# A stellar census in globular clusters with MUSE <br> Extending the CaT-metallicity relation below the horizontal branch and applying it to multiple populations 

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#### Abstract

Aims. We use the spectra of more than 30,000 red giant branch (RGB) stars in 25 globular clusters (GC), obtained within the MUSE survey of Galactic globular clusters, to calibrate the $\mathrm{Ca}_{\text {II }}$ triplet $(\mathrm{CaT})$ metallicity relation and derive metallicities for all individual stars. We investigate the overall metallicity distributions as well as those of the different populations within each cluster. Methods. The Ca II triplet in the near-infrared at 8498,8542 , and $8662 \AA$ is visible in stars with spectral types between F and M and can be used to determine their metallicities. In this work, we calibrate the relation using average cluster metallicities from literature and MUSE spectra, and extend it below the horizontal branch - a cutoff that has traditionally been made to avoid a non-linear relation - using a quadratic function. In addition to the classic relation based on $V-V_{\mathrm{HB}}$ we also present calibrations based on absolute magnitude and luminosity. The obtained relations are then used to calculate metallicities for all the stars in the sample and to derive metallicity distributions for different populations within a cluster, which have been separated using so-called "chromosome maps" based on HST photometry. Results. We show that, despite the relatively low spectral resolution of MUSE ( $R=1900-3700$ ) we can derive single star metallicities with a mean statistical intra-cluster uncertainty of $\sim 0.12$ dex. We present metallicity distributions for the RGB stars in 25 GCs, and investigate the different metallicities of the populations P3 (and higher) in so-called metal-complex or Type II clusters, finding metallicity variations in all of them. We also detected unexpected metallicity variations in the Type I cluster NGC 2808 and confirm the Type II status of NGC 7078.


Key words. methods: data analysis, methods: observational, techniques: imaging spectroscopy, stars: abundances, globular clusters: general

## 1. Introduction

Over the last two decades, the Hubble Space Telescope (HST) has been a game-changer in the research of globular clusters (GCs). Not only did it open the window to an unprecedented view into the crowded centres of the clusters, which today allows us to derive detailed proper motions for single stars (Bellini et al. 2014), but it also provided stellar magnitudes (Sarajedini et al. 2007; Nardiello et al. 2018a) with a precision sufficient to distinguish complex structures in the CMDs of globular clusters.

After early findings of a bimodal main sequence (MS) in the colour-magnitude diagram (CMD) of $\omega$ Centauri (Anderson 1997; Bedin et al. 2004), splits on the MSs, the subgiant (SGB) and red giant branches (RGBs), and even on the asymptotic giant branches and horizontal branches (HBs) have been found for several clusters (see, e.g., Gratton et al. 2012; Piotto et al. 2013; Marino et al. 2014; Milone et al. 2015a). According to most recent studies, it appears that nearly all GCs (older than about 2 Gyrs) show structures in their CMD suggesting the presence of

[^0]multiple groups of stars that are usually referred to as different generations or populations (Milone et al. 2017). The presence of these multiple populations has been further supported by spectroscopic results, especially by the discovery of light element variations that have been observed in all investigated clusters, emerging in the form of anti-correlations of elemental abundances, e.g. Na-O and Mg-Al (Carretta et al. 2010a).

Most of the scenarios proposed to explain these observations are built on the assumption of "self-enrichment" of the interstellar medium and multiple star formation events, thus explaining the use of the term generations. Possible candidates for the polluters range from massive asymptotic giant branch stars (D'Ercole et al. 2010) to fast rotating massive stars (Decressin et al. 2007) to interacting massive binary stars (de Mink et al. 2009). However, Bastian et al. (2015) showed that none of these scenarios alone can reproduce the observed abundance trends in all GCs.

Milone et al. (2015b) showed that a pseudo-CMD, constructed from two peusdo-colours calculated by combining four filters covering wavelength ranges from the near-UV to the op-
tical, allows the different populations to be easily separated, at least on the RGB and along the lower MS. These pseudo-CMDs are commonly referred to as chromosome maps. For the majority of the globular clusters investigated by Milone et al. (2017), the authors divided the clusters' RGB stars into two populations. They called the bulk of stars near the origin of the chromosome map the first generation stars, and all the others, usually extending above, the second generation stars. We will refer to them as populations 1 ( P 1 ) and $2(\mathrm{P} 2)$. The stars belonging to the P 1 populations show a normal abundance pattern while the other stars have a chemistry showing signs of processing such as enhanced Na abundances (see, e.g., Marino et al. 2019a).

Additionally, Milone et al. (2017) identified more than two populations in some of the clusters in their sample. These clusters were referred to as Type II or metal-complex (as compared to the Type I clusters containing only 2 populations). The Type II clusters show a split in their subgiant branch in both optical and UV CMDs and the faint SGB connects with a red-RGB. The stars belonging to the red-RGB form one, or sometimes more, additional population(s). The stars belonging to this additional population (that we will refer to as P3) have been investigated in a few clusters and some of them appear to be enriched in iron, s-process elements, and some also in their $\mathrm{C}+\mathrm{N}+\mathrm{O}$ abundances (e.g., Marino et al. 2018, 2015; Yong et al. 2014b). A few other clusters, although not identified as Type II, also have additional populations that were investigated with the help of their chromosome map. For example, previous studies have identified five populations in NGC 2808 and NGC 7078 (Milone et al. 2015b; Nardiello et al. 2018a). Although variations in metallicity have not been reported so far in Type I clusters, the presence of an iron-spread has been suggested to explain the extension of the P1 stars in the chromosome map of some GCs (Milone et al. 2015b; Marino et al. 2019a). However, whether iron or helium variations are responsible for the colour spread of the P1 stars is still a matter of debate (see e.g., Lardo et al. 2018; Milone et al. 2018). A more detailed investigation of metallicities in globular clusters would certainly help to constrain the possible formation scenarios of their multiple populations.

The common way of deriving metallicities from observed medium resolution spectra is to compare them with models (see, e.g., Husser et al. 2016). However, it is useful to have an alternative method available that is independent of model assumptions and only relies on observations. One of these alternatives is the infrared Ca il triplet (CaT) lines at 8498, 8542, and $8662 \AA$, which is often used as a proxy for metallicity measurements. These three lines are among the most prominent features in the spectra of G, K, and M stars (Andretta et al. 2005) and are easily visible even on low resolution or noisy stellar spectra.

Armandroff \& Zinn (1988) analysed the integrated-light spectra of GCs and found that the measured EWs of the CaT lines strongly correlate with the cluster metallicity $[\mathrm{Fe} / \mathrm{H}]$. Building on this result, Armandroff \& Da Costa (1991) focused on individual RGB stars and revealed an additional dependence between EWs and brightness. Plotting their EWs as function of the magnitude difference to the $\mathrm{HB}, V-V_{\mathrm{HB}}$, they found that the intercepts of the linear fit with the ordinate, which they called the reduced equivalent width $\left(W^{\prime}\right)$, nicely correlate with the metallicity. Studies using the CaT to infer metallicities usually only include RGB stars brighter than the HB (Da Costa et al. 2009) and use a linear relation between the measured EWs and $W^{\prime}$. Since this excludes a large amount of RGB stars, Carrera et al. (2007) suggested to use a quadratic relation and include all stars on the RGB.

In this paper, we combine stellar metallicities, derived from the CaT-metallicity relation, with chromosome maps to investigate the metallicity distributions of the populations within GCs. To achieve this, we use a homogeneous sample of RGB spectra obtained as part of the MUSE survey of Galactic globular clusters. We first calibrate the CaT-metallicity relation using the spectra of RGB stars in 19 GCs and provide a calibration that extends below the HB as well as calibrations based on absolute magnitude and luminosity. We then use these relations to derive metallicities for more than 30000 RGB stars in our total sample of 25 GCs and investigate the metallicity distribution of these clusters. Finally, 21 clusters in our sample have the necessary photometric data to create chromosome maps. For these, we also obtain the metallicity distributions of their individual populations. Our approach is valid as long as the Ca abundances $[\mathrm{Ca} / \mathrm{Fe}]$ do not vary from star to star. This is not expected for Type I clusters, and indeed Marino et al. (2019a) found no significant Ca variation between the P1 and P2 stars. However, for at least two Type II clusters, namely NGC 5139 ( $\omega$ Centauri) and NGC 6715 (M 54, not in our sample), they found an increase in Ca from the blue- to the red-RGB stars. We note that $\omega$ Centauri is not used for the calibration of the CaT-metallicity relation, and our approach should not be affected by changes in Ca abundances. Another Type II cluster with reported variations is NGC 6656 (M 22, see Lee et al. 2009a; Marino et al. 2011).

The paper is organized as follows. We first describe the observations and the data reduction in Sect. 2. The process of creating chromosome maps from HST photometry is discussed in Sect. 3. The measurements of EWs, the CaT calibration itself and its extension below the HB is presented in Sect. 4. Section 5 gives a general overview of the metallicity distributions for all clusters, while in Sect. 6 we investigate on the possibility of a metallicity trend within the primordial populations of the clusters. Finally, Sect. 7 includes short discussions on the results for all 25 individual clusters in our sample and we briefly conclude in Sect. 8.

All the results from this paper are available as tables in VizieR and on our project homepage ${ }^{1}$, containing columns for cluster names, star IDs, RA/Dec coordinates, the measured EWs of the CaT lines (both from Voigt profiles and from simple integration), the derived reduced equivalent widths, and the final metallicities, relative to their respective cluster means.

## 2. Observations and data reduction

Within the guaranteed time observations for MUSE, we are currently carrying out a massive spectroscopic survey (PI: S. Dreizler, S. Kamann) of 29 GCs in the Milky Way and beyond. The survey itself, the obtained data, and the following data reduction are discussed in detail in Kamann et al. (2018). However, more observations have been carried out after that publication, so the current study includes all data taken until September 2018.

The data analysis was performed using a procedure similar to the one described in Husser et al. (2016). After a basic reduction using the standard MUSE pipeline (Weilbacher et al. 2012, 2014) we extracted the spectra from the MUSE data cubes using PampelMuse ${ }^{2}$ (Kamann et al. 2013). For this step we need catalogs from high resolution photometry for the positions and magnitudes of the stars, and, where possible, we used data from the ACS survey of Galactic globular clusters (Sarajedini et al. 2007; Anderson et al. 2008). For some of our clusters these were

[^1]Table 1. Overview of observed RGB stars in the MUSE survey for the 25 GCs investigated in this paper.

| NGC | Name |  |  |  |
| ---: | :--- | ---: | ---: | ---: |
| $(1)$ | RGB |  |  |  |
| $(2)$ | $(3)$ | Valid <br> $(4)$ | $V-V_{\mathrm{HB}}<0.2$ <br> $(5)$ |  |
| 104 | 47 Tuc | 2587 | 2538 | $354(13.9 \%)$ |
| 362 |  | 1236 | 1144 | $237(20.7 \%)$ |
| 1851 |  | 1454 | 1358 | $273(20.1 \%)$ |
| 1904 |  | 454 | 430 | - |
| 2808 |  | 2788 | 2512 | $713(28.4 \%)$ |
| 3201 |  | 139 | 137 | $41(29.9 \%)$ |
| 5139 | $\omega$ Cen | 1485 | 1421 | - |
| 5286 |  | 1376 | 1153 | $212(18.4 \%)$ |
| 5904 | M 5 | 937 | 870 | $198(22.8 \%)$ |
| 6093 |  | 1315 | 1071 | $248(23.2 \%)$ |
| 6218 | M 12 | 245 | 236 | - |
| 6254 | M 10 | 439 | 399 | $90(22.6 \%)$ |
| 6266 | M 62 | 2314 | 2191 | - |
| 6293 |  | 230 | 168 | - |
| 6388 |  | 4668 | 4098 | $741(18.1 \%)$ |
| 6441 |  | 4978 | 4408 | $1047(23.8 \%)$ |
| 6522 |  | 536 | 481 | - |
| 6541 |  | 910 | 820 | $135(16.5 \%)$ |
| 6624 |  | 581 | 539 | $72(13.4 \%)$ |
| 6656 | M 22 | 423 | 397 | $83(20.9 \%)$ |
| 6681 | M 70 | 344 | 327 | $71(21.7 \%)$ |
| 6752 |  | 578 | 539 | $82(5.2 \%)$ |
| 7078 | M 15 | 1685 | 1318 | $337(25.6 \%)$ |
| 7089 | M 2 | 1908 | 1727 | $377(21.8 \%)$ |
| 7099 | M 30 | 341 | 290 | $71(24.5 \%)$ |
| Total |  | 33951 | 30572 | $5382(17.6 \%)$ |

Notes. (1) NGC number. (2) Alternative identifier (if any). (3) Total number of observed RGB stars, (4) of which have valid EW measurements, (5) of which are brighter than the HB (percentage relative to column 4).
not available and a list of additional photometry that we used is listed in Kamann et al. (2018). The extraction yields spectra with the wavelength ranging from 4750 to $9350 \AA$, a spectral sampling of $1.25 \AA$ and a resolution of $2.5 \AA$, which is equivalent to $R \approx 1900-3700$.

