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# High luminosity, slow ejecta and persistent carbon lines: SN 2009dc challenges thermonuclear explosion scenarios<sup>★</sup>

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# **ABSTRACT**

Extended optical and near-IR observations reveal that SN 2009dc shares a number of similarities with normal Type Ia supernovae (SNe Ia), but is clearly overluminous, with a (pseudobolometric) peak luminosity of  $\log(L) = 43.47$  (erg s<sup>-1</sup>). Its light curves decline slowly over half a year after maximum light [ $\Delta m_{15}(B)_{\text{true}} = 0.71$ ], and the early-time near-IR light curves show secondary maxima, although the minima between the first and the second peaks are not very pronounced. The bluer bands exhibit an enhanced fading after  $\sim 200$  d, which might be caused by dust formation or an unexpectedly early IR catastrophe. The spectra of SN 2009dc are dominated by intermediate-mass elements and unburned material at early times, and by iron-group elements at late phases. Strong C II lines are present until  $\sim$ 2 weeks past maximum, which is unprecedented in thermonuclear SNe. The ejecta velocities are significantly lower than in normal and even subluminous SNe Ia. No signatures of interaction with a circumstellar medium (CSM) are found in the spectra. Assuming that the light curves are powered by radioactive decay, analytic modelling suggests that SN 2009dc produced  $\sim$ 1.8 M<sub> $\odot$ </sub> of <sup>56</sup>Ni assuming the smallest possible rise time of 22 d. Together with a derived total ejecta mass of  $\sim$ 2.8 M $_{\odot}$ , this confirms that SN 2009dc is a member of the class of possible super-Chandrasekhar-mass SNe Ia similar to SNe 2003fg, 2006gz and 2007if. A

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study of the hosts of SN 2009dc and other superluminous SNe Ia reveals a tendency of these SNe to explode in low-mass galaxies. A low metallicity of the progenitor may therefore be an important prerequisite for producing superluminous SNe Ia. We discuss a number of possible explosion scenarios, ranging from super-Chandrasekhar-mass white-dwarf progenitors over dynamical white-dwarf mergers and Type  $I_{\frac{1}{2}}$  SNe to a core-collapse origin of the explosion. None of the models seems capable of explaining all properties of SN 2009dc, so that the true nature of this SN and its peers remains nebulous.

**Key words:** supernovae: general – supernovae: individual: SN 2006gz – supernovae: individual: SN 2007if – supernovae: individual: SN 2009dc – galaxies: individual: UGC 10063 – galaxies: individual: UGC 10064.

#### 1 INTRODUCTION

Owing to their remarkable homogeneity in peak luminosity and light-curve shape, Type Ia supernovae (SNe Ia) are considered excellent tools to measure luminosity distances in the Universe, suitable to constrain possible cosmologies also beyond the converged  $\Lambda$  Cold Dark Matter ( $\Lambda$ CDM) model (e.g. Leibundgut 2001). In particular, with sufficiently precise observations of SNe Ia at low and high redshift, the expansion history of the Universe can be reconstructed and a possible time evolution of Dark Energy can be probed (e.g. Riess et al. 2007).

Thanks to extensive observational campaigns and sophisticated modelling efforts over the past decade, some convergence has been achieved about the origin of 'normal' SNe Ia. There is a widespread consensus on the single-degenerate (SD) scenario of a white dwarf (WD) accreting matter from a non-degenerate companion until it approaches the Chandrasekhar mass  $(M_{Ch})$  and ignites carbon near its centre. This leads to a thermonuclear runaway disrupting the star (e.g. Hillebrandt & Niemeyer 2000). Since the explosions always occur close to  $M_{\rm Ch}$ , this scenario provides a natural explanation for the observed homogeneity among 'normal' SNe Ia. Within this picture, the ratio of nuclear-statistical-equilibrium material to intermediate-mass elements (IMEs) in the ejecta is likely the key parameter for both the width of the SN light curve (through the opacity generated by Fe-group elements) and its peak luminosity (through the radioactive decay of <sup>56</sup>Ni; Pinto & Eastman 2001; Mazzali et al. 2001, 2007).

However, this emerging picture has recently been challenged by the discovery of a handful of objects whose properties cannot readily be explained within the  $M_{\rm Ch}$  framework (Howell et al. 2006; Branch 2006; Hicken et al. 2007; Yamanaka et al. 2009). These SNe are characterized by high peak luminosities, a factor ~2 larger than in all other SNe Ia ( $M_{V,\text{max}} \sim -20$ ). At the same time, apart from their comparatively low ejecta velocities they share strong spectroscopic similarity with ordinary SNe Ia. To explain the early light curves of these events within spherical symmetry, a <sup>56</sup>Ni mass exceeding 1 M<sub>☉</sub> and a total ejecta mass in excess of 1.4 M<sub>☉</sub> are required (Howell et al. 2006). The explosion of a super- $M_{\rm Ch}$  WD stabilized by strong differential rotation (Howell et al. 2006; Branch 2006) or a merger of two WDs, in sum again exceeding  $M_{\rm Ch}$  (Hicken et al. 2007), have been suggested as possible scenarios. However, Hillebrandt, Sim & Röpke (2007) and Sim et al. (2007) argued that these events could possibly be consistent with  $M_{Ch}$ -WD explosions if strong deviations from spherical symmetry are invoked, with the ignition point located far off-centre and the <sup>56</sup>Ni distribution being very one-sided. Alternatively, energy sources other than radioactivity may have to be considered.

Understanding superluminous SNe Ia is not only a merit by its own, but has important implications for cosmology. Spectroscopically similar to ordinary SNe Ia, some of these events may have entered into the cosmological SN Ia data sets, especially at high z where they are favoured by their luminosity and where the data quality is mostly poor. Moreover, while they are apparently rare in the present Universe, without a better knowledge of their progenitors and explosion mechanisms, it cannot be ruled out that superluminous SNe Ia were more abundant in the past. Since they may not obey the light-curve width – luminosity relations used to standardize SNe Ia, they may introduce systematic errors in the reconstruction of H(z) using SN data.

With the observations of SN 2009dc presented in this work, a comprehensive optical and near-IR (NIR) data set of a superluminous SN Ia becomes available, extending observations of the same SN presented by Yamanaka et al. (2009) and Silverman et al. (2011) in both temporal and wavelength coverage. This allows us to study the properties and evolution of one member of this class in unprecedented detail, and to put constraints on possible explosion scenarios. The paper is organized as follows. In Section 2 the observations are presented, and the techniques applied for data reduction and calibration are discussed. Sections 3 and 4 are devoted to the analysis of the photometric and spectroscopic evolution of SN 2009dc, respectively. Important physical properties of SN 2009dc and possible explosion mechanisms are discussed in Section 5, before a brief summary of our main results is given in Section 6.

# 2 OBSERVATIONS AND DATA REDUCTION

SN 2009dc was discovered in the course of the Puckett Observatory Supernova Search on UT 2009 April 9.31 at an unfiltered magnitude of 16.5, and confirmed on unfiltered exposures on April 10.42 at a magnitude of 16.3 (Puckett, Moore & Newton 2009). No object was visible at the SN position on images taken by T. Puckett on 2009 March 21 to a limiting magnitude of 19.3. A classification spectrum taken with the Telescopio Nazionale Galileo + DOLORES on UT 2009 April 16.22 revealed that SN 2009dc was a Type Ia supernova well before maximum light (Harutyunyan, Elias-Rosa & Benetti 2009). The SN was reported to share similarity with SN 2006gz (Hicken et al. 2007) at pre-maximum phases in most spectral features, including prominent C II absorption lines, but lower expansion velocities. The presence of carbon and the resemblance to suspected super- $M_{\rm Ch}$  SNe Ia such as SN 2003fg (Howell et al. 2006) was confirmed by Marion, Garnavich & Challis (2009) based on optical and IR spectra obtained on UT 2009 April 18 and 19. Yamanaka et al. (2009) measured a peak absolute magnitude of  $M_{V,\text{max}} \sim -20$  and a slow light-curve decline of  $\Delta m_{15}(B) = 0.65$ , and estimated an ejected  $^{56}$ Ni mass of at least 1.2 M $_{\odot}$ . They concluded that the spectrophotometric properties of SN 2009dc are consistent with the explosion of a super- $M_{Ch}$  WD. In spectropolarimetric observations presented by Tanaka et al. (2010), SN 2009dc shows moderately strong polarization in Si II and Ca II lines, but small continuum polarization indicative of spherical symmetry on global scales. The authors consider this as support for the explosion scenario suggested by Yamanaka et al. (2009).

#### 2.1 Distance and extinction

SN 2009dc is located in the outskirts of the S0 galaxy UGC 10064 (but see Section 5.4 for an in-depth discussion on the host-galaxy interaction with the late-type UGC 10063, and the expected stellar population), at a redshift of z=0.0214 (NED)<sup>1</sup>. This is well within the Hubble flow, and a kinematic distance modulus of  $\mu=34.86\pm0.08$  mag is assumed, based on the average recession velocity of UGC 10064 and UGC 10063 corrected for local flow patterns (see Table 1 for details).

The extinction towards SN 2009dc is subject to some uncertainty. Narrow Na I D absorption lines can be discerned in the spectra both at zero redshift and the host-galaxy rest frame, suggesting a non-negligible amount of dust in the line of sight. The respective equivalent widths (EWs) are  $0.61 \pm 0.13$  and  $0.94 \pm 0.15$  Å, measured from 13 early-time spectra. Application of the formula of Turatto, Benetti & Cappellaro (2003) yields colour excesses of  $E(B-V) = 0.10 \pm 0.02$  and  $0.15 \pm 0.02$  mag in the Milky Way and the host galaxy, respectively. Alternatively, consulting the Schlegel, Finkbeiner & Davis (1998) dust maps suggests a foreground extinction of 0.07 mag towards UGC 10064, and we adopt this value for the Galactic component. In 'normal' SNe Ia, the colours measured at peak or during the tail phase are used to infer the total reddening caused by dust (e.g. Phillips et al. 1999). However, as will be shown in Section 3.1, the colour evolution of SN 2009dc differs significantly from that of ordinary SNe Ia, so that these methods cannot be applied with any confidence. Given the high luminosity of SN 2009dc and its blue early-time colours already before correcting for any host reddening, we rather consider the value derived from the interstellar Na ID lines as an upper limit for the actual host-galaxy colour excess. In the further analysis, we therefore adopt a hostgalaxy colour excess of  $E(B - V) = 0.10 \pm 0.07$  mag as our best estimate, 50 per cent larger than the Galactic colour excess as motivated by the ratio of the Na ID lines. Despite our multi-wavelength coverage, the unknown intrinsic colours of the SN also prevent us from determining the dust properties directly. We therefore adopt a Cardelli, Clayton & Mathis (1989) reddening law with  $R_V = 3.1$ , assuming dust properties not too different from those in the Galaxy.<sup>2</sup>

Details on the SN, the presumed host galaxy UGC 10064 and its interacting companion UGC 10063 are summarized in Table 1.

#### 2.2 Reduction of photometric data

The reduction of optical photometric data (bias subtraction, overscan correction and flat-fielding) was performed using standard

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Table 1. Properties of SN 2009dc and its possible host galaxies.

	I 8	
SN 2009dc		
α (J2000)	15h51m12s10	1
δ (J2000)	$+25^{\circ}42'28''.5$	1
Offset from UGC 10064 nucleus	15".8 W, 20".8 N	1
Host reddening $E(B - V)$	$0.10 \pm 0.07  \mathrm{mag}$	2
$\Delta m_{15}(B)_{\text{true}}$	$0.71 \pm 0.03$	2
${ m JD}_{{ m max},U}$	$2454945.2 \pm 0.5$	2
$\mathrm{JD}_{\mathrm{max},B}$	$2454947.1 \pm 0.3$	2
${ m JD}_{{ m max},V}$	$2454947.7 \pm 0.4$	2
$\mathrm{JD}_{\mathrm{max},R}$	$2454948.2\pm0.5$	2
$\mathrm{JD}_{\mathrm{max},I}$	$2454949.1\pm0.8$	2
$U_{ m max}$	$14.604 \pm 0.038$	2
$B_{ m max}$	$15.329 \pm 0.017$	2
$V_{ m max}$	$15.319 \pm 0.017$	2
$R_{\text{max}}$	$15.304 \pm 0.018$	2
$I_{\max}$	$15.385 \pm 0.018$	2
$M_{U,\mathrm{max}}$	$-21.06 \pm 0.34$	2
$M_{B,\mathrm{max}}$	$-20.22 \pm 0.30$	2
$M_{V,\max}$	$-20.07 \pm 0.23$	2
$M_{R,\mathrm{max}}$	$-19.99 \pm 0.20$	2
$M_{I,\max}$	$-19.79 \pm 0.16$	2
UGC 10064		
$\alpha$ (J2000)	15h51m13s28	3
δ (J2000)	$+25^{\circ}42'07''.5$	3
Redshift	$0.02139 \pm 0.00007$	4
$v_{ m CMB}^a$	$6508 \pm 22 \ \mathrm{km}  \mathrm{s}^{-1}$	4
$v_{ m Virgo}^b$	$6686 \pm 25 \ \mathrm{km  s^{-1}}$	4
$v_{\text{Virgo} + \text{GA} + \text{Shapley}}^{b}$	$7012 \pm 32 \ \mathrm{km \ s^{-1}}$	4
Distance modulus $\mu^c$	$34.85 \pm 0.08 \mathrm{mag}$	4
Extinction-corr. app. B mag	$14.55 \pm 0.28$	3
Absolute <i>B</i> magnitude	$-20.30 \pm 0.29$	3,4
Morphological type <sup>d</sup>	S0, -1.9	3
Galactic reddening $E(B-V)$	0.071 mag	5
UGC 10063		
α (J2000)	15 <sup>h</sup> 51 <sup>m</sup> 08 <sup>s</sup> .51	3
δ (J2000)	+25°43′21″.5	3
Redshift	$0.02158 \pm 0.00003$	4
na a	$6565 \pm 11 \text{ km s}^{-1}$	4
$v_{\mathrm{CMB}}^a$	$6743 \pm 16 \mathrm{km  s^{-1}}$	4
$v_{\mathrm{Virgo}}^{b}$	$7068 \pm 25 \mathrm{km  s^{-1}}$	4
vVirgo + GA + Shapley		
Distance modulus $\mu^c$	$34.87 \pm 0.08 \mathrm{mag}$	4
Extinction-corr. app. vis. mag	16.3	4
Absolute vis. magnitude	-18.6	4
Morphological type <sup>d</sup>	SBd, 8.0	3 5
Galactic reddening $E(B-V)$	0.071 mag	3

<sup>&</sup>lt;sup>a</sup>Recession velocity corrected to the CMB rest frame (Fixsen et al. 1996); <sup>b</sup>recession velocity corrected for Local Group infall on to the Virgo cluster (+ the Great Attractor + the Shapley Supercluster; Mould et al. 2000); <sup>c</sup>from the average of  $v_{\rm CMB}$ ,  $v_{\rm Virgo}$  and  $v_{\rm Virgo+GA+Shapley}$ , using  $H_0 = 72\,{\rm km\,s^{-1}Mpc^{-1}}$ ; <sup>d</sup>numerical code according to de Vaucouleurs.

routines in IRAF.<sup>3</sup> In the NIR, an in-field dithering strategy allowed for the creation of source-free sky images, which were subtracted from the individual scientific images to eliminate the strong NIR sky emission. Sub-exposures taken with the same filter during one night

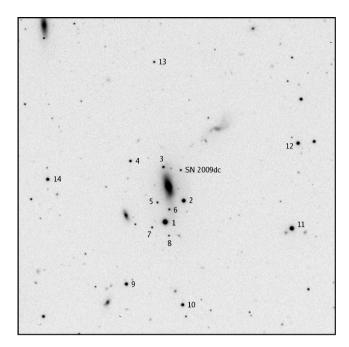
<sup>&</sup>lt;sup>1</sup> NASA/IPAC Extragalactic Database (http://nedwww.ipac.caltech.edu/)

<sup>&</sup>lt;sup>2</sup> Adopting a lower value for the host-galaxy reddening of e.g.  $R_V = 2.36$  as suggested by Wang et al. (2009a) for normal SNe Ia would reduce the inferred extinction in V (and hence the peak luminosity calculated in Section 3.2) by  $\sim$ 7 per cent.

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<sup>1:</sup> Marion et al. 2009; 2: this work; 3: LEDA; 4: NED; 5: Schlegel et al. 1998.

<sup>&</sup>lt;sup>3</sup> IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc, under contract to the National Science Foundation.

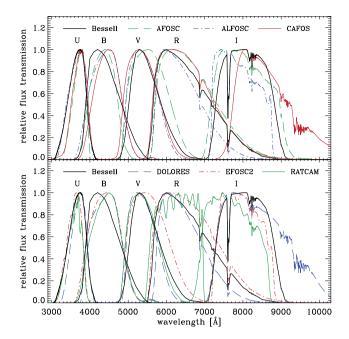


**Figure 1.** *R*-band image of the SN 2009dc field taken with the Calar Alto 2.2-m Telescope + CAFOS on ut 2009 August 13. The field of view is  $7.0 \times 7.0 \, \text{arcmin}^2$ , north is up and east to the left. The local sequence stars are indicated.

were aligned and combined before the photometric measurements were performed.

A sequence of field stars (Fig. 1) was calibrated with respect to Landolt (1992; for *UBVRI*) and Arnica (Hunt et al. 1998; for *JHK'*) standard fields on several photometric nights. The calibrated magnitudes of these field stars, listed in Table 2, were used to determine the SN magnitudes under non-photometric conditions. For the six local standards we have in common, our magnitudes are consistent with those reported by Silverman et al. (2011), with average systematic differences ranging from 0.008 (*B* band) to 0.015 mag (*V* band).

All SN measurements were done with point spread function fitting photometry using the software package snoopy, a dedicated tool for SN photometry written by F. Patat and implemented in IRAF by E. Cappellaro. Measurement errors were estimated through an artificial star experiment. Since instruments with very different



**Figure 2.** *UBVRI* passbands of the instruments used during the follow-up of SN 2009dc. The standard Bessell (1990) passbands are displayed for comparison. Note that the CCD and *UBVRI* filter set of DOLORES were replaced in 2007. The curves shown here refer to the new passbands, which deviate significantly from the old ones presented e.g. in Taubenberger et al. (2008).

passbands were used for the follow-up of SN 2009dc (see Fig. 2), we made use of the 'S-correction' technique (Stritzinger et al. 2002; Pignata et al. 2004) to calibrate the SN magnitudes to the standard photometric system of Johnson and Cousins (Bessell 1990) in the optical bands. Our excellent spectroscopic coverage enabled the computation of the S-correction solely on the basis of SN 2009dc spectra. In the same manner, a K-correction was derived to compensate for the non-negligible redshift of SN 2009dc. At epochs where no spectra were available, the S- and K-correction terms were determined by linear interpolation or constant extrapolation. No S- and K-correction was applied in the NIR bands, where the SN magnitudes were calibrated with first-order colour-term or simple zero-point corrections.

In Table 3, the fully calibrated *S*- and *K*-corrected Bessell *UBVRI* magnitudes of SN 2009dc are reported. The uncertainties in brackets

Table 2. Magnitudes of the local sequence stars in the field of SN 2009dc (Fig. 1).

ID	U	В	V	R	Ι	J	Н	<i>K'</i>
1	$15.894 \pm 0.029$	$15.368 \pm 0.016$	$14.460 \pm 0.014$	$13.922 \pm 0.018$	$13.445 \pm 0.013$	$12.785 \pm 0.022$	$12.308 \pm 0.058$	$12.188 \pm 0.012$
2	$16.939 \pm 0.018$	$16.647 \pm 0.016$	$15.850 \pm 0.016$	$15.392 \pm 0.016$	$14.969 \pm 0.019$	$14.376 \pm 0.015$	$13.967 \pm 0.041$	$13.894 \pm 0.010$
3	$19.512 \pm 0.055$	$18.890 \pm 0.018$	$17.968 \pm 0.022$	$17.411 \pm 0.028$	$16.936 \pm 0.017$	$16.252 \pm 0.052$	$15.786 \pm 0.028$	$15.724 \pm 0.039$
4	$18.870 \pm 0.036$	$18.649 \pm 0.017$	$17.772 \pm 0.019$	$17.229 \pm 0.017$	$16.721 \pm 0.018$	$16.057 \pm 0.061$	$15.539 \pm 0.019$	$15.426 \pm 0.021$
5		$20.464 \pm 0.034$	$19.156 \pm 0.033$	$18.274 \pm 0.019$	$17.464 \pm 0.017$	$16.491 \pm 0.066$	$15.849 \pm 0.010$	$15.678 \pm 0.072$
6	$19.103 \pm 0.109$	$19.191 \pm 0.022$	$18.535 \pm 0.020$	$18.141 \pm 0.022$	$17.737 \pm 0.030$			
7	$19.199 \pm 0.089$	$19.366 \pm 0.040$	$18.742 \pm 0.028$	$18.328 \pm 0.031$	$17.913 \pm 0.034$			
8		$21.674 \pm 0.077$	$20.015 \pm 0.073$	$18.995 \pm 0.050$	$17.214 \pm 0.032$	$15.788 \pm 0.010$	$15.230 \pm 0.053$	$14.932 \pm 0.012$
9	$17.102 \pm 0.013$	$17.152 \pm 0.030$	$16.544 \pm 0.022$	$16.161 \pm 0.007$	$15.792 \pm 0.017$			
10	$17.520 \pm 0.038$	$17.479 \pm 0.021$	$16.803 \pm 0.015$	$16.395 \pm 0.012$	$16.011 \pm 0.011$			
11	$16.009 \pm 0.028$	$15.903 \pm 0.015$	$15.195 \pm 0.009$	$14.793 \pm 0.018$	$14.412 \pm 0.016$			
12	$19.307 \pm 0.051$	$18.123 \pm 0.025$	$16.788 \pm 0.011$	$15.936 \pm 0.020$	$15.217 \pm 0.014$			
13		$20.073 \pm 0.019$	$18.901 \pm 0.021$	$18.125 \pm 0.025$	$17.478 \pm 0.020$			
14	$18.492 \pm 0.104$	$17.798 \pm 0.033$	$16.839 \pm 0.006$	$16.267 \pm 0.006$	$15.794 \pm 0.007$			

