{j}$ being the mean or standard deviation of month $j$ ；
$A_{k}, B_{k}=$ the Fourier coefficients which can be estimated by the least－squares method，and
$m=$ the number of significant har－ monics．
For the $k$－th harmonic，the ratio

$$
\begin{equation*}
(1 / 2)\left(A_{k}^{2}+B_{k}^{2}\right) / \text { Variance }\left(v_{j}\right) \tag{2}
\end{equation*}
$$

represents the part of the variance of $v_{j}$ explained by this harmonic．The num－ ber of significant harmonics is then easily determined using the empirical method of Yevjevich（1972）．It was found that
monthly rainfall sequences at all stations in the region have six significant har－ monics．This means that monthly rain－ fall can be considered to have a periodic part that consists mainly of six compo－ nents corresponding to the following six periods：12，6，4，3， 2.4 and 2 months． Moreover，the variances of the monthly means and monthly standard deviations are explained up to more than $90 \%$ by these six harmonics as shown in Table 1

Table 1 Percent of Variance Explained by the First Six Harmonics

| Station | Mean | Standard <br> Deviation |
| :--- | :---: | :---: |
| Buriram | 9.925 | 0.917 |
| Chaiyaphum | 0.940 | 0.938 |
| Kalasin | 0.924 | 0.920 |
| Khon Kaen | 0.927 | 0.937 |
| Loei | 0.924 | 9.921 |
| Maha Sarakham | 0.935 | 0.921 |
| Nakhon Phanom | 0.924 | 0.979 |
| Nakhon Ratchasima | 0.931 | 0.920 |
| Nong Khai | 0.919 | 0.929 |
| Roi Et | 0.922 | 0.919 |
| Sakhon Nakhon | 0.917 | 0.941 |
| Ubon Ratchathani | 0.922 | 0.942 |
| Udon Thani | 0.917 | 0.927 |
| Yasothon | 0.927 | 0.939 |

for stations at the provincial capitals． Due to the high proportions of the variances being explained by the periodic parts in the monthly means and standard deviations，the removal of these six periodic components from a rainfall sequence yields a stochastic process sta－ tionary in the mean and variance，which is commonly referred to as a weakly stationary process．

## Persistence

To examine the influence of rainfall in
a month on the rainfall in the following month at the same station, the serial correlation coefficient was computed. By inspecting the values obtained, it was found that they are very small, and for most cases, they turn out to be nonsignificantly different from zero by the test of Anderson (1942). Under such a situation, the rainfall sequence at a station for each month can be treated separately.

## Distribution in Time

Most of the monthly rainfall sequences in the region were found to have high positive skewness coefficients. It is wellknown that for positively skewed sequences, lognormal and gamma distributions often yield the best fits. However, the monthly rainfall sequences in the region, especially those in the dry season, consist of several zero values, which make these two distributions unsuitable (see Mekong Secretariat, 1974). Instead, the leakage law (in French: loi des fuites) was employed. This distribution is defined as follows:

$$
\begin{align*}
& P(R=0)=\exp (-a)  \tag{3}\\
& P(x<R<x+d x) \\
& \quad=(a b / x)^{1 / 2} \exp (-a-b x) I_{1}\left[2(a b x)^{1 / 2}\right] d x, \\
& \quad x>0 \tag{4}
\end{align*}
$$

where $a$ and $b$ are the two parameters,
$I_{1}$ is the modified Bessel function of order 1, exp is the exponential function, and $R$ denotes the amount of rainfall.
The mean and variance of the leakage law are given by

$$
\begin{equation*}
\mu=a / b \quad \text { and } \quad \sigma^{2}=2 a / b^{2} \tag{5}
\end{equation*}
$$

from which the moment estimates of the parameters $a$ and $b$ are obtained as

$$
\begin{align*}
& a=2(\bar{R} / S)^{2}  \tag{6}\\
& b=2 \bar{R} / S^{2} \tag{7}
\end{align*}
$$

where $\bar{R}$ and $S$ are the estimates of $\mu$ and $\sigma$, respectively.

