

# Isocurvature perturbations of dark energy and dark matter from the Swampland conjecture

著者	Hiroki Matsui, Fuminobu Takahashi, Masaki Yamada
journal or publication title	Physics letters. Sect. B
volume	789
page range	387-392
year	2019-02-10
URL	<a href="http://hdl.handle.net/10097/00130703">http://hdl.handle.net/10097/00130703</a>

doi: 10.1016/j.physletb.2018.12.055

# Isocurvature Perturbations of Dark Energy and Dark Matter from the Swampland Conjecture

Hiroki Matsui<sup>♠</sup> Fuminobu Takahashi<sup>♠◇♣</sup> and Masaki Yamada<sup>♡</sup>

<sup>♠</sup> Department of Physics, Tohoku University, Sendai, Miyagi 980-8578, Japan

<sup>◇</sup> Kavli IPMU (WPI), UTIAS, The University of Tokyo, Kashiwa, Chiba 277-8583, Japan

<sup>♣</sup> Department of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139 USA

<sup>♡</sup> Institute of Cosmology, Department of Physics and Astronomy, Tufts University, Medford, MA 02155, USA

**Abstract.** We point out that the recently proposed Swampland conjecture on the potential gradient can lead to isocurvature perturbations of dark energy, if the quintessence field acquires large quantum fluctuations during high-scale inflation preferred by the conjecture. Also, if the quintessence field is coupled to a dark sector that contains dark matter, isocurvature perturbation of dark matter is similarly induced. Both isocurvature perturbations can be suppressed if the quintessence potential allows a tracker solution in the early Universe. We find that a vector field of mass  $\lesssim \mathcal{O}(1)$  meV is an excellent dark matter candidate in this context, not only because the right abundance is known to be produced by quantum fluctuations during high-scale inflation without running afoul of isocurvature bounds, but also because its coupling to the quintessence does not spoil the flatness of the potential.

---

## Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
<b>2</b>	<b>Isocurvature perturbations</b>	<b>3</b>
<b>3</b>	<b>DM interacting with quintessence field</b>	<b>4</b>
3.1	Model-dependent constraints	4
3.2	Model-independent constraints	5
<b>4</b>	<b>Discussion and conclusions</b>	<b>7</b>

---

## 1 Introduction

There have been accumulating observational evidence that supports the existence of an inflationary era in the early Universe. The inflation not only solves various initial condition problems of the standard big bang theory but also explains the origin of density perturbations [1–6]. Also, the current expansion of the universe is accelerating. In the  $\Lambda$ CDM paradigm, both accelerated cosmic expansions are realized by simple slow-roll inflation and the cosmological constant. So far, the  $\Lambda$ CDM paradigm is in perfect agreement with the current observations such as the Planck data [7].

The great success of the  $\Lambda$ CDM paradigm plus slow-roll inflation was recently challenged by the so-called Swampland conjectures [8]. The Swampland refers to a set of low-energy theories which look consistent from the low-energy perspective but fail to be UV completed with quantum gravity. One of the conjectures sets a lower bound on the potential gradient as

$$\frac{|\nabla V|}{V} \geq c, \tag{1.1}$$

where  $c$  is a numerical constant expected to be of order unity, and  $V$  is a scalar potential. Here and hereafter, we use the reduced Planck unit:  $8\pi G = M_{\text{Pl}}^{-2} = 1$ . There are a variety of de Sitter no-go theorem in quantum gravity [9–14] and the conjecture originates from a long history of constructing de Sitter solutions in string theory. The cosmological applications and the validity of the conjecture have been extensively studied in Refs. [8, 15–42].

If applied to the inflaton potential, this conjecture leads to a lower bound on one of the slow-roll parameters,  $\varepsilon$ , as

$$\varepsilon = \frac{1}{2} \left( \frac{|\nabla V|}{V} \right)^2 \geq \frac{c^2}{2}. \tag{1.2}$$

As long as the quantum fluctuation of the inflaton is responsible for the observed density perturbation, the  $\varepsilon$  parameter is related to the Hubble parameter during inflation as [7]

$$\varepsilon \simeq 0.010 \left( \frac{H_{\text{inf}}}{10^{14} \text{ GeV}} \right)^2. \tag{1.3}$$

The current bound on  $\varepsilon$  comes from non-detection of the primordial gravitational wave. The Planck 95% CL limit on the tensor-to-scalar ratio reads,  $r \lesssim 0.10$  [7]. Using the slow-roll relation of  $r = 16\varepsilon$ , one obtains

$$\varepsilon \lesssim 0.0063. \quad (1.4)$$

Under the Swampland conjecture (1.1), this can be expressed as the bound on  $c$ :

$$c \lesssim 0.11. \quad (1.5)$$

So, if  $c = \mathcal{O}(1)$  is taken at a face value, there is already a mild tension between the observation and theoretical expectation [8]. In other words, the Swampland gives a preference to high-scale inflation close to the current bound. Assuming the current bound is saturated, the typical Hubble parameter during inflation is  $H_{\text{inf}} \sim 10^{14}$  GeV.

Also, the Swampland conjecture (1.1) excludes the cosmological constant as the explanation of the current accelerated expansion, and supports an idea of the quintessence; the quintessence field  $\varphi$  slow-rolls on a potential, and its potential energy drives the accelerated cosmic expansion [43–56]. When the conjecture is applied to the accelerated expansion of the present Universe, the current bound on  $c$  reads [8, 32, 33, 57]

$$c \lesssim 0.6 - 0.9. \quad (1.6)$$

This leads to the red-shift-dependent lower bound on the equation-of-state parameter of the dark energy (DE).<sup>1</sup>

The quintessence field may have interactions with other sectors such as dark matter (DM). However, its couplings to the standard model are subject to the stringent fifth-force constraints, which substantially restrict a possible form of the interaction [8, 66]. In particular, it has been extensively discussed in the literature if the Swampland conjecture is satisfied before the electroweak and QCD phase transitions [67–69]. We do not discuss this issue further.<sup>2</sup> Rather, we focus on implications of the Swampland conjecture for the inflation and the quintessence as they are the main targets of this conjecture. Indeed, one of the striking features of the Swampland conjecture is that it can connect phenomena that took place at vastly different times; both the inflation and the quintessence potentials must satisfy the same simple requirement.

