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Thermodynamics of deposition flux-dependent intrinsic film stress

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Vapour deposition on polycrystalline films can lead to extremely high levels of compressive stress, exceeding even the yield strength of the films. A significant part of this stress has a reversible nature: it disappears when the deposition is stopped and re-emerges on resumption. Although the debate on the underlying mechanism still continues, insertion of atoms into grain boundaries seems to be the most likely one. However, the required driving force has not been identified. To address the problem we analyse, here, the entire film system using thermodynamic arguments. We find that the observed, tremendous stress levels can be explained by the flux-induced entropic effects in the extremely dilute adatom gas on the surface. Our analysis justifies any adatom incorporation model, as it delivers the underlying thermodynamic driving force. Counterintuitively, we also show that the stress levels decrease, if the barrier(s) for adatoms to reach the grain boundaries are decreased.

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During the growth of a polycrystalline film on a substrate, the film usually develops a significant amount of internal stress. If the film temperature is high enough to reach Volmer–Weber-type growth conditions^{1,2}, the film stress during deposition follows a compressive–tensile–compressive evolution, as is indicated with stages I, II and III in Fig. 1. During stage I, the nucleated islands develop a compressive stress due to surface tension effects^{3,4}. Stage II occurs during film closure when the three-dimensional (3D) islands coalesce and form grain boundaries (GBs). At this stage, the film free energy can be further lowered by GB zipping, which in turn delivers tensile stress^{5,6}. Without sufficient mobility (low temperature or high deposition flux) the film remains tensile on further growth. In contrast, a maximum tensile stress develops for Volmer–Weber-type growth of high-mobility materials, which occurrence coincides approximately with the moment the film closes. From this moment on, the stress turns once again towards compressive values (stage III)⁷. Surprisingly, a significant part of the compressive stress has a reversible nature: on interrupting the deposition flux (Fig. 1), the film stress jumps to less compressive values and the original compressive stress state before interruption is almost fully restored when the flux is switched on again. These stress jumps can be as large as ~ 150 MPa and the time constant of the stress variation on resuming the deposition is in the order of 20 s (refs 8,9).

In the last 20 years several mechanisms have been proposed aiming to explain the observed effects: (1) pre-coalescence surface tension continuation combined with ongoing grain growth¹⁰; (2) surface roughness development during deposition combined with step–step interactions²; (3) adatom insertion into GBs^{11–13}; (4) interaction of adatoms with surface and each other⁹; (5) inside bundling–outside grooving of GBs¹⁴; (6) depth changes in the GB grooves¹⁵; and so on. Whereas several of these mechanisms rely on kinetically limited processes, the GB adatom insertion model suggests that the compressive stress is generated via adatoms that are forced into the GBs by the enhanced chemical potential (CP) of the surface that is set-up by the deposition flux. By switching off this flux, the CP should drop, which should lead to an outflow of the excess atoms from the GBs and, thereby, to a relaxation of the compressive stress¹¹. Recent experiments confirmed that GBs are prerequisite for the existence of the reversible stress jumps¹⁶. However, more questions arise, as the time constant of the stress relaxation on interruption seems to be temperature-independent¹⁷. On the other hand, surface stress effects⁹ are expected to be too low in magnitude¹⁸ to explain the reversible stress jumps. While the discussion on the mechanism(s) still continues, at a more fundamental level, the underlying driving force behind the effect has never been addressed.

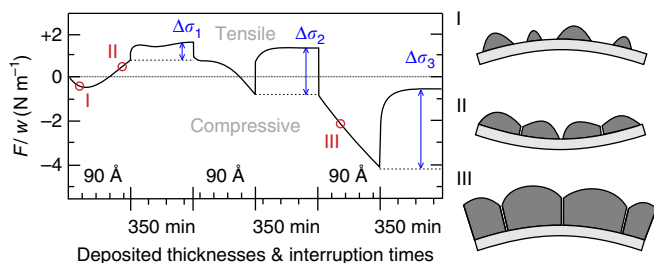


Figure 1 | Stress evolution during Volmer–Weber-type film growth for copper deposition with a flux of 0.1 \AA s^{-1} onto silicon oxide at room temperature. It consists of three main stages: nucleation (I); coalescence (II); and thickening (III). The deposition was interrupted three times for 350 min. The reversible stress jumps are indicated by $\Delta\sigma_i$. Part of graph reprinted with permission from ref. 8. Copyright *Journal of Applied Physics*, 1996, AIP Publishing LLC.