The likelihood equations and their solutions were given by Buishand (1977). It can be seen from these equations that estimation of the parameters by the maximum likelihood method is complicated and time-consuming. Therefore, only the method of moments (Eqs. 6 and 7) was used. Typical results of fitting monthly rainfall sequences at several stations by the leakage law are given in Table 2, together with the results corresponding to lognormal and gamma distributions, where applicable. The computed values of the Smirnov-Kolmogorov test are always less than the critical values at both the significance levels of 0.01 and 0.05 , thus proving the acceptability of the fittings. Since the smaller the value of the test indicates the better the goodness of fit, the above computed values show that there is no absolute superiority of one distribution over the other two, whenever all of them are applicable, because the values of the test corresponding to one distribution is smallest in some cases and largest in other cases. However, the leakage law is relatively superior to the other two distributions because it has the smallest values for the test in most of the cases. The leakage law has a clear advantage

Table 2 Typical Results from Fitting Monthly Rainfall Sequences（For Transitional Months）

| $\begin{gathered} \text { Sta- } \\ \text { tion }^{(+)} \end{gathered}$ | Leakage Law |  |  | Gamma <br> Distri－ <br> bution | Lognormal Distri－ bution |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | a | b | Statis－ tic ${ }^{(*)}$ | Statis－ tic ${ }^{(*)}$ | Statis－ tic ${ }^{(*)}$ |
| April |  |  |  |  |  |
| （1） | 4.735 | 0.061 | 0.111 | 0.121 | 0.147 |
| （2） | 8.455 | 0.104 | 0.076 | － | － |
| （3） | 4.289 | 0.076 | 0.059 | － | － |
| （4） | 5.077 | 0.082 | 0.120 | － | － |
| （5） | 6.628 | 0.056 | 0.058 | 0.070 | 0.097 |
| （6） | 2.800 | 0.041 | 0.041 | 0.080 | 0.097 |
| （ 7 ） | 3.952 | 0.040 | 0.111 | 0.124 | 0.123 |
| （ 8 ） | 6.854 | 0.093 | 0.117 | 0.127 | 0.157 |
| （9） | 8.214 | 0.090 | 0.122 | 0.128 | 0.152 |
| （10） | 5.445 | 0.068 | 0.108 | 0.113 | 0.138 |
| （11） | 6.411 | 0.086 | 0.117 | 0.132 | 0.161 |
| （12） | 4.086 | 0.054 | 0.063 | 0.059 | 0.111 |
| October |  |  |  |  |  |
| （1） | 4.380 | 0.026 | 0.072 | 0.092 | 0.127 |
| （2） | 3.558 | 0.003 | 0.095 | 0.111 | 0.163 |
| （3） | 4.028 | 0.062 | 0.072 | 0.088 | 0.148 |
| （4） | 3.580 | 0.045 | 0.100 | 0.130 | 0.177 |
| （ 5 ） | 3.923 | 0.025 | 0.079 | 0.086 | 0.123 |
| （6） | 3.832 | 0.055 | 0.066 | 0.083 | 0.145 |
| （ 7 ） | 1.842 | 0.034 | 0.172 | － | － |
| （ 8 ） | 7.743 | 0.048 | 0.181 | 0.182 | 0.210 |
| （9） | 2.636 | 0.046 | 0.075 | － | － |
| （10） | 3.751 | 0.043 | 0.102 | 0.139 | 0.198 |
| （11） | 2.359 | 0.036 | 0.132 | 0.107 | 0.108 |
| （12） | 3.767 | 0.041 | 0.061 | 0.064 | 0.096 |

Notes：
（＊）Smirnov－Kolmogorov test：Critical value at 5\％significance level： 0.27
（－）Not applicable
$(+)$ Stations at provincial capitals
（1）Buriram
（2）Chaiyaphum
（3）Kalasin
（4）Khon Kaen
（5）Loei
（6）Maha Sarakham
（7）Nakhon Phanom
（8）Nakhon Ratchasima
（9）Nong Khai
（10）Roi Et
（11）Sakhon Nakhon
（12）Ubon Ratchathani
the Northeast，the monthly means at some representative stations were plotted in Fig．2．These graphs clearly indicate that monthly rain－ falls in the region fluctuate greatly from month to month．In general， monthly rainfall at a station in－ creases from April until a maximum value is reached in August or Sep－ tember．After that it decreases very rapidly and reaches a mini－ mum value in December or Janua－ ry．The monthly rainfall then starts to increase again and the cycle is repeated．

It should be noted that the months of August and September correspond to the time when de－ pressions and storms from the Vietnamese coast penetrate the region，often bringing along heavy rainfalls and causing severe flood－ ing in many areas．On the other hand，rainfalls at most stations in the region during December and January are almost nil，resulting in long periods of severe drought．