In this Letter we point out that isocurvature perturbation of DE is expected from the conjecture, if the quintessence field remains light and frozen during inflation. This is because it would then acquire large quantum fluctuations during high-scale inflation preferred by the conjecture, which result in the unsuppressed isocurvature perturbation of DE. If the quintessence field is coupled to a dark sector that contains DM, isocurvature perturbation of DM is similarly induced. We will also argue that vector DM is a good candidate in this context, not only because the right abundance is known to be produced by quantum fluctuations during high-scale inflation without running afoul of isocurvature bounds, but also

---

<sup>1</sup> The equation-of-state parameter  $w_0$  of today is bounded below as  $1 + w_0 \geq 0.15c^2$  [8] where  $w = \rho/p$  for the dark energy perfect fluid. Currently there is a tension of the Hubble constant  $H_0$  between the Planck and the local luminosity distance measurements [58], leading to a preference for  $1 + w < 0$  [59–61]. This implies the violation of the null energy condition:  $\rho + p \geq 0$  [62–64] and the Big Rip singularity [65]. The Swampland conjecture strengthens this tension [23] and therefore it provides another test for the conjecture.

<sup>2</sup>Note added: after submission of the present paper, the refined conjecture was proposed to allow the existence of the local maxima with a sufficiently large negative curvature [70].

because its coupling to the quintessence does not spoil the flatness of the potential. On the other hand, if the quintessence potential allows a tracker-type solution in the early Universe (e.g. in the case of two exponential terms), the fluctuations of the quintessence field will be significantly suppressed as the late-time dynamics is insensitive to the initial condition.

## 2 Isocurvature perturbations

Let us adopt a simple exponential potential for the quintessence field,

$$V(\varphi) = \Lambda^4 e^{-c\varphi}, \quad (2.1)$$

which saturates the bound (1.6). Then the present value of DE should be explained by  $V(\varphi)$ .

The dynamics of  $\varphi$  with the above potential has been extensively studied in the literature (see, e.g., Ref. [8]). In the early Universe, the quintessence field is almost frozen to the initial value, if the DE density parameter satisfies  $\Omega_{\text{DE}} \ll 3/c^2$ . As the Universe expands, the energy density of matter and radiation decreases and that of the quintessence field comes to dominate over them. Its energy density at present can be fine-tuned by adjusting the initial value of  $\varphi_*$  or  $V(\varphi_*)$ . The present value of cosmological constant is many orders of magnitude smaller than the fundamental scale of physics and requires a fine-tuning in the initial condition by a factor of order  $10^{-120}$ . This is known as the cosmological constant problem, which we do not address in this Letter.

In the above discussion we have assumed that the potential of the quintessence field does not change its form in the early Universe. Here we note that the potential is generically modified during/after inflation. For instance, if the quintessence field is coupled to the standard model particles, its potential would acquire thermal corrections after reheating. Similarly, the quintessence field can acquire a mass of order the Hubble parameter during inflation if it has a gravitational coupling to the inflaton. In fact, in a context of supergravity inflation models, a scalar field generically receives such an effective mass of order the Hubble parameter during inflation for a general form of the Kähler potential. This is the so-called  $\eta$ -problem. One can avoid the  $\eta$ -problem only if the scalar mass is protected by a specific symmetry such as a shift-symmetry or the Heisenberg symmetry of no-scale supergravity, or if there is an accidental cancellation. Therefore, it depends on how we model the quintessence field in UV theories whether the mass correction is suppressed during inflation. Throughout this paper we simply assume that such corrections to the quintessence potential are negligibly small and the quintessence remains light during inflation.

It is known that even gravitational couplings to the standard model particles are tightly constrained by the equivalence principle and fifth force experiments [71–76]. If the inflaton and standard model particles are in the same sector, it may not be so unrealistic to assume that the Hubble-induced correction during inflation is also suppressed by some symmetry. Also, it is non-trivial whether or not the quintessence model works if its potential is largely deformed during inflation: the quintessence potential may be destabilized or the quintessence field might be deviated from the region that leads to the successful explanation of the current accelerated expansion. Alternatively, if the Hubble correction does not create a new local minimum, the quintessence field may continue to roll down the (modified) potential until its mass becomes smaller than the Hubble parameter where the quantum fluctuation dominates. We will discuss later a similar phenomenon in a case with double exponential terms.

Suppose the quintessence field is extremely light during inflation. Then, it acquires quantum fluctuations,

$$\delta\varphi = \frac{H_{\text{inf}}}{2\pi}. \quad (2.2)$$

This results in the isocurvature perturbation of DE, which is given by

$$\left| \frac{\delta\rho_{\text{DE}}}{\rho_{\text{DE}}} \right| \simeq c \frac{H_{\text{inf}}}{2\pi}, \quad (2.3)$$

well before it comes to dominate the Universe.<sup>3</sup> The DE isocurvature perturbation evolves afterward until present, but it does not change significantly as long as  $c$  is less than unity. If the quintessence potential is different from Eq. (2.1), we expect  $|\delta\rho_{\text{DE}}/\rho_{\text{DE}}| \simeq |\nabla V/V| \delta\phi \geq cH_{\text{inf}}/(2\pi)$ . Hence we can regard Eq. (2.3) as the most conservative estimate for models satisfying the conjecture (1.1).

The DE isocurvature affects the late-time Sachs-Wolfe effects, which appear only at large scales of the CMB anisotropies. Therefore, it is subject to the large uncertainty of the cosmic variance. There is a study on such DE isocurvature perturbations of ultralight axions in a context of the axiverse [78, 79]. According to their analysis, the DE isocurvature bound is much weaker than the DM one. However, a dedicated analysis is necessary to derive a rigid constraint, and further study is warranted.