In this paper we derive the magnitudes and the changes of the CP on the surface next to the position of the GBs and show that this indeed forms the driving force for any adatom insertion model. From a thermodynamic point of view, the most fundamental question has never been addressed, probably due to conceptual difficulties in calculating the CP of the surface during the growth: ‘how can a flux (change) as low as ~ 0.1 monolayer per second (ML per s) lead to stress jumps as high as ~ 150 MPa?’ Our study focuses exactly on this question and we show not only that these low fluxes can generate such huge stresses but also that the driving force for the stress jumps is decreased, if it is easier for the adatoms to diffuse towards and into the GBs.

Results

Basic thermodynamic description. To derive our model, it is important to realize that the film is under growth conditions and therefore naturally not in equilibrium. However, as long as the growth conditions do not change, it can be treated in steady state, like the famous Growth–Wulff construction¹⁹. The enhanced surface CP with respect to equilibrium sets up an adatom current to steps, which finally leads to the film growth. This also means that the CP on the surface varies locally and that positions connected to each other will try to balance their difference. If atom transport is sufficiently active on the timescale of consideration, one can approximate adjacent positions to be in equilibrium. Therefore, for constant small deposition fluxes and the absence of kinetic limitations, thermodynamic equilibrium can be assumed between the positions on the surface immediately next to grain boundaries (s/GB), the GBs and the grain interiors (g). This assumption is further underpinned by the small number of total additional atom that have to be incorporated in the GBs. For the surface we solve rate equations to determine the CP immediately next to the GBs and we further treat this position, the GBs, and the grain interior to be in equilibrium. Thermodynamic equilibrium certainly does not hold for the transition between the flux on and off states, but is justified a few tens of seconds after the flux change (see above). Therefore, at constant or zero flux, a change of the CP of the surface next to the GBs, will finally change the CP of the GBs with the same amount, which in turn will change the CP of the grains:

$$\Delta\mu_{s/\text{GB}} \approx \Delta\mu_{\text{GB}} \approx \Delta\mu_{\text{g}} \Rightarrow \Delta\mu_{s/\text{GB}} \approx \Delta\mu_{\text{g}} \quad (1)$$

This core equation enables us to bypass the determination of the CP of the GBs, as well as the absolute CP values on the surface and within the grains.

Chemical potential of the surface. The free energy of a surface depends on the formation and interaction energies of a myriad of surface features such as terraces, steps, kinks, step adatoms, adatoms and so on. As the surface morphology evolves during deposition, the population of these features changes accordingly. However, it is known that the reversible, compressive stress can develop within seconds after starting the flux even with rates as low as 0.1 ML per s. Obviously, the population of point-like features, like adatoms, step adatoms and kinks, can (and will) change abruptly on the arrival of flux on the surface, but extended surface features, like terraces and step edges, do not change significantly within such short timescales, as they consist of a large number of atoms²⁰. For example, the surface roughness is directly linked to changes in the appearance, distribution and amount of steps and terraces. The compressive–tensile–compressive behaviour is usually observed under step-flow growth mode conditions, where changes in the surface roughness are known to happen very slowly^{21,22}. This means that the gradual increase in

surface roughness (and hence the extended surface features) during deposition will only have a long time effect on the surface CP via the Gibbs–Thomson relation. Since the reversible stress jumps occur in a matter of seconds, we safely can ignore these long-term changes in our analysis. Moreover, in contrast to the adatoms that live in a two-dimensional (2D)-space on the terraces, the step adatoms and step kinks are confined to the one-dimensional space on the step edges. This causes the rate, at which the step adatoms and kinks meet and annihilate each other, to be significantly higher than the adatoms on the terraces. As a result, the increase in adatom population on the terraces, on starting the deposition, is orders of magnitude higher than that of kinks or step adatoms²³. The conclusion is that the surface CP change, which is responsible for the almost instantaneous stress jumps, is mainly dominated by a change in the adatom density. Consequently, we can neglect all other contributions, as they would lead only to higher-order correction terms in determining the surface CP variations:

$$\begin{aligned} \Delta\mu_s &= \Delta\mu_{\text{adatom}} + O(\Delta\mu_{\text{step adatom}}, \Delta\mu_{\text{kink}}, \Delta\mu_{\text{step}}, \dots) \\ &\approx \Delta \left[\frac{\partial U_{\text{adatom}}}{\partial N} + \frac{\partial U_{\text{adatom int.}}}{\partial N} - T \frac{\partial S_{\text{adatom}}}{\partial N} \right] \end{aligned} \quad (2)$$

