京都大学
KYOTO UNIVERSITY

| Title | Effect of Time Duration and Intrinsic Features for English <br> Phoneme Recognition |
| :---: | :--- |
| Author（s） | Ariki，Y asuo |
| Citation | 音声科学研究＝Studia phonologica（1990），24：70－82 |
| Issue Date | 1990 |
| URL | http：／hdl．handle．net／2433／52485 |
| Right | Departmental Bulletin Paper |
| Type | publisher |
| Textversion |  |

# Effect of Time Duration and Intrinsic Features for English Phoneme Recognition 

Yasuo Ariki

## Summary

This paper describes methods to improve the performance of English phoneme recognition from linguistic view points．The methods include exploiting time dura－ tion information in hidden Markov model（HMM），intrinsic feature space for vowel． The time duration constraint imposed on states of the phoneme HMM can improve its recognition rate significantly for phoneme data in continuous pseech．As intrin－ sic feature spaces for vowel，formants and the time derivative are employed．They improve the phoneme recognition rate considerably compared with the commonly used LPC cepstral coefficients．

## I．Introduction

The speech signal exhibits variability in both time duration and spectrum even by the same speaker．This variability has been causing difficulty in the realisation of speech recognition by machine．Hidden Markov modelling（HMM）was propos－ ed to absorb the variability，by virture of its computational time alignment capabi－ lity coupled with use of spectral probability distribution functions（pdf）［1］．The HMM made it feasible to recognise continuous speech with large vocabulary by modelling sub－word speech units．The subword models can be easily concatenat－ ed into word models owing to the probabilistic representation of the HMM［2］［3］ ［4］．

Using HMM sub－word modelling as bases for experimentation，we investigat－ ed several methods of increasing its performance．In this paper following two me－ thods to improve phoneme recognition rate are described：
（1）Incorporation of time duration modelling into the phoneme HMM．
（2）Employment of specific feature space intrinsic to vowels and consonants．
The HMM can be thought as a time varying information source which can be modelled as Markov process with the pdf at each state．Speech data are used to estimate the pdf at each state and state transition probability of the Markov model． However，it lacks information about how long the speech data can be likely to stay at each state［5］［6］．In this paper，we formalise the time duration modelling in the HMM and show the recognition improvement of the phoneme in continuous speech，

[^0]compared to the conventional HMM without time duration [7].
In phoneme recognition by HMM, a single acoustic feature space, such as LPC cepstral coefficients, has been employed so far, irrespective of the phoneme classes: consonants or vowels. However, their features may be well represented in intrinsic feature space, since vowels and consonants are produced through different vocal mechanisms. For example, consonants can be characterised largely by spectral envelope and their temporal movement. On the other hand, vowels can be characterised by formant frequencies rather than spectral envelope. In this paper we demonstrate considerable improvement of the vowel recognition by employing formant frequency instead of LPC cepstral coefficients [8].

In order to formalise the time duration modelling in the HMM, we describe EM algorithm for parameter estimation of the HMM in section II, then its application to the discrete HMM is described in section III and IV. Section V formalises the time duration HMM. Phoneme recognition using the discrete HMM and the effect of time duration HMM are described in section VI and VII respectively. Section VIII describes the experimental results of phoneme recognition in intrinsic feature space.

## II. EM Algorithm

We suppose here that observed speech sample $x$ comes out according to probabilistic structure $y$ with the probability density of $f(x, y)$. Information such as from which probabilistic structure (class, state) a data sample $x$ comes is unobservable and only the speech sample $x$ is observed. Observable data are called incomplete data because they are missing the unobservable data $y$, and data composed of observable and unobservable data are called complete data. The purpose of the EM algorithm is to maximise the log-likelihood of incomplete data, by iteratively maximising the expectation of log-likelihood of complete data. The name of the EM algorithm comes from $E$ for expectation and $M$ for maximisation. It can be said that the EM algorithm is a maximum likelihood estimation method, but its computation is less complex than the conventional maximum likelihood estimation method.

Let $L(x, \bar{\lambda})$ denote the log-likelihood of the observed speech sample $x$. Here $\bar{\lambda}$ is the parameters of the probabilistic structure $y$. The $\log$-likelihood $L(x, \bar{\lambda})$ is decomposed into two functions; $Q(\lambda, \bar{\lambda})$ and $H(\lambda, \bar{\lambda})$ as follows.

$$
\begin{equation*}
L(x, \bar{\lambda})=Q(\lambda, \bar{\lambda})-H(\lambda, \bar{\lambda}) \tag{1}
\end{equation*}
$$

where $\lambda$ and $\bar{\lambda}$ indicate the parameters of the probabilistic sturcture $y$ already estimated and to be estimated at this iteration step respectively. The $H$ function has the property that $H(\lambda, \bar{\lambda}) \leq H(\lambda, \lambda)$, then the log-likelihood $L$ increases if the function $Q$ increases for the newly estimated parameters $\bar{\lambda}$. The function $Q$ is
expressed as follows:

$$
\begin{equation*}
Q(\lambda, \bar{\lambda})=\frac{1}{f(x \mid \lambda)} \sum_{y} f(x, y \mid \lambda) \log f(x, y \mid \bar{\lambda}) \tag{2}
\end{equation*}
$$

The procedure of the EM algorithm can be summarised in the following way.