### 3 DM interacting with quintessence field

The quintessence field may have couplings to matter fields. While its couplings to the standard model sector are tightly constrained by the fifth force experiments, it is allowed to have sizable couplings to a dark sector which may contain DM. In this Letter, we consider the case where the DM mass depends on the quintessence field,

$$m_{\text{DM}} \propto e^{-c'\varphi}. \quad (3.1)$$

This kind of model is motivated by the discussion presented in Ref. [70]. The distance swampland conjecture, which is proposed in Ref. [80], is related to the existence of a tower of massive fields in the hidden sector. According to this conjecture, a tower of massive field becomes exponentially light as a scalar field changes its field value beyond the Planck scale. Since the effective field theory breaks down when a massive field becomes lighter than an energy scale in consideration, this limits the range of the field value one can change within the effective field theory. We can think of the case where DM is made of some of these hidden fields. In this case, the mass of DM depends on the quintessence field. This is the motivation of Eq. (3.1) and hence we expect  $c' = \mathcal{O}(1)$ . Note that  $c'$  is not necessarily equal to  $c$  in Eq. (1.1).

#### 3.1 Model-dependent constraints

Possible interactions between the light quintessence field and DM are constrained from particle physics point of view. This is because the interactions generically induce quantum corrections to the quintessence potential, which may spoil the flatness of the potential. The

<sup>3</sup> See also Ref. [77], where they discussed the effect of the isocurvature perturbation of DE in the scalar-tensor theory.

potential becomes stable against radiative corrections if one requires that the one-loop corrections to the effective potential are smaller than the tree-level one. Then one obtains [81]

$$|c'| \lesssim \frac{m_\varphi}{\sqrt{G}m_{\text{DM}}^2} \simeq c \frac{H_0}{\sqrt{G}m_{\text{DM}}^2} \simeq c \left( \frac{1 \text{ meV}}{m_{\text{DM}}} \right)^2. \quad (3.2)$$

Since we expect both  $c$  and  $c'$  to be of order unity, this requires  $m_{\text{DM}} \lesssim 1 \text{ meV}$ . This is much smaller than the Tremaine-Gunn phase-space constraint on fermionic DM:  $m_{\text{DM}} \gtrsim \mathcal{O}(100 \text{ eV})$  [82] (see also Ref. [83]) and therefore the interacting fermionic DM is inconsistent with this framework.

In the case of bosonic DMs, they can be produced in the early Universe with a large occupancy number, e.g., via the misalignment mechanism, and hence can avoid the phase-space constraint. A well-motivated DM model of this kind is an axion-like particle, where its tiny mass is generated by a non-perturbative effect and a sizable energy density can be produced via the misalignment mechanism. However, since its mass is quite small, it acquires quantum fluctuations during inflation. This leads to isocurvature perturbations for DM, which is severely constrained by the Planck data as we discussed above. Several mechanisms have been proposed to suppress its fluctuations by, e.g., making the axion-like particle massive temporarily during inflation [84–100]. Alternatively, if the Peccei-Quinn symmetry is restored during inflation (or reheating epoch) and gets broken after inflation, there is no large correlation for field perturbations beyond the horizon scale. This is a simple solution to the isocurvature problem. We note however that it may suffer from the domain-wall problem depending on models [101, 102].

An interesting possibility is that the DM is a massive vector field  $A_\mu$ . The longitudinal modes are produced by quantum fluctuations during inflation just like a scalar field because of the Goldstone boson equivalence theorem in the relativistic limit. Contrarily to the transverse modes, the longitudinal modes do not lead to large anisotropies. The equivalence theorem implies that the longitudinal mode multiplied by  $m/k$  behaves like a scalar field for a large wavenumber  $k$ , which means that their fluctuations are suppressed at large scales. Thus, the vector DM avoids the isocurvature bound because isocurvature perturbations are suppressed at large scales. The abundance of vector field is calculated as [103]

$$\Omega_{\text{DM}} h^2 \simeq 0.1 \left( \frac{m_{\text{DM}}}{6 \mu\text{eV}} \right)^{1/2} \left( \frac{H_{\text{inf}}}{10^{14} \text{ GeV}} \right)^2. \quad (3.3)$$

This is consistent with the fact that the swampland conjecture favors the large-scale inflation (1.3) and the constraint of quantum corrections to the quintessence potential (3.2).<sup>4</sup>

### 3.2 Model-independent constraints

Now we shall consider constraints that arise independently of the nature of DM.

The coupled system of DM and DE is subject to various cosmological observations. The quintessence field mediates interactions between DMs, whose strength has an upper bound from the long-range self-interactions of DM [71–76]. It reads

$$|c'| \lesssim 0.3. \quad (3.4)$$

---

<sup>4</sup> The abundance can be given by Eq. (3.3) only if its tiny mass is already turned on during inflation. This can be realized when the vector field has a Stueckelberg mass. However, a new conjecture was proposed in Ref. [104], where they show that the Stueckelberg mass cannot be smaller than a certain threshold depending on a cutoff of the theory. If we take the cutoff to be larger than  $H_{\text{inf}}$ , the Stueckelberg mass need to be less than 0.3 eV according to this new conjecture.

Note that this does not apply to the case where the quintessence couples with DM only via spin-dependent interactions, e.g.  $ie^\phi\bar{\psi}\gamma_5\psi$ , where  $\psi$  is a fermionic DM.

The DM mass is time-dependent because of the interaction with the quintessence field. When  $c'$  is positive, the mass starts to decrease around the time when the cosmic expansion gets accelerated. This is similar to the decaying DM scenario as the gravitational potential decays, but it is different because the evolution is correlated with DE. The detailed analysis of the system is beyond the scope of this Letter, and further analysis is warranted. Here we simply require that the DM mass should not change by more than 10% after the matter dominated epoch. This is because, in a context of decaying DM models, the DM lifetime was constrained to be more than ten times longer than the present age of the universe by investigating amplitude of matter fluctuations  $\sigma_8$  [105, 106]. The quintessence field varies by a factor of

$$\Delta\varphi = \int_{N_{\text{eq}}}^{N_{\text{p}}} \frac{\dot{\varphi}}{H} dN \simeq 0.3c, \quad (3.5)$$

for  $c \lesssim 1$  after the matter-dominated epoch, where  $N_{\text{p}}$  and  $N_{\text{eq}}$  represent the e-folding numbers at present and at the matter-radiation equality, respectively. Thus we obtain

$$c' \lesssim 8/c, \quad (3.6)$$

from the constraint on the variation of the energy density of DM after the matter-radiation equality. It is interesting to note that the product of  $c$  and  $c'$  is constrained by the structure formation, which is complementary to (3.2).

