

Electron-positron pairs in hot plasma of accretion column in bright X-ray pulsars

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ABSTRACT

The luminosity of X-ray pulsars powered by accretion onto magnetized neutron stars covers a wide range over a few orders of magnitude. The brightest X-ray pulsars recently discovered as pulsating ultraluminous X-ray sources reach accretion luminosity above 10^{40} erg s⁻¹ which exceeds the Eddington value more than by a factor of ten. Most of the energy is released within small regions in the vicinity of magnetic poles of accreting neutron star - in accretion columns. Because of the extreme energy release within a small volume accretion columns of bright X-ray pulsars are ones of the hottest places in the Universe, where the internal temperature can exceed 100 keV. Under these conditions, the processes of creation and annihilation of electron-positron pairs can be influential but have been largely neglected in theoretical models of accretion columns. In this letter, we investigate properties of a gas of electron-positron pairs under physical conditions typical for accretion columns. We argue that the process of pairs creation can crucially influence both the dynamics of the accretion process and internal structure of accretion column limiting its internal temperature, dropping the local Eddington flux and increasing the gas pressure.

Key words: accretion, accretion discs – X-rays: binaries – neutrinos – stars: neutron – radiative transfer

1 INTRODUCTION

The majority of accreting X-ray binaries is represented by the systems hosting neutron stars (NSs). Highly magnetized NSs form a special class of objects among X-ray binaries powered by accretion - X-ray pulsars (XRPs, see e.g. [Walter et al. 2015](#)). Typical magnetic field strength at the NS surface in XRP is $\gtrsim 10^{12}$ G, which is confirmed independently by a number of different methods: detection of cyclotron lines (see [Staubert et al. 2019](#) for review), transitions into the “propeller” state ([Tsygankov et al. 2016](#); [Lutovinov et al. 2017](#)), detection of spin-up and spin-down effects ([Sugizaki et al. 2017](#)). Detected luminosities of XRP cover a few orders of magnitude from 10^{33} erg s⁻¹ and up to 10^{41} erg s⁻¹, where the brightest pulsars belong to the recently discovered class of pulsating ultraluminous X-ray sources (ULXs, [Bachetti et al., 2014](#); [Israel et al., 2017](#)). The theoretical explanation of ULX pulsars is still under debates, but the most of the theories agree that the extreme

accretion onto magnetized NS results in the formation of accretion columns above the stellar surface, where the matter is confined by a strong magnetic field and produce luminosity well above the Eddington limit ([Basko & Sunyaev 1976](#); [Wang & Frank 1981](#); [Mushtukov et al. 2015a](#)).

A strong magnetic field of a NS in XRP modifies both the geometry of accretion flow (see Chapter 6 in [Frank et al. 2002](#)) and basic properties of matter ([Harding & Lai 2006](#)). Because of a strong magnetic field, the accreting material reaches NS surface in small regions (the typical area is $\sim 10^{10}$ cm²) in the vicinity of NS magnetic poles. At extremely high mass accretion rates the radiation pressure is high enough to stop accretion flow above NS surface in radiation dominated shock ([Lyubarskii & Sunyaev 1982](#); [Mushtukov et al. 2015b](#)). Below the shock, the matter slowly settles to the stellar surface converting its gravitational and kinetic energy into emission in X-ray energy band. A strong energy release within a small region results in extreme temperatures, which are typically about a few keV ([Wang & Frank 1981](#); [Mushtukov et al. 2015a](#)) and

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can be as high as about 1 MeV in the case of ULX pulsars (Mushtukov et al. 2018).

High temperatures in regions of energy release of XRP result in specific processes which might shape properties of XRPs at extreme mass accretion rates and thus have to be taken into account in theoretical models. In particular, high temperatures result in the creation of electron-positron pairs and possibly strong emission of neutrino due to pair annihilation and/or cyclotron neutrino emission (Kaminker et al. 1992, 1994; Mushtukov et al. 2018).

In this papers, we investigate properties of electron-positron gas under conditions of a strong magnetic field and high temperatures typical for internal regions of optically thick accretion columns. Under the assumption of thermodynamic equilibrium, we calculate the number density of the pairs (Section 2.1) and the gas pressure along magnetic field lines (Section 2.2). We discuss the influence of the pair creation process on internal temperature and dynamics of the accretion process.