Besides fluctuating considerably from month to month in the year， rainfall in a given month also fluctuates greatly from year to year． This is indicated by the high values of the variation coefficient，i．e．the ratio of the standard deviation to the mean，as shown in Table 3．Under such a situation，the common practice of assessing the availability of rain water based on the long－term mean of monthly rainfalls is not reliable．Instead it should


Fig. 2 Mean Monthly Rainfall at Some Representative Stations

Table 3 Variation Coefficients of Monthly Rainfall

| Station | Apr. | May | Jun. | Jul. | Aug. | Sept. | Oct. | Nov. | Dec. | Jan. | Feb. | Mar. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Buriram | 0.65 | 0.51 | 0.57 | 0.44 | 0.39 | 0.68 | 1.72 | 5.02 | 3.94 | 2.87 | 1.80 | 0.86 |
| Chaiyaphum | 0.49 | 0.42 | 0.40 | 0.48 | 0.75 | 1.80 | 2.49 | 1.89 | 2.19 | 1.89 | 1.54 | 0.77 |
| Kalasin | 0.68 | 0.51 | 0.40 | 0.40 | 0.46 | 0.70 | 2.44 | 3.26 | 3.03 | 2.81 | 1.21 | 1.13 |
| Khon Kaen | 0.63 | 0.58 | 0.60 | 0.40 | 0.40 | 0.75 | 1.85 | 2.15 | 2.31 | 2.21 | 1.85 | 1.16 |
| Loei | 0.55 | 0.46 | 0.44 | 0.60 | 0.40 | 0.71 | 1.29 | 3.09 | 2.22 | 1.72 | 1.10 | 0.67 |
| Maha Sarakham | 0.85 | 0.53 | 0.69 | 0.39 | 0.32 | 0.72 | 1.78 | 2.42 | 2.50 | 3.16 | 1.55 | 0.83 |
| Nakhon Phanom | 0.71 | 0.33 | 0.45 | 0.26 | 0.39 | 1.04 | 1.84 | 4.77 | 3.36 | 2.36 | 1.25 | 0.76 |
| Nakhon Ratchasima | 0.74 | 0.43 | 0.72 | 0.52 | 0.45 | 0.55 | 1.90 | 2.73 | 2.60 | 2.62 | 1.23 | 1.20 |
| Nong Khai | 0.48 | 0.38 | 0.35 | 0.38 | 0.49 | 0.81 | 1.75 | 2.70 | 2.52 | 2.22 | 1.62 | 0.88 |
| Roi Et | 0.61 | 0.55 | 0.36 | 0.40 | 0.36 | 0.71 | 1.69 | 3.88 | 3.51 | 2.71 | 1.61 | 0.50 |
| Sakhon Nakhon | 0.56 | 0.40 | 0.42 | 0.44 | 0.38 | 0.92 | 2.13 | 2.65 | 2.48 | 1.98 | 1.75 | 0.84 |
| Ubon Ratchathani | 0.70 | 0.64 | 0.35 | 0.37 | 0.34 | 0.73 | 1.20 | 1.94 | 3.18 | 2.21 | 1.75 | 1.25 |
| Udon Thani | 0.66 | 0.45 | 0.46 | 0.29 | 0.42 | 0.72 | 2.05 | 3.46 | 3.69 | 2.78 | 1.53 | 0.87 |
| Yasothon | 0.86 | 0.58 | 0.47 | 0.36 | 0.46 | 0.76 | 1.87 | 3.63 | 2.81 | 3.99 | 1.74 | 1.45 |

be based upon the distribution of the rainfall sequence. This will be considered later in this paper.

## Distribution in Space

Isohyet maps, one for each month, were prepared in order to find how
rainfall is distributed over different parts of the Northeast. Shown in Figs. 3 to 6 are four of them; the first corresponds to April, a transitional month between dry season and wet season, the second to August, a month in the rainy season, the third to October, a transitional month


Fig． 3 Isohyets for Mean Monthly Rainfall，April


Fig． 4 Isohyets for Mean Monthly Rainfall，August
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Fig. 5 Isohyets for Mean Monthly Rainfall, October


Fig. 6 Isohyets for Mean Monthly Rainfall, December
between wet season and dry season，and the fourth to December，a month in the dry season．From examining all the twelve maps，the following observations were made．During the months of the rainy season，i．e．April through Sep－ tember，the isohyets have a general pattern of increasing values towards the eastern and northeastern sections of the region．From July through September， these two sections have monthly rainfalls exceeding 300 mm ．In the months of October to January，when the whole region becomes progressively drier，the isohyets have a general pattern of decreasing values towards the eastern and northeastern sections．Consequently， these sections are the driest parts of the region during this period．The isohyets for February and March do not show any clear tendencies．