If  $c'$  is negative, the DM mass starts to increase around the time when the cosmic expansion gets accelerated. In this case, the amplitude of matter fluctuations gets enhanced because of deeper gravitational potential of DM. Here, we note that the amplitude of matter fluctuation  $\sigma_8$  observed by a large scale structure is slightly smaller than that inferred from the CMB measurement [7]. The negative  $c'$  predicts a larger  $\sigma_8$  at present epoch, which would strengthen the discrepancy between the observations of large scale structure and CMB. On the other hand, if a subdominant component of DM interacts with the quintessence field, negative  $c'$  has an interesting cosmological scenario (see, e.g., Refs. [107, 107–110]).

The isocurvature perturbations of DM are induced by the coupling to the quintessence field with the fluctuation  $\delta\varphi = H_{\text{inf}}/(2\pi)$  as

$$\left| \frac{\delta\rho_{\text{DM}}}{\rho_{\text{DM}}} \right| = \left| \frac{\delta m_{\text{DM}}}{m_{\text{DM}}} \right| = |c'| \frac{H_{\text{inf}}}{2\pi}. \quad (3.7)$$

The Planck observations set a tight bound on the uncorrelated DM isocurvature as [111]

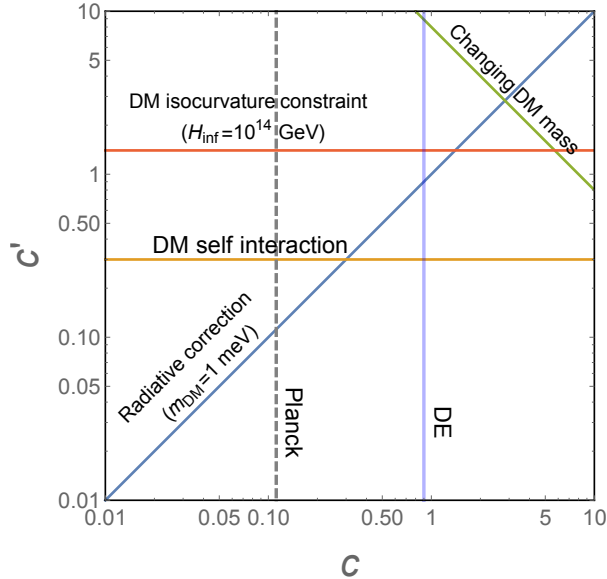
$$\beta_{\text{iso}} \equiv \frac{\mathcal{P}_{II}}{\mathcal{P}_{RR} + \mathcal{P}_{II}} < 0.038 \quad (95\% \text{ CL}), \quad (3.8)$$

where  $\beta_{\text{iso}}$  is the ratio of the isocurvature power spectrum to the total (adiabatic  $\mathcal{P}_{RR}$  plus isocurvature  $\mathcal{P}_{II}$ ) power spectrum. This leads to a bound on  $c'$ :

$$|c'| < 1.4 \left( \frac{10^{14} \text{ GeV}}{H_{\text{inf}}} \right). \quad (3.9)$$

Note that this bound on  $c'$  is complementary to the one derived by non-observation of the primordial gravitational waves (1.5). For a smaller value of  $H_{\text{inf}}$ , the former becomes weaker





**Figure 1.** Constraints on the parameters,  $c$  and  $c'$ , in the swampland conjecture. See Eqs. (1.1) and (3.1) for their definitions. The two vertical lines are the upper bound on  $c$  and the other ones are the upper bound on  $c'$ : CMB temperature anisotropies by Planck (gray dashed line), DE equation of state (light blue line), radiative correction (dark blue line), DM self interaction (orange line), time-dependent DM mass (green line), and DM isocurvature constraint (red line). We set  $m_{\text{DM}} = 1$  meV and  $H_{\text{inf}} = 10^{14}$  GeV as reference parameters.

while the latter gets tighter. These isocurvature perturbations comes from the fluctuation of the quintessence field, so that they are independent of the isocurvature modes of the fluctuation of DM itself that are discussed in Sec. 3.1.

We summarize the constraints on  $c$  and  $c'$  in Fig. 1. The gray line is the upper bound on  $c$  from the observation of CMB temperature fluctuations by Planck, which is given by Eq. (1.5). The light blue line, denoted as DE, is the constraint from the equation of state for dark energy in the quintessence model given by Eq. (1.6). This is an upper bound on  $c$ . The other four lines are the upper bound on  $c'$  from the radiative correction on quintessence potential (dark blue line, Eq. (3.2)), DM self interaction mediated by the quintessence (orange line, Eq. (3.4)), the time-dependent DM mass induced by the dynamics of quintessence (green line, Eq. (3.6)), and DM isocurvature perturbations generated by the fluctuations of quintessence (red line, Eq. (3.9)). The constraints from radiative correction and DM isocurvature perturbations depend on the DM mass and the Hubble parameter during inflation, respectively, and we set  $m_{\text{DM}} = 1$  meV and  $H_{\text{inf}} = 10^{14}$  GeV as reference parameters.

## 4 Discussion and conclusions

The constraints from the isocurvature perturbations can be avoided by introducing another exponential term in the quintessence potential with a large coefficient in the exponent, such as  $V(\varphi) = \Lambda_1^4 e^{-c_1 \varphi} + \Lambda_2^4 e^{-c_2 \varphi}$  [112]. When  $c_2 \gg 1$ , the field  $\varphi$  has an attractor solution with the density parameter  $\Omega_{\text{DE}} = 3/c_2^2$ , which removes the dependence of the DE on the initial condition [113]. In this case the primordial fluctuation of  $\varphi$  does not affect the present value

of DE and the isocurvature perturbations are absent [114–116]. The DE energy density at the present value is realized by the fine-tuning of parameters in its potential.

In this Letter we have applied the Swampland conjecture on the potential gradient to both inflation and quintessence, and studied its implication for isocurvature perturbations of DE and DM. In particular, if  $c = \mathcal{O}(1)$  is taken at face value, it gives a preference to high-scale inflation which almost saturates the current upper bound on the tensor-to-scalar ratio. For such high-scale inflation, the quintessence field generically acquire large quantum fluctuations during inflation, which may results in isocurvature perturbation of DE. However, the current bound on isocurvature perturbation of DE is weak and does not give a meaningful bound on  $c'$ .

