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Ryan C. Fortenberry  
*University of Mississippi*

Tarek Trabelsi  
*University of Pennsylvania*

Brent R. Westbrook  
*St. Edward's University*

Weston A. Del Rio  
*University of Mississippi*

Joseph S. Francisco  
*University of Pennsylvania*

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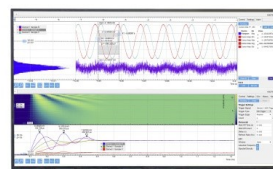
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Ryan C. Fortenberry,<sup>1,a)</sup>  Tarek Trabelsi,<sup>2</sup>  Brent R. Westbrook,<sup>3</sup> Weston A. Del Rio,<sup>1</sup>  
and Joseph S. Francisco<sup>2</sup> 

## AFFILIATIONS

<sup>1</sup>Department of Chemistry and Biochemistry, University of Mississippi, University, Mississippi 38677-1848, USA

<sup>2</sup>Department of Earth and Environmental Science Philadelphia, University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA

<sup>3</sup>Department of Chemistry, St. Edward's University, Austin, Texas 78704, USA

<sup>a)</sup>r410@olemiss.edu

## ABSTRACT

The oxywater cation ( $\text{H}_2\text{OO}^+$ ), previously shown to form barrierlessly in the gas phase from water cations and atomic oxygen, is proposed here potentially to possess a  ${}^2A'' \leftarrow {}^4A''$  excitation leading to the  $\text{H}_2\cdots\text{O}_2^+$  complex. This complex could then easily decompose into molecular hydrogen and the molecular oxygen cation. The present quantum chemical study shows that the necessary electronic transition takes place in the range of 1.92 eV (645 nm), in the orange-red range of the visible and solar spectrum, and dissociation of the complex only requires 5.8 kcal/mol (0.25 eV). Such a process for the abiotic, gas phase formation of  $\text{O}_2$  would only need to be photocatalyzed by visible wavelength photons. Hence, such a process could produce  $\text{O}_2$  at the mesosphere/stratosphere boundary as climate change is driving more water into the upper atmosphere, in the comet 67P/Churyumov-Gerasimenko where surprisingly high levels of  $\text{O}_2$  have been observed, or at gas-surface (ice) interfaces.

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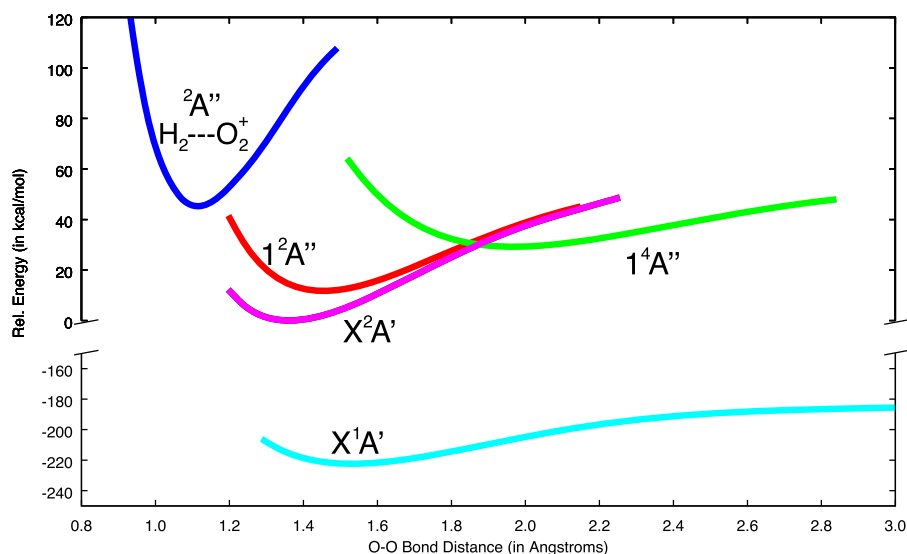
## INTRODUCTION

Recent work has shown that, in the gas phase, water will form bonds originating on the oxygen atom with every atomic cation from hydrogen even to argon.<sup>1</sup> Quintessentially, hydronium ( $\text{H}_3\text{O}^+$ ) is a pillar of acid-base chemistry and has even been observed in the interstellar medium (ISM).<sup>2</sup> More interesting, though, the bonding of water cation with atomic oxygen is shown to be stable in forming the oxywater cation. In this molecule, the O–O bond energy is 54.08 kcal/mol<sup>1</sup> which is notably greater than that of hydrogen peroxide with a O–O bond energy of a meager 33.9 kcal/mol, enough to be cleaved by sunlight. However, this present work will discuss a previously unreported quaternary minimum.

