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High Strength Steel Square and Rectangular Tubular Stub Columns Infilled with Concrete

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Abstract: This paper presents the experimental and numerical investigations of high strength steel square and rectangular tubular stub columns infilled with concrete. Firstly, a series of tests was conducted on cold-formed high strength steel (CFHSS) square and rectangular tubular sections infilled with three different concrete compressive strengths, i.e., 40, 80 and 120 MPa. The CFHSS tubular sections had the nominal 0.2% proof stress (yield stress) up to 900 MPa. Secondly, an extensive numerical study accounting for the confinement effect, as well as the non-linearities of materials, geometry and contacts was performed. Upon validation against the test results, a parametric investigation was conducted. The structural behaviour of concrete-filled CFHSS stub columns was investigated, including the ultimate load, end shortening, strength enhancement index and ductility index. Finally, the experimental and numerical results were used to assess the suitability of the design rules specified in the current American Specification (AISC) and European Code (EC4) for the compressive strength of the concrete-filled CFHSS square and rectangular stub columns. It was found that the predictions from EC4 were generally unconservative while those from the AISC were conservative. However, the predictions by EC4 became conservative if the effective strength of infilled concrete or the effective area of outer steel tubes were considered in the design. In addition, the predictions by EC4 became less scattered for different infilled concrete strengths when the effective concrete strengths were used. However, using the effective concrete strengths or the effective areas did not lead to the improvements of for the AISC specifications.

Keywords: Concrete-filled steel tube; experimental investigation; high strength steel; numerical investigation; square and rectangular hollow sections.

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41 1. Introduction

42 Concrete-filled steel tubular (CFST) members have been used widely in the construction industry for
43 their excellent structural performance. They have been used as mega columns in super high-rise
44 buildings [1], chord members in composite arch bridges [2], piles in floodwall structures [3], bridge
45 piers [4] as well as submarine pipeline structures [5-6]. Their excellent structural performance is
46 mainly benefited from the synergistic interactions between the inner concrete and the outer steel tube;
47 for example, the steel tube provides confinement to the infilled concrete while the infilled concrete
48 prevents the inward buckling and delays the local buckling of the steel tube [7]. These contribute to
49 the structural behaviour of the concrete-filled members, e.g., increased bearing capacity and ductility
50 for concrete-filled steel columns under axial loading condition. Hence, CFST steel columns may
51 provide more economic efficiency than pure structural steel or reinforced concrete columns due to
52 the reduced column size and increased effective space in buildings [8-9].

53 In the last few decades, experimental, numerical and analytical investigations have been carried out
54 on the structural behaviour and practical applications of CFST columns under various loading
55 conditions, as summarized in the recent literature [9-16]. There are two common methods to improve
56 the load resistance of CFST columns [17] - by increasing the cross-section areas or using high strength
57 materials. The first method might be impractical or uneconomic because the increased area will
58 induce larger structural weight with less usable area and subsequently increase the cost of foundation.
59 The second method of using high strength materials such as high strength steel and concrete could be
60 a more effective way. In addition, the use of high strength steel allows for larger strain ranges of
61 elastic behaviour and thus improving the confinement to the infilled concrete core [9].

62 With the advancements in material and fabrication techniques, high strength steels and concrete
63 become available nowadays, for examples, in terms of the yield stress (f_y) of steel tubes greater than
64 1100 MPa [18] and the compressive strength of concrete (f_{ck}) up to 190 MPa [19]. These
65 developments in individual constituent components have driven the investigations on the behaviour
66 and design of higher performance composite structures, such as high strength steel tubes infilled with
67 high strength concrete [17, 19-21]. A recent review by Liew *et al.* [9] on the CFST columns with over
68 2030 test results showed that more than 70% of the test data using normal strength concrete with f_{ck}
69 not greater than 50 MPa, and over 90% of the data using mild steel with f_y not greater than 460 MPa.
70 It should be noted that, up to date, investigations on the high strength steel tubes infilled with high
71 strength concrete are relatively limited.

72 Design of CFST columns are available in current international design specifications, such as the
73 “Eurocode 4: Design of Composite Steel and Concrete Structures - Part 1.1: General Rules and Rules
74 for Buildings” (EC4) [22], the American Specification for Structural Steel Buildings (AISC) [23], the
75 Japanese specification of “Recommendations for design and construction of concrete filled steel
76 tubular structures” (AIJ) [24] and Australian/New Zealand Standard of “Composite structures -
77 Composite steel-concrete construction in buildings” (AS/NZS2327) [25]. It should be noted that
78 limitations of the design rules are specified in these specifications, in particular on the yield stress of
79 steel and the compressive strength of concrete. However, the design of high strength square and

80 rectangular steel tubes infilled with high strength concrete are not explicitly specified in these design
81 codes [22-25], for example, for columns with $f_y \geq 900$ MPa and $f_{ck} \geq 80$ MPa. This will be discussed
82 further in the later section of this paper.

83 In this study, experimental and numerical investigations were carried out on the structural behaviour
84 of concrete-filled cold-formed high strength steel (CFHSS) square and rectangular stub columns.
85 Firstly, a comprehensive test program consisting of 34 specimens was carried out. The specimens
86 were designed with CFHSS square and rectangular tubes infilled with three different compressive
87 cylinder strengths (40, 80 and 120 MPa) of concrete. The CFHSS tubular sections had the nominal
88 0.2% proof stress ($f_{0.2}$) up to 900 MPa. The test specimens were subjected to uniform axial
89 compression. The ultimate loads and failure modes were obtained. Secondly, an extensive numerical
90 study accounting for the confinement effect, as well as the non-linearities of materials, geometry and
91 contacts was performed. After a successful model validation against test results, a parametric study
92 was conducted by using the validated numerical model. The specimens in the parametric study were
93 designed to cover a wide range of the cross-section dimensions and section slenderness of the CFHSS
94 tubes that infilled with different strengths of concrete. The structural behaviour of concrete-filled
95 CFHSS stub columns was investigated, including the ultimate load, end shortening, strength
96 enhancement index and ductility index. Finally, the experimental and numerical results were used to
97 assess the suitability of the design rules specified in the current international specifications (EC4 [22]
98 and AISC360-10 [23]).

99

100 2. Test program

101 2.1 Material properties

102 The CFHSS square and rectangular tubes were used as the outer skin of the concrete-filled steel stub
103 column specimens. The nominal dimensions ($H \times B \times t$) of the steel tubes were 80×80×4.0 mm,
104 100×50×4.0 mm, 100×100×4.0 mm, 120×120×4.0 mm, 140×140×5.0 mm and 160×160×4.0 mm,
105 where H , B and t are the outer depth, width and thickness of the tubes, respectively, as illustrated in
106 [Figure 1](#). The steel tubes of 80×80×4.0 mm and 100×100×4.0 mm had the nominal 0.2% proof stress
107 ($f_{0.2}$) of 700 and 900 MPa, the steel tubes of 100×50×4.0 mm, 140×140×5.0 mm and 160×160×4.0
108 mm had the $f_{0.2}$ of 700 MPa and the steel tubes of 120×120×4.0 mm had the $f_{0.2}$ of 900 MPa. The
109 CFHSS tubes were divided into two groups based on the nominal value of $f_{0.2}$, as shown in [Table 1](#),
110 where in the tube labelling, the letter “A” followed the hyphen of the section legend represents $f_{0.2} =$
111 700 MPa, and the letter “B” stands for $f_{0.2} = 900$ MPa.

112 The coupons were machined from the tubes at 90° angle from the weld. The nominal gauge length
113 and width of the tensile coupons were 25 mm and 6 mm, respectively [18]. The coupon specimens
114 were tested in a 50-kN MTS testing machine. Two linear strain gauges were adhered on both faces at
115 the middle of the coupon. An extensometer was mounted on the coupons over a gauge length of 25
116 mm. Displacement control test method was used with loading rates of 0.05 mm/min and 0.5 mm/min
117 for the elastic range and plastic range, respectively. The results from the strain gauges were used to

118 determine the Young's modulus (E_s) of the coupon specimens. The stress-strain curves of the CFHSS
119 tubular members are shown in [Figures 2\(a\)-\(b\)](#) for the members with nominal $f_{0.2}$ of 700 MPa and
120 900 MPa, respectively. The rest of the material properties were determined from the stress-strain
121 curves that measured by the extensometer. The results from coupon tests are presented in [Table 1](#),
122 including the E_s , $f_{0.2}$, the ultimate strength (f_u), the strain at ultimate (ϵ_u), and the strain at fracture (ϵ_f).

123 Three different mixes of concrete (C40, C80 and C120) with the respective nominal compressive
124 cylinder strengths (f_{ck}) of 40 MPa, 80 MPa and 120 MPa were prepared to infill the steel tubes.
125 Concrete cylinders were prepared to determine the concrete strengths. The concrete cylinder had the
126 nominal diameter of 150 mm and height of 300 mm. The cylinder tests were conducted in accordance
127 with the procedures in the ACI [26]. Two series of cylinder compression tests were conducted to
128 obtain the cylinder strength (f_{ck}), one on the 28th day after casting and the other on the date of the
129 corresponding stub column tests [27]. The average test results of the different concrete mixes are
130 presented in [Table 2](#).

131

132 2.2 Test specimens

133 A series of concrete-filled CFHSS square and rectangular stub column specimens were designed by
134 using the aforementioned seven types of CFHSS tubes ([Table 1](#)) as the outer skin. Each series of tubes
135 were infilled with those three different mixes of concrete ([Table 2](#)), namely, C40, C80 and C120. In
136 addition, to reflect the effects of infilled concrete in the same specimen series, the CFHSS square and
137 rectangular stub columns without infilled concrete were also designed. Hence, there are 34 stub
138 column specimens in this study, including two repeated specimens, as shown in [Tables 3-4](#) for the
139 steel grades of outer tubes in Series A and B, respectively. The parameters of the specimens mainly
140 included the variations of $H/B = 1.0$ and 2.0 , h/t ranging from 15.1 to 35.3 (h represents the flat portion
141 of the section height), the two steel grades (Series A and B) and the three different strengths of
142 concrete infill. The nominal length (L) of each CFHSS tube was taken as $3D$ in order to make sure
143 that each specimen would not fail by overall buckling. The mean values of the measured section
144 dimensions and lengths of the tubular stub column specimens were summarized in [Tables 3-4](#). All the
145 steel square and rectangular tubes were wire cut at both ends before infilling concrete. Concrete of
146 different strengths was then cast into the steel tubes and vibrator was also used in the casting process.

147 The stub column specimens were labelled by distinguishing their nominal section dimensions,
148 nominal concrete cylinder strengths and the steel grades of outer tubes. For example, Specimen
149 $100 \times 100 \times 4$ -C40-A, the first segment of $100 \times 100 \times 4$ ($H \times B \times t$) indicates that the nominal section
150 dimensions of the outer tube, and the symbol following the hyphen indicates the steel tube is infilled
151 with concrete having the nominal cylinder compressive strength of 40 MPa. It should be noted that
152 the symbol "C0" means there is no infilled concrete, namely, it is a CFHSS stub column specimen
153 with hollow section. The last segment represents the nominal strengths of the steel tubes, where "A"
154 and "B" for the $f_{0.2}$ of 700 MPa and 900 MPa, respectively, as mentioned earlier. If it is a repeated
155 test, it is indicated by a letter "r" in the end of the label. The details of the concrete-filled CFHSS
156 square and rectangular tubular stub column specimens are shown in [Tables 3-4](#).

157 2.3 Test setup

158 Tests of the concrete-filled CFHSS tubular stub columns were conducted in the Structural Laboratory
159 at The University of Hong Kong. Figure 3 illustrates a typical test setup. A 5000 kN capacity servo-
160 controlled hydraulic testing machine was used to apply axial compressive force to the concrete-filled
161 CFHSS stub column specimens. Three 50-mm range Linear Voltage Differential Transducers (LVDTs)
162 were used to measure the end shortening of the specimens. These three LVDTs were placed between
163 the top and bottom bearing plates at evenly located positions. To prevent “elephant foot” failure, end-
164 stiffeners (steel frames) with height of around 25 mm were used near each end of the column prior to
165 testing. It should be noted that, for the stub columns infilled with concrete, the top surface of the
166 column might not be at the same level as the end of the steel tube due to shrinkage of the concrete.
167 Hence, plaster materials were used to fill the small gap between the steel tube and infilled concrete
168 [27], as illustrated in Figure 4.

169 A special ball bearing was used at the top end of the specimen. An initial load of around 2 kN was
170 applied to the specimens. During pre-loading, any possible gaps between the specimen and the
171 contacting surfaces of the testing machine were eliminated. The bearing was then locked after pre-
172 loading. Hence, the load was applied uniformly across the whole composite cross-section.
173 Compressive load was applied by displacement control to the specimens with a constant rate of 0.2
174 mm/min using the servo-controlled hydraulic testing machine. By using this test method, the tests
175 could be continued after experiencing the peak loads. The stub column tests were stopped when clear
176 drops of axial loads were observed. A data logger was used to record the readings from the LVDTs
177 and loads at the interval of 1 second. The load-end shortening responses of the test specimens were
178 thus obtained.

179

180 2.4 Test results

181 The compressive behaviour of the stub columns was observed during the tests. The ultimate load (P_t)
182 of the specimen and the corresponding end-shortening (δ_u), as well as the end-shortening ($\delta_{u,0.85}$) at
183 $0.85P_t$ after each specimen experienced its ultimate load are shown in Tables 5-6, for CFHSS series
184 A and B, respectively. The applied load versus axial end-shortening relationship was obtained for
185 each column specimen (e.g., curves in Figures 5(a)-(d)), where the applied load was recorded from
186 the actuator and the end-shortening was taken as the average readings of three LVDTs. Two repeated
187 tests were conducted (i.e. 100×50×4-C40-A-r and 120×120×4-C80-B-r), and the ultimate loads of the
188 repeated tests were very close to their respective first test results, with a maximum difference of 1.9%.
189 This small difference indicated the reliability of the test results. The ultimate loads (P_t) of the
190 concrete-filled stub column specimens were normalized with those ($P_{t,0}$) without infilled concrete for
191 the same series, indicated by the abbreviation of “Nor.”, as shown in Tables 5-6. It is clearly shown
192 that the ultimate loads of the tubular specimens were significantly improved by the infilled concrete
193 in this study, for examples, up to 326% for Series 160×160×4-A and up to 211% for Series
194 120×120×4-B.

195 All the concrete-filled CFHSS square and rectangular stub columns failed by the crushing of the
196 infilled concrete together with outward buckling of the steel tubes at some locations. It should be
197 noted that the use of steel frames at the ends of the columns was able to prevent the “elephant foot”
198 failure of the specimens. The local buckling failure was observed for all specimens. The inward and
199 outward local buckling behaviour was found in specimens without infilled concrete, i.e., specimens
200 of 80×80×4-C0-A, 100×50×4-C0-A (see Figure 6), 100×100×4-C0-A, 140×140×5-C0-A,
201 160×160×4-C0-A, 80×80×4-C0-B, 100×100×4-C0-B and 120×120×4-C0-B. However, the inward
202 local buckling phenomenon was not observed in all concrete-filled CFHSS square and rectangular
203 stub columns, as it was prevented by the infilled concrete in the steel tubes. Figures 6-7 further
204 illustrate the failure modes of the tested concrete-filled CFHSS rectangular stub column Series
205 100×50×4-A and square stub column series 80×80×4-A and 80×80×4-B.

206

207 3. Finite element analysis

208 3.1 Development of model

209 Finite element model (FEM) was developed to simulate the tests of concrete-filled CFHSS square
210 and rectangular stub column specimens. A finite element analysis software ABAQUS [29] was used
211 to develop the FEM. The measured specimen dimensions (Tables 3-4), and material properties of the
212 steel (Table 1) and concrete (Table 2) presented in Section 2 of this paper were used in the analysis
213 of FEM.

214 The steel tube and concrete core were assigned by the S4R (four-node shell element with reduced
215 integration) and the C3D8R (8-node linear brick element with reduced integration and hourglass
216 control), respectively. Based on the mesh convergence study, the element mesh size of $(B+D)/30$ for
217 the steel tube and $(B+D)/15$ for the concrete core was used. The engineering stress-strain (σ - ε) curve
218 was converted to a true stress (σ_{true}) and logarithmic plastic strain (ε_{true}^{pl}) curve, by using the following
219 Equations (1)-(2):

$$220 \quad \sigma_{true} = \sigma(1 + \varepsilon) \quad (1)$$

$$221 \quad \varepsilon_{true}^{pl} = \ln(1 + \varepsilon) - \frac{\sigma_{true}}{E_s} \quad (2)$$

222 The true stress-true plastic strain curves were simplified by means of a piecewise linear stress-strain
223 model, in particular, over the strain-hardening region.

224 The interactive behaviour between the steel tube and concrete was simulated using the interaction
225 algorithm in ABAQUS [29]. The inner surface of the steel tube and the outer surface of the infilled
226 concrete were defined to be a contact pair, of which the former acted as slave surface and the latter
227 acted as master surface. Previous investigations [30] have shown that a friction coefficient from 0.1
228 to 0.5 generally causes limited effect on the prediction of the ultimate strength, but a smaller friction
229 factor may induce a convergent problem with large deformation. It should be noted that different
230 friction coefficients have been used in literature, for examples, coefficients of 0.25 [31], 0.3 [32] and

231 0.6 [33]. In the present study, the friction factor of 0.25 in the tangential direction between the
232 concrete and steel was employed, while the “hard contact” behaviour in the normal direction was
233 assumed with no penetration allowed between the surfaces.