**Table 3.** S- and K-corrected UBVRI magnitudes of SN 2009dc.

937.49 938.66 939.50 939.69 942.44 942.53 943.49 944.57 946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 955.50 956.42 956.42 956.42 956.43 968.56 969.71 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37 970.37	-11.7 -9.7 -8.5 -7.6 -7.5 -4.7 -4.6 -3.7 -2.6 -0.7 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$14.905 \pm 0.076$ $14.800 \pm 0.040$ $14.779 \pm 0.009$ $14.648 \pm 0.025$ $14.767 \pm 0.010$ $14.668 \pm 0.031$ $14.706 \pm 0.032$ $14.869 \pm 0.026$ $14.943 \pm 0.046$ $14.971 \pm 0.087$ $15.257 \pm 0.018$ $15.128 \pm 0.045$ $15.425 \pm 0.037$ $15.258 \pm 0.072$ $15.429 \pm 0.038$ $15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$15.735 \pm 0.022$ $15.639 \pm 0.015$ $15.421 \pm 0.014$ $15.423 \pm 0.027$ $15.347 \pm 0.016$ $15.342 \pm 0.028$ $15.369 \pm 0.022$ $15.348 \pm 0.013$ $15.371 \pm 0.012$ $15.399 \pm 0.026$ $15.525 \pm 0.020$ $15.542 \pm 0.022$ $15.560 \pm 0.041$ $15.628 \pm 0.029$ $15.671 \pm 0.022$ $15.756 \pm 0.026$ $15.809 \pm 0.014$ $15.857 \pm 0.016$ $16.115 \pm 0.018$ $16.202 \pm 0.019$	$15.657 \pm 0.017$ $15.552 \pm 0.023$ $15.385 \pm 0.010$ $15.378 \pm 0.023$ $15.325 \pm 0.012$ $15.328 \pm 0.028$ $15.349 \pm 0.019$ $15.326 \pm 0.011$ $15.360 \pm 0.012$ $15.432 \pm 0.012$ $15.432 \pm 0.012$ $15.414 \pm 0.009$ $15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$ $15.527 \pm 0.036$	$\begin{array}{c} 15.928 \pm 0.058 \\ 15.608 \pm 0.059 \\ 15.671 \pm 0.027 \\ 15.443 \pm 0.026 \\ 15.603 \pm 0.017 \\ 15.313 \pm 0.025 \\ 15.399 \pm 0.016 \\ 15.390 \pm 0.027 \\ 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.338 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.438 \pm 0.007 \\ \end{array}$	$15.781 \pm 0.022$ $15.702 \pm 0.027$ $15.502 \pm 0.010$ $15.520 \pm 0.024$ $15.439 \pm 0.016$ $15.339 \pm 0.026$ $15.398 \pm 0.024$ $15.390 \pm 0.016$ $15.387 \pm 0.008$ $15.348 \pm 0.044$ $15.424 \pm 0.024$ $15.406 \pm 0.017$ $15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$ $15.408 \pm 0.020$	JN EPI NOT JN NOT JIN LT NOT LT JN CA TNG LT LT LT CA TNG LT LT CA TNG JN LT CA LT CA LT NOT NOT	3.16 4.90 0.89 2.96 0.70 3.16 1.84 2.03 1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11
938.66 939.50 939.69 942.44 942.53 943.49 944.57 946.49 949.53 949.54 949.53 955.63 951.58 953.68 954.41 955.50 956.42 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 970.37 970.37 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43 995.43	-8.5 -7.6 -7.5 -4.7 -4.6 -3.7 -2.6 -0.7 2.4 2.5 3.5 3.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.800 &\pm 0.040 \\ 14.779 &\pm 0.009 \\ 14.648 &\pm 0.025 \\ 14.767 &\pm 0.010 \\ \end{aligned}$ $\begin{aligned} 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \\ \end{aligned}$ $\begin{aligned} 14.971 &\pm 0.087 \\ \end{aligned}$ $\begin{aligned} 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned}$ $\begin{aligned} 16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \\ \end{aligned}$	$\begin{aligned} 15.639 &\pm 0.015 \\ 15.421 &\pm 0.014 \\ 15.423 &\pm 0.027 \\ 15.347 &\pm 0.016 \end{aligned}$ $15.342 &\pm 0.028 \\ 15.369 &\pm 0.022 \\ 15.348 &\pm 0.013 \\ 15.371 &\pm 0.012 \\ 15.399 &\pm 0.026 \\ 15.525 &\pm 0.020 \end{aligned}$ $15.542 &\pm 0.022 \\ 15.560 &\pm 0.041 \\ 15.628 &\pm 0.029 \\ 15.671 &\pm 0.022 \\ 15.756 &\pm 0.026 \\ 15.809 &\pm 0.014 \\ 15.857 &\pm 0.016 \\ 16.115 &\pm 0.018 \end{aligned}$	$15.552 \pm 0.023$ $15.385 \pm 0.010$ $15.378 \pm 0.023$ $15.325 \pm 0.012$ $15.328 \pm 0.028$ $15.349 \pm 0.019$ $15.326 \pm 0.012$ $15.350 \pm 0.011$ $15.360 \pm 0.022$ $15.432 \pm 0.012$ $15.414 \pm 0.009$ $15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$\begin{array}{c} 15.671 \pm 0.027 \\ 15.443 \pm 0.036 \\ 15.603 \pm 0.017 \\ 15.313 \pm 0.025 \\ 15.399 \pm 0.016 \\ 15.390 \pm 0.027 \\ 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$15.702 \pm 0.027$ $15.502 \pm 0.010$ $15.520 \pm 0.024$ $15.439 \pm 0.016$ $15.339 \pm 0.026$ $15.398 \pm 0.024$ $15.390 \pm 0.016$ $15.387 \pm 0.008$ $15.348 \pm 0.044$ $15.424 \pm 0.024$ $15.406 \pm 0.017$ $15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	NOT JN NOT JN LT NOT LT JN CA TNG LT LT LT CA TNG JN LT CA TNG JN LT CA LT NOT NOT	0.89 2.96 0.70 3.16 1.84 2.03 1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
939.50 939.69 942.44 942.53 943.49 944.57 946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	-7.6 -7.5 -4.7 -4.6 -3.7 -2.6 -0.7 2.4 2.5 3.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.800 &\pm 0.040 \\ 14.779 &\pm 0.009 \\ 14.648 &\pm 0.025 \\ 14.767 &\pm 0.010 \\ \end{aligned}$ $\begin{aligned} 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \\ \end{aligned}$ $\begin{aligned} 14.971 &\pm 0.087 \\ \end{aligned}$ $\begin{aligned} 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned}$ $\begin{aligned} 16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \\ \end{aligned}$	$\begin{aligned} 15.639 &\pm 0.015 \\ 15.421 &\pm 0.014 \\ 15.423 &\pm 0.027 \\ 15.347 &\pm 0.016 \end{aligned}$ $15.342 &\pm 0.028 \\ 15.369 &\pm 0.022 \\ 15.348 &\pm 0.013 \\ 15.371 &\pm 0.012 \\ 15.399 &\pm 0.026 \\ 15.525 &\pm 0.020 \end{aligned}$ $15.542 &\pm 0.022 \\ 15.560 &\pm 0.041 \\ 15.628 &\pm 0.029 \\ 15.671 &\pm 0.022 \\ 15.756 &\pm 0.026 \\ 15.809 &\pm 0.014 \\ 15.857 &\pm 0.016 \\ 16.115 &\pm 0.018 \end{aligned}$	$15.552 \pm 0.023$ $15.385 \pm 0.010$ $15.378 \pm 0.023$ $15.325 \pm 0.012$ $15.328 \pm 0.028$ $15.349 \pm 0.019$ $15.326 \pm 0.012$ $15.350 \pm 0.011$ $15.360 \pm 0.022$ $15.432 \pm 0.012$ $15.414 \pm 0.009$ $15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$\begin{array}{c} 15.443 \pm 0.036 \\ 15.603 \pm 0.017 \\ 15.313 \pm 0.025 \\ 15.399 \pm 0.016 \\ 15.390 \pm 0.027 \\ 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$15.702 \pm 0.027$ $15.502 \pm 0.010$ $15.520 \pm 0.024$ $15.439 \pm 0.016$ $15.339 \pm 0.026$ $15.398 \pm 0.024$ $15.390 \pm 0.016$ $15.387 \pm 0.008$ $15.348 \pm 0.044$ $15.424 \pm 0.024$ $15.406 \pm 0.017$ $15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	JN NOT JN LT NOT LT JN CA TNG LT LT LT CA TNG JN LT CA TNG JN LT CA LT NOT NOT	2.96 0.70 3.16 1.84 2.03 1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
939.69 942.44 942.53 943.49 944.57 946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.42 956.42 956.43 968.56 969.71 966.43 968.56 969.71 970.37 970.37 970.37 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	-7.5 -4.7 -4.6 -3.7 -2.6 -0.7 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.779 &\pm 0.009 \\ 14.648 &\pm 0.025 \\ 14.767 &\pm 0.010 \end{aligned}$ $\begin{aligned} 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \end{aligned}$ $\begin{aligned} 14.971 &\pm 0.087 \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \end{aligned}$ $\begin{aligned} 16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \end{aligned}$	$\begin{array}{c} 15.421 \pm 0.014 \\ 15.423 \pm 0.027 \\ 15.347 \pm 0.016 \\ \\ 15.342 \pm 0.028 \\ 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.385 \pm 0.010 \\ 15.378 \pm 0.023 \\ 15.325 \pm 0.012 \\ \\ 15.328 \pm 0.028 \\ 15.349 \pm 0.019 \\ 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.603 \pm 0.017 \\ 15.313 \pm 0.025 \\ 15.399 \pm 0.016 \\ 15.390 \pm 0.027 \\ 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{aligned} 15.502 &\pm 0.010 \\ 15.520 &\pm 0.024 \\ 15.439 &\pm 0.016 \end{aligned}$ $15.339 &\pm 0.026 \\ 15.398 &\pm 0.024 \\ 15.390 &\pm 0.016 \\ 15.387 &\pm 0.008 \\ 15.348 &\pm 0.044 \\ 15.424 &\pm 0.024 \end{aligned}$ $15.406 &\pm 0.017 \\ 15.411 &\pm 0.030 \\ 15.400 &\pm 0.007 \\ 15.442 &\pm 0.021 \end{aligned}$	NOT JN LT NOT LT JN CA TNG LT LT LT CA TNG JN LT CA LT NOT NOT	0.70 3.16 1.84 2.03 1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
942.44 942.53 943.49 944.57 946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 970.37 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	-4.7 -4.6 -3.7 -2.6 -0.7 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.779 &\pm 0.009 \\ 14.648 &\pm 0.025 \\ 14.767 &\pm 0.010 \end{aligned}$ $\begin{aligned} 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \end{aligned}$ $\begin{aligned} 14.971 &\pm 0.087 \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \end{aligned}$ $\begin{aligned} 16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \end{aligned}$	$\begin{array}{c} 15.421 \pm 0.014 \\ 15.423 \pm 0.027 \\ 15.347 \pm 0.016 \\ \\ 15.342 \pm 0.028 \\ 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.385 \pm 0.010 \\ 15.378 \pm 0.023 \\ 15.325 \pm 0.012 \\ \\ 15.328 \pm 0.028 \\ 15.349 \pm 0.019 \\ 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.313 \pm 0.025 \\ 15.399 \pm 0.016 \\ 15.390 \pm 0.027 \\ 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{aligned} 15.502 &\pm 0.010 \\ 15.520 &\pm 0.024 \\ 15.439 &\pm 0.016 \end{aligned}$ $15.339 &\pm 0.026 \\ 15.398 &\pm 0.024 \\ 15.390 &\pm 0.016 \\ 15.387 &\pm 0.008 \\ 15.348 &\pm 0.044 \\ 15.424 &\pm 0.024 \end{aligned}$ $15.406 &\pm 0.017 \\ 15.411 &\pm 0.030 \\ 15.400 &\pm 0.007 \\ 15.442 &\pm 0.021 \end{aligned}$	JN LT NOT LT JN CA TNG LT LT LT CA TNG JN LT CA LT CA TNG JN LT CA LT NOT	3.16 1.84 2.03 1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
942.53 943.49 944.57 946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 970.37 977.38 977.43 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	-4.6 -3.7 -2.6 -0.7 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.648 &\pm 0.025 \\ 14.767 &\pm 0.010 \\ \end{aligned} \\ 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \\ \end{aligned} \\ 14.971 &\pm 0.087 \\ \end{aligned} \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned} \\ 16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \\ \end{aligned}$	$\begin{array}{c} 15.423 \pm 0.027 \\ 15.347 \pm 0.016 \\ \\ 15.342 \pm 0.028 \\ 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.378 \pm 0.023 \\ 15.325 \pm 0.012 \\ \\ 15.325 \pm 0.012 \\ \\ 15.328 \pm 0.028 \\ 15.349 \pm 0.019 \\ 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.399 \pm 0.016 \\ 15.390 \pm 0.027 \\ 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{aligned} 15.520 &\pm 0.024 \\ 15.439 &\pm 0.016 \end{aligned}$ $15.339 &\pm 0.026 \\ 15.398 &\pm 0.024 \\ 15.390 &\pm 0.016 \\ 15.387 &\pm 0.008 \\ 15.348 &\pm 0.044 \\ 15.424 &\pm 0.024 \end{aligned}$ $15.406 &\pm 0.017 \\ 15.411 &\pm 0.030 \\ 15.400 &\pm 0.007 \\ 15.442 &\pm 0.021 \end{aligned}$	LT NOT LT JN CA TNG LT LT LT CA TNG JN LT CA LT CA LT NOT NOT	1.84 2.03 1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
943.49 944.57 946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 966.43 970.37 970.37 970.37 977.38 977.43 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	-3.7 -2.6 -0.7 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.648 &\pm 0.025 \\ 14.767 &\pm 0.010 \\ \end{aligned} \\ 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \\ \end{aligned} \\ 14.971 &\pm 0.087 \\ \end{aligned} \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned} \\ 16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \\ \end{aligned}$	$\begin{array}{c} 15.423 \pm 0.027 \\ 15.347 \pm 0.016 \\ \\ 15.342 \pm 0.028 \\ 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.378 \pm 0.023 \\ 15.325 \pm 0.012 \\ \\ 15.325 \pm 0.012 \\ \\ 15.328 \pm 0.028 \\ 15.349 \pm 0.019 \\ 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.390 \pm 0.027 \\ 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{aligned} 15.520 &\pm 0.024 \\ 15.439 &\pm 0.016 \end{aligned}$ $15.339 &\pm 0.026 \\ 15.398 &\pm 0.024 \\ 15.390 &\pm 0.016 \\ 15.387 &\pm 0.008 \\ 15.348 &\pm 0.044 \\ 15.424 &\pm 0.024 \end{aligned}$ $15.406 &\pm 0.017 \\ 15.411 &\pm 0.030 \\ 15.400 &\pm 0.007 \\ 15.442 &\pm 0.021 \end{aligned}$	NOT LT JN CA TNG LT LT CA TNG JN LT CA LT CA LT NOT NOT	2.03 1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
944.57 946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 970.37 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	-2.6 -0.7 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.767 &\pm 0.010 \\ 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \\ \end{aligned}$ $14.971 &\pm 0.087 \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned}$ $16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \\ \end{aligned}$	$\begin{array}{c} 15.347 \pm 0.016 \\ \\ 15.342 \pm 0.028 \\ 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{aligned} 15.325 &\pm 0.012 \\ 15.328 &\pm 0.028 \\ 15.349 &\pm 0.019 \\ 15.326 &\pm 0.012 \\ 15.350 &\pm 0.011 \\ 15.360 &\pm 0.022 \\ 15.432 &\pm 0.012 \\ \end{aligned}$ $15.414 &\pm 0.009 \\ 15.428 &\pm 0.013 \\ 15.453 &\pm 0.019 \\ 15.455 &\pm 0.014 \\ 15.498 &\pm 0.028 \\ 15.533 &\pm 0.022 \end{aligned}$	$\begin{array}{c} 15.339 \pm 0.011 \\ 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{aligned} 15.439 &\pm 0.016 \\ 15.339 &\pm 0.026 \\ 15.398 &\pm 0.024 \\ 15.390 &\pm 0.016 \\ 15.387 &\pm 0.008 \\ 15.348 &\pm 0.044 \\ 15.424 &\pm 0.024 \\ \end{aligned}$ $15.406 &\pm 0.017 \\ 15.411 &\pm 0.030 \\ 15.400 &\pm 0.007 \\ 15.422 &\pm 0.031 \\ 15.479 &\pm 0.021 \\ \end{aligned}$	LT JN CA TNG LT LT CA TNG JN LT CA LT CA LT NOT	1.42 3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
946.49 949.53 949.54 949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 970.37 977.38 977.43 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	-0.7 2.4 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.668 &\pm 0.031 \\ 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \end{aligned}$ $14.971 &\pm 0.087$ $15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \end{aligned}$ $16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \end{aligned}$	$\begin{array}{c} 15.342 \pm 0.028 \\ 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.328 \pm 0.028 \\ 15.349 \pm 0.019 \\ 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.247 \pm 0.036 \\ 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{array}{c} 15.339 \pm 0.026 \\ 15.398 \pm 0.024 \\ 15.390 \pm 0.016 \\ 15.387 \pm 0.008 \\ 15.348 \pm 0.044 \\ 15.424 \pm 0.024 \\ \\ 15.406 \pm 0.017 \\ 15.411 \pm 0.030 \\ 15.400 \pm 0.007 \\ 15.442 \pm 0.031 \\ 15.479 \pm 0.021 \\ \end{array}$	JN CA TNG LT LT CA TNG JN LT CA LT NOT	3.16 2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
949.53 949.54 949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	2.4 2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \end{aligned}$ $14.971 &\pm 0.087$ $15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \end{aligned}$ $16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \end{aligned}$	$\begin{array}{c} 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.349 \pm 0.019 \\ 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.295 \pm 0.025 \\ 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{array}{c} 15.398 \pm 0.024 \\ 15.390 \pm 0.016 \\ 15.387 \pm 0.008 \\ 15.348 \pm 0.044 \\ 15.424 \pm 0.024 \\ \\ 15.406 \pm 0.017 \\ 15.411 \pm 0.030 \\ 15.400 \pm 0.007 \\ 15.442 \pm 0.031 \\ 15.479 \pm 0.021 \\ \end{array}$	CA TNG LT LT CA TNG JN LT CA LT NOT	2.54 1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
949.54 949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	2.4 2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.706 &\pm 0.032 \\ 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \end{aligned}$ $14.971 &\pm 0.087$ $15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \end{aligned}$ $16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \end{aligned}$	$\begin{array}{c} 15.369 \pm 0.022 \\ 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.349 \pm 0.019 \\ 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.339 \pm 0.015 \\ 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{array}{c} 15.398 \pm 0.024 \\ 15.390 \pm 0.016 \\ 15.387 \pm 0.008 \\ 15.348 \pm 0.044 \\ 15.424 \pm 0.024 \\ \\ 15.406 \pm 0.017 \\ 15.411 \pm 0.030 \\ 15.400 \pm 0.007 \\ 15.442 \pm 0.031 \\ 15.479 \pm 0.021 \\ \end{array}$	TNG LT LT CA TNG JN LT CA LT NOT	1.02 1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
949.62 950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	2.5 3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.869 &\pm 0.026 \\ 14.943 &\pm 0.046 \\ \end{aligned} \\ 14.971 &\pm 0.087 \\ \end{aligned} \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned}$ $16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \\ \end{aligned}$	$\begin{array}{c} 15.348 \pm 0.013 \\ 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{array}{c} 15.326 \pm 0.012 \\ 15.350 \pm 0.011 \\ 15.360 \pm 0.022 \\ 15.432 \pm 0.012 \\ \\ 15.414 \pm 0.009 \\ 15.428 \pm 0.013 \\ 15.453 \pm 0.019 \\ 15.455 \pm 0.014 \\ 15.498 \pm 0.028 \\ 15.533 \pm 0.022 \\ \end{array}$	$\begin{array}{c} 15.297 \pm 0.023 \\ 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{array}{c} 15.390 \pm 0.016 \\ 15.387 \pm 0.008 \\ 15.348 \pm 0.044 \\ 15.424 \pm 0.024 \\ \\ 15.406 \pm 0.017 \\ 15.411 \pm 0.030 \\ 15.400 \pm 0.007 \\ 15.442 \pm 0.031 \\ 15.479 \pm 0.021 \\ \end{array}$	LT LT CA TNG JN LT CA LT NOT	1.37 1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.943 &\pm 0.046 \\ 14.971 &\pm 0.087 \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned}$	$\begin{array}{c} 15.371 \pm 0.012 \\ 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{aligned} 15.350 &\pm 0.011 \\ 15.360 &\pm 0.022 \\ 15.432 &\pm 0.012 \end{aligned}$ $15.414 &\pm 0.009 \\ 15.428 &\pm 0.013 \\ 15.453 &\pm 0.019 \\ 15.455 &\pm 0.014 \\ 15.498 &\pm 0.028 \\ 15.533 &\pm 0.022 \end{aligned}$	$\begin{array}{c} 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{aligned} 15.387 &\pm 0.008 \\ 15.348 &\pm 0.044 \\ 15.424 &\pm 0.024 \end{aligned}$ $15.406 &\pm 0.017 \\ 15.411 &\pm 0.030 \\ 15.400 &\pm 0.007 \\ 15.442 &\pm 0.031 \\ 15.479 &\pm 0.021 \end{aligned}$	LT CA TNG JN LT CA LT NOT NOT	1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
950.63 951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	3.5 4.4 6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.943 &\pm 0.046 \\ 14.971 &\pm 0.087 \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned}$	$\begin{array}{c} 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$\begin{aligned} 15.350 &\pm 0.011 \\ 15.360 &\pm 0.022 \\ 15.432 &\pm 0.012 \end{aligned}$ $15.414 &\pm 0.009 \\ 15.428 &\pm 0.013 \\ 15.453 &\pm 0.019 \\ 15.455 &\pm 0.014 \\ 15.498 &\pm 0.028 \\ 15.533 &\pm 0.022 \end{aligned}$	$\begin{array}{c} 15.308 \pm 0.011 \\ 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$\begin{aligned} 15.387 &\pm 0.008 \\ 15.348 &\pm 0.044 \\ 15.424 &\pm 0.024 \end{aligned}$ $15.406 &\pm 0.017 \\ 15.411 &\pm 0.030 \\ 15.400 &\pm 0.007 \\ 15.442 &\pm 0.031 \\ 15.479 &\pm 0.021 \end{aligned}$	LT CA TNG JN LT CA LT NOT NOT	1.51 1.70 1.32 3.57 1.70 1.11 1.56 0.82
951.58 953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	4.4 6.5 7.3 7.4 8.4 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} 14.971 &\pm 0.087 \\ 15.257 &\pm 0.018 \\ 15.128 &\pm 0.045 \\ 15.425 &\pm 0.037 \\ 15.258 &\pm 0.072 \\ 15.429 &\pm 0.038 \\ 15.746 &\pm 0.036 \\ 15.547 &\pm 0.033 \\ \end{aligned}$ $16.128 &\pm 0.049 \\ 16.001 &\pm 0.049 \end{aligned}$	$\begin{array}{c} 15.399 \pm 0.026 \\ 15.525 \pm 0.020 \\ \\ 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \\ \end{array}$	$15.360 \pm 0.022$ $15.432 \pm 0.012$ $15.414 \pm 0.009$ $15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$\begin{array}{c} 15.328 \pm 0.028 \\ 15.397 \pm 0.014 \\ 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$15.348 \pm 0.044$ $15.424 \pm 0.024$ $15.406 \pm 0.017$ $15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	CA TNG JN LT CA LT NOT	1.70 1.32 3.57 1.70 1.11 1.56 0.82
953.68 954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	6.5 7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$15.257 \pm 0.018$ $15.128 \pm 0.045$ $15.425 \pm 0.037$ $15.258 \pm 0.072$ $15.429 \pm 0.038$ $15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$15.525 \pm 0.020$ $15.542 \pm 0.022$ $15.560 \pm 0.041$ $15.628 \pm 0.029$ $15.671 \pm 0.022$ $15.756 \pm 0.026$ $15.809 \pm 0.014$ $15.857 \pm 0.016$ $16.115 \pm 0.018$	$15.432 \pm 0.012$ $15.414 \pm 0.009$ $15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$\begin{aligned} 15.397 &\pm 0.014 \\ 15.305 &\pm 0.041 \\ 15.350 &\pm 0.011 \\ 15.377 &\pm 0.022 \\ 15.410 &\pm 0.012 \\ 15.424 &\pm 0.032 \\ 15.451 &\pm 0.027 \end{aligned}$	$15.424 \pm 0.024$ $15.406 \pm 0.017$ $15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	TNG JN LT CA LT NOT NOT	1.32 3.57 1.70 1.11 1.56 0.82
954.41 954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	7.3 7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$15.257 \pm 0.018$ $15.128 \pm 0.045$ $15.425 \pm 0.037$ $15.258 \pm 0.072$ $15.429 \pm 0.038$ $15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$\begin{array}{c} 15.542 \pm 0.022 \\ 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \end{array}$	$15.414 \pm 0.009$ $15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$\begin{array}{c} 15.305 \pm 0.041 \\ 15.350 \pm 0.011 \\ 15.377 \pm 0.022 \\ 15.410 \pm 0.012 \\ 15.424 \pm 0.032 \\ 15.451 \pm 0.027 \end{array}$	$15.406 \pm 0.017$ $15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	JN LT CA LT NOT NOT	3.57 1.70 1.11 1.56 0.82
954.49 955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	7.4 8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$15.128 \pm 0.045$ $15.425 \pm 0.037$ $15.258 \pm 0.072$ $15.429 \pm 0.038$ $15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$\begin{array}{c} 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \end{array}$	$15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$15.350 \pm 0.011$ $15.377 \pm 0.022$ $15.410 \pm 0.012$ $15.424 \pm 0.032$ $15.451 \pm 0.027$	$15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	LT CA LT NOT NOT	1.70 1.11 1.56 0.82
955.50 956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	8.4 9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$15.128 \pm 0.045$ $15.425 \pm 0.037$ $15.258 \pm 0.072$ $15.429 \pm 0.038$ $15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$\begin{array}{c} 15.560 \pm 0.041 \\ 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \end{array}$	$15.428 \pm 0.013$ $15.453 \pm 0.019$ $15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$\begin{aligned} &15.377 \pm 0.022 \\ &15.410 \pm 0.012 \\ &15.424 \pm 0.032 \\ &15.451 \pm 0.027 \end{aligned}$	$15.411 \pm 0.030$ $15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	CA LT NOT NOT	1.11 1.56 0.82
956.42 956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	9.3 9.3 11.5 12.5 12.6 16.4 17.3 17.6	$\begin{aligned} &15.425 \pm 0.037 \\ &15.258 \pm 0.072 \\ &15.429 \pm 0.038 \\ &15.746 \pm 0.036 \\ &15.547 \pm 0.033 \end{aligned}$ $&16.128 \pm 0.049 \\ &16.001 \pm 0.049 \end{aligned}$	$\begin{array}{c} 15.628 \pm 0.029 \\ 15.671 \pm 0.022 \\ 15.756 \pm 0.026 \\ 15.809 \pm 0.014 \\ 15.857 \pm 0.016 \\ 16.115 \pm 0.018 \end{array}$	$\begin{aligned} &15.453 \pm 0.019 \\ &15.455 \pm 0.014 \\ &15.498 \pm 0.028 \\ &15.533 \pm 0.022 \end{aligned}$	$15.410 \pm 0.012$ $15.424 \pm 0.032$ $15.451 \pm 0.027$	$15.400 \pm 0.007$ $15.442 \pm 0.031$ $15.479 \pm 0.021$	LT NOT NOT	1.56 0.82
956.48 958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	9.3 11.5 12.5 12.6 16.4 17.3 17.6	$15.258 \pm 0.072$ $15.429 \pm 0.038$ $15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$15.671 \pm 0.022$ $15.756 \pm 0.026$ $15.809 \pm 0.014$ $15.857 \pm 0.016$ $16.115 \pm 0.018$	$15.455 \pm 0.014$ $15.498 \pm 0.028$ $15.533 \pm 0.022$	$15.424 \pm 0.032$ $15.451 \pm 0.027$	$15.442 \pm 0.031$ $15.479 \pm 0.021$	NOT NOT	0.82
958.63 959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	11.5 12.5 12.6 16.4 17.3 17.6	$15.429 \pm 0.038$ $15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$15.756 \pm 0.026$ $15.809 \pm 0.014$ $15.857 \pm 0.016$ $16.115 \pm 0.018$	$15.498 \pm 0.028$ $15.533 \pm 0.022$	$15.451 \pm 0.027$	$15.479 \pm 0.021$	NOT	
959.65 959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	12.5 12.6 16.4 17.3 17.6	$15.746 \pm 0.036$ $15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$15.809 \pm 0.014$ $15.857 \pm 0.016$ $16.115 \pm 0.018$	$15.533 \pm 0.022$				
959.69 963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	12.6 16.4 17.3 17.6	$15.547 \pm 0.033$ $16.128 \pm 0.049$ $16.001 \pm 0.049$	$15.857 \pm 0.016 \\ 16.115 \pm 0.018$		$15.438 \pm 0.007$	$15.408 \pm 0.020$		0.55
963.52 964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	16.4 17.3 17.6	$16.128 \pm 0.049$ $16.001 \pm 0.049$	$16.115 \pm 0.018$	$15.527 \pm 0.036$			LT	1.95
964.41 964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	17.3 17.6	$16.001 \pm 0.049$			$15.519 \pm 0.024$	$15.473 \pm 0.028$	NOT	1.25
964.70 966.43 968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	17.6	$16.001 \pm 0.049$	$16.202 \pm 0.019$	$15.672 \pm 0.018$	$15.557 \pm 0.019$	$15.429 \pm 0.010$	LT	1.31
966.43 968.56 969.71 970.37 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53				$15.696 \pm 0.017$	$15.576 \pm 0.005$	$15.412 \pm 0.029$	LT	1.90
968.56 969.71 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53			$16.217 \pm 0.024$	$15.684 \pm 0.021$	$15.570 \pm 0.023$	$15.398 \pm 0.027$	TNG	1.35
969.71 970.37 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	19.3	$16.457 \pm 0.023$	$16.348 \pm 0.015$	$15.773 \pm 0.011$	$15.611 \pm 0.016$	$15.409 \pm 0.013$	LT	1.37
970.37 970.37 970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	21.4	$16.668 \pm 0.015$	$16.537 \pm 0.015$	$15.865 \pm 0.021$	$15.643 \pm 0.013$	$15.401 \pm 0.009$	LT	1.34
970.37 972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	22.6	$16.671 \pm 0.045$	$16.603 \pm 0.037$	$15.932 \pm 0.038$	$15.664 \pm 0.029$	$15.423 \pm 0.026$	NTT	1.30
972.39 973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	23.2				$15.672 \pm 0.042$		JN	2.96
973.47 976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	23.2				$15.691 \pm 0.052$		EP2	3.17
976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	25.3				$15.705 \pm 0.045$		JN	3.16
976.52 977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	26.3	$16.943 \pm 0.055$	$16.939 \pm 0.025$	$16.088 \pm 0.033$	$15.766 \pm 0.015$	$15.484 \pm 0.015$	NOT	1.46
977.38 977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	29.4	$17.237 \pm 0.035$	$17.145 \pm 0.025$	$16.179 \pm 0.020$	$15.828 \pm 0.035$	$15.494 \pm 0.025$	NOT	0.59
977.43 978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	30.2				$15.845 \pm 0.042$		JN	3.16
978.59 981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	30.3	$17.223 \pm 0.072$	$17.164 \pm 0.046$				Ekar	2.84
981.44 982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	31.5		$17.258 \pm 0.033$	$16.309 \pm 0.023$	$15.914 \pm 0.028$	$15.557 \pm 0.039$	Ekar	2.65
982.62 983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	34.3	$17.747 \pm 0.028$	$17.475 \pm 0.017$	$16.423 \pm 0.011$	$16.009 \pm 0.015$	$15.613 \pm 0.025$	LT	1.37
983.41 987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	35.5	$17.747 \pm 0.028$ $17.526 \pm 0.029$	$17.479 \pm 0.017$ $17.499 \pm 0.013$	$16.463 \pm 0.017$	$16.074 \pm 0.023$	$15.576 \pm 0.025$	CA	1.75
987.54 988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	36.3	$17.858 \pm 0.043$	$17.568 \pm 0.013$	$16.511 \pm 0.007$	$16.087 \pm 0.023$ $16.087 \pm 0.014$	$15.678 \pm 0.035$ $15.678 \pm 0.016$	LT	1.73
988.53 991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	40.4	$17.838 \pm 0.043$ $18.043 \pm 0.028$	$17.743 \pm 0.027$	$16.683 \pm 0.007$	$16.266 \pm 0.017$	$15.847 \pm 0.014$	LT LT	1.26
991.54 995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53		$17.883 \pm 0.028$	$17.743 \pm 0.027$ $17.783 \pm 0.026$	$16.706 \pm 0.009$	$16.327 \pm 0.040$	$15.847 \pm 0.014$ $15.897 \pm 0.029$		0.46
995.43 995.60 1006.46 1007.48 1009.56 1013.43 1016.53	41.4						NOT	
995.60 1006.46 1007.48 1009.56 1013.43 1016.53	44.4	$18.129 \pm 0.037$	$17.866 \pm 0.017$	$16.809 \pm 0.025$	$16.420 \pm 0.016$	$15.973 \pm 0.012$	LT	1.42
1006.46 1007.48 1009.56 1013.43 1016.53	48.3	$18.283 \pm 0.050$	$17.930 \pm 0.023$	$16.934 \pm 0.024$	$16.555 \pm 0.017$	$16.125 \pm 0.031$	LT	1.34
1007.48 1009.56 1013.43 1016.53	48.5	$18.014 \pm 0.043$	$17.985 \pm 0.020$	$16.945 \pm 0.024$	$16.596 \pm 0.017$	$16.187 \pm 0.033$	NOT	0.95
1009.56 1013.43 1016.53	59.3	$18.479 \pm 0.053$	$18.143 \pm 0.012$	$17.186 \pm 0.016$	$16.894 \pm 0.015$	$16.483 \pm 0.022$	LT	1.17
1013.43 1016.53	60.3	$18.258 \pm 0.041$	$18.163 \pm 0.022$	$17.229 \pm 0.021$	$16.950 \pm 0.018$	$16.596 \pm 0.024$	NOT	0.65
1016.53	62.4	$18.528 \pm 0.051$	$18.183 \pm 0.014$	$17.248 \pm 0.022$	$16.969 \pm 0.016$	$16.575 \pm 0.014$	LT	1.48
	66.3	$18.567 \pm 0.052$	$18.255 \pm 0.017$	$17.333 \pm 0.017$	$17.085 \pm 0.025$	$16.699 \pm 0.014$	LT	1.34
	69.4	$18.265 \pm 0.074$	$18.282 \pm 0.018$	$17.374 \pm 0.025$	$17.153 \pm 0.018$	$16.766 \pm 0.022$	TNG	1.24
1021.42	74.3	$18.730 \pm 0.044$	$18.344 \pm 0.033$	$17.498 \pm 0.019$	$17.310 \pm 0.028$	$16.959 \pm 0.019$	LT	1.40
1022.43	75.3	$18.534 \pm 0.056$	$18.400 \pm 0.018$	$17.527 \pm 0.017$	$17.358 \pm 0.026$	$17.109 \pm 0.038$	NOT	0.65
1025.43	75.3	$18.854 \pm 0.049$	$18.416 \pm 0.013$	$17.582 \pm 0.018$	$17.414 \pm 0.011$	$17.099 \pm 0.022$	LT	1.26
1028.57	75.3 78.3	$18.690 \pm 0.064$	$18.443 \pm 0.040$	$17.679 \pm 0.026$	$17.507 \pm 0.033$	$17.205 \pm 0.028$	NTT	1.92
1032.42		$18.959 \pm 0.065$	$18.511 \pm 0.013$	$17.735 \pm 0.012$	$17.592 \pm 0.017$	$17.301 \pm 0.018$	LT	1.51
1033.42	78.3 81.4	$18.950 \pm 0.037$	$18.532 \pm 0.012$	$17.747 \pm 0.015$	$17.627 \pm 0.015$	$17.332 \pm 0.013$	LT	1.87
1034.42	78.3 81.4 85.3	$19.003 \pm 0.064$	$18.546 \pm 0.018$	$17.776 \pm 0.014$	$17.641 \pm 0.028$	$17.366 \pm 0.016$	LT	1.40
1037.41	78.3 81.4 85.3 86.3	$18.848 \pm 0.051$	$18.605 \pm 0.030$	$17.830 \pm 0.024$	$17.737 \pm 0.029$	$17.530 \pm 0.010$ $17.530 \pm 0.032$	NOT	1.29
1037.41	78.3 81.4 85.3 86.3 87.3	10.0 10 1 0.001	$18.586 \pm 0.016$	$17.830 \pm 0.024$ $17.827 \pm 0.013$	$17.737 \pm 0.029$ $17.726 \pm 0.012$	$17.330 \pm 0.032$ $17.428 \pm 0.019$	LT	1.73
1037.42	78.3 81.4 85.3 86.3 87.3 90.3		$18.626 \pm 0.010$ $18.626 \pm 0.029$	$17.827 \pm 0.013$ $17.912 \pm 0.020$	$17.720 \pm 0.012$ $17.876 \pm 0.033$	$17.428 \pm 0.019$ $17.624 \pm 0.030$	CA	1.73
	78.3 81.4 85.3 86.3 87.3 90.3	$19.080 \pm 0.067$						
1047.52 1052.46	78.3 81.4 85.3 86.3 87.3 90.3		$18.748 \pm 0.026$ $18.813 \pm 0.040$	$18.056 \pm 0.027$ $18.141 \pm 0.028$	$17.987 \pm 0.019 \\ 18.120 \pm 0.016$	$17.707 \pm 0.021$ $17.834 \pm 0.020$	LT LT	1.45 1.73