We have also studied the case in which the quintessence field is coupled to the mass term of DM. In this case, CDM isocurvature perturbation is similarly induced. The DM mass should be smaller than meV to avoid producing too large radiative corrections to the quintessence potential. This excludes a possibility of fermionic DM. Among bosonic DM candidates, we find that vector DM with mass  $\lesssim$  meV is an excellent candidate, because it is known that the right abundance of massive vector fields is naturally produced by quantum fluctuations during inflation, while isocurvature perturbations on large scales are suppressed. The vector DM has been an active target of various proposed experiments [117–122].

## Acknowledgments

F.T. thanks Mohammad Hossein Namjoo and Alan H. Guth for useful discussion. F.T. thanks the hospitality of MIT Center for Theoretical Physics and Tufts Institute of Cosmology where the present work was done. This work is partially supported by JSPS KAKENHI Grant Numbers JP15H05889 (F.T.), JP15K21733 (F.T.), JP17H02878 (F.T.), and JP17H02875 (H.M. and F.T.), Leading Young Researcher Overseas Visit Program at Tohoku University (F.T.), and by World Premier International Research Center Initiative (WPI Initiative), MEXT, Japan (F.T.).

## References

- [1] A. A. Starobinsky, *Spectrum of relict gravitational radiation and the early state of the universe*, *JETP Lett.* **30** (1979) 682.
- [2] D. Kazanas, *Dynamics of the Universe and Spontaneous Symmetry Breaking*, *Astrophys. J.* **241** (1980) L59.
- [3] K. Sato, *First Order Phase Transition of a Vacuum and Expansion of the Universe*, *Mon. Not. Roy. Astron. Soc.* **195** (1981) 467.
- [4] A. H. Guth, *The Inflationary Universe: A Possible Solution to the Horizon and Flatness Problems*, *Phys. Rev.* **D23** (1981) 347.
- [5] A. D. Linde, *A New Inflationary Universe Scenario: A Possible Solution of the Horizon, Flatness, Homogeneity, Isotropy and Primordial Monopole Problems*, *Phys. Lett.* **108B** (1982) 389.
- [6] A. Albrecht and P. J. Steinhardt, *Cosmology for Grand Unified Theories with Radiatively Induced Symmetry Breaking*, *Phys. Rev. Lett.* **48** (1982) 1220.

- [7] PLANCK collaboration, N. Aghanim et al., *Planck 2018 results. VI. Cosmological parameters*, [1807.06209](#).
- [8] P. Agrawal, G. Obied, P. J. Steinhardt and C. Vafa, *On the Cosmological Implications of the String Swampland*, *Phys. Lett.* **B784** (2018) 271 [[1806.09718](#)].
- [9] G. W. Gibbons, *Thoughts on tachyon cosmology*, *Class. Quant. Grav.* **20** (2003) S321 [[hep-th/0301117](#)].
- [10] J. M. Maldacena and C. Nunez, *Supergravity description of field theories on curved manifolds and a no go theorem*, *Int. J. Mod. Phys.* **A16** (2001) 822 [[hep-th/0007018](#)].
- [11] K. Dasgupta, R. Gwyn, E. McDonough, M. Mia and R. Tatar, *de Sitter Vacua in Type IIB String Theory: Classical Solutions and Quantum Corrections*, *JHEP* **07** (2014) 054 [[1402.5112](#)].
- [12] D. Kutasov, T. Maxfield, I. Melnikov and S. Sethi, *Constraining de Sitter Space in String Theory*, *Phys. Rev. Lett.* **115** (2015) 071305 [[1504.00056](#)].
- [13] U. H. Danielsson and T. Van Riet, *What if string theory has no de Sitter vacua?*, *Int. J. Mod. Phys.* **D27** (2018) 1830007 [[1804.01120](#)].
- [14] E. Witten, *Quantum gravity in de Sitter space*, in *Strings 2001: International Conference Mumbai, India, January 5-10, 2001*, 2001, [hep-th/0106109](#).
- [15] M. P. Hertzberg, S. Kachru, W. Taylor and M. Tegmark, *Inflationary Constraints on Type IIA String Theory*, *JHEP* **12** (2007) 095 [[0711.2512](#)].
- [16] D. Andriot, *On the de Sitter swampland criterion*, *Phys. Lett.* **B785** (2018) 570 [[1806.10999](#)].
- [17] S. Banerjee, U. Danielsson, G. Dibitetto, S. Giri and M. Schillo, *Emergent de Sitter cosmology from decaying AdS*, [1807.01570](#).
- [18] A. Achucarro and G. A. Palma, *The string swampland constraints require multi-field inflation*, [1807.04390](#).
- [19] S. K. Garg and C. Krishnan, *Bounds on Slow Roll and the de Sitter Swampland*, [1807.05193](#).
- [20] A. Kehagias and A. Riotto, *A note on Inflation and the Swampland*, [1807.05445](#).
- [21] J.-L. Lehners, *Small-Field and Scale-Free: Inflation and Ekpyrosis at their Extremes*, [1807.05240](#).
- [22] M. Dias, J. Frazer, A. Retolaza and A. Westphal, *Primordial Gravitational Waves and the Swampland*, [1807.06579](#).
- [23] E. O. Colgain, M. H. P. M. Van Putten and H. Yavartanoo,  *$H_0$  tension and the de Sitter Swampland*, [1807.07451](#).
- [24] C. Roupec and T. Wrase, *de Sitter extrema and the swampland*, [1807.09538](#).
- [25] D. Andriot, *New constraints on classical de Sitter: flirting with the swampland*, [1807.09698](#).
- [26] H. Matsui and F. Takahashi, *Eternal Inflation and Swampland Conjectures*, [1807.11938](#).
- [27] I. Ben-Dayan, *Draining the Swampland*, [1808.01615](#).
- [28] W. H. Kinney, S. Vagnozzi and L. Visinelli, *The Zoo Plot Meets the Swampland: Mutual (In)Consistency of Single-Field Inflation, String Conjectures, and Cosmological Data*, [1808.06424](#).
- [29] K. Dasgupta, M. Emelin, E. McDonough and R. Tatar, *Quantum Corrections and the de Sitter Swampland Conjecture*, [1808.07498](#).
- [30] M. C. D. Marsh, *The Swampland, Quintessence and the Vacuum Energy*, [1809.00726](#).
- [31] M. Cicoli, S. De Alwis, A. Maharana, F. Muia and F. Quevedo, *De Sitter vs Quintessence in String Theory*, [1808.08967](#).