1. Choose an initial estimate $\lambda$.
2. E-step. Compute $Q(\lambda, \bar{\lambda})$ based on the given $\lambda$.
3. M-step. Choose $\bar{\lambda} \in \underset{\lambda}{\operatorname{argmax}} Q(\lambda, \bar{\lambda})$. Here, $\underset{\bar{\lambda}}{\operatorname{argmax}} Q(\lambda, \bar{\lambda})$ denotes the set of values $\bar{\lambda}$ which maximise $Q(\lambda, \bar{\lambda})$.
4. Set $\lambda=\bar{\lambda}$, repeat from step 2 until convergence.

The $Q$ function expressed in $E Q .(2)$ is concerned with a single observed incomplete data $x_{k}$. Applying it to multiple observed incomplete data $X=\left\{x_{1}, \cdots, x_{N}\right\}$, the $Q$ function is extended to:

$$
\begin{align*}
Q(\lambda, \bar{\lambda}) & =\sum_{k=1}^{N} Q_{k}(\lambda, \bar{\lambda}) \\
& =\sum_{k=1}^{N} \sum_{y} \frac{f\left(x_{k}, y \mid \lambda\right)}{f\left(x_{k} \mid \lambda\right)} \log f\left(x_{k}, y \mid \bar{\lambda}\right) \tag{3}
\end{align*}
$$

where $N$ denotes the number of observed data.
The EM algorithm is used in applications which permit easy maximisation of the $Q$-function instead of maximising $L(x, \bar{\lambda})$ directly. In such applications, the $M$-step maximisation of $Q(\lambda, \bar{\lambda})$ is easily carried out.

## III. Appligation of EM Algorithm to HMM

H dden Markov modelling is the probabilistic modelling to deal with a time sequence of speech data. Stable state of the speech data is modelled by one simple probabilistic model and the time sequence is modelled by the transition from one probabilistic model to anther model.[7] Let $X=x_{1} \cdots x_{t} \cdots x_{T}$ denote a time sequnece of speech data and $S=s_{1} \cdots s_{t} \cdots s_{T}$ denote a time sequence of stable states of the model. The $x_{t}$ is referred to as frame data hereafter. The complete data is expressed as $(X, S)$. In order to apply the EM algorithm to the HMM, it is necessary to formalise the probability density function (pdf) of the complete data. Then the $Q$ function expressed in $E Q$.(2) can be applied. The pdf of the complete data is expressed as:

$$
\begin{align*}
& f(X, S \mid \lambda)=f\left(x_{1} \cdots x_{t} \cdots x_{T}, s_{1} \cdots s_{t} \cdots s_{T} \mid \lambda\right) \\
&=f\left(x_{1}, s_{1} \mid \lambda\right) \cdots f\left(x_{t}, s_{t} \mid X_{1}^{t-1}, S_{1}^{t-1}, \lambda\right)  \tag{4}\\
& \cdots f\left(x_{T}, s_{T} \mid X_{1}^{T-1}, S_{1}^{T-1}, \lambda\right)
\end{align*}
$$

where $X_{1}^{t-1}$ and $S_{1}^{t-1}$ denote the partial sequence from time 1 to $t-1$ of the speech data $X$ and state sequence $S$. Here, we call $f\left(x_{t}, s_{t} \mid X_{1}^{t-1}, S_{1}^{t-1}, \lambda\right)$ conditional pdf of the complete data at time $t$. We introduce following hypothesis into the model.

The conditional pdf of the complete data at time $t$ does not depend on the previous frame data sequence $X_{1}^{t-1}$, but only depends on the previous stable state $s_{t-1}$ Under this hypothesis, the conditional pdf of the complete data at time $t$ is simplified as follows:

$$
\begin{align*}
& f\left(x_{t}, s_{t} \mid X_{1}^{t-1}, S_{1}^{t-1}, \lambda\right)=f\left(x_{t}, s_{t} \mid s_{t-1}, \lambda\right) \\
& \quad=\operatorname{Pr}\left(s_{t} \mid s_{t-1}, \lambda\right) f\left(x_{t} \mid s_{t-1}, s_{t}, \lambda\right) \tag{5}
\end{align*}
$$

We introduce the following terms to make the model more clear.

$$
\begin{array}{llll}
\text { Transition probability } & a_{s_{t-1} s_{t}}=\operatorname{Pr}\left(s_{t} \mid s_{t-1}, \lambda\right) & & (2 \leq t \leq T) \\
\text { initial probability } & \pi_{s_{1}} & =\operatorname{Pr}\left(s_{1} \mid \lambda\right) & (t=1)  \tag{6}\\
\text { output probability } & b_{s_{t-1} s_{t}}\left(x_{t}\right) & =f\left(x_{t} \mid s_{t-1}, s_{t}, \lambda\right) & (1 \leq t \leq T)
\end{array}
$$

