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# Measurement of Inelastic $J / \boldsymbol{\psi}$ and $\boldsymbol{\Psi}{ }^{\prime}$ Photoproduction at HERA 

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# Measurement of inelastic $J / \psi$ and $\psi^{\prime}$ photoproduction at HERA 

## The ZEUS collaboration

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Abstract: The cross sections for inelastic photoproduction of $J / \psi$ and $\psi^{\prime}$ mesons have been measured in $e p$ collisions with the ZEUS detector at HERA, using an integrated luminosity of $468 \mathrm{pb}^{-1}$ collected in the period 1996-2007. The $\psi^{\prime}$ to $J / \psi$ cross section ratio was measured in the range $0.55<z<0.9$ and $60<W<190 \mathrm{GeV}$ as a function of $W, z$ and $p_{T}$. Here $W$ denotes the photon-proton centre-of-mass energy, $z$ is the fraction of the incident photon energy carried by the meson and $p_{T}$ is the transverse momentum of the meson with respect to the beam axis. The $J / \psi$ cross sections were measured for $0.1<z<0.9,60<W<240 \mathrm{GeV}$ and $p_{T}>1 \mathrm{GeV}$. Theoretical predictions within the nonrelativistic QCD framework including NLO colour-singlet and colour-octet contributions were compared to the data, as were predictions based on the $k_{T}$-factorisation approach.

Keywords: Lepton-Nucleon Scattering, QCD

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## 1 Introduction

The inelastic production of $J / \psi$ and of $\psi^{\prime}$ has been studied for several years in hadron and electron-proton colliders and in fixed target experiments [1]. At HERA, the reactions

$$
\begin{equation*}
e p \rightarrow e J / \psi X \tag{1.1}
\end{equation*}
$$

and

$$
\begin{equation*}
e p \rightarrow e \psi^{\prime} X \tag{1.2}
\end{equation*}
$$

have been studied $[2,3]$ for low virtuality of the exchanged photon (photoproduction) in the range $z<0.9$, where $z$ denotes the fraction of the incident photon energy carried by the meson in the proton rest frame, thus excluding the diffractive process for which $z \sim 1$. In the HERA photoproduction regime, the production of inelastic $J / \psi$ or $\psi^{\prime}$ mesons arises mostly from direct and resolved photon interactions. In leading-order (LO) Quantum Chromodynamics (QCD), the two processes can be distinguished; in directphoton processes the photon enters directly into the hard interaction; in resolved-photon processes the photon acts as a source of partons, one of which participates in the hard
interaction. The inelastic process in the photoproduction region is dominated by photongluon fusion. In this direct-photon process the photon emitted from the incoming electron interacts with a gluon from the proton to produce a pair of charm-anticharm quarks, $c \bar{c}$, which then turn into the $J / \psi$ or the $\psi^{\prime}$ mesons. When the $c \bar{c}$ pair emerges from the hard process with the quantum numbers of the mesons, the reaction is described in the framework of perturbative Quantum Chromodynamics (pQCD) by models such as the Colour Singlet (CS) model. In the Colour Octet (CO) model, the $c \bar{c}$ pair emerges from the hard process with quantum numbers different from those of the mesons and emits one or more soft gluons before turning into the physical meson state. Examples of direct-photon LO diagrams with a CS and a CO hard subprocess are shown in figure 1.

Full next-to-leading order (NLO) $J / \psi$ cross section predictions using only the directphoton CS contributions have already been performed [4-6]. The non-relativistic QCD framework (NRQCD) [7] allows the evaluation of $J / \psi$ cross sections including direct and resolved photon processes with CS and CO contributions. The former contribution can be thought of as the first term of the NRQCD expansion and so it is an integral component of this theoretical formalism. Recently, the full computation was performed in the HERA photoproduction regime at the NLO level $[8,9]$. The numerical values of the CS and CO matrix elements were obtained from a global fit to hadroproduction, electroproduction and photoproduction inelastic $J / \psi$ data $[8,9]$.
$J / \psi$ cross sections have also been evaluated $[10,11]$ in the $k_{T}$-factorisation approach [1215]. In this model, based on non-collinear parton dynamics governed by the CCFM [16, 17] evolution equations, effects of non-zero gluon transverse momentum are taken into account. Cross sections are then calculated as the convolution of unintegrated, transversemomentum dependent gluon densities and LO off-shell matrix elements. Direct and resolved photon processes are included. The matrix elements are computed in the CS model.

Measurements of the reactions (1.1) and (1.2) have been previously performed by the ZEUS collaboration [2], using an integrated luminosity of $38 \mathrm{pb}^{-1}$, and by the H1 collaboration [3], using an integrated luminosity of $165 \mathrm{pb}^{-1}$. Total and differential cross sections were presented as a function of various kinematical variables. The H1 and ZEUS collaborations have also published a measurement of the $J / \psi$ helicity distribution [3, 18], the ZEUS result was obtained using the full HERA luminosity. LO and NLO QCD predictions, as well as LO NRQCD calculations, were compared to the measurements. None of the calculations could describe the data in the whole kinematic range of the measurements. The data were shown to have the potential to reduce the large uncertainties in the phenomenological parameters used in the calculations.

In this paper, measurements of reactions (1.1) and (1.2) are presented using a luminosity of $468 \mathrm{pb}^{-1}$. The $J / \psi$ and $\psi^{\prime}$ mesons were identified using the $\mu^{+} \mu^{-}$decay modes.

The $\psi^{\prime}$ to $J / \psi$ cross section ratio was measured in the range $60<W<190 \mathrm{GeV}$ and $0.55<z<0.9$ as a function of $W, z$ and $p_{T}$. Here $W$ is the $\gamma p$ centre-of-mass energy and $p_{T}$ is the transverse momentum of the mesons with respect to the beam axis. The cross sections for inelastic $J / \psi$ photoproduction as a function of $p_{T}^{2}$, for different $z$ ranges, and as a function of $z$, for different $p_{T}$ ranges, were measured in the range $60<W<240 \mathrm{GeV}$, $0.1<z<0.9$ and $p_{T}>1 \mathrm{GeV}$. The momentum flow along and against the $J / \psi$ direction
of flight in the laboratory frame, as obtained from the charged tracks produced together with the $J / \psi$ in the range $60<W<240 \mathrm{GeV}, 0.3<z<0.9$ and $1<p_{T}<10 \mathrm{GeV}$, was studied in order to shed further light on the production mechanisms.

