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Electrical Transport Properties of Vanadium-Doped Bi₂Te_{2.4}Se_{0.6}

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Vanadium-doped Bi_{2-x}Te_{2.4}Se_{0.6} single crystals, with x = 0.015 and 0.03, are grown by the Bridgman method. Bandstructure characterization by angleresolved photoemission spectroscopy (ARPES) measurements shows gapless topological surface states for both vanadium concentrations. The Van-der-Pauw resistivity, the Hall charge carrier density, and the mobility in the temperature range from 0.3 to 300 K are strongly dependent on vanadium concentration, with carrier densities as low as 1.5×10^{16} cm⁻³ and mobilities as high as $570 \text{ cm}^2 \text{ V}^{-1} \text{s}^{-1}$. As expected for transport in gapless topological surface states, the resistivity, carrier density, and mobility are constant below 10 K. The magnetoresistance shows weak antilocalization for both vanadium concentrations in the same temperature range. The weak antilocalization is analyzed with the Hikami–Larkin–Nagaoka model, which yields phase-coherence lengths of up to 250 nm for x = 0.015.

1. Introduction

Topological insulators (TIs) have received a lot of interest in recent years due to their possible applications in spintronics and quantum computation. This interest derives from the topological surface states (TSSs) that allow the observation of a variety of quantum effects,^[1,2] some of which require magnetic

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doping of the TI.^[3,4] Effects of magnetic impurities on the band structure of TIs is presently under debate.^[5]

Due to its relatively high energy gap of 0.3 eV and its simple surface-state structure, a considerable amount of effort has been put into the investigation of Bi₂Se₃. However, the transport properties of the TSSs are often masked by the bulk contribution due to the presence of Se vacancies and the resulting n-type doping.^[6–8] A similar effect occurs in Bi₂Te₃ due to Bi-Te antisite defects.^[9] Both TIs have the tetradymite structure which allows to form Bi₂Te₂Se with a quintuple layer unit of Te-Bi-Se-Bi-Te.^[10] This ternary TI is reasonably insulating compared with Bi2Se3 and Bi2Te3 and yields a resistivity which exceeds 1Ω cm. In this material system, the strong bonding

suppresses both the Se vacancies and the Te–Bi antisite defects.^[11] These desirable properties make Bi₂Te₂Se a promising candidate to investigate the TSSs. Among the Bi₂Te_{3-x}Se_x materials, the Bi₂Te_{2.4}Se_{0.6} alloy is known to have one of the widest bandgaps.^[12] In V_xBi_{2-x}Se₃ materials with a vanadium concentration of x = 0.04, angle-resolved photoemission spectroscopy (ARPES) measurements at 100 K revealed the opening of a non-magnetic energy gap of ≈180 meV in the surface states.^[4]

Magnetically doped ternary^[13] and nonternary^[4,14] TIs allow to observe the quantum anomalous Hall effect, which may enable the development of low-power-consumption electronics. Other investigations involve the systematic crossover between weak antilocalization (WAL) and weak localization with the change of magnetic impurity concentration.^[3] However, to date, investigations of electrical transport in magnetically doped Bi₂Te_{2.4}Se_{0.6} are still lacking.

In this work, $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ crystals with x = 0.015 and x = 0.03 are investigated with respect to the electrical resistivity, the charge carrier concentration, and the mobility. In addition, low-field magnetotransport characteristics of the longitudinal resistance are studied to investigate WAL.