## Degree of Irregularity

As mentioned earlier，rainfall in the Northeast fluctuates greatly from month to month in the year．In order to ex－ press quantatively the variation of rain－ fall within the year，the concept of the degree of irregularity introduced by Shver（1975）was used．For each month of the year，the ratio $r_{j}=P m(i, j) / P y(i)$ is represented by a vector of magnitude $r_{j}$ making with the horizontal line an angle $a_{j}$ which is defined by the following equation

$$
\begin{equation*}
a_{j}=360 n_{j} / 365 \tag{8}
\end{equation*}
$$

where $n_{j}$ is the number of days from the beginning of the year to the middle of
month $j, \operatorname{Pm}(i, j)$ is the rainfall in month $j$ of year $i$ and $P y(i)$ is the annual rainfall in year $i$ ．

Vectors for all months of the year were plotted on a polar diagram representing a bundle of vectors issuing at different angles from a single point．The magni－ tude $D$ of the vectorial sum of all twelve vectors is called the degree of precipitation irregularity which was previously referred to as the degree of precipitation seasonality by Shver（1973）．If all the months of the year have nearly the same amount of rainfall，$D$ is very close to zero．The higher the value of $D$ ，the greater is the fluctuation in rainfall among the different months of the year．Shown in Fig． 7 are the zones in the Northeast having the same mean value of $D$ over the period of the record．It can be seen that the monthly rainfalls in the Northeast have high degrees of irregularity，ranging from $45 \%$ to $70 \%$ and they tend to fluctuate more greatly towards the eastern and northeastern sections of the region．

## Amount of Monthly Rainfall

Ten intervals $(0-10 \mathrm{~mm}, 10-25 \mathrm{~mm}$ ， $25-50 \mathrm{~mm}, 50-75 \mathrm{~mm}, 75-100 \mathrm{~mm}, 100-$ $200 \mathrm{~mm}, 200-300 \mathrm{~mm}, 300-400 \mathrm{~mm}, 400-$ 500 mm and $>500 \mathrm{~mm}$ ）were selected to distribute the monthly rainfalls in the Northeast．Typical results are summa－ rized in Table 4．It can be seen clearly that the monthly rainfalls in the region mostly fall into the first interval $0-10 \mathrm{~mm}$ ， indicating that most of the time，the amount of monthly rainfall is quite small． For intervals with larger amounts，the


Fig. 7 Degree of Rainfall Irregularity

Table 4 Frequency Distribution of Monthly Rainfall

| Station | $\begin{array}{r} \hline 0-10 \\ \mathrm{~mm} \end{array}$ | $\begin{gathered} \hline 10-25 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} \hline 25-50 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} \hline \hline 50-75 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} 75-100 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} \hline \hline 100-200 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} \hline 200-300 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} 300-400 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} \hline 400-500 \\ \mathrm{~mm} \end{gathered}$ | $\begin{gathered} >500 \\ \mathrm{~mm} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Buriram | 0.31 | 0.06 | 0.07 | 0.05 | 0.07 | 0.22 | 0.15 | 0.05 | 0.02 | 0.00 |
| Chaiyaphum | 0.29 | 0.06 | 0.09 | 0.08 | 0.09 | 0.28 | 0.08 | 0.02 | 0.00 | 0.01 |
| Kalasin | 0.32 | 0.06 | 0.08 | 0.07 | 0.04 | 0.19 | 0.12 | 0.08 | 0.02 | 0.02 |
| Khon Kaen | 0.29 | 0.08 | 0.08 | 0.08 | 0.07 | 0.25 | 0.11 | 0.02 | 0.02 | 0.00 |
| Loei | 0.23 | 0.04 | 0.07 | 0.07 | 0.08 | 0.20 | 0.15 | 0.09 | 0.03 | 0.03 |
| Maha | 0.31 | 0.06 | 0.09 | 0.09 | 0.08 | 0.17 | 0.13 | 0.07 | 0.01 | 0.00 |
| Sarakham |  |  |  |  |  |  |  |  |  |  |
| Nakhon | 0.29 | 0.08 | 0.08 | 0.07 | 0.05 | 0.19 | 0.08 | 0.11 | 0.03 | 0.02 |
| Phanom |  |  |  |  |  |  |  |  |  |  |
| Nakhon | 0.29 | 0.06 | 0.08 | 0.11 | 0.08 | 0.24 | 0.09 | 0.03 | 0.01 | 0.01 |
| Ratchasima |  |  |  |  |  |  |  |  |  |  |
| Nong Khai | 0.29 | 0.08 | 0.08 | 0.04 | 0.04 | 0.16 | 0.17 | 0.09 | 0.02 | 0.03 |
| Roi Et | 0.32 | 0.05 | 0.07 | 0.06 | 0.04 | 0.21 | 0.14 | 0.06 | 0.03 | 0.00 |
| Sakhon | 0.30 | 0.06 | 0.10 | 0.05 | 0.06 | 0.19 | 0.15 | 0.07 | 0.02 | 0.01 |
| Nakhon |  |  |  |  |  |  |  |  |  |  |
| Ubon | 0.30 | 0.07 | 0.07 | 0.04 | 0.05 | 0.19 | 0.15 | 0.08 | 0.04 | 0.01 |
| Ratchathani |  |  |  |  |  |  |  |  |  |  |
| Udon Thani | 0.29 | 0.07 | 0.07 | 0.06 | 0.05 | 0.18 | 0.20 | 0.05 | 0.03 | 0.01 |
| Yasothon | 0.35 | 0.06 | 0.07 | 0.03 | 0.08 | 0.19 | 0.12 | 0.08 | 0.02 | 0.01 |