- [32] Y. Akrami, R. Kallosh, A. Linde and V. Vardanyan, *The landscape, the swampland and the era of precision cosmology*, [1808.09440](#).
- [33] L. Heisenberg, M. Bartelmann, R. Brandenberger and A. Refregier, *Dark Energy in the Swampland II*, [1809.00154](#).
- [34] S. Brahma and M. Wali Hossain, *Avoiding the string swampland in single-field inflation: Excited initial states*, [1809.01277](#).
- [35] K. Choi, D. Chway and C. S. Shin, *The dS swampland conjecture with the electroweak symmetry and QCD chiral symmetry breaking*, [1809.01475](#).
- [36] S. Das, *A note on Single-field Inflation and the Swampland Criteria*, [1809.03962](#).
- [37] K. Dimopoulos, *Steep Eternal Inflation and the Swampland*, [1810.03438](#).
- [38] S. D. Odintsov and V. K. Oikonomou, *Finite-time Singularities in Swampland-related Dark Energy Models*, [1810.03575](#).
- [39] A. Ashoorioon, *Rescuing Single Field Inflation from the Swampland*, [1810.04001](#).
- [40] S. Das, *Warm Inflation in the light of Swampland Criteria*, [1810.05038](#).
- [41] S.-J. Wang, *Quintessential Starobinsky inflation and swampland criteria*, [1810.06445](#).
- [42] Y. Olguin-Trejo, S. L. Parameswaran, G. Tasinato and I. Zavala, *Runaway Quintessence, Out of the Swampland*, [1810.08634](#).
- [43] C. Wetterich, *Cosmology and the Fate of Dilatation Symmetry*, *Nucl. Phys.* **B302** (1988) 668 [[1711.03844](#)].
- [44] Y. Fujii, *Origin of the Gravitational Constant and Particle Masses in Scale Invariant Scalar - Tensor Theory*, *Phys. Rev.* **D26** (1982) 2580.
- [45] L. H. Ford, *COSMOLOGICAL CONSTANT DAMPING BY UNSTABLE SCALAR FIELDS*, *Phys. Rev.* **D35** (1987) 2339.
- [46] P. J. E. Peebles and B. Ratra, *Cosmology with a Time Variable Cosmological Constant*, *Astrophys. J.* **325** (1988) L17.
- [47] B. Ratra and P. J. E. Peebles, *Cosmological Consequences of a Rolling Homogeneous Scalar Field*, *Phys. Rev.* **D37** (1988) 3406.
- [48] Y. Fujii and T. Nishioka, *Model of a Decaying Cosmological Constant*, *Phys. Rev.* **D42** (1990) 361.
- [49] T. Chiba, N. Sugiyama and T. Nakamura, *Cosmology with  $x$  matter*, *Mon. Not. Roy. Astron. Soc.* **289** (1997) L5 [[astro-ph/9704199](#)].
- [50] P. G. Ferreira and M. Joyce, *Structure formation with a selftuning scalar field*, *Phys. Rev. Lett.* **79** (1997) 4740 [[astro-ph/9707286](#)].
- [51] P. G. Ferreira and M. Joyce, *Cosmology with a primordial scaling field*, *Phys. Rev.* **D58** (1998) 023503 [[astro-ph/9711102](#)].
- [52] E. J. Copeland, A. R. Liddle and D. Wands, *Exponential potentials and cosmological scaling solutions*, *Phys. Rev.* **D57** (1998) 4686 [[gr-qc/9711068](#)].
- [53] R. R. Caldwell, R. Dave and P. J. Steinhardt, *Cosmological imprint of an energy component with general equation of state*, *Phys. Rev. Lett.* **80** (1998) 1582 [[astro-ph/9708069](#)].
- [54] S. M. Carroll, *Quintessence and the rest of the world*, *Phys. Rev. Lett.* **81** (1998) 3067 [[astro-ph/9806099](#)].
- [55] I. Zlatev, L.-M. Wang and P. J. Steinhardt, *Quintessence, cosmic coincidence, and the cosmological constant*, *Phys. Rev. Lett.* **82** (1999) 896 [[astro-ph/9807002](#)].