The output probability $b_{s_{t-1} s_{t}}\left(x_{t}\right)$ is the probability to output the data $x_{t}$ at the transition from the state $s_{t-1}$ to $s_{t}$. If all the output probabilities from any state to the state $s_{t}$ are tied, the output probability is expressed as:

$$
\begin{equation*}
b_{s_{t}}\left(x_{t}\right)=f\left(x_{t} \mid s_{t}, \lambda\right) \quad(1 \leq t \leq T) \tag{7}
\end{equation*}
$$

Then the conditional pdf of the complete data at time $t$ is expressed as:

$$
f\left(x_{t}, s_{t} \mid X_{1}^{t-1}, S_{1}^{t-1}, \lambda\right)= \begin{cases}a_{s_{t}-1 s_{t}} b_{s_{t}}\left(x_{t}\right) & (2 \leq t \leq T)  \tag{8}\\ \pi_{s_{1}} b_{s_{1}}\left(x_{1}\right) & (t=1)\end{cases}
$$

From the EQ.(4) and EQ.(8), the pdf of the complete data $f(X, S \mid \lambda)$ is obtained as:

$$
\begin{align*}
& f(X, S \mid \lambda)=\pi_{s_{1}} b_{s_{1}}\left(x_{1}\right) \prod_{t=2}^{T} a_{s_{t-1} s_{t}} b_{s_{t}}\left(x_{t}\right) \\
& \quad=\pi_{s_{1}} \prod_{t=1}^{T-1} a_{s_{t} s_{t+1}} \prod_{i=1}^{T} b_{s_{t}}\left(x_{t}\right) \tag{9}
\end{align*}
$$

By substituting the EQ.(9) to the EQ.(2), the HMM parameters are iteratively obtained by the EM algorithm under the hypothesis of data independence and one state dependency (Markov chain).

## IV. Discrete HMM

In discrete HMM, frame data $x_{t}$ in speech data $X$ is quantised into finite set of repersentatives, called codewords. The process of quantisation is called vector quantisation. In the application of the EM algorithm to the quantised speech data $O=o_{1} \cdots o_{t} \cdots o_{T}$, the pdf of the complete data ( $O, S$ ) is substituted into the EQ.(2). Using the notation of the initial probability $\pi_{s_{1}}$, state transition probability $a_{s_{t} s_{t+1}}$ and output probability $b_{s_{t}}\left(o_{t}\right)$, the $\log$-likelihood ( $\log \mathrm{pdf}$ ) of the complete data is expressed as follows, applying log operation to the EQ.(9):

$$
\begin{equation*}
\log \operatorname{Pr}(O, S \mid \bar{\lambda})=\log \bar{\pi}_{s_{1}}+\sum_{t=1}^{T-1} \log \bar{a}_{s_{t} s_{t}+1}+\sum_{t=1}^{T} \log \bar{b}_{s_{t}}\left(o_{t}\right) \tag{10}
\end{equation*}
$$

Then $Q(\lambda, \bar{\lambda})$ function is expressed as:

$$
\begin{align*}
& Q(\lambda, \bar{\lambda})=\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \operatorname{Pr}(O, S \mid \lambda) \log \bar{\pi}_{s_{1}} \\
& \quad+\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \operatorname{Pr}(O, S \mid \lambda) \sum_{t=1}^{T-1} \log \bar{a}_{s_{t} s_{t+1}}  \tag{11}\\
& \quad+\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \operatorname{Pr}(O, S \mid \lambda) \sum_{t=1}^{T} \log \bar{b}_{s_{t}}\left(o_{t}\right)
\end{align*}
$$

By maximising the first term of the right hand side in terms of $\bar{\pi}_{s_{1}}$, the initial probability estimation is obtained.

$$
\begin{equation*}
\bar{\pi}_{\boldsymbol{i}}=\operatorname{Pr}\left(s_{1}=i \mid O, \lambda\right)=r_{1}(i) \tag{12}
\end{equation*}
$$

By maximising the second term of the right hand side in terms of $\bar{a}_{s t_{t+1}}$, the transition probability estimation is obtained.

$$
\begin{equation*}
\bar{a}_{i j}=\frac{\sum_{t=1}^{T-1} \operatorname{Pr}\left(s_{t}=i, s_{t+1}=j \mid O, \lambda\right)}{\sum_{j} \sum_{t=1}^{T-1} \operatorname{Pr}\left(s_{t}=i, s_{t+1}=j \mid O, \lambda\right)}=\frac{\sum_{t=1}^{T-1} r_{t}(i, j)}{\sum_{j} \sum_{t=1}^{T-1} r_{t}(i, j)} \tag{13}
\end{equation*}
$$

By maximising the third term of the right hand side in terms of $\bar{b}_{s_{t}}\left(o_{t}\right)$, the output probability estimation is obtained.