## 2 Experimental set-up

The analysis presented here is based on data collected by the ZEUS detector at HERA in the period 1996-2007. In 1998-2007 (1996-1997), HERA provided electron ${ }^{1}$ beams of energy $E_{e}=27.5 \mathrm{GeV}$ and proton beams of energy $E_{p}=920(820) \mathrm{GeV}$, resulting in a centre-ofmass energy of $\sqrt{s}=318(300) \mathrm{GeV}$, giving an integrated luminosity of $430(38) \mathrm{pb}^{-1}$.

A detailed description of the ZEUS detector can be found elsewhere [19, 20]. A brief outline of the components that are most relevant for this analysis is given below.

Charged particles were tracked in the central tracking detector (CTD) [21-23], which operated in a magnetic field of 1.43 T provided by a thin superconducting coil. Before the 2003-2007 running period, the ZEUS tracking system was upgraded with a silicon microvertex detector (MVD) [24]. In the following, the term "CTD-MVD track" denotes generically both the tracks measured in the CTD and (after 2002) in the CTD and MVD.

The high-resolution uranium-scintillator calorimeter (CAL) [25-28] consisted of three parts: the forward (FCAL), the barrel (BCAL) and the rear (RCAL) calorimeters. ${ }^{2}$ Each part was subdivided transversely into towers and longitudinally into one electromagnetic section (EMC) and either one (in RCAL) or two (in BCAL and FCAL) hadronic sections (HAC). The smallest subdivision of the calorimeter was called a cell. The CAL energy resolutions, as measured under test-beam conditions, were $\sigma(E) / E=0.18 / \sqrt{E}$ for electrons and $\sigma(E) / E=0.35 / \sqrt{E}$ for hadrons ( $E$ in GeV ). The timing resolution of the CAL was better than 1 ns for energy deposits greater than 4.5 GeV .

Muons were identified as tracks measured in the barrel and rear muon chambers (BMUON and RMUON) [29]. The muon chambers were placed inside and outside the magnetised iron yoke surrounding the CAL. The barrel and rear inner muon chambers (BMUI and RMUI) covered the polar-angle regions $34^{\circ}<\theta<135^{\circ}$ and $135^{\circ}<\theta<171^{\circ}$, respectively.

The luminosity was measured using the Bethe-Heitler reaction $e p \rightarrow e \gamma p$ with the luminosity detector which consisted of a lead-scintillator calorimeter [30-32] and, after 2002, of an additional magnetic spectrometer [33] system. The fractional systematic uncertainty on the measured luminosity was $1.9 \%$.

[^0]
## 3 Event selection and kinematic variables

The online and offline selections, as well as the reconstruction of the kinematic variables, closely follow the previous analysis [2].

Online, the BMUI and RMUI chambers were used to tag muons by matching segments in the muon chambers with CTD-MVD tracks, as well as with energy deposits in the CAL consistent with the passage of a minimum-ionising particle (m.i.p.).

The different steps of the offline selection procedure are described in the following paragraphs. An event was accepted if it had two primary-vertex CTD-MVD tracks with invariant mass between $2-5 \mathrm{GeV}$. One track had to be identified in the inner muon chambers and matched to a m.i.p. cluster in the CAL. It was required to have a momentum greater than 1.8 GeV if it was in the rear region or a transverse momentum greater than 1.4 GeV if in the barrel region. The other track had to be matched to a m.i.p. cluster in the CAL and was required to have a transverse momentum greater than 0.9 GeV . Both tracks were restricted to the pseudorapidity region $|\eta|<1.75$. To reject cosmic rays, events in which the angle between the two muon tracks was larger than $174^{\circ}$ were removed.

In addition, events were required to have a calorimetric energy deposit larger than 1 GeV in a cone of $35^{\circ}$ around the forward direction (excluding possible calorimeter deposits due to the decay muons). This requirement completely rejects exclusively produced $J / \psi$ mesons, $e p \rightarrow e p J / \psi$. It also strongly suppresses the background from proton diffractivedissociation, $e p \rightarrow e N J / \psi$, because the low invariant mass hadronic system $N$ can often (but not always) escape along the outgoing proton direction without any activity in the FCAL. A reduction of the remaining background is achieved by requiring the events to have, in addition to the two decay muon tracks, at least one additional track with transverse momentum larger than 250 MeV and pseudorapidity $|\eta|<1.75$.

The $\psi^{\prime}$ production in proton diffractive-dissociation processes with the decay chain $J / \psi\left(\rightarrow \mu^{+} \mu^{-}\right) \pi^{+} \pi^{-}$was identified in the selected data sample. For the bulk of these events only four charged tracks are visible in the detector. For the events with a $\mu^{+} \mu^{-}$ invariant mass, $m_{\mu \mu}$, in the interval $[2.85,3.30] \mathrm{GeV}$, and with exactly two additional primary-vertex tracks of opposite charge, the total invariant mass $m_{4}$ of the four tracks was evaluated. Events with a mass difference $m_{4}-m_{\mu \mu}$ within $\pm 60 \mathrm{MeV}$ of the nominal mass difference $m_{\psi^{\prime}}-m_{J / \psi}=589 \mathrm{MeV}$ [34] were discarded. This topology was tagged only in $1.2 \%$ of the overall selected $J / \psi$ sample and removed.

These requirements effectively select inelastic $J / \psi$ and $\psi^{\prime}$ mesons. $J / \psi$ and $\psi^{\prime}$ mesons from decays of $b$ hadrons are also included in the data sample.

The kinematic region considered was defined by the inelasticity variable $z$ and by the photon-proton centre-of-mass energy

$$
\begin{equation*}
W^{2}=(P+q)^{2}, \tag{3.1}
\end{equation*}
$$

where $P$ and $q$ are the four-momenta of the incoming proton and the exchanged photon, respectively. It was calculated using

$$
\begin{equation*}
W^{2}=2 E_{p}\left(E-p_{Z}\right), \tag{3.2}
\end{equation*}
$$

where $\left(E-p_{Z}\right)$, the difference between the energy and the momentum along the $Z$ axis, is summed over all final-state energy-flow objects [35, 36] (EFOs) which combine the information from calorimetry and tracking.

