

Quantum dot nonlinearity through cavity-enhanced feedback with a charge memory

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In an oxide apertured quantum dot (QD) micropillar cavity-QED system, we observe strong QD hysteresis effects and line-shape modifications even at very low intensities corresponding to $<10^{-3}$ intracavity photons. We attribute this to the excitation of charges by the intracavity field; they get trapped at the oxide aperture, where they screen the internal electric field and blueshift the QD transition. This in turn strongly modulates light absorption by cavity-QED effects, eventually leading to the observed hysteresis and line-shape modifications. The cavity also enables us to observe the QD dynamics in real time, and all experimental data agree well with a power-law charging model. The observed charging effect can serve as a tuning mechanism for quantum dots.

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Cavity quantum electrodynamics with quantum dots (QDs) coupled to microcavities enables various applications, such as single-photon switches [1–5], generation of nonclassical states of light [6–8], and hybrid quantum information schemes [9,10]. However, QDs deviate from ideal atomlike systems as they strongly interact with their environment, for example, through nuclear spins [11,12] and via charge traps [13,14]. These interactions need to be understood and controlled in order to improve the QD coherence properties. For this purpose, cavities are very useful to probe the QD environment, through increased light-matter interactions.

In this Rapid Communication we investigate such a QD-cavity system. For a sufficiently low optical field intensity this system can be described by the QED of an effective two-level system in a single-mode cavity. For increasing intensities we report on bistable and strong nonlinear behavior. The sample under study consists of InAs self-assembled QDs inside a p - i - n diode structure embedded in a micropillar cavity. This system combines QD charge and Stark shift control by applying a bias voltage with high-quality polarization-degenerate cavity modes [15–19]. The mode confinement in the transversal direction is achieved by an oxide aperture formed through a wet oxidation step. The observed bistability and nonlinear behavior in the cavity-QED system can be explained by attributing a second role to the oxide aperture, namely, that of a charge memory. Charges in this memory, created by resonant absorption, will cause a modification of the internal electric field which shifts the QD frequency, and this in turn modifies the amount of absorption. In Fig. 1(a) the sample structure, with charges trapped at the oxide aperture, is schematically shown.

We consider one of the fine-split transitions of a charge neutral QD coupled to a polarization-degenerate cavity mode in the intermediate coupling regime. Figure 1(b) shows reflection spectra, recorded at a sufficiently low incident intensity $P_{\text{in}} = 1$ pW such that no nonlinear effects occur. Upward and downward frequency scans overlap perfectly and can be fitted by theory for a dipole inside an optical cavity, which we will discuss later in detail. However, when a higher intensity of 1 nW is used, several strong deviations occur [see Fig. 1(c)]. First of all, a hysteresis feature appears when the QD is tuned at or below the cavity resonance. Second, while at

the high frequency side of the cavity resonance the hysteresis is much less, a line-shape modification is still visible. Finally, in order to obtain the same QD detuning compared to the low intensity scans, a lower bias voltage has to be applied. After a thorough characterization of this effect, we present a model that explains all features, as is shown in Fig. 1(d).