- [56] P. J. Steinhardt, L.-M. Wang and I. Zlatev, *Cosmological tracking solutions*, *Phys. Rev.* **D59** (1999) 123504 [[astro-ph/9812313](#)].
- [57] L. Heisenberg, M. Bartelmann, R. Brandenberger and A. Refregier, *Dark Energy in the Swampland*, [1808.02877](#).
- [58] A. G. Riess, S. Casertano, W. Yuan, L. Macri, J. Anderson, J. W. MacKenty et al., *New parallaxes of galactic cepheids from spatially scanning the hubble space telescope : Implications for the hubble constant*, *The Astrophysical Journal* **855** (2018) 136.
- [59] E. Di Valentino, A. Melchiorri and J. Silk, *Reconciling Planck with the local value of  $H_0$  in extended parameter space*, *Phys. Lett.* **B761** (2016) 242 [[1606.00634](#)].
- [60] Q.-G. Huang and K. Wang, *How the dark energy can reconcile Planck with local determination of the Hubble constant*, *Eur. Phys. J.* **C76** (2016) 506 [[1606.05965](#)].
- [61] G.-B. Zhao et al., *Dynamical dark energy in light of the latest observations*, *Nat. Astron.* **1** (2017) 627 [[1701.08165](#)].
- [62] S. M. Carroll, M. Hoffman and M. Trodden, *Can the dark energy equation - of - state parameter  $w$  be less than  $-1$ ?*, *Phys. Rev.* **D68** (2003) 023509 [[astro-ph/0301273](#)].
- [63] J. M. Cline, S. Jeon and G. D. Moore, *The Phantom menaced: Constraints on low-energy effective ghosts*, *Phys. Rev.* **D70** (2004) 043543 [[hep-ph/0311312](#)].
- [64] S. Dubovsky, T. Gregoire, A. Nicolis and R. Rattazzi, *Null energy condition and superluminal propagation*, *JHEP* **03** (2006) 025 [[hep-th/0512260](#)].
- [65] R. R. Caldwell, M. Kamionkowski and N. N. Weinberg, *Phantom energy and cosmic doomsday*, *Phys. Rev. Lett.* **91** (2003) 071301 [[astro-ph/0302506](#)].
- [66] T. D. Brennan, F. Carta and C. Vafa, *The String Landscape, the Swampland, and the Missing Corner*, *PoS TASI2017* (2017) 015 [[1711.00864](#)].
- [67] F. Denef, A. Hebecker and T. Wrase, *The dS swampland conjecture and the Higgs potential*, [1807.06581](#).
- [68] H. Murayama, M. Yamazaki and T. T. Yanagida, *Do We Live in the Swampland?*, [1809.00478](#).
- [69] C. Han, S. Pi and M. Sasaki, *Quintessence Saves Higgs Instability*, [1809.05507](#).
- [70] H. Ooguri, E. Palti, G. Shiu and C. Vafa, *Distance and de Sitter Conjectures on the Swampland*, [1810.05506](#).
- [71] J. A. Frieman and B.-A. Gradwohl, *Dark matter and the equivalence principle*, *Phys. Rev. Lett.* **67** (1991) 2926.
- [72] B.-A. Gradwohl and J. A. Frieman, *Dark matter, long range forces, and large scale structure*, *Astrophys. J.* **398** (1992) 407.
- [73] J. A. Frieman and B. A. Gradwohl, *Dark matter and the equivalence principle*, *Science* **260** (1993) 1441.
- [74] S. S. Gubser and P. J. E. Peebles, *Structure formation in a string inspired modification of the cold dark matter model*, *Phys. Rev.* **D70** (2004) 123510 [[hep-th/0402225](#)].
- [75] S. S. Gubser and P. J. E. Peebles, *Cosmology with a dynamically screened scalar interaction in the dark sector*, *Phys. Rev.* **D70** (2004) 123511 [[hep-th/0407097](#)].
- [76] A. Nusser, S. S. Gubser and P. J. E. Peebles, *Structure formation with a long-range scalar dark matter interaction*, *Phys. Rev.* **D71** (2005) 083505 [[astro-ph/0412586](#)].
- [77] D. Paoletti, M. Braglia, F. Finelli, M. Ballardini and C. Umilta, *Isocurvature fluctuations in the effective Newton's constant*, [1809.03201](#).

- [78] J. Liu, M. Li and X. Zhang, *On Dark Energy Isocurvature Perturbation*, *JCAP* **1106** (2011) 028 [[1011.6146](#)].
- [79] R. Hlozek, D. J. E. Marsh and D. Grin, *Using the Full Power of the Cosmic Microwave Background to Probe Axion Dark Matter*, *Mon. Not. Roy. Astron. Soc.* **476** (2018) 3063 [[1708.05681](#)].
- [80] H. Ooguri and C. Vafa, *On the Geometry of the String Landscape and the Swampland*, *Nucl. Phys.* **B766** (2007) 21 [[hep-th/0605264](#)].
- [81] G. D’Amico, T. Hamill and N. Kaloper, *Quantum field theory of interacting dark matter and dark energy: Dark monodromies*, *Phys. Rev.* **D94** (2016) 103526 [[1605.00996](#)].
- [82] S. Tremaine and J. E. Gunn, *Dynamical Role of Light Neutral Leptons in Cosmology*, *Phys. Rev. Lett.* **42** (1979) 407.
- [83] J. J. Dalcanton and C. J. Hogan, *Halo cores and phase space densities: Observational constraints on dark matter physics and structure formation*, *Astrophys. J.* **561** (2001) 35 [[astro-ph/0004381](#)].
- [84] A. D. Linde and D. H. Lyth, *Axionic domain wall production during inflation*, *Phys. Lett.* **B246** (1990) 353.
- [85] A. D. Linde, *Axions in inflationary cosmology*, *Phys. Lett.* **B259** (1991) 38.
- [86] D. H. Lyth and E. D. Stewart, *Axions and inflation: String formation during inflation*, *Phys. Rev.* **D46** (1992) 532.
- [87] S. Kasuya, M. Kawasaki and T. Yanagida, *Cosmological axion problem in chaotic inflationary universe*, *Phys. Lett.* **B409** (1997) 94 [[hep-ph/9608405](#)].
- [88] M. Dine and A. Anisimov, *Is there a Peccei-Quinn phase transition?*, *JCAP* **0507** (2005) 009 [[hep-ph/0405256](#)].
- [89] S. Folkerts, C. Germani and J. Redondo, *Axion Dark Matter and Planck favor non-minimal couplings to gravity*, *Phys. Lett.* **B728** (2014) 532 [[1304.7270](#)].
- [90] K. S. Jeong and F. Takahashi, *Suppressing Isocurvature Perturbations of QCD Axion Dark Matter*, *Phys. Lett.* **B727** (2013) 448 [[1304.8131](#)].
- [91] T. Higaki, K. S. Jeong and F. Takahashi, *Solving the Tension between High-Scale Inflation and Axion Isocurvature Perturbations*, *Phys. Lett.* **B734** (2014) 21 [[1403.4186](#)].
- [92] M. Dine and L. Stephenson-Haskins, *Hybrid Inflation with Planck Scale Fields*, *JHEP* **09** (2015) 208 [[1408.0046](#)].
- [93] K. Nakayama and M. Takimoto, *Higgs inflation and suppression of axion isocurvature perturbation*, *Phys. Lett.* **B748** (2015) 108 [[1505.02119](#)].
- [94] K. Harigaya, M. Ibe, M. Kawasaki and T. T. Yanagida, *Dynamics of Peccei-Quinn Breaking Field after Inflation and Axion Isocurvature Perturbations*, *JCAP* **1511** (2015) 003 [[1507.00119](#)].
- [95] K. Choi, E. J. Chun, S. H. Im and K. S. Jeong, *Diluting the inflationary axion fluctuation by a stronger QCD in the early Universe*, *Phys. Lett.* **B750** (2015) 26 [[1505.00306](#)].
- [96] M. Kawasaki, M. Yamada and T. T. Yanagida, *Cosmologically safe QCD axion as a present from extra dimension*, *Phys. Lett.* **B750** (2015) 12 [[1506.05214](#)].
- [97] F. Takahashi and M. Yamada, *Strongly broken Peccei-Quinn symmetry in the early Universe*, *JCAP* **1510** (2015) 010 [[1507.06387](#)].
- [98] M. Kawasaki, F. Takahashi and M. Yamada, *Suppressing the QCD Axion Abundance by Hidden Monopoles*, *Phys. Lett.* **B753** (2016) 677 [[1511.05030](#)].