$$
\begin{equation*}
\bar{b}_{i}(k)=\frac{\sum_{t \theta_{t}=v_{k}} P r\left(s_{t}=i \mid O, \lambda\right)}{\sum_{t} \operatorname{Pr}\left(s_{t}=i \mid O, \lambda\right)}=\frac{\sum_{t \in o_{t}=o_{k}} r_{t}(i)}{\sum_{t} r_{t}(i)} \tag{14}
\end{equation*}
$$

where $v_{k}$ is the k -th codeword. $\gamma_{t}(i)=\operatorname{Pr}\left(s_{t}=i \mid O, \lambda\right)$ is the probability that state is $i$ at time $t$ after having observed speech data $O$, then;

$$
\begin{equation*}
r_{t}(i)=\alpha_{t}(i) \beta_{t}(i) / \operatorname{Pr}(O \mid \lambda) \tag{15}
\end{equation*}
$$

$\alpha_{t}(i), \beta_{t}(i)$ are called forward probability and backward probability respectively, and expressed as followed:

$$
\begin{align*}
& \alpha_{t}(i)=\sum_{j} \alpha_{t-1}(j) a_{j i} b_{i}\left(o_{t}\right)  \tag{16}\\
& \beta_{t}(i)=\sum a_{i j} \beta_{t+1}(j) b_{j}\left(o_{t+1}\right) \tag{17}
\end{align*}
$$

$r_{t}(i, j)=\operatorname{Pr}\left(s_{t}=i, s_{t+1}=j \mid O, \lambda\right)$ is the transition probability from the state $i$ to the state $j$ at time $t$ after having observed the speech data $O$ and is expressed as followed:

$$
\begin{equation*}
r_{t}(i, j)=\alpha_{t}(i) a_{i j} \beta_{t+1}(j) b_{j}\left(o_{t+1}\right) / \operatorname{Pr}(O \mid \lambda) \tag{18}
\end{equation*}
$$

## V. Time Duration Modelling

In a basic HMM, the probability that speech data can be produced from one state decreases exponentially with time $t$ according to the expression of $p(1-p)^{t}$, where the $p$ is a transition probability from the state to the next state. This does not present the true property of the state because the short duration is always preferred. Ideally, there should be more representative limits on duration time, preventing both short durations as well as long durations in the state. This types of time duration probability can be modelled by a Gaussian distribution.

The conventional discrete HMM, whose output probability is computed on vector quantised codewords, can be extended to use time duration probabilities which are also represented in discrete form. The HMM parameters such as transition probability $\bar{a}_{i j}$, output probability $\bar{b}_{j}(k)$, and time duration probability $\bar{d}_{j}(\tau)$ can be directly obtained from the EM algorithm. [9]

Let $O=o_{1} \cdots o_{t} \cdots o_{T}, S=s_{1} \cdots s_{k} \cdots s_{N}$ and $D=\pi_{1} \cdots \pi_{k} \cdots \tau_{N}$ denote the quantised speech data, state sequence and time duration sequence respectively. The states included in the state sequence are different each other, unlike the discrete HMM without time duration. Then, the state $s_{k}$ denotes the k -th state in the state sequence, not the state at time k. The $b_{s_{k}}\left(o_{t}\right)$ is the probability that the frame data $o_{t}$ is produced from the state $s_{k}$. The $a_{s_{k} s_{k+1}}$ and $\pi_{s_{k}}$ is the transition probability and initial probability defined in the same way as discrete HMM. The $d_{k}(\tau)$ is the probability that the state $s_{k}$ is occupied for duration $\tau$. Notation $t_{k}$ is used to present the starting time of the k-th state so that the pair $\left(t_{k}, \tau_{k}\right)$ denotes the time information at the k-th state. Using these notations, the pdf of the complete data $(O, S, D)$ is expressed as:

$$
\begin{align*}
& \operatorname{Pr}(O, S, D \mid \lambda)=\operatorname{Pr}\left(O_{t_{1}^{1} t_{1}+\tau_{1}-1}, s_{k}, \tau_{1} \mid \lambda\right) \\
& \quad \cdots \operatorname{Pr}\left(O_{t_{k}^{k}+\tau_{k} t^{-1}}^{t_{k}}, s_{k}, \tau_{k} \mid \lambda, O_{1}^{t_{k}-1}, s_{1}^{k-1}, t_{k}-1\right)  \tag{19}\\
& \quad \cdots \operatorname{Pr}\left(O_{t_{N}}^{T}, s_{N}, \tau_{N} \mid \lambda, O_{1}^{t} N^{-1}, S_{1}^{N-1}, t_{N}-1\right)
\end{align*}
$$