The first term in the brackets, $\partial U_{\text{adatom}}/\partial N$, accounts for the surface temperature-dependent change in average energy (potential and kinetic) of individual adatoms. Given by the radiation of the evaporator and the kinetic energy of the arriving atoms, the increase in film temperature is <10 K for Cu, Ag and Au (ref. 24), which corresponds to ~ 2.6 meV per film atom according to the classical Dulong–Petit limit of the heat capacity in solids. As these materials all have an excellent thermal conductivity, the surface and the bulk temperatures are virtually identical. Since we finally have to compare only the CP variation of the surface and the grains, we can safely neglect this term, as we would have to add the same value to both sides of equation (1).

The second term $\partial U_{\text{adatom int.}}/\partial N$ corresponds to the interaction energy between the individual adatoms given by (combinations of) van der Waals, electrostatic (dipole), elastic and electronic (substrate-mediated) effects²⁵. We safely can ignore this term, as scanning tunneling microscopy (STM) experiments at ~ 15 K have shown that the absolute value of the interaction energy drops below 0.1 meV for two Cu adatoms separated more than 60 Å on a Cu(111) surface²⁶. This is equivalent to an adatom density (fractional coverage) of $<6.0 \times 10^{-4}$ ML, and as it will be shown in the following, we never reach such densities during the deposition.

The third term $-T \times \partial S_{\text{adatom}}/\partial N$ involves the entropic effects of the 2D adatom gas. In general, depending on the adatom mobility, adatoms can be assumed to be confined on discrete lattice sites (adatom lattice gas) or to be delocalized behaving as a 2D van der Waals surface gas (2D adatom gas)²⁷ (Supplementary Note 1). As these two models naturally set the lower and upper limits for the adatom gas entropy, we calculated the boundary values of the CP for copper in Fig. 2a (Supplementary Fig. 1). Although the absolute values differ more than 0.3 eV, both models show a linear behaviour in this logarithmic plot below 0.01 ML such that the following approximation holds for the CP variations:

$$\Delta \left[-T \frac{\partial S}{\partial N} \right] \approx k_B T \ln(\theta_2/\theta_1) \quad (3)$$

Adatom density on terraces. To calculate the adatom densities during deposition and interruption, Fig. 2b shows a simplified model of the film surface, in which we define the position of the first lattice row next to the ascending step edge as the origin of a terrace with width w in lattice units. By solving the differential equation for mass conservation, the adatom density at site n on the terrace, θ_n , can be derived as a function of deposition flux F (Supplementary Note 2 and Supplementary Figs 2, 3 and 4):

$$\theta_n = \theta_{\text{eq}} + \frac{Fw(an+1)(sw+2)}{2v_d(asw+a+s)} - \frac{Fn^2}{2v_d} \quad (4)$$

where $\theta_{\text{eq}} = \exp(-E_{\text{form}}/k_B T)$, $v_d = v_0 \exp(-E_{\text{diff}}/k_B T)$, $a = \exp(-\Delta E_{\text{att}}/k_B T)$ and $s = s_0 \exp(-\Delta E_{\text{ES}}/k_B T)$, in which v_0 , E_{diff} , E_{form} , ΔE_{att} , s_0 and ΔE_{ES} are the diffusion rate prefactor, diffusion barrier, adatom formation energy from a kink site of the step, the attachment barrier, correction prefactor for hop over the step and the Ehrlich–Schwoebel barrier, respectively (Fig. 2b)^{27,28}. Note that at zero deposition flux, the adatom density at each position n of the terrace is equal to the equilibrium density θ_{eq} . For constant deposition with $\Delta E_{\text{ES}} \gg \Delta E_{\text{att}}$, $s \ll a$, the adatom density is highest close to the end of the terrace (Fig. 2b), whereas the maximum shifts to the middle of the terrace for low values of ΔE_{ES} (Fig. 2c). Note that the maximum of the adatom density is only exactly at the end of the terrace for $E_{\text{ES}} = \infty$.

Combining equations (2)–(4), one can calculate $\Delta\mu_s$ as a function of deposition flux for any site n on the terrace.

