Efficiency of the energy contained in modulators in the Arabic vowels recognition

Nesrine Abajaddi¹, Youssef Elfahm², Badia Mounir³, Laila Elmaazouzi⁴, Ilham Mounir⁵, Abdelmajid Farchi⁶

^{1,2,6}IMMII Laboratory, Faculty of Sciences and Technics, University Hassan First, Settat, Morocco ^{3,4,5}LAPSSII Laboratory, Graduate School of Technology, University Cadi Ayyad, Safi, Morocco

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ABSTRACT

The speech signal is described as many acoustic properties that may contribute differently to spoken word recognition. Vowel characterization is an important process of studying the acoustic characteristics or behaviors of speech within different contexts. This current study focuses on the modulators characteristics of three Arabic vowels, we proposed a new approach to characterize the three Arabic vowels /a/, /i/ and /u/. The proposed method is based on the energy contained in the speech modulators. The coherent subband demodulation method related to the spectral center of gravity (COG) was used to calculate the energy of the speech modulators. The obtained results showed that the modulators energy help characterize the Arabic vowels /a/, /i/ and /u/ with an interesting recognition rate ranging from 86% to 100%.

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Corresponding Author:

Nesrine Abajaddi Department of Electrical and Computer Engineering IMII Laboratory, Faculty of Sciences and Technics University Hassan First FST of Settat, Km 3, B.P: 577 Road of Casablanca, Settat, Morocco Email: n.abajaddi@uhp.ac.ma

1. INTRODUCTION

The vowel is a sound of the language characterized, in its production, by a free passage of the air in the cavities located above the glottis, namely the nasal cavity and/or the oral cavity. These cavities serve as filters whose shape and the relative contribution to the airflow affect the quality of the sound obtained [1]. The majority of the vowels are sound, that is, they are pronounced with a vibration of the vocal cords [2]. The phonetic system of the Arabic language has six vowels which are divided into two types, the short vowels (/a/, /i/ and /u/) and the long vowels (/a:/, /i:/ and /u:/). Quality and quantity are two phonetic variables used in the description of vowels. The quantity describes the duration of the vowel while the quality relates to the description of the position of the tongue in the vocal tract, the place of articulation of the vowel, the shape of the lips, the size of the narrowing and the status of the vowel [3].

Several searches have been done on the vowels in order to recognize them or to understand the physiological behavior of the vocal tract during their production. The acoustic indices most used by researchers for the characterization of vowels are the formants and the spectral moments as well as the energy in the frequency bands. Thyer *et al.* [4] worked on the identification of English vowels of Australia; they found out that the most important cues in the characterization of vowels are the first two formants F1 and F2. In another research related to the classification of vowels. Weber *et al.* [5] evaluated formant characteristics for vowel classification, they disclosed that MFCCs and formants have almost the same effect

on noisy and clean speech signals. To differentiate between racial populations, other researches have used formants. Xue *et al.* [6] recorded that, relative to white Africa, Chinese male speakers have a lower F1 form, compared to Afro-Americans, a larger F2 form for Chinese and white Americans. They concluded, on the one hand, that the configuration of the vocal tract differentiates the Chinese from the people of White Africa and the Americans of African descent. On the other hand, the difference is related to the context of the vowels which is influenced by the dialect and the specificities of the language. These findings were also mentioned by Linville *et al.* [7] who have reported that vocal tract elongation is related to the speaker and articulatory changes in vowels. Savela *et al.* [8] presented a study on the identification of different vowels of the Udmurt language using spectral moments and formants (F1 and F2). They reported that the spectral moments help get an exhaustive description of the category of the vowel.

Vaissière [9] studied six focal vowels of the French language. He concluded that these vowels are characterized by a complete fusion of two adjacent formants. He noticed that for /i/, F3 and F4 (sometimes F4 and F5) are very close. For /u/, F1 and F2 are so close that they appear as a single formant whose values are less than 1000 Hertz. /a/ presents a rapprochement of F1 and F2, F1 has a maximum value around 1000 Hz. Korkmaz and Aytug [10] exploited the formant frequency values (F1, F2 and F3) of eight Turkish vowels within CVC syllables to identify the most efficient classification method. They deduced that support vector machines (SVM) distinguishes Turkish vowels from formant frequencies with a classification success of 90%. Some studies were conducted on Arabic vowels. Alghamdi [11] performed a frequency comparison between short and long vowels for several Arabic dialects (Sudanese, Egyptian and Saudi). He stated that the first two formants of long vowels differ from those of short vowels. Iqbal et al. [12] carried out a new study on the segmentation and identification of vowels using formant transitions in the continuous recitation of Quranic Arabic. they identified the Arabic vowels based on the analysis of the extracted formants. The average accuracy of the vowel identification system is 90%. From another viewpoint, Alotaibi and Hussain [13] analyzed standard Arabic vowels formants. They showed that Formants F1 and F2 contribute to the classification of vowels; The vowel /i/ or /i:/ have a high value of F2 (F2> 1500 Hz) and the vowel /a/ or /a:/ is characterized by a high value of F1 (F1> 500 Hz).