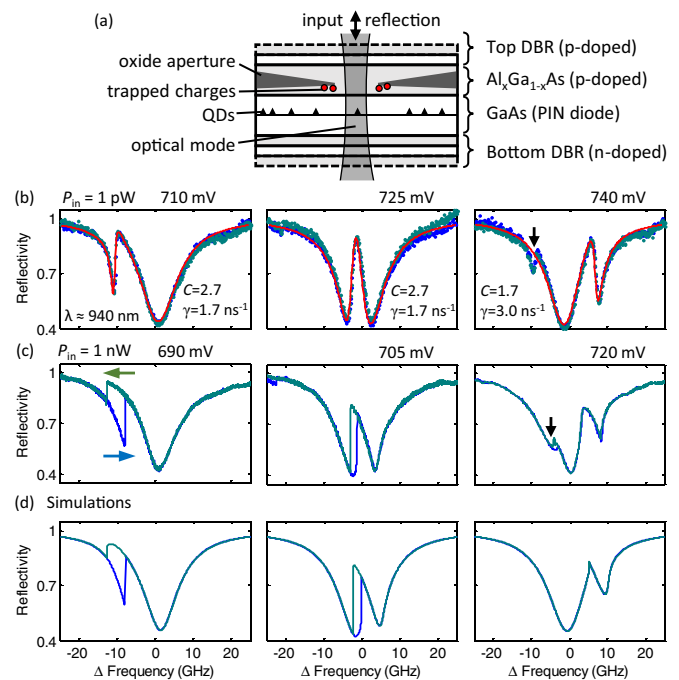


FIG. 1. (Color online) (a) Schematic of the sample structure with charges trapped at the oxide aperture. The figure is not to scale and only a couple of distributed Bragg reflector (DBR) pairs are shown. Resonant reflection spectroscopy scans recorded using laser intensities of (b) 1 pW and (c) 1 nW for various applied bias voltages. Blue (green) curve: Upward (downward) frequency scan. Red lines in (b) are fits using Eq. (1) and reflectivity $R = |1 - t|^2$. The QD cooperativity C and dephasing rate γ obtained from the fits are given in the figures. The black arrows denote a second QD in the same cavity. Scans were taken on a \sim s time scale. (d) presents simulations that predict the scans in (c).

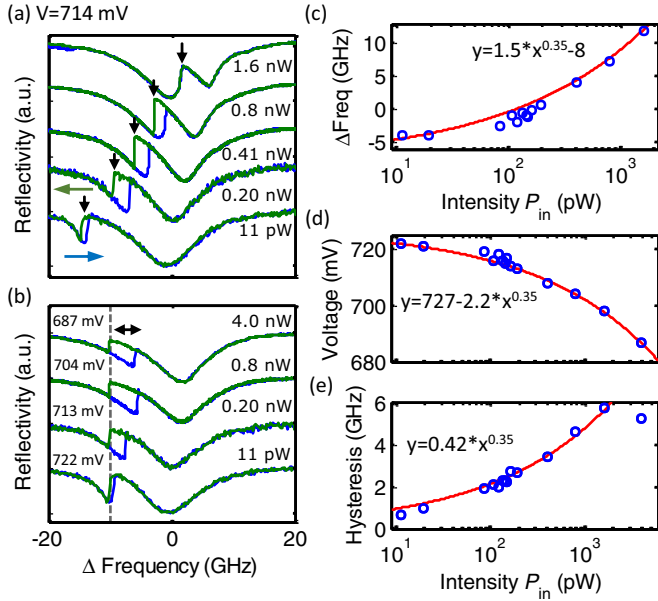


FIG. 2. (Color online) Characterization of the QD blueshift and nonlinearity. (a) Resonant reflection spectra for a fixed bias voltage and various intensities of the scanning laser. Blue (green): Low to high (high to low) frequency scan. (b) Scans where the QD-cavity detuning is kept constant by varying the bias voltage for various laser intensities. (c) Relative QD shift [estimated from the vertical arrows in (a)], (d) applied bias voltage to keep the QD-cavity detuning constant [vertical dashed line in (b)], and (e) hysteresis width [horizontal arrow in (b)], all as functions of the laser intensity. The red lines in (c), (d), and (e) show empirical power-law fits (see main text). Vertical offsets have been added to the scans in (a) and (b).