Chemical potential of the grains. Considering an in-plane isotropic biaxial film ($\sigma_x = \sigma_y$ and $\sigma_z = 0$), it can be proven for the right-hand side of equation (1) that the CP within the grains is proportional to its total internal stress level σ_g (Supplementary

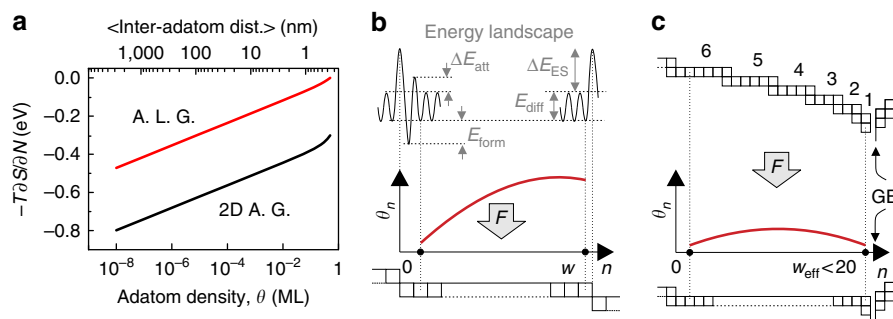


Figure 2 | Surface CP on terraces and next to GBs. (a) Entropic component of the CP on Cu(111), estimated by the adatom lattice gas and the 2D adatom gas model. (b) Adatom density profile, θ_n , on a terrace; the corresponding energy landscape is indicated on the top. (c) Typical step configuration in the vicinity of a GB caused by the Zeno effect (top). As ΔE_{ES} vanishes for terrace widths with $w < 6$, the combination of these terraces can be approximated with one effective terrace (bottom). This leads to a lower adatom density near the GB and, therefore, to lower stresses. dist., distance.

Note 3 and Supplementary Fig. 5):

$$\Delta\mu_g = - \int_{\sigma_x^0}^{\sigma_x^0 + \Delta\sigma_x^{\text{rev}}} \Omega_{ij} d\sigma_{ij} = - \Omega_x \Delta\sigma_x - \Omega_y \Delta\sigma_y \approx - \frac{2}{3} \Omega \Delta\sigma_g \quad (5)$$

where Ω is the atomic volume²⁹.

Derivation of the stress jumps. Motivated by the fact that stress emergence has to be GB-related¹⁶, it is crucial to derive the stress jumps using the $\Delta\mu_g$ immediately next to the GBs. Combining the above equations at position $n = w$, the predicted upper limit for the reversible stress jumps based on pure thermodynamics is given by

$$|\Delta\sigma_{\text{rev}}| \approx \frac{3k_B T}{2\Omega} \ln \left(1 + \frac{Fw(aw + 2)}{2v_d(asw + s + a)\theta_{\text{eq}}} \right) \quad (6)$$

It has been shown for gold at room temperature that step-flow growth is the underlying atomic process for polycrystalline film growth in the Volmer–Weber regime²¹. On the basis of the so-called Zeno effect, terraces closer to the GB get progressively decreased in their width during deposition, which leads to an enhanced surface curvature at the GB vicinity, as sketched in Fig. 2c, top^{21,30}. This results in a deviation from the macroscopic equilibrium surface of an annealed polycrystalline film³¹. Although not mentioned in ref. 21, this deviation changes only slightly back over 1 h on stopping the deposition while keeping the film at room temperature. The same effect, which is due to the existence of a significant Ehrlich–Schwoebel barrier, has also been observed on Cu(111)²⁰. For our study, we, therefore, safely omit Gibbs–Thompson correction terms associated with macroscopic surface curvature variations.

The red dashed lines in Fig. 3 show the predicted stress jumps derived via equation (6) for surface terrace widths between 1 and 500 atomic spacings and the existence of an Ehrlich–Schwoebel barrier. It is striking that the obtained stress values exceed even the experimental ones (crosses), and that we receive a rather good agreement already for a terrace width with $w = 1$ atomic spacing. Please note also that the experimentally observed stress values are often above the compressive yield strength of copper, which is ~ 63 MPa (ref. 32). To get a feeling for the numbers, the top horizontal axis shows the adatom density at the end point ($w = n$) for a terrace with a width of $w = 500$ (74 nm). Note that the adatom density is $< 10^{-4}$ ML even for fluxes as high as 100 ML per s. This validates our dilute adatom gas assumption while calculating the surface CP and justifies our steady-state thermodynamic approach. Note also that it is surprising that a dilute adatom gas of $< 10^{-4}$ ML has the potential to induce ~ 1 GPa stress in the film, which is more than both the yield and the ultimate strength of copper. Please note that this stress can be realized in the bulk only, if there exists a kinetically not limited atomic mechanism that transfers the CP variation of the surface to the grain interior. The curves are calculated for Cu(111) and we have used $T = 298$ K, $\Omega = \frac{1}{4}(361.49 \text{ pm})^3$, $v_0 = 10^{12}$ Hz, $E_{\text{diff}} = 0.040$ eV (ref. 33), $s_0 = 15$ (ref. 27), $\Delta E_{\text{ES}} = 0.224$ eV (ref. 34), $\Delta E_{\text{att}} = 0$ eV ($\Delta E_{\text{att}} \approx 0$ for most metals at room temperature) and $E_{\text{form}} = 0.714$ eV (ref. 35), for our calculations, which implies an adatom equilibrium density of $\theta_{\text{eq}} = 8.6 \times 10^{-13}$ ML at zero deposition flux.