The inelasticity $z=\frac{P \cdot p_{\psi}}{P \cdot q}$ was determined as

$$
\begin{equation*}
z=\frac{\left(E-p_{Z}\right)_{\psi}}{\left(E-p_{Z}\right)} \tag{3.3}
\end{equation*}
$$

where $\psi$ can be either a $J / \psi$ or a $\psi^{\prime}$ meson, $p_{\psi}$ is the four-momentum of the $\psi$ and $\left(E-p_{Z}\right)_{\psi}$ was calculated using the two tracks forming the $\psi$.

In order to reject deep inelastic scattering, events were required to have $E-p_{Z}<32$ GeV . This restricts the virtuality of the exchanged photon, $Q^{2}=-q^{2}$, to $Q^{2} \lesssim 1 \mathrm{GeV}^{2}$, with a median of about $10^{-4} \mathrm{GeV}^{2}$. The elimination of deep inelastic scattering events was independently confirmed by searching for scattered electrons in the CAL [37]; none was found.

Table 1 summarises the various kinematic regions used for the presented measurements.

## 4 Monte Carlo models

The inelastic production of $J / \psi$ and $\psi^{\prime}$ mesons was simulated using the Herwig 6.100 [38] program, which generates direct photon events according to the LO diagrams of the photongluon fusion process, $\gamma g \rightarrow \psi g$. The processes are calculated in the framework of the CS model. The Herwig MC provides in general a good description of the data. To improve the agreement further, the $p_{T}$ spectrum was reweighted to the data. The average weight of the MC events with $p_{T}$ around 1 GeV is 0.85 . The average weight for $p_{T}>4 \mathrm{GeV}$ is instead 1.8.

Diffractive production of $J / \psi$ and $\psi^{\prime}$ mesons with proton dissociation was simulated with the Epsoft [39] MC generator, which was tuned to describe such processes at HERA [40].

The Pythia 6.220 MC generator [41-43] was used to generate $J / \psi$ and $\chi_{c}$ states from the resolved-photon process, with LO matrix elements computed in the CS model. The generator cross sections for the $J / \psi$ and $\chi_{c}$ states are very similar. For the generation of the $\chi_{c 1}(1 P)$ and $\chi_{c 2}(1 P)$ mesons, only the $J / \psi \gamma$ decay channel was considered. The final state photon is at low energy, $O(400) \mathrm{MeV}$, basically indistinguishable from the remaining hadronic activity of the event. Hence the effective resolved-photon $J / \psi$ contribution can be thought of as due to the genuine resolved-photon component plus the $\chi_{c}$ feed-down. The resolved $\psi^{\prime}$ contribution was neglected due to the small resolved-to-direct cross section ratio and to the additional reduction due to the $\psi^{\prime} \rightarrow J / \psi X$ branching ratio.

The Pythia MC was also used to generate the production of $J / \psi$ and $\psi^{\prime}$ mesons originating from $b$ hadron decays, mostly from $B$-mesons. The following beauty-quark production processes were generated (according to the PYthia notation): direct, resolved, $\gamma$ and proton excitation. The beauty-quark mass was set to 4.75 GeV and the branching ratios of the $b$ hadrons to $J / \psi$ and $\psi^{\prime}$ were set to the corresponding PDG [34] values.

All generated events were passed through a full simulation of the ZEUS detector based on Geant 3 [44]. They were then subjected to the same trigger requirements and processed by the same reconstruction program as the data.

## 5 Signal determination and cross sections calculation

The invariant-mass spectrum of the muon pairs measured in the phase space region used in the determination of the $\psi^{\prime}$ to $J / \psi$ cross section ratio, $60<W<190 \mathrm{GeV}$ and $0.55<$ $z<0.9$, is shown in figure 2. A non-resonant background contribution, mostly due to hadrons misidentified as muons, is also visible. This contribution was estimated by fitting the product of a second-order polynomial and an exponential function to the region $2-$ 2.75 and $3.8-5 \mathrm{GeV}$, outside the $J / \psi$ and $\psi^{\prime}$ invariant-mass window. The number of $J / \psi$ events was obtained by subtracting the number of background events, estimated from the fit procedure, from the total number of events inside the $J / \psi$ invariant-mass window, 2.853.3 GeV . This procedure resulted in $11295 \pm 114 \mathrm{~J} / \psi$ events. The same procedure applied to the $\psi^{\prime}$ invariant-mass window, $3.55-3.8 \mathrm{GeV}$, gave $448 \pm 34$ events.

Applying the same procedure to the phase space region used for the differential $J / \psi$ cross section measurements, $60<W<190 \mathrm{GeV}, 0.1<z<0.9$ and $p_{T}>1 \mathrm{GeV}, 12671 \pm$ $161 J / \psi$ events were found. The fitting procedure described above was performed for each measurement bin presented in this paper.

The cross section for any observable, $\mathcal{O}$, was computed for each bin, $i$, using correction factors, $C_{i}(\mathcal{O})$, defined as $C_{i}(\mathcal{O})=N_{i}^{\text {gen }}(\mathcal{O}) / N_{i}^{\mathrm{rec}}(\mathcal{O})$, where $N_{i}^{\text {gen }}(\mathcal{O})$ is the number of events generated with the Herwig MC and $N_{i}^{\text {rec }}(\mathcal{O})$ is the number of the events reconstructed by the standard analysis chain. The factors $C_{i}(\mathcal{O})$ take into account the overall acceptance including the geometrical acceptance and the detector, trigger and reconstruction efficiencies. They also take into account bin-to-bin migrations.

For $0.9<z<1$, the events are largely diffractive. Therefore, the analysis of inelastic $J / \psi$ production was restricted to the region $0.1<z<0.9$. In order to further suppress diffractive events, the transverse momentum of the $J / \psi$ mesons had to fulfill $p_{T}>1$ GeV . The remaining contamination was estimated by fitting the relative fractions of nondiffractive and diffractive events to the data $z$-distribution, using the Herwig and Epsoft MC simulations as templates. From this fit, the overall diffractive background contribution for $0.1<z<0.9$ is $4.6 \pm 1.6 \%$.