A first hint on the underlying dynamics is provided by investigating the power dependence in single-laser scans. In Fig. 2(a) we first keep the QD bias voltage constant and show scans for increasing laser intensity. A QD blueshift occurs, as is displayed in Fig. 2(c). In a second set of measurements in Fig. 2(b), we keep the QD-cavity detuning constant by changing the bias voltage as a function of the laser intensity. A lower bias voltage has to be applied for increasing laser intensity, shown in Fig. 2(d). Furthermore, the hysteresis width increases with intensity [see Fig. 2(e)], up to nearly 6 GHz, but then saturates and even decreases slightly when the intensity is above the QD saturation intensity (~ 2.5 nW). All three observations in Figs. 2(c)–2(e) obey the same empirical power law $\propto P_{\text{in}}^{\beta}$, with $\beta \approx 0.35$. Already at an incident intensity $P_{\text{in}} = 11$ pW, corresponding to a maximum mean photon number per cavity lifetime of $\langle \bar{n} \rangle \approx 4 \times 10^{-4}$, a QD blueshift and line-shape modification are clearly visible. Here, the mean intracavity photon number is found from $\langle \bar{n} \rangle = P_{\text{out}} / \kappa_m \hbar \omega$, where $\kappa_m \sim 11$ ns $^{-1}$ is the mirror loss rate, ω is the light angular frequency, and the maximum output intensity $P_{\text{out}} = |t|^2 P_{\text{in}} \sim 1$ pW (see below).

We now switch to a two-laser experiment (see Fig. 3) in order to further investigate the phenomenon that the QD blueshifts with increasing laser intensity. The QD transition is probed with a low intensity (1 pW) probe laser such that no line-shape modification occurs. We then add a second high intensity (1 nW) pump laser with orthogonal polarization,

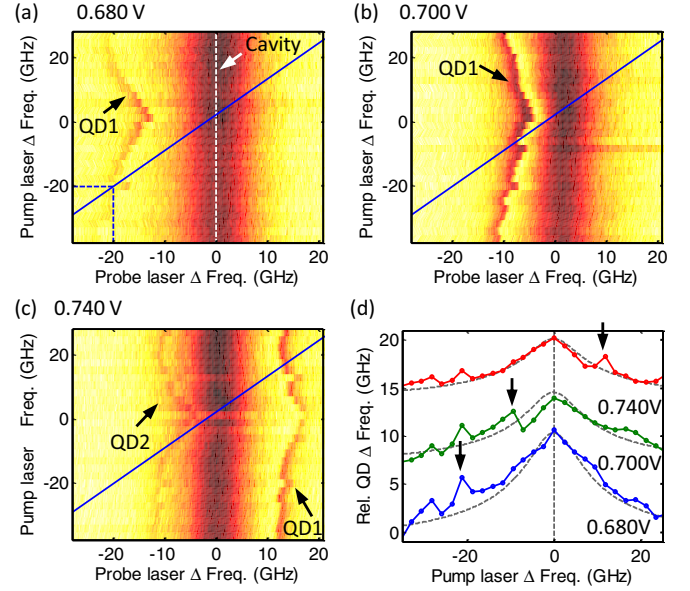


FIG. 3. (Color online) Two-laser scans with resonant lasers. (a)–(c) Reflectivity color map of a weak (1 pW) probe laser (light: $>90\%$; dark: $\approx 50\%$) as a function of probe laser frequency and second high intensity (1 nW) pump laser frequency for three bias voltages. The blue line shows the pump laser frequency compared to the probe laser. The arrows indicate the QD position. (d) Relative QD frequency shift as a function of the pump laser-cavity detuning. The arrows denote where the laser is resonant with the QD. Gray dashed lines: Lorentzian functions convoluted with the power law from Fig. 2(c) that have been added as a reference. Vertical offsets are added to the curves.

such that it can be filtered out with a crossed polarizer in the detection channel. The pump laser is scanned in steps across the cavity resonance; for each step the QD-cavity spectrum is measured with the weak probe laser. Figures 3(a)–3(c) present these measurements for various bias voltages such that the average QD-cavity and pump laser-cavity detunings are determined, and the relative QD frequency as a function of the pump laser-cavity detuning is shown in Fig. 3(d). The maximum QD blueshift (of about 8 GHz) occurs when the pump laser is resonant with the cavity mode, corresponding to the vertical dashed line. An increased blueshift also occurs when the pump laser is close to the QD frequency, indicated by the arrows in Fig. 3(d), at which point the intracavity field also increases due to cavity-QED effects. The gray dashed curves are Lorentzian lines convoluted with the $\propto P_{\text{in}}^{0.35}$ power law from Fig. 2(c) and correspond nicely to the data. In conclusion, the data clearly show that the QD resonance blueshifts when the intracavity field increases, and this effect is independent of the QD-laser or the QD-cavity detuning.