Tsukada [14] studied the long and short vowels in Standard Arabic, Japanese and Thai. He informed that the length of long vowels is twice the length of short vowels. He also noticed that in the three languages, the ratio between the length of short and long vowels differed significantly. Natour et al. [15] worked on the examination of Arabic vowels created by men, women, and children in different languages, namely French, German and American English. They indicated that, in general, the Arabic language has a low value of F1 and F2 and a high value of F3. Moreover, the dispersion of the formants of Arabic vowels is identical to that of other studies in other languages. Abuoudeh and Crouzet [16] examined the impact of the length of the Jordanian Arabic vowel on the parameters of the locus equation. They observed that the length of the vowel systematically influences the data of the locus equation and that variations in the length of the vowel are associated with changes in the spectral configuration. Another research on vowels in Palestinian Arabic was carried out by Adam [17] who studied the variation in vowel duration in normal speakers and speakers with Broca's aphasia. The study concluded that, relative to regular speakers, vowel duration was longer for speakers with Broca's aphasia. Tahiry et al. [18] used another approach to characterize Arabic vowels. This approach is based on three methods: formants frequencies extraction, calculation of spectral moments and calculation of energy in six frequency bands. They concluded that for all three methods, the behavior of vowels depends on their place of articulation rather than their duration of production.

Aloqayli and Alotaibi [19] were analysis the values of the formants frequencies and their derivatives to evaluate the vowels in the modern standard Arabic (MSA) dialect. To develop an automatic recognition system of the six MSA vowels, they used artificial neural networks (ANN). The networks were examined with one and two hidden layers, each with a different number of neurons. In the case of one hidden layer, they detected that the system using 16 neurons had an overall performance of 87.96%, while the system using 30 neurons had an overall performance of 86.11%. In the case of two hidden layers, the system with 5 neurons in the first hidden layer and 7 neurons in the second hidden layer had an overall system performance of 83.33%, and the system with 8 neurons in the two hidden layer had an overall system performance of 87.04%. Farchi *et al.* [20] analyzed long and short Arabic vowels using production duration and energy distribution located in the first and second formant. They spotted that long vowels are twice longer than short vowels and also when the production duration of long vowels increases, the F2 band energy remains constant for all vowels, and the F1 band energy increases or decreases depending on the vowel.

This paper seeks to characterize and recognize Arabic vowels using energy in the modulators to integrate it into many applications of speech recognition and speech intelligibility. Indeed, recognition and speech enhancement systems have gained popularity in recent years. Parallel to that, the modulation domain has been extensively studied in speech applications as it offers a more compact representation. So, this work can be useful in many applications. Its main goal is to determine if and how modulators can contribute to the

identification and recognition of each Arabic vowel. This document is structured as follows. The first part describes the methods and tools used as well as the experiments carried out. The second section is devoted to the analysis and the discussion of the results. Finally, the last part presents a conclusion of this work.

2. METHODS

2.1. Corpus

The vowels corpus of the Arabic language was constructed by asking nine people (male) in their twenties to pronounce the vowels /a/, /i/ and /u/ repeatedly. The speakers have repeated each of the vowels 50 times. We have recorded 1350 vowel samples. These recordings were done as a mono sound in the laboratory using the vocal sounds process tool "Praat" with a sampling frequency of 22050 Hz, in a noise-isolated room.

2.2. Proposed method

The study existed is treated in the acoustic or spectral domain. In this paper, we focused on a demodulation method to discover the characteristics of the Arabic language in the modulation domain. Such a study constitutes the first step of a larger project which aims to add new characteristics of the Arabic language in this domain. Indeed, to identify the Arabic vowels, we adopted the schematic approach in Figure 1. First of all, the speech signal passed through a filter bank (called the analysis filter bank) in order to decompose it into subband signals. Then, each signal coming from a subband was demodulated so as to extract the modulator on which we calculated the energy. This energy makes it possible to characterize and identify each of the three Arabic vowels.