In figure 3 the Herwig and Epsoft MC mixture, in the kinematic region $60<W<$ $240 \mathrm{GeV}, 0.3<z<0.9$ and $p_{T}>1 \mathrm{GeV}$, is compared to the data: a reasonable description is found. The region $0.1<z<0.3$ was removed because no diffractive background is present at low $z$. The estimated diffractive background was subtracted bin by bin from the measured differential cross sections.

The cross sections measured in this analysis include also contributions from resolvedphoton processes and from decays of beauty hadrons. Inelastic $J / \psi$ production via the resolved-photon process has not been measured explicitly up to now in the photoproduction regime. QCD predictions, as well as the Pythia MC simulation described in section 4, indicate that this contribution is largest at low $z$ values. For $z<0.1$, the expected size of
this contribution can be larger than the direct-photon component. However, for $z>0.1$, the resolved-to-direct photon production ratio is expected to be small. Since the acceptances obtained from the Herwig and Pythia MC simulations are similar, the Herwig MC alone was used for the overall acceptance corrections.

The contribution to the measured cross sections due to $J / \psi$ originating from $B$ meson decays was estimated using the inclusive beauty Pythia MC sample described in section 4. The simulation predictions were scaled by a factor 1.11 according to the recent ZEUS measurement [45] of beauty photoproduction. ${ }^{3}$ This leads to the estimation that on average $1.6 \%$ of the observed $J / \psi$ mesons originated from beauty hadron decays. The largest relative contribution, $4.5 \%$, is in the kinematic region $0.1<z<0.3$ and $1<p_{T}^{2}<2 \mathrm{GeV}^{2}$. This component is not subtracted from the measured cross sections.

## 6 Systematic uncertainties

For all the measured quantities, the following sources of systematic uncertainties were investigated (their effects on the measured cross sections are given in parentheses):

- muon trigger and reconstruction efficiencies: the BMUI and RMUI muon chamber efficiencies were extracted from the data using muon pairs from elastic $J / \psi$ events and from the process $\gamma \gamma \rightarrow \mu^{+} \mu^{-}$. These efficiencies take into account the full muon acquisition chain, from the online to the offline level and are known with a $\pm 5 \%$ uncertainty ( $5 \%$ uniformly distributed in $p_{T}$ and $z$ );
- hadronic energy resolution: the $W$ and $z$ resolutions are dominated by the hadronic energy resolution affecting the quantity $\left(E-p_{Z}\right)$. The hadronic $\left(E-p_{Z}\right)$ resolution in the MC was smeared event by event by $\pm 20 \%$, a conservative upper limit of a possible systematic difference between data and MC. This gave only small cross sections variations ( $<5 \%$ );
- Herwig MC $p_{T}$ spectrum: the $p_{T}$ spectrum of the $J / \psi$ mesons in the Herwig MC simulation was varied within ranges allowed by the comparison between data and simulation and the correction factors were re-evaluated ( $<5 \%$ );
- $J / \psi$ helicity distribution: the $J / \psi$ helicity distribution can be described by two parameters $\lambda$ and $\nu$ [47]. In the Herwig MC these are set to zero. According to the direct measurement of the helicity parameters performed by ZEUS [18], all data points lie within the region of the $\lambda-\nu$ plane defined by $|\lambda|<0.5$ and $|\nu|<0.5$ with only a mild $p_{T}$ or $z$ dependence. Hence, as a systematic check, the Herwig MC was reweighted varying independently $\lambda$ and $\nu$ in the range $\pm 0.5$ and the correction factors were re-evaluated ( $5-10 \%$ depending on the $p_{T}$ and $z$ region);
- diffractive simulation: the Epsoft MC simulation parameters were varied within ranges allowed by the comparison between data and the Epsoft MC simulation in

[^1]the region $0.9<z<1$. The diffractive background was re-evaluated ( $<5 \%$ at high $z$ and low $p_{T}$, negligible elsewhere);

- diffractive subtraction: the relative fraction of inelastic and diffractive processes, as represented by the HERwig and Epsoft MC, was fixed by the procedure described in section 5 . It is known to a precision limited by the number of $J / \psi$ events in the data and the process modeling by the MCs. The relative fractions were varied within ranges allowed by the comparison between data and simulation (up to $10 \%$ at high $z$ and low $p_{T}$, negligible elsewhere);
- invariant-mass window: the $m_{\mu^{+} \mu^{-}}$invariant-mass window used to estimate the number of $J / \psi$ events above the non-resonant background was enlarged to $[2.8,3.35] \mathrm{GeV}$ and tightened to $[2.9,3.3] \mathrm{GeV}$. For the $\psi^{\prime}$ to $J / \psi$ cross section ratios, similar mass window variations were also applied for the $\psi^{\prime}$ signal (generally $<5 \%$, up to $10 \%$ at low $z$ values where the number of expected and observed events is small and the non-resonant background is largest);
- additional track cut: the requirement of three tracks, including the two $J / \psi$ decay muons, with transverse momentum larger than 250 MeV and pseudorapidity $|\eta|<$ 1.75 , was replaced by the requirement of five tracks with transverse momentum larger than 125 MeV , in the same pseudorapidity range. With this stronger requirement the diffractive $J / \psi$ background and the diffractive $\psi^{\prime}$ contribution via the cascade decay $J / \psi\left(\rightarrow \mu^{+} \mu^{-}\right) \pi^{+} \pi^{-}$are expected to vanish. Furthermore, a change in the overall multiplicity cut allows a test of how well the MC model reproduces the data in this respect. The MC mixture gives a fair description of the track multiplicity observed in the data. The cross sections were re-evaluated with the harder multiplicity cut (generally $<5 \%$, up to $20 \%$ in some bins at low $z$ and high $z$ high $p_{T}$ ).

All of the above individual sources of systematic uncertainty were added in quadrature. The following sources would result in an overall small shift of the cross sections:

- the integrated luminosity determination gave an uncertainty of $\pm 1.9 \%$;
- the $J / \psi \rightarrow \mu^{+} \mu^{-}$branching ratio, $5.93 \pm 0.06 \%$ [34], gave an uncertainty of $\pm 1 \%$.

They were not included.