It is known that stress relaxation mechanisms are active both during the growth and after stopping the deposition, which reduce the absolute intrinsic film stress^{36–38}. Indeed, the experimental stress values (black crosses) are in general lower than the red dashed stress lines. However, if one considers that the time constant of the stress relaxation processes is distinctively larger than the time constant of the reversible jumps³⁹, the discrepancy between the observed and the predicted values for

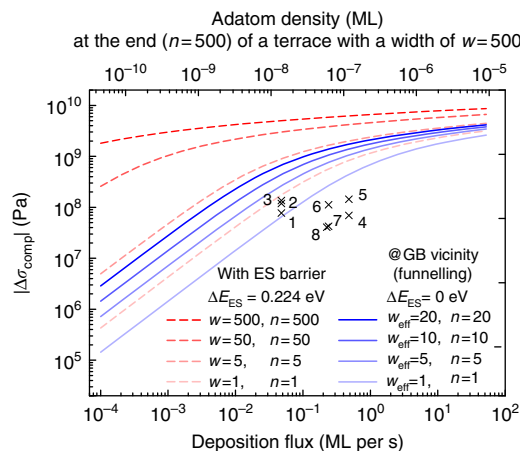


Figure 3 | Reversible stress jumps for a (111) textured copper film as a function of flux. The dashed red curves are calculated for typical terraces ($1 < w < 500$ and $\Delta E_{\text{ES}} = 0.224$ eV), whereas the solid blue curves describe terraces in the vicinity of GBs ($w_{\text{eff}} \leq 20$ and $\Delta E_{\text{ES}} = 0$ eV), where funnelling takes place. The top horizontal axis shows the adatom density for a typical surface terrace ($w = 500$ and $\Delta E_{\text{ES}} = 0.224$ eV). Crosses show experimentally reported literature values: 1, 2, 3 (ref. 8), 4 (ref. 43), 5, 6 (ref. 9), 7 (ref. 36) and 8 (ref. 44). Note that the stresses are lower, if it is easier for atoms to diffuse to and into GBs.

typical surface terraces is too large to be explained by the stress relaxation effects alone.

Stress jumps considering funnelling. As our derivation of the stress jumps exceeds in general the experimental values, we turn our attention to experiments on both Cu(111) and Ag(111) at room temperature: these experiments revealed that the Ehrlich–Schwoebel barrier of the lower step vanishes, if the distance between two neighbouring steps becomes less than six atomic spacings^{40,41}. This effect opens a fast mass transfer channel for terraces with $w \leq 5$ called funnelling. The fast mass transport region can extend up to 21 atomic sites (over five steps) away from the GB. We account for this by setting the critical terrace width to $w = 5$ and by assuming that the Zeno effect reduces the width of the subsequent terraces by one atomic spacing. With this approximations, the last six terraces next to a GB can be treated as one single terrace with an effective width of $w_{\text{eff}} \approx 20$, with $\Delta E_{\text{ES}} = 0$ ($s = 1$) (Fig. 2c, bottom). However, as intermediate step edges given by the five steps can potentially act as adatom sinks, we evaluate the stress jumps for effective terrace widths, w_{eff} , ranging 1–20 atomic spacings (see blue lines in Fig. 3). As our calculations define upper limits for the stress jumps, a funnelling width of three spacings represents the best fit. This means that it is enough, if only the last step (and not five) before the GB shows funnelling. The fact that our result with the inclusion of funnelling delivers a rather good fit with the experimental values is a strong indication for the validity of the GB insertion model, especially, as we calculate the CP on the surface exactly next to the GBs. Note, however, that we do not address the exact atomic pathway (for example, diffusion, exchange and so on), as we evaluate only the thermodynamics.