In the same way as the discrete HMM , we call $\operatorname{Pr}\left(O_{t_{k} t_{k}+\tau_{k}-1}, s_{k}, \tau_{k} \mid \lambda, O_{\left.1^{k}{ }^{-1}, s_{1}^{k-1}, t_{k}-1\right) ~}^{\text {a }}\right.$, the conditional pdf of the complete data at the state $s_{k}$. Under the assumption of data independency, one previous state dependency, and absolute time independency, the conditional pdf of the complete dats at the state $s_{k}$ is simplified as follows:

$$
\begin{align*}
& \operatorname{Pr}\left(O_{\left.t_{k}^{t_{k}+\tau_{k}+1}, s_{k}, \tau_{k} \mid \lambda, O_{1}^{t_{k}-1}, s_{1}^{k-1}, t_{k}-1\right)}^{\quad=\operatorname{Pr}\left(s_{k} \mid \lambda, s_{k-1}\right) \operatorname{Pr}\left(O_{t_{k}^{k}}^{t_{k}+\tau_{k}-1} \mid \lambda, s_{k-1}, s_{k}\right) \operatorname{Pr}\left(\tau_{k} \mid \lambda, s_{k-1}, s_{k}\right)}\right.
\end{align*}
$$

We introduce the following terms to make the model more clear.

| Transition probability | $a_{s_{k-1} s_{k}}$ | $=\operatorname{Pr}\left(s_{k} \mid s_{k-1}, \lambda\right)$ | $(2 \leq k \leq T)$ |
| :--- | :--- | :--- | :--- |
| initial probability | $\pi_{s_{1}}$ | $=\operatorname{Pr}\left(s_{1} \mid \lambda\right)$ | $(k=1)$ |
| output probability | $b_{s_{k}}\left(o_{t_{k}+n-1}\right)=\operatorname{Pr}\left(o_{t_{k}+n-1} \mid s_{k}, \lambda\right)$ | $(1 \leq k \leq N)\left(1 \leq n \leq \tau_{k}\right)$ |  |
| duration probability | $d_{s_{k}}\left(\tau_{k}\right)$ | $=\operatorname{Pr}\left(\tau_{k} \mid s_{k-1}, s_{k}, \lambda\right)$ | $(1 \leq k \leq N) \quad$ (21) |

Then the log-likelihood of the complete data is expressed as:

$$
\begin{align*}
& \log \operatorname{Pr}(O, S, D \mid \lambda)=\log \pi_{s_{1}}+\sum_{k=1}^{N} \sum_{n=1}^{\tau_{k}} \log b_{s_{k}}\left(o_{t_{k}+n-1}\right) \\
& \quad+\sum_{k=1}^{N} \log d_{s_{k}}\left(\tau_{k}\right)+\sum_{k=1}^{N-1} \log a_{s_{k} s_{k+1}} \tag{22}
\end{align*}
$$

Then $Q$ function is expressed as:

$$
\begin{align*}
& Q(\lambda, \bar{\lambda}) \\
& \quad=\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \sum_{D} \operatorname{Pr}(O, S, D \mid \lambda) \log \operatorname{Pr}(O, S, D \mid \bar{\lambda}) \\
& \quad=\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \sum_{D} \operatorname{Pr}(O, S, D \mid \lambda) \log \bar{\pi}_{s_{1}} \\
& \quad+\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \sum_{D} \operatorname{Pr}(O, S, D \mid \lambda) \sum_{k=1}^{N-1} \log \bar{a}_{s_{k} s_{k+1}} \\
& \quad+\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \sum_{D} \operatorname{Pr}(O, S, D \mid \lambda) \sum_{k=1}^{N} \sum_{n=1}^{\tau_{k}} \log \bar{b}_{s_{k}}\left(o_{t_{k}+n-1}\right) \\
& \quad+\frac{1}{\operatorname{Pr}(O \mid \lambda)} \sum_{S} \sum_{D} \operatorname{Pr}(O, S, D \mid \lambda) \sum_{k=1}^{N} \log \bar{d}_{s_{k}}\left(\tau_{k}\right) \tag{23}
\end{align*}
$$

By maximising the first term of the right hand side in terms of $\bar{\pi}_{s_{1}}$, the initial probability estimation is obtained.

$$
\begin{equation*}
\bar{\pi}_{i}=\operatorname{Pr}\left(s_{1}=i \mid O, \lambda\right)=\sum_{\tau} r_{0, \tau}(i) \tag{24}
\end{equation*}
$$

By maximising the second term of the right hand side in terms of $a_{s_{k^{s}}{ }^{s+1}}$, the transition probability estimation is obtained.

$$
\begin{equation*}
a_{i j}=\frac{\sum_{\tau} \sum_{t} r_{t, \tau}(i, j)}{\sum_{j} \sum_{\tau} \sum_{t} r_{t, \tau}(i, j)} \tag{25}
\end{equation*}
$$

By maximising the third term of the right hand side in terms of $\bar{b}_{s_{k}}\left(o_{t_{k}+n-1}\right)$, the output probability estimation is obtained.

$$
\begin{equation*}
\bar{b}_{i}(l)=\frac{\sum_{t} \sum_{\tau} r_{t, \tau}(i) c_{t, \tau}(l)}{\sum_{l} \sum_{t} \sum_{\tau} r_{t, \tau}(i) c_{t, \tau}(l)}=\frac{\sum_{t} \sum_{\tau} r_{t, \tau}(i) c_{t, \tau}(l)}{\sum_{t} \sum_{\tau} r_{t, \tau}(i) \tau} \tag{26}
\end{equation*}
$$

where $c_{t, \tau}(k)$ is the number of vector quantised output symbols $v_{k}$ from time $t+1$ to $t+\tau$. The $r_{t, \tau}(i, j)$ is the time duration probability that speech data can be produced from the state $s_{j}$ for duration $\tau$, after transition from the state $s_{i}$ to $s_{j}$ at time $t$.