234 Local imperfections were considered in the FEM of the square and rectangular tubular stub column
235 specimens without infilled concrete (specimens of 80×80×4-C0-A, 100×50×4-C0-A, 100×100×4-C0-
236 A, 140×140×5-C0-A, 160×160×4-C0-A, 80×80×4-C0-B, 100×100×4-C0-B and 120×120×4-C0-B),
237 as those FEM for CFHSS square and rectangular tubular stub columns performed by Ma *et al.* [34].
238 However, local imperfections of steel tubes for concrete-filled CFHSS square and rectangular stub
239 columns were not considered. This is because the influence of local imperfections on the behaviour
240 of concrete-filled steel stub columns is negligible due to the infilled concrete. This has been proved
241 by the sensitivity study for the effects of imperfections on the structural behaviour of concrete-filled
242 stainless steel and carbon steel tubular stub columns, as detailed in Tao *et al.* [35-36]. Hence, unlike
243 the FEM for CFHSS square and rectangular tubular stub columns [34], the initial imperfections of
244 steel tubes were not considered in the FEM for the concrete-filled CFHSS stub columns in the present
245 study.

246 A reference node located at the centroid of the cross-section for each column end was defined. The
247 reference node was coupled with the corresponding cross-section at each column end in
248 displacements and rotations. The reference nodes were restrained against all degrees of freedom,
249 except for the longitudinal displacement (along the length direction of the stub column) at the loading
250 point. A specified axial displacement was assigned to the reference node at the loading point. General
251 Static analysis step was adopted [29]. Hence, the adopted displacement control method in the tests
252 was simulated in the FEM analyses. The nonlinear geometric parameter (NLGEOM) was enabled to
253 deal with the large displacement analysis.

254

255 3.2 *Stress-strain of the confined concrete model*

256 The lateral expansion of the infilled concrete is confined by the outer steel tube when the stub columns
257 subjected to axial compression. This confinement helps to increase the strength and ductility of
258 concrete, which refers as “composite action” between the steel tube and infilled concrete [37]. In this
259 study, the confined model of concrete proposed by Tao *et al.* [38] was adopted in the FEM.

260 The key parameters in determining the “concrete damaged plasticity” of the confined concrete model
261 were summarized in the following. The dilation angle (ψ) was assumed to be a constant value of 40°
262 for concrete filled steel stub square and rectangular columns, as suggested by Tao *et al.* [38]. The
263 flow potential eccentricity and viscosity parameters were taken as -1.0 and 0, respectively. The ratio
264 of the compressive strength under biaxial loading to uniaxial compressive strength f_{bol}/f_{ck} was
265 determined by $1.5f_{ck}^{-0.075}$, as suggested by Papanikolaou and Kappos [39]. Hence, in the validation of
266 the FEM, the actual ratios of f_{bol}/f_{ck} for concrete of C40, C80 and C120 were taken as 1.148, 1.074
267 and 1.051, respectively, based on the respective measured compressive strengths of 35.5 MPa, 85.7
268 MPa and 114.9 MPa, as shown in [Table 2](#). The ratio of the second stress invariant on the tensile

269 meridian to that on the compressive meridian (K) is one of the important parameters for determining
 270 the yield surface of concrete plasticity model. It is commonly taken from 0.5 to 1.0 by the researchers
 271 while the default value is 2/3 in ABAQUS [29]. In this study, the equation proposed by Yu *et al.* [40]
 272 was used to calculate the ratio of K . Thus, the values of K were 0.72, 0.71 and 0.70 for concrete
 273 compressive cylinder strengths of 40, 80 and 120 MPa, respectively. In addition, the fracture energy
 274 (G_F) was determined based on the reference [41-42], which are 0.068, 0.11 and 0.143 for concrete of
 275 C40, C80 and C120, respectively.

276 As mentioned previously, the stress-strain model (three stages) of the infilled concrete that
 277 considering the strain hardening/softening rule of concrete core proposed by Tao *et al.* [38] was used
 278 in this study, as illustrated in the following.

279 The initial stage ($0 < \varepsilon \leq \varepsilon_{c0}$) of the curve was determined by Equation (3):

$$280 \quad \frac{\sigma}{f_{ck}} = \frac{A \cdot X + B \cdot X^2}{1 + (A-2)X + (B+1)X^2} \quad 0 < \varepsilon \leq \varepsilon_{c0} \quad (3)$$

281 in which $X = \varepsilon/\varepsilon_{c0}$; $A = E_c \varepsilon_{c0}/f_{ck}$; $B = (A-1)^2/0.55 - 1$; E_c is the Young's modulus of the infilled concrete;
 282 ε_{c0} is the strain at peak stress under uniaxial compression determined by using Equation (4).

$$283 \quad \varepsilon_{c0} = 0.00076 + \sqrt{(0.626f_{ck} - 4.33) \times 10^{-7}} \quad (4)$$

284 In the second stage ($\varepsilon_{c0} < \varepsilon \leq \varepsilon_{cc}$) of the curve, the relationship of stress-strain was determined by the
 285 following Equations (5) and (6):

$$286 \quad \frac{\varepsilon_{cc}}{\varepsilon_{c0}} = e^k \quad (5)$$

$$287 \quad k = (2.9224 - 0.00367f_{ck}) \left(\frac{f_B}{f_{ck}}\right)^{0.3124 + 0.002f_c} \quad (6)$$

288 where f_B represents the confining stress in concrete at strain of ε_{cc} . The confining stress of f_B was
 289 determined by Equation (7):

$$290 \quad f_B = \frac{0.25(1+0.027f_{0.2})e^{\frac{-0.02\sqrt{B^2+D^2}}{t}}}{1+1.6e^{-10}(f_{ck})^{4.8}} \quad (7)$$

291 The last stage ($\varepsilon_{cc} < \varepsilon$), i.e., descending branch, of the stress-strain curve was determined by Equation
 292 (8):

$$293 \quad \sigma = f_r + (f_{ck} - f_r) \exp \left[- \left(\frac{\varepsilon - \varepsilon_{cc}}{\alpha} \right)^\beta \right] \quad \varepsilon \geq \varepsilon_{cc} \quad (8)$$

294 where f_r is the residual stress as determined by Equation (9). The parameters α and β are the factors
 295 that influence the shape of curve.

$$296 \quad f_r = 0.1f_{ck} \quad (9)$$

297 The parameter α is calculated as:

298

$$\alpha = 0.005 + 0.0075\xi_c \quad (10)$$

299 The parameter β is taken as 0.92 for concrete-filled square and rectangular steel stub columns [43].

300

301 3.3 Validation of FEM

302 Based on the developed FEM by using the measured dimensions and material properties, the
303 modelling parameters as well as the confined concrete model, the analysis of the FE were performed.
304 The developed FEM was validated by comparing the FE results with the test results in terms of the
305 ultimate loads, failure modes and the load-end shortening curves. The comparison of the ultimate
306 loads (P_t) from tests with those (P_{FEA}) predicted from the FE analysis are shown in Table 7. The mean
307 value of the P_t/P_{FEA} is 1.00 with the corresponding coefficient of variation (COV) of 0.079. It is
308 shown that the developed FEM can successfully replicate the ultimate capacities of the concrete-filled
309 CFHSS square and rectangular stub columns. Figures 8-9 illustrate the comparison of load-end
310 shortening curves and failure modes obtained from the test and FEA for specimens 80×80×4-C80-A
311 and 120×120×4-C120-B, respectively. The contributions of the outer steel tubes and the concrete
312 infill in the history of the load-end shortening curves that obtained from the FEA were also plotted in
313 the figures. It is clearly shown that the infilled concrete reached its ultimate load (or first peak) earlier
314 than that of the outer steel tube, as reflected in the smaller end shortening values. However, due to
315 the confinement effect, the load resistance of the infilled concrete may increase as the end shortening
316 increased even the load resistance of the outer steel tube reduced due to local buckling. Generally, it
317 is shown that the end-shortenings (δ_u) of the concrete-filled CFHSS stub columns at the ultimate loads
318 (or first peaks) were dominated by those of the concrete infill, namely, the values of end shortening
319 for the concrete-filled CFHSS stub columns were close to those of the infilled concrete at the ultimate
320 loads (or first peaks).

321

322 4. Parametric study

323 4.1 Design of specimens

324 The validated FEM was used to perform a further study on the behaviour of concrete-filled CFHSS
325 square and rectangular stub columns. The parameters that may affect the structural behaviour of the
326 stub columns were considered, including the cross-section dimensions, section slenderness (ratios of
327 h/t), $f_{0.2}$ of the steel tubes (steel grades), compressive strengths of infilled concrete. A total of 52
328 specimens were carefully designed to cover a wide range of parameters, including 24 for rectangular
329 specimens and 28 for square specimens. The ratios of h/t varied from 35.0 to 75.0 and from 10.0 to
330 55.0 for rectangular and square tubes, respectively. The stress-strain curves of sections 100×100×4-
331 A and 100×100×4-B having the respective nominal $f_{0.2}$ of 700 MP and 900 MPa were used. As those
332 of the test specimens, the compressive cylinder strengths (f_{ck}) of the infilled concrete were 40, 80 and
333 120 MPa, respectively, and the length of each stub column was taken to be $3D$. The dimensions of
334 concrete-filled CFHSS square and rectangular stub columns used in this parametric study are detailed

335 in [Tables 8-9](#), respectively. The criterion for the specimen labelling is the same as those described in
336 Section 2.2 of this paper. In this sense, the last letters “A” and “B” in the specimen labelling represent
337 the different steel grades by using stress-strain curves of sections 100×100×4-A ($f_{0.2} = 700$ MPa) and
338 100×100×4-B ($f_{0.2} = 900$ MPa), respectively. The CFHSS stub columns without infilled concrete are
339 also included, as distinguished by the segment of “C0”.

340

341 4.2 Definition of parameters

342 The parametric study of the concrete-filled CFHSS square and rectangular stub columns aims to study
343 its structural behaviour under axial compression. These included the ultimate load, end shortening,
344 the strength enhancement index (**SI**), as well as the ductility index (**DI**) [28].

345 The strength enhancement index (**SI**), as expressed in Equation (11), is defined by the ratio of the
346 ultimate compressive load (P_u) of the concrete-filled steel tubular stub column to the sum of the
347 strengths of the individual constituent components (i.e., the concrete core and steel tube). The
348 parameter **SI** reflects the contribution of composite action in concrete-filled CFHSS square and
349 rectangular stub columns. A **SI** value higher than 1.0 indicates that the positive interaction between
350 the steel hollow section and the concrete core was achieved. The positive interaction benefits from
351 the confinement effect of the concrete core from the steel tube, as well as the contribution of the
352 concrete core to the delay or elimination of the local buckling in the steel tubular hollow section.

$$353 \quad \mathbf{SI} = P_u / (f_{0.2}A_s + f_{ck}A_c) \quad (11)$$

354 where A_s and A_c correspond to the cross-section areas of the outer steel tube and the concrete core.
355 The ductility index (**DI**), as expressed in Equation (12), is defined as the ratio of $\delta_{u,0.85}$ to δ_u . The
356 higher value of the parameter **DI** represents that the better ductility of the specimens.

$$357 \quad \mathbf{DI} = \delta_{u,0.85} / \delta_u \quad (12)$$

358

359 4.3 Influence of parameters

360 The parametric study results are presented in [Tables 8-9](#), including P_{FEA} , δ_u and $\delta_{u,0.85}$ for the concrete-
361 filled CFHSS square and rectangular stub column specimens. The stub column specimens without
362 infilled concrete (specimens $H \times B \times t$ -C0-A and $H \times B \times t$ -C0-B), which had the same nominal section
363 sizes as those specimens with the infilled concrete, were also included. In addition, the ultimate loads
364 of the concrete-filled CFHSS square and rectangular stub column specimens were normalized by the
365 ultimate load ($P_{FEA,0}$) of the CFHSS tubular specimen (without infilled concrete) in the same series,
366 as indicated by “Nor.” in the [Tables 8-9](#), respectively. The normalized column strengths from the tests
367 and FEA were plotted against the infilled concrete strengths associated with different steel grades
368 (series A and B) and the ratios of h/t , as shown in [Figures 10\(a\)-\(c\)](#). Generally, it is shown that the
369 normalized column strength increased linearly with the increment of the infilled concrete strength for
370 the CFHSS square and rectangular stub column specimens with a given value of h/t ([Figures 10\(a\)-](#)

371 (c)), where the infilled concrete strength of “0” in the horizontal axis means the CFHSS square and
372 rectangular hollow section columns without any infilled concrete. Similar findings have been
373 presented by Su *et al.* [27] for concrete-filled CFHSS circular tubular stub columns and by Cai *et al.*
374 [28] for concrete-filled cold-formed and hot-finished steel elliptical tubular stub columns.

375 The behaviour of the concrete-filled CFHSS square and rectangular stub column specimens was
376 investigated in terms of the parameters of **SI** and **DI** based on the results from the tests and FEA, as
377 shown in Tables 5-6 and Tables 8-9. Figure 11 presents the relationships between the strength
378 enhancement index (**SI**) and ratios of h/t for stub columns with square sections. As shown in Figure
379 11, under a given infilled concrete strength, the value of **SI** decreased regularly as the value of h/t
380 increased. The decrements for the infilled concrete with nominal f_{ck} of 40 MPa are more obvious than
381 those infilled with nominal f_{ck} of 120 MPa. Similar trends were found for those stub column
382 specimens with rectangular sections as illustrated in Figure 12. Furthermore, for the stub columns
383 with square and rectangular sections, it was found that the value of **SI** generally decreased with the
384 increment of the infilled concrete strength under the same value h/t when $h/t \leq 25.0$; however, when
385 $h/t \geq 25.0$, the value of **SI** increased with the increment of the infilled concrete strength for a given
386 value of h/t , as shown in Figures 11-12. Meanwhile, the values of **SI** that larger than 1.00 tended to
387 be smaller than 1.00 as the ratio of h/t became larger, e.g., $h/t \geq 35$ for specimens with rectangular
388 sections. One of the main reasons is due to the changing of the section slenderness, a larger value of
389 h/t (i.e., from compact to slender) would fail in local buckling earlier and thus provide less
390 confinement effect to the concrete core, which subsequently decreasing the section capacity.

391 The ductility indexes (**DI**) of the CFHSS square and rectangular stub columns with and without
392 infilled concrete were also investigated, as presented in Tables 5-6 and Tables 8-9. As shown in the
393 tables, the values of **DI** for the concrete-filled CFHSS square and rectangular e stub column
394 specimens were generally higher than those of specimens without infilled concrete, except for those
395 square and rectangular specimens with larger value of h/t , e.g., specimens with $h/t = 55.0$. This could
396 be due to load resistance drops largely as the failure of local buckling in the outer steel tube occurs.
397 However, these test and FE results indicated that the ductility of the CFHSS square and rectangular
398 stub column specimens could be significantly enhanced by the infilled concrete, as discussed in the
399 Section 1 of this paper.

400

401 5. Existing design rules

402 5.1 General

403 Design of concrete-filled steel square and rectangular stub columns are provided by the existing
404 international design specifications [22-25], as mentioned in Section 1 of this paper. It should be noted
405 that concrete grades over C60 are beyond the upper limit of the specified concrete grade in EC4 [22],
406 where the strength classes of the normal weight concrete used in composite members range from
407 C20/C25 to C50/C60 only. The design rules provided in EC4 [22] apply to steel grades from S235 (f_y
408 = 235 MPa) to S460 ($f_y = 460$ MPa). The design rules specified in AISC [23] are applicable to CFST

409 members with $f_y \leq 525$ MPa and $21 \leq f_{ck} \leq 69$ MPa. The AIJ Specification [24] allows the steel yield
 410 stress and concrete compressive cylinder strength of 440 MPa and 90 MPa, respectively while the
 411 AS/NZS2327 [25] allows steel yield stress not greater than 690 MPa and concrete cylinder
 412 compressive strength in the range of 20 MPa to 100 MPa. In the present study, the existing design
 413 rules specified in EC4 [22] and AISC [23] were selected to calculate the nominal strengths of
 414 concrete-filled CFHSS square and rectangular stub columns. In addition, the recent proposal on the
 415 strength reduction of high strength concrete in concrete-filled steel tubular members [8] due to the
 416 effects of infilled concrete strength was also incorporated in the calculations, for the nominal strengths
 417 predicted by the aforementioned design specifications [22-23].

418

419 5.2 Eurocode 4: Design of Composite Steel and Concrete Structures (EC4)

420 EC4 [22] covers the design rules for encased, partially encased and concrete-filled columns both with
 421 and without reinforcements. In the present study, no reinforcement was used in the concrete-filled
 422 CFHSS stub columns. The compressive design resistance of concrete-filled square and rectangular
 423 sections in EC4 [22] is a simple summation of the steel tube and concrete contributions. Account is
 424 taken of the higher resistance of the concrete, which is caused by confinement from the outer steel
 425 tube, by adopting a concrete coefficient of 1.0, rather than 0.85, as specified in Section 6.7.3.2 in EC4
 426 [22]. The cross-section capacity (P_{EC}) of a concrete-filled steel square and rectangular tubular stub
 427 column is thus given by Equation (13)

$$428 \quad P_{EC} = A_s f_{0.2} + A_c f_{ck} \quad (13)$$

429 A slenderness limit of $H/t \leq 52(235/f_{0.2})^{0.5}$ for the outer steel tube is specified in the Table 6.3 of EC4
 430 [22]. It should be noted that the yield strength (f_y) of the steel tube was replaced by the 0.2% proof
 431 stress ($f_{0.2}$) of the CFHSS stubs in the present study. Beyond the slenderness limit, local buckling
 432 needs to be explicitly accounted for, but is not specified in EC4 [22]. Hence, a further investigation
 433 was recommended to determine a more appropriate limit for concrete-filled tubes [42]. In this study,
 434 for the cross sections exceeding the slenderness limit of $52(235/f_{0.2})^{0.5}$, the effective width equations
 435 provided in EC3-1.5 [43], as given by the following Equations (14) and (15), were adopted to
 436 calculate the effective area of the outer steel tubes.

$$437 \quad \rho \leq \frac{\bar{\lambda}_p^{-0.055(3+\varphi)}}{\bar{\lambda}_p^2} \leq 1.0 \quad \text{for } \bar{\lambda}_p > 0.5 + \sqrt{0.085 - 0.055\varphi} \quad (14)$$

438

$$439 \quad \bar{\lambda}_p = \frac{(H-3t)/t}{28.4\epsilon\sqrt{k_\sigma}} \quad (15)$$

440 where ρ = reduction factor for local buckling for plate buckling; φ is the stress ratio which equals to
 441 1.0 in this study; $\bar{\lambda}_p$ is the plate slenderness; k_σ is the buckling factor corresponding to the φ and
 442 boundary conditions and $k_\sigma = 4.0$ in this study according to Table 4.1 in EC3-1.5 [43]; H is the flat
 443 height of the outer steel tube (replaced by B for the flat width). In the present study, for the test
 444 specimens and numerical specimens (shown in Tables 10-11) that exceed the above slenderness limit

445 of 52.0, the reduction factor ρ was used in the calculation of the cross-section area instead of the full
 446 cross-section area. Similar approach was also adopted by Wang *et al.* [42] to determine the cross-
 447 section strength of concrete-filled double skin rectangular stub columns.