2. Results

The results of the ARPES measurements at T = 300 K are shown in **Figure 1**. The TSSs and the Dirac point are visible in all samples. The Dirac point for undoped Bi₂Te_{2.4}Se_{0.6} is located at $E_{\rm D} = 0.28$ eV binding energy.^[10] For V_xBi_{2-x}Te_{2.4}Se_{0.6}, it shifts to higher binding energies: $E_{\rm D} = 0.33$ eV for x = 0.015 and www.advancedsciencenews.com



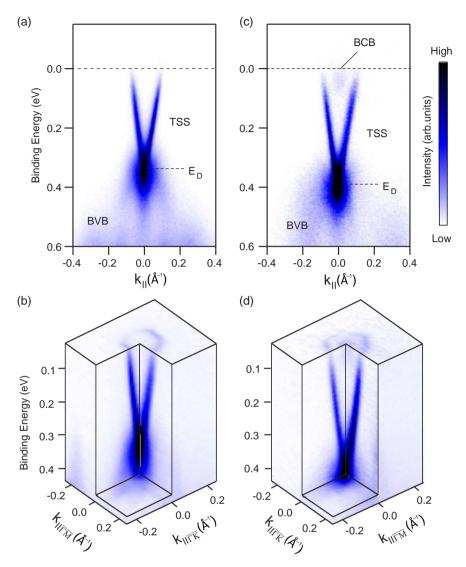


Figure 1. a,c) High-resolution ARPES dispersions and b,d) full photoemission mapping of the TSS of $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ with (a,b) x = 0.015 and (c,d) x = 0.03. In (a,c), bulk conduction band and bulk valence band states are denoted as BCB and BVB, respectively. The shift in the energy position of the Dirac point E_D with increasing V content is emphasized by horizontal dashed lines. The spectra were taken at T = 300 K using a photon energy of $h\nu = 66$ eV.

 $E_{\rm D} = 0.38 \,\mathrm{eV}$ for x = 0.03. The Fermi energy $E_{\rm F}$ appears to be located inside the bandgap for x = 0.015. In the crystal with x = 0.03, it appears to be close to the bulk conduction band. The Fermi wavevectors for the TSSs are $k_{\rm F,TSS} = 0.084 \,\mathrm{\AA^{-1}}$ and $k_{\rm F,TSS} = 0.10 \,\mathrm{\AA^{-1}}$ for x = 0.015 and x = 0.030, respectively. This yields a charge carrier density in the TSSs of $n_{\rm TSS} = 5.6 \times 10^{12} \,\mathrm{cm^{-2}}$ and $n_{\rm TSS} = 8.0 \times 10^{12} \,\mathrm{cm^{-2}}$ for x = 0.015 and x = 0.030, respectively.

The V-doped Bi₂Te_{2.4}Se_{0.6} single crystals are electrically characterized by performing Hall and Van-der-Pauw measurements in the temperature range of 0.3 to 300 K. The *I*–*V* curves show ohmic characteristics in this temperature range.

The temperature-dependent sample resistivity ρ is shown in **Figure 2**a. The resistivity for x = 0.015 is approximately one order of magnitude higher than for x = 0.03. All samples show a semiconducting-like temperature dependence of ρ above T = 40 K. However, below T = 10 K, we observe a nearly constant resistivity, which indicates the influence of the TSSs.

From Hall measurements, we observe *n*-type behavior. Under the assumption of one-band conductivity, the charge carrier density *n* is derived and shown in Figure 2b. At 300 K, *n* increases with increasing vanadium concentration *x*. In the temperature range between 10 K and 150 K, a strong temperature dependence of *n* is observed. *n* is approximately constant below T = 10 K. A minimum of $n = 1.5 \times 10^{16}$ cm⁻³ for x = 0.015 is found at T = 40 K. The activation energy is determined from the slope of the Arrhenius equation $\ln(n) = \ln(n^*) - (E_A/k_B) \cdot (1/T)$, with the Boltzmann constant k_B and the high-temperature limit of the carrier density *n**. The fits are shown in **Figure 3**. The sample with x = 0.03 yields $E_A = 6.9$ meV. The sample with x = 0.015 yields $E_A = 24.9$ meV, supporting the observation by photoemission spectroscopy that E_F is located inside the bulk bandgap.