2 ELECTRON-POSITRON PAIRS IN ACCRETION COLUMN

The accretion columns in bright XRPs are confined by a strong magnetic field and supported by the internal radiation and gas pressure (Basko & Sunyaev 1976). The conditions of matter inside the columns are determined by the local mass density and temperature. The main mechanism of opacity in accretion columns is Compton scattering of photons by electrons/positrons influenced by a strong magnetic field. Because the accretion column is optically thick due to the scattering, the photons created in the accretion flow undergo a number of scatterings before they leave the column. A fraction of radiation is truly absorbed while the photons diffuse towards the edges of the accretion channel.

Let consider a case of fully ionized hydrogen plasma. A number density of protons n_p is determined by the mass accretion rate \dot{M} , cross section of the accretion channel S and local velocity $v = \beta c$ of accretion flow

$$n_p \approx \frac{\dot{M}}{2Sv m_p} \simeq 10^{23} \frac{\dot{M}_{20}}{S_{10}\beta} \text{ cm}^{-3}, \quad (1)$$

where $\dot{M}_{20} = \dot{M}/10^{20} \text{ g s}^{-1}$ and $S_{10} = S/10^{10} \text{ cm}^2$. Because the typical geometrical thickness of accretion column is of order of $d \sim 10^4 \text{ cm}$, the optical thickness of the column across magnetic field lines due to the scattering can be estimated as $\tau_{\perp} \gtrsim n_p \sigma_{\perp} d \simeq 6.7 \times 10^2 \dot{M}_{20} S_{20}^{-1} \beta^{-1} (\sigma_{\perp}/\sigma_T)$, where σ_{\perp} is a scattering cross section across B -field lines and σ_T is the Thomson cross section. The number of scattering experienced by photon in accretion column is

$$N_{sc} \sim \tau_{\perp}^2 \approx 4.4 \times 10^5 \frac{\dot{M}_{20}^2}{S_{20}^2 \beta^2} \left(\frac{\sigma_{\perp}}{\sigma_T} \right)^2. \quad (2)$$

The absorption cross section can be roughly estimated as $\sigma_a \simeq 23.7 \sigma_T Z^4 (E/1 \text{ keV})^{-3}$, where Z is the atomic number, E is a photon energy (Bethe & Salpeter 1957). The accreting material is slowing down from a free-fall velocity v_{ff} to about $v_{ff}/10$ in the radiation dominated shock at the top of accretion column. Thus, the velocity below the shock region can be estimated from above as $v < 0.05c$ and a typical number of absorption events corresponding to a given number of

scatterings can be estimated as

$$N_a \sim N_{sc} \frac{\sigma_a}{\sigma_{\perp}} \approx 30 \frac{\dot{M}_{20}^2 Z^4}{S_{20}^2 (\beta/0.05)^2} \left(\frac{\sigma_{\perp}}{\sigma_T} \right) \left(\frac{E}{511 \text{ keV}} \right)^{-3}. \quad (3)$$

The estimated number of absorption events will be even larger if one will account for the actual chemical composition of accreting material, which is affected by nuclear reactions in accretion column. In particular, for the case of carbon dominated material $Z \simeq 6$ and an estimated number of absorption events (3) increases by a factor of $\sim 10^3$. Thus, the photons emitted in the accretion column will be likely absorbed on their way to the edges of the accretion channel in the case of sufficiently large mass accretion rates. Under these conditions, the gas of electron/positron pair can be considered to be in thermodynamic equilibrium (Bisnovatyi-Kogan et al. 1971). It worth to note that the outer layers of the accretion column might be far from thermodynamic equilibrium and more detailed analyses accounting for detailed balance between a number of processes is required (see e.g. Guilbert & Stepany 1985).

Another essential condition for establishing of the equilibrium concentrations and distributions of electrons and positrons is sufficiently long dynamical time scale in accretion column: the dynamical time scale has to be longer than the time scale required for equilibrium establishing. Because the annihilation cross section is of order of $\sigma_{ann} \sim 10^{-24} \text{ cm}^2$ (see e.g. Daugherty & Bussard 1980) and typical velocity of electrons and positrons are of order of speed of light at temperatures $> 50 \text{ keV}$, the time scale of equilibrium establishing can be estimated as

$$t_{eq} \lesssim \frac{1}{\sigma_{ann} n_p c} \lesssim 3 \times 10^{-10} \frac{S_{10}\beta}{\dot{M}_{20}} \text{ s},$$

while the dynamical time scale in the column can be estimated as

$$t_{dyn} \sim \frac{R}{\beta c} \approx 3 \times 10^{-5} \beta^{-1} \text{ s}.$$

Thus, the time scale of equilibrium establishing is much smaller than the dynamical time scale ($t_{eq} \ll t_{dyn}$) and pairs in the central parts of accretion column can be considered to be in the equilibrium.