## 7 Results

## $7.1 \quad \psi^{\prime}$ to $J / \psi$ cross section ratio

The $\psi^{\prime}$ to $J / \psi$ cross section ratio was measured using the rates of $\psi^{\prime} \rightarrow \mu^{+} \mu^{-}$and $J / \psi \rightarrow$ $\mu^{+} \mu^{-}$. The ratio was determined in the region $60<W<190 \mathrm{GeV}, 0.55<z<0.9$. The $p_{T}>1 \mathrm{GeV}$ requirement was removed to maximise the available statistics. An increase of the diffractive background is expected. But under the assumption that this background contribution will be the same for the $\psi^{\prime}$ and $J / \psi$ mesons it will cancel in the cross section
ratio. The range $190<W<240 \mathrm{GeV}$ and $0.1<z<0.55$ was not included because the $\psi^{\prime}$ peak was not visible in this high $W$ and low $z$ region. The $\psi^{\prime}$ to $J / \psi$ cross section ratio was computed in bins of $W, z$ and $p_{T}$ from

$$
\frac{\sigma_{i}\left(\psi^{\prime}\right)}{\sigma_{i}(J / \psi)}=\frac{N_{i}^{2 S}}{N_{i}^{1 S}} \cdot \frac{C_{i}^{1 S}}{C_{i}^{2 S}} \cdot \frac{B r^{\mu}}{B r^{\mu^{\prime}}} \cdot\left(1-\frac{N_{i}^{2 S}}{N_{i}^{1 S}} \frac{C_{i}^{1 S}}{C_{i}^{2 S}} \frac{B r^{\mu}}{B r^{\mu^{\prime}}} B r^{\prime}\right)^{-1}
$$

where, for the considered bin $i, N_{i}^{1 S}\left(N_{i}^{2 S}\right)$ is the number of $J / \psi\left(\psi^{\prime}\right)$ events observed, $C_{i}^{1 S}$ $\left(C_{i}^{2 S}\right)$ is the correction factor (see section 5) computed using the Herwig MC, $B r^{\mu}\left(B r^{\mu^{\prime}}\right)$ is the $J / \psi\left(\psi^{\prime}\right)$ muonic branching ratio and $B r^{\prime}$ is the $\psi^{\prime} \rightarrow J / \psi X$ branching ratio. The values used are $B r^{\mu}=5.93 \%, B r^{\mu^{\prime}}=0.77 \%$ and $B r^{\prime}=59.5 \%$ [34]. With this technique, the cross section ratio was corrected for the $\psi^{\prime} \rightarrow J / \psi\left(\rightarrow \mu^{+} \mu^{-}\right) X$ cascade decay.

Since NLO predictions are not available for $\psi^{\prime}$, only the LO CS model expectations can be compared to the data. In the CS model, the underlying production mechanism is the same for $J / \psi$ and $\psi^{\prime}$, hence all cross section ratios should be largely independent of the kinematic variables. Using the values of $B r^{\mu}$ and $B r^{\mu^{\prime}}$ given above, the expected ratio is $0.25[4,5]$. Since the NLO corrections, though being large, should be similar for $J / \psi$ and $\psi^{\prime}$, the ratio at NLO is not expected to differ significantly from that at LO.

The results, shown in figure 4 and listed in table 2, are dominated by the statistical uncertainties while most of the systematic uncertainties cancel in the ratio. The LO CS predictions agree reasonably well with the data.

## 7.2 $J / \psi$ differential cross sections

The $J / \psi$ differential cross sections presented here include the inelastic $\psi^{\prime}$ feed-down via the decay $\psi^{\prime} \rightarrow J / \psi\left(\rightarrow \mu^{+} \mu^{-}\right) X$ and the contribution from $b$ hadron decays. The $\psi^{\prime}$ feed-down contributes about $15 \%$ and the $b$ hadron decays $1.6 \%$ (see section 5). The $W$ range of the differential cross sections is $60<W<240 \mathrm{GeV}$.

The differential cross sections $d \sigma / d p_{T}^{2}$ were measured in the range $1<p_{T}^{2}<100 \mathrm{GeV}^{2}$ for different $z$ ranges. The results are listed in table 3 and shown in figures 5 and 6. The predictions of a NRQCD calculation $[8,9]$ are compared to the data in figure 5 and those based on the $k_{T}$-factorization approach [11] in figure 6. ${ }^{4}$

The differential cross sections $d \sigma / d z$ were measured in the range $0.1<z<0.9$ for different $p_{T}$ ranges. The results are shown in figures 7 and 8 and listed in table 4 .

The present measurements are in agreement with the results obtained by the H 1 collaboration [3] except in the region $z>0.6$ and $p_{T}>3 \mathrm{GeV}$ where the ZEUS cross sections are above the H 1 measurements.

### 7.2.1 Comparison of NRQCD calculation

In figure 5 a prediction [8, 9] performed in the NRQCD framework including direct and resolved photon processes is compared to the measured $d \sigma / d p_{T}^{2}$. The hard subprocesses take into account both CS and CO terms to NLO. The square of the renormalisation

[^2]and factorisation scales used is $4 \cdot m_{c}^{2}+p_{T}^{2}$, the charm quark mass, $m_{c}$, is set to 1.5 GeV and the strong coupling constant, $\alpha_{s}\left(M_{Z}\right)$, to 0.118 . The NRQCD scale, connected to the colour-octet terms, is set to $m_{c}$. The CS contribution alone predicts cross sections significantly below the data ${ }^{5}$ and fails to describe the data in all $z$ regions shown here. Including CO terms give a dramatic improvement and leads to a rough agreement with the data. In general the calculation reproduces the steep drop of $d \sigma / d p_{T}^{2}$ with $p_{T}^{2}$, however, in the intermediate $z$ range, $0.3<z<0.75$, the prediction rises less steeply than the data towards the smallest values of $p_{T}^{2}$.

In figure 7 the NRQCD predictions described above are compared to the measured $d \sigma / d z$. The predictions rise too steeply with $z$ compared to the data, for all the $p_{T}$ ranges.