448 Recently, investigations on the effects of concrete strength for concrete-filled steel short columns
 449 revealed that the complexity and severity increased as the infilled concrete strength increased [8]. In
 450 particular, it was found that for ultra-high strength concrete with $f_{ck} > 90$ MPa, the increment of
 451 concrete strength due to the confinement effect from steel tube should be ignored [9]. Based on the
 452 calibrations against the design rules in EC4 [22], a reduction factor (η) for the effective compressive
 453 strength of the infilled concrete in steel tubes was proposed, as shown in Equation (16). The formula
 454 has been used in the predictions of concrete-filled steel tubular stub columns where the effects of
 455 infilled concrete strength was considered, such as by Wei *et al.* [17] and Wang *et al.* [43]. The
 456 reduction factor was also employed in the calculation of concrete-filled steel square and rectangular
 457 stub columns in this study when the effects of infilled concrete strengths was considered.

$$458 \quad \eta = \begin{cases} 1.0 - \frac{(f_{ck}-50)}{200} & 50 \text{ MPa} < f_{ck} \leq 90 \text{ MPa} \\ 0.8 & f_{ck} > 90 \text{ MPa} \end{cases} \quad (16)$$

459

460 5.3 Specification for Structural Steel Buildings (AISC)

461 The nominal compressive strength (P_{AISC}) of concrete-filled steel square and rectangular tubular
 462 sections under axial loading refers to the design rules specified in Section I2.2b in AISC [23]. For the
 463 cross-section strengths of concrete-filled steel square and rectangular stub columns, sections are
 464 categorized as compact, non-compact or slender according to the width-to-thickness ($\lambda = h/t$) ratios
 465 of the outer tubes, as specified in Section I1.4 and Table I1.1a of AISC [23]. The value of P_{AISC} was
 466 determined by Equations (17)-(19):

467 For compact sections ($\lambda \leq \lambda_p$),

$$468 \quad P_{AISC} = P_p \quad (17a)$$

$$469 \quad P_p = f_{0.2}A_s + 0.85f_{ck}A_c \quad (17b)$$

$$470 \quad \lambda_p = 2.26\sqrt{E_s/f_{0.2}} \quad (17c)$$

471 where P_p is the compressive strength of compact sections; λ_p is the slenderness limit for determining
 472 whether a section is compact or non-compact.

473 For non-compact sections ($\lambda_p < \lambda \leq \lambda_r$),

$$474 \quad P_{AISC} = P_p - \frac{P_p - P_y}{(\lambda_r - \lambda_p)^2} (\lambda - \lambda_p)^2 \quad (18a)$$

$$475 \quad P_y = f_{0.2}A_s + 0.7f_{ck}A_c \quad (18b)$$

$$476 \quad \lambda_r = 3.00\sqrt{E_s/f_{0.2}} \quad (18c)$$

477 where P_y is the compressive strength of non-compact sections; λ_r is the slenderness limit for
478 determining whether a section is non-compact or slender.

479 For slender sections ($\lambda_r < \lambda \leq \lambda_{limit}$),

$$480 \quad P_{no} = f_{cr}A_s + 0.7f_{ck}A_c \quad (19a)$$

$$481 \quad f_{cr} = 9E_s\left(\frac{t}{b}\right)^2 \quad (19b)$$

$$482 \quad \lambda_{limit} = 5.00\sqrt{E_s/f_{0.2}} \quad (19c)$$

483 where f_{cr} is the compressive strength of slender sections. In the present study, all the CFHSS square
484 and rectangular specimens are categorized as compact, non-compact or slender sections based on the
485 above criterion except specimen Series 320×160×4-B in the parametric study, whose section
486 slenderness (λ) exceeds the limit of $5.00(E_s/f_{0.2})^{0.5}$. Since the section slenderness beyond this value is
487 not explicitly specified in the AISC [23], the reduction factor in Equation (14) for the effective cross-
488 section area is also adopted in the calculation of the nominal strengths (P_{AISC}) for the specimen Series
489 320×160×4-B.

490

491 **6. Assessment of codified strength predictions**

492 *6.1 General*

493 The ultimate load (P_u) from the experimental (P_t) and numerical results (P_{FEA}) were compared with
494 the nominal strengths predicted by the aforementioned design specifications [22-23], as summarized
495 in [Tables 10-11](#) and [Figures 13-16](#). Comparisons were performed with all safety factors set to unity.
496 In the comparisons, the specimens without infilled concrete were not included, as this study mainly
497 focused on the structural behaviour of concrete-filled CFHSS column specimens with square and
498 rectangular sections.

499 In the calculation of the nominal strengths (unfactored design strengths) for the test specimens,
500 measured values of the material properties ([Table 1](#)) and specimen dimensions ([Tables 3-4](#)) were
501 used, which enables a direct comparison between test results and compressive strengths predicted
502 from existing design rules. In calculating the compressive strength of the test specimens, the concrete
503 cylinder strength at the day of the stub column test were used ([Table 2](#)). The stress-strain curves of
504 cold-worked materials did not possess sharp yield points. Hence, the measured 0.2% proof stress ($f_{0.2}$)
505 was used as the yield strength (f_y) in calculating the compressive strength for the test specimens. For
506 specimens generated in the parametric study, the measured $f_{0.2}$ of sections 100×100×4-A and
507 100×100×4-B were used for specimen using steel grades of series A ($f_{0.2} = 700$ MPa) and B ($f_{0.2} =$
508 900 MPa), respectively. The nominal cylinder strengths of the concrete were used. This is because,
509 in the FE model for the parametric study, measured stress-strain curves of the CFHSS sections
510 100×100×4-A and 100×100×4-B were used together with the stress-strain curves obtained from the
511 confined concrete model that were developed based on nominal concrete strengths.

512

513 6.2 Predictions by EC4

514 **Table 10** shows the comparison of the test and FE strength-to-predicted strength by EC4 [22] for stub
515 columns with square and rectangular section specimens. The relationships between the comparisons
516 with EC4 [22] and the section slenderness values were plotted in **Figures 13-14** for specimens with
517 square and rectangular sections, respectively. Overall, predictions from EC4 [22] were generally
518 unconservative as the mean values for the ratios of the P_u/P_{EC} were smaller than 1.00. As the CFHSS
519 tubular sections became more slender, larger values of $H/t(f_{0.2}/235)^{0.5}$, the predictions generally
520 became more unconservative. The modified predicted strength, P_{EC^*} , represents that effective cross-
521 section area of the steel tube was considered in the calculation of the cross-section area for those
522 sections exceed the slenderness limit of $H/t(f_{0.2}/235)^{0.5} = 52.0$. Under this circumstance, the
523 predictions by EC4 [22] became conservative, with the mean values of P_u/P_{EC^*} equalled to 1.07 and
524 1.09 for specimens with square and rectangular sections, respectively. Furthermore, the coefficients
525 of variation (COV) were significantly reduced, for example in the predictions of specimens with
526 rectangular sections, COV of 0.059 for P_u/P_{EC^*} compared with that of 0.141 for P_u/P_{EC} . It means that
527 the consideration of using effective section area for the specimens exceed the slenderness limit in
528 EC4 [22] improved the strength predictions as the predictions became safer and less scattered. As
529 mentioned in Section 5.2, the reduction factor of η , using Equation (16), for the effective compressive
530 strength of the infilled concrete was also considered in the design predictions, as represented by P_{EC^\wedge}
531 in **Table 10**. It is shown that the predictions were slightly improved as reflected in the mean values
532 P_u/P_{EC^\wedge} closer to 1.00 with smaller values of COV. The predictions by EC4 [22] were further modified
533 by considering both the reduction factor of ρ for the effective cross-section area of steel tube and the
534 reduction factor of η for the effective compressive strength of the infilled concrete, as represented by
535 $P_{EC^{*\wedge}}$ in **Table 10**. The predictions by $P_{EC^{*\wedge}}$ became more conservative than those by P_{EC} , P_{EC^*} and
536 P_{EC^\wedge} , as reflected by the largest mean values; however, less scattered predictions were achieved as
537 shown in the smaller values of corresponding COV, which was comparable with those of P_u/P_{EC^*} .
538 The specimens were divided into two groups based on the steel grades of series A and B for the outer
539 steel tubes, it was found that EC4 [22] provided relatively more conservative predictions for those
540 specimens with relatively lower steel grade for both square and rectangular specimens, namely, steel
541 Series A with nominal $f_{0.2} = 700$ MPa.

542

543 6.3 Predictions by the AISC

544 **Table 11** shows the comparison of the test and FE strength-to-predicted strength by AISC [23] for
545 stub columns with square and rectangular section specimens. The relationships between the
546 comparisons with AISC [23] and the section slenderness values were plotted in **Figures 15-16** for
547 square and rectangular specimens, respectively. On the contrary, the predictions from AISC [23] were
548 overall conservative, i.e., the mean values (P_u/P_{AISC}) of 1.18 and 1.09 for the square and rectangular
549 specimens, respectively. It should be noted that the section slenderness of rectangular specimen Series
550 320×160×4-B exceeded the value of λ_{limit} [23], limit of $5.00(E_s/f_{0.2})^{0.5}$, hence, the reduction factor ρ
551 in Equation (16) was incorporated in the calculation of the cross-section area (A_s) of the steel tube in
552 the strength prediction, as distinguished by “#” for the values in the bracket in **Table 11**. Similarly,

553 the reduction factor of η for the effective compressive strength of the infilled concrete was also
554 considered in the design predictions, as represented by modified predictions P_{AISC}^{\wedge} in Table 11. It is
555 shown that generally, the modified predictions were not improved for AISC [23]. This may be due to
556 the reduction factor (η) was proposed based on the design rules in EC4 [22]. The specimens were also
557 divided into two groups based on the steel grades (i.e. series A and B) for the outer steel tubes. The
558 AISC [23] provided relatively more conservative and more scattered predictions for those specimens
559 with relatively higher steel grade (Series B with $f_{0.2} = 900$ MPa) for rectangular specimens, however,
560 relatively more conservative with less scattered predictions were provided for those specimens with
561 relatively lower steel grade (Series A with $f_{0.2} = 700$ MPa) for square specimens. Due to the limited
562 numbers of specimens that exceeded the section slenderness limit (λ_{limit}), the specimens using the
563 effective cross-section area instead of full cross-section area in the calculation were not plotted. As
564 shown in Figures 15-16, for both square and rectangular sections, the predictions by AISC [23] were
565 generally conservative for compact sections ($\lambda \leq \lambda_p$), however, for the non-compact ($\lambda_p < \lambda \leq \lambda_r$) and
566 slender sections ($\lambda_r < \lambda \leq \lambda_{limit}$) as well as those beyond the slenderness limit ($\lambda_{limit} < \lambda$), the predictions
567 became more conservative as the section slenderness increased.

568

569 6.4 Effects of infilled concrete strengths and section slenderness

570 Tables 12 (a)-(b) presents the summary of the comparisons between test and FE strengths with
571 codified predictions [22-23] for square and rectangular sections, respectively. In each section type in
572 each table, the specimens were divided by the different strengths of infilled concrete. For the
573 predictions by EC4 [22], it is shown that the predictions were improved for both square and
574 rectangular sections by P_u/P_{EC}^* , safer with less scattered predictions for all the concrete strengths as
575 the effective cross-section areas were used for those slender sections; the predictions also became
576 safer with less scattered predictions by P_u/P_{EC}^{\wedge} , when the effective strengths were considered for the
577 infilled concrete strengths of 80 and 120 MPa. However, when considering both effective cross-
578 section area and effective concrete strengths in the calculation for P_u/P_{EC}^{\wedge} , the mean values generally
579 became similar for the different infilled concrete strengths (e.g., mean values of 1.17, 1.16 and 1.16
580 for infilled concrete of C40, C80 and C120, respectively), which means the effects due to infilled
581 concrete strengths and section slenderness were minimized, as reflected in Figure 13(d) and Figure
582 14(d). On the contrary, the predictions by the AISC [23], did not show an obvious improvement
583 when the effects due to infilled concrete strengths and section slenderness were taken into
584 consideration, as illustrated in Table 12 and Figures 15-16. For both predictions by EC4 [22] and
585 AISC [23], the predictions were generally more conservative for the lower infilled concrete strengths
586 with less slender sections (non-slender sections), shown in Figures 13(a) and 14(a) for EC4 [22], or
587 more compact sections, shown in Figures 15(a) and 16(a) for AISC [23]. However, the predictions
588 became more conservative (safer) for the higher infilled concrete strengths with more slenderer
589 sections for both EC4 [22] and AISC [23], as shown in Figures 13(a), 14(a), 15(a) and 16(a).

590

591

592 7. Conclusions

593 The structural behaviour of high strength steel square and rectangular tubular stub columns infilled
594 with concrete has been investigated in the present study. A series of tests was conducted on cold-
595 formed high strength steel (CFHSS) square (ranged from 80×80 mm to 160×160 mm) and rectangular
596 (100×50 mm) tubes infilled with three different grades of concrete (i.e., 40, 80 and 120 MPa). The
597 CFHSS tubular sections had the nominal 0.2% proof stress (i.e. the yield stress) up to 900 MPa. A
598 total of 34 test specimens were designed and tested by applying uniform axial compressive loading.
599 An extensive numerical study accounting for the confinement effect, as well as the non-linearities of
600 materials, geometry and contacts have also been performed by using a validated finite element model.

601 The behaviour of CFHSS square and rectangular stub columns has been investigated, including the
602 compressive capacities, the end shortening, the strength enhancement index (*SI*) and the ductility
603 index (*DI*). The results showed that the ultimate loads of the CFHSS tubular specimens were
604 significantly improved up to 326% by the infilled concrete in this study. Both the capacities and
605 ductility of the CFHSS square and rectangular stub columns could be significantly enhanced by the
606 infilled concrete. Furthermore, the experimental and numerical results were used to assess the
607 suitability of the design equations specified American Specification (AISC) and European Code
608 (EC4) for the cross-section strength of CFHSS stub columns. Overall, the predictions from EC4 were
609 generally unconservative while the predictions from AISC were conservative. In particular, the
610 predictions were more conservative for the lower infilled concrete strengths with less slender sections
611 (non-slender sections) using EC4 and more compact sections using AISC; however, the predictions
612 became more conservative for the higher infilled concrete strengths with more slender sections.

613

614

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618

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Table 1: Material properties of CFHSS square and rectangular tubes

Tube labelling	E_s (GPa)	$f_{0.2}$ (MPa)	f_u (MPa)	ε_u (%)	ε_f (%)
80×80×4-A	211	756	852	3.0	16.0
100×50×4-A	212	721	842	4.3	14.7
100×100×4-A	215	722	819	5.7	18.0
140×140×5-A	210	682	822	6.4	21.0
160×160×4-A	215	629	881	3.8	13.4
80×80×4-B	210	1022	1179	1.9	11.8
100×100×4-B	206	980	1092	1.7	12.1
120×120×4-B	206	991	1140	2.9	12.2

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Table 2: Compressive strength (f_{ck}) of concrete cylinders

Concrete mixes	28 days (MPa)	Column test day (MPa)
C40	34.9	35.5
C80	79.9	85.7
C120	112.7	114.9

Note: data source from Ref. [27].