## RESULTS AND DISCUSSION

The creation of the oxywater cation ( $\text{H}_2\text{OO}^+$ )<sup>3–5</sup> from water cations and atomic oxygen progresses barrierlessly through a wide minimum for the association of  $\text{O}({}^3P)$  to  $\text{H}_2\text{O}^+$  potential energy

surface (PES), shown in the green ( $1^4A''$ ) line of Fig. 1 and previously demonstrated by Ref. 1. Then, electronic emission can create the doublet surface(s) (magenta  $X^2A'$  and red  $1^2A''$  lines of Fig. 1) where the molecule can relax into its optimized and stable minimum. In such a process, the resulting vibrational cascade would be reduced since the doublet surface crosses the quartet surface nearly at its minimum making the bonding reaction much faster than is typical of radiative association reactions which are notoriously slow. Consequently, these CCSD(T)-F12/cc-pVTZ-F12 computations<sup>6,7</sup> show that not only is the oxywater cation stable, but it should also form relatively easily.<sup>1</sup> These computations have also been verified with multireference configuration interaction theory via MRCISD(+Q)/aug-cc-pVTZ computations<sup>8,9</sup> giving the same potential energy curves as provided in Fig. S1 of the [supplementary material](#). Furthermore, these MRCI computations clearly show that formation of  $\text{H}_2\text{OO}^+$  in this process likely is initiated with  $\text{H}_2\text{O}^+$  and oxygen atoms. Formation through the alternate  $\text{O}^+({}^3S)$  and  $\text{H}_2\text{O}$  channel does not appear to couple with these low-lying states. Further work will explore this pathway.



**FIG. 1.** The CCSD(T)-F12/cc-pVTZ-F12 one-dimensional potential energy surface (in kcal/mol) for the O–O stretch of  $\text{H}_2\text{OO}^+$ . Curves: cyan,  $1A'$   $\text{H}_2\text{OO}$ ; magenta,  $X^2A'$   $\text{H}_2\text{OO}^+$ ; red,  $1^2A''$   $\text{H}_2\text{OO}^+$ ; green,  $1^4A''$   $\text{H}_2\text{OO}^+$ ; and blue,  $^2A''$   $\text{H}_2\cdots\text{O}_2^+$ .

The oxywater neutral will break apart more easily since the O–O bond dissociation energy is on the order of 40 kcal/mol (cyan  $X^1A'$  line in Fig. 1). The ionization potential of  $\text{H}_2\text{OO}$  is computed here to be 9.58 eV, significantly more than the O–O bond energy as observed in Fig. 1 where the magenta  $X^2A'$  line is well above the cyan  $X^1A'$  asymptotic dissociation limit. Furthermore, there do not appear to be any other states that interact with the ground state of  $\text{H}_2\text{OO}$ . The oxywater cation, on the other hand, is more likely to engage in novel chemistry. Most notably,  $\text{H}_2\text{OO}^+$  has another state of interest that gives many indications of leading to molecular oxygen.

The blue line in Fig. 1 represents a  $^2A''$  electronically excited state of a  $\text{H}_2\text{OO}^+$  that ultimately gives rise to the  $\text{H}_2\cdots\text{O}_2^+$  complex,  $\text{H}_2$  weakly bound to  $\text{O}_2^+$ . The ionization potential of  $\text{O}_2$  is notably less than  $\text{H}_2$  (12.07 eV vs 15.43 eV)<sup>10</sup> likely forbidding the formation of the  $\text{O}_2\cdots\text{H}_2^+$  system. Present CCSD(T)-F12/cc-pVTZ-F12 computations predict the optimized O–O bond length in this molecular complex to be 1.117 Å which is nearly exactly that for  $\text{O}_2^+$  at 1.116 Å from the experiment,<sup>10</sup> putting the positive charge on the oxygen molecule portion. Additionally, with X defined as the center-of-mass in the  $\text{H}_2$  portion, the optimized X–H value is 0.374 Å making H–H 0.748 Å, close to the experimental 0.741 Å for  $\text{H}_2$ .<sup>10</sup> The rest of the geometric parameters for  $\text{H}_2\cdots\text{O}_2^+$ , as well as the doublet and quartet forms of  $\text{H}_2\text{OO}^+$  for comparison, are given in Table I.