Table 3 - continued

$\mathrm{JD}^a$	Epoch <sup>b</sup>	U	В	V	R	I	Telescope	Seeing
1056.37	109.2		$18.773 \pm 0.017$	$18.184 \pm 0.017$	$18.196 \pm 0.018$	$18.033 \pm 0.024$	CA	1.54
1056.40	109.3	$19.231 \pm 0.034$	$18.833 \pm 0.023$	$18.187 \pm 0.020$	$18.219 \pm 0.024$	$17.947 \pm 0.029$	NOT	0.68
1061.38	114.2		$18.879 \pm 0.044$	$18.322 \pm 0.025$	$18.352 \pm 0.030$	$18.102 \pm 0.024$	Ekar	1.70
1063.34	116.2		$18.913 \pm 0.040$	$18.363 \pm 0.039$	$18.438 \pm 0.044$	$18.145 \pm 0.038$	Ekar	1.51
1063.39	116.3		$18.944 \pm 0.025$	$18.356 \pm 0.018$	$18.422 \pm 0.028$	$18.110 \pm 0.021$	LT	1.59
1065.38	118.2	$19.623 \pm 0.074$					LT	1.37
1066.40	119.3		$19.002 \pm 0.021$	$18.404 \pm 0.014$	$18.481 \pm 0.016$	$18.218 \pm 0.018$	LT	1.28
1072.36	125.2		$19.025 \pm 0.045$	$18.532 \pm 0.040$	$18.660 \pm 0.048$	$18.490 \pm 0.046$	CA	1.27
1073.38	126.2		$19.070 \pm 0.023$	$18.564 \pm 0.017$	$18.675 \pm 0.024$	$18.349 \pm 0.029$	LT	1.12
1077.44	130.3		$19.180 \pm 0.030$	$18.643 \pm 0.025$	$18.778 \pm 0.020$	$18.422 \pm 0.022$	LT	1.17
1079.39	132.3		$19.248 \pm 0.049$	$18.673 \pm 0.051$	$18.801 \pm 0.067$		CA	2.70
1084.39	137.3		$19.227 \pm 0.022$	$18.753 \pm 0.016$	$18.907 \pm 0.013$	$18.605 \pm 0.017$	LT	1.14
1086.36	139.2	$20.001 \pm 0.096$					LT	1.09
1092.39	145.3			$18.863 \pm 0.067$	$18.995 \pm 0.060$		LT	1.95
1098.35	151.2		$19.480 \pm 0.021$	$19.007 \pm 0.015$	$19.293 \pm 0.028$	$18.897 \pm 0.033$	LT	1.17
1113.35	166.2		$19.684 \pm 0.019$	$19.271 \pm 0.015$	$19.664 \pm 0.020$	$19.175 \pm 0.029$	LT	0.95
1116.34	169.2			$19.306 \pm 0.144$	$19.732 \pm 0.104$	$19.165 \pm 0.256$	LT	1.34
1209.75	262.6		$21.696 \pm 0.036$	$21.457 \pm 0.035$	$22.078 \pm 0.067$		NOT	0.74
1247.85	300.7		$22.645 \pm 0.116$	$22.481 \pm 0.070$	$22.997 \pm 0.172$	$22.140 \pm 0.137$	NTT	1.34
1260.83	313.7		$22.941 \pm 0.171$	$22.500 \pm 0.160$	$23.338 \pm 0.273$	$22.123 \pm 0.123$	NTT	1.25
1263.90	316.8		$23.163 \pm 0.114$	$22.797 \pm 0.070$	$23.505 \pm 0.421$		NTT	1.03
1275.69	328.6				$23.583 \pm 0.271$	$22.345 \pm 0.142$	NOT	1.27
1409.48	462.3			$24.997 \pm 0.271$		$24.329 \pm 0.260$	TNG	0.75

 $<sup>^</sup>a$ JD  $- 2454\,000.00$ ;  $^b$ phase in days with respect to  $^a$ -band maximum JD  $= 2454\,947.1 \pm 0.3$ ;  $^c$ -stellar full width at half-maximum (FWHM) (arcsec).

are the quadratic sums of the measurement errors and the uncertainties in the photometric zero-points of the nights. Table A1 lists the *S*- and *K*-correction separately, meant as the quantity added to the zero-point calibrated magnitudes instead of a colour-term correction. The temporal evolution of the *S*-correction for the different instruments is shown in Fig. 3. The colour-term corrected *JHK'* magnitudes and their uncertainties (determined analogously to the optical bands) are shown in Table 4.

#### 2.3 Reduction of spectroscopic data

An overview of our spectroscopic observations of SN 2009dc is given in Table 5. All spectra were taken with the slit along the parallactic angle to avoid differential flux losses (Filippenko 1982). The reduction of the optical data followed standard procedures. The two-dimensional spectroscopic frames were debiased and flatfielded, before an optimal, variance-weighted extraction of the spectra (Horne 1986) was performed using the IRAF routine APALL. Wavelength calibration was accomplished with the help of arc-lamp exposures and checked against isolated night-sky lines. Second-order contamination in the spectra taken with NOT + ALFOSC was eliminated following the method of Stanishev (2007). The instrumental response functions were determined from observations of spectrophotometric standard stars (Oke 1990; Hamuy et al. 1992, 1994). An atmospheric extinction correction was applied using tabulated extinction coefficients for each observatory. Telluric features were

identified in the smooth spectra of the spectrophotometric standard stars and removed from the SN spectra. To check the flux calibration of the spectra, synthetic photometry was computed using Bessell (1990) passbands. If necessary, the spectral fluxes were adjusted to match the contemporaneous photometry. Finally, spectra obtained during the same night (at late phases also in subsequent nights) were combined to increase the signal-to-noise ratio (S/N); if the wavelength range of these spectra was different, they were averaged in their overlap region.

The reduction of our NIR spectra mostly followed the procedure described for the optical bands, with a few noticeable differences. The total integration time in the NIR was split into several sub-exposures, with the target offset along the slit. Subsequent exposures could thus be subtracted from each other to remove the sky emission. After extraction and wavelength-calibration, the SN spectra were divided by those of a telluric A0 standard star taken at similar airmass to remove telluric absorptions, and multiplied by a Vega spectrum to provide a relative flux calibration. Proper absolute flux calibration was achieved by comparison with contemporaneous JHK' photometry.

# 3 PHOTOMETRIC EVOLUTION

Fig. 4 shows that our photometry of SN 2009dc is generally in good agreement with that published by Silverman et al. (2011). There are some systematic discrepancies in the U band and – at more

CA = Calar Alto 2.2-m Telescope + CAFOS SiTe; http://www.caha.es/CA/Instruments/CAFOS/

TNG = 3.58-m Telescopio Nazionale Galileo + DOLORES; http://www.tng.iac.es/instruments/lrs/

LT = 2.00-m Liverpool Telescope + RATCAM; http://telescope.livjm.ac.uk/Info/TelInst/Inst/RATCam/

NOT = 2.56-m Nordic Optical Telescope + ALFOSC; http://www.not.iac.es/instruments/alfosc/

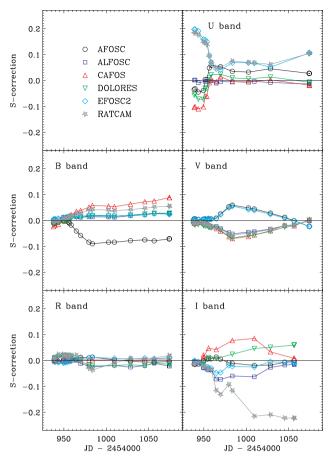
Ekar = 1.82-m Copernico Telescope + AFOSC; http://www.oapd.inaf.it/asiago/2000/2300/2310.html

NTT = 3.58-m New Technology Telescope + EFOSC2; http://www.eso.org/sci/facilities/lasilla/instruments/efosc/

JN = unfiltered image by JN; 0.28-m Celestron C11 + SBIG ST-8; http://www.astrosurf.com/snaude/

EP1 = unfiltered image by EP; 0.35-m Meade LX200 GPS 14 inches + SBIG ST-9XE; http://www.webalice.it/e.prosperi/

EP2 = unfiltered image by EP; 0.30-m Meade LX200 12 inches + SBIG ST-10XME; http://www.skylive.it/



**Figure 3.** Temporal evolution of the *S*-correction in the *UBVRI* bands for the different instrumental configurations used for follow-up observations of SN 2009dc.

advanced epochs – in the B band, which we attribute to missing S-and K-corrections in the Silverman et al. (2011) data. With absolute peak magnitudes between -19.8 and -21.1 in the optical bands, SN 2009dc is roughly a factor of 2 more luminous than the bulk of SNe Ia, and also slightly more luminous than the possible super- $M_{\rm Ch}$  SNe 2003fg (Howell et al. 2006) and 2006gz (Hicken et al. 2007).