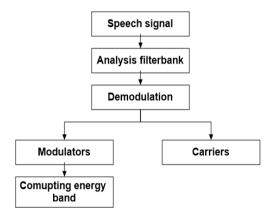


Figure 1. Block diagram used for processing the speech signal

2.3. Analysis filter bank

A filter bank is a set of low-pass, band-pass and high-pass filters. Each filter extracts a single frequency subband from the signal. These filters are used for the spectral decomposition of signals [21]. The input signal is decomposed into M subband signals by applying M analysis filters with different bandwidths. Thus, each of these subband signals contains the input signal information relating to a particular frequency band. The blocks with arrows pointing downwards indicate downsampling by factor N.

2.4. Demodulation

Naturally, speech can be described as a modulated signal, expressed as a sum of amplitudemodulated (AM) signals in a set of narrow frequency subbands covering the signal bandwidth [22]. Each subband can be considered as a pair (modulator "envelope"/carrier "fine structure"). Each modulator can be studied, modified and analyzed independently of the carrier or recombined with its corresponding carrier separately. So, in discrete-time, we can describe the full-band speech by:

$$\kappa(n) = \sum_{k=1}^{M} s_k(n) = \sum_{k=1}^{M} m_k(n) \circ c_k(n)$$
(1)

where x(n) is the observed speech signal, $m_k(n)$ and $c_k(n)$ represent the k-th modulator and the carrier waveforms of each subband $s_k(n)$, respectively. M is the number of subbands. (o) the operator designates the sample-by-sample multiplication (Hadamard product).

Two classes of methods (coherent and incoherent) are used in the modulation decomposition of the speech signal [23]. Using the non-coherent subband demodulation technique, $m_k(n)$ and $c_k(n)$ are calculated from the analytic bandpass subband signal $s_k(n)$ obtained from the filter bank. To extract the modulator from each subband, the non-coherent demodulation seems simple and easy to implement. The modulator (also known as the "Hilbert envelope") and the carrier are written, respectively, in the form:

$$m_k(n) = |s_k(n)| \tag{2}$$

$$c_k(n) = \exp(j \angle s_k(n)) \tag{3}$$

However, the modulator and the carrier are not limited in the predefined frequency band then it's not possible to modify them individually. For this reason, we adopted a coherent subband demodulation. We used the spectral center-of-gravity (COG) method [24] to evenly track the evolution of spectral concentration within subband over time, as an estimate of the instantaneous frequency $f_k(n)$. The carrier phase is defined in (4). Coherent demodulation defines the modulator according to the estimated carrier in (5) and (6).

$$\phi_k(n) = \sum_{p=0}^n f_k(p) \tag{4}$$

$$c_k(n) = \exp(j \angle s \phi_k(n)) \tag{5}$$

$$\mathbf{m}_{\mathbf{k}}(\mathbf{n}) = \mathbf{s}_{\mathbf{k}}(\mathbf{n}) \cdot \mathbf{c}_{\mathbf{k}}^{*}(\mathbf{n}) \tag{6}$$

2.5. Energy band

The analysis of the temporal variations and the average energy of the modulators reveals that five bands allow identifying each of the vowels. The energy distribution of the speech signal in these frequency bands makes it possible to determine the modulators which characterize each vowel /a/, /u/, or /i/. The five frequency bands used in this study are as follows: Band 1 (100-400 Hz); Band 2 (400-800 Hz); Band 3 (800-2000 Hz); Band 4 (2000-3500 Hz) and Band 5 (3500-5000 Hz). The modulator of each subband was hamming windowed (256 points with an overlap of 50%). Then, the energy in each window of the modulator was calculated by (7):

$$E(b,j) = \sum_{k=0}^{i-1} |m(b,k)|^2$$
(7)

where b is the number of modulators, j is the number of windows and i is the length of the window. Next, we calculated the percentage energy of each window for each modulator as (8):

$$P_{\rm ET} = \frac{E(b,j)}{E_{\rm T}(j)} * 100$$
(8)