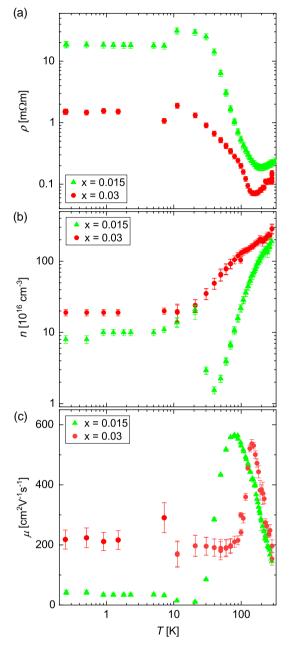


Figure 2. a) Temperature-dependent resistivity obtained from Van-der-Pauw measurements of $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ crystals with x = 0.015 and x = 0.03. From temperature-dependent Hall measurements, b) the charge carrier density *n* and c) the mobility μ is obtained.

Under the assumption of one-band conductivity, the electron mobility $\mu = 1/\rho en$ is calculated from the resistivity ρ and the carrier concentration n, and is shown in Figure 2c. Above T = 200 K, the mobility μ has the same values for all samples within the measurement uncertainty. Note that the Debye temperature of Bi₂Te_{2-x}Se_x is $\Theta_D = 155$ K.^[15] Below Θ_D maxima of μ are found: $\mu_{max} = 570$ cm² V⁻¹ s⁻¹ at T = 80 K for x = 0.015 and $\mu_{max} = 530$ cm² V⁻¹ s⁻¹ at T = 150 K for x = 0.03. Below T = 20 K, the mobility is constant for x = 0.015 and x = 0.03 at $\mu_{0 \text{ K}} = 40$ cm² V⁻¹ s⁻¹ and $\mu_{0 \text{ K}} = 220$ cm² V⁻¹ s⁻¹, respectively.

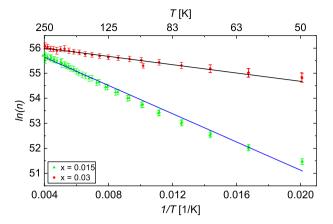


Figure 3. Arrhenius plot for $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ crystals with x = 0.015 and x = 0.03. The solid lines are fits to the Arrhenius equation (see text). The slopes yield $E_A = 24.9 \text{ meV}$ and $E_A = 6.9 \text{ meV}$ for x = 0.015 and x = 0.03, respectively. The intercepts yield $n^* = 4.5 \times 10^{18} \text{ cm}^{-3}$ and $n^* = 2.9 \times 10^{18} \text{ cm}^{-3}$ for x = 0.015 and x = 0.03, respectively.

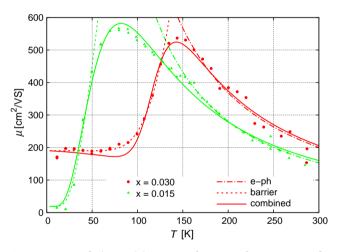


Figure 4. Fits of the mobility as a function of temperature for $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ crystals with x = 0.015 and x = 0.03. The dash-dotted lines are fits to electron-phonon (deformation potential) scattering, with a $T^{-3/2}$ dependence. The dashed lines are fits to thermal activation over a barrier and with a constant background mobility, with an exponential temperature dependence. These fits yield a barrier height of $\phi_B = 12 \text{ meV}$ and $\phi_B = 68 \text{ meV}$ for x = 0.015 and x = 0.03, respectively. The solid lines are the combination of both processes following the Matthiessen rule.

The Debye temperature Θ_D separates the temperature dependence in two regimes (see **Figure 4**). In the high-temperature range, electron–phonon scattering dominates the mobility (dash–dotted lines in Figure 4). In the low-temperature range, the temperature dependence is consistent with an activation over a barrier, in addition to a constant background mobility (dashed lines in Figure 4). However, in the presence of multiple parallel conducting layers or bands, like the bulk states and the TSSs in this instance, a one-band analysis of the transport data can yield counter-intuitive results.^[6] The measurement results are summarized in **Table 1**.