Discussion

Although we lowered the barriers for the atoms to diffuse towards and into the GB, we receive lower stresses than without funnelling. This seemingly counterintuitive behaviour demonstrates that we are not addressing a certain atomic diffusion/incorporation model, but calculate the thermodynamic driving

force on the basis of the CP. Lowering the barriers for atoms to diffuse towards and into the GB, decreases the adatom density near the GB and results in a reduction of the driving force for the atoms to diffuse into the GB. Evidently, the funnelling curves predict the correct order of magnitude for the stress levels. By setting ($s = a = 1$) in equation (4), one gets an estimate of the adatom density at the GB vicinity $n = w_{\text{eff}}$: for a deposition rate of 1 ML per s the adatom density is predicted to be lower than 10^{-10} ML.

Finally, we address another hypothetical mechanism in combination with the equilibrium situation between the surface and the bulk. For materials with a low enough Ehrlich–Schwoebel barrier and funnelling terraces, the CP distribution shows a maximum around the middle of the terrace (Fig. 2c). In addition, the CP at the end position of, for example, a large terrace in the middle of the grain (with Ehrlich–Schwoebel barrier) is significantly larger than the CPs of funnelling terraces that connect to the grain boundaries. Pure thermodynamic considerations imply that also these maxima tend to establish equilibrium with the interior of the grain underneath. As the grain is comparable to a single crystal, dislocation nucleation would be an imaginable pathway to balance the CP differences. However, on epitaxial films and single crystals the reversible stress jumps are not observed¹⁶. The reason for this is a high nucleation barrier: a critical stress of 1.3 GPa has been determined to nucleate dislocations in Cu at 300 K (ref. 42). Such high absolute stress values are neither observed experimentally nor does our model predict an equivalent rise of the surface CP (except for large terraces in combination with high deposition fluxes). Dislocation nucleation is, therefore, kinetically limited. The overall picture is that during the growth all points on the surface are in parallel trying to balance their CPs with adjacent positions, as well as with the grain underneath. However, in which way and by which rate the CP of the grains will change clearly depends on the rates of the pathways between all subsystems: surface, GB and bulk. With a significant dislocation nucleation barrier and active GB diffusion, as well as atom incorporation, the whole system quickly evolves towards equilibrium via atom insertion in GBs. As a result the CP difference between the grain and the surface CP maxima is reduced, which effectively lowers the driving force for dislocation nucleation making this latter process even less favourable.

If one intends to compare our results with experiments, it is important to realize that we determine only the pure reversible equilibrium jumps. For a proper comparison the experiments should have no kinetic limitation of atoms going in/out of the grain boundaries, should be performed long enough such that equilibrium has reached (all GBs show the equilibrium density of additional atoms), and no stress relaxation mechanisms should occur. In this limit, we expect the stress jumps to be GB density-independent. Kinetic limitations would immediately result in a GB density dependence, as equilibrium will not be reached and the rate towards equilibrium scales with the number of the pathways and hence the GB density.

The deposition flux and temperature dependence is more complex, as the growth mode (layer-by-layer, step-flow and 3D/rough growth) that determines the size of the terrace next to the GBs also changes with deposition rate and mobility. If one, for example, lowers the rate for a film that grows in 3D growth mode, one might enter step-flow growth conditions in which effective larger terraces (with higher adatom density) might communicate with the GBs, such that the stress jumps are even higher instead of lower.

Our analysis shows that entropic effects in the extremely dilute adatom gas on the surface of a polycrystalline film during vapour deposition are strong enough to cause plastic deformation in the film. The predicted film stresses are even higher than the observed

ones. If we lower the barriers for atoms to diffuse towards and into the GB by funnelling, the stresses decrease and the predicted values perfectly match the experimental ones. With this we deliver the, until now missing, thermodynamic driving force for any GB atom insertion model. Further experimental research, similar to^{15,21}, is needed to clarify the exact atomistic mechanisms and pathways behind this effect.

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Author contributions

The project was initiated and conceptualized by M.J.R. In his discussions with A.S., he pointed out the deficiencies of stress generation models at the time. Inspired by the discussions, A.S. envisioned a possible path to calculate the reversible stress analytically. Encouraged by this, the authors developed the thermodynamical description together, for which A.S. worked out the equations. Together they discussed the approach, interpreted the results and wrote the manuscript.

Additional information

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