We now introduce a model that explains the dynamic line-shape modifications. We start from the transmission amplitude of a cavity with a coupled dipole [4,20,21],

$$t = \eta_{\text{out}} \frac{1}{1 - i\Delta + \frac{2C}{1-i\Delta}}, \quad (1)$$

where $\Delta = 2(\omega - \omega_c)/\kappa$ is the relative detuning between the laser (ω) and cavity (ω_c) angular frequencies, $C = g^2/\kappa\gamma$ is the QD cooperativity, g the QD-cavity coupling rate, $\Delta' = (\omega - \omega_{\text{QD}})/\gamma$ is the relative detuning between the laser and QD transition (ω_{QD}), η_{out} is the output coupling efficiency, κ is the total intensity damping rate of the cavity, and γ is the QD dephasing rate. We obtain close to perfect mode matching and both mirrors have approximately equal losses, and therefore the total transmittivity through the cavity is given by $T = |t|^2$, and the total reflectivity is given by $R = |1 - t|^2$. In Fig. 1(a) we show that the model fits the low intensity measurements very well. The QD cooperativity and dephasing parameters C and γ are noted in the subfigure windows, and a cavity damping rate $\kappa \sim 77 \text{ ns}^{-1}$ and an output coupling efficiency $\eta_{\text{out}} = 2\kappa_m/\kappa \sim 0.3$ is found, corresponding to a cavity Q factor of $Q \sim 2.6 \times 10^4$.

As a next step, we introduce an empirical model for the QD frequency $f_{\text{QD}} = \omega_{\text{QD}}/2\pi$ that dynamically changes with the intracavity intensity, which is proportional to $|t|^2$,

$$f_{\text{QD}} = f_0 + \alpha \left(\frac{P_{\text{in}} |t|^2}{\text{pW} \eta_{\text{out}}^2} \right)^\beta, \quad (2)$$

where f_0 equals the QD frequency in the limit of vanishing intracavity intensity. Based on the measurements in Fig. 2(c), we find $\alpha = 1.5 \text{ GHz}$ and $\beta = 0.35$. Due to cavity-QED effects, the intracavity field depends strongly on the QD frequency such that the cavity can change from being largely transparent to being largely reflective through only small changes in the QD frequency. This interplay leads to the observed nonlinear behavior.

Finally, we take into account that we are operating the QD-cavity system close to the saturation intensity, which slightly suppresses the QD features. We take this into account by calculating the reflectivity R' by taking the weighted sum of the reflectivities of a coupled (R) and uncoupled (R_0) cavity, $R' = xR + (1 - x)R_0$, with $x = 0.8$. This is a strong simplification of a more rigorous approach based on the quantum master equation and calculation of the intracavity photon number [4], but is sufficient for our purpose. For QD cooperativity C and dephasing rate γ we use the values obtained in the fits in Fig. 1(a). Figure 1(c) shows that the predicted scans match the actual measurements very well.

As the underlying physical mechanism, we hypothesize that charges are excited by the resonant laser and get trapped at the oxide aperture. Reasonably high doping concentrations were used, up to $6 \times 10^{18} \text{ cm}^{-3}$ for the carbon p -doped layers and up to $5 \times 10^{18} \text{ cm}^{-3}$ for the silicon n -doped layers, and it is well known that absorption takes place in these doped layers [22]. The excited charges partly screen the internal electric field responsible for the quantum confined Stark effect in the QD, leading to the observed blueshift of the QD transitions.