By maximising the fourth term of the right hand side in terms of $\bar{d}_{s_{k}}\left(\tau_{k}\right)$, the duration probability estimation is obtained.

$$
\begin{equation*}
\bar{d}_{i}(\tau)=\frac{\sum_{t} r_{t, \tau}(i)}{\sum_{\tau} \sum_{t} r_{t, \tau}(i)} \tag{27}
\end{equation*}
$$

Here, $r_{t, \tau}(i, j)$ is the probability that the state transition occurred from state $i$ to state $j$ at time $t$ and the state $j$ is occupied for duration $\gamma$, after having observed speech data $O$. It is calculated using the following expression:

$$
\begin{align*}
& r_{t, \tau}(i, j)=\sum_{k=1}^{N-1} \operatorname{Pr}\left(s_{k}=i, s_{k+1}=j, t_{k+1}=t, \tau_{k+1}=\tau \mid O, \lambda\right) \\
& \quad=\alpha_{t-1}(i) a_{i j} d_{j}(\tau) \prod_{n=1}^{\tau} b_{j}\left(o_{t+n-1}\right) \beta_{t+\tau-1}(j) \tag{28}
\end{align*}
$$

and

$$
\begin{equation*}
r_{t, \tau}(j)=\sum_{i} r_{t, \tau}(i, j) \tag{29}
\end{equation*}
$$

The $\alpha_{t}(j)$ and $\beta_{t}(i)$ is the forward probability and backward probability. They are computed by the following expression.

$$
\begin{equation*}
\alpha_{t}(j)=\sum_{\tau} \sum_{\substack{i \\ i \neq j}} \alpha_{t-\tau}(i) a_{i j} d_{j}(\tau) \prod_{n=1}^{\tau} b_{j}\left(o_{t-\tau+n}\right) \tag{30}
\end{equation*}
$$

and

$$
\begin{equation*}
\beta_{t}(i)=\sum_{\tau} \sum_{\substack{j \\ j \neq i}} a_{i j} d_{j}(\tau) \prod_{n=1}^{\tau} b_{j}\left(o_{t+n}\right) \beta_{t+\tau}(j) \tag{31}
\end{equation*}
$$

In the case where uniform probability distribution is used as the initial time duration probability for $d_{j}(\tau)$ and the final probability is estimated this results in the Fergusson model.[5] In the case where a Gaussian probability distribution is used, this is termed he:e as the Gaussian model. The Gaussian model can prevent errors produced by short token durations or long token durations by virtue of its statistical nature.

## VI. Phoneme Regognition Experiment

As a guide line for comparison, phoneme recognition experiments were carri-
Table 1, Conditions for acoustic analysis (AA), vector quantisation (VQ) and Hidden Markov Modelling (HMM).

| AA | Sampling frequency | 16 kHz |
| :--- | :--- | :--- |
|  | High-pass filter | $x_{t}-0.97 x_{t-1}$ |
|  | Feature parameter | LPC cepstrum (20th) |
|  | Frame length | 20 ms |
|  | Frame shift | 5 ms |
|  | Window type | Hamming window |
| VQ | Codebook size | Distance measure |
|  | Data amount | 256 codewords |
|  | Number of states | Euclidean distance |
| HMM | Learning method | 100 frames/phoneme |
|  | Recognition method | 3 states |
|  |  | Baum-Welch Algorithm |
|  |  |  |

ed out using basic discrete HMM without time duration modelling. The experi mental speech data used here consisted of 98 sentences which were spoken twice by a single speaker: these were hand-labelled to a phoneme level. Half of the sentences were used as training data and the remaining half were used for testing. The conditions of the acoustic analysis, vector quantisation and Hidden Markov Modelling are shown in Table 1.

The phoneme recognition results are shown in Table 2, organised by phoneme:
Table 2. Phoneme recognition results by HMM without time duration modelling.