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Table 3: Dimensions of high strength steel tubes of Series A

Specimens	H (mm)	B (mm)	r_i (mm)	t (mm)	L (mm)
80×80×4-C0-A	80.6	80.2	5.0	4.00	240.0
80×80×4-C40-A	80.1	80.4	4.9	4.00	240.0
80×80×4-C80-A	80.5	80.2	5.0	3.98	240.0
80×80×4-C120-A	80.7	80.2	5.0	3.96	240.0
100×50×4-C0-A	100.2	50.9	3.5	3.97	300.0
100×50×4-C40-A	100.2	50.6	3.4	3.98	300.0
100×50×4-C40-A-r	100.2	50.7	3.5	3.96	300.0
100×50×4-C80-A	100.2	50.9	3.5	4.00	300.0
100×50×4-C120-A	100.3	50.8	3.6	3.96	299.0
100×100×4-C0-A	100.6	100.8	4.3	4.00	300.0
100×100×4-C40-A	100.4	100.7	4.2	3.99	300.0
100×100×4-C80-A	100.9	100.6	4.3	3.97	300.0
100×100×4-C120-A	100.8	100.5	4.3	3.96	299.5
140×140×5-C0-A	140.8	141.7	7.0	4.91	420.0
140×140×5-C40-A	141.2	140.7	7.0	4.94	420.0
140×140×5-C80-A	141.0	141.4	7.1	4.97	420.0
140×140×5-C120-A	141.4	141.1	7.0	4.93	420.0
160×160×4-C0-A	161.8	161.1	6.0	4.05	480.0
160×160×4-C40-A	161.2	161.7	6.0	4.01	480.0
160×160×4-C80-A	161.5	161.9	6.0	4.01	480.0
160×160×4-C120-A	162.0	161.2	6.0	4.04	480.0

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Table 4: Dimensions of high strength steel tubes of Series B

Specimens	H (mm)	B (mm)	r_i (mm)	t (mm)	L (mm)
80×80×4-C0-B	80.5	80.3	6.0	3.98	239.0
80×80×4-C40-B	80.3	80.5	6.1	3.97	240.0
80×80×4-C80-B	80.5	80.2	5.8	3.99	240.0
80×80×4-C120-B	80.4	80.3	6.0	3.98	240.0
100×100×4-C0-B	100.6	100.7	7.0	4.01	300.0
100×100×4-C40-B	100.6	100.6	7.0	4.00	299.5
100×100×4-C80-B	100.9	100.6	7.0	3.97	299.5
100×100×4-C120-B	100.7	100.7	7.0	3.99	299.5
120×120×4-C0-B	121.8	121.6	6.0	3.93	360.0
120×120×4-C40-B	121.9	121.8	6.0	3.93	360.0
120×120×4-C80-B	121.8	121.8	6.0	3.91	359.0
120×120×4-C80-B-r	121.9	121.8	6.0	3.93	359.0
120×120×4-C120-B	121.9	121.9	6.0	3.92	360.0

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Table 5: Test results of concrete-filled CFHSS stub columns using Series A steel tubes

Specimens	H/B	h/t	P_t (kN)	δ_u (mm)	$\delta_{0.85u}$ (mm)	$Nor.$	DI
80×80×4-C0-A	1.0	15.7	1064	3.2	4.0	1.00	1.25
80×80×4-C40-A	1.0	15.6	1328	3.3	5.4	1.25	1.64
80×80×4-C80-A	1.0	15.7	1462	3.3	>9.8	1.37	>2.97
80×80×4-C120-A	1.0	15.8	1504	3.4	6.5	1.41	1.91
100×50×4-C0-A	2.0	21.5	922	2.8	3.9	1.00	1.39
100×50×4-C40-A	2.0	21.5	1113	3.0	4.6	1.21	1.53
100×50×4-C40-A-r	2.0	21.5	1112	5.1	6.0	1.21	1.18
100×50×4-C80-A	2.0	21.3	1211	4.0	6.0	1.31	1.50
100×50×4-C120-A	2.0	21.5	1198	3.4	5.1	1.30	1.50
100×100×4-C0-A	1.0	21.0	1241	2.3	2.8	1.00	1.22
100×100×4-C40-A	1.0	21.0	1666	3.0	>4.7	1.34	>1.57
100×100×4-C80-A	1.0	21.3	1853	2.8	5.1	1.49	1.82
100×100×4-C120-A	1.0	21.3	1957	2.9	>8.2	1.58	>2.83
140×140×5-C0-A	1.0	23.8	2033	2.6	3.2	1.00	1.23
140×140×5-C40-A	1.0	23.7	2992	5.2	15.1	1.47	2.90
140×140×5-C80-A	1.0	23.5	3237	4.3	13.3	1.59	3.09
140×140×5-C120-A	1.0	23.8	3760	2.6	5.0	1.85	1.92
160×160×4-C0-A	1.0	35.0	1246	1.7	3.6	1.00	2.12
160×160×4-C40-A	1.0	35.2	2785	3.9	>6.4	2.24	>1.64
160×160×4-C80-A	1.0	35.3	3600	2.3	4.7	2.89	2.04
160×160×4-C120-A	1.0	35.1	4062	2.1	3.9	3.26	1.86

Note: “ $Nor.$ ” represents the P_t normalized by that ($P_{t,0}$) without infilled concrete in the same series.

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Table 6: Test results of concrete-filled CFHSS stub columns using Series B steel tubes

Specimens	H/B	h/t	P_t (kN)	δ_u (mm)	$\delta_{0.85u}$ (mm)	$Nor.$	DI
80×80×4-C0-B	1.0	15.2	1431	3.3	3.8	1.00	1.15
80×80×4-C40-B	1.0	15.1	1722	3.4	4.6	1.20	1.35
80×80×4-C80-B	1.0	15.3	1791	3.7	7.5	1.25	2.03
80×80×4-C120-B	1.0	15.2	1898	3.4	5.9	1.33	1.74
100×100×4-C0-B	1.0	19.6	1474	2.8	3.2	1.00	1.14
100×100×4-C40-B	1.0	19.7	2009	4.7	7.2	1.36	1.53
100×100×4-C80-B	1.0	19.9	2177	4.1	7.1	1.48	1.73
100×100×4-C120-B	1.0	19.7	2266	4.3	>9.3	1.54	>2.16
120×120×4-C0-B	1.0	25.9	1400	1.9	3.3	1.00	1.74
120×120×4-C40-B	1.0	26.0	2557	4.1	5.5	1.83	1.34
120×120×4-C80-B	1.0	26.1	2853	4.2	>11.7	2.04	>2.79
120×120×4-C80-B-r	1.0	26.0	2798	3.3	>11.6	2.00	>3.52
120×120×4-C120-B	1.0	26.0	2950	2.9	>11.0	2.11	>3.79

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Table 7: Comparison of test strengths with FE predictions

Specimens	P_t (kN)	P_{FEA} (kN)	P_t/P_{FEA}
80×80×4-C0-A	1064	1039	1.02
80×80×4-C40-A	1328	1242	1.07
80×80×4-C80-A	1462	1418	1.03
80×80×4-C120-A	1504	1513	0.99
100×50×4-C0-A	922	902	1.02
100×50×4-C40-A	1113	1129	0.99
100×50×4-C80-A	1211	1250	0.97
100×50×4-C120-A	1193	1360	0.88
100×100×4-C0-A	1241	1205	1.03
100×100×4-C40-A	1666	1580	1.05
100×100×4-C80-A	1853	1825	1.02
100×100×4-C120-A	1957	2076	0.94
140×140×5-C0-A	2033	2134	0.95
140×140×5-C40-A	2992	3028	0.99
140×140×5-C80-A	3237	3321	0.97
140×140×5-C120-A	3760	3735	1.01
160×160×4-C0-A	1246	1225	1.02
160×160×4-C40-A	2785	2257	1.23
160×160×4-C80-A	3600	3198	1.13
160×160×4-C120-A	4062	4226	0.96
80×80×4-C0-B	1431	1377	1.04
80×80×4-C40-B	1722	1637	1.05
80×80×4-C80-B	1791	1728	1.04
80×80×4-C120-B	1898	1797	1.06
100×100×4-C0-B	1474	1639	0.90
100×100×4-C40-B	2009	2006	1.00
100×100×4-C80-B	2177	2214	0.98
100×100×4-C120-B	2266	2387	0.95
120×120×4-C0-B	1400	1874	0.75
120×120×4-C40-B	2557	2606	0.98
120×120×4-C80-B	2853	2864	1.00
120×120×4-C120-B	2950	3085	0.96
		Mean	1.00
		COV	0.079

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Table 8: Dimensions and results of concrete-filled CFHSS square stub columns in parametric study

Specimens	h/t	P_{FEA} (kN)	δ_u (mm)	$\delta_{0.85u}$ (mm)	$Nor.$	DI
45×45×3-C0-A	10.0	408	1.93	2.88	1.00	1.49
45×45×3-C40-A		499	8.62	-	1.22	
45×45×3-C80-A		529	4.31	13.36	1.30	3.10
45×45×3-C120-A		567	5.05	8.98	1.39	1.78
250×250×5-C0-A	45.0	2310	3.75	8.55	1.00	2.28
250×250×5-C40-A		4603	1.88	4.07	1.99	2.16
250×250×5-C80-A		7050	2.05	2.69	3.05	1.31
250×250×5-C120-A		9650	2.45	2.93	4.18	1.20
360×360×6-C0-A	55.0	4543	3.33	10.63	1.00	3.19
360×360×6-C40-A		8690	2.67	4.42	1.91	1.66
360×360×6-C80-A		13994	2.96	3.64	3.08	1.23
360×360×6-C120-A		19071	3.32	4.10	4.20	1.23
45×45×3-C0-B	10.0	545	1.55	1.96	1.00	1.26
45×45×3-C40-B		641	1.93	-	1.18	
45×45×3-C80-B		663	2.00	2.91	1.22	1.46
45×45×3-C120-B		682	1.77	2.85	1.25	1.61
160×160×4-C0-B	35.0	1437	2.34	4.26	1.00	1.82
160×160×4-C40-B		2182	1.83	2.06	1.52	1.13
160×160×4-C80-B		3428	1.59	2.97	2.39	1.87
160×160×4-C120-B		4460	1.76	2.42	3.10	1.38
250×250×5-C0-B	45.0	2718	4.80	7.89	1.00	1.64
250×250×5-C40-B		5089	4.01	7.12	1.87	1.78
250×250×5-C80-B		7410	2.34	3.62	2.73	1.55
250×250×5-C120-B		10125	2.59	3.22	3.73	1.24
360×360×6-C0-B	55.0	5093	3.42	3.56	1.00	1.04
360×360×6-C40-B		8996	2.74	10.74	1.77	3.92
360×360×6-C80-B		14406	3.09	4.03	2.83	1.30
360×360×6-C120-B		19615	3.20	3.89	3.85	1.22

Note: “ $Nor.$ ” represents the P_{FEA} normalized by that ($P_{FEA,0}$) without infilled concrete in the same series.

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Table 9: Dimensions and results of concrete-filled CFHSS rectangular stub columns in parametric study

Specimens	h/t	P_{FEA} (kN)	δ_u (mm)	$\delta_{0.85u}$ (mm)	$Nor.$	DI
120×60×3-C0-A	35.0	659	1.82	3.64	1.00	2.00
120×60×3-C40-A		912	1.98	3.99	1.38	2.02
120×60×3-C80-A		1096	1.23	2.25	1.66	1.83
120×60×3-C120-A		1382	1.30	1.54	2.10	1.18
180×90×3-C0-A	55.0	759	2.23	4.10	1.00	1.84
180×90×3-C40-A		1550	1.46	2.90	2.04	1.99
180×90×3-C80-A		2044	1.72	1.94	2.69	1.13
180×90×3-C120-A		2673	1.95	2.17	3.52	1.11
320×160×4-C0-A	75.0	1829	5.53	11.64	1.00	2.10
320×160×4-C40-A		3595	2.55	2.83	1.97	1.11
320×160×4-C80-A		5619	2.91	3.18	3.07	1.09
320×160×4-C120-A		7586	3.10	4.24	4.15	1.37
120×60×3-C0-B	35.0	807	2.46	3.33	1.00	1.35
120×60×3-C40-B		1128	2.38	3.37	1.40	1.42
120×60×3-C80-B		1232	2.08	3.14	1.53	1.51
120×60×3-C120-B		1468	1.33	2.33	1.82	1.75
180×90×3-C0-B	55.0	920	2.99	4.19	1.00	1.40
180×90×3-C40-B		1543	1.74	3.41	1.68	1.96
180×90×3-C80-B		2182	1.83	2.06	2.37	1.13
180×90×3-C120-B		2781	1.98	2.23	3.02	1.13
320×160×4-C0-B	75.0	2142	6.41	9.83	1.00	1.53
320×160×4-C40-B		3778	2.65	6.47	1.76	2.44
320×160×4-C80-B		5805	2.94	3.25	2.71	1.11
320×160×4-C120-B		7652	3.34	3.69	3.57	1.10

Note: “ $Nor.$ ” represents the P_{FEA} normalized by that ($P_{FEA,0}$) without infilled concrete in the same series.

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Table 10: Comparison of test and FE results with predictions from EC4 [22]

Specimens	No.			P_u/P_{EC}	P_u/P_{EC^*}	P_u/P_{EC^\wedge}	$P_u/P_{EC^{*\wedge}}$
Square specimens	21	Series A	Mean	1.03	1.10	1.09	1.18
			COV	0.137	0.096	0.115	0.074
	22	Series B	Mean	0.95	1.08	1.01	1.15
			COV	0.180	0.097	0.167	0.091
	43	Series A&B	Mean	0.99	1.09	1.05	1.17
			COV	0.162	0.096	0.147	0.083
Rectangular specimens	13	Series A	Mean	0.96	1.09	1.02	1.16
			COV	0.127	0.064	0.115	0.063
	9	Series B	Mean	0.81	1.05	0.86	1.13
			COV	0.084	0.041	0.109	0.065
	22	Series A&B	Mean	0.90	1.07	0.95	1.15
			COV	0.141	0.059	0.138	0.064

918 Note: P_{EC^*} = modified predicted strength incorporating effective area of steel tube; P_{EC^\wedge} = modified predicted
919 strength incorporating the effective compressive strength of concrete; and $P_{EC^{*\wedge}}$ = modified predicted strength
920 incorporating both the effective area of steel tube and effective compressive strength of concrete.
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Table 11: Comparison of test and FE results with predictions from AISC [23]

Specimens	No.			P_u/P_{AISC}	P_u/P_{AISC^\wedge}
Square specimens	21	Series A	Mean	1.12	1.19
			COV	0.101	0.097
	22	Series B	Mean	1.07	1.12
			COV	0.140	0.147
	43	Series A&B	Mean	1.09	1.16
			COV	0.123	0.126
Rectangular specimens	13	Series A	Mean	1.17	1.24
			COV	0.142	0.173
	9	Series B	Mean	1.20 (1.30)*	1.29 (1.41)*
			COV	0.209 (0.300)*	0.242(0.325)*
	22	Series A&B	Mean	1.18 (1.22)*	1.26 (1.31)*
			COV	0.170 (0.228)*	0.200 (0.256)*

926 Note: “(x)*” = modified predicted strength incorporating effective area of steel tube; P_{AISC^\wedge} = modified predicted
927 strength incorporating the effective compressive strength of concrete
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Table 12: Comparison of test and FE results with codified predictions for specimens with different infilled concrete compressive strengths

(a) Square specimens

Cases		No. of columns	P_u/P_{EC}	P_u/P_{EC^*}	P_u/P_{EC^\wedge}	$P_u/P_{EC^{*\wedge}}$	P_u/P_{AISC}	P_u/P_{AISC^\wedge}
Infilled concrete C40	Mean	14	1.04	1.17	1.04	1.17	1.12	1.12
	COV		0.232	0.120	0.232	0.120	0.176	0.176
Infilled concrete C80	Mean	15	0.97	1.07	1.05	1.16	1.08	1.15
	COV		0.121	0.050	0.109	0.051	0.088	0.087
Infilled concrete C120	Mean	14	0.96	1.03	1.06	1.16	1.08	1.20
	COV		0.076	0.046	0.060	0.072	0.086	0.102
All cases	Mean	43	0.99	1.09	1.05	1.17	1.09	1.16
	COV		0.162	0.096	0.147	0.083	0.123	0.126

Note: P_{EC^*} = modified predicted strength incorporating effective area of steel tube; P_{EC^\wedge} = modified predicted strength incorporating the effective compressive strength of concrete; and $P_{EC^{*\wedge}}$ = modified predicted strength incorporating both the effective area of steel tube and effective compressive strength of concrete; P_{AISC^\wedge} = modified predicted strength incorporating the effective compressive strength of concrete.

(b) Rectangular specimens

Cases		No. of columns	P_u/P_{EC}	P_u/P_{EC^*}	P_u/P_{EC^\wedge}	$P_u/P_{EC^{*\wedge}}$	P_u/P_{AISC}	P_u/P_{AISC^\wedge}
Infilled concrete C40	Mean	8	0.92	1.12	0.92	1.12	1.18 (1.24)*	1.18 (1.24)*
	COV		0.211	0.054	0.211	0.054	0.157 (0.256)*	0.157 (0.256)*
Infilled concrete C80	Mean	7	0.88	1.05	0.94	1.14	1.18 (1.21)*	1.27 (1.32)*
	COV		0.106	0.038	0.101	0.056	0.195 (0.245)*	0.220 (0.281)*
Infilled concrete C120	Mean	7	0.89	1.03	1.00	1.18	1.19 (1.21)*	1.35 (1.38)*
	COV		0.061	0.043	0.060	0.076	0.183 (0.211)*	0.221 (0.258)*
All cases	Mean	22	0.90	1.07	0.95	1.15	1.18 (1.22)*	1.26 (1.31)*
	COV		0.141	0.059	0.138	0.064	0.170 (0.228)*	0.200 (0.256)*

Note: “(x)” result by using reduced cross section area of steel tube.