Furthermore, the fact that even for a very low cavity mean photon number of ~ 0.001 ($P_{\text{in}} = 11 \text{ pW}$) nonlinearities take place indicates that the oxide aperture must form an efficient and long-lived charge memory compared to the QD-cavity decay rate (77 ns^{-1}). It is well known that the interface between GaAs and aluminum oxide (AlO_x), produced by wet oxidation of AlAs, provides a very high density of charge traps, in the form of amorphous oxide and microcrystallites [23], and in the form of elemental interfacial As [24], leading to spatially

nonuniform Fermi level pinning [25]. The time-resolved charge decay measurements presented below confirm that the charges are relatively long lived on a $\sim 10 \text{ ms}$ time scale. Also, a comparison with QDs outside of the oxide aperture region shows that laser-induced blueshift is negligible in these regions.

Our results agree with observations in Ref. [13], where single-charge fluctuations are probed at a GaAs/AlAs interface located about 50 nm away from the QDs, while a gradual variation was observed for charge traps more than 150 nm away. We did not observe any single-charge influences as the distance between the QDs and the oxide aperture is about 200 nm in our sample. In contrast to our work, the GaAs/AlAs interface studied in Ref. [13] is located in the intrinsic region, while the aperture in our sample is located in the p -doped region, but a similar QD blueshift for increasing laser intensity and constant bias voltage was observed.

Finally, we performed a set of measurements to gain insight in the temporal dynamics of the charge buildup and decay. For this purpose we use a laser ($\lambda = 852 \text{ nm}$) that is off resonant with the cavity but is absorbed by the wetting layer. At a higher laser intensity, more charges are excited compared to the resonant laser and larger QD shifts can be obtained. We now use the coupled QD-cavity system as a very sensitive probe of the internal electric field, a principle that was also used to monitor a single charge trap in real time [26].

Figure 4(a) shows, for various off-resonant pump laser intensities, the bias voltage that has to be applied to tune the QD to the cavity resonance, determined by using a weak ($\sim 1 \text{ pW}$) resonant probe laser. Again, as in Fig. 2(d), a clear sublinear behavior $\propto P_{\text{in}}^\beta$ with $\beta \approx 0.35$ is visible. At an even higher intensity of $100 \mu\text{W}$, a bias voltage of 350 mV had to be applied to tune the QD into resonance, clearly indicating that the charge buildup and QD blueshift is not easily saturated. Strikingly, even for an excitation power of 200 nW, the QD has the same cooperativity C and dephasing rate γ as when no off-resonant laser is present [see Fig. 4(b)]. This indicates that, even though many charges are excited, they are located relatively far away and give rise to a more or less constant effective electric field, thereby preserving the QD coherence.

In order to directly monitor the time dynamics of the charge buildup and decay, we fix a weak probe laser that will not excite any additional charges at the cavity resonance, and monitor the reflectivity as a function of bias voltage and time. Figure 4(c) shows, for various off-resonant pump laser intensities, reflectivity color maps of the probe laser when the off-resonant pump laser is turned on at $t = 0 \text{ ms}$. For $t < 0 \text{ ms}$, the QD is resonant with the cavity resonance at $V = 713 \text{ mV}$ (white dashed lines), corresponding with a high probe laser reflectivity at this voltage and a low reflectivity at different voltages. The reflectivity at $V = 713 \text{ mV}$ abruptly decreases as the pump laser is turned on, but is then restored at lower bias voltages, demonstrating direct probing of the charge buildup. For increasing pump laser intensities, the reflectivity is restored at a lower voltage, but also the time for the charge buildup to reach an equilibrium decreases.

The decay of the charges is monitored in Fig. 4(d), where the pump laser is turned off at $t = 0 \text{ ms}$. For $t < 0 \text{ ms}$ the QD reflectivity signal is now highest for a low bias voltage when