With $E_T(j)$ is the total energy of all modulators in the same window, calculated by (9):

$$\mathbf{E}_{\mathrm{T}}(\mathbf{j}) = \sum_{n=0}^{\mathrm{b}} \mathbf{E}(\mathbf{j}, n) \tag{9}$$

3. RESULTS AND DISCUSSION

3.1. The energy in the modulators and recognition system

The aim of this part is to analyze the modulators of the three Arabic vowels (/a/, /i/ and /u/). We calculated the percentage of total energy in each modulator by (8) for all samples in our vocal corpus as shown in Figures 2, 3 and 4. Then, we calculated the average percentage of each modulator relative to the others in order to extract the dominant modulators for each vowel. Based on the average energy percentage value for each modulator for the three vowels, we can see that:

The vowel /a/: the majority of energy is located in the second modulator (49%), the third modulator (35%), and the first modulator which contains less important energy of the order of 14% as shown in Figure 2. These results can be justified by the fact that for the vowel /a/, the first formant F1 is located around 600 Hz which corresponds to the second modulator (400-800 Hz). On the other hand, the second formant F2 is located around 1000 Hz, hence the energy contained in the third modulator (800-2000 Hz) [18].

The vowel /i/: the energy is focused in the first modulator (77%) and the fourth modulator (20%) as shown in Figure 3. We can explain this result by the fact that the first formant F1 of the vowel /i/ is about

300 Hz which implies the first modulator (100-400 Hz). On the other hand, the second formant F2 is located around 2000 Hz, hence the energy located in the fourth modulator (2000-3500 Hz) [18].

The vowel /u/: the energy is concentrated on the first two modulators (27% for M1 and 68% for M2) as shown in Figure 4. This is justified by the fact that the first two formants F1 and F2 are concentrated on the low frequencies and the distance between them is small (F1> 300 Hz and F2 <1000 Hz). This shows the existence of the first two modulators (M1: 100-400 Hz and M2: 400-800 Hz) [18].

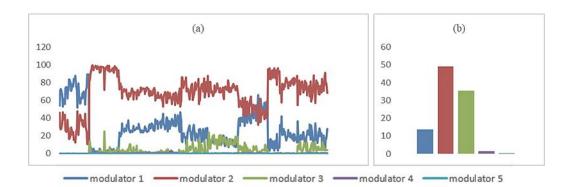


Figure 2. The calculation results of (a) The modulators energy percentage distribution of the vowel /a/, (b) The modulators energy percentage average of the vowel /a/

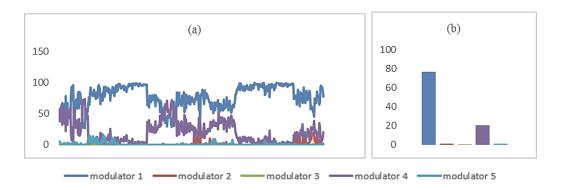


Figure 3. The calculation results of (a) The modulators energy percentage distribution of the vowel /i/, (b) The modulators energy percentage average of the vowel /i/

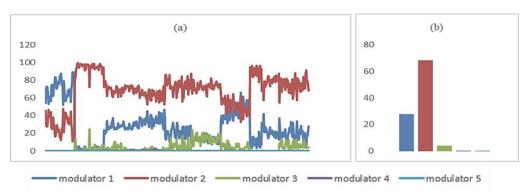


Figure 4. The calculation results of (a) The modulators energy percentage distribution of the vowel /u/, (b) The modulators energy percentage average of the vowel /u/

Therefore, we can notice that each of these Arabic vowels can be at most characterized by two main modulators. So, we have developed a simple recognition system that classifies these three Arabic vowels based on the previously proposed modulators. Figure 5 presents the adopted algorithm.

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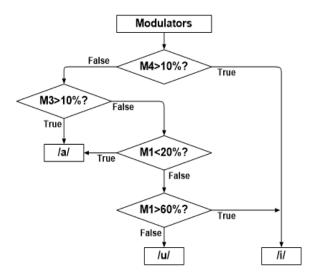


Figure 5. Algorithm of classification of Arabic vowels

3.2. Recognition system performance

To test the performance of our approach, it was implemented under MATLAB and tested utilizing the records from our corpus. The number of all vowels in this experiment is 1350. To evaluate our identification algorithm, we calculated the confusion matrix as shown in Table 1. This confusion matrix represents the recognition percentage of Arabic vowels. The last column (Unclassified) represents the number of cases that could not be identified.