Table 1. Overview of the measurement results for the samples $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ in this work: the thickness *t*; the binding energy E_D of the Dirac point, the Fermi wavevector for the TSS $k_{F,TSS}$, and the corresponding charge carrier densities n_{TSS} from the ARPES measurements; charge carrier density $n_{268 \text{ K}}$ at T = 268 K and its constant value at low temperatures $n_{0 \text{ K}}$ from Hall measurements, the activation energy E_A ; the mobility μ at T = 268 K, its maximum μ_{max} and its saturation value for low temperatures $\mu_{0 \text{ K}}$, the temperature of the maximum mobility $T_{\mu,max}$; the maximum of the phase-coherence length $I_{\varphi,max}$ from the HLN fits, the highest temperature $T_{\varphi,max}$ above which the WAL in the magnetoresistance is not observed; the highest temperature T^* above which the hysteresis in the magnetoresistance is not observed. See text for details.

x	0.015	0.03
t [μm]	170	650
E _D [eV]	0.33	0.38
$k_{\rm F,TSS}$ [Å ⁻¹]	0.084	0.10
$n_{\rm TSS} \ [10^{12} {\rm cm}^{-2}]$	5.6	8.0
$n_{268 \mathrm{K}} [10^{18} \mathrm{cm}^{-3}]$	1.6	2.3
$n_{0\mathrm{K}} [10^{16} \mathrm{cm}^{-3}]$	8	19
E _A [meV]	24.9	6.9
$\mu_{268K} \ [\text{cm}^2 \text{V}^{-1} \text{s}^{-1}]$	190	250
$\mu_{\rm max} [{\rm cm}^2 {\rm V}^{-1} {\rm s}^{-1}]$	570	530
$\mu_{0\mathrm{K}} [\mathrm{cm}^2 \mathrm{V}^{-1} \mathrm{s}^{-1}]$	40	220
$T_{\mu,\max}$ [K]	70	145
$I_{\varphi,\max}$ [nm]	250	180
$T_{\varphi,\max}$ [K]	≈10	≈1
<i>T</i> * [K]	2.3	0.9

The magnetoresistance is measured by applying a magnetic field perpendicular to the sample surface in the temperature range from T = 0.3 K to T = 10 K. The measurement data are shown for each sample in **Figure 5**. All samples show a dip in the resistance at zero field, which is consistent with WAL.^[1] For higher fields, the magnetoresistance is approximately linear, as a result of the competition between the WAL cusp and the semiclassical B^2 -dependence.^[16]

At low temperatures, a sweeprate-dependent hysteresis in the magnetoresistance is observed in all samples. In **Figure 6**a, the time-dependent resistivity of the sample is depicted after sweeping the magnetic field from B = 0 T to B = 0.6 T with a sweeprate of dB/dT = 0.5 T min⁻¹. Figure 6b shows the reverse sweep. A ferromagnetic-like hysteresis is excluded because of this time-dependence. The hysteresis is more distinct at higher sweeprates of the magnetic field and vanishes at higher temperatures. For x = 0.015 the temperature above which the hysteresis is not visible is $T^* = 2.3$ K, much higher than for x = 0.03 (see Table 1).

To evaluate the negative magnetoresistance, the data taken at the smallest sweeprate are fitted with the Hikami–Larkin– Nagaoka (HLN) equation^[17]

$$\Delta \sigma = \sigma(B) - \sigma(0)$$

= $\alpha \frac{e^2}{2\pi^2 \hbar} \left[\ln\left(\frac{B_{\varphi}}{B}\right) - \Psi\left(\frac{1}{2} + \frac{B_{\varphi}}{B}\right) \right]$ (1)



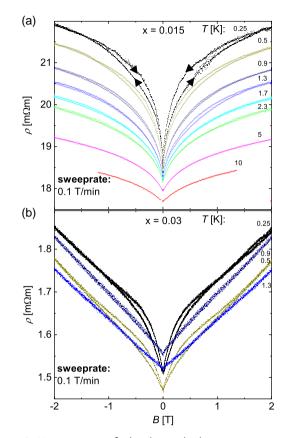


Figure 5. Measurement of the longitudinal magnetoresistivity at low magnetic fields of $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ crystals with a) x = 0.015 and b) x = 0.03. Arrows in (a) indicate whether the magnetic field is increasing or decreasing.