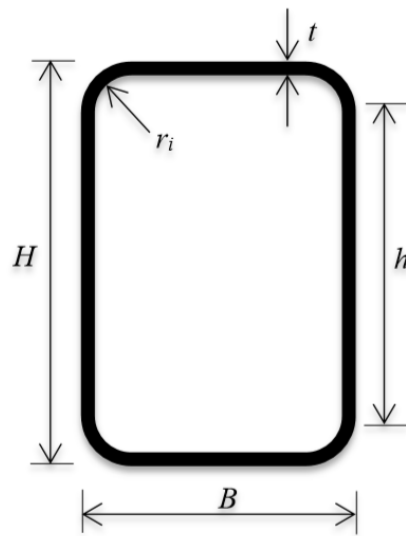
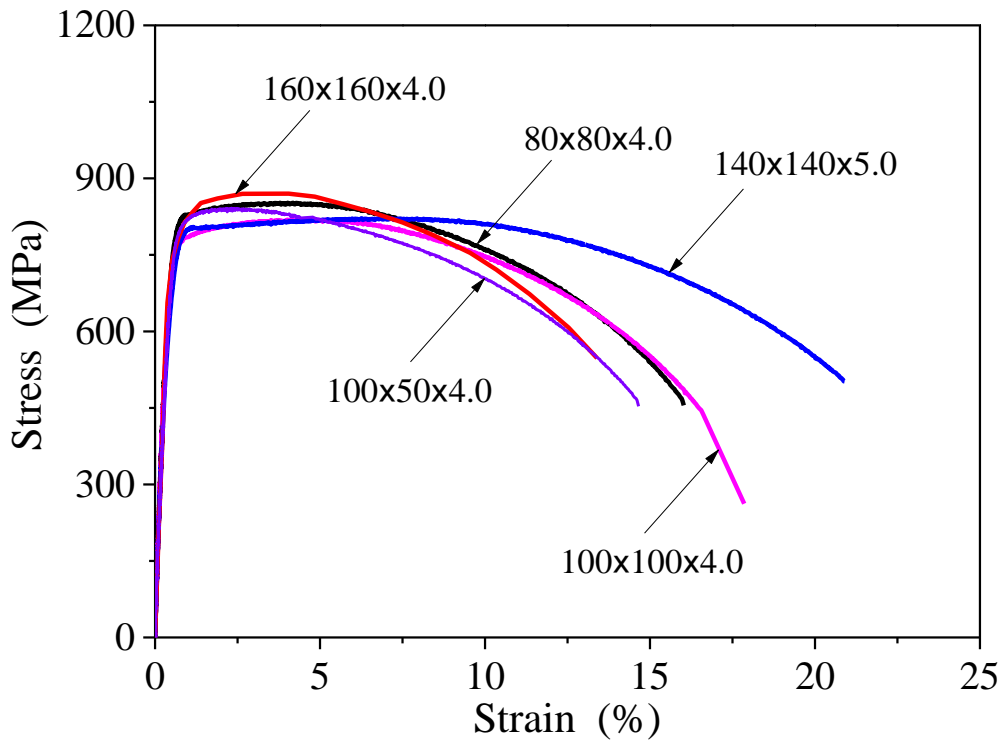
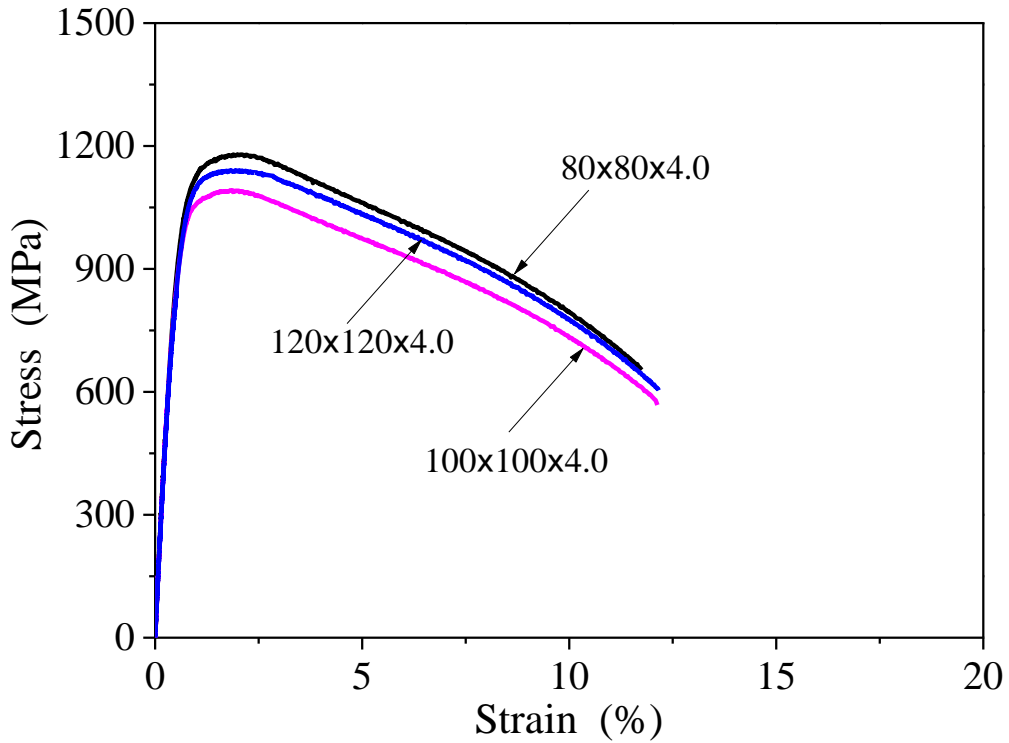


Figure 1: Symbols of CFHSS cross section



a) Members with nominal 0.2% proof stress of 700 MPa



b) Members with nominal 0.2% proof stress of 900 MPa

Figure 2: Measured stress-strain curves of high strength steel tubular members

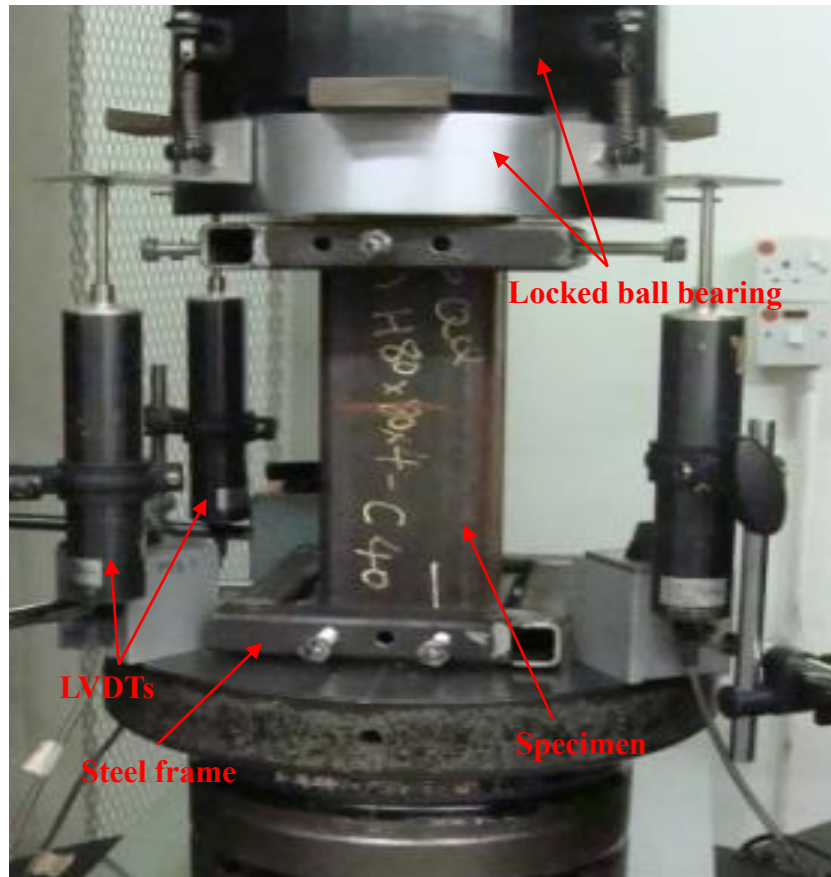


Figure 3: Test setup of concrete-filled stub column Specimen 80×80×4-C40-A

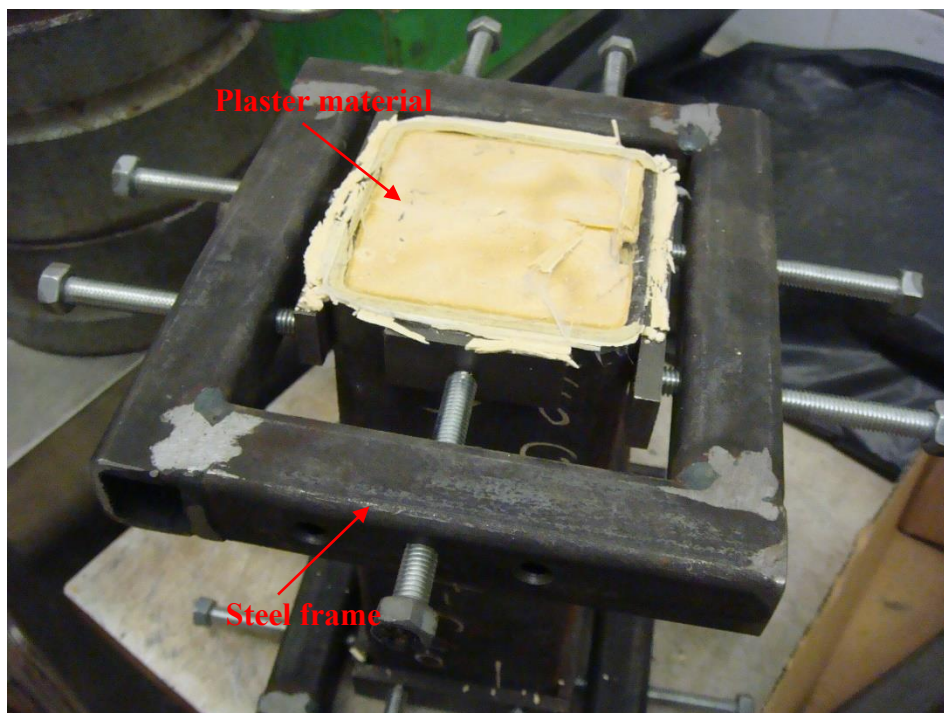
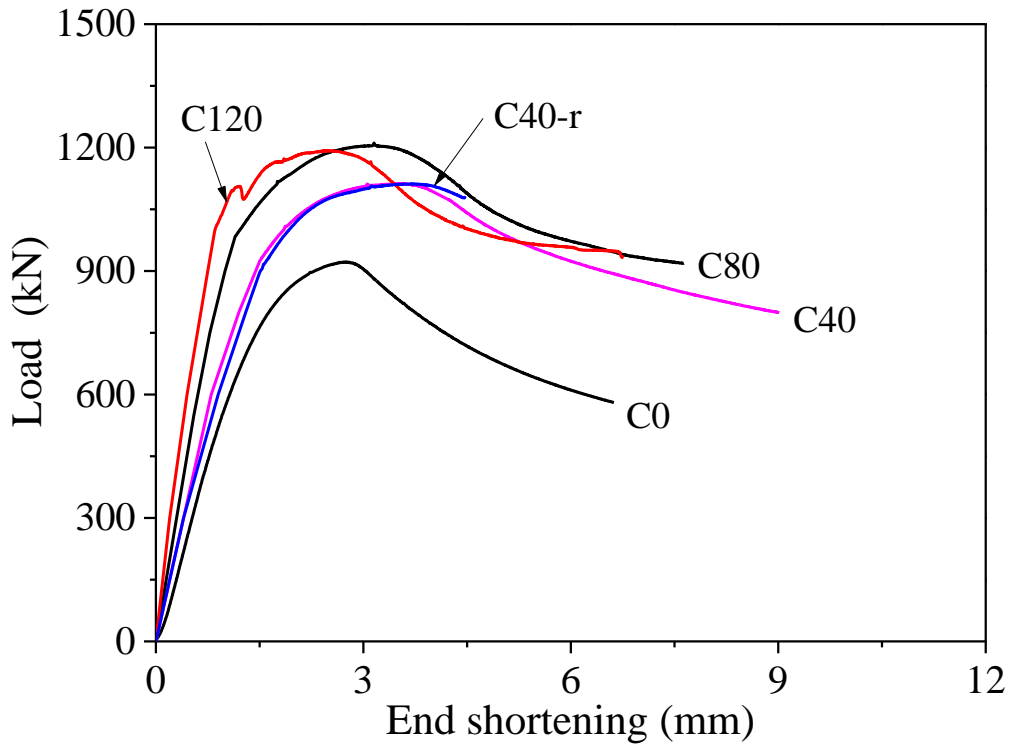
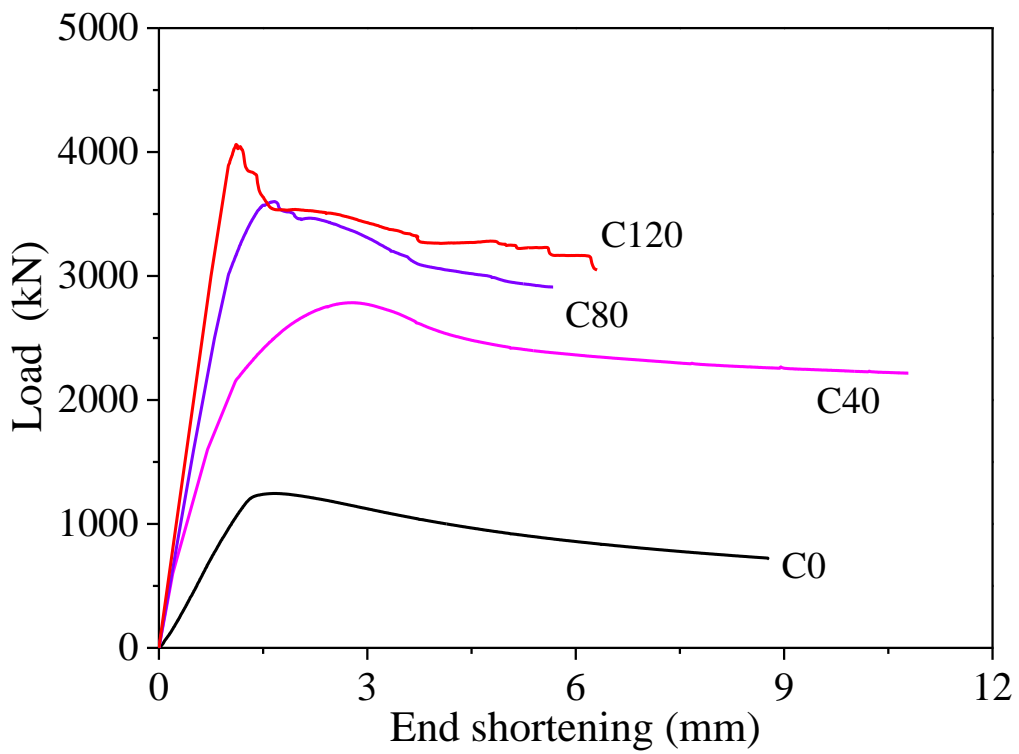


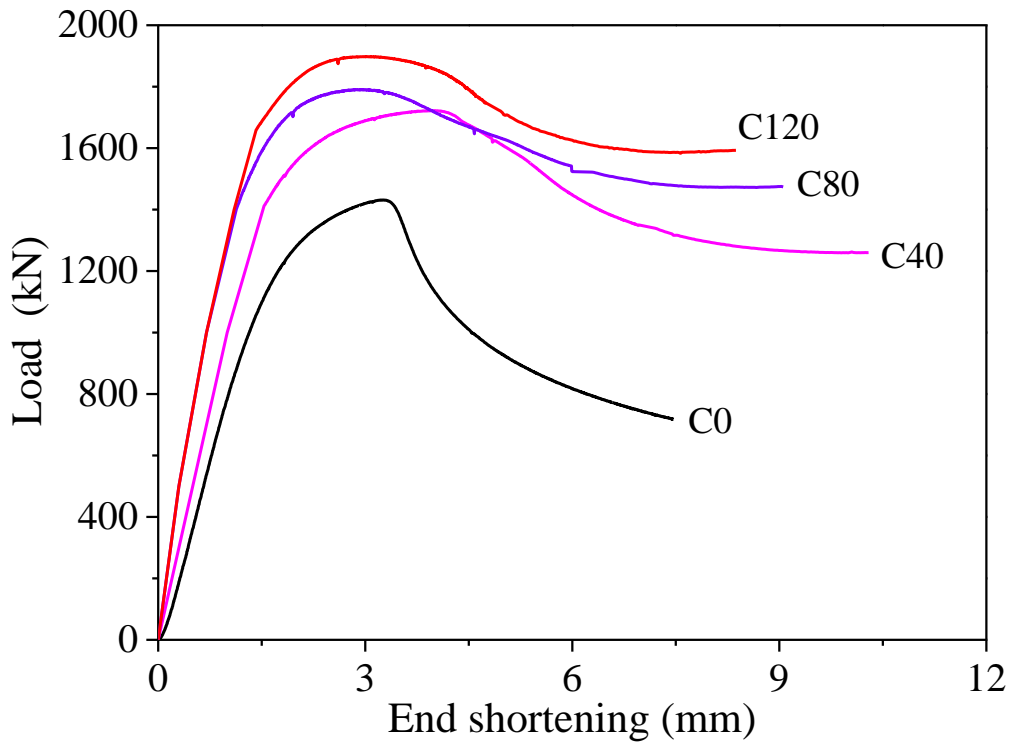
Figure 4: Specimen 80×80×4-C40-A after compressive test