For each cluster in our sample we found an isochrone from Marigo et al. (2017) matching the HST photometry by Sarajedini et al. (2007). This photometry has already been used before for the extraction process, so it is readily available. Values for effective temperatures $\left(T_{\text {eff }}\right)$ and surface gravities $(\log g)$ were obtained by finding the nearest neighbour for each star on the isochrone in the CMD. Using these values, template spectra were taken from the Göttingen Spectral Library ${ }^{3}$ of PHOENIX spectra and then used for performing a cross-correlation on each spectrum, yielding a radial velocity ( $v_{\mathrm{rad}}$ ). These results were used as initial guesses for a full-spectrum fit with spexxy ${ }^{4}$ using the grid of PHOENIX spectra, yielding final values for $T_{\text {eff }}$, $[\mathrm{Fe} / \mathrm{H}]$, and $v_{\mathrm{rad}}$. The surface gravity was taken from the comparison with the isochrone due to problems with fitting $\log g$ from low-resolution spectra.

Two of our clusters, namely NGC 6388 and NGC 6441, are almost twins in many regards (see, e.g., Bellini et al. 2013; Tailo et al. 2017), with both being old, massive, metal-rich bulge clus-

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Fig. 1. In the upper panel the chromosome map of NGC 1851 is shown with the three identified populations marked in different colours ((see text in Sect. 3 for explanation). The same colour-coding is used for the colour-magnitude diagram in the lower panel, where the populations can also easily be distinguished.
ters. Anderson et al. (2008) comment on the difficulties when creating the catalogs due to blending in the crowded centers, especially at absolute magnitudes about -12.5 mag in F606W and F814W. Probably as a result, we see extremely broadened main sequences and giant branches in the CMDs of both clusters, which make further analyses challenging.

In order to get high signal-to-noise spectra for each star, we combined all the spectra that we obtained for a single star. During the full-spectrum fit, spexxy also fits a model for the telluric absorption lines and a polynomial that, multiplied with the model spectrum, best reproduce the observed spectrum. This polynomial eliminates the effects of reddening and ensures that we fit only spectral lines and not the continuum, which is therefore completely ignored during the fit. Before combining the individual spectra, we first removed the tellurics and divided the spectra by the polynomial in order to get rid of a wavy structure that we sometimes observe in MUSE spectra. Finally, we co-add the individual raw spectra with their respective signal-to-noise ratios as weights.

We selected the RGB stars for this study by manually drawing a corresponding region into the CMD of each cluster. Furthermore, we determined membership of the stars to the cluster using $[\mathrm{Fe} / \mathrm{H}]$ and $v_{\text {rad }}$ from the full-spectrum fits (see Kamann et al. 2018), and removed non-members from the sample. The total number of observed RGB stars per cluster is given in col-

Table 2. Line and continuum bandpasses from Carrera et al. (2007).

| Line bandpasses | Continuum bandpasses |
| :---: | :---: |
| $8484-8513 \AA$ | $8474-8484 \AA$ |
| $8522-8562 \AA$ | $8563-8577 \AA$ |
| $8642-8682 \AA$ | $8619-8642 \AA$ |
|  | $8700-8725 \AA$ |
|  | $8776-8792 \AA$ |

umn (3) of Table 1, adding up to a full sample of almost 34,000 stars.

Cenarro et al. (2001) suggested that the best targets for a CaT analysis are stars with spectral types between F5 ( $T_{\text {eff }} \approx$ 6500 K ) and M2 ( $T_{\text {eff }} \approx 3700 \mathrm{~K}$ ). We used only stars within this given temperature range, according to the effective temperatures derived from our full-spectrum fits as described in Husser et al. (2016). We also excluded the very brightest stars with $V-V_{\mathrm{HB}}<$ -3 or $\log L / L_{\odot}>\sim 3$ (depending on the cluster). Column (4) of Table 1 gives the numbers of remaining stars, for which we obtained a valid EW measurement (see Sect. 4.1).

## 3. Chromosome maps

The pseudo-two-colour diagrams introduced by Milone et al. (2015a,b) and then termed as chromosome map (Milone 2016) proved to be an optimal way to distinguish the various populations of a given RGB of a GC. These maps are built using a combination of HST filters ( $F 275 W, F 336 W, F 438 W$, and $F 814 W$ ) that are sensitive to spectral features affected by the chemical variations that characterize the different populations (see e.g. Milone et al. 2018).

The details for creating the chromosome maps used in this study are described in Latour et al. (2019), but we will summarize it here. We use the astrophotometric catalogues presented by Nardiello et al. (2018a) that are part of the HST UV Globular cluster Survey (HUGS, see Piotto et al. 2015). First, we clean the data, then we construct the chromosome maps following the approach described in Milone et al. (2017). For doing this, we create two CMDs using the F814W magnitude and the two pseudo-colours $\Delta \mathrm{G}_{\mathrm{F} 275 \mathrm{~W}-\mathrm{F} 814 \mathrm{~W}}$ and $\Delta \mathrm{C}_{\mathrm{F} 275 \mathrm{~W}-2 \cdot \mathrm{~F} 336 \mathrm{~W}+\mathrm{F} 438 \mathrm{~W}}$. Then both CMDs are verticalized using red and blue fiducial lines (i.e. they are stretched and shifted so that these fiducial lines become straight vertical lines), and the results are combined to become the chromosome map. Figure 1 shows the chromosome map and the corresponding CMD for the Type II cluster NGC 1851, using the same colours for the three populations in both panels. Although the populations are defined in the chromosome map, they also separate nicely in the CMD.

In order to use the chromosome maps with our data, we had to match the ACS catalogue (Sarajedini et al. 2007) used for identifying our stars, with the HUGS catalogue. Some stars could not be unambiguously identified in both catalogues and thus were not used for the multiple populations study.

## 4. Calibrating the CaT-metallicity relation

### 4.1. Measuring equivalent widths

In the past, different functions have been used for fitting the Ca lines. While, for instance, Armandroff \& Da Costa (1991) used Gaussians, Cole et al. (2004) found that for high metallicities, these deviate strongly from the real line shapes due to strong


Fig. 2. Three example spectra with $\mathrm{S} / \mathrm{N} \approx 50$ from different clusters covering the whole range of metallicities in our sample. The observed spectra are shown in black, overplotted with the best fitting Voigt profiles. The areas marked in yellow were used for the continuum correction, while those in blue define the line bandpasses that were used for fitting the Voigt profiles and calculating the equivalent widths. The given metallicities are mean cluster metallicities from Dias et al. (2016).
damping wings. As an alternative they suggested the sum of a Gaussian and a Lorentzian, which was adopted by many later studies (see, e.g., Carrera et al. 2007; Gullieuszik et al. 2009). Saviane et al. (2012) distinguished between low and high metallicity clusters and fitted Gaussians and Gaussian+Lorentzians, respectively. We found a problem with this approach for spectra with relatively low signal-to-noise, in which case often a broad Lorentzian just fitted the noise. Rutledge et al. (1997) and others used a Moffat function. We decided to adopt the method from Yong et al. (2016) and used Voigt profiles, representing the convolution of the thermal and pressure broadening.

In order to fit profiles to the lines, we need to define the bandpasses first, for both the lines and the pseudo-continuum, which will be used for normalizing the spectra. Carrera et al. (2007) compared the bandpasses given by Armandroff \& Zinn (1988), Rutledge et al. (1997), and Cenarro et al. (2001). Following their argument that only the line bandpasses of Cenarro et al. (2001) cover the wings of the lines completely, we adopted those for our analysis (see Table 2).

For determining the equivalent widths of the three Ca lines, we first fit a low-degree polynomial to the continuum bandpasses to remove the continuum. Then we fit a Voigt profile to each line individually within its given bandpass using a LevenbergMarquardt optimisation. This is done with the VoigtModel profile within LMFIT (Newville et al. 2014). The integration of the fitted Voigt profiles (also in the given bandpasses) yields the equivalent widths of the lines.

In Fig. 2 some spectra from three globular clusters covering the whole range of metallicities in our sample are shown,


Fig. 3. Comparison between equivalent widths derived from simply integrating the lines in the given bandpasses ( $\Sigma \mathrm{EW}_{\text {int }}$ ) and from fitting Voigt profiles $\left(\Sigma E W_{\text {Voigt }}\right)$ for all spectra with $\mathrm{S} / \mathrm{N}>20$ and the $\mathrm{S} / \mathrm{N}$ ratio as colour-coding. Note that we clipped the colour range to a maximum value of 150 , although we reach $\mathrm{S} / \mathrm{N}$ ratios of up to 400 for single spectra. The dashed black line provides a linear fit to the data, while the green one indicates the identity.
together with the bandpasses for continuum and lines and the best-fitting Voigt profiles.

There has been some discussion in the literature on whether to use the (weighted) sum of the equivalent widths of all three Ca lines, or just the sum of the two strongest ones. Since the weakest line at $8498 \AA$ is significantly fainter than the other two and therefore more difficult to fit in low $\mathrm{S} / \mathrm{N}$ spectra, we chose to use the sum of the two broader lines at 8542 and $8662 \AA$, hereafter called $\Sigma$ EW.

We can check the quality of the equivalent widths derived from Voigt profile fits by comparing them with the results of a simple numerical integration of the lines within their respective bandpasses. In Fig. 3 a comparison between both is shown for the sum $\Sigma \mathrm{EW}$ of the two strongest lines for all spectra. Apparently, the equivalent widths from the numerical integration are slightly but systematically higher than those from Voigt profile fits, especially at larger widths. Presumably at higher metallicities not only the Ca lines broaden, but also fainter metal lines get stronger, which affects the numerical integration more than the Voigt profiles. However, the correlation is linear as expected.

For obtaining uncertainties for our equivalent widths, we take the full covariance matrix from the Voigt profile fits and use it to draw 10,000 combinations of parameters for each fitted line. We evaluate and integrate the Voigt profiles as before and use the standard deviation of all results as the uncertainty for the EW of the single line. Figure 4 shows those uncertainties for the $\mathrm{Ca}_{8542}$ line as a function of $\mathrm{S} / \mathrm{N}$. Unfortunately, we cannot use the raw spectra for calibrating the uncertainties (like in, e.g., Battaglia et al. 2008), since we have significant variations in signal-to-noise ratios between all spectra for a single star.

The quality of the fit on a single spectrum can also be derived from the ratio of the equivalent widths of the two strongest lines, which should be constant. In Fig. 5 we show the equivalent widths of those two lines as a function of their sum. A line, fitted to the data using the inverse square of the uncertainties as weights on both axes, yields a negligible error for the slope. We found $E W_{8542}=0.567 \Sigma E W$ and $E W_{8662}=0.434 \Sigma E W$, which is in perfect agreement with Vásquez et al. (2015), who determined the slopes to be 0.57 and 0.43 , respectively. Written as a ratio of


Fig. 4. The uncertainties for the equivalent width of the $\mathrm{Ca}_{8542}$ line as function of signal to noise.


Fig. 5. Measured equivalent widths of the two strongest Ca lines plotted as a function of their sum. Colour-coded are the uncertainties of the EW measurements on the single line.
line strengths, we find $W_{8542} / W_{8662}=1.31 \pm 0.20$, which, again, agrees with the value of $1.32 \pm 0.09$ derived by Carrera et al. (2013).