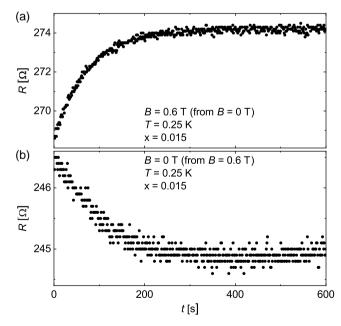


Figure 6. The change in the longitudinal resistance for the sample x = 0.015 is shown at T = 0.3 K when the magnetic field is swept a) from B = 0 to B = 0.6 T and b) from B = 0.6 T to B = 0 with a rate of dB/dT = 0.5 T min⁻¹.





with the characteristic magnetic field $B_{\varphi} = \hbar/4el_{\varphi}^2$, expressed in terms of the phase-coherence length l_{φ} , and the prefactor α , which is expected to be -1 for weak localization and +1/2 for WAL^[17] in 2D electron systems. The magneotconductivity, after subtracting the background, and the applied fits are shown for x = 0.015 in **Figure 7**a and x = 0.03 in Figure 7b, respectively. The hysteresis is considered by applying the fit to each arm of the hysteresis separately and taking the average value of the

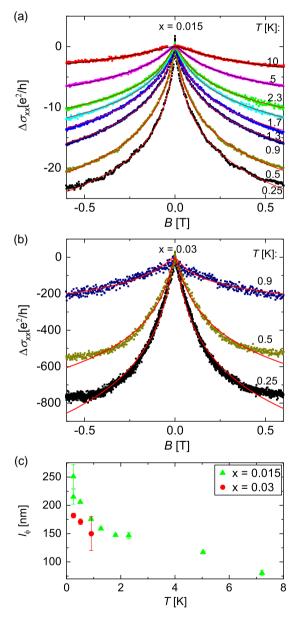


Figure 7. Low-field magnetoconductivity of $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ bulk crystals at different temperatures, for a) x = 0.015 and b) x = 0.03. The magneto-conductivity $\Delta \sigma_{xx}$ is determined by subtracting a background (squares). The HLN equation is fitted to these data (solid lines). In c) the phase-coherence length I_{φ} is extracted from the fits in (a) and (b) at different temperatures. The parameter α varies between 7 and 20 for x = 0.015, and between 160 and 1200 for x = 0.03. These values are larger than for 2D conductors, because of parallel conduction from bulk states.

fit parameters B_{φ} and α . The parameter l_{φ} derived from the fits is shown in Figure 7c. It decreases with increasing temperature, as is expected due to increasing scattering and thermal averaging. The parameter α exceeds values for 2D conductors due to the contribution of the bulk conductivity.

3. Discussion

The photoemission spectra show a shift in the binding energy of the Dirac point E_D with increasing vanadium concentration *x*. The Fermi energy increases relative to E_D with increasing *x*. This is consistent with the increase in the charge carrier density with *x* observed in the Hall measurements. Calculations of energy spectra^[10] yield a shift of the Fermi energy of up to 50 meV, depending on the type of disorder. This gives a disorderinduced uncertainty in the Fermi energy, which is larger than the change in activation energy derived from our data. In this work, both samples are expected to have the same type and degree of disorder, so a disorder-induced shift in the Fermi energy is not anticipated.

The temperature-dependent resistivity $\rho(T)$ shows deviations from a semiconducting-like behavior by saturating at a constant value at lower temperatures. This can be attributed to a metalliclike behavior of the TSSs, as supported by the photoemission spectra. Transport in the TSSs is also consistent by the constant charge carrier density *n* in the low-temperature regime below T = 10 K. Above T = 40 K, *n* is thermally activated from donor states, which yield a bulk-dominated transport.