Morphologically, the light curves of SN 2009dc resemble those of other SNe Ia. In the I and probably also the JHK' bands, a secondary light-curve maximum exists, delayed by  $\sim 25$  d with respect to the peak in B. The immediate post-maximum decline is faster in the bluer bands, accompanied by a strong evolution towards redder colours within the first month after peak.

However, compared to other SNe Ia the evolution of the light curves is very slow, both during the rise and the decline. With an unfiltered discovery magnitude of 16.5 (Puckett et al. 2009) on April 9.3, SN 2009dc was only ~1.2 mag below peak more than 16 d before *B*-band maximum light. Silverman et al. (2011) reported a detection of SN 2009dc at 3.5 mag below peak in an even earlier, unfiltered image taken with KAIT on April 4, 21.2 d before *B*-band maximum. This is clearly longer than the canonical rise time of SNe Ia of 17–20 d (Riess et al. 1999; Conley et al. 2006; Strovink 2007; Hayden et al. 2010). Silverman et al. (2011) also mentioned a non-detection in an unfiltered image taken on March 28, 28 d before *B*-band maximum, to a limiting magnitude of ~19.3. The rise time of SN 2009dc is therefore at least 22 d, but probably not more than 30 d.

With a polynomial fit to the *S*-corrected *B*-band light curve of SN 2009dc, a  $\Delta m_{15}(B)$  of  $0.69 \pm 0.03$  is inferred. Correcting for the effect of reddening (Phillips et al. 1999), this turns into  $\Delta m_{15}(B)_{\rm true} = 0.71 \pm 0.03$ . Yamanaka et al. (2009) reported a  $\Delta m_{15}(B)$  of  $0.65 \pm 0.03$ , marginally consistent with our result within the uncertainties, whereas Silverman et al. (2011) derived  $\Delta m_{15}(B) = 0.72 \pm 0.03$ , in excellent agreement with our value. This decline rate is among the lowest ever measured for SNe Ia, similar to those of SNe 2006gz (0.69; Hicken et al. 2007) and 2007if (0.71; Scalzo et al. 2010).

The decline of the R-band light curve is remarkably linear for more than 300 d after maximum, with only a slight shoulder after one month. The first and second maximum in the I band are almost equally bright. However, the minimum in between is not very pronounced, and with  $\sim$ 25 d the offset of the two maxima is not particularly large. This is similar to the situation in SN 2006gz, but contrary to the trend of more pronounced and delayed secondary maxima that is observed in other SNe Ia with small  $\Delta m_{15}(B)$ (Hamuy et al. 1996). Moreover, the first I-band maximum does not precede those in the bluer band as in other luminous SNe Ia, but is slightly delayed. This behaviour is reminiscent of subluminous SNe Ia. However, in the latter it appears to be a consequence of the small <sup>56</sup>Ni mass (Kasen 2006), which cannot be the reason in SN 2009dc. Alternatively, <sup>56</sup>Ni could be more strongly mixed (Kasen 2006), but this is disfavoured by the long rise time and the weak line blanketing in the UV part of early spectra, indicative of little Fe-group material in the outer shells (cf. Section 4.1).

The late-time photometric behaviour of SN 2009dc deserves special attention after the lesson taught by SN 2006gz (Maeda et al. 2009): the slow decline of the light curves of SN 2006gz soon after peak must have been followed by a rapid drop at later times, when the SN was too close to the Sun to be observed. An attempt to recover the SN photometrically one year after maximum failed, and the derived upper limits indicate a faster average post-maximum decline than observed in normal SNe Ia (Maeda et al. 2009). In SN 2009dc, no accelerated decline is seen until 180 d after peak. The decline rates between 60 and 170 d, ranging from  $1.42 \pm 0.02$  mag  $(100 \,\mathrm{d})^{-1}$  in B to  $2.62 \pm 0.02 \,\mathrm{mag} \,(100 \,\mathrm{d})^{-1}$  in R (cf. Table 6), are comparable to those of normal SNe Ia. However, thereafter the situation changes completely. While the R-band light curve continues its linear decline from earlier phases, the bluer bands now show a much more rapid fading than before, with decline rates very similar to that in R (Table 6). This behaviour is at odds with both that of normal SNe Ia and the expectation that around 300 d the (bolometric) decline rate should slow down and approach the <sup>56</sup>Co decay rate of  $0.98 \,\mathrm{mag} \,(100 \,\mathrm{d})^{-1}$ , since the ejecta are then fully transparent to  $\gamma$ -rays, but still mostly opaque to positrons. There are hints that the decline might eventually slow down more than 400 d after the explosion. However, this very late decline rate is very uncertain, since our last photometric measurement might be contaminated by host-galaxy light or background sources. The discrepancy between expectation and observation is addressed again when studying the pseudo-bolometric light curve in Section 3.2, and possible reasons are discussed in Section 5.2.

In the JHK' bands (Fig. 5), the paucity of observations makes an analysis of the light curves less robust. Nevertheless, in all three bands the secondary maximum seems to be particularly bright, whereas the first maximum is weak (J) or degraded to a shoulder (HK'). The steep decline in J characteristic for normal SNe Ia after the first peak is almost entirely absent in SN 2009dc. Since the majority of the flux in the NIR is caused by fluorescence (e.g. Kromer & Sim 2009), the lack of emission compared to ordinary SNe Ia around the time of B-band maximum suggests less flux

Table 4. Colour-term/zero-point calibrated JHK' magnitudes of SN 2009dc.

$\mathrm{JD}^a$	Epoch <sup>b</sup>	J	Н	<i>K'</i>	Telescope	Seeing
941.68	-5.4	$15.728 \pm 0.025$	$15.826 \pm 0.028$	$15.707 \pm 0.028$	TNG-N	1.43
947.81	0.7	$15.653 \pm 0.150$			REM	3.24
952.72	5.6	$15.668 \pm 0.170$			REM	2.76
954.70	7.6	$15.751 \pm 0.033$	$15.680 \pm 0.031$	$15.410 \pm 0.029$	TNG-N	1.15
963.55	16.4	$16.042 \pm 0.032$	$15.620 \pm 0.037$	$15.388 \pm 0.034$	NOT-N	0.68
967.56	20.4	$15.958 \pm 0.213$			REM	3.36
969.78	22.6	$15.921 \pm 0.029$	$15.516 \pm 0.029$	$15.415 \pm 0.045$	NTT-S	0.78
993.61	46.5	$16.119 \pm 0.207$			REM	3.00
1031.41	84.3	$18.332 \pm 0.069$	$17.335 \pm 0.036$	$17.522 \pm 0.074$	TNG-N	0.83
1057.48	110.3	$19.197 \pm 0.078$	$18.119 \pm 0.064$	$18.119 \pm 0.091$	NTT-S	1.12
1212.06	264.9		≥20.4		LBT	1.55
1213.02	265.9	$21.788 \pm 0.078$			LBT	0.53
1305.84	358.7	≥19.9	≥18.8	≥18.6	NTT-S	1.29

 $<sup>^{</sup>a}$ JD - 2454000.00;  $^{b}$ phase in days with respect to *B*-band maximum JD = 2454947.1  $\pm$  0.3;  $^{c}$  stellar FWHM (arcsec).

TNG-N = 3.58-m Telescopio Nazionale Galileo + NICS; http://www.tng.iac.es/instruments/nics/ REM = 0.60-m Rapid Eye Mount + REMIR; http://www.rem.inaf.it/

NOT-N = 2.56-m Nordic Optical Telescope + NOTCam; http://www.not.iac.es/instruments/notcam/ NTT-S = 3.58-m New Technology Telescope + SOFI; http://www.eso.org/sci/facilities/lasilla/

instruments/sofi/ LBT =  $2 \times 8.4$ -m Large Binocular Telescope + LUCIFER; http://abell.as.arizona.edu/~lbtsci/Instruments/LUCIFER/

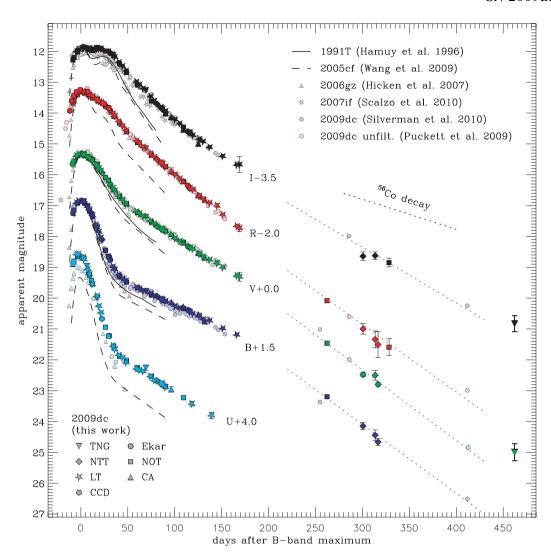
Table 5. Log of spectroscopic observations of SN 2009dc.

$\mathrm{JD}^a$	$Epoch^b$	Exposure time (s)	Telescope <sup>c</sup>	Grism/Grating	Range (Å)	Res. (Å) <sup>d</sup>
937.7	-9.4	1500	TNG	LR-B	3200-7900	10
938.6	-8.5	1500	NOT	gm4	3200-9100	13
939.7	-7.5	900	NOT	gm4	3200-9100	13
941.7	-5.4	$1800 \times 2$	TNG-N	IJ,HK	8650-24700	18,36
943.5	-3.7	900	NOT	gm4	3200-9100	14
949.5	2.4	$900 \times 2$	TNG	LR-B,LR-R	3200-9750	13
949.6	2.5	$1800 \times 2$	CA	b200,r200	3300-10200	10
951.6	4.5	2400	CA	b200	3200-8750	10
953.7	6.5	$900 \times 2$	TNG	LR-B,LR-R	3250-9750	10
954.7	7.5	$1800 \times 2$	TNG-N	IJ,HK	8650-24700	18,36
955.5	8.4	$1800 \times 2$	CA	b200,r200	3250-10300	9
956.5	9.3	900	NOT	gm4	3250-9100	14
958.6	11.5	900	NOT	gm4	3250-9100	14
959.6	12.5	$600 \times 3$	NOT	gm4	3300-9100	13
964.7	17.5	$900 \times 2$	TNG	LR-B,LR-R	3200-9600	10
969.7	22.5	$900 \times 2$	NTT	gm11,gm16	3350-9500	14
970.8	23.6	3240 + 3000	NTT-S	GB,GR	9350-25 000	23,32
979.5	32.4	2400 + 2000	Ekar	gm4,gm2	3600-9200	24,34
983.6	36.4	$2100 \times 2$	CA	b200,r200	3300-10300	10
1002.6	55.5	2100	TNG	LR-B	3400-7900	14
1009.5	62.4	$2400 \times 2$	CA	b200,r200	3400-10300	10
1028.5	81.4	$1800 \times 2$	NTT	gm11,gm16	3400-9500	21
1031.5	84.3	3600 + 5760	TNG-N	IJ,HK	8650-24700	18,36
1045.4	98.3	$3600 \times 2$	CA	b200,r200	3600-10000	10
1056.5	109.3	$4800/2700 \times 2$	NOT/CA	gm4/r200	3650-10000	17,11
1074.4	127.2	$2700 \times 4$	CA	b200	3400-8750	12
1112.3	165.1	3600 × 2	CA	b200	3500–8750	12

 $<sup>^</sup>a$  JD  $-2454\,000.0$ ;  $^b$ phase in days with respect to *B*-band maximum JD  $=2454\,947.1\pm0.3$ ;  $^c$ see Tables 3 and 4 for details;  $^d$ FWHM of isolated, unblended night-sky lines.

re-distribution from the blue and UV part of the spectrum to redder wavelengths. This is in agreement with a high UV flux until  $\sim$ 10 d after maximum light as also reported by Silverman et al. (2011), and a strong fading in the UV thereafter. After the secondary peak, the *JHK'* light curves of SN 2009dc decline more slowly than those of ordinary SNe Ia, and it was possible to recover the SN in deep

J-band images taken at the LBT 266 d after B-band maximum light. Note that with peak absolute magnitudes of about -19.3 to -19.4, SN 2009dc is overluminous also in J, H and K'. It does not follow the behaviour of normal SNe Ia, which are nearly standard candles in the NIR (with  $M_{JHK'} \sim -18.1$  to -18.3; Krisciunas, Phillips & Suntzeff 2004; Wood-Vasey et al. 2008).



**Figure 4.** Bessell *UBVRI* light curves of SN 2009dc (coloured symbols). The data are *S*- and *K*-corrected with the exception of the unfiltered amateur data, which were calibrated to the *R* band employing colour-term corrections (Table 3). The unfiltered discovery magnitudes reported by Puckett et al. (2009, open red pentagons) are plotted with the same vertical shift as our *R* magnitudes. In this figure, a constant shift of −0.2 mag has been applied to the Liverpool Telescope (LT) *U*-band photometry to eliminate a systematic offset with respect to the *U*-band data of other telescopes. The SN 2009dc light curves of Silverman et al. (2011), the light curves of the superluminous SNe 2006gz (Hicken et al. 2007) and 2007if (Scalzo et al. 2010), and light-curve templates of the luminous SN Ia 1991T (Hamuy et al. 1996) and the normal SN Ia 2005cf (Wang et al 2009b) are shown for comparison, shifted in time and magnitude to match SN 2009dc at maximum light in *B*.

Table 6. Light-curve tail decline rates of SN 2009dc.

Interval <sup>a</sup>	$\Delta U^b$	$\Delta B^b$	$\Delta V^b$	$\Delta R^b$	$\Delta I^b$
60–170 d 150–330 d	1.94	1.42 2.19	1.95 2.28	2.62 2.48	2.59 2.04
260–330 d 260–460 d		2.59	2.30 1.69	2.40	1.42

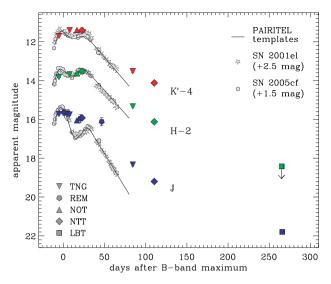
<sup>&</sup>lt;sup>a</sup>With respect to *B*-band maximum; <sup>b</sup>in mag  $(100 \,\mathrm{d})^{-1}$ .

#### 3.1 Colour evolution

Fig. 6 presents the time-evolution of the U-B, B-V, V-R and V-I colours of SN 2009dc. The basic behaviour of these curves appears typical of a SN Ia, starting with relatively blue colours before and around maximum light, turning redder until  $\sim$ 40 d thereafter, and then again evolving towards bluer colours (except for U-B which monotonically becomes redder). However,

at a higher level of detail differences become evident. The early U-B colour of SN 2009dc is unusually blue because of little UV line blanketing and the weakness of Ca II H&K (cf. Section 4.1). In normal SNe Ia, the V-R and V-I colours are bluest around and immediately after maximum light, whereas in SN 2009dc they monotonically turn redder from the start of our observations until 40 d after maximum light. Even more importantly, SN 2009dc does not conform with the uniform B-V colour evolution of other SNe Ia between 30 and 90 d after maximum, known as the Lira relation (Lira 1995; Phillips et al. 1999). Instead, its B-V colour evolves much more slowly, and is redder than predicted by the Lira relation by almost 0.3 mag at 90 d. Hence, for SN 2009dc, none of the colour criteria usually used to estimate the reddening in SNe Ia can be employed confidently.

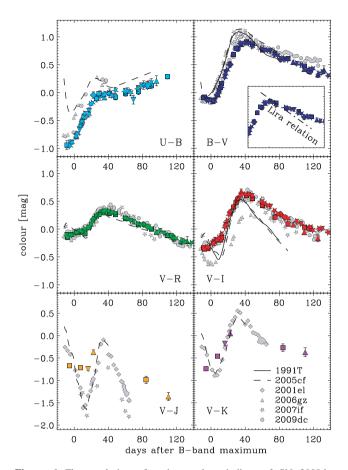
Note that the colour evolution of SN 2009dc shares more similarities with those of SNe 2006gz and 2007if than with the bulk of SNe Ia (Fig. 6), suggesting that some of the observed colour characteristics may be generic for superluminous SNe Ia.



**Figure 5.** *JHK'* light curves of SN 2009dc. The phase is in days with respect to *B*-band maximum light on JD = $2454947.1 \pm 0.3$ . The NIR light curves of SNe 2001el (Krisciunas et al. 2003) and 2005cf (Pastorello et al. 2007a; Wang et al 2009b), and the NIR template light curves constructed from PAIRITEL observations (Wood-Vasey et al. 2008) are shown for comparison, shifted to line up with SN 2009dc at maximum.

#### 3.2 Bolometric light curve

A pseudo-bolometric light curve (see e.g. Nomoto, Filippenko & Shigeyama 1990) of SN 2009dc was constructed from our filtered photometry. To this aim, the U-through-K'-band magnitudes were first converted into monochromatic fluxes. The spectral energy distribution (SED) was then interpolated linearly and integrated over wavelength, assuming zero flux at the blue edge of the U band and the red edge of the K' band. In case of missing JHK' data, a NIR correction to the U-through-I light curve was estimated by interpolation between adjacent epochs with NIR data. At very late phases, constant I - H and I - K' colours were assumed. We find a NIR contribution to the pseudo-bolometric light curve of  $\sim$ 10 per cent around maximum light, ~28 per cent 40 d after maximum, and  $\sim$ 20 per cent 100 d after maximum. Compared to ordinary SNe Ia and core-collapse SNe, this NIR contribution in SN 2009dc is quite low (Fig. 7, bottom panel). Wavelength regions other than the optical and NIR are believed to contribute very little to the total bolometric flux in SNe Ia (Contardo, Leibundgut & Vacca 2000), and are neglected here.4 The resulting quasi-bolometric light curve of SN 2009dc is shown in Fig. 7 (top panel), along with those of the normal Type Ia SNe 2003du [Stanishev et al. 2007a,  $\Delta m_{15}(B) =$ 1.02], 2001el [Krisciunas et al. 2003,  $\Delta m_{15}(B) = 1.13$ ] and 2004eo [Pastorello et al. 2007b,  $\Delta m_{15}(B) = 1.46$ ], the subluminous SN Ia 1999by [Garnavich et al. 2004,  $\Delta m_{15}(B) = 1.90$ ], the superluminous SN Ia 2007if [Scalzo et al. 2010,  $\Delta m_{15}(B) = 0.71$ ] and the Type Ic hypernova 1998bw (Galama et al. 1998; McKenzie & Schaefer 1999; Sollerman et al. 2000; Patat et al. 2001). Neither SN 1998bw, which is one of the most luminous non-interacting



**Figure 6.** Time-evolution of various colour indices of SN 2009dc, reddening-corrected adopting a Cardelli et al. (1989) extinction law with E(B-V)=0.17 mag and  $R_V=3.1$  (coloured symbols). A constant shift of -0.2 mag has been applied to the Liverpool Telescope (LT) *U*-band photometry to eliminate a systematic offset with respect to other telescopes. The SN 2009dc colour curves of Silverman et al. (2011), the colour curves of the superluminous SNe 2006gz (Hicken et al. 2007) and 2007if (Scalzo et al. 2010), and those of the Type Ia SNe 1991T (Hamuy et al. 1996), 2001el (Krisciunas et al. 2003, 2007) and 2005cf (Pastorello et al. 2007a; Wang et al 2009b) – all of them reddening-corrected – are shown for comparison. The inset in the top-right panel illustrates the deviation of the B-V curve of SN 2009dc from the Lira relation (Lira 1995; Phillips et al. 1999).

core-collapse SNe known to date (with about  $0.4~M_{\odot}$  of  $^{56}$ Ni synthesised; Maeda, Mazzali & Nomoto 2006), nor any of the classical SNe Ia can compete with SN 2009dc in terms of luminosity. With  $\log L = 43.47 \pm 0.11$  (erg s<sup>-1</sup>), SN 2009dc outshines ordinary SNe Ia by a factor  $\sim$ 2 at peak<sup>5</sup>, and the difference increases during the first  $\sim$ 150 d past maximum. Only SN 2007if keeps up with SN 2009dc, showing a strikingly similar bolometric light curve. After the peak phase, SNe generally have a decline rate which is significantly faster than the  $^{56}$ Co decay. The reason for this behaviour is an increasing escape fraction of  $\gamma$ -rays due to decreasing opacities. SN 2009dc also shows this behaviour, but fades more slowly than

<sup>&</sup>lt;sup>4</sup> Actually, owing to the relatively high UV flux in SN 2009dc indicated by its very blue early-time spectra, the mid- and far-UV could have a non-negligible effect on the pre-maximum bolometric light curve. Unfortunately, the *Swift* UVOT photometry presented by Silverman et al. (2011) only starts at maximum light, when the contribution of these bands has dropped below the 10 per cent level.

<sup>&</sup>lt;sup>5</sup> For the same assumption on the host-galaxy reddening  $[E(B-V)_{\text{host}}=0.10 \text{ mag}]$ , Silverman et al. (2011) derive a peak bolometric luminosity of  $\log L=43.52\pm0.08$  (erg s<sup>-1</sup>). Based on a slightly larger host reddening  $[E(B-V)_{\text{host}}=0.14 \text{ mag}]$ , Yamanaka et al. (2009) obtain  $\log L=43.52\pm0.12$  (erg s<sup>-1</sup>). Both results are in agreement with our estimate.

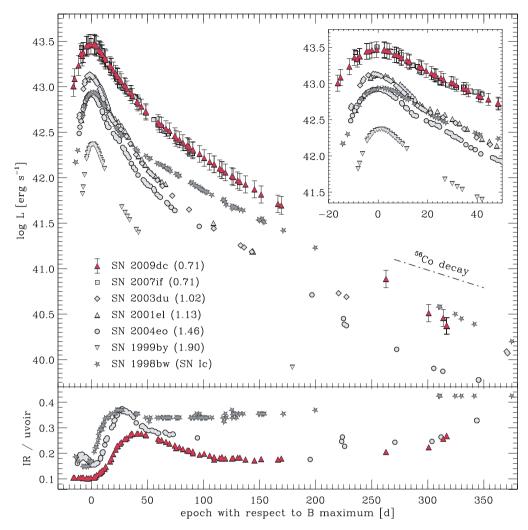


Figure 7. Top panel: pseudo-bolometric light curves of SN 2009dc, the superluminous SN Ia 2007if, the normal Type Ia SNe 2003du, 2001el and 2004eo, and the subluminous SN Ia 1999by. The exceptionally energetic and luminous Type Ic SN 1998bw is shown for comparison. All light curves were obtained by integrating the U-through-K'-band fluxes. Error bars are shown for SN 2009dc only, and account for uncertainties in the photometric calibration, distance and extinction estimates. The  $\Delta m_{15}(B)_{true}$  of all SNe Ia is given in parentheses. Bottom panel: NIR contribution to the pseudo-bolometric light curves of SNe 2009dc, 2004eo and 1998bw.