A comparison of single results with literature is a little more difficult, since the very dense centres of the clusters that we observed are usually too crowded for other observation techniques. One exception that we found are the AAOmega observations performed by Lane et al. (2011), with which we have 155 stars in 4 different GCs in common, covering almost our full range of metallicities from -2.28 (NGC 7099) to -0.69 dex (NGC 104). They published the sum of the EWs for all three CaT lines, so we did the same and compared the results in Fig. 6, from which three outliers have been removed, all of which have unusually high EW measurements in the literature. Our equivalent widths show a constant offset of $0.52 \AA$, which is most probably due to a different method for determining the widths (e.g. different integration intervals), with a scatter of 0.51 A.


Fig. 6. Comparison of our derived equivalent widths with those of Lane et al. (2011). For the purpose of this plot, $\Sigma E W$ denotes the sum of all three lines in the Ca triplet. In the upper plot the dashed black line shows the identity, while in the lower plot it indicates the mean offset of $\sim 0.52$ Å.

### 4.2. Reduced equivalent widths

In general, the strength of an atomic absorption line is driven by the effective temperature of the star, its surface gravity, and the abundance of the element in question. Pont et al. (2004) showed theoretically that for a fixed metallicity the strength of the CaT lines for stars on the RGB increases with increasing $T_{\text {eff }}$ and decreases for increasing $\log g$, and that both effects roughly cancel each other. Therefore, the strength of the lines is a function of luminosity alone.

Since luminosity is a parameter not easily obtained, other indicators can replace it, usually the (extinction corrected) absolute magnitudes in $V$ or $I$, or the brightness difference to the horizontal branch $V-V_{\mathrm{HB}}$, which are all independent of reddening, distance, and photometric zero-point.

As discussed before, we use the HST photometry to extract spectra from the observed MUSE datacubes. The available F606W photometry in these catalogs can also be used to calculate the brightness difference to the HB $F 606 W-F 606 W_{\mathrm{HB}}$ using HB brightnesses in this filter available from Dotter et al. (2010), with which we have 19 cluster in common. We will, however, continue calling it $V-V_{\mathrm{HB}}$.

Da Costa et al. (2009) observed that the relation between $V$ $V_{\mathrm{HB}}$ and $\Sigma \mathrm{EW}$ flattens for $V-V_{\mathrm{HB}}>+0.2$ mag. This change of slope was confirmed theoretically by Starkenburg et al. (2010). Consequently, at least for the course of this Section we will only proceed with stars with $V<V_{\mathrm{HB}}+0.2 \mathrm{mag}$ (assuming that $V$ and $F 606 \mathrm{~W}$ magnitudes - or at least the brightness differences to the HB in these bands - are similar enough). The numbers and percentages (relative to all RGB stars) of stars fulfilling this criterion are listed in column (5) of Table 1. The brightnesses of the horizontal branches $V_{\mathrm{HB}}$ are taken from Dotter et al. (2010) - if non is given, that column is marked with a dash.

Using the assumption of the strengths of the Ca lines being a function of $V-V_{\mathrm{HB}}$ alone, we can define the reduced equivalent

Table 3. Derived mean reduced equivalent widths from different methods and cluster metallicities.

| NGC | $\left\langle W_{\text {HB }}^{\prime}\right\rangle$ | $\left\langle W_{\text {all }}^{\prime}\right\rangle$ | $\left\langle W_{\mathrm{M}}^{\prime}\right\rangle$ | $\left\langle W_{\text {lum }}^{\prime}\right\rangle$ | $[\mathrm{Fe} / \mathrm{H}]$ |
| ---: | :---: | :---: | :---: | :---: | :---: |
| 104 | 5.59 | 5.66 | 5.60 | 5.63 | -0.69 |
| 362 | 4.84 | 4.82 | 4.76 | 4.78 | -1.05 |
| 1851 | 4.99 | 4.97 | 4.91 | 4.94 | -1.19 |
| 1904 | - | - | - | 3.80 | -1.61 |
| 2808 | 5.05 | 5.04 | 4.99 | 5.02 | -1.13 |
| 3201 | 4.39 | 4.29 | 4.22 | 4.24 | -1.46 |
| 5139 | - | - | 3.74 | 3.77 | -1.56 |
| 5286 | 3.57 | 3.64 | 3.52 | 3.55 | -1.63 |
| 5904 | 4.79 | 4.76 | 4.67 | 4.69 | -1.15 |
| 6093 | 3.46 | 3.51 | 3.53 | 3.55 | -1.73 |
| 6218 | - | - | 4.58 | 4.60 | -1.35 |
| 6254 | 4.17 | 4.06 | 4.09 | 4.11 | -1.65 |
| 6266 | - | - | - | 5.07 | -1.11 |
| 6293 | - | - | - | 2.37 | -1.86 |
| 6388 | 5.67 | 5.70 | 5.81 | 5.82 | -0.57 |
| 6441 | 5.64 | 5.66 | 5.79 | 5.78 | -0.49 |
| 6522 | - | - | - | 4.83 | -1.35 |
| 6541 | 3.48 | 3.52 | 3.41 | 3.44 | -1.80 |
| 6624 | 5.71 | 5.72 | 5.68 | 5.70 | -0.36 |
| 6656 | 3.45 | 3.51 | 3.50 | 3.52 | -1.91 |
| 6681 | 4.18 | 4.21 | 4.20 | 4.23 | -1.54 |
| 6752 | 4.09 | 4.10 | 4.06 | 4.08 | -1.44 |
| 7078 | 1.99 | 2.15 | 2.02 | 2.05 | -2.28 |
| 7089 | 3.95 | 3.98 | 3.90 | 3.93 | -1.58 |
| 7099 | 2.32 | 2.46 | 2.38 | 2.40 | -2.28 |

Notes. The index "HB" denotes results from the linear relation using stars with $V-V_{\mathrm{HB}}<+0.2$ as discussed in Sect. 4.2, while "all" uses the results for all RGB stars using a quadratic relation from Sect. 4.3. Finally, "M" uses the absolute magnitude in F606W instead of $V-V_{\mathrm{HB}}$ and "lum" the luminosity, both as presented in Sect. 4.4. The uncertainties for the reduced EWs are usually of the order 0.1-0.4 dex, the metallicities are taken from Dias et al. (2016).
$W^{\prime}$ as
$\Sigma \mathrm{EW}=\beta \cdot\left(V-V_{\mathrm{HB}}\right)+W^{\prime}$.
We performed a linear fit for $\Sigma \mathrm{EW}$ as a function of $V-V_{\mathrm{HB}}$ for every single cluster, yielding a slope $b$ and a reduced EW $W^{\prime}$ for each. In addition, a global function was fitted to all the data, deriving individual $W^{\prime}$ for each cluster, but using the same slope $\beta$ for all. The data itself and the results for both approaches (blue and orangen lines) are shown in Fig. 7.

The global fit with all clusters yielded a slope of $\beta=$ $-0.581 \pm 0.004$. The slopes from the individual fits are given in brackets in each single plot and are usually similar to the globally fitted one. In the literature we find values of -0.55 (Vásquez et al. 2018), -0.627 (Saviane et al. 2012), with both using V magnitudes, and $-0.74 \pm 0.01$ and $-0.60 \pm 0.01$ (Carrera et al. 2007) when using $V$ and I magnitudes, respectively.

The intercept of the fitted lines correspond to the reduced equivalent width $W^{\prime}$ for each cluster. From these fits, the uncertainties are unrealistically small due to the large number of points. Therefore we derived $W^{\prime}$ for each spectrum using the obtained global slope $\beta$ and calculated the mean reduced equivalent widths $\left\langle W^{\prime}\right\rangle$ for all clusters (see Mauro et al. 2014), which are given in Table 3 with the index "HB". This approach also yields uncertainties for the reduced equivalent widths (i.e. the standard


Fig. 7. The sum of the equivalent widths $\Sigma E W$ of the two strongest Ca lines plotted over $V-V_{\mathrm{HB}}$ for all 20 clusters in the sample, sorted by mean metallicity. Only stars are included with $V-V_{\mathrm{HB}}<+0.2$ as described in the text. A linear fit to the data for each individual cluster is plotted in orange, for which the slope $\beta$ is given in the title of each panel. The blue lines show the result of a global fit, where the same slope has been used for all clusters, yielding $\beta=-0.581 \pm 0.004$. In some cases, the individual and global fits are indistinguishable.


Fig. 8. The slopes $\beta$ from individual fits for each cluster are shown as a function of metallicity. The blue line indicates a linear fit to the data with the shaded area representing its $1 \sigma$ uncertainty band, while the orange line is the equivalent when ignoring the three most metal-poor clusters. As discussed in the text, there might be a real trend, but for the further analysis we assume $\beta$ to be constant.
deviation of all results per cluster) and has been used before by Mauro et al. (2014).

As a result, we get the following calibration using a linear relation on all RGB stars brighter than the HB:
$W^{\prime}=\Sigma \mathrm{EW}+0.581 \cdot\left(V-V_{\mathrm{HB}}\right)$.
With the negligible statistical uncertainty for the slope $\beta$, the error on the reduced equivalent width $W^{\prime}$ is just equal to the error on the sum of equivalent widths, i.e. $\sigma_{W^{\prime}}=\sigma_{\text {IEW }}$.

Using theoretical models from Jorgensen et al. (1992) a prediction was made by Pont et al. (2004) that there should be an increasing slope $\beta$ with increasing metallicity. In Fig. 8 we show the slopes from the individual fits for each cluster as a function of metallicity. Two lines have been fitted to the data, one to all the clusters (orange) and one without our three most metal-poor ones (blue), both using the uncertainties as weights. The slopes $m$ and Spearman correlation coefficients $r_{S}$ are given in the legend. While with all data there might be some trend, it completely disappears when ignoring the three clusters. We therefore chose to ignore any trend and use the same slope $\beta=-0.581$ from the global fit for all clusters.

Carrera et al. (2007) reported to see a trend of slope with metallicity, but within the uncertainties, while in Carrera et al. (2013) they detect a significant trend and suggest to add more terms to the final CaT-metallicity (see also Sect. 4.4) relation as described by Starkenburg et al. (2010).


Fig. 9. Similar to Fig. 7 the sum of the equivalent widths $\Sigma E W$ of the two strongest Ca lines is plotted over $V-V_{\mathrm{HB}}$ for all RGB stars. Quadratic fits to each individual cluster are shown in orange, while a global fit, where the same values for $\beta$ and $\gamma$ are used (giving $\beta=-0.442 \pm 0.002$ and $\gamma=0.058 \pm 0.001$ ), is plotted for each cluster in blue.

### 4.3. Extending the calibration below the $H B$

Carrera et al. (2007) stated that from theoretical predictions there is no reason why the relation between $V-V_{\mathrm{HB}}$ and $\Sigma \mathrm{EW}$ must be linear, so they suggested adding a quadratic term:
$\Sigma \mathrm{EW}=W^{\prime}+\beta\left(V-V_{\mathrm{HB}}\right)+\gamma\left(V-V_{\mathrm{HB}}\right)^{2}$.
This approach removes the necessity for using only stars brighter than the HB, and thus, following Table 1 , we can actually increase our sample size by a factor of $\gtrsim 5$. The results of the fits with the quadratic equation are shown in Fig. 9. Again we perform a fit for each individual cluster (orange) as well as a global fit (blue), for which we forced the same values for $\beta$ and $\gamma$ for all clusters. As before, the two results only differ significantly for those clusters with very few RGB stars. The global fit yields values of $\beta=-0.442 \pm 0.002$ and $\gamma=0.058 \pm 0.001$, respectively.

This yields the final calibration for the reduced equivalent width using a quadratic relation on all RGB stars, even extending below the HB:
$W^{\prime}=\Sigma \mathrm{EW}+0.442\left(V-V_{\mathrm{HB}}\right)-0.058\left(V-V_{\mathrm{HB}}\right)^{2}$.
As before for the linear relation, we calculated the reduced equivalent widths for all stars using this equation and derived a mean width for each cluster. The results are listed in Table 3 with the index "all".


Fig. 10. A comparison of average reduced equivalent widths $\left\langle W^{\prime}\right\rangle$ obtained from a linear fit to stars with $V-V_{\mathrm{HB}}<+0.2$ ("HB") and from a quadratic fit to the full sample ("all"). The error bars on the $y$ axis are those of $\left\langle W_{\text {all }}^{\prime}\right\rangle$.