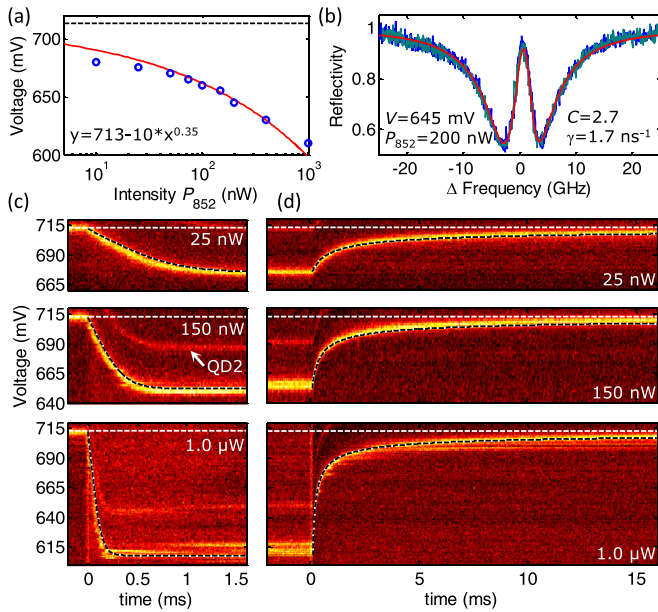


FIG. 4. (Color online) Two-laser scans with an off-resonant ($\lambda = 852$ nm) laser. (a) shows the bias voltage where the QD transition is resonant with the cavity mode, as a function of the intensity P_{852} of the off-resonant laser. The black dashed line indicates the QD bias voltage when no off-resonant laser is applied. (b) Example of resonant reflection scans using a weak (1 pW) probe laser, recorded in the presence of an off-resonant laser. The text in the figures denotes the applied bias voltage V , intensity P_{852} , and QD cooperativity C and dephasing rate γ of the predicted red line. (c), (d) Color maps of the reflected intensity of the probe laser fixed to the center of the cavity resonance (light/dark: high/low signal, corresponding to an on/off resonant QD), as a function of the time and applied bias voltage, for various off-resonant pump intensities. The off-resonant laser is turned (c) on and (d) off at $t = 0$ ms. The red line in (a) and the black-white dashed line in (c) and (d) are reproduced using the same parameters (see the main text for an explanation). Note that the time axes of (c) and (d) are different.

the charge reservoir is saturated. After the pump is turned off and the charges disappear, the reflectivity now gets restored at an increasing bias voltage. The charge decay rate is initially fastest, when many charges are still present and the QD is

resonant at a lower bias voltage, but then strongly decreases and finally occurs on a ~ 10 ms time scale, much slower than the charge buildup rate.

We now introduce a simple power-law model to describe the charge buildup and decay dynamics. We assume that the QD voltage shift ΔV is proportional to the number of trapped charges Q , and increases as a function of the pump laser intensity P , such that $\Delta V = -Q = -\Gamma P^\beta$. As a result, the charge decay and buildup is described using $\frac{dQ}{dt} = P - (Q/\Gamma)^{1/\beta}$. The red line in Fig. 4(b) and the white-black dashed lines Figs. 4(c) and 4(d) are reproduced with $\Gamma = 10$ and the same power-law scaling factor $\beta = 0.35$ as found earlier; these lines nicely describe the data.

The effect we found enables a method to tune QD transitions without the need for electrical contacts, or enable independent tuning of QDs sharing the same voltage contacts. Furthermore, it could serve as a low power all-optical switch mediated by a charge memory. The cavity-enhanced feedback mechanism with the charge environment could in principle also occur in other solid-state microcavity structures, where doped layers are present in which charges can be excited and where material defects or interfaces could act as a charge trap. This interaction therefore also has to be taken into account when studying dynamical nuclear spin polarization (DNP) effects in a cavity, which is of general interest to prolong the QD coherence time and the potential to form a quantum memory. DNP gives rise to QD line-shape modifications, hysteresis, and bistability behavior [11,27–32], phenomena that could also give rise to cavity-enhanced feedback mechanisms.

In conclusion, we have studied a neutral QD transition coupled to a microcavity and observed strong cavity-enhanced feedback with the charge environment. Hysteresis and modifications of the QD line shape are demonstrated at intensities of way less than 1 photon per cavity lifetime, which we explain and model by a QD frequency blueshift attributed to charges trapped at the oxide aperture as a function of the intracavity field. In general, these results demonstrate the potential of studying and controlling the QD environment using a cavity-QED system.

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