| Phoneme |  | Rate (\%) | Phoneme |  | Rate (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| @ | (191) | 53.4 | n | (111) | 64.9 |
| 1 | (96) | 34.4 | 1 | (80) | 56.3 |
| ii | (68) | 79.4 | t | (76) | 84.2 |
| ai | (56) | 73.2 | m | (72) | 70.8 |
| a | (44) | 31.8 | r | (58) | 89.7 |
| ei | (43) | 46.5 | d | (60) | 60.0 |
| uu | (47) | 72.3 | w | (53) | 77.4 |
| ou | (38) | 42.1 | y | (47) | 91.5 |
| e | (38) | 5.3 | p | (47) | 91.5 |
| uh | (33) | 36.4 | z | (41) | 73.2 |
| oo | (32) | 43.8 | b | (39) | 89.7 |
| o | (21) | 47.6 | k | (36) | 61.1 |
| aa | (15) | 20.0 | s | (29) | 96.6 |
| u | (10) | 10.0 | ng | (27) | 25.9 |
| au | (8) | 12.5 | ch | (27) | 63.0 |
| i@ | (6) | 66.7 | jh | (26) | 61.5 |
| @@ | (5) | 0.0 | g | (24) | 45.8 |
| u@ | (3) | 0.0 | dh | (23) | 43.5 |
| oi | (2) | 50.0 | v | (23) | 56.5 |
| e@ | (3) | 0.0 | f | (19) | 89.5 |
|  |  |  | th | (19) | 73.7 |
|  |  |  | sh | (18) | 38.9 |
|  |  |  | h | (17) | 35.3 |
|  |  |  | zh | (17) | 23.5 |
| Total | (759) | 59.8 (\%) |  |  |  |

consonants on the right hand side, vowels on the left hand side. The number in the parentheses is the number of the data tokens used in training and testing. The recognition rate up to the first candidate was $59.8 \%$ as shown in Table 2. The recognition rate up to the second, third, fourth and fifth candidates were $76.3 \%$, $84.3 \%, 88.6 \%$ and $91.4 \%$ respectively.

## VII. Time Duration Effect

Phoneme recognition experiments were carried out by using discrete HMM with time duration modelling described in section V. In this experiment, we applied following, three kinds of time duration modelling according to the type of initial time duration probability $d_{j}(\tau)$.
(1) Fergusson model

The initial time duration probability $d_{j}(\tau)$ is set to be uniform distribution, and the EM algorithm is applied to estimate the parameters. In the Fergusson model, the time duration is limited up to 64 frames.
(2) Gaussian model

The initial time duration probability $d_{j}(\tau)$ is set to be Gaussian distribution, whose initial mean and standard deviation are computed from the training data. In the EM algorithm, time duration probabilities are updated and remodelled by Gaussian distributions at each iteration.

## (3) Enhanced Graussian Model

The time duration probability computed in (2) is raised to the fifth power after setting the highest probability equal to unity only in the decoding process.

The result is shown in Table 3. The enhanced Gaussian model showed the highest phoneme recognition rates of $68.0 \%$. The main reason for this increase is attributable to the time duration constraint which enables the most probable path to be optimised in the Viterbi decoding algorithm.

The recognition rates of vowels, consonants and total phonemes by time duration modelling are listed in Table 4, together with the result without time duration

Table 3, Comparison of discrete time duration modelling in phoneme recognition (\%).

| Without time | Fergusson | Gaussian | Enhanced Gaussian |
| :---: | :---: | :---: | :---: |
| 59.8 | 61.2 | 62.8 | 68.0 |

Table 4. Phoneme recognition results by time duration modelling (\%).

|  | Vowel | Consonant | Total phoneme |
| :---: | :---: | :---: | :---: |
| Without time | 54.3 | 77.5 | 59.8 |
| Time duration | 63.9 | 80.2 | 68.0 |

modelling. In vowel and consonant recognition, separate codebooks were used. The time duration modelling increased vowel recognition rates by $9.6 \%$. It is directly related to the total phoneme recognition rate. On the other hand, consonant accuracy increased by only $2.7 \%$. The improvement of vowel recognition is attributed to the successful allocation of the respective states of vowel HMMs to stationary part of the vowel data by the time duration constraint.

## VIII. Feature Subspace Effect

In Table 4, it can be seen that vowel recognition rate is $63.9 \%$ and is still lower than consonant rate by $16.3 \%$, though it was improved by time duration modelling. In order to improve the vowel recognition rate still further, the most suitable feature space should be prepared for vowel recognition, instead of using LPC cepstral coefficients which are commonly used for both vowel and consonant recognition.

The formants are the most representative feautres for vowel because the resonance at the vocal tract causes the formants and produces the vowel sound. Vowel recognition was carried out using three formant frequencies: the first, second and third formants [10].

Table 5 shows the details of vowel recognition in the following feature spaces:
(1) Formant (F).
(2) Mel-formant (MF) which is the formant frequency after mel-transformation and has the effect to increase the frequency resolution around 1 kHz .
(3) Mel-formant and its time derivative (MFD) which includes the mel-formant and its frequency derivatives between consecutive frames ( 5 ms ).
In the Table, LPG cepstral coefficients with and without time duration modelling are listed for comparison. From the tablel time duration modelling is effective for the almost all vowels, and formant representation is most effective for short vowels like $/ \mathrm{a} / \mathrm{l} / \mathrm{e} /$ and $/ \mathrm{o} /$. The table also shows that the mel-formant representation is effective for diphthong and long vowels like/ai/, /ei/ and/ou/. The highest recognition rate $75.4 \%$ is achieved by the mel-formant and its derivative, mainly due to the non-linear transformation of the mel-frequency and its dynamic features.