Although the one-band analysis is limited, the temperature dependence of the mobility $\mu(T)$ above the Debye temperature $\Theta_D = 155$ K shows a semiconducting-like behavior, i.e., it is dominated by electron–phonon scattering. Below Θ_D , the temperature dependence is consistent with thermal activation across a barrier, with a constant mobility background. One possible origin for such a barrier is the formation of grain-like areas due to different distributions of Se atoms in the lattice,^[10] with local changes in the bandstructure and in particular of the energy gap at the Γ -point. The barrier height is affected by the V concentration, by partially filling trap states at the interfaces between areas with mismatched bandstructures.

WAL is observed for all the V-doped Bi₂Te_{2.4}Se_{0.6} crystals, as expected for transport dominated by the TSSs. This may indicate that the V-concentration does not affect strongly the spin-orbit coupling and in consequence the band inversion. The phase-coherence length l_{φ} from the fits yields values typical for TIs.^[6] However, the values for α are orders of magnitude larger than expected in purely 2D systems. This indicates that the magnetoresistance cannot be easily evaluated under this assumption.

Although the general behavior of the vanadium-doped Bi₂Te_{2.4}Se_{0.6} crystals can be understood, the following observations remain to be clarified. The x = 0.015 appears to be a special case, with respect to the increased activation energy E_A , the strongly suppressed (one-band) mobility, the minimum in the (one-band) charge carrier density at T = 40 K, and the enhanced phase-coherence length l_{φ} . Possible explanations may be found in mechanisms of compensation doping and hole density due to thermal activation into a second band near the M-point.^[10]





However, the increased l_{φ} and $T_{\varphi,\max}$ indicate that inelastic scattering is reduced. The enhanced values of α warrant further investigation.

Furthermore, the sweeprate-dependent hysteresis in the magnetoresistance needs clarification. We propose as a possible origin a spin-dependent scattering for eddy currents in the TSSs. The higher surface conductivity due to the TSSs makes eddy currents more likely to be carried by the spin-momentum-locked TSSs. The dependence of the hysteresis on the sign of the time-derivative of the magnetic field is consistent with a scattering that depends on the direction of the eddy currents, which, for spin-momentum-locked states, could indicate a spin-dependent scattering.

4. Conclusion

We investigated $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ single crystals. Photoemission spectra and resistivity measurements confirm the existence of the TSSs. The chemical potential is shifted with increasing vanadium concentration. For both vanadium concentrations, the photoemission spectra and the WAL in the magnetoresistance show that there is no gap at the Dirac point. For x = 0.015, we observed an increased phase-coherence length and maximum temperature for phase-coherent effects, which indicate suppressed inelastic scattering.

5. Experimental Section

 $V_x Bi_{2-x} Te_{2.4} Se_{0.6}$ crystals with x = 0.015 and x = 0.03 were grown by the Bridgman method. The bandstructure of these crystals was characterized by angle-resolved photoemission spectroscopy (ARPES) at the ARPES1² station at the synchrotron radiation source BESSY II.

From these crystals, bulk samples with a surface of 2 mm × 5 mm and a thickness of $t_{0.015} = (170 \pm 20) \,\mu\text{m}$ and $t_{0.03} = (650 \pm 60) \,\mu\text{m}$ were cleaved and glued onto a SiO₂ substrate with an oxide thickness of 1 μm . Ohmic contacts were established by Ag paint and wedge bonding with Al wires.

The contact pattern allowed to perform Hall and Van-der-Pauw measurements,^[18] as well as measurements of the longitudinal resistance. The temperature-dependent Van-der-Pauw and Hall measurements were performed in a Konti Kryostat IT using Keithley SourceMeter Units. The magnetoresistance measurements were performed in a Helium-3-System HelioxVL using a Signal Recovery 7265 Lock-in Amplifier.

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Conflict of Interest

The authors declare no conflict of interest.

Keywords

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