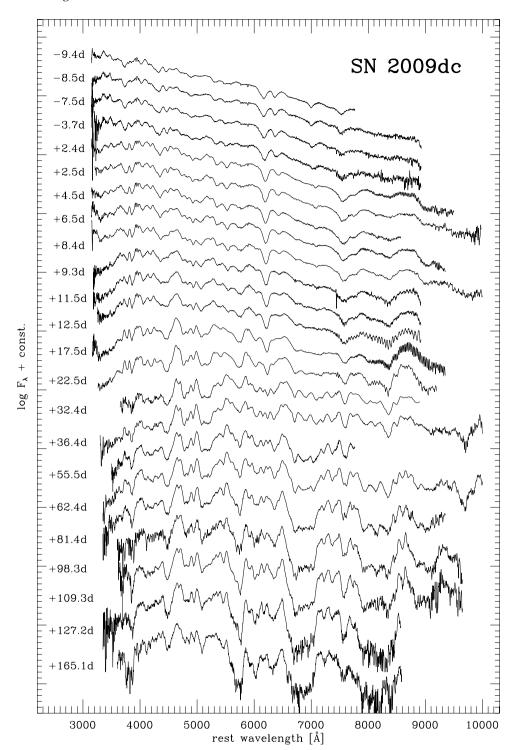
normal SNe Ia until  $\sim$ 150 d past maximum. This is an indication for a larger  $\gamma$ -ray opacity, caused by the low ejecta velocities or by a larger ejecta mass. SN 1998bw has very massive ejecta (Maeda et al. 2006 estimated  $M_{\rm ej} \sim 10~{\rm M}_{\odot}$ ) and thus shows an even slower late-time decline.

However, as already noted in Section 3, the behaviour of SN 2009dc changes substantially 200–250 d after maximum. The decline of the pseudo-bolometric light curve becomes steeper than it was the months before. In fact, one year after the explosion, SN 2009dc is no longer more luminous than the normal SN Ia 2003du. Unfortunately, we do not have full wavelength coverage at those late phases (the pseudo-bolometric light curve is based on *B*-through-*J*-band photometry), so that this statement must be taken with a grain of salt. Nevertheless, there is a clear flux deficit in the optical regime (out to the *J* band) with respect to expectations based on an extrapolation from earlier epochs. It is unlikely that an increased *H*- and *K'*-band flux could make up for this.

## 4 SPECTROSCOPIC EVOLUTION

#### 4.1 Optical spectra

The optical spectra of SN 2009dc, presented in Fig. 8 show a transition from a blue pseudo-continuum with superimposed P-Cygni features at early phases to line-dominated emission after a few months. Throughout its evolution, SN 2009dc is characterized by comparatively narrow spectral features, indicating a small extension (in velocity space) of the line-formation zone, and resulting in reduced line blending compared to ordinary SNe Ia. In this respect, SN 2009dc resembles 02cx-like SNe Ia (Li et al. 2003), which have comparably low ejecta velocities. However, given that the latter are at least moderately subluminous, no direct conclusions on similar progenitors or explosion mechanisms can be drawn. In what follows, the spectra of SN 2009dc at several characteristic epochs will be described in more detail and compared with those of other normal and peculiar SNe Ia.

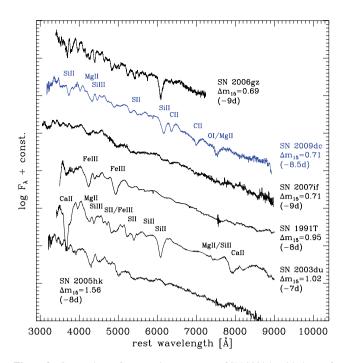


**Figure 8.** Time sequence of SN 2009dc spectra in the SN rest frame. The phases reported next to each spectrum are with respect to *B*-band maximum light (JD =  $2454947.1 \pm 0.3$ ). The +165.1 d spectrum has been smoothed with a kernel of 2500 km s<sup>-1</sup> for presentation purposes.

# 4.1.1 One week before maximum

In the -8.5 d spectrum of SN 2009dc (Fig. 9), lines of Si II, Si II, S II, C II, O I and possibly Mg II can be identified. Compared to normal SNe Ia, represented by SN 2003du in Fig. 9, all features due to IMEs appear shallower. In particular, the Ca II lines, very prominent in SN 2003du, are weak. The Ca II NIR triplet cannot be identified, and Ca II H&K form merely a shoulder to the red of Si II  $\lambda 3859$ . The

EW of Si II  $\lambda$ 6355 is only 44 Å, compared to 71 Å in SN 2003du. On the contrary, lines due to unburned material are very pronounced. While in most normal SNe Ia at best a hint of O I  $\lambda$ 7774 can be discerned at early phases (probably blended with Mg II), the line is one of the strongest features in SN 2009dc. The same is true for C II features ( $\lambda\lambda$ 6580, 7234), which are only occasionally identified in very early SN Ia spectra (e.g. Thomas et al. 2007; Tanaka et al. 2008; Taubenberger et al. 2008), but are present at unprecedented strength



**Figure 9.** Comparison of pre-maximum spectra of SN 2009dc with those of other superluminous SNe Ia (2006gz and 2007if; Hicken et al. 2007; Scalzo et al. 2010), the classical luminous SN 1991T (Filippenko et al. 1992; Ruiz-Lapuente et al. 1992; Gómez, López & Sánchez 1996), the normal SN Ia 2003du (Stanishev et al. 2007a) and the peculiar, 02cx-like SN 2005hk (Phillips et al. 2007; Stanishev et al. 2007b). The spectra of SNe 2006gz and 2007if have been slightly smoothed for clarity. An identification of the major absorption lines has been attempted.

in the -8.5 d spectrum of SN 2009dc. The overall continuum shape is rather blue, and down to the blue cut-off of the spectrum at  $\sim$ 3200 Å no severe flux depression due to blanketing of Fe-group lines is observed. In summary, lines from unburned material are strong in SN 2009dc at early phases, whereas all lines from burning products are relatively weak. Of course, line formation does not only depend on the composition, but also on the ionization and excitation conditions, and indeed the weakness of lines from singly ionized IMEs and Fe-group elements could be explained by a high ionization (supported also by the relative strength of Si III  $\lambda$ 4563). However, the simultaneous strength of O I  $\lambda$ 7774 and the lack of detectable Fe III lines do not favour this scenario. Instead, we believe that the composition of the line-formation zone at day -8.5 is indeed dominated by unburned material.

With its spectral properties, SN 2009dc deviates from any of the established subclasses of peculiar SNe Ia. The classical very luminous SN Ia 1991T is characterized by very high ionization, the blue spectrum being dominated by prominent Fe III lines and little else. In particular, lines from IMEs are very weak, and no features of C II or O I are found. Contrary to the low-velocity SN 2009dc, the lines in SN 1991T are rather broad, and their blueshift is similar to that in normal SNe Ia. 02cx-like SNe like SN 2005hk show the same low ejecta velocities as SN 2009dc, but apart from that their early-time spectra closely resemble those of 91T-like objects.

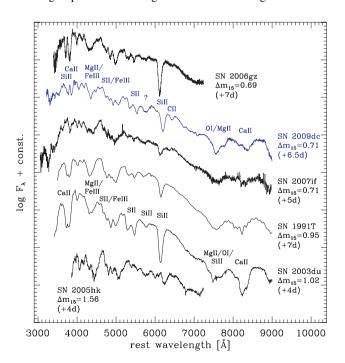
A comparison with other superluminous SNe Ia reveals that SN 2007if has similar velocities as SN 2009dc, but apparently a higher ionization. This results in much weaker lines from IMEs and unburned material and the presence of Fe III lines. However, Fe III in SN 2007if is not as strong as in SN 1991T, indicating that the ionization is not quite as high, or the Fe-group-element abundance above the

photosphere is lower. In SN 2006gz, on the contrary, the same features as in SN 2009dc are present (though with weaker C II lines). Line blending seems to be even lower, and all features are sharp and pronounced. However, contrary to common sense these narrow lines do not correspond to particularly low velocities of the ejecta as determined from the blueshift of the P-Cygni minima (which is comparable to that in normal SNe Ia and significantly larger than in SN 2009dc).

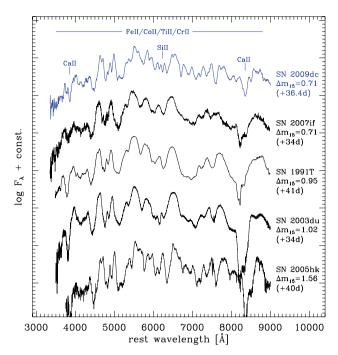
#### 4.1.2 One week past maximum

By a week after maximum (Fig. 10), the spectrum of SN 2009dc has evolved significantly, but its main characteristics have not changed too much. There is still a blue continuum, spectral features are not particularly deep, and the line velocities are even lower than before. The UV flux has diminished compared to the first observations, suggesting stronger UV line blanketing due to Fe-group elements. Also the lines from IMEs (Si II, S II, Mg II) have become more pronounced, and the Ca II H&K and NIR triplet lines are now clearly visible (though still weak compared to normal SNe Ia). O 1 λ7774 is very pronounced, although the shape of the feature indicates blending with another line, most likely Mg II λ7890. The C II lines are weaker than before maximum light, but still clearly detected. This is remarkable given that in no other SN Ia have such strong C II lines been found at such a relatively late epoch. The identification of an absorption feature at ~5760 Å remains unclear: compared to Si II  $\lambda 6355$  it is at too blue a wavelength to be identified with Si II  $\lambda 5972$ . Na I D, possibly blended with Si II λ5972, could be an explanation.

Apart from the lower velocities and the C II lines, the spectrum of SN 2009dc is now fairly similar to that of SN 1991T. A normal SN Ia like 2003du has deeper Si II, S II and Ca II lines, whereas in SN 2005hk these IME features are shallower than in SN 2009dc and at even lower velocity. SN 2009dc's superluminous colleagues again reveal some variation in line velocities and strengths within this subgroup: both SN 2006gz and 2007if show higher velocities



**Figure 10.** The same as Fig. 9, but for spectra taken about a week after maximum light.



**Figure 11.** The same as Fig. 9, but 5–6 weeks after maximum light. The spectrum of SN 2007if has been slightly smoothed for better clarity.

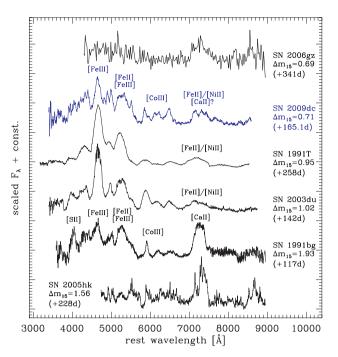
than SN 2009dc at this phase, but while the absorption lines in SN 2006gz are as deep as in a normal SN Ia, those in SN 2007if are even less pronounced than those in SN 2009dc.

#### 4.1.3 Five weeks past maximum

Five to six weeks after maximum, the spectra of all SNe Ia are dominated by lines of Fe-group elements (Fe II, Co II, Ti II, Cr II) and Ca II, and SN 2009dc is no exception in this respect (Fig. 11). SN 2003du, SN 1991T and the superluminous SN 2007if are very similar at this epoch, showing fairly broad and blended spectral features. This suggests that at least the inner ejecta of SN 2007if have velocities comparable to normal SNe Ia. SN 2009dc, on the contrary, has much narrower and less blended lines. There is now a remarkable similarity between SN 2009dc and the 02cx-like SN Ia 2005hk in terms of velocities and line blending, but also in the relative strengths of different lines. Exceptions are Ca II (which is weaker in SN 2009dc) and Si II  $\lambda$ 6355 (which can still be identified in SN 2009dc but is absent in SN 2005hk).

#### 4.1.4 Nebular phase

Fig. 12 presents late-time spectra of SNe 2009dc, 2006gz, 1991T, 2003du, 2005hk and the prototypical subluminous Type Ia SN 1991bg. Several of the spectra are too early to be considered fully nebular, but in all of them the (forbidden) emission lines dominate over residual photospheric flux. SNe 2003du and 1991T have very similar spectra with prominent [Fe II], [Fe III] and [Co III] emission lines, the reduced strength of the [Co III] lines in SN 1991T being a consequence of the later epoch of the spectrum with more Co already decayed to Fe. The lines in SN 1991T are also broader than those in SN 2003du, indicating more Fe-group material at higher velocities, in agreement with the larger Ni mass and the detection of Fe-group material in the outer layers in early spectra (Ruiz-Lapuente et al. 1992; Mazzali, Danziger & Turatto 1995). SN 2009dc once



**Figure 12.** Comparison of SN 2009dc with SNe 2006gz (Maeda et al. 2009), 1991T, 2003du, 2005hk (Sahu et al. 2008) and the subluminous 1991bg (Turatto et al. 1996) during the nebular phase. The +165.1 d spectrum of SN 2009dc has been smoothed with a kernel of 2500 km s $^{-1}$  for presentation purposes. Prominent emission features have been identified.

more shows narrower and better resolved emission lines owing to the low ejecta velocities. However, there are also more subtle differences. The emission feature at  $\sim$ 4650 Å, mostly a blend of [Fe III] lines, is much less pronounced in SN 2009dc, indicating a lower Fe III-to-Fe II ratio than normal. This lower ionization is most likely explained by enhanced recombination as a consequence of the relatively low velocities/high densities in the inner ejecta of SN 2009dc. In this particular aspect, SN 2009dc resembles subluminous SNe Ia such as SN 1991bg, which also show suppressed [Fe III] lines in their nebular spectra because of low velocities and temperatures (Mazzali et al. 1997). However, 91bg-like SNe also show a prominent emission feature at  $\sim$ 7300 Å, identified as [Ca II]  $\lambda\lambda$ 7291, 7323 by Mazzali et al., which is significantly weaker and probably dominated by [Fe II] and [Ni II] in SN 2009dc.

The nebular spectra of SNe 2006gz (Maeda et al. 2009) and 2005hk (Sahu et al. 2008) deserve some comments. The SN 2005hk spectrum is characterized by a multitude of extremely narrow features (much narrower now than those of SN 2009dc) and by the complete absence of prominent [Fe II] and [Fe III] lines. In fact, despite the relatively advanced epoch, this spectrum is not yet nebular in most parts, which is probably a consequence of the low velocities and the corresponding high densities. The spectrum of SN 2006gz also is highly peculiar: there is a strong feature at  $\sim$ 7300 Å, but like in SN 2005hk there is almost no emission in the blue (though this region suffers from very low S/N). In SN 2006gz this unusual spectral appearance comes along with an unexpectedly low luminosity for the given epoch, seemingly inconsistent with the large <sup>56</sup>Ni mass derived from early-time data. Given that we find an accelerated light-curve decline also in SN 2009dc past 200 d (Section 3), one could speculate that at a sufficiently late epoch (more than a year after the explosion) the spectra of SN 2009dc might look similar to the nebular spectrum of SN 2006gz.

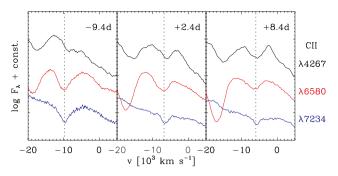


Figure 13. C II lines in SN 2009dc. The profiles of C II λ4267 (top black line; possibly Cr II instead of C II, see text), C II λ6580 (middle red line) and C II λ7234 (bottom blue line) are compared at three different epochs. The vertical dotted lines correspond to velocities of 9700, 6800 and 6000 km s<sup>-1</sup> at -9.4, +2.4 and +8.4 d, respectively.

#### 4.1.5 C II lines

As mentioned earlier, SN 2009dc is the Type Ia SN with the strongest and most persistent C II lines ever observed. C II can be identified from the earliest spectra to about two weeks after maximum light. Previously, C II features were only reported in very early spectra of normal SNe Ia (e.g. Thomas et al. 2007), in pre-maximum spectra of the superluminous SN Ia 2006gz (Hicken et al. 2007) and more tentatively - around maximum light in some 02cx-like SNe (e.g. Sahu et al. 2008) and the superluminous SNe 2003fg (Howell et al. 2006) and 2007if (Scalzo et al. 2010). In SN 2009dc there is little doubt that the C<sub>II</sub> identification is correct, since not only the  $\lambda 6580$  line, but also the  $\lambda 7234$  line is clearly detected (Fig. 13). There may even be C<sub>II</sub>  $\lambda$ 4267 in form of a notch around 4150 Å, but Scalzo et al. (2010) suggested Cr II as an alternative explanation for this feature in SN 2007if. Given that this line strengthens while CII  $\lambda\lambda6580$  and 7234 fade with time we tend to agree with this interpretation.

# 4.2 NIR spectra

At four epochs, our optical spectra of SN 2009dc are complemented by NIR spectra, so that combined spectra can be constructed which cover a wavelength interval from  $\sim 0.35$  to  $\sim 2.45 \,\mu m$  (with gaps in the NIR where the earth's atmosphere is opaque). These spectra are presented in Fig. 14. Starting with a relatively smooth, blue continuum before maximum light, the NIR spectra of SN 2009dc show increasing structure as the SN evolves, and develop some flux deficit in the J band. In the +23.6 d spectrum, Co II lines start to be visible in the K-band region, which is a typical feature of SNe Ia at these epochs (Marion et al. 2009a). The +84.3 d spectrum, finally, shows a large number of narrow absorptions and emissions in the J- and H-band regions, most of them due to Co II, Fe II and other Fe-group elements (Marion et al. 2009a). In spite of the prominent C II features in the optical part of the spectrum, there is no evidence at any time for C<sub>I</sub> lines in the NIR. On the contrary, in the carbonrich Type Ic SN 2007gr, C1 was unambiguously detected in the NIR early on (Valenti et al. 2008), indicating a quite different level of ionization. Similarly, we do not find any features which could be attributed to the NIR He I 1.083 and 2.058 µm lines. Being the strongest He I lines in the entire optical and NIR regime, these lines are sensitive indicators of the amount of He present in the SN ejecta. Their absence requires nearly He-free conditions, which could be a challenge for some of the potential explosion models discussed in Section 5.3.

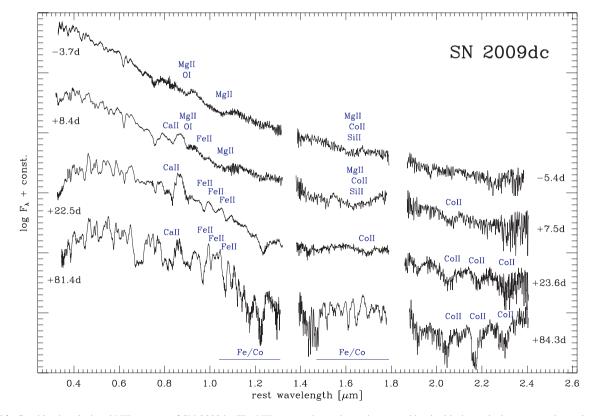


Figure 14. Combined optical and NIR spectra of SN 2009dc. The NIR spectra have always been combined with the optical spectrum closest in time. The -5.4 and +84.3 d spectra of SN 2009dc have been smoothed for better clarity. Line identifications have been adopted from Marion et al. (2009a).

by Leiden University user on 23 November 2017

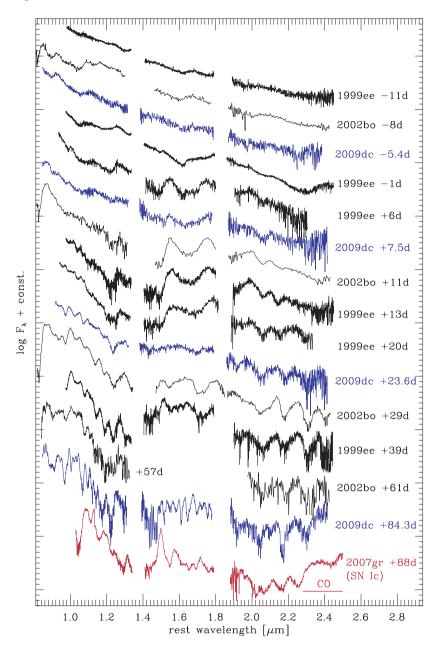


Figure 15. Comparison of NIR spectra of SN 2009dc with those of the normal Type Ia SNe 1999ee (Hamuy et al. 2002) and 2002bo (Benetti et al. 2004). The -5.4 and +84.3 d spectra of SN 2009dc have been smoothed for presentation purposes. A late-phase NIR spectrum of the Type Ic SN 2007gr is shown to illustrate the possibility of CO molecular-band emission in the +84.3 d spectrum of SN 2009dc.

Fig. 15 presents a comparison of the NIR spectra of SN 2009dc with those of the well-sampled normal SNe Ia 1999ee (Hamuy et al. 2002) and 2002bo (Benetti et al. 2004). While SNe 1999ee and 2002bo are very consistent with each other in their spectral evolution, SN 2009dc shows both similarities and differences. The overall SED of SN 2009dc and its time evolution resemble those of the other objects, but the flux deficit between 1.2 and 1.5  $\mu$ m in the +23.6 d spectrum of SN 2009dc is less pronounced compared to SNe 1999ee and 2002bo. This is reflected by the weaker postmaximum drop in the *J* band seen in the light curves (Fig. 5).

With its fairly smooth, blue continuum, the  $-5.4\,d$  spectrum of SN 2009dc resembles the  $-8\,d$  spectrum of SN 2002bo. At  $+7.5\,d$ , the difference to normal SNe Ia is most pronounced in the region around 1.5  $\mu$ m, where SN 2009dc shows only a hint of the strong

P-Cygni feature seen in other objects and normally attributed to Fegroup elements (Marion et al. 2009a). On day +23.6, SN 2009dc shows the typical blends of Co II lines in the K-band region, which all SNe Ia develop a few weeks after maximum light. Also the J-band region strongly resembles e.g. that of SN 2002bo on day +29. At the same time, however, the H-band region in SN 2009dc shows less structure than in ordinary SNe Ia.

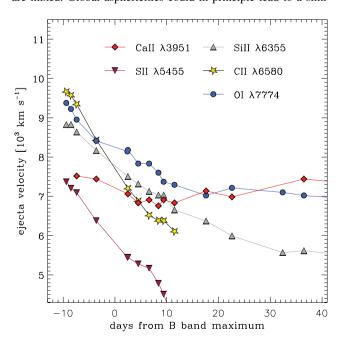
Interestingly, as a consequence of the decreasing velocities, the same region is resolved into a large number of individual, narrow lines by day +84.3, most of them attributed to Fe-group elements (Co II and Fe II, in particular). Probably the same lines dominated this region already at earlier epochs, but were so strongly blended that they mimicked a continuous emission. The *J*-band region of SN 2009dc on day +84.3 is characterized by the same features as that

of SN 2002bo on day +61 (Fe II and other Fe-group lines), but again all lines are narrower and better resolved. Only the Co II lines in the K-band region are still strongly blended. Accordingly, little evolution is seen in that region compared to the +23.6 d spectrum, except for a relative increase in the flux beyond  $2.3 \,\mu m$ . The latter might be caused by emission of the first overtone band of CO, as observed at similar epochs in some stripped-envelope CC-SNe (e.g. in SN 2007gr; Hunter et al. 2009, see Fig. 15). Given that SN 2009dc had similarly strong C and O features at early phases and comparably low ejecta velocities as SN 2007gr, molecule formation at comparable epochs in these two objects appears possible, although it has never been observed in ordinary SNe Ia even at much later phases (Bowers et al. 1997; Spyromilio et al. 2004).