### 7.2.2 Comparison of $k_{T}$-factorisation approach

In figure 6 a prediction [11] performed in the $k_{T}$-factorisation approach is compared to the measured $d \sigma / d p_{T}^{2}$. The matrix elements are computed in the CS model using $m_{c}=$ 1.5 GeV and $\alpha_{s}\left(M_{Z}\right)=0.1232$. In the numerical calculation, the renormalisation and factorisation scales squared are set to $m_{J / \psi}^{2}+p_{T}^{2}$ and $\hat{s}+Q_{T}^{2}$, respectively, where $\hat{s}$ is the four-momentum squared of the hard subprocess and $Q_{T}$ is the transverse momentum of the initial parton. The unintegrated CCFM parton density [49] was selected. Using different sets of parton densities leads to changes in the prediction that are small with respect to the effects of scale variations already shown in figure 6 . Thus this source of theoretical uncertainties was neglected. The $k_{T}$-factorisation prediction, with the values of $m_{c}$ and $\alpha_{s}$ given above, provides a better description of the data than the NRQCD model.

The above $k_{T}$-factorisation predictions are compared to the differential cross sections $d \sigma / d z$ in figure 8 . Here too the description is better than that of the NRQCD model. Note however that the $k_{T}$-factorisation model prediction suffers from large theoretical uncertainties, in particular at low $p_{T}$.

### 7.3 Momentum flow along and against the $J / \psi$ direction

As pointed out by Brambilla et al. [1], the different colour flow in CS and CO hard subprocesses is expected to translate into different properties of the hadronic final state. In the photoproduction regime, the transverse momentum of the incoming photon is negligible. Thus in the CS model (see figure 1 (a)), at LO the $J / \psi$ and the final state gluon are expected to be back to back. Hence, in this model, the momentum flow along the $J / \psi$ direction, $\mathrm{P}_{\text {along }}$, is expected to be small. The momentum flow against the $J / \psi$ direction, $\mathrm{P}_{\text {against }}$, should instead be driven by the hadronisation of the gluon. In the CO framework (see figure 1 (b)), no substantial difference is expected for $\mathrm{P}_{\text {against }}$, compared to the CS framework. Instead, a contribution due to the soft gluons emitted by the $c \bar{c}$ pair forming the physical $J / \psi$ state should be present. Hence, $\mathrm{P}_{\text {against }}$ is again sensitive to gluon fragmentation while $\mathrm{P}_{\text {along }}$ can shed light on the CO dynamics. As NRQCD framework MC

[^3]generators are not presently available for ep collisions, only predictions of the CS model Herwig MC are compared to the data.

The momentum flow analysis was performed for different $p_{T}$ ranges. All track quantities described in the following were measured in the laboratory frame at the reconstruction level. Only primary vertex tracks with $p_{T}>150 \mathrm{MeV}$ and $|\eta|<1.75$ were selected. The $J / \psi$ decay muon tracks were discarded. For each track whose component of momentum along the $J / \psi$ direction in the laboratory frame was positive, the component was included in $\mathrm{P}_{\text {along }}$. If it was negative, it was included, in absolute value, in $\mathrm{P}_{\text {against }}$. The data were restricted to $z>0.3$ where the signal to background ratio is highest. The $W$ and $p_{T}$ ranges were $60<W<240 \mathrm{GeV}$ and $1<p_{T}<10 \mathrm{GeV}$, respectively. The residual non-resonant background was subtracted for both $\mathrm{P}_{\text {against }}$ and $\mathrm{P}_{\text {along }}$ variables using the shapes measured in the $J / \psi$ side bands region and the normalisation obtained from the signal extraction procedure described in section 5 .

The $P_{\text {against }}\left(\mathrm{P}_{\text {along }}\right)$ distribution, normalized to one, is shown in figure 9 (10). The prediction obtained from the Herwig MC simulation (including detector simulation) is also shown. The $\mathrm{P}_{\text {against }}$ distribution of the MC simulation shows a softer drop from the first to the second momentum bin than that of the data. This situation is reversed for the higher momenta values where Herwig predicts a steeper decrease than that observed in the data. This behavior is seen for all $p_{T}$ regions.

For the $\mathrm{P}_{\text {along }}$ distribution, shown in figure 10, a better agreement is found between the Herwig MC prediction and the data.

## 8 Conclusions

A measurement of the inelastic photoproduction of $J / \psi$ and $\psi^{\prime}$ mesons at HERA was presented. The $\psi^{\prime}$ to $J / \psi$ cross section ratio was measured as a function of several kinematical observables. The constant value of 0.25 predicted by the LO CS model is in reasonable agreement with the data.

Double differential cross sections of inelastic $J / \psi$ photoproduction were measured. A LO $k_{T}$ calculation [11] using CS terms alone gives, within large normalisation uncertainties, a good description of the differential cross sections. However, for a better comparison with the data, a reduction of the theoretical uncertainties is very important.

A recent NLO calculation [8, 9], using CS and CO terms in the collinear approximation, gives a rough description of the double differential cross sections. The same calculation with only CS terms is in strong disagreement with the data. This leads to the conclusion that CO terms are an essential ingredient for this particular model.

Predictions of the Herwig MC, which includes only CS processes, were compared to the measured momentum flow along and against the $J / \psi$ direction. Herwig reproduces the fall off of the momentum distribution against the $J / \psi$ direction as the momentum increases but fails to describe the exact shape of this distribution. A better description is obtained along the $J / \psi$ direction.

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| $\psi^{\prime}$ to $J / \psi$ cross section ratio: kinematic range |  |  |
| :---: | :---: | :---: |
| $60<W<190 \mathrm{GeV}$ | $p_{T}>0 \mathrm{GeV}$ | $0.55<z<0.9$ |
| Differential cross sections: kinematic range |  |  |
| $60<W<240 \mathrm{GeV}$ | $p_{T}>1 \mathrm{GeV}$ | $0.1<z<0.9$ |
| Momentum flow: kinematic range |  |  |
| $60<W<240 \mathrm{GeV}$ | $1<p_{T}<10 \mathrm{GeV}$ | $0.3<z<0.9$ |

Table 1. The different kinematic regions used in the measurement of the $\psi^{\prime}$ to $J / \psi$ cross section ratio, $J / \psi$ differential cross sections and momentum flow along and against the $J / \psi$ direction.