We expect this method using a quadratic equation and including all stars on the RGB to produce the same reduced equivalent widths as the classical approach, for which a linear relation is fitted to only stars brighter than the HB. We compare


Fig. 11. As in Fig. 8, slopes are plotted as function of metallicity, but here for the quadratic fit from Fig. 9 at three different values for $V-V_{\mathrm{HB}}$. The blue line shows the fitted relation from Fig. 8.
the results for both methods in Fig. 10. We find large deviations for only four clusters, of which two are the ones with the lowest metallicity in our sample. i.e. NGC 7078 and NGC 7099, which might indicate problems with the calibration for very low metallicities. The other two mild outliers are NGC 3201 and NGC 6254, both with a relatively low number of RGB stars in our sample. Otherwise, the reduced equivalent widths derived from both methods are well within the error bars.

We can also repeat our analysis on the slope of the relation as it was done for the linear relation in Sect. 4.2 (see Fig. 8). Since the slope is not constant now, it is plotted for three different values of $V-V_{\mathrm{HB}}$ in Fig. 11 in different colours. For stars brighter than the HB , the trend of this relation is similar to the linear case, which is indicated by the blue line, only showing some offset. However, already for stars at the HB this trend seems to vanish, especially when ignoring the two low-metallicity clusters, which seem to cause some problems. For stars fainter than the HB there might even be a reversal of the trend, with the slope increasing again for more metal-rich clusters.

### 4.4. Using absolute magnitude and luminosity instead of $V-V_{\mathrm{HB}}$

The CaT metallicity relation as presented in this paper requires the brightness difference of a star to the horizontal branch. While this can be obtained easily in stellar populations like globular clusters, it is next to impossible for field stars. However, with $V-V_{\mathrm{HB}}$ just being a proxy for the luminosity, we can use the luminosity directly, or - a quantity easier to measure - the absolute brightness in any given filter.

As before, we will use HST magnitudes measured in the F606W filter, which we correct for distance and extinction as given by Harris (1996, 2010 edition) to obtain absolute magnitudes $M_{\text {F606w. }}$. For deriving luminosities, we need bolometric corrections, which we calculate from our grid of PHOENIX spectra (Husser et al. 2013). The necessary effective temperatures and surface gravities for applying the corrections to the data come from our analysis pipeline as described in Husser et al. (2016). These two approaches open up new windows especially


Fig. 12. Absolute magnitude in F606W (left panels) and luminosity (right panels) over brightness difference to the HB for all stars in the sample. Different colours belong to different clusters. The dashed black lines indicate linear fits to the data, to which the differences are shown in the lower panels.
for investigating the CaT-metallicity in field stars, for which, in the era of Gaia (Gaia Collaboration et al. 2016), distances and spectral types are now easily available. While we have F606W photometry available for most of our clusters, there are some exceptions for which we have to use different filters for deriving luminosities: for NGC 1904, NGC 6266, and NGC 6293 we use F555W, and F625W for NGC 6522.

Figure 12 shows a comparison between $V-V_{\mathrm{HB}}$ magnitudes and both the derived absolute magnitudes and the logarithm of the derived luminosities. As can be seen, there is a linear relation for both parameters as expected (dashed black line). The offset between individual clusters (different colours) might stem from the difficulty of determining HB brightnesses, especially in clusters where the HB is not really horizontal.

We can repeat the analysis from Section 4.3 with absolute magnitudes and luminosities instead of brightness differences to the HB. For the case of the absolute brightness we get $\beta=-0.426 \pm 0.002$ and $\gamma=0.054 \pm 0.001$, and therefore, equivalent to Eq. 4:
$W^{\prime}=\Sigma \mathrm{EW}+0.426 M_{\mathrm{F} 606 \mathrm{~W}}^{\prime}-0.054 M_{\mathrm{F} 606 \mathrm{~W}}^{\prime 2}$,
with $M_{\text {F606W }}^{\prime}=M_{\mathrm{F} 606 \mathrm{~W}}-0.687$ from the $y$-intercept of the linear relation in Fig. 12. We apply this correction to get similar reduced equivalent widths as from the method using $V-V_{\mathrm{HB}}$.

The same way we can obtain a calibration for the luminosities (see Fig. A.2) and get $\beta=1.006 \pm 0.005$ and $\gamma=$ $0.259 \pm 0.007$, and therefore:
$W^{\prime}=\Sigma E W+1.006 L^{\prime}-0.259 L^{\prime 2}$,
with $L^{\prime}=\log \left(L / L_{\odot}\right)-1.687$.
The calibrations for both $M_{\text {F606W }}$ and $L$ are shown in Figs. A. 1 and A.2, respectively. In the case of absolute magnitude, we get NGC 5139 ( $\omega$ Centauri) as an additional cluster, that we could not use for the previously discussed $V-V_{\mathrm{HB}}$ calibration due to a missing HB brightness. With its many populations and broad range of metallicities (see Sect. 7.7), it does not show the same narrow trend as the other clusters. However, since the global fit was not affected by this significantly, we kept it for the calibration. For all the other cluster, we again see some deviations between the global and the individual fits of the quadratic relation, but they are mostly minor.


Fig. 13. A comparison of average reduced equivalent widths $\left\langle W_{M}^{\prime}\right\rangle$ and $\left\langle W_{\text {lum }}^{\prime}\right\rangle$ based on absolute magnitudes and luminisities with those obtained using the brightness difference to the $\mathrm{HB}\left\langle W_{\text {all }}^{\prime}\right\rangle$.

The full sample of 25 cluster can only be calibrated using the relation based on luminosities $L$ (see Fig. A.2). In addition to the previously discussed clusters, we can now include, among others, NGC 6293, for which we have only very few RGB stars, and therefore the individual fit is significantly different from the global one, which, however, still looks reasonable.

The average reduced equivalent widths for all clusters in the sample are given in Table 3 with the indices " M " for absolute magnitudes in F606W and "lum" for luminosities, respectively. Figure 13 compares the derived average reduced equivalent widths per cluster with those from the analysis as described in Sect. 4.3. As one can see, they agree well within the error bars.

### 4.5. Metallicity calibration

In total we have now presented four different methods for calculating reduced EWs $W^{\prime}$, identified by the following indices in plots and tables:

- HB: Using only stars with $V>V_{\mathrm{HB}}+0.2$ and a linear relation based on brightness differences to the $\mathrm{HB} V-V_{\mathrm{HB}}$.
- all: Using all RGB stars and a quadratic relation based on $V-V_{\mathrm{HB}}$.
- M: Same as all, but based on the absolute magnitudes $M_{\mathrm{F} 606 \mathrm{~W}}$.
- lum: Same as all, but based on luminosities $L$.

Although the calibrations based on luminosity $L$ should be the method of choice in most scenarios, it also depends heavily on model assumptions - not only for deriving $T_{\text {eff }}$ and $\log g$ for each star, but also for calculating the bolometric corrections. Calculating the luminosity also requires an absolute magnitude $M$, which, in turn, can only be derived using good values for distance and extinction. However, using $L$ or $M$ for the calibration it is not necessary to derive brightness differences to the HB $V-V_{\mathrm{HB}}$, which is complicated even in some globular clusters, and impossible for field stars.


Fig. 14. In the upper panel the metallicity from the literature (Dias et al. 2016) is plotted over the mean reduced equivalent width of each cluster, derived from the quadratic relation on all RGB stars based on $V-V_{\mathrm{HB}}$. Three polynomials of different degree are fitted to the data and the RMS for each is given in the legend. In the lower panel, quadratic fits to three more calibrations using the same metallicity scale (only brighter than HB, and based on $M$ and $L$ ) are provided for comparison, together with all four on a different metallicity scale (C09, from Carretta et al. 2009a).

Nevertheless, we do have reliable HB brightnesses for 19 of our clusters from Dotter et al. (2010) and we prefer not to depend on any model assumptions, so we will use the calibration based on $V-V_{\mathrm{HB}}$ for these 19 clusters. For the remaining clusters the absolute magnitude calibration would be the best choice, but we only have F606W photometry available for two more clusters. So instead of presenting results from three different calibrations, the metallicities for all the remaining six clusters are derived from the luminosity approach. When necessary, these six clusters are marked in plots and tables with an asterisk.

With the set of average reduced equivalent widths as given in Table 3, we can now calibrate them with mean cluster metallicities from the literature (from Dias et al. 2016). The upper plot in Fig. 14 shows the metallicities from the literature as a function of reduced equivalent width. The three lines show a linear, quadratic, and cubic fit to the data, taking into account the errors on both axes (which are small), together with their corresponding RMS. The coefficients for all relations are given in Table 4 for the following equation:
$[\mathrm{Fe} / \mathrm{H}]=p 0+p_{1} \cdot W^{\prime}+p_{2} \cdot W^{\prime 2}+p_{3} \cdot W^{\prime 3}$.
Since both the Bayesian (BIC) and the Akaike (AIC) information criteria give the best results for the quadratic relation, we choose this for further analyses. Therefore the relation between reduced equivalent width and metallicity is given by:
$[\mathrm{Fe} / \mathrm{H}]=-2.52-0.04 W^{\prime}-0.07 W^{\prime 2}$.

Table 4. Coefficients for CaT metallicity calibration as given by Eq. 7 for three different polynomial degrees.

| $p_{0}$ | $p_{1}$ | $p_{2}$ | $p_{3}$ |
| :---: | :---: | :---: | :---: |
| $-3.61 \pm 0.13$ | $0.52 \pm 0.03$ | - | - |
| $-2.52 \pm 0.32$ | $-0.04 \pm 0.16$ | $0.07 \pm 0.02$ | - |
| $-4.02 \pm 1.29$ | $1.22 \pm 1.07$ | $-0.27 \pm 0.28$ | $0.03 \pm 0.02$ |

Table 5. Coefficients for CaT metallicity calibration as given by Eq. 12.

| a | b | c | d | e | f |
| :---: | :---: | :---: | :---: | :---: | :---: |
| -3.456 | -0.074 | -0.100 | 0.540 | 2.101 | -0.011 |
| $\pm 0.050$ | $\pm 0.017$ | $\pm 0.005$ | $\pm 0.009$ | $\pm 0.117$ | $\pm 0.004$ |

The metallicities derived from this relation show two systematic errors: the mean metallicity of a cluster will be the value of the relation given above at the mean reduced EW of the cluster, and therefore will have a small offset to the literature value for most clusters. Furthermore, the slope of the relation at any given point defines the metallicity spread.

Following previous studies (see, e.g., Vásquez et al. 2018), the uncertainties are calculated as the quadratic sum of the uncertainty $\sigma_{W^{\prime}}$ and the root mean squares (RMS) for the used relation as given in Fig. 14. For the quadratic relation this yields:
$\sigma_{[\mathrm{Fe} / \mathrm{H}]}=\sqrt{\sigma_{r}^{2}+\mathrm{RMS}^{2}}$,
where RMS is the root mean square for the used relation and $\sigma_{r}$ is the propagated uncertainty for $\sigma_{W^{\prime}}$ :
$\sigma_{r}=\left(p_{1}+2 \cdot p_{2} \cdot W^{\prime}\right) \sigma_{W^{\prime}}=\left(-0.03+0.14 W^{\prime}\right) \sigma_{W^{\prime}}$.
We already demonstrated that all previously discussed approaches yield similar $W^{\prime}$. The lower panel in Fig. 14 shows that the metallicity calibrations are comparable, no matter what method for calculating the reduced EWs has been used. There is also no significant variation when using different metallicity scales, in this case taken from Dias et al. $(2016$, D16) and Carretta et al. (2009a, C09).

Using absolute magnitudes or luminosities allows us to use a different approach and get rid of the intermediate step of calculating reduced equivalent widths completely. A CaT-metallicity relation based on absolute magnitudes was described by Starkenburg et al. (2010). They suggest a direct relation between the equivalent widths of the Ca lines and the metallicity:
$[\mathrm{Fe} / \mathrm{H}]=a+b \cdot M+c \cdot \Sigma \mathrm{EW}+d \cdot \Sigma \mathrm{EW}^{-1.5}+e \cdot \Sigma \mathrm{EW} \cdot M$,
where M is the absolute magnitude in an arbitrary filter and the term for $\Sigma \mathrm{EW}^{-1.5}$ was introduced to account for variations at low metallicities. The limits for this calibration were given as $-3<V_{\mathrm{HB}}<0$ and $-3<M_{V}<0.8$, i.e. for stars brighter than the HB only.