The  $^2A''$   $\text{H}_2\cdots\text{O}_2^+$  complex lies adiabatically 39.3 kcal/mol (1.70 eV) above the  $X^2A'$  ground state of  $\text{H}_2\text{OO}^+$  and only a mere 12.6 kcal/mol (0.54 eV) above the  $1^4A''$  state. The binding of the oxygen molecular cation to the hydrogen molecule in  $\text{H}_2\cdots\text{O}_2^+$  is computed here to be 5.8 kcal/mol from a simple products minus reactants model. While the O–X distance gives a fairly flat potential, the  $\angle\text{O–O–X}$  angle is more rigid at the optimized 111.5° similar to ligands of  $\text{NO}^+$ .<sup>11</sup>

As shown in Fig. 2, the electronic states of  $\text{H}_2\text{OO}^+$  and that from the  $\text{H}_2\cdots\text{O}_2^+$  complex have different orbital occupations,

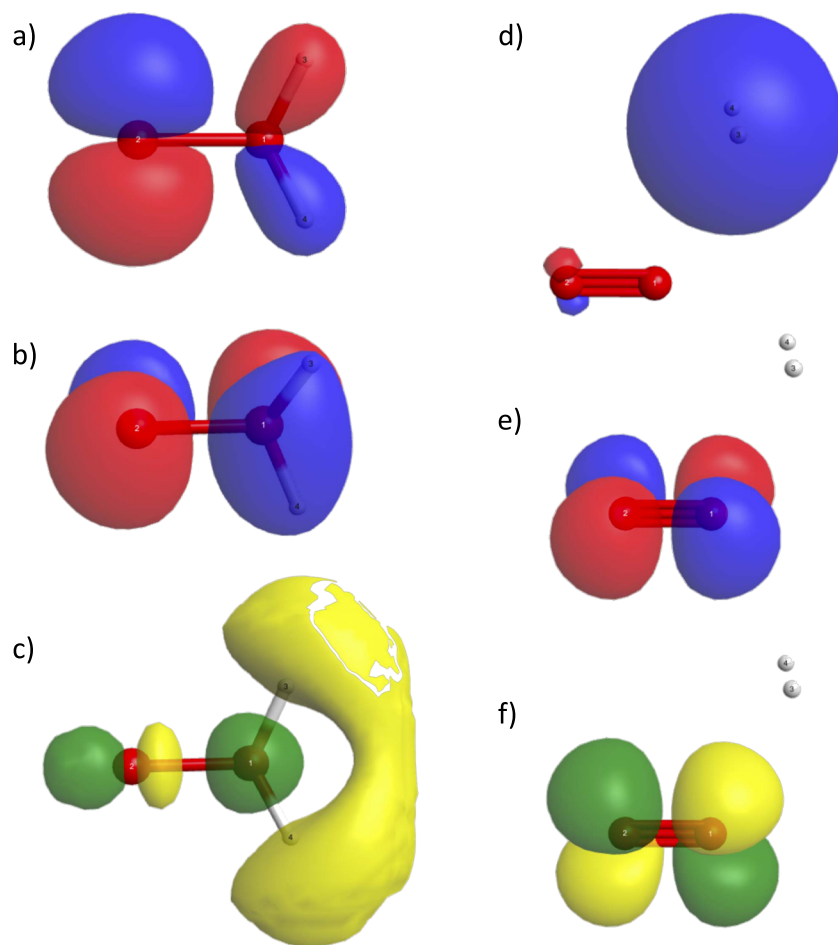
but the topologies of the orbitals themselves largely remain consistent. The ground  $X^2A'$  state of the oxywater cation has a (core)( $3a'$ )<sup>2</sup>( $4a'$ )<sup>2</sup>( $1a''$ )<sup>2</sup>( $5a'$ )<sup>2</sup>( $6a'$ )<sup>2</sup>( $2a''$ )<sup>2</sup>( $7a'$ ) orbital occupation. The other doublet ( $1^2A''$ , red line in Fig. 1) excites one electron from the  $2a''$  orbital into the  $7a'$ , as shown in Fig. 3. The  $1^4A''$  state excites one electron from the same  $2a''$  orbital in the ground  $X^2A'$  state of  $\text{H}_2\text{OO}^+$  into a higher  $8a'$  in the third column in Fig. 3. These three orbitals in this active space represent the three antibonding  $p$  orbital combinations from the oxygen atoms:  $2a''$  being  $\pi_y^*$ ,  $7a'$  being the  $\pi_z^*$  highest-occupied molecular orbital (HOMO), and  $8a'$  being the  $\sigma^*$  lowest-unoccupied molecular orbital (LUMO). These are visually depicted in Figs. 2(a)–2(c), respectively.