Table 1. Vowels confusion matrix

	/a/	/i/	/u/	Unclassified
/a/	100	0	0	0
/i/	0	95.33	4.66	0
/u/	13.77	0	86.22	0

We can see from the results of the adopted approach that the identification error is null, all the vowels have thus been identified. The values 13.77% and 4.66% represent the confusion percentage of a vowel with another (/a/ with /u/ and /u/ with /i/ respectively). The confusion between the vowel /u/ and /a/ or /i/ respectively is due to the energy distribution of /u/ which is concentrated on the first two modulators M1 and M2. Thus, an interlocutor variation may lead to drop-in energy in the first modulator following a value of the first F1 formant greater than 400 Hz. Hence, a confusion between /u/ and /a/. In the same way, an interlocutor variation can generate a higher value of the second formant F2 (> 3500 Hz), the energy in the fourth modulator decreases, and consequently, confusion is induced between /u/ and /i/.

3.3. Discussion

The characterization of Arabic vowels based on modulators reveals that modulators can classify Arabic vowels (/a/, /i/ and /u/). Each of these vowels can be characterized by two main modulators. According to the analysis of the modulators in the subbands, we can notice that all the vowels have a significant energy percentage in the first modulator because they are all voiced sounds. However, this percentage of energy varies from one vowel to another (/a/: $\approx 13\%$; /i/: $\approx 77\%$ and /u/: $\approx 27\%$).

The results show that vowel /a/ is identified by the two main modulator M2 (second modulator) and M3 (third modulator). These results may be justified by the fact that the vowel /a/ is produced by lifting the central part of the tongue to the junction between hard and soft palates [25]. Thus, the distribution of Formants F1 and F2 is in agreement with our results: F1 is greater than 600 Hz, this energy is thus found in the second modulator M2 (400-800 Hz). F2 is greater than 1000 Hz, then the third modulator M3 (800-2000 Hz) contains an important part of energy [18].

The vowel i is distinguished by its energetic distribution in the fourth modulator because it is produced by raising the tip of the tongue towards the hard palate [25] so F2 moves towards the high frequencies (F2> 2000 Hz) and therefore the energy is concentrated in M4. On the other hand, i also

contains a significant percentage of energy in the first modulator. This concentration of energy in the first modulator M1 can be explained by the value of the first formant F1 (F1 <300 Hz) which is located in the low frequencies in addition to the energy due to the glottal vibration (<400 Hz) generated by the voiced sounds [18].

For the vowel /u/, most of the energy is focused on the first modulator (M1: 100-400 Hz) and the second modulator (M2: 400-800 Hz). This behavior is due to the two first formants F1 and F2 which are so close and concentrated in low frequencies (F1> 300 and F2 <1000 Hz) [18]. These results may be justified by the fact that the vowel /u/ is a back vowel and is produced by raising the back of the tongue towards the soft palate [25].

Therefore the obtained results in this work are consistent with those reported by other research studies on the classification of vowels using formants in the spectral domain (Alghamdi [11]; Alotaibi [13]; Vaissière [9]; Tahiry [18]; Aloqayli and Alotaibi [19]). On the other hand, the recognition system of Arabic vowels proposed in this work presents interesting advantages. Indeed, it is a simple system in its implementation whose recognition performance is very interesting (100% for /a/, 95.33% for /i/ and 86.22% for /u) comparing with the other methods [19] as shown in Table 2.

Table 2. Recognition rate comparison							
	The proposed method (%)	ANN (One hidden	ANN (One hidden	ANN (Two hidden	ANN (Two hidden		
		layers with 16	layers with 30	layers with [5-7]	layers with [8-8]		
		neurons) (%)	neurons) (%)	neurons) (%)	neurons) (%)		
/a/	100	100	88.89	83.33	83.33		
/i/	95	83.33	83.33	72.22	77.78		
/u/	86.22	72.22	83.33	83.33	100		

4. CONCLUSION

In this article, a new approach is presented to recognize Arabic vowels based on modulators energy. This method is based on the calculation of the percentage of energy contained in modulators in predefined frequency bands. The results showed that each vowel can be identified by two main modulators whose energy percentage is quite important. The recognition rate of the vowels is largely satisfactory to ensure the robustness of this algorithm. These results encourage us to characterize the remaining consonants in future work in order to build a simple and efficient speech recognition system that can be used in denoising applications, sound separations and segmentation.

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