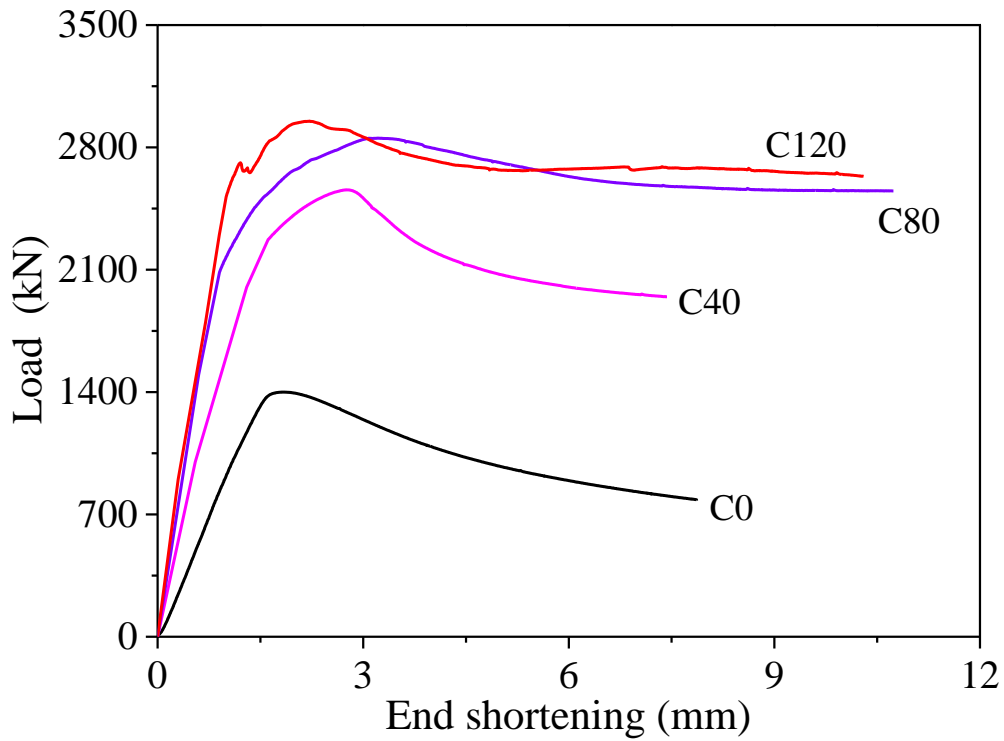
(a) Series 100×50×4-A



(b) Series 160×160×4-A



(c) Series 80×80×4-B



(d) Series 120×120×4-B

Figure 5: Load-end shortening curves of concrete-filled CFHSS stub columns

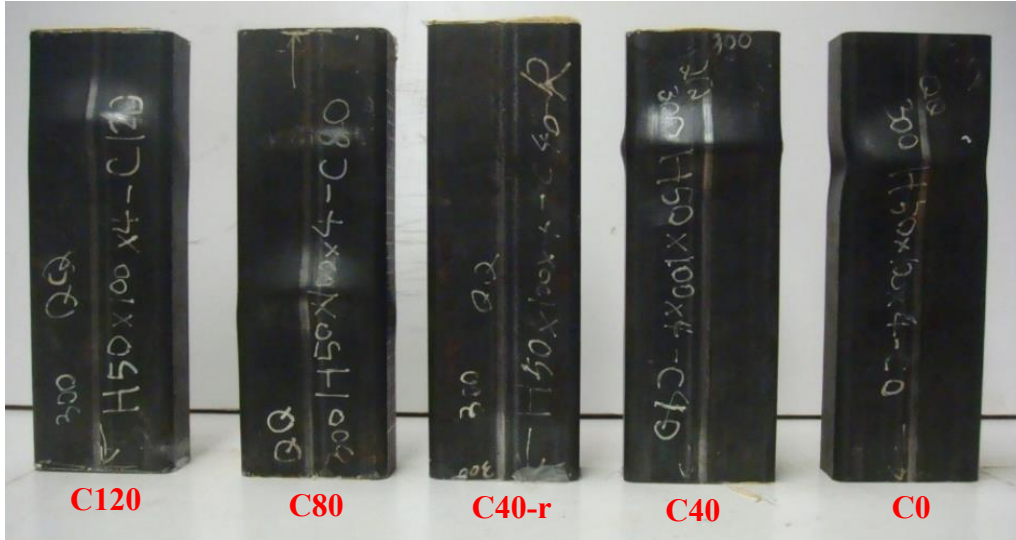


Figure 6: Failure modes of stub columns (series 100×50×4-A)

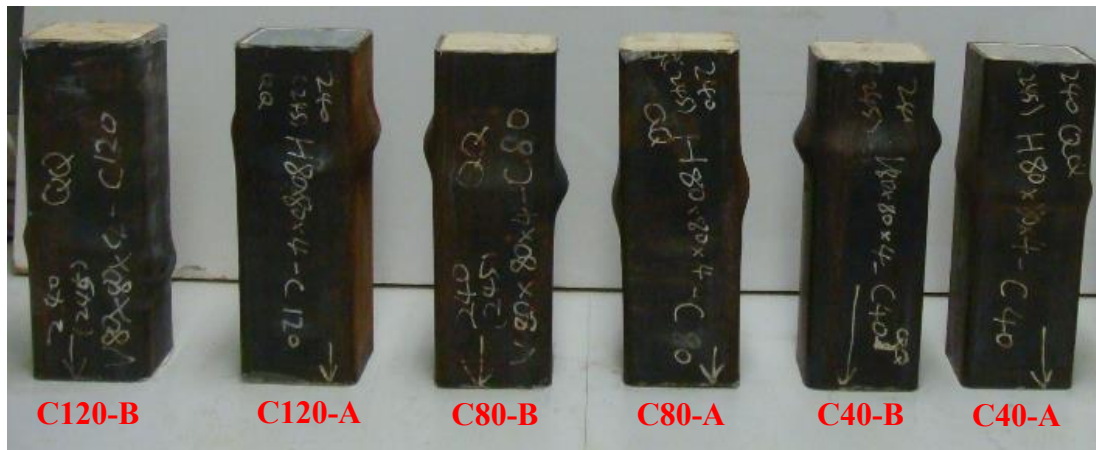


Figure 7: Failure modes of stub columns (series 80×80×4-A and 80×80×4-B)

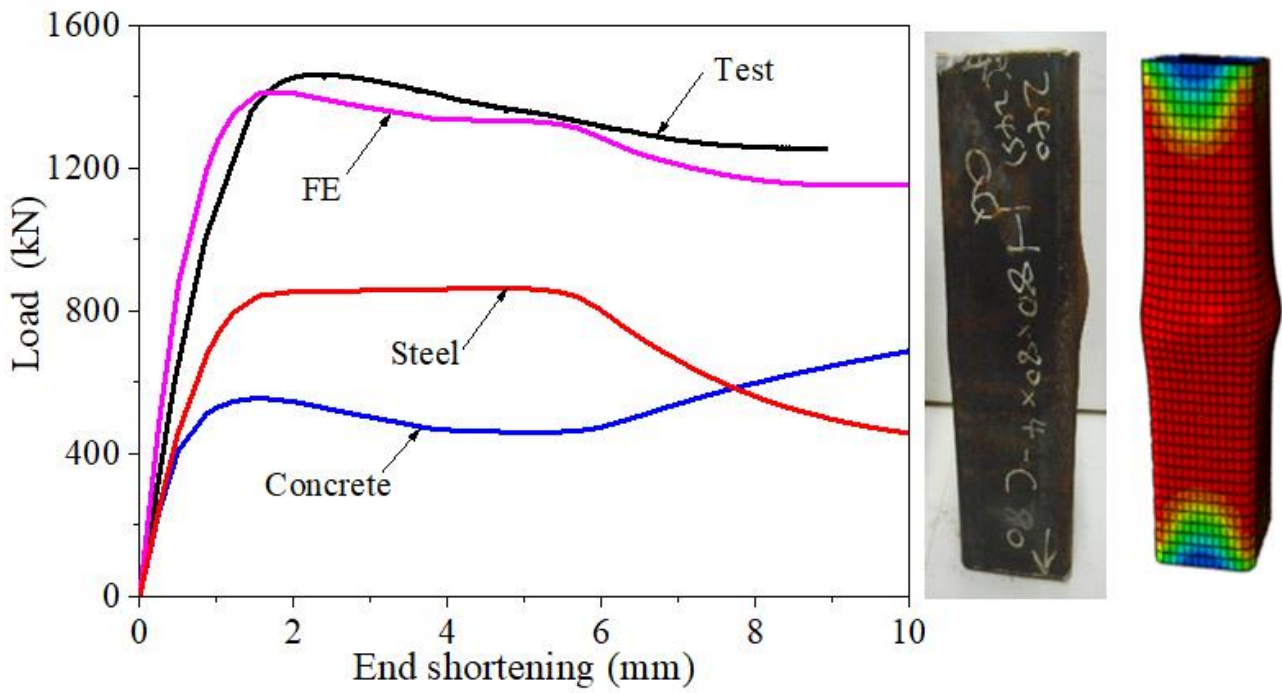


Figure 8: Comparison of test results and numerical predictions for Specimen 80×80×4-C80-A

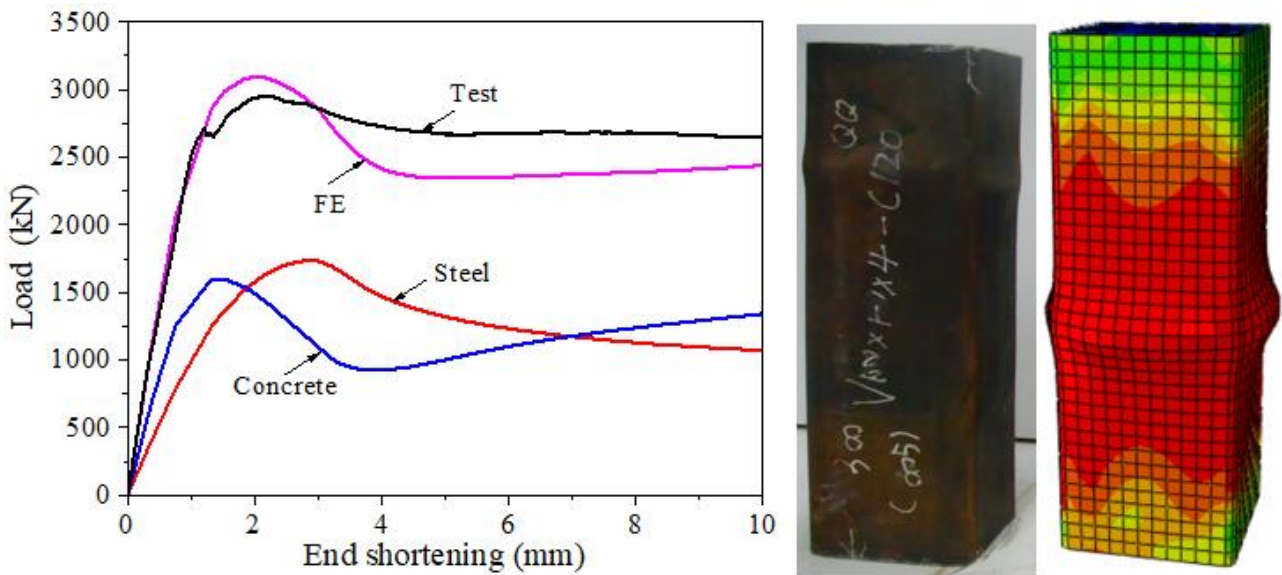
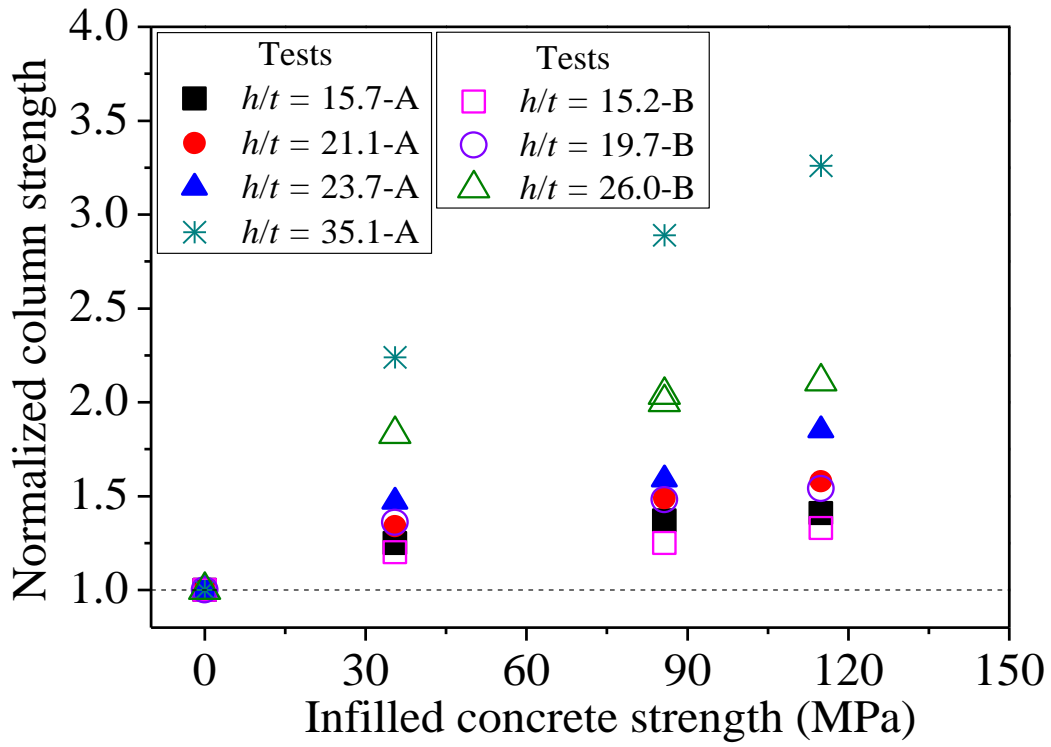
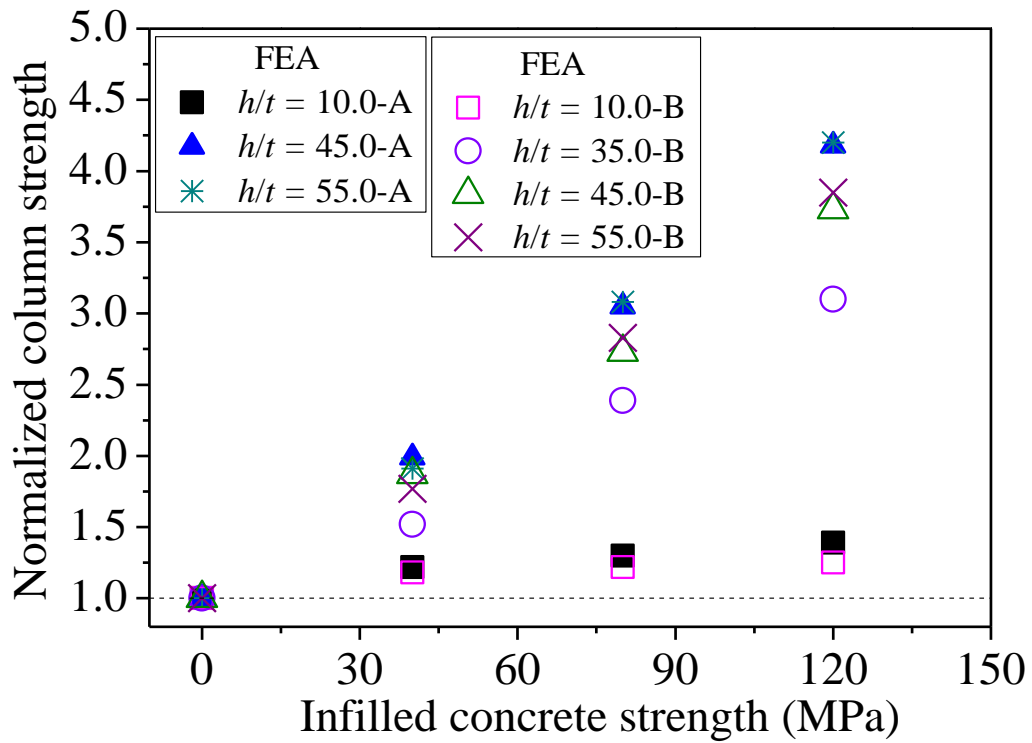


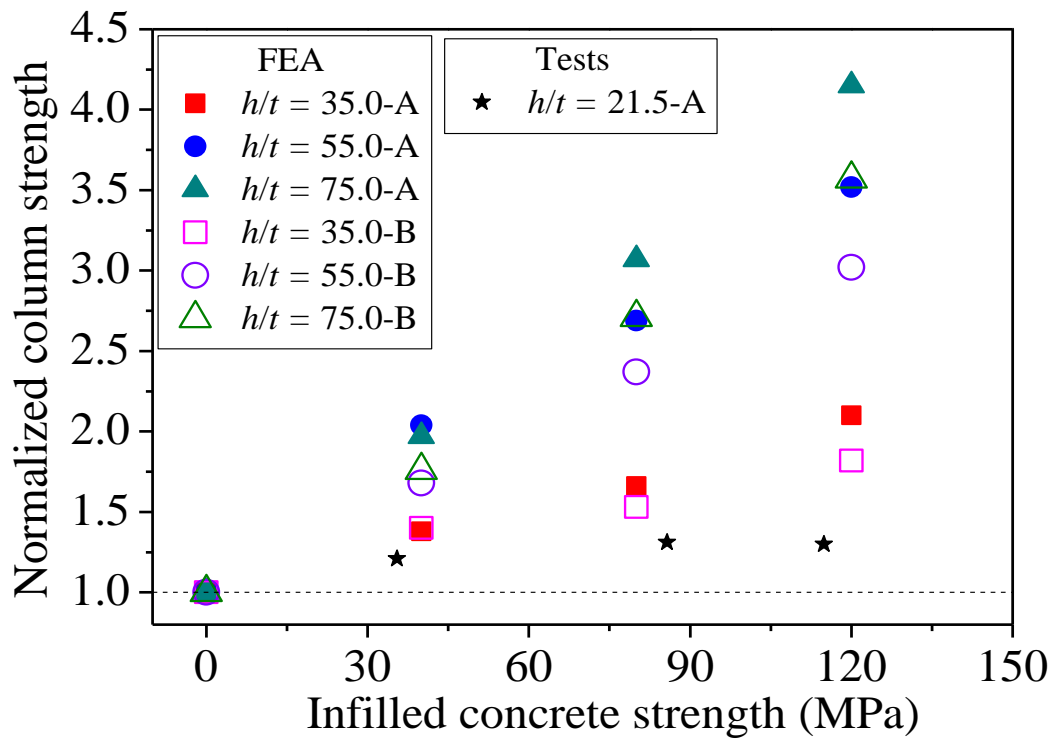
Figure 9: Comparison of test results and numerical predictions for Specimen 120×120×4-C120-B