Table 5 Potential Evapotranspiration（mm）

| Station | Apr． | May | Jun． | Jul． | Aug． | Sept． | Oct． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Buriram | 209 | 207 | 181 | 180.5 | 176 | 162.5 | 171 |
| Chaiyaphum | 206 | 204 | 178.5 | 177 | 169 | 150 | 165 |
| Kalasin | 207 | 203 | 175 | 177 | 166 | 155 | 167 |
| Khon Kaen（＊） | 217 | 213 | 182 | 180 | 171 | 159 | 173 |
| Loei ${ }^{(*)}$ | 198 | 197 | 171 | 171 | 162 | 151 | 157 |
| Maha Sarakham | 210 | 208 | 181 | 180 | 172 | 158 | 169 |
| Nakhon Phanom（＊） | 179 | 176 | 143 | 147 | 142 | 140 | 157 |
| Nakhon Ratchasima ${ }^{(*)}$ | 205 | 204 | 182 | 180 | 174 | 160 | 167 |
| Nong Khai | 194 | 191 | 165 | 168 | 158 | 149 | 161 |
| Roi Et ${ }^{(*)}$ | 210 | 208 | 180 | 180 | 171 | 156 | 167 |
| Sakhon Nakhon（＊） | 196 | 189 | 161 | 170 | 157 | 152 | 165 |
| Si Sa Ket | 211 | 206 | 177 | 179 | 172 | 159 | 172 |
| Surin（＊） | 213 | 210 | 180 | 181 | 178 | 165 | 175 |
| Ubon Ratchathani（＊） | 209 | 203 | 174 | 177 | 166 | 153 | 170 |
| Udon Thani ${ }^{(*)}$ | 204 | 202 | 177 | 180 | 167 | 153 | 165 |
| Yasothon | 209 | 205 | 177 | 178 | 168 | 154 | 168 |

Note：Data for stations marked with（＊）were obtained from Mekong Secreteriat（1975）． For other stations，etimated values were obtained by taking the average of values at neighboring provinces．
probability of occurrence becomes less． This is in agreement with the fact that monthly rainfall in the region follows positively skewed distributions such as the leakage law．

For irrigation purposes，the two inter－ vals $100-200 \mathrm{~mm}$ and $200-300 \mathrm{~mm}$ are of important interest（See Table 5）．In the interval $100-200 \mathrm{~mm}$ ，the lowest probability is $9 \%$ ，the highest is $28 \%$ and the average is $20 \%$ for the stations listed in Table 4．In the interval $200-300 \mathrm{~mm}$ ， the lowest probability is $8 \%$ ，the highest is $20 \%$ and the average is $13 \%$ ．For the last two intervals，monthly rainfalls have very low probabilities of occurrence． This result shows that the rainfall at these stations can hardly amount to more than 400 mm per month．

## III Assessment of Water Availability for Irrigation

Using the fact that monthly rainfalls in the Northeast can be fitted very well by the leakage law，an assessment of the availability of water for irrigation purposes in a month can be made by comparing the amount of rainfall cor－ responding to a specified probability with the potential evapotranspiration in that month．Potential evapotranspira－ tion data employed in this analysis are the monthly mean values and these are shown in Table 5.