- [99] P. Agrawal, G. Marques-Tavares and W. Xue, *Opening up the QCD axion window*, *JHEP* **03** (2018) 049 [[1708.05008](#)].
- [100] M. Kawasaki, F. Takahashi and M. Yamada, *Adiabatic suppression of the axion abundance and isocurvature due to coupling to hidden monopoles*, *JHEP* **01** (2018) 053 [[1708.06047](#)].
- [101] Ya. B. Zeldovich, I. Yu. Kobzarev and L. B. Okun, *Cosmological Consequences of the Spontaneous Breakdown of Discrete Symmetry*, *Zh. Eksp. Teor. Fiz.* **67** (1974) 3.
- [102] P. Sikivie, *Of Axions, Domain Walls and the Early Universe*, *Phys. Rev. Lett.* **48** (1982) 1156.
- [103] P. W. Graham, J. Mardon and S. Rajendran, *Vector Dark Matter from Inflationary Fluctuations*, *Phys. Rev.* **D93** (2016) 103520 [[1504.02102](#)].
- [104] M. Reece, *Photon Masses in the Landscape and the Swampland*, [1808.09966](#).
- [105] B. Audren, J. Lesgourgues, G. Mangano, P. D. Serpico and T. Tram, *Strongest model-independent bound on the lifetime of Dark Matter*, *JCAP* **1412** (2014) 028 [[1407.2418](#)].
- [106] K. Enqvist, S. Nadathur, T. Sekiguchi and T. Takahashi, *Decaying dark matter and the tension in  $\sigma_8$* , *JCAP* **1509** (2015) 067 [[1505.05511](#)].
- [107] L. Amendola, M. Baldi and C. Wetterich, *Quintessence cosmologies with a growing matter component*, *Phys. Rev.* **D78** (2008) 023015 [[0706.3064](#)].
- [108] F. Marulli, M. Baldi and L. Moscardini, *Clustering and redshift-space distortions in interacting dark energy cosmologies*, *Mon. Not. Roy. Astron. Soc.* **420** (2012) 2377 [[1110.3045](#)].
- [109] M. Baldi and P. Salucci, *Constraints on interacting dark energy models from galaxy Rotation Curves*, *JCAP* **1202** (2012) 014 [[1111.3953](#)].
- [110] B. Wang, E. Abdalla, F. Atrio-Barandela and D. Pavon, *Dark Matter and Dark Energy Interactions: Theoretical Challenges, Cosmological Implications and Observational Signatures*, *Rept. Prog. Phys.* **79** (2016) 096901 [[1603.08299](#)].
- [111] PLANCK collaboration, Y. Akrami et al., *Planck 2018 results. X. Constraints on inflation*, [1807.06211](#).
- [112] T. Barreiro, E. J. Copeland and N. J. Nunes, *Quintessence arising from exponential potentials*, *Phys. Rev.* **D61** (2000) 127301 [[astro-ph/9910214](#)].
- [113] T. Chiba, A. De Felice and S. Tsujikawa, *Observational constraints on quintessence: thawing, tracker, and scaling models*, *Phys. Rev.* **D87** (2013) 083505 [[1210.3859](#)].
- [114] L. R. W. Abramo and F. Finelli, *Attractors and isocurvature perturbations in quintessence models*, *Phys. Rev.* **D64** (2001) 083513 [[astro-ph/0101014](#)].
- [115] M. Kawasaki, T. Moroi and T. Takahashi, *Cosmic microwave background anisotropy with cosine type quintessence*, *Phys. Rev.* **D64** (2001) 083009 [[astro-ph/0105161](#)].
- [116] M. Kawasaki, T. Moroi and T. Takahashi, *Isocurvature fluctuations in tracker quintessence models*, *Phys. Lett.* **B533** (2002) 294 [[astro-ph/0108081](#)].
- [117] S. R. Parker, J. G. Hartnett, R. G. Povey and M. E. Tobar, *Cryogenic resonant microwave cavity searches for hidden sector photons*, *Phys. Rev.* **D88** (2013) 112004 [[1410.5244](#)].
- [118] S. Chaudhuri, P. W. Graham, K. Irwin, J. Mardon, S. Rajendran and Y. Zhao, *Radio for hidden-photon dark matter detection*, *Phys. Rev.* **D92** (2015) 075012 [[1411.7382](#)].
- [119] B. Dobrich et al., *The FUNK search for Hidden Photon Dark Matter in the eV range*, in *Photon 2015: International Conference on the Structure and Interactions of the Photon and 21th International Workshop on Photon-Photon Collisions and International Workshop on High Energy Photon Linear Colliders Novosibirsk, Russia, June 15-19, 2015*, 2015, [1510.05869](#).

- [120] M. Silva-Feaver et al., *Design Overview of DM Radio Pathfinder Experiment*, *IEEE Trans. Appl. Supercond.* **27** (2017) 1400204 [[1610.09344](#)].
- [121] I. M. Bloch, R. Essig, K. Tobioka, T. Volansky and T.-T. Yu, *Searching for Dark Absorption with Direct Detection Experiments*, *JHEP* **06** (2017) 087 [[1608.02123](#)].
- [122] M. Baryakhtar, J. Huang and R. Lasenby, *Axion and hidden photon dark matter detection with multilayer optical haloscopes*, *Phys. Rev.* **D98** (2018) 035006 [[1803.11455](#)].