(a) Square sections from test results



(b) Square sections from FEA results



(c) Rectangular sections

Figure 10: Comparison of column strength enhancement with different infilled concrete strengths

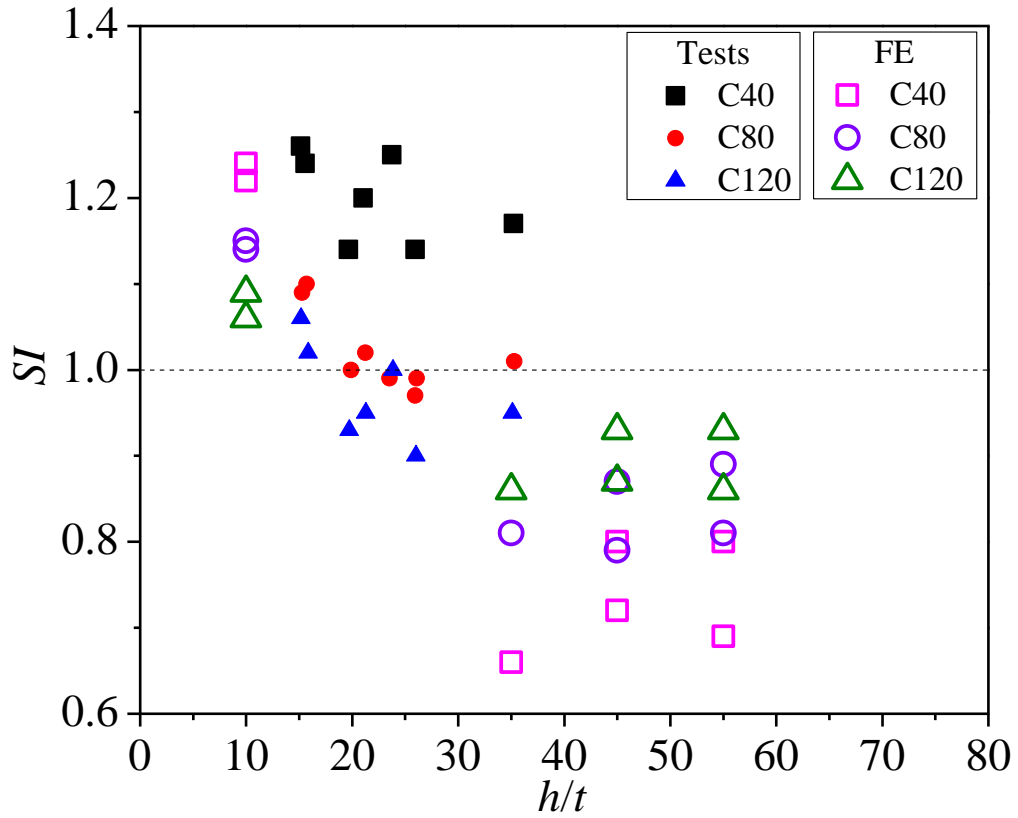


Figure 11: Effects of h/t on SI on concrete-filled CFHSS stub columns with square sections

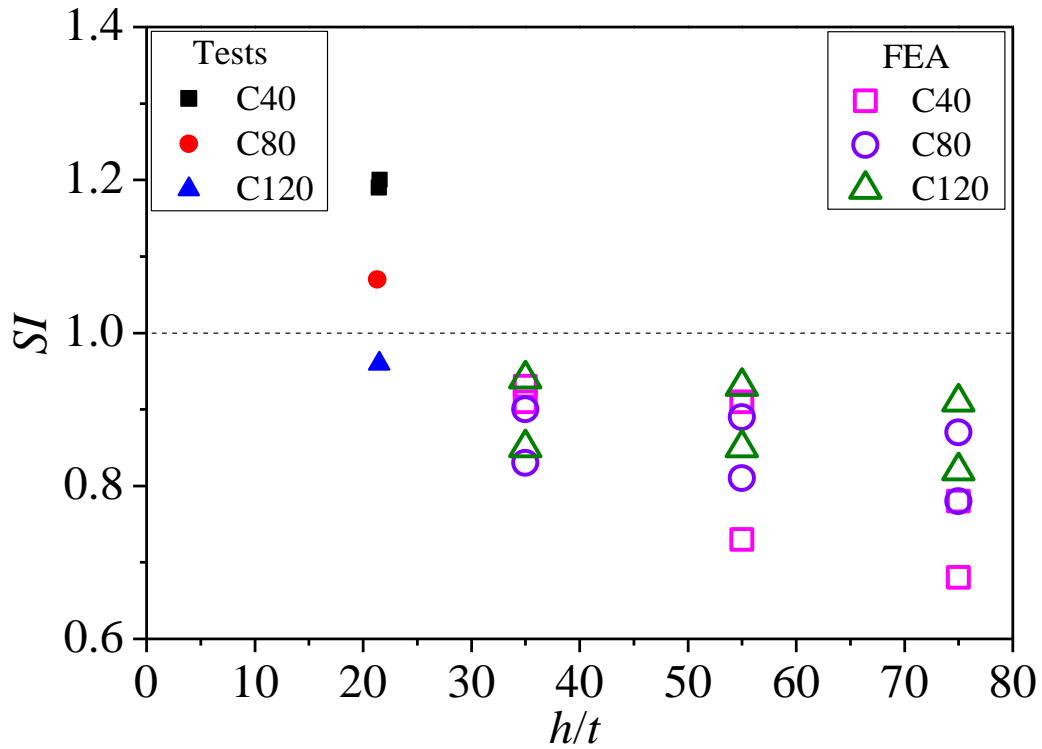
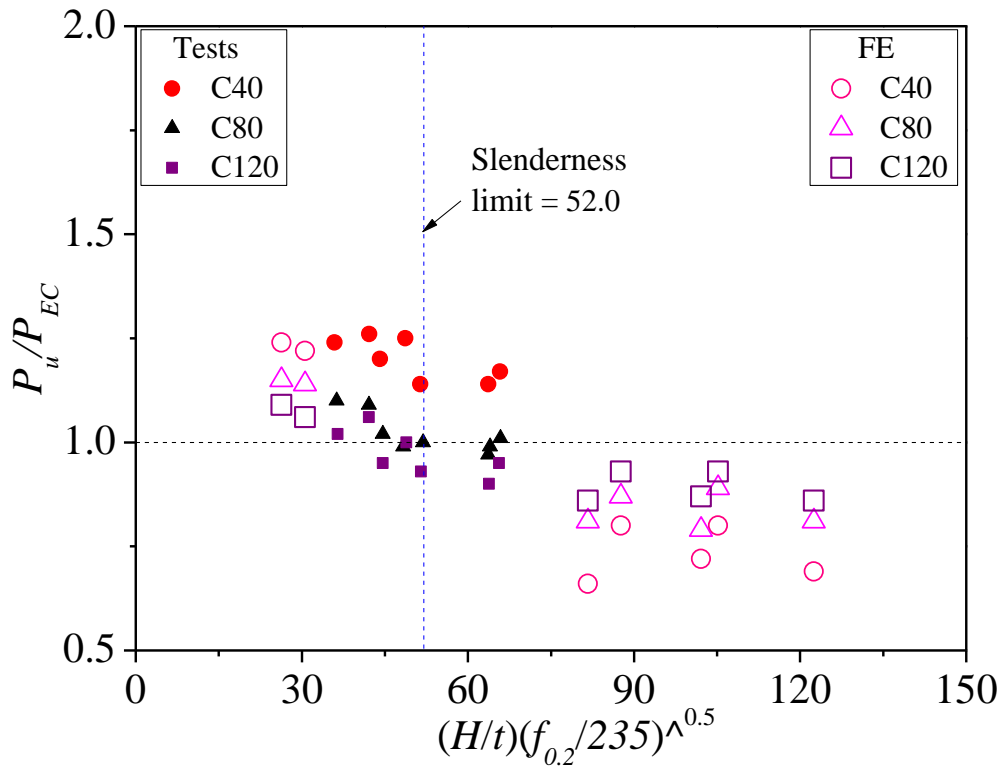
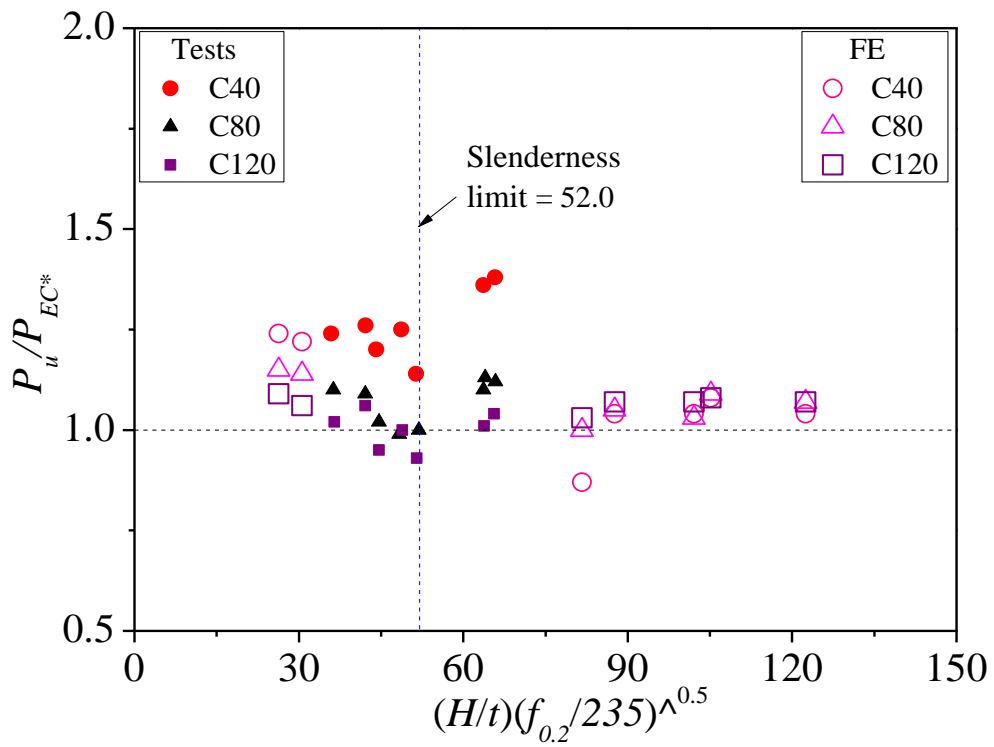


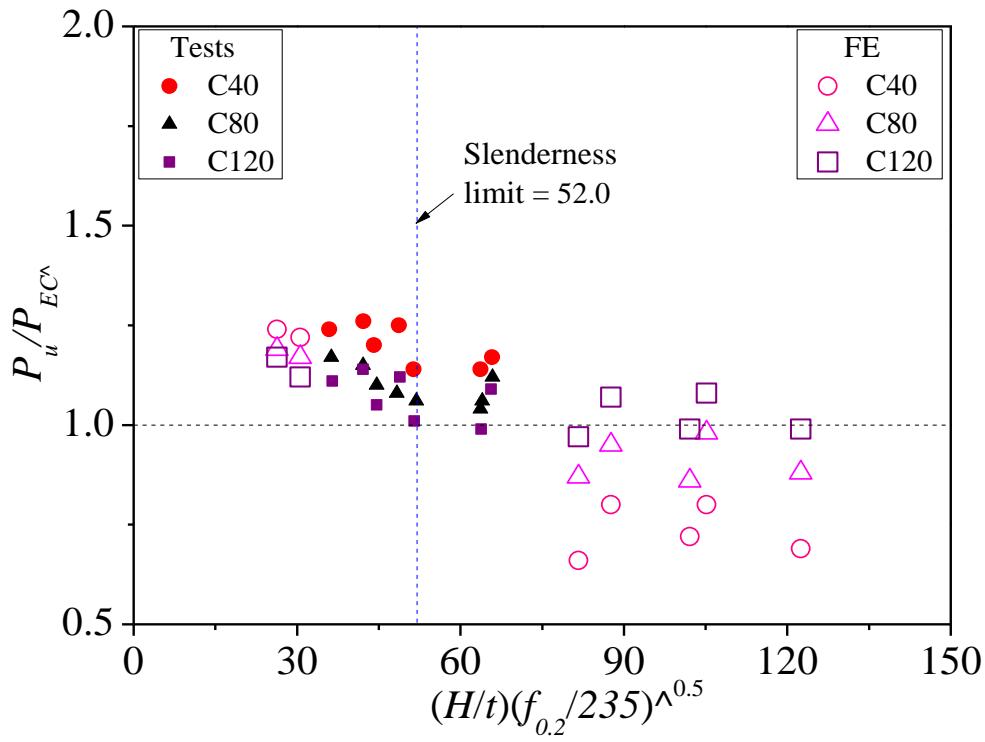
Figure 12: Effects of h/t on SI for concrete-filled CFHSS stub columns with rectangular sections