2.1 Number density of electrons and positrons

At low temperature regime, the number density of electrons is similar to the number density of protons $n_- \simeq n_p$, while at high temperature regime, the creation of electron-positron pairs becomes essential and the number density of leptons (both electrons and positrons) can significantly exceed the number density of protons. The number density of electrons n_- and positrons n_+ in the equilibrium are given by (Canuto & Chiu 1968; Kaminker et al. 1992)

$$\begin{aligned} n_{\mp} &= \left(\frac{mc}{\hbar} \right)^3 \frac{b}{4\pi^2} \sum_{n=0}^{\infty} g_n \int_{-\infty}^{\infty} dp_z f_{\mp} \\ &\approx 4.415 \times 10^{29} b \sum_{n=0}^{\infty} g_n \int_{-\infty}^{\infty} dp_z f_{\mp} \text{ cm}^{-3}, \end{aligned} \quad (4)$$

where $b = B/B_{crit}$ is dimensionless magnetic field strength, $B_{crit} \equiv m_e^2 c^2 / e \hbar \simeq 4.412 \times 10^{13} \text{ G}$, the distribution functions

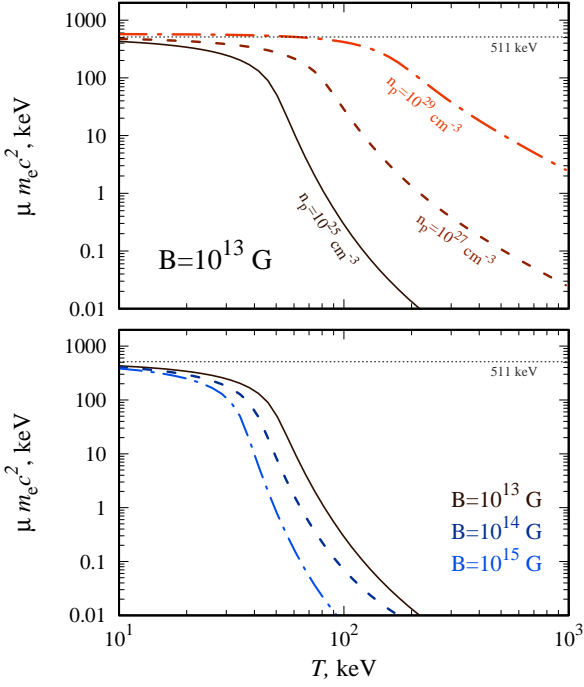


Figure 1. The chemical potential of electrons calculated as a function of temperature for different number densities of protons at fixed magnetic field strength 10^{13} G (top panel), and for different magnetic field strength at fixed number density of protons $n_p = 10^{25}$ cm^{-3} (bottom panel).

of particles

$$f_{\mp} = \left(\exp \left[\frac{E_n(p_z) \mp \mu}{t} \right] + 1 \right)^{-1}, \quad (5)$$

dimensionless energy $E_n(p_z) = (1 + p_z^2 + 2bn)^{1/2}$ of electron/positron at n th Landau level, dimensionless temperature $t \equiv T/(m_e c^2)$, g_n is the spin degeneracy of Landau level ($g_0 = 1$ and $g_n = 2$ for $n \geq 1$), and the dimensionless (in units of $m_e c^2$) chemical potential μ is determined by the condition of electro-neutrality $n_- - n_+ = n_p$.