| $p_{T}$ range <br> $(\mathrm{GeV})$ | $\left\langle p_{T}\right\rangle$ <br> $(\mathrm{GeV})$ | $\sigma\left(\psi^{\prime}\right) / \sigma(J / \psi)$ |
| :---: | :---: | :---: |
| $0.0-1.0$ <br> $1.0-1.75$ <br> $1.75-5.0$ | 0.63 | $0.262 \pm 0.043_{-0.014}^{+0.003}$ |
| 2.68 | $0.317 \pm 0.049_{-0.005}^{+0.010}$ |  |
| $W$ range <br> $(\mathrm{GeV})$ | $\langle W\rangle$ <br> $(\mathrm{GeV})$ | $\sigma\left(\psi^{\prime}\right) / \sigma(J / \psi)$ |
| $60-95$ | 81.42 | $0.368 \pm 0.054_{-0.042}^{+0.052}$ |
| $95-120$ | 108.03 | $0.409 \pm 0.057_{-0.015}^{+0.006}$ |
| $120-190$ | 149.11 | $0.218 \pm 0.040_{-0.015}^{+0.026}$ |
| $z$ range | $\langle z\rangle$ | $\sigma\left(\psi^{\prime}\right) / \sigma(J / \psi)$ |
|  |  |  |
| $0.55-0.70$ | 0.62 | $0.250 \pm 0.043_{-0.015}^{+0.014}$ |
| $0.70-0.80$ | 0.75 | $0.289 \pm 0.040_{-0.019}^{+0.007}$ |
| $0.80-0.90$ | 0.85 | $0.344 \pm 0.054_{-0.008}^{+0.036}$ |

Table 2. Cross section ratio of $\psi^{\prime}$ to $J / \psi$ as a function of $p_{T}, W$ and $z$ in the kinematic region $60<W<190 \mathrm{GeV}$ and $0.55<z<0.9$. In the quoted ratios, the first uncertainty is statistical and the second is systematic.
$\left.\begin{array}{|c|c|c|c|c|}\hline z \text { range } & p_{T}^{2} \text { range } & \begin{array}{c}\left\langle p_{T}^{2}\right\rangle \\ \left(\mathrm{GeV}^{2}\right)\end{array} & \begin{array}{c}d \sigma / d p_{T}^{2} \\ (\mathrm{GeV})\end{array} & \begin{array}{c}d \sigma\left(b \rightarrow \mathrm{GeV} \mathrm{V}^{2}\right)\end{array} \\ \hline \hline 0.10-0.30 & 1.0-2.0 & 1.46 & 1.03 \pm 0.13_{-0.15}^{+0.18} \\ \left(\mathrm{nb} / \mathrm{GeV}^{2}\right)\end{array}\right]$

Table 3. Measured $J / \psi$ differential photoproduction cross sections in the kinematic region $0.1<$ $z<0.9$ and $60<W<240 \mathrm{GeV}$ as a function of the squared transverse momentum of the $J / \psi$ mesons in bins of inelasticity $z$. In the quoted cross sections, the first uncertainty is statistical and the second is systematic. The bin center values $\left\langle p_{T}^{2}\right\rangle$ and the expected, but not subtracted, beauty contribution (estimated through the Pythia MC) are also given in the table. The beauty contribution is only given when its value is above $1 \%$ with respect to the corresponding measured differential photoproduction cross section.

| $p_{T}$ range <br> $(\mathrm{GeV})$ | $z$ range | $\langle z\rangle$ | $d \sigma / d z$ <br> $(\mathrm{nb})$ | $d \sigma(b \rightarrow J / \psi) / d z$ <br> $(\mathrm{nb})$ |
| :---: | :---: | :---: | :---: | :---: |
| $1.0-2.0$ | $0.10-0.30$ | 0.21 | $11.5 \pm 1.0_{-1.9}^{+1.5}$ | 0.6 |
|  | $0.30-0.45$ | 0.37 | $17.3 \pm 1.0_{-2.2}^{+2.3}$ | 0.4 |
|  | $0.45-0.60$ | 0.52 | $29.9 \pm 0.9_{-3.4}^{+3.3}$ | - |
|  | $0.60-0.75$ | 0.67 | $40.2 \pm 1.0_{-4.5}^{+4.4}$ | - |
|  | $0.75-0.90$ | 0.82 | $36.6 \pm 1.2_{-4.9}^{+6.6}$ | - |
| $2.0-3.0$ | $0.10-0.30$ | 0.21 | $1.94 \pm 0.78_{-0.45}^{+0.31}$ | 0.43 |
|  | $0.30-0.45$ | 0.37 | $6.42 \pm 0.71_{-0.81}^{+0.78}$ | 0.28 |
|  | $0.45-0.60$ | 0.52 | $12.4 \pm 0.6_{-1.5}^{+1.5}$ | 0.8 |
| $3.0-4.5$ | $0.60-0.75$ | 0.67 | $18.6 \pm 0.6_{-2.2}^{+2.2}$ | - |
|  | $0.75-0.90$ | 0.82 | $19.4 \pm 0.8_{-2.3}^{+2.4}$ | - |
|  | $0.10-0.30$ | 0.20 | $2.55 \pm 0.47_{-0.28}^{+0.36}$ | 0.30 |
|  | $0.30-0.45$ | 0.38 | $3.51 \pm 0.41_{-0.37}^{+0.37}$ | 0.26 |
|  | $0.45-0.60$ | 0.52 | $6.61 \pm 0.37_{-0.72}^{+0.66}$ | 0.08 |
| $>4.5$ | $0.60-0.75$ | 0.68 | $7.79 \pm 0.35_{-0.75}^{+0.74}$ | - |
|  | $0.75-0.90$ | 0.82 | $9.29 \pm 0.46_{-1.15}^{+0.84}$ | - |
|  | $0.10-0.30$ | 0.21 | $1.01 \pm 0.20_{-0.13}^{+0.10}$ | 0.16 |
|  | $0.30-0.45$ | 0.38 | $1.31 \pm 0.18_{-0.12}^{+0.15}$ | 0.24 |
|  | $0.45-0.60$ | 0.52 | $1.98 \pm 0.17_{-0.16}^{+0.16}$ | 0.08 |
|  | $0.60-0.75$ | 0.67 | $2.11 \pm 0.16_{-0.19}^{+0.18}$ | - |
| $0.75-0.90$ | 0.82 | $2.16 \pm 0.18_{-0.49}^{+0.18}$ | - |  |

Table 4. Measured $J / \psi$ differential photoproduction cross sections in the kinematic region $p_{T}>$ 1 GeV and $60<W<240 \mathrm{GeV}$ as a function of the inelasticity $z$ in bins of transverse momentum of the $J / \psi$ meson. In the quoted cross sections, the first uncertainty is statistical and the second is systematic. The bin center values $\langle z\rangle$ and the expected, but not subtracted, beauty contribution (estimated through the Pythia MC) are also given in the table. For further details see table 3.