Instead of the absolute magnitude $M$ we are using the luminosity $\log L / L_{\odot}$ again and extend the relation to stars fainter than the HB in the same way as before by introducing a quadratic term for the luminosity:

$$
\begin{align*}
{[\mathrm{Fe} / \mathrm{H}]=a } & +b \cdot \log \left(L / L_{\odot}\right)+c \cdot \log \left(L / L_{\odot}\right)^{2}+d \cdot \Sigma \mathrm{EW} \\
& +e \cdot \Sigma \mathrm{EW}^{-1.5}+f \cdot \Sigma \mathrm{EW} \cdot \log \left(L / L_{\odot}\right) \tag{12}
\end{align*}
$$



Fig. 15. The upper panel shows the metallicity distributions for NGC 1851 as derived from all four CaT-metallicity relations discussed in the text. The lower panel shows the distributions for the three populations we obtained from the chromosome map in Fig. 1 for the "all" calibration from above. As for all the following, similar plots, the bars at the top of the plots show the $5-95 \%$ range of the data (lines with caps), the interquartile range ( $Q_{1}-Q_{2}$, boxes) and medians (vertical line) for all distributions.

Unfortunately, we do not have metallicities for all the stars in our sample available for the calibration, so we assume it to be the same for all stars in each cluster. The coefficients for the best fitting polynomial are given in Table 5. This calibration will be referenced to using the index poly and is treated more as an experimental approach for comparison.

## 5. Metallicity distributions

Having presented five different approaches for deriving metallicities from reduced EWs, we can now apply all of them to all stars in our sample. The upper panel of Fig. 15 shows the resulting metallicity distributions for NGC 1851. The thinner lines show classical histograms with a bin size of $0.05 d e x$. Since the shape of a histogram not only depends on the bin size, but also significantly on the starting value, we decided to also include a rolling histogram or convolved frequency, which was obtained by shifting the positions of the bins in steps of 0.1 and connecting the points with a solid line. This way, smaller structures in the shape of the distribution show up more prominently.

In the case of NGC 1851, all calibrations produce similar metallicity distributions, although the one based only on stars brighter than the HB , apart from including fewer stars, shows


Fig. 16. Classic (red) and rolling (black) histograms for the $[\mathrm{Fe} / \mathrm{H}]$ distributions for all clusters (except NGC 1851, which is shown in Fig. 15) as derived from the CaT relation. The metallicities for all clusters are shifted by their respective means so that they peak around 0 . The $x$ axes all show the same range within $\pm 0.5 \mathrm{dex}$, while the y axes are scaled to the peak values of each clusters. Horizontal grid lines are shown at peak height and at half that height, while vertical lines are located at $0, \pm 0.2$, and $\pm 0.4 \mathrm{dex}$. For each cluster, the number of stars is given (\#) that have been used for calculating the distribution, as well as the mean $\mu=\langle[\mathrm{Fe} / \mathrm{H}]\rangle$ and the median $\Theta$. All the numbers are also given in Table 7.
a significant tail towards higher metallicities that does not exist in the other distributions. The distributions derived from the other methods based on the intermediate step of calculating reduced EWs (all, M, and lum) are all very similar, and also show the same small features, e.g. the little bump at $\sim-1.3$ dex. On the other hand, the metallicities derived from the polynomial fit (poly) are systematically lower, and the distribution is a little narrower and does not exhibit the smaller features that exist in the others.

While the metallicity distribution for NGC 1851 has already been shown in Fig. 15, those for the remaining 24 clusters in our sample are given in Fig. 16. The results for clusters marked with a star have been obtained using the luminosity calibration as discussed in Sect. 4.4, since for those there was no HB brightness available from Dotter et al. (2010). The medians, means, standard deviations, and first and third quartiles for the metallicities of all clusters are listed in Table 7. In order to allow assessing the width of the distribution, i.e. whether it is domi-


Fig. 17. Distribution for the uncertainties of the derived metallicities for all RGB stars in all clusters, convolved with a Gaussian with $\sigma=$ 0.001 dex. The NGC numbers of the clusters are given at the right end of the distributions, while the mean metallicities from Dias et al. (2016) are listed on the left.
nated by the errors on the individual measurements, the distribution of metallicity uncertainties are shown for every cluster in Fig. 17 - the median uncertainty we get for the whole sample is $\sim 0.12$ dex. With the mean metallicities of the clusters given on the left side of the distributions, we see a clear trend of the uncertainties with metallicity. The uncertainty distributions for high-metallicity clusters are significantly broader and peak at higher values as compared to the low-metallicity end. This result confirms our assumption, that for high metallicities our EW measurements (or at least their uncertainties) are presumably affected by smaller lines in the wings of the CaT lines, likely more as a systematic than a random error.

We also investigated the reliability of our metallicity measurements using a maximum likelihood approach. Under the assumption that a cluster has a mean metallicity of $\mu_{[\mathrm{Fe} / \mathrm{H}]}$ and an intrinsic metallicity spread of $\sigma_{[\mathrm{Fe} / \mathrm{H}]}$, the probability of measuring a value $m$ with uncertainty $\delta_{\mathrm{m}}$ can be approximated as
$p\left(m, \delta_{\mathrm{m}}\right)=\frac{1}{2 \pi \sqrt{\sigma_{[\mathrm{Fe} / \mathrm{H}]}^{2}+\delta_{\mathrm{m}}^{2}}} \exp \left(-\frac{\left(m-\mu_{[\mathrm{Fe} / \mathrm{H}]}\right)^{2}}{2\left(\sigma_{[\mathrm{Fe} / \mathrm{H}]}^{2}+\delta_{\mathrm{m}}^{2}\right)}\right)$.
For each cluster, we determined the intrinsic parameters $\mu_{[\mathrm{Fe} / \mathrm{H}]}$ and $\sigma_{[\mathrm{Fe} / \mathrm{H}]}$ of the metallicity distribution using the affineinvariant MCMC sampler emcee (Foreman-Mackey et al. 2013).


Fig. 18. Intrinsic metallicity distributions for all clusters as derived from a maximum-likelihood analysis. Metal-complex type II clusters are marked with blue squares.

Most clusters in our sample do not show an intrinsic metallicity spread, hence we expect $\sigma_{[\mathrm{Fe} / \mathrm{H}]}$ to be consistent with zero in such objects. On the other hand, if significant spreads are found, they can be attributed to residual trends in our metallicity measurements (e.g. with luminosity) or systematic effects in the analysis that are not accounted for by our formal uncertainties.

Figure 18 shows the results of this analysis for all clusters. For all our Type I clusters (in orange), we would expect an intrinsic spread of $\sigma_{[\mathrm{Fe} / \mathrm{H}]}=0$. While this is true for most clusters with $[\mathrm{Fe} / \mathrm{H}] \lesssim-1.7$, we see values significantly larger than this for higher metallicities, which indicates that at least for those clusters we under-estimate the uncertainties for the metallicities. At the same time, all Type II clusters (in blue) show intrinsic spreads, which we would expect from these metal-complex clusters.

Taking the distributions for both the metallicities and their uncertainties, we can identify some problematic cases: those with erratic metallicity distributions and those with high average uncertainties. While for NGC 6293 and NGC 6522 this is certainly due to low number statistics, this does not apply to NGC 6388 and NGC 6441, both with more than 2,000 RGB stars. For both clusters the available photometry is difficult to handle due to extremely broadened main sequences and giant branches (see Sect. 2), which directly affects the extraction process of the raw spectra from the data cubes, and therefore the quality of the extracted spectra. However, two more highmetallicity clusters, namely NGC 6624 and NGC 6522, show a similar behaviour, so this is presumably connected to systematic errors as discussed before.

We combined the derived metallicities for all stars with the chromosome maps that we created for all clusters with available UV HST photometry and plot metallicity distributions for the different populations. The CMD and the chromosome map for NGC 1851 have been shown before in Fig. 1, revealing three different, clearly separated populations. The lower panel in Fig. 15 shows the metallicity distributions for all three populations, using the same colour-coding. The bars at the top of the plot show the $5-95 \%$ range of the data (lines with caps), the interquartile range ( $Q_{1}-Q_{2}$, boxes) and medians (vertical line) for all distributions.

The derived parameters for the metallicity distributions for all populations are listed in Table 7. Please note that the clusters NGC 1904, NGC 6266, NGC 6293, and NGC 6522 were not


Fig. 19. Metallicity distributions for the stellar populations of five more Type II clusters are shown in the big panels (as in Fig. 15 for NGC 1851 ). The upper smaller panels show the chromosome maps and the lower panels the CMDs of the RGBs of the respective clusters (both as in Fig. 1). The colour-coding is the same in all plots for a single cluster.
included in the HUGS survey (Nardiello et al. 2018a), so we cannot create chromosome maps from them.

### 5.1. Type I/II clusters

For those clusters with UV photometry, for which we can create chromosome maps, we can investigate the metallicity distribu-
tions of the different populations in each cluster. For Type I cluster we do not expect any variations in metallicity, and for almost all of them in our sample this seems to be true. Figure 27 shows the distributions for all Type I cluster, and they seem to be very similar for all clusters only showing two populations. For each cluster the distributions are shown in the larger panel on the left, while the chromosome map and the CMD are shown next to it


Fig. 20. In the panels on the left, the chromosome maps are plotted for all our Type II clusters, colour-coded with our derived metallicity, ranging from the median minus 0.3 (blue) to median plus 0.3 dex (orange). The arrows show the directions of the metallicity slopes and their lengths indicate a change of 0.15 dex . In the panels on the right, the metallicities are plotted as function of a pseudo-colour $\Delta \mathrm{A}$ along the arrows on the left, colour-coded by population. A linear fit to the data is shown as dashed red line. The Spearman correlation coefficient $r_{S}$ is given for every cluster.
on the right. However, for two of the Type I clusters, more than two populations have been found: NGC 2808 and NGC 7078 which has recently been re-labeled as Type II by Nardiello et al. (2018b) - will be discussed in detail in Sections 7.5 and 7.23, respectively.

The previously discussed NGC 1851 on the other hand is one of those clusters that Milone et al. (2017) classified as Type II (or metal-complex) clusters. These clusters do not show a simple bimodal distribution of populations, but contain a third population - or even more. Previous studies have shown that these populations also show a significant difference in their chemical compositions, showing up as a split in metallicity.

Figures 19 and 24 show the metallicity distributions for different populations for the six remaining Type II clusters in our sample. For all of them we see a difference between the mean and median metallicities of populations P1/P2 and P3 of $\sim 0.2$ dex, only NGC 362 and NGC 1851 show a smaller variation of only $\sim 0.12 \mathrm{dex}$. The populations P3 of all clusters usually contain a hundred or more stars (only NGC 362 and NGC 7089 have significantly less). Table 6 shows the results of Two-sample Kolmogorov-Smirnov tests comparing the metallic-

Table 6. Results from a Two-sample Kolmogorov-Smirnov test for all Type II clusters comparing the metallicities of their P3 stars with that of all the other stars.

| Cluster | $D$ | $D_{\text {crit }}$ | $p$-value |
| :--- | :---: | :---: | :---: |
| NGC 362 | 0.435 | 0.050 | 0.00032 |
| NGC 1851 | 0.403 | 0.005 | $3.1 \cdot 10^{-15}$ |
| NGC 5286 | 0.534 | 0.011 | $2.1 \cdot 10^{-15}$ |
| NGC 6388 | 0.340 | 0.003 | $1.2 \cdot 10^{-37}$ |
| NGC 6656 | 0.615 | 0.013 | $1.3 \cdot 10^{-15}$ |
| NGC 7089 | 0.162 | 0.008 | 0.0018 |

Notes. $D$ denotes the result of the Two-sample KS test. $D_{\text {crit }}=$ $c(\alpha) \sqrt{(n+m) /(n m)}$ is the critical value (with sample sizes $n$ and $m)$ for $\alpha=0.1$ and $c(\alpha)=1.073$. Finally, the last column gives the two-tailed $p$-value.
ities of the clusters' P3 stars with that of all their other stars. With $D \gg D_{\text {crit }}$ and $p \ll 1$ for all clusters, we assume the splits in the metallicities to be significant.