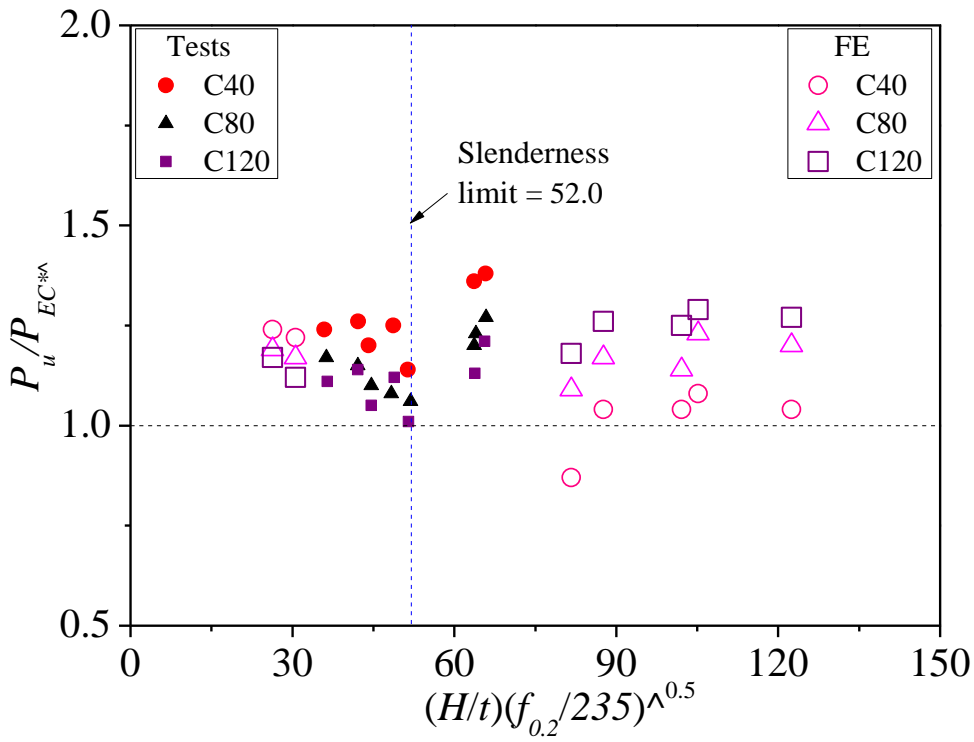
(a) Predictions of P_{EC}



(b) Predictions of P_{EC^*} with consideration of effective area

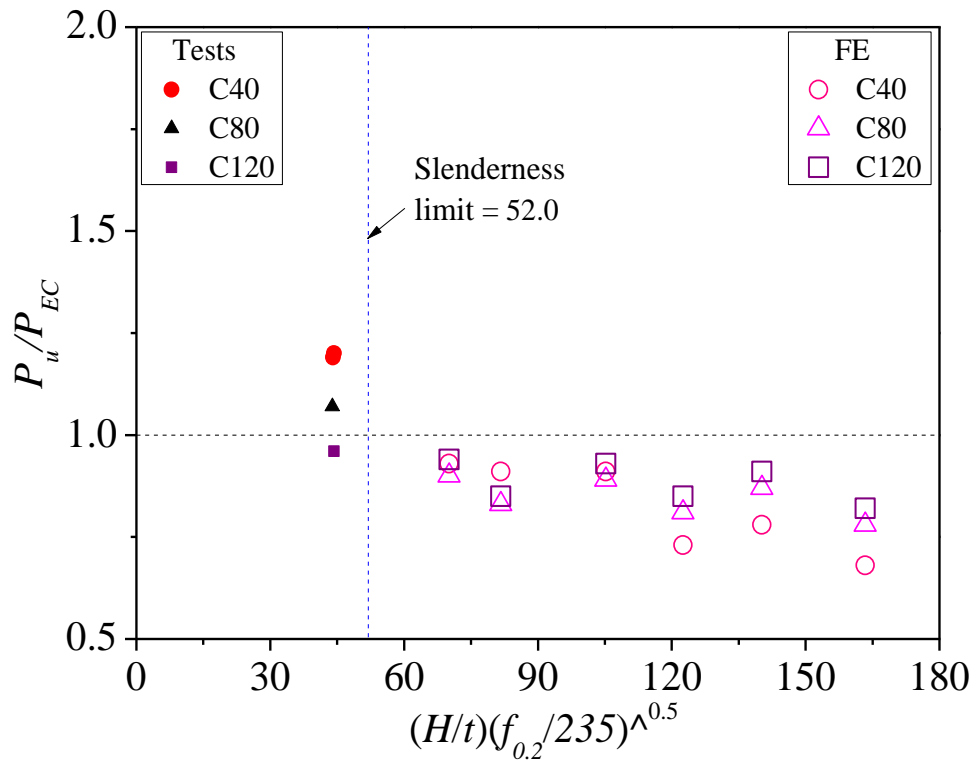


(c) Predictions of P_{EC^A} with consideration of effective concrete strength

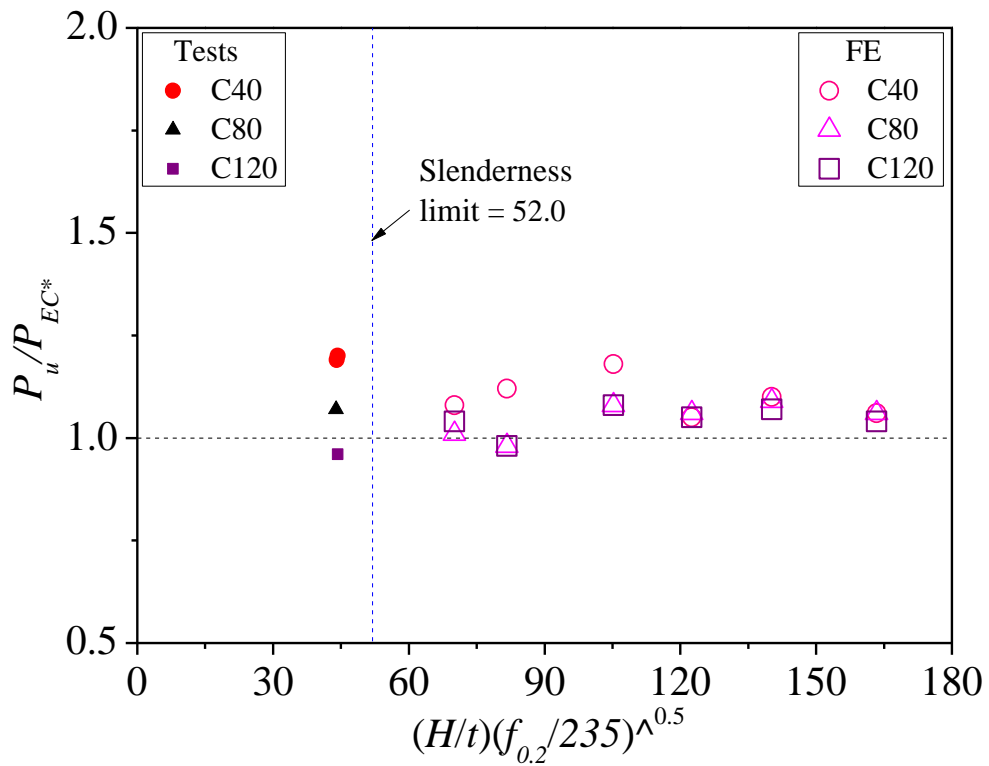


(d) Predictions of $P_{EC^{A*}}$ with consideration of both effective area and effective concrete strength

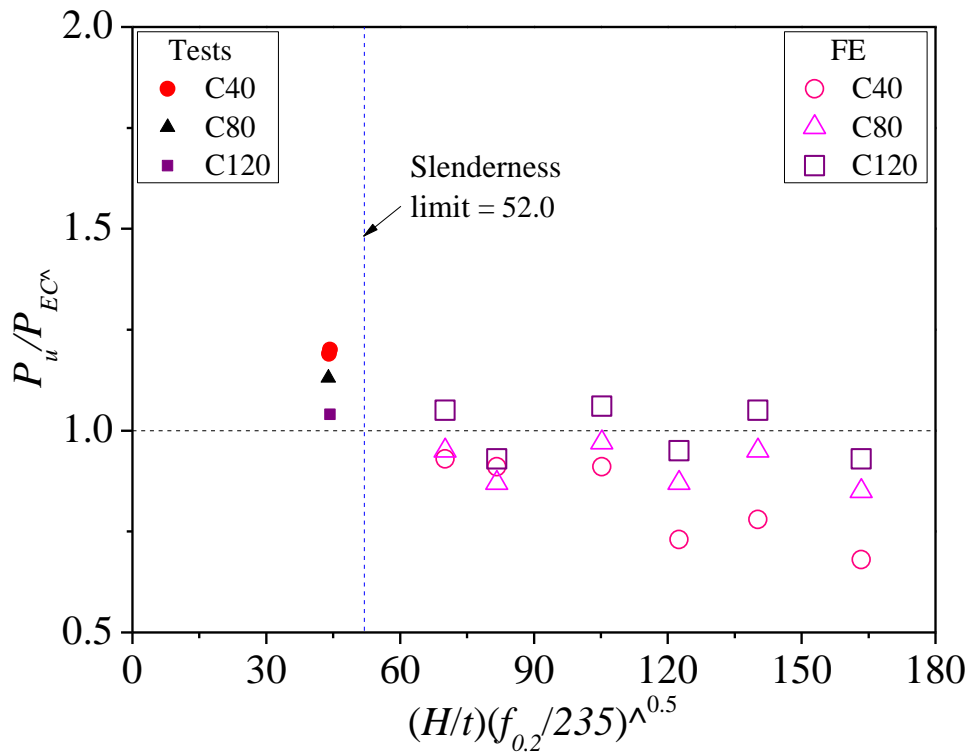
Figure 13: Assessment of predictions from EC4 [22] for square sections



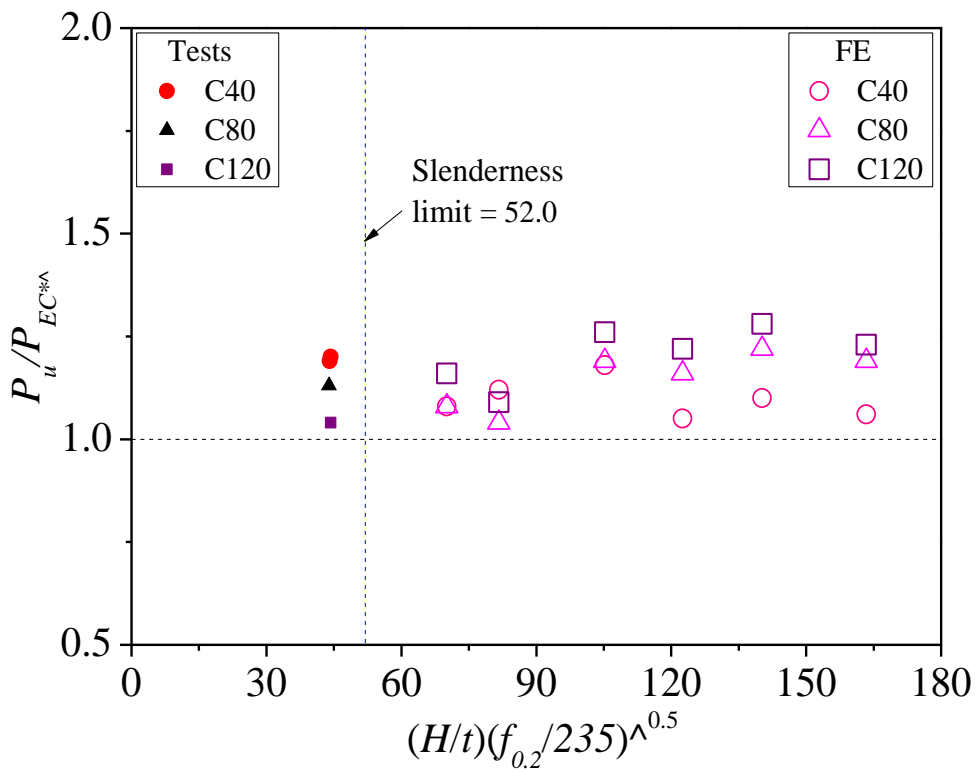
(a) Predictions of P_{EC}



(b) Predictions of P_{EC^*} with consideration of effective areas

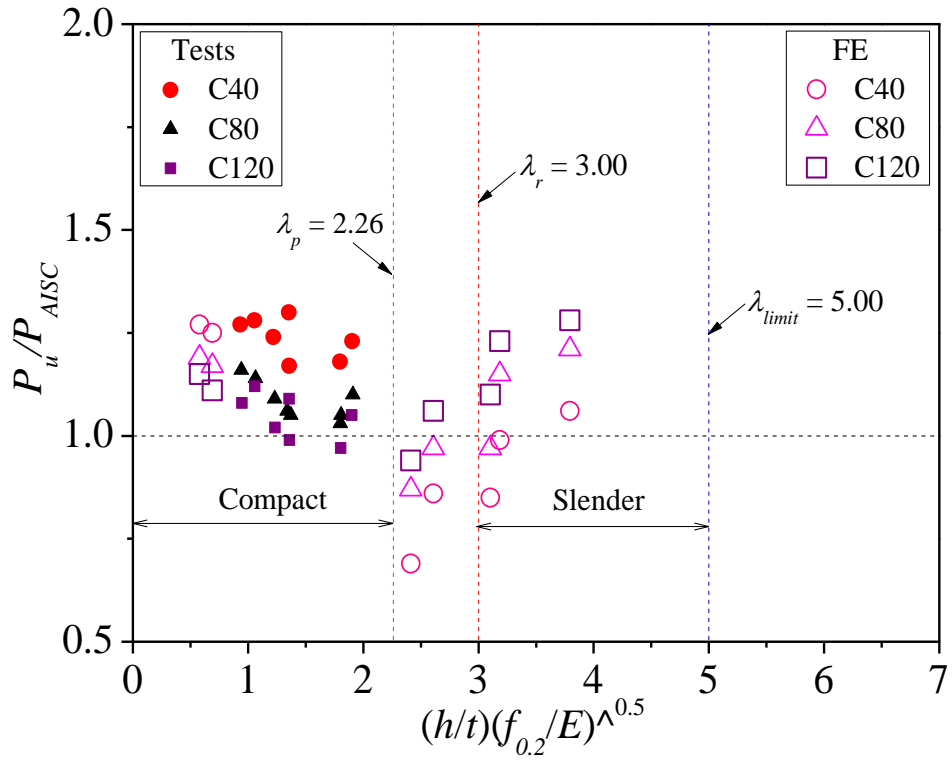


(c) Predictions of P_{EC^A} with consideration of effective concrete strength

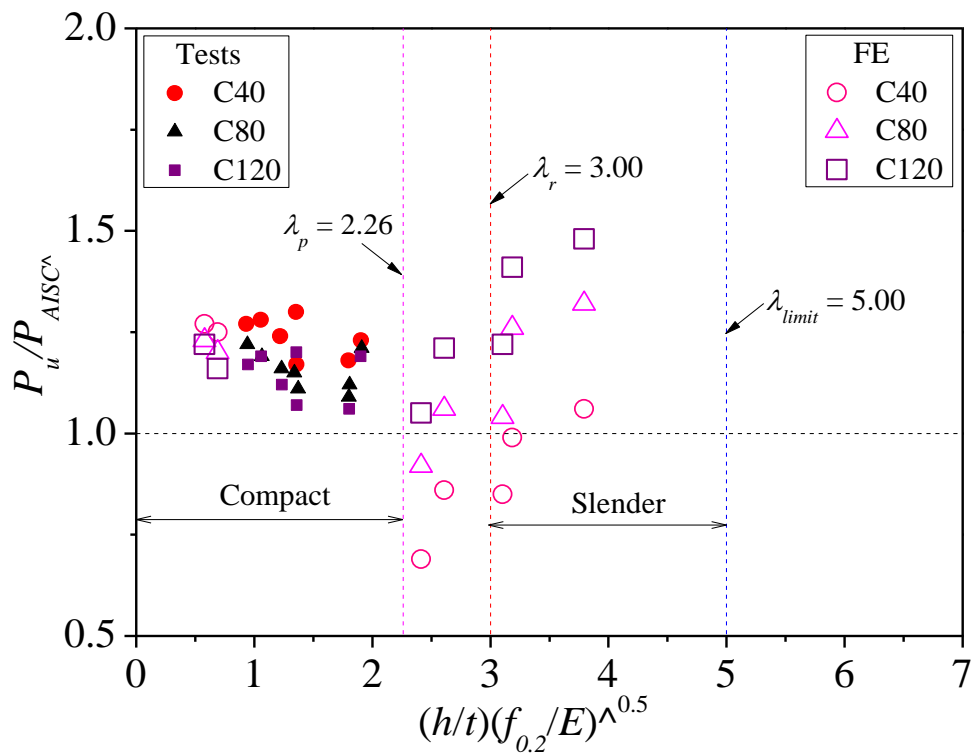


(d) Predictions of $P_{EC^{*A}}$ with consideration of both effective area and effective concrete strength

Figure 14: Assessment of predictions from EC4 [22] for rectangular sections

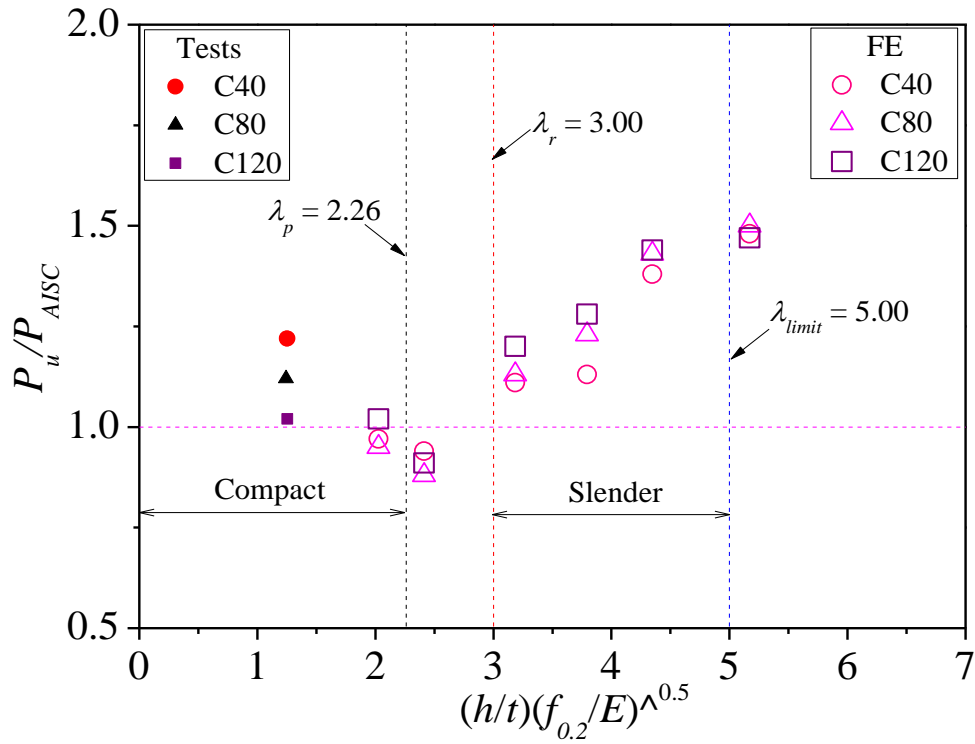


(a) Predictions of P_{AISC}

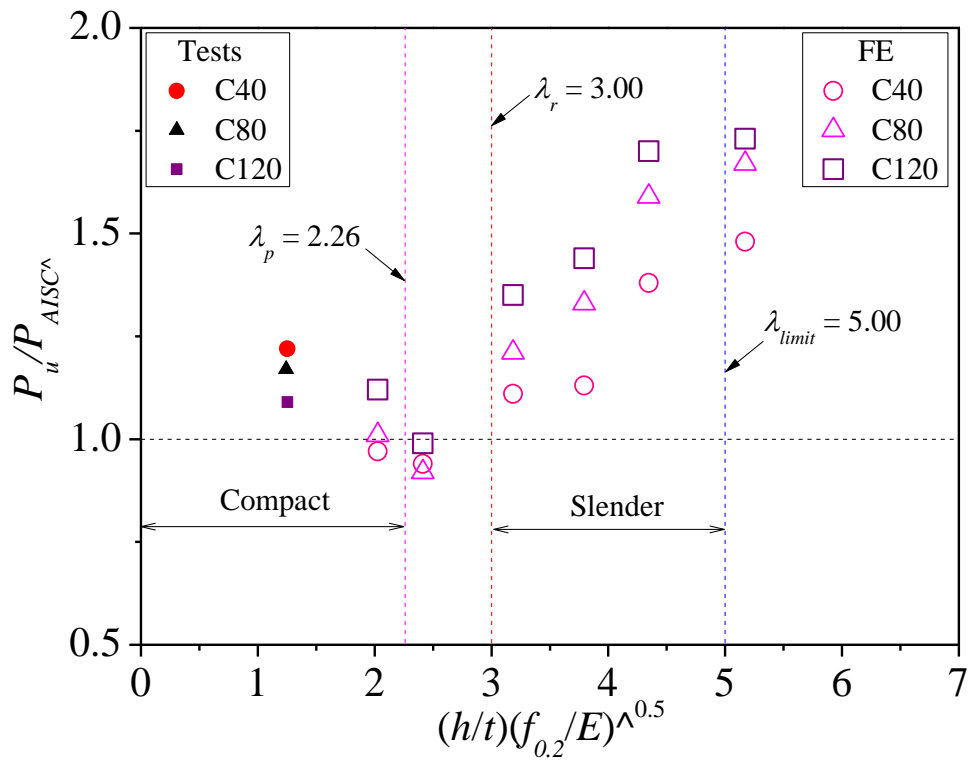


(b) Predictions of P_{AISC^*} with consideration of effective concrete strength

Figure 15: Assessment of predictions from AISC [23] for square sections



(a) Predictions of P_{AISC}



(b) Predictions of $P_{AISC^}$ with consideration of effective concrete strength

Figure 16: Assessment of predictions from AISC [23] for rectangular sections