In the limit of zero magnetic field and relatively low temperatures ($T \ll m_e c^2$) the number densities of electrons and positrons can be estimated as (Zeldovich & Novikov 1971)

$$\begin{aligned} n_+ \simeq n_- &\simeq \frac{1}{\pi^2} \left(\frac{m_e c}{\hbar} \right)^3 e^{-1/t} t^{3/2} \\ &\simeq 1.8 \times 10^{30} e^{-1/t} t^{3/2} \text{ cm}^{-3}, \end{aligned} \quad (6)$$

while at high temperatures ($T \gg m_e c^2$) the approximations is given by

$$n_+ \simeq n_- \simeq \frac{1.82}{\pi^2} \left(\frac{m_e c}{\hbar} \right)^3 t^3 \simeq 3.2 \times 10^{30} t^3 \text{ cm}^{-3}. \quad (7)$$

The calculations with the accurate equations (4) and (5) give a result which depends both on number density of protons and magnetic field strength (see Fig. 1,2). Influence of a strong magnetic field on the chemical potential and number density of electron-positron pairs becomes valuable at $B \gtrsim 10^{13}$ G. At lower B -field strength and temperature

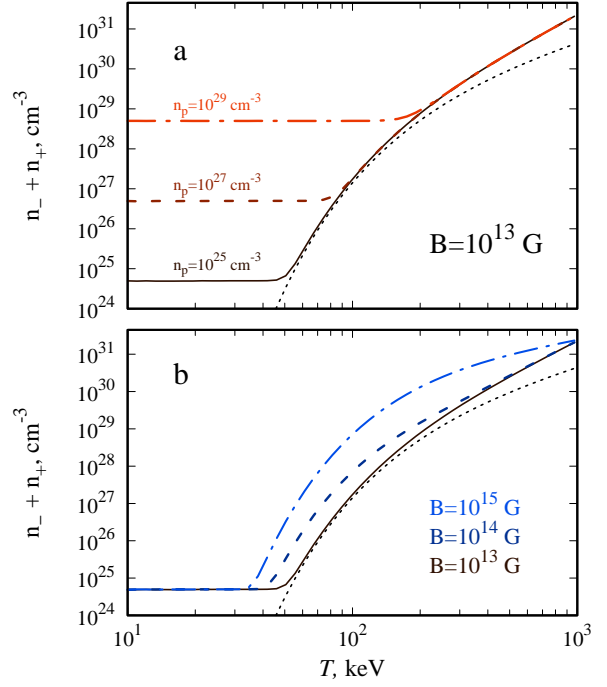


Figure 2. Number density of electrons and positrons as a function of temperature calculated for (a) different number densities of protons: 10^{25} (black solid line), 10^{27} (brown dashed line) and 10^{29} cm^{-3} (red dashed-dotted line), and (b) different magnetic field strength: 10^{13} (black solid line), 10^{14} (dark-blue dashed line) and 10^{15} G (blue dashed-dotted line). Black dotted line represents approximation given by (6).

$T \gtrsim 10$ keV, the chemical potential and number density of the pairs can be calculated in approximation of zero field strength. In the case of low number density of protons n_p , the contribution of created electron-positron pairs to the total number density of leptons is dominant at temperatures of a few tens of keV already (see Fig. 2a), which is typical temperature for accretion column interior (Mushtukov et al. 2015a). Note, that the stronger the magnetic field, the larger the number density of electron-positron pairs (see Fig. 2b).

The fast increase of a number density of electron-positron pairs with temperature requires that a fraction of energy of accreting material is going into a process of pair creation. Because the energy budget of the accretion process is limited by the mass accretion rate and compactness of a NS, the process of pairs creation limits the increase of internal temperature in the accretion column. The upper limit of a number density of the pairs can be obtained from the assumption that the energy of accretion flow is going entirely in a pair creation. The total energy budget per one baryon due to the accretion process is determined by local free-fall velocity: $(\gamma_{\text{ff}} - \gamma)m_p c^2$ where $\gamma_{\text{ff}} = (1 - \beta_{\text{ff}}^2)^{-1/2}$ is the Lorentz factor due to a local free-fall velocity and γ is actual Lorentz factor of accreting material at a given height above stellar surface. Then the number density of the pairs, which is similar to the number density of positrons n_+ in accretion flow, can be limited from above by

$$(\gamma_{\text{ff}} - \gamma)m_p n_p > 2m_e n_+. \quad (8)$$

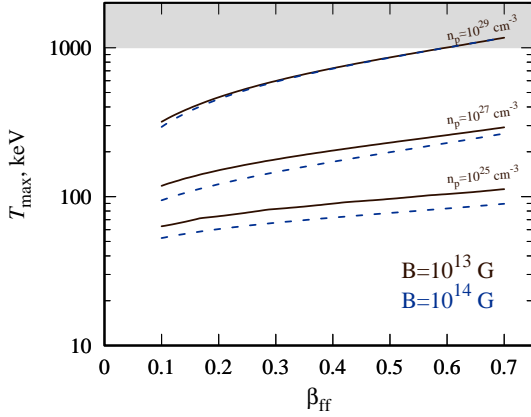


Figure 3. The maximal temperature achievable in accretion column as a function of local dimensionless free fall velocity β_{ff} . Different curves are given for various number density of protons in the accretion flow: $n_p = 10^{25}$, 10^{27} and 10^{29} cm^{-3} (down up). Black solid and dark-blue dashed line correspond to local magnetic field strength of 10^{13} and 10^{14} G respectively. At temperatures above ~ 1 MeV (grey area) the energy losses are strongly affected by neutrino emission.