For a given month，the amount of rain－ fall，$R$ ，corresponding to a probability $p$ can be determined as follows：
$p=$ Probability $(X \leq R)$

$$
\begin{align*}
& =\exp (-a)+\int_{0}^{R} \exp (-a-b x)(a b / x)^{1 / 2} \\
& I_{1}\left[2(a b x)^{1 / 2}\right] d x \tag{9}
\end{align*}
$$

where $X$ is a random variable representing the rainfall in that month, $I_{1}$ is the modified Bessel function of order 1 and $a$ and $b$ are the two parameters of the leakage law. From eq. 9,

$$
\begin{equation*}
\text { if } \quad p \leq \exp (-a), \quad R=0 \tag{10}
\end{equation*}
$$

and if $p>\exp (-a), R$ can be obtained by interpolation. Generally speaking, the potential evapotranspiration indicates the water requirement for irrigation purposes. The ratio, $r$, of rainfall to the potential evapotranspiration therefore represents the portion of water requirement met by rainfall.

For the case $p=0.1$, this ratio was found to be smaller in the dry season (November through March) and larger
during the wet season (April through October). In April, the value of $r$ is less than $25 \%$ for the entire region. In May, most of the region has values for $r$ ranging from $25 \%$ to $50 \%$. Even at this probability, rainfall reaches $150 \%$ of the evapotranspiration in the months of July and August in the extreme northeastern part of the region. Shown in Fig. 8 are the isolines of $r$ for the month of July, expressed in percentages, together with a division of the region into five zones. Thus the portion of water requirement met by rainfall in different parts of the region can be clearly seen.

The amount of available rainfall over each part of the region was evaluated for different return periods by varying


Fig. 8 Isolines of r in percent for $p=0.1$, July
the value of the probability $p$ ．The value of $r$ was computed accordingly，and hence an assessment of water availiability for irrigation purposes was achieved．As predicted，even for high values of $p$ ，the portion of water requirement met by rainfall was found to be very small during the dry season for the whole region，and hence no rainfed irrigation is expected for any part of the Northeast during this period．

The value of $r$ becomes larger when the region becomes wetter，indicating that rain water can meet a higher portion of irrigation demand．However，during the months of August and September， rainfall is overabundant in the north－ eastern and eastern sections of the region even for low values of $p$ ．During these months，with depressions and storms entering the region，attention should be given to appropriate measures for efficient drainage as well as for flood protection in these sections，rather than just be con－ cerned with having enough water for irrigation．

## Summary and Conclusions

In an attempt to provide guidelines for crop scheduling，better cropping patterns and the planning and design of water resources projects in the Northeast， the distribution of monthly rainfall in space and time was investigated in this study．Rainfall data at 56 stations were used in the analysis and from the investi－ gation，the following conclusions can be drawn：
（1）Monthly rainfall sequences in the

Northeast can be represented by periodic－stochastic processes in which the periodic parts consist mainly of six constituents cor－ responding to the following six periods：12，6，4，3， 2.4 and 2 months．
（2）Rainfall sequences in successive months at a station have very low values for the serial correlation coefficient，indicating that rainfall in a month is independent of rainfall in other months at the same station．
（3）Monthly rainfall sequences in the region are fitted very well by the leakage law．Sequences without zero values are also fitted well by the lognormal and gamma dis－ tributions．
（4）Monthly rainfalls in the region vary greatly from month to month，resulting in high values for the degree of irregularity， ranging from $45 \%$ to $70 \%$ ．
（5）Rainfalls in a month fluctuate greatly from year to year．
（6）The maximum monthly rainfall occurs in August or September and the minimum，which is al－ most nil，occurs in December or January．
（7）The eastern and northeastern sections of the region generally receive the most and the least amounts of rainfall in the rainy and dry seasons，respectively．
（8）The ratio of rainfall at a specified probability level to the potential
evapotranspiration in a month varies from month to month. It has low values in the dry season even at high probability levels and high values in the rainy season even at low probability levels.

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[^0]:    * Division of Computer Applications, Asian Institute of Technology, Bangkok, Thailand
    ** Division of Water Resources Engineering, Asian Institute of Technology, Bangkok, Thailand