The  $^2A''$   $\text{H}_2\cdots\text{O}_2^+$  complex occupation is defined as (core)( $3a'$ )<sup>2</sup>( $4a'$ )<sup>2</sup>( $1a''$ )<sup>2</sup>( $5a'$ )<sup>2</sup>( $6a'$ )<sup>2</sup>( $7a'$ )<sup>2</sup>( $2a''$ ) and is compared to the other states' occupations in the last column of Fig. 3. Hence, the  $^2A''$   $\text{H}_2\cdots\text{O}_2^+$  state and the ground  $X^2A'$  state of  $\text{H}_2\text{OO}^+$  have the same occupation of the same orbitals up to the HOMO-2  $6a'$  orbital. These are mostly the expected  $\text{O}_2$  MOs for the first six levels. The actual HOMO-1, HOMO, and LUMO for this complex are all shown in Figs. 2(d)–2(f). In this complex,  $7a'$  HOMO-1 is the H–H  $\sigma$  bond, the  $2a''$  HOMO is the  $\pi_y^*$ , and the  $8a'$  LUMO is the  $\pi_z^*$ .

**TABLE I.** The CCSD(T)-F12/cc-pVTZ-F12 optimized geometries.<sup>a</sup>

	$X^2A'$ $\text{H}_2\text{OO}^+$	$1^4A''$ $\text{H}_2\text{OO}^+$	$^2A''$ $\text{H}_2\cdots\text{O}_2^+$
O–O (Å)	1.362	1.964	1.117
X–H (Å)	0.846	0.791	0.374
O–X (Å)	0.507	0.578	2.424
$\angle\text{O–O–X}$ (deg)	137.4	112.9	111.5

<sup>a</sup>X represents the center-of-mass in the  $\text{H}_2$  moiety, i.e., half of the H–H bond length. This parameter gives more generic coordinates between the two isomers.

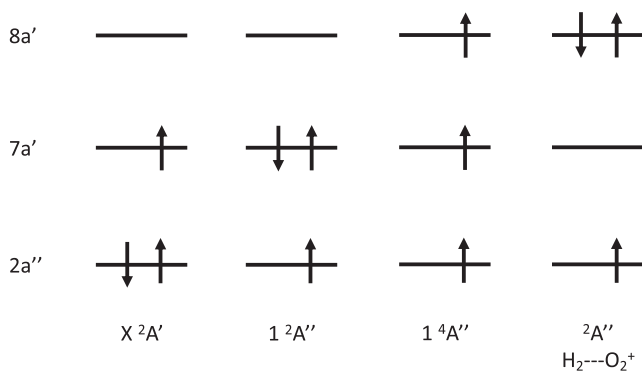


**FIG. 2.** The  $\text{H}_2\text{OO}^+$  MOs: (a)  $2a''$  HOMO-1, (b)  $7a'$  HOMO, and (c)  $8a'$  LUMO; as well as the  $\text{H}_2\cdots\text{O}_2^+$  MOs: (d)  $7a'$  HOMO-1, (e)  $2a''$  HOMO, and (f)  $8a'$  LUMO.