Thus, a conservative upper limit for the number density of pairs is

$$n_{+, \text{max}} \leq \frac{n_p}{2} \frac{m_p}{m_e} (\gamma_{\text{ff}} - 1). \quad (9)$$

The maximal number density of pairs determines the maximal temperature T_{max} achievable at a given local free-fall velocity β_{ff} and number density of protons (see Fig. 3). One can see that the temperatures of a few hundred keV in accretion channel are achievable only in the case of sufficiently high densities (see Fig. 3).

2.2 Gas and radiation pressure in accretion column

The gas pressure along z -direction due to the electron and positrons can be derived from the distribution function of the particles:

$$P_{z, \text{ee}^+} = \frac{m_e^4 c^5}{\hbar^3} \frac{b}{4\pi} \sum_{n=1}^{\infty} g_n \int_{-\infty}^{\infty} dp_z \beta_z p_z [f_- + f_+] \quad (10)$$

where the dimensionless velocity along z axis $\beta_z = p_z \gamma^{-1} = p_z (1 + p_z^2 + 2bn)^{-1/2}$. Expression (10) can be rewritten as

$$P_{z, \text{ee}^+} \simeq 3.5 \times 10^{23} b \times \sum_{n=0}^{\infty} g_n \int_0^{\infty} dp_z \frac{p_z^2 [f_-(p_z) + f_+(p_z)]}{(1 + p_z^2 + 2bn)^{1/2}} \text{ dyn cm}^{-2}. \quad (11)$$

The results of calculations with equation (11) are given in Fig. 4. At low temperatures, when the effects of pair creation are negligible and $P \propto T$, then the pressure increases rapidly with the increase of the number density of electron-positron pairs. In the limiting case of high temperatures, $P \propto T^4$ and the gas pressure becomes very close to the radiation

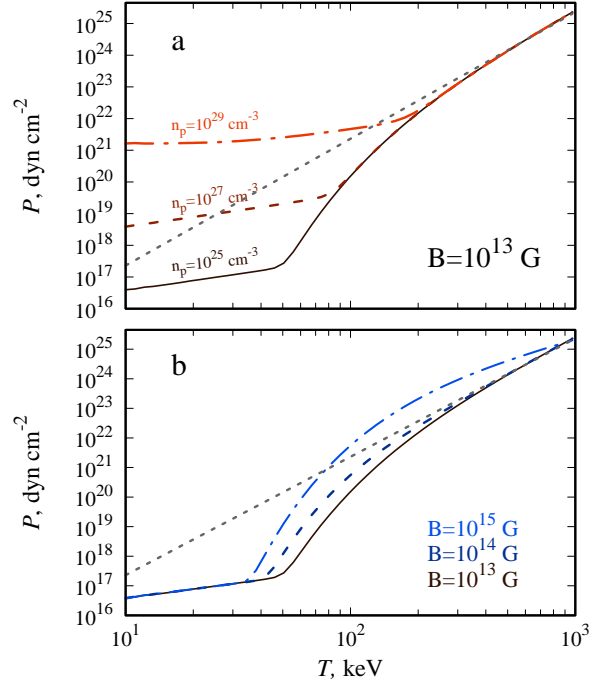


Figure 4. The pressure of electron-positron gas along magnetic field lines calculated as a function of temperature for (a) different number densities of protons: 10^{25} (black solid line), 10^{27} (brown dashed line) and 10^{29} cm^{-3} (red dashed-dotted line), and (b) different magnetic field strength: 10^{13} (black solid line), 10^{14} (dark-blue dashed line) and 10^{15} G (blue dashed-dotted line). Black dotted line represents radiation pressure calculated according to (12).

pressure, which is given in the equilibrium by

$$P_{\text{rad}} = \frac{1}{3} a T^4 \simeq 4.6 \times 10^{13} T_{\text{keV}}^4 \text{ dyn cm}^{-2}, \quad (12)$$

where a is the radiative constant.