With the large number of stars in our sample, we can now investigate, whether the Type II clusters show a real bimodality in metallicity or whether it is a continuous trend. In the left panels of Fig. 20, the chromosome maps of all our Type II clusters are plotted, colour-coded by metallicity. An arrow in each panel shows the direction of the metallicity gradient and its length indicates a change of 0.15 dex. Interestingly these arrows all point in the same direction, indicating a global trend. Note that NGC 362 is missing in this overview, because we could not determine a metallicity gradient due to the small number of stars in its P3 population.

In the panels on the right of Fig. 20 the metallicity is plotted as a function of the pseudo-colour $\Delta \mathrm{A}$ along the arrows on the left. The stars are colour-coded by population, using the same colours as in the other figures. A line has been fitted through all the data (in red) and the Spearman correlation coefficient $r_{S}$ is given for all clusters. For NGC 7089 the number of stars in P3 is probably too low (30) for this kind of analysis, but for all other clusters we see a clear, narrow, and continuous trend of metallicity with $\Delta$ A. Even NGC 5139 with its complicated structure follows this relation very nicely with all stars and all populations. The other clusters also do not show a clear separation of P3 in these diagrams. These results hint towards a continuous trend, and not a bimodality.

## 6. Intrinsic abundance variations in the primordial populations

In the chromosome maps, the primordial P 1 population is often extended along the $\Delta \mathrm{G}_{\mathrm{F} 275 \mathrm{~W}-\mathrm{F} 814 \mathrm{~W}}$ axis, indicating some variations in the chemical composition. Marino et al. (2019a) discussed two possible explanations for this colour spread: a variation in He content, or in $[\mathrm{Fe} / \mathrm{H}]$ and $[\mathrm{O} / \mathrm{Fe}]$. They also state that a spread in metallicity would result in a positive correlation with $\Delta \mathrm{G}$, although they could not find strong evidences supporting this. While Lardo et al. (2018) assumed the cause to be a spread in the initial helium and possibly nitrogen abundance, Tailo et al. (2019) found no conclusive explanation for the spread in P1.

In Fig. 21 the metallicity for all P1 stars is plotted as a function of $\Delta \mathrm{G}$ for all clusters in our sample with available UV photometry, and the black lines represent linear fits to the data with their lengths indicating the FWHM of the metallicity distribution in $\Delta \mathrm{G}$. For each cluster the slope $m$ of the linear fit is shown as well as the Spearman correlation coefficient $r_{S}$ and the difference in metallicity between the ends of the black lines, which can be used as an estimator for the total change in metallicity within the P1 populations.

Although the Spearman correlation coefficient barely reaches +0.5 for some clusters, it is positive for all except NGC 6681, for which the slope is dominated by some outliers - removing them yields a correlation of about zero. Except for this one, the slope is also positive for all clusters, and for the remaining ones the $1 \sigma$ error interval excludes a flat line, with the possible exceptions of NGC 362 and NGC 7099.

For the case of NGC 3201, the slope of the metallicity as a function of $\Delta \mathrm{G}$ has also been determined by Marino et al. (2019b). They found a value of 0.5 , which is within the error bars of our result of $0.41 \pm 0.10$.

The total variation in metallicity (given as $\Delta$ in the plots) typically is about 0.04 dex, but also goes up to about 0.1 dex and above for some clusters. The cases of NGC 6388 and NGC 6441 might be explainable by large uncertainties (see Fig. 17), but due to the large number of stars the trends are significant. As expected, the trend is more pronounced for wide distributions in
$\Delta \mathrm{G}$, but some of the narrower ones also show a clear increase of $[\mathrm{Fe} / \mathrm{H}]$ with $\Delta \mathrm{G}$. Surprisingly, the trend does not seem to be affected by the Type I/II classification.

When using model spectra for deriving element abundances, an error in the determination of the effective temperature can cause variations in metallicity. We derive our results using a different method, but we might also see a trend with temperature. However, we do not see any significant change in $T_{\text {eff }}$ and $\log g$ (from our full-spectrum fits) with the pseudo-colour $\Delta \mathrm{G}$, so the trends we see in Fig. 17 are probably not temperature related.

Although our results cannot give strong evidence on the variation of metallicity within the primordial populations of globular clusters, we also cannot exclude this possibility. The case of NGC 2808 will be discussed a little more in detail in Sect. 7.5.

## 7. Individual clusters

In this Section, we will discuss the results for all individual clusters in detail. While some of them show peculiarities and are therefore of interest in other regards, we will concentrate only on their metallicity distributions - both for the whole cluster (mainly Fig. 16), and for its different populations (Figs. 27 and 19 , and for some individual clusters), where available.

### 7.1. NGC 104 / 47 Tuc

The metal-rich, nearby, and well-studied globular cluster NGC 104 harbours two known populations. The Na-O anticorrelation has been observed, among others, by Carretta et al. (2009b, 2013b) and Gratton et al. (2013). The presence of two populations has been shown photometrically by Milone et al. (2012a). Although Fu et al. (2018) did not find a split in [Fe/H], they reported different values for the alpha element abundance [ $\alpha / \mathrm{Fe}$ ] for the two populations of 0.41 and 0.23 dex, respectively. With our method being based on CaT equivalent width, we are presumably biased by different alpha element abundances, so the difference in metallicity as visible in the 47 Tuc panel of Fig. 27 of 0.07 dex presumably corresponds to the split from the literature.

### 7.2. NGC 362

Being classified as a Type II cluster, NGC 362 shows a small P3 population, which unfortunately in our sample only consists of 17 stars. The distribution is also very broad, but its median of -0.99 dex differs significantly from that of P1 ( -1.09 dex) and P2 ( -1.13 dex).

Carretta et al. (2013a) found a split in the RGB of this cluster with a secondary sequence that consists of about $6 \%$ of all RGB stars, which most likely corresponds to our population P3. They found an enrichment in Ba and probably all s-process elements.

### 7.3. NGC 1851

In this well-studied Type II cluster, multiple RGBs have already been found by Lee et al. (2009b); Han et al. (2009). An actual split in the metallicity was suggested by Carretta et al. (2010b) and estimated to be in the range of $0.06-0.08 \mathrm{dex}$. Lim et al. (2015) found a split of $\sim 0.14$ dex. A split in the SGB was reported by Milone et al. (2008), and they suggested that this could be explained by a difference of 0.2 dex in $[\mathrm{Fe} / \mathrm{H}]$, which, however, could be ruled out from the narrowness of the MS. On the other hand, Yong \& Grundahl (2008) found this possible with a


Fig. 21. Plotted is the metallicity as a function of $\Delta \mathrm{G}=\Delta \mathrm{F} 275 \mathrm{~W}, \mathrm{~F} 814 \mathrm{~W}$ for the primordial populations P1 in
all clusters in our sample with available UV photometry. The black lines show a linear fit (with the length being the FWHM of the distribution) and values are given for the fitted slopes $m$, the Spearman correlation coefficients $r_{S}$, and the differences $\Delta$ in metallicity between the ends of the black lines. Note that for NGC 6388 and NGC 6441 not the full ranges are shown.
higher He content. Other studies like Milone et al. (2012b) and Villanova et al. (2010) did not find any variation in metallicity.

In our results we see a separation in metallicity for NGC 1851 of $\sim 0.12$ dex between median values for P3 and P1/P2 and $\sim 0.12$ dex between the means. Furthermore, there is only a slight overlap of the $Q_{1}-Q_{3}$ intervals.

### 7.4. NGC 1904 / M 79

The metallicity distribution for NGC 1904 shows no spread in metallicity, and without UV photometry we cannot create chromosome maps and investigate the different populations of this cluster. No anomalous metallicity distribution could be found in the literature.

### 7.5. NGC 2808

For the Type I cluster NGC 2808, Milone et al. (2015b) reported five different populations from an analysis of the HUGS photometry, and, assuming a constant metallicity (see Carretta et al. 2006), found four of those populations (our P2-P4) to be en-
hanced in He when compared to the primordial population (our P1). According to Sbordone et al. (2011) and Lardo et al. (2018) a change in He also produces a change in luminosity and effective temperature.

We applied the same grouping in the chromosome map of NGC 2808 into five populations and see no significant split in metallicity (see Fig. 22). However, the metallicity seems to be increasing from P2 to P4, i.e. with decreasing $\Delta \mathrm{G}$. This trend is opposite to what we see in Type II clusters, where metallicity increases with increasing $\Delta \mathrm{G}$. In Figure 20 we showed that at least for Type II cluster the metallicity also increases with $\Delta \mathrm{C}$, so we might see the same effect in NGC 2808.

For NGC 2808 we want to investigate a little more in detail the metallicity variations in the P1 populations as discussed in Sect. 6. The chromosome map for the two sub-populations in P1, called PA and PB, is shown in Fig. 23. When looking at the metallicity histograms for the two populations in the small panel on the right hand side, we see a little shift of about 0.12 in the medians and even 0.16 dex in means. However, the middle panel shows a more continuous trend, as was already suggested from Fig. 21 for all the other clusters. The black line shows a linear


Fig. 22. Metallicity distributions for NGC 2808 . Note that population P 1 is a combination of PA and PB .


Fig. 23. Splitting population P1 of NGC 2808 into two sub-populations $A$ and $B$.
fit to the data, and the residuals are shown in the lower panel, indicating that what we see is rather a continuous trend than an actual split.

We present a more in-depth analysis of the multiple populations chemistry of NGC 2808 in Latour et al. (2019).

### 7.6. NGC 3201

NGC 3201 is a halo cluster, for which Simmerer et al. (2013) found an unusual intrinsic spread in iron abundance of 0.4 dex. Mucciarelli et al. (2015) obtained the same result, but only when deriving the abundance from $\mathrm{Fe}_{\text {I }}$ lines. For $\mathrm{Fe}_{\text {II }}$ they reported no spread, so they argue that this is caused by NLTE effects driven by iron overionization. Simmerer et al. (2013) also detected a metal-poor tail, although containing only 5 stars. In our results we see neither a spread in metallicity nor a metal-poor tail. If at all, we see some stars with an excess metallicity. The binary content of multiple populations in NGC 3201 will be investigated in detail in Kamann et al. (in prep.).

### 7.7. NGC5139 / $\omega$ Centauri

For the peculiar cluster $\omega$ Centauri, a bimodal distribution of metallicities has been known for a long time (Hesser et al. 1985) and has been quantified by Norris et al. (1996) using Calcium abundances, giving $[\mathrm{Ca} / \mathrm{H}]=-1.4 \mathrm{dex}$ for one and -0.9 for the other population. This bimodality has been confirmed later photometrically using HST (Anderson 1997; Bedin et al. 2004), showing a split all along its CMD, from the MS to the RGB.

On the sub-giant branch (SGB), Sollima et al. (2005b) found four populations with $[\mathrm{Fe} / \mathrm{H}]=-1.7 \mathrm{dex},-1.3,-1.0$ (all with $[\alpha / \mathrm{Fe}]=+0.3$ ), and -0.6 (with $[\alpha / \mathrm{Fe}]=+0.1$ ) using CaT abundances. Villanova et al. (2007) identified four populations using GIRAFFE spectra: two old populations with -1.7 and -1.1 dex, and two 1-2 Gyrs younger populations with -1.7 and -1.4 dex. Six different SGBs have been identified by Villanova et al. (2014), with $[\mathrm{Fe} / \mathrm{H}]=-1.83,-1.65,-1.34,-1.05,-0.78$, and -0.42.

Sollima et al. (2005a) found four different populations on the RGB using FORS1 photometry at the VLT and derived metallic-


Fig. 24. Metallicity distributions for the type II cluster NGC 5139. Note that the median values for populations P7 and P9 are outside the plotted metallicity range.


Fig. 25. Comparison of metallicities for different populations in NGC 5139 as reported in the literature with the results from this work.
ities photometrically using the colour distribution. The metallicities they obtained were $[\mathrm{Fe} / \mathrm{H}]=-1.4 \mathrm{dex},-1.2,-0.9,-0.7$, and -0.5 , respectively. Strömgren photometry was used by Calamida et al. (2009) to find four major peaks in the metallicity distribution at $[\mathrm{Fe} / \mathrm{H}]=-1.73$ dex, $-1.29,-1.05$, and -0.80 , and three minor ones at $-0.42,-0.07$, and +0.24 dex. High resolution spectroscopy of 855 red giants was obtained by Johnson \& Pilachowski (2010), who found five peaks in their metallicity distribution at $[\mathrm{Fe} / \mathrm{H}] \approx-1.75,-1.50,-1.15,-1.05$, and -0.75 .