At first glance, these two sets of MOs appear unrelated, but a closer inspection indicates that they are actually connected as is further exposed in Fig. 3. The key is from the  $1^4A''$  state where the  $\text{H}_2\text{OO}^+$   $8a'$  orbital is singly occupied. As shown in Fig. 2(c), the hydrogen atoms are in-phase with one another even if the

adjacent atoms have antibonding interactions. Similar  $\sigma$  antibonding but in-phase hydrogen backbonding has been previously shown in the related  $1^4A''$  state of  $\text{H}_2\text{SS}^+$ .<sup>12</sup> This is the same topology as  $7a'$  HOMO-1 (H–H  $\sigma$ -bonding orbital) in  $\text{H}_2\cdots\text{O}_2^+$  shown in Fig. 2(d). Succinctly, the difference between the MOs in  $\text{H}_2\text{OO}^+$  and  $\text{H}_2\cdots\text{O}_2^+$  can be described from Fig. 2 where (a), (b), and (c) become (e), (f), and (d), respectively. Hence, a spin-flip excitation in the  $1^4A''$   $\text{H}_2\text{OO}^+$  state out of the  $7a'$  HOMO into the  $8a'$  LUMO would create orbital occupations consistent with the occupations of the  $2^2A''$  state of  $\text{H}_2\cdots\text{O}_2^+$  again shown in Fig. 3.

The  $1^4A''$  state of  $\text{H}_2\text{OO}^+$  and  $2^2A''$   $\text{H}_2\cdots\text{O}_2^+$  have further commonalities.  $\angle\text{O–O–X}$  is close between the two at  $112.9^\circ$  and  $111.5^\circ$ , respectively, from Table I. Figure 4 is a  $2^2A''$  two-dimensional PES scanning over the X–H and O–X bond lengths in this case where  $\angle\text{O–O–X}$  and O–O are frozen at the optimized  $2^2A''$   $\text{H}_2\cdots\text{O}_2^+$  values. The  $\text{H}_2\cdots\text{O}_2^+$  minimum is clearly produced, but a second local minimum  $31.7$  kcal/mol ( $1.37$  eV) above the minimum for the complex is also present. The X–H value ( $y$ ) is  $0.8$  Å, and the O–X value ( $x$ ) is  $0.7$  Å at this local minimum in Fig. 4. These values are nearly the same as the X–H and O–X bond lengths in  $1^4A''$   $\text{H}_2\text{OO}^+$  indicating that the  $2^2A'' \leftarrow 4^4A''$  excitation in  $\text{H}_2\text{OO}^+$  takes place here. The excitation energy is approximated to be  $44.3$  kcal/mol ( $1.92$  eV



**FIG. 3.** The  $\text{H}_2\text{OO}^+$  MO occupations for the  $X^2A'$ ,  $1^2A''$ , and  $1^4A''$  states of  $\text{H}_2\text{OO}^+$  and the  $2^2A''$  state of  $\text{H}_2\cdots\text{O}_2^+$  as labeled from the  $X^2A'$  state.

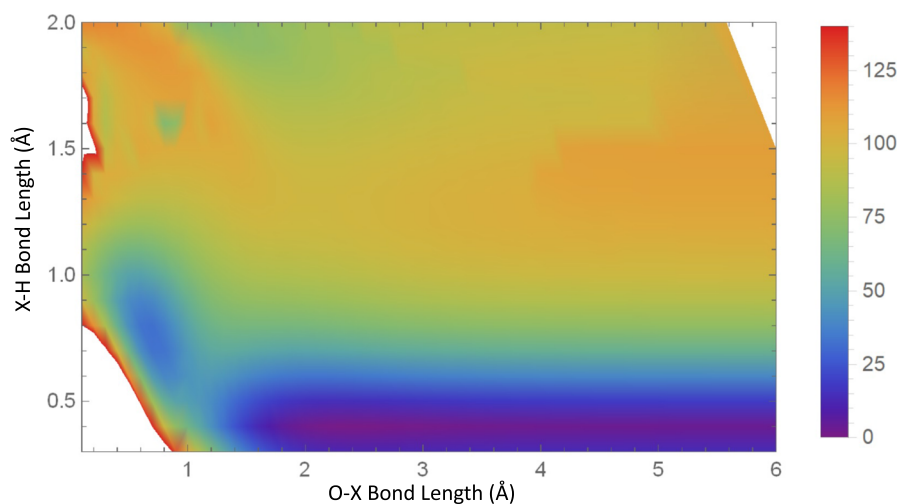


FIG. 4. The  ${}^2A''$   $\text{H}_2\cdots\text{O}_2^+$  2D PES with energy gradations in kcal/mol.

or 645 nm) in this region since, again,  $1^4A''$   $\text{H}_2\text{OO}^+$  and  ${}^2A''$   $\text{H}_2\cdots\text{O}_2^+$  are separated by 12.6 kcal/mol. Additionally, a saddle point between these two minima at  $X\text{-H} = 0.6$  Å and  $\text{O-X} = 1.1$  Å lies 46.0 kcal/mol (1.99 eV) above the  $\text{H}_2\cdots\text{O}_2^+$  minimum.