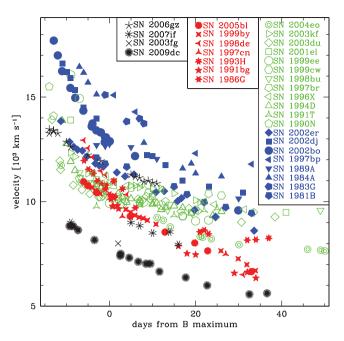
#### 4.3 Ejecta velocities

One of the most characteristic properties of SN 2009dc throughout its spectroscopic evolution is the low expansion velocity of the ejecta deduced from spectral lines. As shown in Fig. 16, even 10 d before maximum light the velocities do not exceed 10 000 km s<sup>-1</sup>, regardless of which element is considered. The highest velocities are measured in carbon and oxygen, in agreement with the idea that unburned material should predominantly be found in the outer layers. IMEs are at somewhat lower velocities: Si II  $\lambda 6355$  yields a velocity estimate of  $\sim 9000$  km s<sup>-1</sup>, whereas the S II blend with an effective wavelength of 5455 Å yields just 7500 km s<sup>-1</sup>. Given that the sulphur lines are intrinsically quite weak, they are often considered to be a better tracer of the photosphere than Si II  $\lambda 6355$ .

During the following 20–30 d, the measured line velocities generally decrease, levelling at  $\sim$ 7000 km s<sup>-1</sup> in the case of oxygen, and at  $\sim$ 5500 km s<sup>-1</sup> in the case of silicon. C II  $\lambda$ 6580 has a steeper velocity gradient than Si II  $\lambda$ 6355, and by the time the carbon features disappear (about two weeks after maximum) they form in deeper layers than Si II  $\lambda$ 6355. This suggests the presence of a zone at  $\sim$ 6000–9000 km s<sup>-1</sup> where IMEs and unburned material are mixed. Global asphericities could in principle lead to a simi-



**Figure 16.** Expansion velocities of Ca  $\scriptstyle\rm II$   $\lambda$ 3951, S  $\scriptstyle\rm II$   $\lambda$ 5455, Si  $\scriptstyle\rm II$   $\lambda$ 6355, C  $\scriptstyle\rm II$   $\lambda$ 6580 and O  $\scriptstyle\rm I$   $\lambda$ 7774, determined from the minima of P-Cygni absorption profiles.



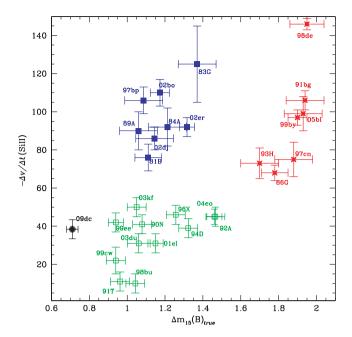
**Figure 17.** Si  $\pi$   $\lambda$ 6355 velocity evolution of SN 2009dc compared to that of other superluminous SNe Ia (SNe 2003fg, 2006gz and 2007if) as well as normal and subluminous SNe Ia. Open green symbols stand for LVG SNe, filled blue symbols for HVG SNe and red starred symbols correspond to the FAINT SNe, as defined by Benetti et al. (2005). Superluminous SNe Ia are shown as black symbols.

lar behaviour, but are disfavoured for the respective layers by the spectropolarimetry presented by Tanaka et al. (2010). S II  $\lambda5455$  always has the lowest velocities of all lines studied here, reaching 5000 km s $^{-1}$  already a week after maximum light. Thereafter, the identification of this feature is not certain; in fact the accelerated slow-down seen in Fig. 16 is an indication that blending with other lines becomes important at that epoch.

An exception to the trend of decreasing velocities is made by Ca  $\rm II$ . The Ca  $\rm II$  H&K lines are hardly detected in the earliest spectra, but then remain at a fairly constant velocity of  $7000-7500~\rm km~s^{-1}$  throughout the photospheric phase. In particular, no high-velocity features are seen in the Ca  $\rm II$  lines, which are otherwise ubiquitous in early spectra of SNe Ia (Mazzali et al. 2005). The constantly low velocity constrains the Ca  $\rm II$  abundance in the layers above  $\sim 8000~\rm km~s^{-1}$  to be very low, since already small amounts of Ca  $\rm II$  should be visible given the intrinsic strength of the H&K lines.

In Fig. 17, where the Si II  $\lambda 6355$  velocity evolution of a large number of SNe Ia is compared, the exceptional position of SN 2009dc is evident. At all times, SN 2009dc has significantly lower velocities than all other SNe Ia, including subluminous, 91bg-like events. Even most other superluminous SNe Ia (with the exception of SN 2003fg, for which only one epoch of spectroscopy is available) show significantly higher velocities than SN 2009dc, SN 2007if by  $\sim$ 2000 km s<sup>-1</sup> and SN 2006gz by  $\sim$ 4000 km s<sup>-1</sup>.

In a hierarchical cluster analysis, Benetti et al. (2005) arranged all SNe Ia in three groups (LVG, HVG and FAINT) based on their post-maximum velocity gradient and their  $\Delta m_{15}(B)$ . With a velocity gradient of  $\dot{v}=38\pm5~{\rm km\,s^{-1}}\,(100\,{\rm d})^{-1}$ , and  $\Delta m_{15}(B)=0.71\pm0.03$ , SN 2009dc extends the group of LVG SNe to smaller  $\Delta m_{15}(B)$  (Fig. 18). However, given the peculiarities of SN 2009dc, we hesitate to blindly assign it to the LVG group. Branch et al. (2006) proposed an alternative scheme, based on the EWs of Si II  $\lambda\lambda$ 6355 and 5972 at



**Figure 18.** Si II  $\lambda$ 6355 post-maximum velocity gradient  $\dot{v}$  versus  $\Delta m_{15}(B)$  (cf. Benetti et al. 2005 for a precise definition of  $\dot{v}$ ). Filled blue squares are HVG SNe, open green squares LVG SNe, and filled red stars FAINT SNe. The velocity gradient of SN 2009dc is comparable to those of LVG SNe.

maximum light. With 50–60 Å and 5–8 Å, respectively, SN 2009dc would end up in the shallow-silicon group, close to the boundary to core-normal SNe. However, again the overall spectrophotometric similarity of SN 2009dc to other members of this group (e.g. SN 1991T) is limited.

#### 5 DISCUSSION

#### 5.1 Explosion parameters

In order to estimate the most relevant explosion parameters of SN 2009dc, we have employed the analytic description of Arnett (1982). This model allows to derive the mass of  $^{56}\mathrm{Ni}$  produced in the explosion, the ejecta mass and the total explosion energy on the basis of the early-time bolometric luminosity evolution (cf. Section 3.2). The model makes the simplifying assumptions of spherical symmetry, homologously expanding ejecta, no mixing of  $^{56}\mathrm{Ni}$ , a constant mean optical opacity  $\kappa_{\mathrm{opt}}$ , radiation-pressure dominance, and the applicability of the diffusion approximation for photons, restricting its application to early phases when the ejecta are optically thick.

In the Arnett model, the peak of the bolometric light curve occurs when the radiative losses equal the energy release by radioactivity. Numerical simulations (Höflich & Khokhlov 1996) have shown that this equality holds at least approximately, and that the deviations to either side are typically not larger than 20 per cent in a broad set of models studied in detail. Lacking information on the nature of SN 2009dc, we make use of the original Arnett relation, but add in quadrature an additional 20 per cent to the error of the derived <sup>56</sup>Ni masses. The SN luminosity at peak is thus given by

$$L(t_{\text{max}}) = \varepsilon_{\text{Ni}} M_{\text{Ni}}(t_{\text{max}}) + \varepsilon_{\text{Co}} M_{\text{Co}}(t_{\text{max}}), \tag{1}$$

where  $\varepsilon_{\rm Ni/Co} = \frac{Q_{\rm Ni/Co}}{m_{\rm Ni/Co} \, \tau_{\rm Ni/Co}}$ .  $Q_{\rm Ni/Co}$  is the energy release per decay (1.73 and 3.57 MeV for  $^{56}{\rm Ni}$  and  $^{56}{\rm Co}$ , respectively, not taking into account the energy in neutrinos, for which the ejecta are optically thin).  $\tau_{\rm Ni/Co}$  is the decay time (8.77 d and 111.4 d, respectively) and

 $m_{\rm Ni/Co}$  the atomic mass of  $^{56}\rm Ni/^{56}\rm Co$ . For a given  $t_{\rm max}$ , the masses of  $^{56}\rm Ni$  and  $^{56}\rm Co$  at peak can be calculated from the initial  $^{56}\rm Ni$  mass  $(M_{\rm Ni}^0)$  through the decay chain  $^{56}\rm Ni \rightarrow ^{56}\rm Co \rightarrow ^{56}\rm Fe$  (assuming that  $M_{\rm Co}^0=0$ ).

A complication in the case of SN 2009dc is the unknown rise time. Since the explosion was different from a normal SN Ia, there is a priori no reason to believe that the rise time should be the same. A lower limit to the rise time is provided by a very early detection 21.2 d before maximum light in a pre-discovery image, as reported by Silverman et al. (2011), when the SN was about 3.5 mag below peak. The last non-detection down to a limiting magnitude of 19.3 dates to one week before this detection, i.e. 28 d before maximum light (Silverman et al. 2011). We have therefore carried out the calculations twice, once for a rise time of 22 d and once for a rise time of 28 d. With  $\log L(t_{\rm max}) = 43.47 \pm 0.11$  (erg s<sup>-1</sup>) and  $t_{\rm max}=22\,{\rm d}$ , a <sup>56</sup>Ni mass of  $M_{\rm Ni}^0=1.78\pm0.58\,{\rm M}_{\odot}$  is derived. For  $t_{\text{max}} = 28 \,\text{d}$ , a <sup>56</sup>Ni mass of  $M_{\text{Ni}}^0 = 2.21 \pm 0.75 \,\text{M}_{\odot}$  would be required to power the light curve. In both cases the quoted errors include uncertainties in the distance and reddening estimates, and a 20 per cent error intrinsic to the analytic model. These numbers are consistent with those obtained by Yamanaka et al. (2009) and Silverman et al. (2011) using Arnett's law and assuming a similar host reddening, i.e.  $M_{\text{Ni}}^0 = 1.8 \pm 0.5 \text{ M}_{\odot}$  [for  $E(B - V)_{\text{host}} =$ 0.14 mag and  $t_{\rm max}=20\,{\rm d}$ ] and 1.7  $\pm$  0.4  ${\rm M}_{\odot}$  [for  $E(B-V)_{\rm host}=$  $0.10 \,\mathrm{mag}$  and  $t_{\mathrm{max}} = 23 \,\mathrm{d}$ , respectively. Based on our calculation, the lowest <sup>56</sup>Ni mass for SN 2009dc, as derived for a short rise time, small distance, low reddening and a peak luminosity exceeding the instantaneous energy deposition by 20 per cent, is 1.20  $M_{\odot}$ . This is just below  $M_{Ch}$ , which may be important to reconcile SN 2009dc with thermonuclear explosion scenarios (see Section 5.3).

The Arnett (1982) description also allows to obtain estimates of the ejecta mass  $M_{\rm ej}$  of SN 2009dc, using the relation

$$\tau_{\rm m} = \left(\frac{2}{\beta c} \frac{\kappa_{\rm opt} M_{\rm ej}}{v_{\rm sc}}\right)^{1/2} \propto \kappa_{\rm opt}^{1/2} M_{\rm ej}^{3/4} E_{\rm kin}^{-1/4}.$$
 (2)

In this formula,  $\tau_{\rm m}$  is the effective photon diffusion time,  $v_{\rm sc}$  the velocity scale of the homologous expansion, and  $\beta$  an integration constant. We have calculated all quantities relative to SN 2003du [ $\Delta m_{15}(B)=1.02$ ], assuming that the mean optical opacity  $\kappa_{\rm opt}$  is approximately the same in these two SNe.<sup>6</sup> The ratio of the effective diffusion times in SNe 2009dc and 2003du has been estimated measuring the widths of the bolometric light-curve peaks [between points where  $L(t)={\rm e}^{-1}L(t_{\rm max})$ ], yielding  $\tau_{\rm m,09dc}\approx 1.65\,\tau_{\rm m,03du}$ . Similarly, the ratio of velocity scales has been estimated from the velocities measured in Si II  $\lambda$ 6355 at maximum light, yielding  $v_{\rm sc,09dc}\approx 0.75\,v_{\rm sc,03du}$ . With equation (2) we obtain  $M_{\rm ej,09dc}\approx 2.04\,M_{\rm ej,03du}=2.84\,M_{\odot}$  assuming that SN 2003du was a  $M_{\rm Ch}$ -explosion.  $E_{\rm kin}\propto M_{\rm ej}v_{\rm sc}^2$  then yields  $E_{\rm kin,09dc}\approx 1.15\,E_{\rm kin,03du}\approx 1.61$  for

These numbers confirm the conclusion of Yamanaka et al. (2009) and Silverman et al. (2011), i.e. that it is impossible to explain SN 2009dc by the explosion of a  $M_{\rm Ch}$ -WD. In fact, already the  $^{56}$ Ni mass – whose estimate is more robust than that of the total ejecta mass – probably exceeds 1.4 M $_{\odot}$ . A total ejecta mass of  $\sim$ 2.8 M $_{\odot}$  is furthermore an utmost challenge for all scenarios that invoke thermonuclear explosions of WDs. It is noteworthy that the total explosion energy is just  $\sim$ 15 per cent larger than in ordinary SNe

 $<sup>^6</sup>$  Given the large abundance of Fe-group material in SN 2009dc, the  $\kappa_{\rm opt}$  of a Type Ia SN appears to be a better match than that of a core-collapse SN, no matter what the nature of SN 2009dc actually is.

Ia. At the same time, the energy production through nuclear burning probably exceeds that in normal SNe Ia by at least a factor of 2. This indicates that whatever the progenitor is, it should have a high binding energy per unit mass unless we underestimate the amount of low-opacity material (and hence also the total ejecta mass).

Of course, there is the caveat that in the case of SN 2009dc Arnett's law might simply not be applicable, if some of the assumptions that enter into this model are not fulfilled. Strong deviations from spherical symmetry could for instance produce significant deviations from the Arnett model. However, the degree of asphericity is limited by the negligible continuum polarization found by Tanaka et al. (2010) in polarization spectra of SN 2009dc.

#### 5.2 Enhanced late-time decline

As shown in Sections 3 and 3.2, starting at 200–250 d after maximum the late-time light curves of SN 2009dc decline much more rapidly than before. This behaviour is most pronounced in the B and V filters (Fig. 4), which are characterized by forbidden Fe emission lines (Section 4.1). Since the B and V bands dominate the optical emission at late times, also the pseudo-bolometric light curve, constructed from B- to J-band data with estimated corrections for the U, H and K' contributions, reflects this trend (Fig. 7). The enhanced late-time fading of SN 2009dc was also noted by Silverman et al. (2011), who showed that an estimate based on their photometry taken 403 d after maximum would yield a  $^{56}$ Ni mass of only  $\sim$ 0.4  $M_{\odot}$ . In the following, we discuss possible explanations for this behaviour, although no final conclusion can be achieved with the available data.

First of all, it should be stressed that an increased luminosity decline after some point cannot be explained by other radioactive species starting to dominate over <sup>56</sup>Co. In order to dominate at *late* times, such a nucleus needs to have a longer half-life than <sup>56</sup>Co, which would result in a slow-down of the decline rather than an acceleration once it starts to dominate the energy deposition.

Depending on the perspective, the situation encountered in SN 2009dc can be interpreted in two ways: as a late-time flux deficit (at least in the optical regime) or as a flux excess during the first 200–250 d after the explosion. If interpreted as late-time deficit, there are again two scenarios: a decrease in the true bolometric luminosity, or a redistribution of flux into wavelength regions not covered by our observations.

A drop in the true bolometric luminosity would require a change in the energy deposition rate, caused by an increased  $\gamma$ -ray or positron escape fraction. While this happens in all SNe as the ejecta expand, it is normally a gradual process, and it may be doubted whether a situation can be constructed that leads to a rather sudden drop of the opacity after some point in time. The alternative is a redistribution of the emission into other wavelength regions, most likely the IR (Silverman et al. 2011). Since we have no constraints on the late-time IR luminosity of SN 2009dc beyond the J band, this is, however, a pure speculation. A flux redistribution into the IR could be achieved by an unexpectedly early IR catastrophe (Axelrod 1980), where Fe II recombines to Fe I which emits predominantly at IR wavelengths. Alternatively, dust may form within the ejecta, leading to an absorption of optical light and re-emission in form of a thermal continuum determined by the temperature of the dust grains. Dust formation has never been observed in SNe Ia so far. However, from the early spectra we have indications that the ejecta of SN 2009dc contained more carbon than those of other SNe Ia, which opens the possibility of graphite condensation once the ejecta have cooled down sufficiently. In fact, if the (highly uncertain) detection of CO emission in the +84.3 d NIR spectrum was correct, the additional cooling through molecular bands might create favourable conditions for dust formation at a later moment (Fassia et al. 2001). The scenario of an IR catastrophe, on the other hand, seems to suffer from more shortcomings. First of all, even in very late observations of SNe Ia, no IR catastrophe has ever been observed, although theoretical models predict it to occur between one and two years after the explosion (see e.g. Leloudas et al. 2009). An IR catastrophe requires low densities; the densities in the slowly expanding SN 2009dc after 200 d, however, are much higher than those in a two or three times older normal SN Ia.

Seen from a different perspective, it might well be that the reason for the strange light curve of SN 2009dc must not be searched for in its late-time, but rather in its early-time behaviour, in a sense that during the first 200-250 d there was some extra emission that stopped after that time. Such a flux excess could arise from ejecta-CSM interaction. This scenario would help to turn SN 2009dc into a more 'normal' object since much less <sup>56</sup>Ni would be required to power the light curve. Moreover, it would partially explain the low velocities by kinetic energy transfer to swept-up material, and – if the extra emission was in the form of an underlying continuum the fairly shallow spectral features at early epochs could be understood (Hamuy et al. 2003). What argues against this interaction scenario is the lack of direct interaction signatures such as highvelocity spectral features or narrow emission lines. At least if the CSM was hydrogen-rich, narrow H $\alpha$  emission should have shown up. On the other hand, a sufficiently massive, hydrogen-free CSM is not straightforward to obtain. Eventually, a lot of fine-tuning would be necessary for the interaction contribution to mimic the temporal evolution of a SN light curve, especially if the interaction is supposed to boost the SN luminosity by a factor of 2 or more (in the end, the colour evolution of SN 2009dc is not too different from that of a normal SN Ia, and the light-curve decline after the peak phase follows the slope of objects powered by <sup>56</sup>Co decay).

Whatever the truth behind the late-time light-curve dimming is, it was very likely also the reason for the highly peculiar late-time behaviour of SN 2006gz (Maeda et al. 2009). The mechanism may have worked more efficiently in SN 2006gz – a spectrum taken a year after maximum shows essentially no emission in the blue part, and a photometric recovery of the SN almost failed – but by extrapolation one may guess that SN 2009dc is on a good way to catch up.

# 5.3 Explosion models

The high luminosity of SN 2009dc, its low ejecta velocities, and the chemical composition of the ejecta with a lot of IMEs, C and O, but without any trace of H or He, pose a challenge to any explosion model one can think of, be it thermonuclear or core collapse. In particular, as demonstrated by Yamanaka et al. (2009) and Silverman et al. (2011) and as is evident from the derived explosion parameters (Section 5.1), in the absence of CSM interaction there is no way for SN 2009dc to be the explosion of a regular  $M_{\rm Ch}$ -WD. In what follows, we go through possible progenitors and explosion channels for SN 2009dc, some of them already scrutinized in the literature, others being new suggestions to widen the discussion. A successful model has to explain the large production of <sup>56</sup>Ni, the ejection of  $\geq 2.5 \text{ M}_{\odot}$  of material with low kinetic energy per mass, the presence of C and O in all layers down to 6000 km s<sup>-1</sup>, the absence of H and He and the peculiar evolution of the late-time SN luminosity. This discussion is based on SN 2009dc and the explosion parameters derived for it. However, given the similarities within the group of superluminous SNe Ia, most arguments are also valid for other members of this class.

#### 5.3.1 Rotating 'super-M<sub>Ch</sub>' white dwarfs

Rapidly rotating WDs were first suggested by Howell et al. (2006) as a progenitor for the superluminous SN Ia 2003fg. Indeed, as shown by Yoon & Langer (2005), differentially rotating WDs can be stabilized by centrifugal force and exceed the Chandrasekhar mass of non-rotating WDs by quite a margin. However this model faces some problems.

At least within the SD scenario, it is difficult for a WD to accrete all the material and gain all the angular momentum needed to grow to  $\geq$ 2 M $_{\odot}$ . CO WDs are typically born with masses of  $\sim$ 0.6 M $_{\odot}$ (Koester, Schulz & Weidemann 1979; Weidemann & Koester 1983; Liebert, Bergeron & Holberg 2005) and with slow rotation (e.g. Spruit 1998). Even if the WD was initially as massive as  $1 M_{\odot}$ , it would still have to accrete at least another solar mass of material, provided by the binary companion. This large mass requires the companion itself to be quite massive, but its mass is limited by the fact that its zero-age main-sequence (ZAMS) mass must have been lower than that of the primary, since it is less evolved. This narrows down the possible parameter space for primary and secondary significantly. In fact, Langer et al. (2000) estimated that no CO WD can grow much beyond 2 M<sub>☉</sub> by accretion from a non-degenerate companion, which is probably not enough to explain the ejecta mass of  $\sim$ 2.8 M $_{\odot}$  derived for SN 2009dc (Section 5.1).

Some of the problems concerning the accretion and spin-up could be avoided if the secondary was also a CO WD, disrupted in the course of a merger, with its material being accreted steadily on to the primary (Hicken et al. 2007). However, in the case of a merger of two massive WDs with a mass ratio close to one, a dynamical merger with a detonation triggered already during the act of merging (Pakmor et al. 2010) may be the more likely outcome. This scenario is discussed in the next section.