NGC 5139 is one of our clusters without a $V-V_{\mathrm{HB}}$ magnitude, so we relied on the luminosity calibration as presented in Sect. 4.3. Due to the complex structure of $\omega$ Centauri, its $\Sigma$ EWluminosity diagram shows a large spread (see Fig. A.2) and we expect some offset in our metallicities. In the metallicity calibration itself it is offset from the model by $\sim 0.11$ dex towards lower metallicities, so we considered this as a systematic error. Furthermore, the reported variations in $[\mathrm{Ca} / \mathrm{Fe}]$ and $[\alpha / \mathrm{Fe}]$ will have an effect on our results, presumably causing another systematic error.

Using chromosome maps created from HST UV photometry Bellini et al. (2017) found at least 15 different populations, of which we identified nine, as shown in Fig. 24. We derived significantly different mean metallicities for most of these populations, which are all listed in Table 7. In order to compare our results with the previously discussed literature values, they are all plotted in Fig. 25. Note that our three most metal-rich clusters have metallicities of -0.57 (NGC 6388), -0.49 (NGC 6441), and -0.36 (NGC 6624), so our CaT-metallicity is only valid up about these values. Therefore, the most metal-rich populations in NGC 5139 are either outside this limit (P7), or very close to it (P9), and must be treated with care. One of these, namely P7, is part of the bimodality that has been known for decades. Due to the limitation of our calibration at high metallicity, and the fact Ca is enhanced in P7, our metallicity value is higher than expected.

For the more metal-poor populations, the comparison with literature values is better, although we did not try to match individual populations to those from the literature. The metallicity for our lowest-metallicity populations P1 and P2 is a little too low compared to all literature values except Villanova et al. (2014). The intermediate metal-rich populations all have a matching population in at least one previous study. But obviously, not even those agree well with each other.

Comparing the metallicity distributions with the chromosome map, which is also shown in Fig. 15, we see that the metallicity increases steadily both with $\Delta \mathrm{G}$ and $\Delta \mathrm{C}$, as discussed in Sect. 5.1 and shown in Fig. 20.

### 7.8. NGC 5286

The poorly studied cluster NGC 5286 has been classified as Type II by Milone et al. (2017). Three sub-populations have been

Table 7. Parameters of the metallicity distributions, for the whole clusters and single populations (given in 2nd column). Given are the number of stars, the medians $\Theta$, means $\mu$, and standard deviations $\sigma$ of the distributions, as well as the 1 st and 3 rd quartiles $Q_{1}$ and $Q_{3}$.

| NGC | P | \# | $\Theta$ | $\mu$ | $\sigma$ | $Q_{1}$ | $Q_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 104 | - | 2538 | -0.57 | -0.56 | 0.21 | -0.65 | -0.49 |
| 104 | P1 | 340 | -0.51 | -0.50 | 0.17 | -0.58 | -0.42 |
| 104 | P2 | 1270 | -0.58 | -0.56 | 0.18 | -0.64 | -0.51 |
| 362 | - | 1144 | -1.12 | -1.12 | 0.21 | -1.23 | -1.03 |
| 362 | P1 | 218 | -1.09 | -1.08 | 0.19 | -1.17 | -0.99 |
| 362 | P2 | 579 | -1.13 | -1.12 | 0.18 | -1.23 | -1.04 |
| 362 | P3 | 22 | -0.99 | -0.97 | 0.28 | -1.10 | -0.89 |
| 1851 | - | 1358 | -1.02 | -0.99 | 0.32 | -1.13 | -0.90 |
| 1851 | P1 | 184 | -1.03 | -0.99 | 0.41 | -1.12 | -0.95 |
| 1851 | P2 | 353 | -1.05 | -1.04 | 0.23 | -1.12 | -0.98 |
| 1851 | P3 | 265 | -0.92 | -0.89 | 0.22 | -1.00 | -0.80 |
| 1904* | - | 213 | -1.66 | -1.64 | 0.20 | -1.72 | -1.59 |
| 2808 | - | 2512 | -0.98 | -0.96 | 0.35 | -1.13 | -0.84 |
| 2808 | P1 | 297 | -0.95 | -0.93 | 0.31 | -1.08 | -0.83 |
| 2808 | P2 | 336 | -1.00 | -0.97 | 0.33 | -1.13 | -0.86 |
| 2808 | P3 | 481 | -0.94 | -0.88 | 0.35 | -1.06 | -0.78 |
| 2808 | P4 | 144 | -0.91 | -0.88 | 0.37 | -1.06 | -0.76 |
| 2808 | PA | 114 | -0.87 | -0.83 | 0.36 | -1.01 | -0.73 |
| 2808 | PB | 171 | -0.99 | -0.99 | 0.23 | -1.10 | -0.90 |
| 3201 | - | 137 | -1.43 | -1.42 | 0.12 | -1.50 | -1.35 |
| 3201 | P1 | 52 | -1.42 | -1.40 | 0.12 | -1.46 | -1.33 |
| 3201 | P2 | 66 | -1.44 | -1.42 | 0.10 | -1.48 | -1.37 |
| 5139* | - | 1247 | -1.65 | -1.50 | 0.45 | -1.82 | -1.31 |
| 5139* | P1 | 174 | -1.84 | -1.83 | 0.08 | -1.90 | -1.79 |
| 5139* | P2 | 216 | -1.83 | -1.80 | 0.15 | -1.89 | -1.76 |
| 5139* | P3 | 96 | -1.74 | -1.72 | 0.12 | -1.80 | -1.67 |
| 5139* | P4 | 87 | -1.53 | -1.50 | 0.16 | -1.60 | -1.40 |
| 5139* | P5 | 127 | -1.21 | -1.24 | 0.19 | -1.35 | -1.09 |
| 5139* | P6 | 59 | -1.48 | -1.47 | 0.18 | -1.59 | -1.35 |
| 5139* | P7 | 28 | -0.15 | -0.18 | 0.19 | -0.28 | -0.03 |
| 5139* | P8 | 144 | -1.51 | -1.50 | 0.22 | -1.66 | -1.39 |
| 5139* | P9 | 78 | -0.69 | -0.72 | 0.39 | -1.02 | -0.45 |
| 5286 | - | 1149 | -1.76 | -1.74 | 0.22 | -1.86 | -1.65 |
| 5286 | P1 | 226 | -1.79 | -1.77 | 0.14 | -1.86 | -1.69 |
| 5286 | P2 | 332 | -1.76 | -1.75 | 0.15 | -1.83 | -1.68 |
| 5286 | P3 | 104 | -1.57 | -1.53 | 0.27 | -1.66 | -1.48 |
| 5904 | - | 863 | -1.17 | -1.16 | 0.20 | -1.26 | -1.08 |
| 5904 | P1 | 167 | -1.14 | -1.14 | 0.14 | -1.23 | -1.06 |
| 5904 | P2 | 506 | -1.18 | -1.17 | 0.15 | -1.25 | -1.11 |
| 6093 | - | 1071 | -1.81 | -1.78 | 0.20 | -1.89 | -1.73 |
| 6093 | P1 | 269 | -1.81 | -1.80 | 0.14 | -1.88 | -1.74 |
| 6093 | P2 | 437 | -1.80 | -1.77 | 0.19 | -1.87 | -1.73 |
| 6218* | - | 236 | -1.25 | -1.26 | 0.10 | -1.31 | -1.21 |
| 6218* | P1 | 83 | -1.24 | -1.23 | 0.13 | -1.31 | -1.20 |
| 6218* | P2 | 120 | -1.26 | -1.27 | 0.07 | -1.31 | -1.23 |
| 6254 | - | 396 | -1.56 | -1.54 | 0.18 | -1.64 | -1.47 |
| 6254 | P1 | 109 | -1.52 | -1.51 | 0.17 | -1.63 | -1.42 |
| 6254 | P2 | 178 | -1.57 | -1.54 | 0.14 | -1.63 | -1.49 |
| 6266* | - | 2182 | -0.96 | -0.96 | 0.25 | -1.07 | -0.85 |
| 6293* | - | 168 | -2.17 | -2.15 | 0.12 | -2.23 | -2.10 |
| 6388 | - | 4098 | -0.48 | -0.43 | 0.48 | -0.69 | -0.24 |
| 6388 | P1 | 579 | -0.50 | -0.45 | 0.45 | -0.68 | -0.31 |
| 6388 | P2 | 1203 | -0.51 | -0.44 | 0.42 | -0.67 | -0.28 |
| 6388 | P3 | 411 | -0.28 | -0.25 | 0.39 | -0.45 | -0.13 |

Table 7 (Cont.). Parameters of the metallicity distributions.

| NGC | P | $\#$ | $\Theta$ | $\mu$ | $\sigma$ | $Q_{1}$ | $Q_{3}$ |
| :--- | :---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 6441 | - | 4408 | -0.53 | -0.46 | 0.48 | -0.71 | -0.32 |
| 6441 | P 1 | 826 | -0.52 | -0.46 | 0.42 | -0.65 | -0.35 |
| 6441 | P 2 | 1546 | -0.53 | -0.48 | 0.40 | -0.68 | -0.36 |
| $6522^{*}$ | - | 481 | -1.10 | -1.07 | 0.36 | -1.25 | -0.93 |
| 6541 | - | 820 | -1.82 | -1.81 | 0.11 | -1.87 | -1.76 |
| 6541 | P 1 | 274 | -1.81 | -1.80 | 0.09 | -1.85 | -1.75 |
| 6541 | P 2 | 396 | -1.81 | -1.80 | 0.10 | -1.86 | -1.76 |
| 6624 | - | 539 | -0.48 | -0.44 | 0.39 | -0.62 | -0.32 |
| 6624 | P 1 | 119 | -0.39 | -0.34 | 0.33 | -0.56 | -0.20 |
| 6624 | P 2 | 286 | -0.52 | -0.50 | 0.29 | -0.66 | -0.39 |
| 6656 | - | 397 | -1.81 | -1.78 | 0.20 | -1.89 | -1.68 |
| 6656 | P 1 | 107 | -1.87 | -1.87 | 0.09 | -1.93 | -1.82 |
| 6656 | P 2 | 119 | -1.85 | -1.84 | 0.11 | -1.92 | -1.78 |
| 6656 | P 3 | 116 | -1.65 | -1.65 | 0.13 | -1.75 | -1.57 |
| 6681 | - | 325 | -1.47 | -1.44 | 0.27 | -1.56 | -1.38 |
| 6681 | P 1 | 50 | -1.45 | -1.36 | 0.37 | -1.55 | -1.34 |
| 6681 | P 2 | 208 | -1.47 | -1.45 | 0.24 | -1.55 | -1.38 |
| 6752 | - | 539 | -1.54 | -1.53 | 0.12 | -1.61 | -1.48 |
| $6752^{*}$ | P 1 | 114 | -1.52 | -1.52 | 0.10 | -1.59 | -1.47 |
| $6752^{*}$ | P 2 | 264 | -1.53 | -1.51 | 0.12 | -1.58 | -1.46 |
| 7078 | - | 1318 | -2.25 | -2.24 | 0.10 | -2.30 | -2.20 |
| 7078 | P 1 | 331 | -2.28 | -2.27 | 0.08 | -2.32 | -2.23 |
| 7078 | P 2 | 259 | -2.26 | -2.26 | 0.09 | -2.31 | -2.22 |
| 7078 | P 3 | 292 | -2.24 | -2.23 | 0.07 | -2.27 | -2.19 |
| 7089 | - | 1727 | -1.59 | -1.57 | 0.19 | -1.67 | -1.51 |
| 7089 | P 1 | 238 | -1.59 | -1.57 | 0.15 | -1.66 | -1.50 |
| 7089 | P 2 | 930 | -1.59 | -1.58 | 0.15 | -1.66 | -1.52 |
| 7089 | P 3 | 30 | -1.42 | -1.34 | 0.25 | -1.50 | -1.18 |
| 7099 | - | 289 | -2.20 | -2.18 | 0.09 | -2.23 | -2.16 |
|  |  |  |  |  |  |  |  |

found based on a CN index by Lim et al. (2017), which they also group into two populations with different calcium HK' strengths that also differ in abundances of Fe and s-process elements. Marino et al. (2015) called the cluster anomalous and found two populations with a metallicity split of 0.17 dex. In our data we also see a clear split in metallicity, with -1.72 and -1.71 dex for the populations P1 and P2, respectively, and -1.60 dex for population P3.