Hence, the  $1^4A''$  state of  $\text{H}_2\text{OO}^+$  and the  ${}^2A''$   $\text{H}_2\cdots\text{O}_2^+$  state could interact in the region where the blue second minimum in Fig. 4 occurs. This  ${}^2A'' \leftarrow {}^4A''$  excitation appears to take place in the red of the visible spectrum clearly within the wavelengths of sunlight. Other  $\text{H}_2\cdots\text{O}_2^+$  minima have also been localized in this study, but their  $X\text{-O}$  bond distances are greater than 4.0 Å. In order to fully characterize any transition from  $\text{H}_2\text{OO}^+$  into  $\text{H}_2\cdots\text{O}_2^+$ , spin-flip excited state determinants and electron dynamics computations originating with the  $1^4A''$  state of  $\text{H}_2\text{OO}^+$  or a semiglobal 6D PES surface are necessary in future work. However, the local minimum described above is a very promising region to explore the formation of  $\text{O}_2^+$  from water in the gas phase.

## CONCLUSIONS

The oxywater cation is shown here to be a possible intermediate in the creation of molecular oxygen from water cations and atomic oxygen. The formation of the oxywater cation begins with  $\text{O}(^3P)$  atoms bonding with water cations to produce  $1^4A''$   $\text{H}_2\text{OO}^+$ . Before becoming  $X^2A'$  or  $1^2A''$   $\text{H}_2\text{OO}^+$ , the quartet state may convert to a different  ${}^2A''$  state instead,  $\text{H}_2\cdots\text{O}_2^+$ . The minima of  $1^4A''$   $\text{H}_2\text{OO}^+$  and  ${}^2A''$   $\text{H}_2\cdots\text{O}_2^+$  are only 12.6 kcal/mol apart adiabatically. Furthermore, the lowest  $1^4A''$  state of  $\text{H}_2\text{OO}^+$  has a similar geometry to the local minimum on the  ${}^2A''$  PES corresponding to the  $\text{H}_2\cdots\text{O}_2^+$  complex. The approximated  ${}^2A'' \leftarrow {}^4A''$  excitation for  $\text{H}_2\text{OO}^+$  in this region is 645 nm, and further refinements of this value likely leading to the  $\text{H}_2\cdots\text{O}_2^+$  complex should not shift it out of the range for solar radiation. The resulting complex after excitation and crossing a low-lying saddle point is then easily dissociated into molecular hydrogen and molecular oxygen. Consequently, the oxywater cation and its  $\text{H}_2\cdots\text{O}_2^+$  complex give all indication of facilitating the creation of molecular oxygen. This has application to various natural processes ranging from the creation of surprisingly high amounts of molecular oxygen in the coma of comet 67P/Churyumov-Gerasimenko

observed during the *Rosetta* mission<sup>13</sup> to the provenance of oxygen on the early Earth potentially including the “snowball Earth” epoch and even to oxygen generation in the upper atmosphere where climate change is driving more water vapor into the stratosphere where it can ionize and react with known atomic oxygen.

## COMPUTATIONAL DETAILS

All relative energies and PES scans employ the CCSD(T)-F12/cc-pVTZ-F12 level of theory, except where MRCISD(+Q)/aug-cc-pVTZ is noted. In either case, the MOLPRO2015.1 quantum chemistry program<sup>14,15</sup> is solely utilized. All geometry optimizations are followed by harmonic vibrational frequency computations to ensure that the structures examined are minima and to provide the harmonic zero-point vibrational corrections which are included in the relative energy determinations. The PES scans have displacements of 0.1 Å for the O–O bond lengths (Fig. 1), 0.2 Å for the O–X bond lengths (Fig. 4), and 0.1 Å displacements for the X–H bond lengths (Fig. 4).

## SUPPLEMENTARY MATERIAL

The [supplementary material](#) contains the MRCISD(+Q)/aug-cc-pVTZ data as a scan of states for the O–O bond elongation.

## ACKNOWLEDGMENTS

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