A problem of all rotating models, be it a single WD or the result of a WD merger, may be the kinetic energy of the ejecta. Synthesizing at least 1.2  $\rm M_{\odot}$  of  $^{56}\rm Ni$  plus some IMEs, SN 2009dc produced 50–100 per cent more energy than a normal SN Ia. If this energy is distributed to 2  $\rm M_{\odot}$  of ejecta, it will result in high ejecta velocities unless the specific binding energy is significantly larger than in a  $\rm \textit{M}_{Ch}$ -WD. Yoon & Langer (2005) indeed see an increase in the specific binding energy by a factor of  $\sim$ 1.7 when going from a nonrotating  $\rm \textit{M}_{Ch}$ -WD to a rotating WD with 2  $\rm \textit{M}_{\odot}$ . However, given that the binding energy is only a fraction of the total explosion energy, this does not affect the specific kinetic energy by too much. Accordingly, Pfannes, Niemeyer & Schmidt (2010) find that the ejecta velocities of a detonating 2.1- $\rm \textit{M}_{\odot}$  WD are very similar to those encountered in normal SNe Ia, and too high to be compatible with SN 2009dc.

Finally, rapidly rotating massive WDs are significantly deformed (Yoon & Langer 2005), and the oblate geometry of the WD would likely result in an aspherical SN explosion. However, spectropolarimetry suggests that SN 2009dc was overall spherical (Tanaka et al. 2010).

#### 5.3.2 Dynamical white-dwarf mergers

Pakmor et al. (2010) presented WD merger calculations in which a detonation was triggered dynamically in a hotspot during the process of merging. The computation was performed for the merger

of two  $0.9\text{-}\mathrm{M}_{\odot}$  WDs, which produced  $\sim 0.1~\mathrm{M}_{\odot}$  of  $^{56}\mathrm{Ni}$ . However, the prerequisite for a dynamical explosion is not only the absolute mass of the WDs, but also a mass ratio close to one (Pakmor et al. 2010). The central densities of WDs are a steep function of their mass. Hence, it may be expected that e.g. a pair of  $1.2\text{-}\mathrm{M}_{\odot}$  WDs produces much more  $^{56}\mathrm{Ni}$  during a dynamical merger, although it may not be sufficient for SN 2009dc. The total ejecta mass of such an event would be  $2.4~\mathrm{M}_{\odot}$ , which is at least closer to the value deduced for SN 2009dc than rotating models can probably get. Of course, CO WDs with  $\geq 1.2~\mathrm{M}_{\odot}$  are rare (e.g. Liebert et al. 2005) and so are binary systems of them, but since the rate of superluminous SNe Ia is low (and not well known) this would per se not exclude this scenario.

Beyond 1.2 Mo, essentially all WDs which have not grown through accretion or mergers are ONe rather than CO WDs (Koester et al. 1979; Weidemann & Koester 1983). From the detection of carbon in the early spectra, one can conclude that SN 2009dc cannot have been a merger of two ONe WDs, but a merger of an ONe WD and a similarly massive CO WD could be feasible. Because of its higher mean atomic mass, an ONe WD releases less energy when burned to <sup>56</sup>Ni than a CO WD, which could help in keeping the ejecta velocities low. A problem might be the susceptibility of ONe WDs to electron captures on <sup>20</sup>Ne and <sup>24</sup>Mg. In fact, numerical simulations have shown that ONe WDs do not explode, but collapse to a neutron star when approaching  $M_{\rm Ch}$  (Miyaji et al. 1980; Saio & Nomoto 1985). This, of course, does not have to be true for a dynamical merger, where the detonation triggered by an 'external event' and propagating supersonically might leave the ONe WD no time to collapse.

#### 5.3.3 Core collapse in an envelope-stripped massive star

Explaining SN 2009dc as a core-collapse explosion of a stripped star has the obvious advantage that no strict limits on the ejecta mass apply. Core-collapse events whose ejecta exceed  $M_{\rm Ch}$  are common. Unfortunately, other hallmarks of core-collapse explosions are not met by SN 2009dc. Typical core-collapse SNe produce of the order of 0.1 M<sub> $\odot$ </sub> of <sup>56</sup>Ni, and this number goes up to ~0.5 M<sub> $\odot$ </sub> for some  $\gamma$ -ray burst related hypernovae like SNe 1998bw (Galama et al. 1998; Maeda et al. 2006) or 2003dh (Hjorth et al. 2003) which contrary to SN 2009dc - are characterized by a very large kinetic energy and high ejecta velocities. Beyond this, Umeda & Nomoto (2008) recently constructed a series of core-collapse models from very massive (20–100 M<sub>☉</sub>) progenitors, assuming little fall-back of synthesized <sup>56</sup>Ni on to the newly formed black hole. They found ejected  $^{56}$ Ni masses up to several  $M_{\odot}$  (see also Moriya et al. 2010). However, given the very large total ejecta masses, the composition of these objects – as of all core-collapse SNe – cannot be considered Ni-rich. SN 2009dc is different in this respect, with probably more than half of its ejecta being made up of <sup>56</sup>Ni. More generally, the overall abundance pattern as suggested by the spectral time series of SN 2009dc is not typical of core-collapse SNe. SN 2009dc is characterized by prominent IME lines, most notably those of Si II and S II, which are weak (Si II  $\lambda 6355$ , see e.g. Branch et al. 2006) or absent (S II lines) in stripped-envelope core-collapse SNe. The latter events, on the other hand, always eject a large amount of oxygen, giving rise to a prominent [O I]  $\lambda\lambda6300$ , 6364 emission in the nebular phase. SN 2009dc does show O<sub>I</sub> lines in early-time spectra, but no hint of  $[O I] \lambda\lambda6300$ , 6364 at late times, contrary to all objects with an undisputed classification as stripped-envelope core-collapse SNe known to date. This indicates a lack of mixing of O and <sup>56</sup>Ni, which is difficult to achieve in core-collapse explosions.

#### 5.3.4 Core collapse with activity of the central remnant

Within the core-collapse scenario, a possible way to reduce the mass of <sup>56</sup>Ni needed to power the light curve of SN 2009dc could be heating from an active compact remnant. Indeed, the birth of a magnetar was proposed by Maeda et al. (2007) to explain the unusual light-curve evolution of the Type Ib SN 2005bf, characterized by a broad, delayed peak and a deep luminosity drop thereafter. An energy source different from radioactivity allows more freedom in the light-curve shape, as an exponential tail is not a necessary consequence. Accordingly, within such a scenario the late-time luminosity drop seen in SN 2009dc could be explained by the termination of the heating from the central object. Compared to CSM interaction as an alternative non-radioactivity-related energy source, heating from a compact remnant has the advantage that the energy is injected at the centre and released on photon diffusion time-scales, which allows the light curve to rise smoothly to peak (Maeda et al. 2007). Moreover, since the photons propagate through the entire ejecta, the normal processes of spectrum formation take place, resulting in a fairly normal SN spectrum (as was the case for SN 2005bf; Tominaga et al. 2005; Folatelli et al. 2006). Narrow emission lines are not expected.

What remains a problem, however, is the SN Ia-like abundance pattern derived from the spectra of SN 2009dc, as detailed above. SN 2005bf was spectroscopically undoubtedly a stripped-envelope core-collapse SN, and showed the hallmark [O I] and [Ca II], but only weak Fe emission lines in its nebular spectra. All of this is not the case for SN 2009dc.

# 5.3.5 Type $I_{\frac{1}{2}}$ SNe: thermonuclear explosions of AGB-star cores

Developed back in the 1970s (Ergma & Paczyński 1974; Couch & Arnett 1975; Iben 1982, but see Iben & Renzini 1983), the idea of exploding asymptotic giant branch (AGB) star cores has not found much resonance during the past two decades. While stars with ZAMS masses between  $\sim$ 8 and 10 M $_{\odot}$  are predicted to form ONeMg cores and possibly undergo electron-capture core collapse, those between 0.5 and 8 M<sub>☉</sub> end up with degenerate CO cores after core He burning. The subsequent He shell burning or AGB phase is characterized by strong mass loss, and is usually terminated by the ejection of the envelope as planetary nebula and the formation of a CO WD that cools by radiative processes. However, in the most massive AGB stars the degenerate CO core might grow to 1.4 M<sub>☉</sub> before mass-loss processes can reduce the total mass of the star below that value. In this case, carbon would be ignited in the core and a thermonuclear runaway would drive a flame through the entire star and disrupt it. Iben & Renzini (1983) proposed the term 'Type  $I_{\frac{1}{2}}$  SN' for such an explosion, based on its thermonuclear origin but the likely presence of H lines in the spectrum.

To make Type  $I_2^1$  SNe a suitable model for SN 2009dc, several conditions have to be fulfilled. At the time of explosion, the AGB star needs to have a total mass between 2.5 and 3  $M_{\odot}$ , which is probably feasible. It must have lost its H envelope through stellar winds or binary interaction to prevent H lines, most notably  $H\alpha$ , from appearing in the SN spectra. The mass of the degenerate CO core (i.e.  $1.4 M_{\odot}$ ) is an upper limit for the amount of  $^{56}$ Ni that can be produced in such an explosion, but if the core is burned entirely to Fe-group material this might still be consistent with SN 2009dc within the large uncertainties (Section 5.1). Such a complete burning of the core is only possible if the thermonuclear flame propagates as a detonation, and not as a deflagration that gives the star time to pre-expand. The He envelope would then have to be burned to carbon,

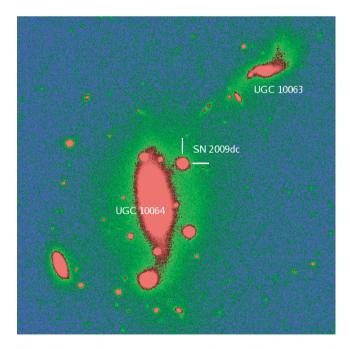
oxygen and IMEs, in order to match the abundance pattern observed in the ejecta of SN 2009dc. This could be problematic, since too much energy might be released by the He burning to be consistent with the low ejecta velocities. If, on the other hand, a part of the He is left unburned, it might show up in the spectra, in particular in the NIR. If such Type  $I_2^{\frac{1}{2}}$  SNe exist, they are probably rare, but small rates are not a problem as long as only superluminous SNe Ia shall be explained. In the end, detailed numerical simulations of hydrodynamics and radiative transfer are required to assess the feasibility of this model.

#### 5.4 The host galaxy of SN 2009dc

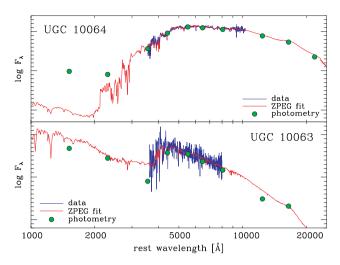
As mentioned in Section 2.1, SN 2009dc is located in the outskirts of the S0 galaxy UGC 10064. Although lenticular galaxies are by no means dead stellar systems (e.g. Emsellem et al. 2007; Kawabata et al. 2010), such a host galaxy might still be considered as an indication for a predominantly old stellar population. This is consistent with the lack of H II-region emission lines in the spectra of SN 2009dc, suggesting no strong star formation activity at the SN location.

However, UGC 10064 is not an isolated, unperturbed system. At the same redshift, about 98.1 arcsec to its north-west (corresponding to a projected distance of 44.6 kpc), there is the irregularly shaped, strongly distorted galaxy UGC 10063. Almost an order of magnitude less luminous than UGC 10064, UGC 10063 is characterized by a distinctly blue colour, indicative of luminous, young stars. It shows a tidal tail bridging the gap to its larger neighbour, and, as already mentioned by Silverman et al. (2011), SN 2009dc is located at the approximate endpoint of this tail (see Fig. 19).

Coincident to our observations of SN 2009dc, we obtained deep photometry of UGC 10064 and UGC 10063 of the NOT on 2009 August 12, spectroscopy of UGC 10064 with DOLORES at the TNG on 2009 July 4, and spectroscopy of UGC 10063 with CAFOS at the Calar Alto 2.2-m on 2009 May 4. In addition to our own optical



**Figure 19.** Stacked, contrast-enhanced r-band image of the environment of SN 2009dc. The two potential host galaxies are labelled, and the tidal bridge between them can be discerned. The field of view is  $3 \times 3$  arcmin<sup>2</sup>, north is up and east to the left.



**Figure 20.** Optical spectra of UGC 10064 (upper panel) and UGC 10063 (lower panel). The fluxes derived from UV (*GALEX*), optical (NOT) and NIR (2MASS) photometry, and the best-fitting zpeg template spectra are overplotted. Compared to the template, an UV excess in UGC 10064 is evident.

photometry, UV photometry from *GALEX* (Morrissey et al. 2007) and NIR photometry from the Two Micron All-Sky Survey (2MASS; Skrutskie et al. 2006) were available. We used SEXTRACTOR (Bertin & Arnouts 1996) in common aperture mode, using the *B* band to define the apertures, to derive magnitudes from all imaging data. We then used ZPEG (Le Borgne & Rocca-Volmerange 2002) to match our photometry to galaxy evolutionary scenarios. Using the standard set of nine evolutionary scenarios included with this code and the internal prescriptions for treating extinction by dust, we match the photometry of UGC 10064 to a galaxy with a mass  $\log(M_*/\mathrm{M}_{\odot}) = 10.68^{+0.07}_{-0.06}$  that underwent a starburst 4 Gyr ago. The photometry of UGC 10063 matches an Sd galaxy of mass  $\log(M_*/\mathrm{M}_{\odot}) = 9.52^{+0.01}_{-0.08}$ . Our spectra, the fluxes inferred from our photometry, and the best-fitting ZPEG template for each galaxy are shown in Fig. 20.

Interestingly, there appears to be an excess of UV flux for UGC 10064 compared to the best-fitting zpeg template, that of a starburst of 4.0-Gyr age. Inspection of the *GALEX* images indeed shows a visible UV flux concentrated at the core of UGC 10064. Using the methods described by Childress et al. (2010), we measure the emission-line fluxes of UGC 10064 by subtracting a best-fitting stellar template. Though weak emission lines are detected, their flux ratios indicate ionization by an active galactic nucleus according to the BPT (Baldwin, Phillips & Terlevich 1981) diagram boundaries defined by Kewley et al. (2006). This indicates that the UV excess and weak-emission-line flux in UGC 10064 are likely to be caused by an active nucleus, and that no significant star formation has occurred in the galaxy for at least several Gyr. Thus, if SN 2009dc was born from the stellar population of UGC 10064, it is likely to have a long delay time.

In contrast to the old stellar population of UGC 10064 is the much younger population of UGC 10063. The best-fitting ZPEG template is that of an Sd galaxy whose luminosity-weighted stellar age is 1.5 Gyr. The spectrum of UGC 10063 shows no emission from recent star formation, and is dominated by strong Balmer absorption features indicating the galaxy to be in a post-starburst phase (as was also noted by Silverman et al. 2011). This implies that UGC 10063 underwent a strong burst of star formation a few hundred Myr before the explosion of SN 2009dc, perhaps induced by a close encounter

with UGC 10064. Intriguingly, this is a time-scale similar to that reported by Childress et al. (2010) for the parent population of SN 2007if, and could be indicative of a similar time-scale for the explosion of SN 2009dc.

A more in-depth study of the stellar population at the SN site has to be postponed to a moment when the SN will have faded below detectability. For the time being, it is not possible to decide if the SN descended from an old, low-mass stellar population as expected for its S0 host, or from the significantly younger population that dominates the tidal tail of the companion galaxy.

#### 5.5 Host galaxies of superluminous SNe Ia

The question of host galaxies and parent populations is crucial for narrowing down the range of possible explosion scenarios for superluminous SNe Ia. In particular, it might help discriminating between a thermonuclear or core-collapse origin, since the stellar populations involved are significantly different. To date, at least seven SNe Ia are known to be superluminous in the sense that their  $^{56}$ Ni yields are incompatible with the explosions of  $M_{\rm Ch}$  WDs. These SNe do not form a homogeneous group: differences in their early (ionization state, line velocities) and late spectra (linewidths, strength of Fe lines; Taubenberger et al., in preparation) are evident. Their hosts also exhibit some heterogeneity, but we will show below that the ensemble of superluminous SN Ia hosts have on average lower masses, and presumably lower metallicities, than those of full samples of SNe Ia from untargeted surveys. In Table 7, some basic properties of the host galaxies of superluminous SNe Ia are summarized

We derived the host masses by collecting previously published host masses where available, and by applying the code ZPEG to multiband photometry of the other hosts, available from public sources [Sloan Digital Sky Survey (SDSS), GALEX, 2MASS] or our own observations. Previously published masses for host galaxies of superluminous SNe Ia include that of the host of SN 2003fg at  $\log(M_*/\mathrm{M}_{\odot}) = 8.93^{+0.81}_{-0.50}$  (Howell et al. 2006) and that of the host of SN 2007if at  $\log (M_*/M_{\odot}) = 7.30 \pm 0.31$  (Childress et al. 2010). For FGC 175A, the host of SN 2004gu (Contreras et al. 2010), optical ugriz photometry was obtained from SDSS DR7 (Abazajian et al. 2009), UV data from GALEX and JHK photometry from 2MASS. Archival BVR photometry from Subaru was available for IC 1277 (Maeda et al. 2009), the host of SN 2006gz, along with 2MASS data. We used our own optical VLT + FORS2 BVRI photometry for the host of SNF20080723-012 to derive its mass. Our own NOT images of 2009 August 12 provided UBVRI photometry of both UGC 10064 and UGC 10063, while GALEX UV and 2MASS IR were also available. Optical ugriz photometry from SDSS is available at the site of SN 2009dr (Quimby et al. 2009), but the host is not detected.

We used SExtractor in common aperture mode, using either the g band or B band to define the apertures, to derive magnitudes from all imaging data. We then used zpeg to derive host masses from our photometry, finding  $\log(M_*/\mathrm{M}_\odot) = 10.45^{+0.04}_{-0.20}$  for FGC 175A,  $\log(M_*/\mathrm{M}_\odot) = 10.28^{+0.01}_{-0.14}$  for IC 1277,  $\log(M_*/\mathrm{M}_\odot) = 8.52^{+0.04}_{-0.07}$  for the host of SNF20080723-012,  $\log(M_*/\mathrm{M}_\odot) = 10.68^{+0.06}_{-0.06}$  for UGC 10064 and  $\log(M_*/\mathrm{M}_\odot) = 9.52^{+0.01}_{-0.08}$  for UGC 10063. The host of SN 2009dr is undetected in SDSS data, so using the  $3\sigma$  SDSS g-band limiting magnitude of  $m_g \approx 22.6$  (Stoughton et al. 2002) at the redshift of this object ( $z \approx 0.10$ ; Quimby et al. 2009) we estimate that the host must be fainter than  $M_g \approx -15.6$ . With a (conservatively large) solar mass-to-light ratio from Blanton et al. (2003), this places an upper mass limit for its host at  $\log(M_*/\mathrm{M}_\odot) \lesssim 8.3$ .

**Table 7.** Properties of the host galaxies of superluminous SNe Ia.

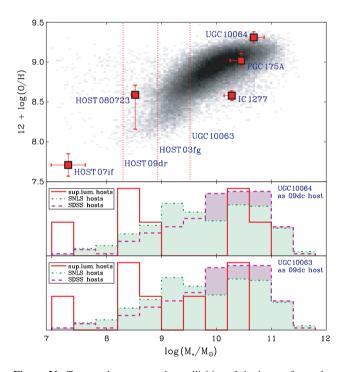
SN	SN $\Delta m_{15}(B)$	Survey <sup>a</sup>	Host galaxy	Morphology <sup>b</sup>	Redshift	Host $M_{B/g}^c$	Host $\log (M*/M_{\odot})$
SN 2003fg	$0.84 \pm 0.15$	SNLS	anonymous	Irr	0.244	?	$8.93^{+0.81}_{-0.50}$ d
SN 2004gu	$0.80 \pm 0.04$	Texas	FGC 175A	spiral	0.046	-18.9	$10.45^{+0.04}_{-0.20}$
SN 2006gz	$0.69 \pm 0.04$	Puckett/LOSS	IC 1277	Scd	0.024	-21.0	$10.28^{+0.01}_{-0.14}$
SN 2007if	$0.71 \pm 0.06$	ROTSE/SNF	anonymous	?	0.074	-14.1	$7.30^{+0.31}_{-0.31}e$
SNF20080723-012	?	SNF	anonymous	spiral	0.075	-17.1	$8.52^{+0.04}_{-0.07}$
SN 2009dc	$0.71 \pm 0.03$	Puckett	UGC 10064	S0	0.021	-20.3	$10.68^{+0.07}_{-0.06}$
			UGC 10063	SBd	0.021	-18.8	$9.52^{+0.01}_{-0.08}$
SN 2009dr	?	PTF	anonymous	?	~0.1	≥-15.6	_0.06 ≤8.3

<sup>a</sup>SNLS = Supernova Legacy Survey, Texas = Texas Supernova Search, Puckett = Puckett Supernova Search, LOSS = Lick Observatory Supernova Search, ROTSE = ROTSE Supernova Verification Project, SNF = Nearby Supernova Factory, PTF = Palomar Transient Factory. <sup>b</sup>From LEDA, NED, <sup>c</sup>From LEDA, NED and own measurements in archival images, <sup>d</sup>Howell et al. (2006), <sup>e</sup>Childress et al. (2010).

The mass—metallicity (MZ) relation (Tremonti et al. 2004) supports the interpretation of this result as a prevalence of low-metallicity environments for the preferred birthplace of superluminous SNe Ia. To confirm this interpretation, we collected spectroscopic data for the hosts of SN 2004gu, SN 2006gz, SNF20080723-012 and SN 2009dc. Note that contrary to the case of SN 2007if (Childress et al. 2010), whose host was a dwarf galaxy and therefore chemically well mixed, a metallicity gradient is expected for these more massive galaxies. The derived core metallicities are hence upper limits for the actual metallicities in the immediate SN environments.

The emission-line fluxes from the SDSS spectrum of the host of SN 2004gu were derived by Tremonti et al. (2004), while we measured emission-line fluxes for the host of SN 2006gz from an archival Subaru + FOCAS spectrum (Maeda et al. 2009), and for the host of SNF20080723-012 from our own nebular-phase observations of the SN using FORS2 on the VLT. We then employed the O3N2 method of Pettini & Pagel (2004) to derive gas-phase oxygen abundances of  $12 + \log (O/H)_{04gu,PP04} = 8.74 \pm 0.05$ ,  $12 + \log (O/H)_{06gz,PP04} = 8.35 \pm 0.03$  and  $12 + \log (O/H)_{SNF,PP04} =$  $8.36 \pm 0.15$ . We note that the error bar for the metallicity of the host of SNF20080723-012 is likely underestimated, as contamination from the nebular SN prevents fitting of the stellar continuum to obtain absorption corrections for Balmer-line fluxes. Using the conversion formulae of Kewley & Ellison (2008), we converted these metallicity values to the scale of Tremonti et al. (2004) to place them on a common scale with the fiducial MZ relation, and compared these to the solar oxygen abundance of Delahaye et al. (2010). This yields final metallicities of  $\log{(Z/Z_{\odot})_{04gu}} = 0.16 \pm 0.05$ ,  $\log{(Z/Z_{\odot})_{06gz}} = -0.28 \pm 0.04$  and  $\log{(Z/Z_{\odot})_{SNF}} = -0.27 \pm$ 0.15. The metallicity of the host of SN 2007if was determined in precisely the same manner by Childress et al. (2010), who found  $\log{(Z/Z_{\odot})_{07if}} = -1.15 \pm 0.14$ . The metallicity of UGC 10064 was previously measured by Wegner & Grogin (2008) using stellar absorption features. They found log (Z/Z $_{\odot}$ )<sub>UGC 10064</sub> = 0.45  $\pm$ 0.07. Though systematic discrepancies between galaxy metallicities measured from stellar features and those from nebular emission are known, this metallicity for UGC 10064 is consistent with its host mass and the MZ relation.