Figure 1. Examples of direct photon-processes at leading-order in (a) the colour-singlet and (b) the colour-octet frameworks.

## ZEUS



Figure 2. Invariant-mass distribution, $m_{\mu \mu}$, in the kinematic region $0.55<z<0.9$ and $60<W<$ 190 GeV . The continuous line shows the estimated background contribution (for further details see the text). The right insert highlights the $\psi^{\prime}$ mass peak.

## ZEUS



Figure 3. $J / \psi$ events fraction measured in the kinematic region $0.3<z<0.9,60<W<240 \mathrm{GeV}$ and $p_{T}>1 \mathrm{GeV}$ as a function of (a) the polar angle $\theta_{\mu}$ of the muon tracks, (b) $W$, (c) the inelasticity $z$ and (d) the $J / \psi p_{T}$. The data are shown as points. The error bars are the statistical uncertainties. The sum of the Herwig and Epsoft MC predictions, according to the relative fraction described in the text and normalised to the data are also shown (continuous lines). The Epsoft MC component is shown separately (dashed lines).

## ZEUS



Figure 4. $\psi^{\prime}$ to $J / \psi$ photoproduction cross section ratio measured in the kinematic region $0.55<$ $z<0.9$ and $60<W<190 \mathrm{GeV}$ as a function of (a) $W$, (b) the inelasticity $z$ and (c) $p_{T}$. The data are shown as points. The inner error bars are the statistical uncertainties, while the outer error bars show the statistical and systematic uncertainties added in quadrature. The leading-order colour-singlet model expectation (horizontal lines) is also shown.

## ZEUS



Figure 5. Differential cross sections $d \sigma / d p_{T}^{2}$ measured in 5 different $z$ ranges. The measurement is performed in the kinematic region $60<W<240 \mathrm{GeV}$ and $p_{T}>1 \mathrm{GeV}$. The data are shown as points. The inner (outer) error bars represent the statistical (total) uncertainties. The solid lines show the NLO CS $+\mathrm{CO}(\mathrm{BK})$ prediction $[8,9]$ obtained in the non-relativistic QCD framework. The uncertainties are indicated by the band. The colour-singlet model contribution is presented separately as the dashed lines.

## ZEUS



Figure 6. Differential cross sections $d \sigma / d p_{T}^{2}$ measured in 5 different $z$ ranges. The measurement is performed in the kinematic region $60<W<240 \mathrm{GeV}$ and $p_{T}>1 \mathrm{GeV}$. The data are shown as points. The inner (outer) error bars represent the statistical (total) uncertainties. The solid lines show the $k_{T}$-factorisation (BLZ) prediction [10, 11]. The uncertainties are indicated by the band.

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Figure 7. Differential $J / \psi$ cross sections $d \sigma / d z$ measured in 4 different $p_{T}$ ranges. The measurement is performed in the kinematic region $60<W<240 \mathrm{GeV}$ and $0.1<z<0.9$. The data are shown as points. The inner (outer) error bars represent the statistical (total) uncertainties. The solid lines show the NLO CS $+\mathrm{CO}(\mathrm{BK})$ prediction $[8,9]$ obtained in the non-relativistic QCD framework. The uncertainties are indicated by the band.

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Figure 8. Differential $J / \psi$ cross sections $d \sigma / d z$ measured in 4 different $p_{T}$ ranges. The measurement is performed in the kinematic region $60<W<240 \mathrm{GeV}$ and $0.1<z<0.9$. The data are shown as points. The inner (outer) error bars represent the statistical (total) uncertainties. The solid lines show the $k_{T}$-factorisation (BLZ) prediction $[10,11]$. The uncertainties are indicated by the band.

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Figure 9. Momentum flow against the $J / \psi$ direction of flight in the laboratory frame, $\mathrm{P}_{\text {against }}$, for different $p_{T}$ ranges. The distributions are normalized to unity and are not corrected for detector acceptance. The measurement is performed in the kinematic region $60<W<240 \mathrm{GeV}$ and $0.3<z<0.9$. The data are shown as points with error bars indicating their uncertainties. The predictions obtained from the HERWIG MC are also shown as rectangular shaded boxes. The height of these boxes represents the uncertainties of the prediction.

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Figure 10. Momentum flow along the $J / \psi$ direction of flight in the laboratory frame, $\mathrm{P}_{\text {along }}$, for different $p_{T}$ ranges. The distributions are normalized to unity and are not corrected for detector acceptance. The measurement is performed in the kinematic region $60<W<240 \mathrm{GeV}$ and $0.3<z<0.9$. The data are shown as points with error bars indicating their uncertainties. The predictions obtained from the Herwig MC are also shown as rectangular shaded boxes. The height of these boxes represents the uncertainties of the prediction.

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[^0]:    ${ }^{1}$ Here and in the following, the term "electron" denotes generically both the electron ( $e^{-}$) and the positron ( $e^{+}$).
    ${ }^{2}$ The ZEUS coordinate system is a right-handed Cartesian system, with the $Z$ axis pointing in the proton-beam direction, referred to as the "forward direction", and the $X$ axis pointing towards the centre of HERA. The coordinate origin is at the nominal interaction point. The polar angle, $\theta$, is measured with respect to the proton-beam direction. The pseudorapidity is defined as $\eta=-\ln \left(\tan \frac{\theta}{2}\right)$.

[^1]:    ${ }^{3}$ The scaling factors obtained in the measurements [45, 46] vary between 1.11 and 1.84

[^2]:    ${ }^{4}$ Both the NRQCD and the $k_{T}$-factorisation calculations do not include $\psi^{\prime}$ feed-down and $b$ hadron decays, however these expected contributions are small compared to the uncertainties of the calculations.

[^3]:    ${ }^{5}$ The NLO CS predictions [4, 5] shown in the previous publication [2] were the first performed and used extreme values for the renormalisation and factorisation scales, with the effect of artificially increasing the normalisation of the predicted cross sections [48].