## IX. Conclusion

Two methods to improve the HMM-based phoneme recognition were described considering EM algorithm and its application to ordinary basic discrete HMM, the time duration modelling in the HMM frame work is analysed and formalised. The experimental results based on the formalisation of time duration significantly improved the phoneme recognition rate. Formants play an important role compared to the LPC coefficients in vowel recognition and showed considerable improvement of vowel recognition. The further work will be to integrate the recognition

Table 5. Detailed results of vowel recognition (\%).

| Phoneme |  | CEP | $\begin{aligned} & \text { CEP } \\ & \text { time } \end{aligned}$ | $\underset{\text { time }}{\mathrm{F}}$ | $\underset{\text { time }}{\text { MF }}$ | MFD time |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | (191) | 58.1 | 75.4 | 62.8 | 60.7 | 70.7 |
| i | (96) | 52.1 | 52.1 | 53.1 | 58.2 | 66.7 |
| ii | (68) | 82.4 | 88.2 | 91.2 | 88.2 | 91.2 |
| ai | (56) | 85.7 | 94.6 | 92.9 | 98.2 | 100.0 |
| a | (44) | 36.4 | 38.6 | 86.4 | 86.4 | 90.9 |
| ei | (43) | 58.1 | 74.4 | 76.7 | 90.7 | 90.7 |
| uu | (47) | 70.2 | 80.9 | 83.0 | 85.1 | 85.1 |
| ou | (38) | 36.8 | 63.2 | 81.6 | 86.8 | 92.1 |
| e | (38) | 7.9 | 15.8 | 44.7 | 52.6 | 52.6 |
| uh | (33) | 30.3 | 36.4 | 42.4 | 54.6 | 51.5 |
| oo | (32) | 90.6 | 93.8 | 93.8 | 96.9 | 96.9 |
| o | (21) | 52.4 | 57.1 | 81.0 | 90.5 | 90.5 |
| aa | (15) | 13.3 | 13.3 | 66.7 | 66.7 | 46.7 |
| u | (10) | 0.0 | 0.0 | 10.0 | 20.0 | 0.0 |
| au | (8) | 12.5 | 12.5 | 25.0 | 25.0 | 12.5 |
| i@ | (6) | 33.3 | 33.3 | 66.7 | 66.7 | 66.7 |
| @ @ | (5) | 0.0 | 20.0 | 20.0 | 40.0 | 40.0 |
| u@ | (3) | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| oi | (2) | 50.0 | 50.0 | 50.0 | 0.0 | 0.0 |
| e@ | (3) | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Total | (759) | 54.3 | 63.9 | 68.9 | 71.8 | 75.4 |

CEP: Cepstral coefficients of 20th order.
F: Formant.
MF: Mel-formant.
MFD: Mel-formant and its derivative.
time: With time duration.
( ): The number of tokens.
results of vowel and consonants. Also the application of time duration HMM to phoneme or word spotting will be left for further work.

## References

[1] F. Jelinek, "Continuous Speech Recognition by Statistical Methods," Proc. IEEE, Vol. 64, No. 4, pp. 532-556, 1976.
[2] A. Averbuch, et al., "Experiments with the TANGORA 20,000 Word Speech Recognizer," ICASSP87, pp. 701-704, 1987.
[3] Y.L. Chow, et al., "BYBLOS: The BBN Continuous Speech Recognition System," ICASSP 87, pp. 89-92, 1987.
[4] K.F. Lee and H.W. Hon, "Large-Vocabulary Speaker-Independent Continuous Speech Recognition using HMM," ICASSP88, pp. 123-126, 1988.
[5] S.E. Levinson, "Continuously Variable Duration Hidden Markov Models for Automatic Speech Recognition," Computer Speech and Language, No. 1, pp. 29-45, 1986.
[6] M.J. Russel and A.E. Cook, "Experimental Evaluation of Duration Modelling Techniques for Automatic Speech Recognition," ICASSP87, pp. 2376-2379, 1987.
[7] Y. Ariki and M.A. Jack, "Enhanced Time Duration Constraints in Hidden Markov Modelling for Phoneme Recognition," IEE Electronics Letters, Vol. 25, No. 13, pp. 824-825, 1989.
[8] Y. Ariki, F.R. McInnes and M.A. Jack, "Hierarchical Phoneme Discrimination by Hidden Markov Modelling using Cepstrum and Formant Information," ICASSP89, pp. 663-666, 1989.
[9] H.D. Huang, Y. Ariki and M.A. Jack, "Hidden Markov Models for Speech Recognition," Edinburgh University Press, 1990.
[10] A. Crowe and M.A. Jack, 'Globally Optimising Formant Tracker using Generalised Centroids," IEE Electronics Letters, Vol. 23, No. 19, pp. 1019-1020, 1987.


[^0]:    Yasuo Ariki（有木康雄）：Associated Professor，Department of Electronics and informatics，Ryukoku University