### 7.9. NGC 5904 / M 5

Lee (2017) found bimodal CN and $[\mathrm{N} / \mathrm{Fe}]$ distributions in NGC 5904 and Carretta et al. (2009c) also confirmed the existence of the well-known Na-O anticorrelation. They found it to be homogeneous in $[\mathrm{Fe} / \mathrm{H}]$ at a level below $6 \%$, so we do not expect to see any split.

### 7.10. NGC 6093 / M 80

Even in their title Carretta et al. (2015) call NGC 6093 a cluster with a "normal chemistry", which we can confirm with the inconspicuous, Gaussian-shaped metallicity distribution as derived from our results.

### 7.11. NGC6218 / M 12

Carretta et al. (2007) found no star-to-star scatter of metallicity in NGC 6218, which we can confirm from our results, both
with the overall distribution as well as with the non-existence of any separation of metallicities between the two populations (see Fig. 27).

### 7.12. NGC 6254 / M 10

NGC 6254 shows no sign of any metallicity spread and no significant separation can be found for its two populations, which is consistent with no report of abnormalities in the literature.

### 7.13. NGC 6266 / M 62

For NGC 6266 we see a very broad metallicity distribution, similar to that of NGC 104 or NGC 1851. Also the typical uncertainties are similar, although the distribution for NGC 6266 extends to higher values. Unfortunately, due to missing UV photometry we could not create a chromosome map, so we were not able to investigate, whether this is caused by a split in metallicity between populations. However, Yong et al. (2014a) found no evidence for a dispersion in metallicity - however, with data for only 7 bright giants.

### 7.14. NGC 6293

With only 168 stars, our sample for NGC 6293 is very small, which is reflected in the metallicity distribution in Fig. 16. There may be a second peak in metallicity at $[\mathrm{Fe} / \mathrm{H}]-\langle[\mathrm{Fe} / \mathrm{H}]\rangle \approx$ +0.2 dex. No chromosome map is available for this cluster.

### 7.15. NGC 6388

Similar to NGC 6441, the analysis of the results for NGC 6388 get a little cumbersome due to the large uncertainties we get for the metallicities, yielding a very broad and asymmetric distribution of metallicities. Furthermore, as a result of the difficult photometry (see discussion in Sect. 2) the chromosome map for this cluster is a little messy, so separating populations becomes difficult. Nevertheless, as shown in Fig. 27, we still see a significant split of about 0.22 dex in metallicity between the populations P1/P2 and P3, as expected for a Type II cluster. However, Carretta \& Bragaglia (2018) excluded the existence of any intrinsic Fe dispersion in NGC 6388.

### 7.16. NGC 6441

While NGC 6388 and NGC 6441 are pretty similar with both being massive metal-rich bulge clusters, Milone et al. (2017) classified the former as Type II and the latter as Type I cluster. Both also share the problematic photometry, so the quality of the spectra seems to be degraded from the extraction process (see Sect. 2), affecting the metallicity distribution we obtain. However, lacking an obvious P3 population in the chromosome map, we can only confirm the status of NGC 6441 as a simple Type I.

### 7.17. NGC 6522

Our sample of stars in the oldest known globular cluster in the Milky Way is very small, but the derived metallicity distribution does not show any abnormalities. No chromosome map is available for this cluster.

### 7.18. NGC6541

The metallicity distribution of the poorly studied NGC 6541 shows no sign of any metallicity spread and also no variation in metallicity between its two populations.

### 7.19. NGC 6624

NGC 6624 is one of the clusters, for which we only have a very small sample of RGB stars and also get relatively large uncertainties for the derived metallicities. Nevertheless, we might see a bimodal distribution for its two populations in Fig. 19, although with both being very broad.

### 7.20. NGC 6656 / M 22

Mauro et al. (2014) found a split in [ $\mathrm{Fe} / \mathrm{H}]$ for this Type II cluster using CaT spectroscopy - although the separation they found is quite large with $0.3-0.4$ dex. A separation of populations was also observed in Ca by photometry by Lee (2015), where they suggest a merger scenario. Milone et al. (2012b) found a bimodality of metallicities with $[\mathrm{Fe} / \mathrm{H}]_{\text {rich }}=(-1.68 \pm 0.02)$ dex and $[\mathrm{Fe} / \mathrm{H}]_{\text {poor }}=(-1.82 \pm 0.02)$ dex, i.e. $\sigma_{[\mathrm{Fe} / \mathrm{H}]}=0.14 \mathrm{dex}$. An abundance difference of $(0.15 \pm 0.02)$ dex was reported by Marino et al. (2015). Marino et al. (2011) also found a difference of about 0.1 dex in Ca between their $s$-rich and $s$-poor stars. From our data we get a separation of $\sim 0.2$ dex, which might be overestimated if the populations indeed have a different Ca abundance.

### 7.21. NGC 6681 / M 70

O'Malley et al. (2017) confirmed the existence of the Na-O anticorrelation and found no sign of an intrinsic metallicity dispersion. Although having only few stars in our sample, their results are of good quality and we also see no sign of any spread in metallicity.

### 7.22. NGC6752

Although Milone et al. (2013) identified three different populations along the whole evolutionary sequence in NGC 6752, they could only find two of them using their chromosome maps in Milone et al. (2017), which we adopted for our analysis. Two stellar populations have also been reported by Yong et al. (2015) and Lee (2018), based on their different $\mathrm{C}+\mathrm{N}+\mathrm{O}$ content, while Yong et al. (2013) found no significant variation in iron-peak elements, even calling it one of the least complex clusters. We can confirm this conclusion with our results, which show neither any kind of broadening in the overall distribution, nor any variation between the two populations.

### 7.23. NGC 7078 / M 15

Together with NGC 7099, the massive cluster NGC 7078 is the most metal-poor one in our sample $\left([\mathrm{Fe} / \mathrm{H}]_{\mathrm{D} 16}=-2.28\right)$. M 15 is a peculiar cluster with an unusual distribution of P1 stars being more centrally concentrated than P2 stars (Larsen et al. 2015). It also shows no sign of a CN bimodality on the RGB (Cohen et al. 2005), but, in contrast to other low-metallicity clusters, there is one on the MS (Pancino et al. 2010).

Three populations have originally been identified in the chromosome map (Larsen et al. 2015). Nardiello et al. (2018b) even


Fig. 26. Metallicity distributions for NGC 7078.
found five populations and argue that it might actually be Type II cluster. For our analysis, as shown in Fig. 26, we ignore the suggested split in the primordial population and we were not able to separate their population E that hints towards Type II. However, we see a clear offset of population P3, which is probably caused by a contamination of this population. The difference in metallicity between $\mathrm{P} 1 / \mathrm{P} 2$ and P 3 is $\sim 0.03$ dex.

No spread in metallicity has been reported in the literature and Carretta et al. (2009c) suggests that NGC 7078 may not contain a large number of stars with a different chemical composition. According to Nardiello et al. (2018b), only 5\% of stars should belong to this population.

### 7.24. NGC 7089 / M2

After a split on the SGB for this Type II cluster has been reported by Piotto et al. (2012), a connection to the s-process bimodality along the RGB was made by Lardo et al. (2013), emphasizing also a similarity to the other Type II clusters NGC 1851 and NGC 6566. Even seven populations have been found by Milone et al. (2015a) based on UV photometry.

Metallicities on the RGB have been measured from highresolution spectra by Yong et al. (2014b), finding three distinct populations: a main population with $[\mathrm{Fe} / \mathrm{H}]=-1.67 \pm$ 0.02 dex and two anomalous groups with $-1.51 \pm 0.04$ and $-1.03 \pm 0.03$ dex, respectively, yielding a split of $\sim 0.16$ dex of the first one to the main group. They also adopted a CaT analysis like the one presented in this paper, and calculated metallicities from some medium-resolution spectra, obtaining $[\mathrm{Fe} / \mathrm{H}]=-1.58 \pm 0.08 \mathrm{dex}$ for the normal and $-1.29 \pm 0.09 \mathrm{dex}$ for the anomalous groups. They separate the latter into two subgroups with five stars each and obtain similar results as for the high-resolution spectra, i.e. $-1.47 \pm 0.05$ and $-0.98 \pm 0.06 \mathrm{dex}$, respectively.

Unfortunately, in our data we only have 30 stars from population P3, so its metallicity distribution is not well defined. We obtain a difference of about 0.17 dex from the medians and even 0.23 dex from the means. There is also a clear separation of the $Q_{1}-Q_{3}$ intervals.

### 7.25. NGC 7099 / M 30

From our data, NGC 7099 shows neither a significant broadening of the overall metallicity distribution, nor any separation for its two populations, which is consistent with previous studies (like, e.g., O'Malley \& Chaboyer 2018), which found evidence for multiple populations, but no abnormalities in metallicity.

## 8. Conclusions

In this paper, we measured equivalent widths of the infrared Ca triplet for almost 34,000 red giants in 25 Galactic globular clusters. We followed a classical approach using a linear relation on stars brighter than the HB to obtain so-called reduced equivalent widths. However, with this approach, about $80 \%$ of our RGB sample would excluded, so we presented an extension of this calibration to stars fainter than the HB and showed that it is still valid when using a quadratic term in the relation.

Being aware that the brightness of the horizontal branch can not be used as a reference for field stars, we also presented a calibration based on absolute magnitudes in F606W. Furthermore, we calculated bolometric corrections for all the stars in our sample and derived luminosities. That way, we were able to replace the commonly used calibration based on $V-V_{\mathrm{HB}}$ by one using luminosities, which, in the era of Gaia, is now readily available for many stars, or will be in the near future.

Using our CaT-metallicity calibration, we derived metallicities for about 30,000 stars in 25 globular clusters with typical

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Fig. 27. Metallicity distributions for the different stellar populations in our Type I clusters, equivalent to Fig. 19.




Fig. 27 (Cont.). Metallicity distributions.
uncertainties of $\sim 0.12$ dex. We created histograms for each of the clusters, showing the distribution of metallicities. Then we used HST UV photometry, when available, to create chromosome maps of the clusters and investigated the metallicity distributions of the different populations. We found that the metallicity distribution of the P3 population is clearly different than that of P1 and P2 in the seven Type II clusters in our sample. This adds further evidence to the idea that these clusters, also called metal-complex, harbor populations that have different metallicities. We discussed NGC 5139 ( $\omega$ Centauri) in detail, presenting its complex metallicity structure, and the Type I cluster NGC 2808, which also shows some interesting sub-structure among its various populations. For NGC 7078 we show more evidence that it probably also is a Type II cluster, as discussed by Nardiello et al. (2018b). For all the other Type I clusters we find no significant split or spread in metallicity.

In this paper, we showed that our unprecedented large sample of spectra from GC stars, even with a relatively low resolution of $R=2000-4000$, could be used to measure abundances in groups of stars to an accuracy formerly only reached with high-resolution spectroscopy. This finding is in comfortable agreement with Kirby et al. (2008) who made a careful one-toone comparison of metallicities obtained from medium and high resolution spectroscopy, however avoiding the CaT. In the future, we are planning to extend the equivalent width technique towards higher metallicities in partially resolved stellar populations of nearby galaxies (Roth et al. 2018).
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## Appendix A: Additional figures



Fig. A.1. Similar to Figs. 7 and 9, but here the sum of the equivalent widths $\Sigma \mathrm{EW}$ of the two strongest Ca lines is plotted over the absolute magnitude in F606W $M_{\mathrm{F} 606 \mathrm{~W}}$ for all RGB stars. Quadratic fits to each individual cluster are shown in orange, while a global fit, where the same values for $\beta$ and $\gamma$ are used (giving $\beta=-0.426 \pm 0.002$ and $\gamma=0.053 \pm 0.001$ ), is plotted for each cluster in blue.


Fig. A.2. Similar to Figs. 7 and 9 , but here the sum of the equivalent widths $\Sigma E W$ of the two strongest Ca lines is plotted over log $L / L_{\odot}$ for all RGB stars. Quadratic fits to each individual cluster are shown in orange, while a global fit, where the same values for $\beta$ and $\gamma$ are used (giving $\beta=1.006 \pm 0.005$ and $\gamma=0.260 \pm 0.007$ ), is plotted for each cluster in blue.


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