In Fig. 21 (top panel) we compare the derived masses and metallicities of the hosts of superluminous SNe Ia with those of SDSS galaxies. For the hosts of SNe 2003fg and 2009dr, as well as for UGC 10063, no metallicities could be determined, so that these galaxies are included as vertical lines; for the SN 2009dr host the upper mass limit is shown. There seems to be a tendency of the hosts of superluminous SNe Ia to have on average lower masses than the



**Figure 21.** Top panel: masses and metallicities of the hosts of superluminous SNe Ia, compared to SDSS galaxies. Whenever no spectroscopic metallicity was available, a vertical line was drawn. The mass reported for the SN 2009dr host is an upper limit, following the non-detection in SDSS images. Middle and bottom panels: binned mass distribution of superluminous SN Ia hosts, compared to 162 SN Ia hosts from SDSS and 231 SN Ia hosts from SNLS. In the middle panel UGC 10064 is considered to be the host of SN 2009dc, in the lower panel UGC 10063. The distributions are scaled by arbitrary amounts to enable a comparison by eye.

SDSS galaxies. This trend also holds in the histograms in the lower two panels, where the host-mass distribution of superluminous SNe Ia is compared to those of SNe Ia from the non-targeted SDSS and SNLS (Sullivan et al. 2010) surveys. In the middle panel, UGC 10064 has been assumed to be the host of SN 2009dc, in the bottom panel UGC 10063.

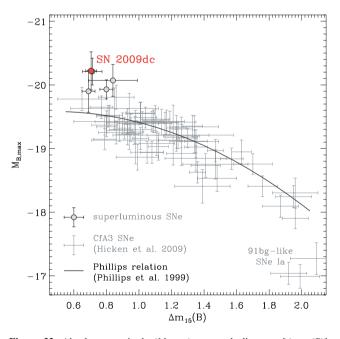
The host-mass distribution of superluminous SNe Ia has a mean and dispersion of  $\log{(M_*/{\rm M}_\odot)} = 9.2 \pm 1.3$  or  $\log{(M_*/{\rm M}_\odot)} = 9.0 \pm 1.1$ , depending on whether UGC 10064 or UGC 10063 is considered as the host of SN 2009dc. These numbers are conspicuously lower than the  $\log{(M_*/{\rm M}_\odot)} = 9.8 \pm 1.0$  and  $\log{(M_*/{\rm M}_\odot)} = 10.0 \pm 0.9$  obtained for all SNLS and SDSS SN Ia hosts, respectively.

To verify whether the observed distributions differ to a statistically significant degree, we ran a Kolmogorov-Smirnov test, using the SDSS and SNLS host-mass distributions as a reference, and assuming in our null hypothesis that the hosts of superluminous SNe Ia have been drawn from the same distributions. At a customary significance level of  $\alpha = 0.05$ , this null hypothesis is not rejected for both reference distributions. If, however, the significance is relaxed to  $\alpha = 0.10$ , the null hypothesis is rejected for the SDSS reference distribution (but not yet for the SNLS reference distribution). This outcome is independent of which galaxy is adopted as the host of SN 2009dc, since it is driven by the high frequency of low-mass dwarf galaxies among the hosts of superluminous SNe Ia. Of course, this is all low-number (n = 7) statistics, and one should note that the addition of a single event might change the result considerably. Nevertheless, we tentatively claim weak evidence for an excess of low-mass galaxies as hosts of superluminous SNe Ia.

#### 5.6 Concerns for cosmology

The group of superluminous SNe Ia deserves particular attention for their potential role as troublemakers in SN cosmology. Spectroscopically fairly similar to ordinary SNe Ia (of the core-normal or shallow-silicon variety; Branch et al. 2006), these objects will be identified as SNe Ia in surveys, especially at high *z* where the S/N of spectra is usually poor.

However, superluminous SNe Ia are no good standardizable candles. This is demonstrated in Fig. 22, where SN 2009dc is plotted in an absolute-magnitude versus decline-rate diagram. It is clearly brighter than all other SNe Ia (from the CfA3 data set; Hicken et al. 2009), and also  $\sim$ 0.65 mag brighter than anticipated by the Phillips et al. (1999) relation for its  $\Delta m_{15}(B)$  of 0.69.



**Figure 22.** Absolute-magnitude  $(M_{B,\max})$  versus decline-rate  $[\Delta m_{15}(B)]$  diagram for SN 2009dc, other superluminous SNe Ia and a subsample of the CfA3 SNe Ia (Hicken et al. 2009). SN 2009dc is clearly more luminous than normal SNe Ia with similar decline rates, and a factor  $\sim$ 1.8 more luminous than predicted by the Phillips et al. (1999) relation for the given  $\Delta m_{15}(B)$ . In this context, the Phillips relation is representative for all calibration methods used in present-day surveys; the basic result should not be sensitive to which light-curve fitter is actually employed.

It is hence likely that in high-z SN surveys, SN 2009dc would be regarded as less luminous than it actually is, and that too small a distance would be inferred. At the same time, if the redshift was to be determined from a cross-correlation with other SN Ia spectra, it would probably be slightly overestimated due to the lower expansion velocities. In sum, these effects would move SN 2009dc towards the lower right in a Hubble diagram where the distance is plotted as a function of redshift.

Having a small number of outliers in the Hubble diagram is by itself not sufficient to really affect SN cosmology. Instead, an evolution of the average SN Ia properties with look-back time would be required. However, such an evolutionary effect could exactly be generated by superluminous SNe Ia. First of all, while apparently rare in the local Universe, their tentative tendency to be affiliated with low-metallicity dwarf galaxies (cf. Section 5.5) might suggest an intrinsically larger abundance at high z. Even more importantly, a Malmquist bias is expected, making it more likely for cosmological SN Ia data sets to contain superluminous SNe Ia at the highest redshifts, where they are favoured by their sheer luminosity. Systematic errors in the reconstruction of H(z) using SN Ia data may thus be introduced by superluminous SNe Ia unless they are recognized and treated correctly.

#### 6 CONCLUSIONS

Optical and NIR observations of SN 2009dc have revealed an overall similarity with SNe Ia in light-curve shape and spectral evolution, but also highlighted a number of important differences. Most evidently, SN 2009dc is by a factor of >2 more luminous than ordinary SNe Ia over the first  $\sim$ 200 d after the explosion ( $M_{V,\text{max}}$  =  $-20.07 \pm 0.23$ ,  $\log L_{\rm peak} = 43.47 \pm 0.11$ ), and is characterized by a slow decline from the light-curve peak  $[\Delta m_{15}(B)_{\text{true}} = 0.71 \pm$ 0.03]. The *IJHK'* bands show secondary maxima, delayed by  $\sim$ 25 d with respect to the peak in B. The minima between the first and secondary maxima, however, are not very pronounced. The spectra of SN 2009dc are characterized by a blue pseudo-continuum with lines of IMEs, carbon and oxygen early on, but dominated by Fegroup material at later phases, when the photosphere recedes into <sup>56</sup>Ni-rich zones. In particular, the nebular spectra show mostly [Fe II] emission, indicative of a low level of ionization. At early epochs most spectral lines are relatively shallow, and the ionization is typical of normal to bright SNe Ia. The ejecta velocities are  $\sim$ 30 per cent lower than in typical LVG SNe Ia.

A curiosity of SN 2009dc is an enhanced fading of its optical light curves after  $\sim\!200\,d$ , at a phase when the decline in normal SNe Ia slows down. Lacking IR information, we cannot verify whether this results from a redistribution of radiation into the IR regime (through dust formation or an IR catastrophe). Nevertheless, we are inclined to believe this, since the only alternative seems to be CSM interaction that contributes to the earlier light curve and suddenly ends at  $\sim\!200\,d-a$  scenario that generates more problems than it solves (see below). The late-time behaviour of SN 2009dc reminds of what was observed in SN 2006gz, and we speculate that both SNe shared the same fate.

Using the analytic light-curve model of Arnett (1982), the <sup>56</sup>Ni mass synthesized in the explosion was estimated. The biggest uncertainty in this exercise is the unknown rise time. For the minimum possible rise time of 22 d we obtained  $M_{\rm Ni}^0=1.78\pm0.58~{\rm M}_{\odot}$ , for a rise time of 28 d  $M_{\rm Ni}^0=2.21\pm0.75~{\rm M}_{\odot}$ . Using the velocity information from spectra, the model also allowed us to estimate a total ejected mass of ~2.8  ${\rm M}_{\odot}$ , and a kinetic energy of ~1.6 foe.

These numbers confirm that – in the absence of CSM interaction – the progenitor of SN 2009dc cannot have been a  $M_{\text{Ch}}$ -WD.

Finding an explosion scenario that explains SN 2009dc with all its peculiarities turns out to be difficult. For all models based on WDs, an ejecta mass of  $2.8 \, \mathrm{M}_{\odot}$  is either the very limit of what could potentially be achieved (for a merger of two  $M_{\mathrm{Ch}}$ -WDs) or already beyond (for a super- $M_{\mathrm{Ch}}$  WD grown by accretion from a non-degenerate companion). Thermonuclear explosions in hydrogen-stripped stellar cores (Type  $\mathrm{I}_{2}^{1}$  SNe) might be an alternative, but detailed numerical calculations which show whether this model may work have not yet been performed. In particular, it is unclear whether H- and He-free SNe can be achieved in this way, and whether the ejecta velocities would match the observations. Core collapse of an envelope-stripped progenitor, finally, might be another option. Large ejecta masses are easy to achieve in this way, but the  $^{56}\mathrm{Ni}$ -and IME-rich composition of the SN 2009dc ejecta and the lack of nebular [O 1]  $\lambda\lambda6300$ , 6364 emission disfavour this scenario.

A completely different approach is to assume that SN 2009dc was a relatively normal (probably thermonuclear) explosion, and that the observed peculiarities arise from interaction with a dense CSM. Such a scenario might explain both the high luminosity and the low ejecta velocities by conversion of kinetic energy into radiation, and the light-curve fading after  $\sim 200\,\mathrm{d}$  by the end of the CSM interaction. However, we have argued that it would require a lot of fine-tuning to have a temporal evolution of the interaction strength that mimics a radioactivity-driven light curve over more than half a year. Moreover, an interaction strong enough to boost the SN luminosity by a factor of 2 or more should leave a direct spectroscopic imprint in the form of narrow emission lines (which are not observed). At least a H-rich CSM can thus be excluded.

Whatever mechanism produces objects like SN 2009dc, it should be consistent with the finding that these events show a tendency to explode in low-mass hosts (and probably low-metallicity environments). While this trend for the entire group is fairly robust, little can be said about the stellar population giving rise to SN 2009dc in particular, since it is not clear whether the SN 'belongs' to the outskirts of an SO galaxy (UGC 10064) or to a tidal tail from an interacting less luminous, blue companion (UGC 10063).

A final warning is addressed to the high-z SN Ia surveys. Superluminous SNe Ia deviate systematically from the light-curve width versus luminosity relations used to standardize SNe Ia for cosmological distance determination. For this reason, care should be taken to exclude superluminous SNe from the cosmological SN Ia data sets, which could be achieved e.g. by disregarding SNe with  $\Delta m_{15}(B) \leq 0.9$  (Fig. 22). This is even more important as their high intrinsic luminosity and their association with (probably metal-poor) low-mass host galaxies should result in a bias that favours their detection at high redshift. If not accounted for, this could lead to systematic errors in the reconstruction of the expansion history of the Universe.

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#### APPENDIX A: TABLE OF S- AND K-CORRECTIONS

Table A1. S- and K-correction added to the zero-point corrected SN magnitudes (instead of colour-term corrections).

Epoch <sup>a</sup>	$S_U$	$S_B$	$S_V$	$S_R$	$S_I$	$K_U$	$K_B$	$K_V$	$K_R$	$K_I$	Tel.b
-8.5	0.001	0.003	-0.012	0.009	-0.004	-0.021	0.019	0.026	0.048	0.057	NOT
-7.5	0.002	0.004	-0.012	0.011	-0.005	-0.023	0.019	0.026	0.050	0.056	NOT
-4.6	0.178	-0.002	-0.011	0.021	-0.006	-0.016	0.019	0.027	0.054	0.052	LT
-3.7	-0.009	0.006	-0.010	0.017	-0.010	-0.014	0.019	0.028	0.056	0.050	NOT
-2.6	0.171	-0.001	-0.010	0.023	-0.008	-0.020	0.017	0.027	0.055	0.045	LT
2.4	-0.102	0.000	-0.008	-0.002	0.017	-0.048	0.007	0.025	0.048	0.021	CA
2.4	-0.073	-0.003	-0.019	0.019	-0.015	-0.048	0.007	0.025	0.048	0.021	TNG
2.5	0.148	0.006	-0.012	0.020	-0.021	-0.049	0.007	0.025	0.048	0.020	LT
3.5	0.147	0.007	-0.013	0.020	-0.023	-0.055	0.005	0.024	0.047	0.017	LT
4.4		0.006	-0.010	-0.003	0.027		0.004	0.023	0.046	0.015	CA
6.5	-0.032	0.000	-0.021	0.019	0.002	-0.063	0.004	0.023	0.047	0.010	TNG
7.4	0.124	0.011	-0.016	0.016	-0.031	-0.078	0.003	0.019	0.045	0.007	LT
8.4	-0.026	0.007	-0.016	0.001	0.047	-0.093	0.001	0.015	0.044	0.004	CA
9.3	0.094	0.016	-0.020	0.020	-0.035	-0.108	-0.007	0.013	0.042	-0.001	LT
9.3	-0.003	0.015	-0.020	0.012	-0.037	-0.108	-0.007	0.013	0.042	-0.001	NOT
11.5	-0.002	0.015	-0.023	0.009	-0.036	-0.129	-0.015	0.007	0.040	-0.012	NOT
12.5	0.067	0.019	-0.024	0.021	-0.049	-0.131	-0.019	0.006	0.039	-0.020	LT
12.6	-0.012	0.015	-0.023	0.007	-0.042	-0.131	-0.019	0.006	0.039	-0.020	NOT
16.4	*****	0.025	-0.026	0.021	-0.100	0.22	-0.032	0.001	0.035	-0.038	LT
17.3	0.050	0.026	-0.026	0.021	-0.115	-0.139	-0.035	0.000	0.035	-0.042	LT
17.6	0.023	0.012	-0.029	0.004	0.007	-0.139	-0.036	0.000	0.034	-0.043	TNG
19.3	0.050	0.027	-0.029	0.011	-0.121	-0.142	-0.040	-0.006	0.033	-0.039	LT
21.4	0.050	0.028	-0.032	0.002	-0.127	-0.145	-0.044	-0.012	0.031	-0.034	LT
22.6	0.041	0.015	0.023	0.002	-0.047	-0.147	-0.046	-0.015	0.030	-0.032	NTT
26.3	-0.005	0.013	-0.037	-0.016	-0.069	-0.143	-0.055	-0.028	0.030	-0.028	NOT
29.4	-0.005	0.013	-0.042	-0.018	-0.067	-0.140	-0.062	-0.037	0.031	-0.025	NOT
30.3	0.043	-0.078	-0.042	-0.016	-0.007	-0.140 $-0.139$	-0.065	-0.037	0.031	-0.023	Ekar
31.5	0.043	-0.078	0.050	0.010	-0.008	-0.137	-0.067	-0.044	0.031	-0.023	Ekar
34.3	0.071	0.041	-0.054	-0.033	-0.104	-0.135	-0.074	-0.053	0.029	-0.023	LT
35.5	-0.004	0.056	-0.068	0.002	0.075	-0.133 $-0.134$	-0.074 $-0.077$	-0.056	0.029	-0.020 $-0.019$	CA
36.3	0.075	0.030	-0.008 $-0.057$	-0.037	-0.115	-0.134 $-0.133$	-0.077 -0.079	-0.050 $-0.058$	0.029	-0.019 $-0.018$	LT
40.4	0.073	0.042	-0.057 -0.055	-0.037 $-0.033$	-0.113 $-0.131$	-0.133	-0.079 $-0.078$	-0.058 $-0.055$	0.028	-0.018 $-0.019$	LT
41.4	-0.006	0.042	-0.055 $-0.050$	-0.033 -0.024	-0.131 -0.061	-0.133 $-0.133$	-0.078 $-0.078$	-0.055 $-0.055$	0.030	-0.019 $-0.019$	NOT
41.4 44.4	0.072	0.014	-0.050 $-0.054$	-0.024 -0.029	-0.061 $-0.146$	-0.133 $-0.133$	-0.078 -0.077	-0.053 $-0.053$	0.030	-0.019 -0.020	LT
48.3	0.072	0.041	-0.054 -0.052	-0.029 $-0.025$			-0.077 -0.076	-0.053 $-0.050$	0.032	-0.020 $-0.021$	LT
48.5	-0.006	0.041	-0.032 $-0.048$	-0.023 -0.022	-0.162 $-0.061$	-0.134 $-0.134$	-0.076 $-0.076$	-0.050 $-0.050$	0.033	-0.021 $-0.021$	NOT
59.3		0.013	-0.048 -0.047	-0.022 $-0.013$			-0.076 $-0.073$	-0.030 $-0.043$	0.034	-0.021 $-0.023$	LT
60.3	0.068		-0.047 -0.044	-0.013 -0.019	-0.204	-0.132	-0.073 $-0.073$		0.039		
	-0.005	0.012			-0.063	-0.132		-0.042		-0.024	NOT
62.4	0.067	0.037	-0.046	-0.010	-0.215	-0.131	-0.073 $-0.073$	-0.040	0.040	-0.024	LT
66.3	0.066	0.038	-0.044	-0.006	-0.214	-0.133		-0.036	0.041	-0.017	LT
69.4	0.010	0.018	-0.051	-0.019	0.048	-0.135	-0.074	-0.033	0.042	-0.012	TNG
74.3	0.064	0.040	-0.039	0.001	-0.211	-0.137	-0.074	-0.027	0.044	-0.004	LT
75.3	-0.007	0.016	-0.036	-0.024	-0.038	-0.138	-0.074	-0.026	0.044	-0.002	NOT
78.3	0.063	0.041	-0.037	0.005	-0.210	-0.139	-0.075	-0.023	0.045	0.003	LT
81.4	0.051	0.020	0.024	0.007	-0.005	-0.141	-0.075	-0.020	0.046	0.008	NTT
85.3	0.066	0.043	-0.031	0.008	-0.212	-0.139	-0.075	-0.015	0.046	0.009	LT
86.3	0.067	0.043	-0.031	0.007	-0.213	-0.138	-0.075	-0.013	0.047	0.010	LT
87.3	0.067	0.044	-0.030	0.007	-0.214	-0.138	-0.075	-0.012	0.047	0.010	LT
90.3	-0.009	0.020	-0.026	-0.023	-0.022	-0.136	-0.076	-0.008	0.047	0.011	NOT

by Leiden University user on 23 November 2017

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Table A1 - continued

Epoch <sup>a</sup>	$S_U$	$S_B$	$S_V$	$S_R$	$S_I$	$K_U$	$K_B$	$K_V$	$K_R$	$K_I$	Tel.b
90.3	0.070	0.045	-0.027	0.007	-0.216	-0.136	-0.076	-0.008	0.047	0.011	LT
96.3	-0.005	0.071	-0.021	0.002	0.020	-0.133	-0.076	0.001	0.048	0.013	CA
100.4		0.048	-0.020	0.007	-0.222		-0.077	0.006	0.048	0.014	LT
105.3		0.050	-0.019	0.009	-0.222		-0.079	0.010	0.049	0.013	LT
109.2		0.075	-0.021	0.005	0.008		-0.081	0.013	0.049	0.013	CA
109.3	-0.012	0.027	-0.017	-0.011	-0.015	-0.126	-0.081	0.013	0.049	0.013	NOT
114.2		-0.077	-0.007	-0.006	$-0.001^{c}$		-0.083	0.023	0.047	$0.013^{c}$	Ekar
116.2		-0.076	-0.010	-0.006	$-0.001^{c}$		-0.084	0.027	0.046	$0.013^{c}$	Ekar
116.3		0.053	-0.011	0.013	$-0.222^{c}$		-0.084	0.027	0.046	$0.013^{c}$	LT
118.2	0.096					-0.121					LT
119.3		0.054	-0.008	0.015	$-0.222^{c}$		-0.086	0.032	0.045	$0.013^{c}$	LT
125.2		0.087	0.000	0.005	$0.008^{c}$		-0.089	0.044	0.042	$0.013^{c}$	CA
126.2		0.055	-0.001	0.018	$-0.222^{c}$		-0.089	0.046	0.041	$0.013^{c}$	LT
130.3		0.056	0.000	0.014	$-0.222^{c}$		-0.091	0.049	0.040	$0.013^{c}$	LT
132.3		0.090	0.004	0.005			-0.091	0.050	0.039		CA
137.3		0.058	0.001	0.004	$-0.222^{c}$		-0.093	0.052	0.036	$0.013^{c}$	LT
139.2	$0.104^{c}$					$-0.116^{c}$					LT
145.3			0.002	-0.008				0.055	0.032		LT
151.2		0.062	0.002	-0.016	$-0.222^{c}$		-0.097	0.057	0.029	$0.013^{c}$	LT
166.2		0.066	0.003	-0.038	$-0.222^{c}$		-0.102	0.062	0.022	$0.013^{c}$	LT
169.2			0.004	-0.042	$-0.222^{c}$			0.063	0.020	$0.013^{c}$	LT
262.6		0.053	0.018	-0.106			-0.130	0.098	-0.027		NOT
300.7		$0.040^{c}$	$-0.099^{c}$	$0.054^{c}$	$-0.011^{c}$		$-0.140^{c}$	$0.110^{c}$	$-0.043^{c}$	$0.013^{c}$	NTT
313.7		$0.040^{c}$	$-0.099^{c}$	$0.054^{c}$	$-0.011^{c}$		$-0.140^{c}$	$0.110^{c}$	$-0.043^{c}$	$0.013^{c}$	NTT
316.8		$0.040^{c}$	$-0.099^{c}$	$0.054^{c}$			$-0.140^{c}$	$0.110^{c}$	$-0.043^{c}$		NTT
328.6				$-0.126^{c}$	$-0.015^{c}$				$-0.043^{c}$	$0.013^{c}$	NOT
426.3			$0.035^{c}$		$0.059^{c}$			$0.110^{c}$		$0.013^{c}$	TNG

<sup>&</sup>lt;sup>a</sup>Phase in days with respect to *B*-band maximum JD =  $2454947.1 \pm 0.3$ ; <sup>b</sup> see Table 3 for details; <sup>c</sup> constant extrapolation to later epochs.

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