2.3 The Eddington flux affected by electron-positron pairs

The Eddington flux is the photon energy flux which is high enough to compensate the gravitational attraction of the central object. The Eddington flux plays a key role in the theory of super-Eddington accretion onto compact objects and particularly in the theory of the accretion column in bright XRP (Basko & Sunyaev 1976; Wang & Frank 1981; Mushtukov et al. 2015a). The Eddington flux is given by

$$F_{\text{Edd}} = \frac{\rho c}{(n_- + n_+) \sigma_{\text{eff}}} \frac{GM}{r^2} = \mu_e \frac{m_p c}{\sigma_{\text{eff}}} \frac{GM}{r^2}, \quad (13)$$

where σ_{eff} is the effective cross section, which is affected by a strong magnetic field and local energy spectrum of photons, and the mean molecular weight is

$$\mu_e \simeq \frac{1}{1836} \frac{1837 n_p + 2 n_+}{n_p + 2 n_+}. \quad (14)$$

The temperature increase and the corresponding increase of electron/positron number density result in a drop of the

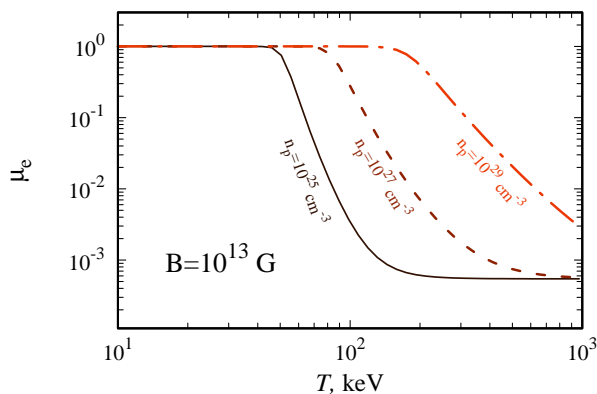


Figure 5. The mean molecular weight as a function of temperature for different number densities of protons: 10^{25} (black solid line), 10^{27} (brown dashed line) and 10^{29} cm^{-3} (red dashed-dotted line) at magnetic field strength fixed at 10^{13} G .

mean molecular weight (see Fig. 5). This affects the local Eddington flux and can principally make it smaller by more than 3 orders of magnitude. The accurate calculations of the Eddington flux require accounting for special features of Compton scattering in a strong magnetic field (see e.g. Herold 1979; Daugherty & Harding 1986; Mushtukov et al. 2016), which is behind the scope of this letter.

3 SUMMARY AND DISCUSSION

We have investigated properties of electron-positron gas in accretion columns of bright X-ray pulsars accounting for specific physical conditions of a strong magnetic field and high temperatures. Because of a large optical thickness of accretion column due to Compton scattering, the gas of electron-positron pairs can be considered to be close to the thermodynamic equilibrium in the central parts of accretion column at high mass accretion rates typical for recently discovered ULX pulsars. However, in the outer parts accretion column the gas of pairs can be far from the equilibrium and its conditions has to be obtained from kinetic equations accounting for a number of processes (see e.g. Guilbert & Stepney 1985).

We have demonstrated that the process of pair creation might have key importance in extreme accretion onto magnetized NSs influencing the dynamical and temperature structure of accretion columns. In the case of high velocity of the accretion flow and relatively low mass density, the number density of pairs becomes comparable to the number density of protons at temperatures of about a few tens of keV already (see Fig. 2). Because the energy budget of the accretion process is limited, the process of pair creation puts an upper limit on the internal temperature of the accretion column (see Fig. 3) and, therefore, on the energy losses due to neutrino production (Mushtukov et al. 2018). The temperatures of a few hundred keV are achievable only in the case of the sufficiently high mass density of material in the accretion channel and only in the very vicinity of a NS surface. The electron-positron pairs affect the gas pressure, which becomes comparable to the radiation pressure at temperatures $\gtrsim 100 \text{ keV}$ (see Fig. 4). The process of pair creation

reduces the mean molecular weight of the accreting material (see Fig. 5) and, thus, drops the Eddington flux, which supports accretion columns. According to our knowledge, these effects were largely neglected in the models of accretion columns developed up to date and have to be taken into account in further numerical models.

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